Temporal Experts Averaging for Large-Scale Temporal Domain Generalization

Anonymous ACL submission

Abstract

Temporal Domain Generalization (TDG) aim at generalizing across temporal distribution shifts, e.g., lexical change over time, by predicting future models. Due to the prohibitive full model prediction cost on large-scale scenarios, recent TDG works only predict the classifier, but this limits generalization potential by failing to adjust other model components. To address this, we propose Temporal Experts Averaging (TEA), a novel TDG framework based on weight averaging that adjusts the entire model to maximize generalization potential while maintaining minimal computational overhead when scaling to large-scale datasets and models. Our theoretical analysis of weight averaging for TDG guided us to develop two steps that enhance generalization to future domains. First, we create expert models with functional diversity yet parameter similarity by fine-tuning a domain-agnostic base model on individual temporal domains while constraining weight changes. Second, we optimize the bias-variance tradeoff through adaptive averaging coefficients derived from modeling temporal weight trajectories in a principal component subspace and weighting experts based on their projected proximity to future domains in the subspace. Extensive experiments across 7 TDG benchmarks, 5 models, and 2 TDG settings reports TEA outperforms prior TDG methods by up to 69% while being up to 60x more efficient.

1 Introduction

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Temporal Domain Generalization (TDG) (ying Bai et al., 2022; Nasery et al., 2021; Qin et al., 2022; Xie et al., 2024c,a; Yong et al., 2023; Xie et al., 2024b) aims at generalizing to unseen future data under temporal distribution shift without retraining the models, as illustrated in Fig. 1. Unlike traditional Domain Generalization (DG) lacking target domain information (Li et al., 2017a; Muandet et al., 2013; Li et al., 2018a,b), TDG could leverage temporal patterns for prediction, such as



(a) Temporal distribution shift in vehicle appearance.



(b) Temporal distribution shift in NLP paper keywords.

Figure 1: Examples of temporal domain generalization (TDG) span both vision and language tasks. TDG aims at enabling models trained on historical data to directly generalize to future data without retraining.

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predicting NLP research trends (Yao et al., 2022a), to better adapt the models for future domains. However, prior work faces limitations in scaling. Early brute-force approaches predict entire models but encounter prohibitive computational costs on largescale models and datasets (Nasery et al., 2021; ying Bai et al., 2022; Qin et al., 2022). As shown in Fig. 2a, recent methods improve efficiency by only predicting classifier (Xie et al., 2024c,b), but sacrifice generalization potential by failing to adjust other model components. In large-scale benchmarks (Yao et al., 2022a; Lin et al., 2022), these methods struggle to surpass basic ERM baselines.

To address the scaling challenges, we propose Temporal Experts Averaging (TEA), a TDG framework based on weight averaging (WA) that predicts the averaging coefficients of temporal experts for future domains. As standard WA methods for DG, e.g., (Cha et al., 2021; Rame et al., 2022; Wortsman et al., 2022), lack mechanisms to exploit temporal patterns in TDG, we identify two key strategies to leverage temporal patterns in WA through a biasvariance-covariance-locality decomposition analysis of generalization error: a) creating weights with functional diversity yet parameter similarity, and b) optimizing averaging coefficients to achieve better bias-variance tradeoffs than uniform averaging.

Thus, our TEA first creates a set of temporal



(a) Classifier-only TDG framework

(b) Our Temporal Expert Averaging (TEA) framework

Figure 2: TDG framework comparison. (a) Classifier-only TDG (Xie et al., 2024c,b) only predicts future classifiers to reduce computational costs in large-scale scenarios, but limits generalization potential by neglecting other model components. (b) Our Temporal Expert Averaging (TEA) enables higher generalization potential by adjusting the entire model through predicting future averaging coefficients of temporal experts capturing diverse functionalities. The low-dimensional nature of these coefficients ensures TEA's efficiency in large-scale scenarios.

072 experts with functional diversity yet parameter similarity by training a domain-agnostic base model 073 on all source domains, followed by constrained in-074 cremental fine-tuning on each individual domain. To create adaptive averaging coefficients, we then extract principal components from the deviations between expert weights and the base model, creating a low-dimensional subspace to model temporal weight trajectories. This enables forecasting future domain positions and averaging experts based on their projected proximity to the future domain. This enables TEA to temporally-adapt all model parameters with computational costs comparable to standard ERM training, offering higher generalization potential than merely adjusting the classifier. 086

> The superiority of TEA is demonstrated through comprehensive evaluation across 7 diverse TDG benchmarks and 5 different models, covering both vision and language tasks. Beyond standard TDG with simultaneous access to all source domains, we also evaluate on Continual Domain Generalization over Temporal Drift (CDGTD) settings, where new domains arrive sequentially. Across this extensive evaluation, TEA consistently achieves new state-ofthe-art results, outperforming prior TDG methods by up to 69% while being up to 60x more efficient.

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Our contributions can be summarized as follows:

- We propose TEA, a novel weight-averagingbased TDG framework that efficiently enhances generalization across temporal shifts with broad model/dataset compatibility.
- We provide valuable theoretical insights on the under-explored WA-TDG integration, design our method based on these insights, and validate our insights and method through superior generalization performance across various benchmarks.
- We enhance TDG evaluation comprehensiveness by addressing both TDG and CDGTD, unlike prior work that typically focused on just one set-

ting. We also introduce CLEAR-10 and CLEAR-100 as new evaluation benchmarks for TDG.

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2 Related Work

Temporal Domain Generalization (TDG) (Ortiz-Jiménez et al., 2019; Mancini et al., 2019; Wang et al., 2020; ying Bai et al., 2022; Nasery et al., 2021; Zeng et al., 2023; Wang et al., 2022; Xie et al., 2024c,a; Yong et al., 2023; Xie et al., 2024b) exploits temporal patterns in ordered domains with smooth distribution shifts to enhance generalization to future domains. Early approaches like GI (Nasery et al., 2021) and DRAIN (ying Bai et al., 2022) predict entire model parameters but face computational challenges with large-scale models, while recent methods like EvoS (Xie et al., 2024c) and W-Diff (Xie et al., 2024b) reduce costs by only adjusting classifiers, potentially limiting generalization. TDG encompasses multiple settings: the original setting with simultaneous access to all source domains, Continual Domain Generalization over Temporal Drift (CDGTD) with sequentially available domains, and Continuous Temporal Domain Generalization (CTDG) for continuously distributed temporal data. We focus on the original TDG and CDGTD settings as CTDG remains impractical for most realistic benchmarks.

Domain Adaptation and Generalization. Enabling models to perform well on out-ofdistribution (OOD) data has been a crucial challenge in machine learning. Two specific tasks highly relevant to our work are Domain Adaptation (DA) and Domain Generalization (DG). DA methods (Saenko et al., 2010; Sun et al., 2015; Sun and Saenko, 2016; Gong et al., 2012; Tzeng et al., 2017; Li et al., 2016) typically adapt models against distribution shift by utilizing data from the target domain. In contrast, DG methods (Li et al., 2017a; Muandet et al., 2013; Li et al., 2018a,

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2017b; Gulrajani and Lopez-Paz, 2021; Li et al.,
2018b, 2019) operate without target domain information, solely leveraging source domain patterns
to enhance OOD generalization.

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Weight Averaging (WA) (Cha et al., 2021, 2022; Rame et al., 2022; Wortsman et al., 2022) proves effective for Domain Generalization, with DiWA (Rame et al., 2022) showing reduced variance against marginal distribution shifts. While WA is also used in Multi-task Learning (Ilharco et al., 2022b; Yadav et al., 2023; Ortiz-Jimenez et al., 2023; Wang et al., 2024; Stoica et al., 2023) with our design partly inspired by task arithmetic (Ilharco et al., 2022a), fundamental differences between MTL and TDG make direct application impractical.

3 Temporal Experts Averaging

Let \mathcal{X} be the input space, \mathcal{Y} the label space, ℓ : $\mathcal{Y}^2 \to \mathbb{R}^+$ a loss function, $\{D_i\}$ a sequence of domains with timestamps $t_i \in \mathcal{T}$ and distributions p_i . Given source domains $\mathbf{D}_S = \{D_i\}_{i=1}^S$, where $t_1 < \ldots < t_S$, and a neural network $f(\cdot, \theta)$: $\mathcal{X} \to \mathcal{Y}$ with weights θ , we aim to minimize the generalization error at future time $t_f > t_S$:

$$\mathcal{E}_f(\theta) = \mathbb{E}_{(x,y) \sim p_f}[\ell(f(x,\theta), y)]. \tag{1}$$

We obtain the weights of S temporal expert models $\{\theta_i\}_{i=1}^S = \{\theta(l_i)\}_{i=1}^S$, where θ_i is optimized for domain D_i while using data from other domains, with learning procedure noted as $l_i =$ $\{\{D_i\}_{i=1}^S, t_i, c\}$ and other configurations (e.g., hyper-parameters) as c. We leverage temporal patterns to derive adaptive coefficients $\{\alpha_i\}_{i=1}^S$, where $\sum_{i=1}^S \alpha_i = 1$ and $\alpha_i \ge 0$, for combining expert weights into the final weight θ_{TEA} , formulated as:

$$f_{\text{TEA}} \triangleq f(\cdot, \theta_{\text{TEA}}),$$

$$\theta_{\text{TEA}} \triangleq \sum_{i=1}^{S} \alpha_i \left(\{t_i\}_{i=1}^{S}, \{\theta_i\}_{i=1}^{S}, t_f \right) \cdot \theta_i. \quad (2)$$

To leverage temporal shift patterns for reducing future generalization error, we gain insight into TEA through theoretical analysis in Section 3.1. Following the insights, we implement our TEA by creating functionally diverse yet parametrically similar experts $\{\theta_i\}_{i=1}^S$ (Section 3.2) and determining coefficients $\{\alpha_i\}_{i=1}^S$ based on expert-future proximity (Section 3.3). Section 3.4 details TEA's application to the CDGTD setting.

3.1 Theoretical Analysis and Insights

To gain insight into TEA, we extend DiWA's (Rame et al., 2022) theoretical analysis developed for DG to our WA-TDG integration setting. Since our primary goal is to guide method design, we briefly summarize the theoretical analysis and results in the main text, with complete derivations and proofs available in the supplementary.

Bias-variance-covariance-locality Decomposition. Similar to DiWA (Rame et al., 2022), we introduce the bias-variance-covariance-locality (BVCL) decomposition of generalization error for TDG and TEA by leveraging the similarity between averaging in weight space and function space. Denoting $\mathbb{E}_f = \mathbb{E}_{(x,y)\sim p_f}$, $\mathbf{l} = \{l_1, \ldots, l_S\}$, $\bar{f}_i(x) = \mathbb{E}_{l_i}[f(x, \theta(l_i))]$, bias $_i = y - \bar{f}_i(x)$, $\operatorname{var}_i = \mathbb{E}_{l_i}\left[\left(f(x, \theta(l_i)) - \bar{f}_i(x)\right)^2\right]$, $\operatorname{cov}_{i,j} =$ $\mathbb{E}_{l_i,l_j}\left[\left(f(x, \theta(l_i)) - \bar{f}_i(x)\right)\left(f(x, \theta(l_j)) - \bar{f}_j(x)\right)\right]$ and $\Delta_{\{\theta\}} = \max_{i=1}^S \|\theta_i - \theta_{\text{TEA}}\|_2$, the expected generalization error on future timestamp t_f of $\theta_{\text{TEA}} = \sum_{i=1}^S \alpha_i \theta_i$ over the joint distribution of the learning procedures is:

$$\mathbb{E}_{\mathbf{I}}[\mathcal{E}_f(\theta_{\mathrm{TEA}})] = \mathbb{E}_f\left[\mathcal{B} + \mathcal{V} + \mathcal{C}\right] + O(\bar{\Delta}^2), \quad (3)$$

$$\mathcal{B} = \left(\sum_{i=1}^{S} \alpha_i \cdot \operatorname{bias}_i\right)^{-}, \ \mathcal{V} = \sum_{i=1}^{S} \alpha_i^2 \cdot \operatorname{var}_i,$$
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$$\mathcal{C} = \sum_{i \neq j} \alpha_i \alpha_j \operatorname{cov}_{i,j}, \ \bar{\Delta}^2 = \mathbb{E}_{\mathbf{l}} \left[\Delta_{\{\theta\}} \right].$$
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To reduce future generalization error in Equation 3, we can control learning procedures $\{l_i\}_{i=1}^{S}$ affecting expert weights $\{\theta_i\}_{i=1}^{S}$ and modify averaging coefficients $\{\alpha_i\}_{i=1}^{S}$, which constitute the key differences between our TEA and WA for typical DG. While finding optimal solutions remains challenging due to real-world complexity, qualitative analysis provides valuable insights summarized as two tradeoffs implemented through experts and coefficients respectively. Detailed analysis and assumptions are in the supplementary material.

Insight 1 Tradeoff between Functional Diversity and Parameter Similarity among Experts. Covariance C reduction necessitates functional diversity among experts, while the locality constraint $\overline{\Delta}^2$ demands parameter similarity among experts.

Insight 2 Tradeoff between Bias and Variance via Averaging Coefficients. Reducing variance V requires averaging weights evenly, while reducing bias \mathcal{B} demands concentrating coefficients on experts with lower bias magnitudes on future data.



Figure 3: Overview of our TEA framework. Firstly, we obtain a base model θ_{base} through domain-agnostic pretraining on all source domains, then derive experts $\theta_1, ..., \theta_n$ via constrained domain-specific incremental finetuning in reverse temporal order. Secondly, we apply PCA to expert weight deviations $\{\theta_i - \theta_{\text{base}}\}_{i=1}^n$, forecast future positions along the *P* most significant components with Autoregressive Integrated Moving Average (ARIMA), effectively projecting experts into a low-dimensional space for prediction. Finally, we assign averaging coefficients based on projected expert-future proximity, where closer experts receive higher coefficients.

3.2 Training Temporal Experts

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TDG assumes smooth temporal distribution shifts with moderate changes between adjacent domains. This allows an expert to be fine-tuned for learning domain-specific functionality of neighboring domains with minimal parameter adjustments. Therefore, we can satisfy Insight 1 through incremental domain-specific fine-tuning while constraining minimal parameter changes. However, a prerequisite is that experts must have already thoroughly learned the intrinsic distribution.

A "Pretraining-Finetuning" approach is adopted for our expert training that efficiently generates diverse temporal experts with similar parameters. The overall process can be formulated as:

$$\theta_{\text{base}} = \theta_{S+1} = \theta(l_{\text{ERM}}(\mathbf{D}_S)), \quad (\text{Pretraining})$$
$$\theta_i = \theta(l_{\text{SI}}(\{D_{t_i}\}, \theta_{i+1})), \quad (\text{Finetuning})$$

where $i \in \{S, ..., 1\}$, $\mathbf{D}_S = \{D_1, ..., D_S\}$, l_{ERM} represents the Empirical Risk Minimization (ERM) learning process, and l_{SI} represents the learning process with Synaptic Intelligence (SI) (Zenke et al., 2017) constraining parameter changes.

Pretraining aims to capture intrinsic, timeinvariant distributions. We apply standard ERM training with source domains $\{D_1, \ldots, D_S\}$. No temporal information is incorporated during this stage. Unlike WA for DG (Cha et al., 2021, 2022; Rame et al., 2022; Wortsman et al., 2022), we update normalization layers during pretraining to prevent underfitting, as TDG exhibits smaller distribution differences than DG settings.

Temporal Finetuning sequentially adapts the base model to capture time-varying distributions. We freeze the normalization layers and proceed in reverse temporal order $(t_S \rightarrow ... \rightarrow t_1)$ in this stage. For each domain D_i , we uniformly sample Kweights during finetuning, $\{\theta_i^k\}_{k=1}^K$, and expert θ_i is obtained by uniform averaging: $\theta_i = \sum_{k=1}^K \frac{1}{K} \theta_i^k$

SI (Zenke et al., 2017) is used to constrain parameter changes, which also prevent catastrophic forgetting of intrinsic distributions. Other continual learning methods can also be used. Since later fine-tuning stages are influenced by previous ones, we use reverse temporal order (recent to earliest) to better capture distributions from recent domains that more likely resemble future test domains under smooth distribution shift assumptions.

3.3 Adaptive Weight Averaging

If future weights are available, we could satisfy Insight 2 by assigning coefficients based on expertfuture weight proximity, although we could directly 265

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use future weights. However, precisely predicting the future in high-dimensional weight space is
both hard and computationally prohibitive. As we
only need relative rankings of expert-future proximity, we can project experts into a low-dimensional
space that captures the principal components of
weight temporal evolution, enabling us to predict
future positions and measure expert-future proximity efficiently for assigning averaging coefficients.

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PCA over Temporal Weight Deviation. The weight deviations $\{\delta\theta_i\}_{i=1}^S$, $\delta\theta_i = \theta_i - \theta_{\text{base}}$ of all experts captures weight dynamics under temporal distribution shifts, though these dynamics typically stem from multiple underlying factors and contain noise. We apply PCA to $\{\delta\theta_i\}_{i=1}^S$ to decompose the principal components of weight temporal evolution and reduce noise. By considering only the *P* most significant components $\{v_p\}_{p=1}^P$, we can obtain a *P*-dimensional space and project the experts into points in this space, where $\mathbf{c}_i = (c_i^1, ..., c_i^P)$ is the projection of θ_i :

$$\mathbf{c}_{i} = (c_{i}^{1}, ..., c_{i}^{P})$$

$$= (\langle \theta_{i} - \theta_{\text{base}}, v_{1} \rangle, ..., \langle \theta_{i} - \theta_{\text{base}}, v_{P} \rangle)$$
(4)

Principal Component Trajectory Forecasting. We could construct a temporal evolution trajectory of the *P* principle components with all experts' projected points and their timestamps, $\{(\mathbf{c}_i, t_i)\}_{i=1}^S$. Then we predict the future domain position in this *P*-dimensional space by forecasting along this temporal evolution trajectory. As we often have limited temporal domains available leading to few historical points in the trajectory, we simply model the *P*-dimensional trajectory as *P* separate time series, $\{(c_i^p, t_i)\}_{i=1}^P$ for $p \in \{1, ..., P\}$, by treating all the dimensions independently. For prediction, we apply the Autoregressive Integrated Moving Average (ARIMA) model to each time series:

$$c^{p}(t_{f}) = \operatorname{ARIMA}(\{(c_{i}^{p}, t_{i})\}_{i=1}^{S}, t_{f})$$
 (5)

where $p \in \{1, ..., P\}$ and t_f is the future domain's timestamp. The predicted future point in the principle component space is $\mathbf{c}_f = (c^1(t_f), ..., c^P(t_f))$. **Distance-based Averaging Coefficients** Based on Insight 2, we assign higher averaging coefficients to experts with greater expert-future proximity (lower expert-future distance) in the principal component space. Specifically, for expert θ_i with projected point $\mathbf{c}_i = (c_i^1, ..., c_i^P)$ and our predicted future point $\mathbf{c}_f = (c^1(t_f), ..., c^P(t_f))$, we calculate distance $d_i = \|\mathbf{c}_i - \mathbf{c}_f\|$. We then assign the averaging coefficient for θ_i as:

$$\alpha_{i} = \frac{(d_{\max} - d_{i})^{r}}{\sum_{j=1}^{n} (d_{\max} - d_{j})^{r}},$$
(6)

where $d_{\max} = \max(d_1, ..., d_n)$ and r is a hyperparameter controlling the sharpness of the weighting distribution. Higher r concentrates the averaging more on experts closer to the predicted future.

3.4 TWA for CDTDG

The TWA method described above targets the original TDG setting with access to all source domains, and cannot be directly applied to the CDTDG setting with sequentially available domains. Simply sampling models during the incremental learning process fails because adjacent domains have variations not only from temporal distribution shifts but also from newly introduced data, which inevitably leads to significant parameter differences even between models from adjacent domains, thereby violating the locality constraints.

We therefore slightly relax the CDTDG constraints by maintaining small memory buffers (e.g., 10%) of used training data $\{d_1, d_2, \ldots, d_S\}$ from each domain. After training on the final source domain, we can access these buffers, which is reasonable in practice with minimal impacts on fairness by using only previously seen data. Based on this relaxation, we apply the original TWA framework:

$$\theta_{\text{base}} = \theta_{S+1} = \theta(l_{\text{IncERM}}(\{\mathbf{D}_S\})) \text{ (Pretraining)}$$
$$\theta_i = \theta(l_{\text{SI}}(\{d_{t_i}\}, \theta_{i+1})), \text{ (Finetuning)}$$

where $i \in \{S, ..., 1\}$, l_{IncERM} is the incremental learning process with ERM, and l_{SI} is the learning process with SI constraining parameter changes.

4 Experimental Results

4.1 Experimental Setup

We first introduce the major experimental setups, with detailed configurations provided in the supplementary material. Note that for overlapped benchmarks, we follow the configurations from Xie et al. (2024c,b) for fair and consistent comparisons.

Benchmarks. We include 4 benchmarks from Yao et al. (2022a) (Huffpost, Arxiv, Yearbook and FMoW), 2 benchmarks from Lin et al. (2022) (CLEAR-10/100), and Rotated MNIST (RMNIST). Huffpost and Arxiv are text benchmarks; others are image benchmarks. RMNIST and Yearbook are small-scale; others are large-scale. Each dataset is

| | | | | | | Method | 1 | | | | |
|---------------------------------|----------------------|--------------|-------|-------|-------|--------------|-------|--------|--------------|--------------|------------|
| Dataset | Metric | ERM | IRM | CORAL | Mixup | LISA | GI§ | LSSAE§ | SWAD | DiWA | TEA (ours) |
| Versleet | D_{S+1} | 89.30 | 97.09 | 95.94 | 94.98 | 95.51 | 97.42 | 93.93 | 97.18 | 97.66 | 97.71 |
| Yearbook (Yao et al., 2022a) | OOD _{avg.} | 88.46 | 94.52 | 91.79 | 91.12 | 92.97 | 96.37 | 92.12 | 95.00 | <u>95.36</u> | 95.95 |
| (100 ct ul., 20220) | OODworst | 86.81 | 92.58 | 88.84 | 88.35 | 91.29 | 95.73 | 88.75 | <u>93.89</u> | 94.42 | 94.80 |
| | D_{S+1} | <u>98.15</u> | 95.10 | 93.04 | 97.11 | 96.21 | 97.78 | 96.73 | 97.93 | 97.67 | 98.61 |
| RMNIST | OOD _{avg.} | <u>92.14</u> | 85.05 | 79.10 | 89.66 | 87.04 | 91.00 | 90.36 | 94.51 | 92.06 | 94.47 |
| | OODworst | <u>83.89</u> | 72.52 | 62.96 | 79.63 | 75.15 | 82.46 | 82.13 | 84.89 | 84.31 | 88.83 |
| EM . W | D_{S+1} | 72.43 | 64.77 | 62.14 | 70.27 | 70.05 | 61.62 | 59.15 | 71.59 | 73.85 | 75.63 |
| FMoW (Yao et al., 2022a) | OOD _{avg.} | <u>59.76</u> | 54.92 | 51.42 | 57.73 | 55.52 | 50.83 | 48.66 | 59.96 | 60.77 | 62.45 |
| (100 ct ul., 20220) | OOD _{worst} | <u>49.85</u> | 46.51 | 42.19 | 48.04 | 44.61 | 42.78 | 41.38 | 50.48 | 51.00 | 52.45 |
| CLEAD 10 | D_{S+1} | 80.83 | 77.50 | 77.57 | 78.57 | 71.50 | 72.73 | 55.63 | 69.20 | 81.03 | 83.53 |
| CLEAR-10 (Lin et al., 2022) | OOD _{avg.} | 81.20 | 77.03 | 77.89 | 78.21 | 70.89 | 71.31 | 55.74 | 68.14 | 81.17 | 83.16 |
| (Liff et al., 2022) | OOD _{worst} | 80.83 | 76.60 | 77.47 | 76.90 | 70.27 | 70.33 | 54.83 | 67.53 | 80.60 | 82.43 |
| CLEAD 100 | D_{S+1} | 63.92 | 57.74 | 61.95 | 62.96 | 53.80 | 51.87 | 39.82 | 47.38 | 65.64 | 67.39 |
| CLEAR-100 (Lin et al., 2022) | OOD _{avg.} | <u>63.19</u> | 56.79 | 60.53 | 62.42 | 52.82 | 51.06 | 39.41 | 46.04 | 64.71 | 66.96 |
| (Enret un, 2022) | OODworst | <u>62.62</u> | 56.24 | 59.46 | 61.93 | 52.08 | 50.32 | 38.87 | 45.18 | 63.96 | 66.43 |
| Huffpost | D_{S+1} | 72.74 | 71.04 | 71.34 | 73.34 | 72.19 | 68.06 | - | 73.40 | 73.31 | 73.43 |
| (Yao et al., 2022a) | OOD _{avg.} | <u>71.50</u> | 70.31 | 70.08 | 71.16 | 70.24 | 66.32 | - | 71.59 | 71.51 | 72.12 |
| (1a0 ct al., 2022a) | OOD _{worst} | <u>69.63</u> | 68.97 | 68.68 | 69.29 | 68.60 | 64.64 | - | 70.10 | 70.18 | 70.64 |
| A | D_{S+1} | 57.49 | 51.11 | 50.98 | 57.58 | 56.53 | 53.43 | - | 57.08 | 57.21 | 59.28 |
| Arxiv (Yao et al., 2022a) | OOD _{avg.} | 52.38 | 45.89 | 45.77 | 52.77 | 52.41 | 49.19 | - | 52.96 | 52.80 | 55.23 |
| (140 ct al., 2022a) | OODworst | 49.28 | 42.86 | 42.71 | 49.62 | <u>49.67</u> | 46.13 | - | 50.09 | 49.92 | 52.31 |
| | D_{S+1} | 76.41 | 73.48 | 73.28 | 76.40 | 73.68 | 71.70 | - | 73.25 | 77.91 | 79.37 |
| Overall Avg. | OOD _{avg.} | 72.66 | 69.22 | 68.08 | 71.87 | 69.13 | 67.87 | - | 69.74 | <u>74.77</u> | 75.76 |
| | OOD _{worst} | <u>69.13</u> | 64.90 | 62.04 | 67.54 | 65.95 | 64.63 | - | 65.71 | 70.55 | 72.56 |

Table 1: Accuracy (%) on all benchmarks under TDG setting. Baselines include ERM, IRM (Arjovsky et al., 2019), CORAL (Sun and Saenko, 2016), Mixup (Zhang et al., 2018), LISA (Yao et al., 2022b), GI (Nasery et al., 2021), LSSAE (Qin et al., 2022), SWAD (Cha et al., 2021), and DiWA (Rame et al., 2022). Best and second-best results are **bolded** and <u>underlined</u>. For FMoW, CLEAR-10&100, Huffpost and Arxiv, we only apply GI to classifiers due to backbone size limitations. LSSAE only applies to image benchmarks. § indicates TDG baselines.

divided into first *S* source and last *F* target domains with ratios S : F of: Yearbook (16:5), RMNIST (6:3), FMoW (13:3), Huffpost (4:3), Arxiv (9:7), and CLEAR-10/100 (5:5). Each source domain uses a random 90%-10% train-validation split.

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Model Architectures. We use: 4-layer CNN for Yearbook, ConvNet (Qin et al., 2022) for RMNIST, DenseNet-121 (Huang et al., 2017) for FMoW, DistilBERT (Sanh et al., 2019) for Huffpost/Arxiv, and ResNet-18/50 (He et al., 2016) for CLEAR-10/100.

395 **Baselines:** For TDG, we evaluate against ERM, IRM (Arjovsky et al., 2019), CORAL (Sun and Saenko, 2016), Mixup (Zhang et al., 2018), LISA (Yao et al., 2022b), GI (Nasery et al., 2021), LSSAE (Qin et al., 2022), SWAD (Cha et al., 2021), and DiWA (Rame et al., 2022), where GI 400 and LSSAE are representative TDG methods and 401 SWAD and DiWA are representative weight averag-402 ing approaches. For CDGTD, we include Incremen-403 tal ERM (IncERM), Mixup (Zhang et al., 2018), 404 405 SimCLR (Chen et al., 2020), SwAV (Caron et al., 2020), EWC (Kirkpatrick et al., 2017), SI (Zenke 406 et al., 2017), A-GEM (Chaudhry et al., 2018), 407 DRAIN (ying Bai et al., 2022), EvoS (Xie et al., 408 2024c), and W-Diff (Xie et al., 2024b), with EvoS 409

and W-Diff being state-of-the-art CDGTD methods. Due to computational constraints (e.g., GI finetuning costs 400 GPU hours per epoch), full GI and DRAIN are applied only on Yearbook and RM-NIST. For larger benchmarks, we use GI without finetuning and apply DRAIN only to the classifier. **Method Configurations.** Overlapped baselines use configurations from (Xie et al., 2024c,b). TEA maintain equivalent total training steps (e.g., 25 baseline epochs = 20 pretraining + 5 finetuning for TEA). Other details including CLEAR configurations are in the supplement. 410

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4.2 Main Results

TDG setting results and comparisons are presented in Table 1. Our TEA outperforms all baseline methods on both image and text benchmarks. Specifically, we observe: a). Prior TDG baselines (GI (Nasery et al., 2021) and LSSAE (Qin et al., 2022)) perform well on small-scale benchmarks (RMNIST and Yearbook (Yao et al., 2022a)) but degrade significantly on other large-scale benchmarks (Lin et al., 2022; Yao et al., 2022a). While GI's poor performance potentially stems from computational constraints preventing finetuning stage, LSSAE was fully applied, indicating that prior

| D. i. i | | | | | | Me | thod | | | | | |
|---------------------------------|----------------------|--------|-------|--------|--------------|-------|--------------|-------|--------|-------------------|---------------------|--------------|
| Dataset | Metric | IncERM | Mixup | SimCLR | SwAV | EWC | SI | A-GEM | DRAIN§ | EvoS [§] | W-Diff [§] | TEA (ours) |
| V l l. | D_{S+1} | 96.61 | 90.21 | 95.94 | 97.37 | 97.18 | 97.09 | 94.36 | 96.23 | 97.37 | 97.32 | 97.75 |
| Yearbook (Yao et al., 2022a) | OOD _{avg.} | 94.72 | 89.83 | 93.07 | 94.27 | 95.12 | 94.67 | 90.96 | 94.71 | 95.53 | 95.03 | <u>95.29</u> |
| (100 01 0, 20220) | OOD _{worst} | 93.48 | 88.43 | 89.65 | 91.44 | 93.64 | 93.48 | 88.88 | 93.73 | 94.78 | 94.05 | 94.40 |
| | D_{S+1} | 98.62 | 98.43 | 98.23 | 98.08 | 98.56 | 98.61 | 95.99 | 98.52 | 98.64 | <u>98.70</u> | 98.74 |
| RMNIST | OOD _{avg.} | 92.80 | 92.38 | 90.98 | 90.85 | 92.02 | 93.27 | 86.95 | 93.09 | <u>93.84</u> | 94.12 | 93.76 |
| | OOD _{worst} | 84.61 | 83.45 | 81.05 | 80.96 | 82.80 | 85.65 | 75.45 | 85.75 | 87.04 | 87.36 | <u>87.05</u> |
| FMoW | D_{S+1} | 65.52 | 64.84 | 64.97 | 66.47 | 66.23 | 66.61 | 54.54 | 67.22 | 67.18 | 68.80 | 67.87 |
| (Yao et al., 2022a) | OOD _{avg.} | 53.99 | 52.00 | 53.20 | 54.51 | 54.55 | 54.89 | 47.61 | 55.05 | 54.64 | 55.86 | <u>55.21</u> |
| (140 01 41, 20224) | OOD _{worst} | 45.23 | 42.54 | 44.71 | 45.29 | 45.80 | <u>46.46</u> | 41.13 | 46.24 | 45.86 | 46.51 | 46.27 |
| CLEAR-10 | D_{S+1} | 75.90 | 74.97 | 78.43 | 77.53 | 75.07 | 76.73 | 60.67 | 74.40 | 77.03 | 68.00 | 79.20 |
| (Lin et al., 2022) | OOD _{avg.} | 75.82 | 74.99 | 78.41 | <u>78.05</u> | 73.71 | 76.07 | 59.49 | 74.52 | 77.06 | 67.85 | 77.87 |
| (Lin et an, 2022) | OOD _{worst} | 74.83 | 74.10 | 77.73 | 77.13 | 72.30 | 75.00 | 58.17 | 73.97 | 76.87 | 66.03 | 77.43 |
| CLEAR-100 | D_{S+1} | 56.73 | 51.68 | 60.52 | 58.89 | 56.22 | 31.76 | 23.61 | 54.74 | 57.02 | 52.33 | 58.93 |
| (Lin et al., 2022) | OOD _{avg.} | 55.67 | 50.86 | 59.67 | 57.59 | 55.20 | 30.82 | 22.55 | 53.16 | 56.09 | 51.92 | <u>58.43</u> |
| (Lin et an, 2022) | OOD _{worst} | 54.47 | 50.32 | 58.65 | 56.53 | 54.30 | 30.35 | 21.64 | 51.90 | 55.47 | 51.65 | <u>57.70</u> |
| Huffpost | D_{S+1} | 73.57 | 73.07 | - | - | 73.64 | 72.58 | 72.23 | 73.42 | 73.42 | 73.91 | 73.99 |
| (Yao et al., 2022a) | OOD _{avg.} | 71.98 | 71.52 | - | - | 71.53 | 71.50 | 71.16 | 71.75 | 72.36 | 72.29 | 72.40 |
| (100 01 01., 20220) | OOD _{worst} | 69.80 | 69.44 | - | - | 68.99 | 69.61 | 69.10 | 69.69 | 70.19 | 70.40 | 70.61 |
| Arxiv | D_{S+1} | 56.22 | 56.64 | - | - | 56.60 | 49.98 | 52.02 | 56.04 | 56.60 | 56.66 | 57.34 |
| (Yao et al., 2022a) | OOD _{avg.} | 52.43 | 52.95 | - | - | 52.78 | 47.27 | 48.91 | 52.07 | 53.15 | <u>53.43</u> | 54.20 |
| (| OOD _{worst} | 49.37 | 49.97 | - | - | 49.73 | 44.77 | 46.03 | 48.97 | 50.19 | <u>50.70</u> | 51.41 |
| | D_{S+1} | 73.88 | 72.01 | - | - | 74.79 | 69.34 | 64.77 | 74.29 | 75.32 | 73.67 | 76.26 |
| Overall Avg. | OOD _{avg.} | 71.23 | 69.55 | - | - | 71.88 | 66.48 | 61.34 | 70.99 | 71.81 | 70.07 | 72.45 |
| | OOD _{worst} | 67.59 | 65.46 | - | - | 67.84 | 63.40 | 57.09 | 67.94 | 68.63 | 66.67 | 69.27 |

Table 2: Accuracy (%) under CDGTD setting. Baselines include: ERM (IncERM), Mixup (Zhang et al., 2018), SimCLR (Chen et al., 2020), SwAV (Caron et al., 2020), EWC (Kirkpatrick et al., 2017), SI (Zenke et al., 2017), A-GEM (Chaudhry et al., 2018), DRAIN (ying Bai et al., 2022), EvoS (Xie et al., 2024c), and W-Diff (Xie et al., 2024b). Best and second-best results are **bolded** and <u>underlined</u>. For FMoW, CLEAR-10, CLEAR-100, Huffpost and Arxiv, we only apply DRAIN to classifiers due to backbone size limitations. SimCLR and SwAV only apply to image benchmarks. § indicates TDG baselines.

TDG methods also struggle to model temporal distribution shifts on large-scale tasks beyond computational limitations. In contrast, TEA consistently improves performance across all scales, outperforming GI by up to 30% and LSSAE by up to 69%; b). TEA also consistently outperforms weight averaging methods (DiWA (Rame et al., 2022) and SWAD (Cha et al., 2021)), validating that our approach not only benefits from sampling experts with functional diversity and parameter similarity but further leverages adaptive averaging coefficients to specifically address temporal shifts, thereby enhancing temporal generalization beyond standard weight averaging techniques.

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CDGTD setting results and comparisons are pre-449 sented in Table 2. Our TEA still achieves the best 450 performance on average, outperforming state-of-451 the-art CDGTD baselines, EvoS (Xie et al., 2024c) 452 and W-Diff (Xie et al., 2024b). On text benchmarks, 453 our TEA consistently performs the best, while on 454 image benchmarks, although different benchmarks 455 456 favor different methods, our TEA generally ranks within the top two. These results demonstrate the 457 superiority and flexibility of TEA, showing that 458 TEA can effectively improve temporal generaliza-459 tion even under imited data access constraints. 460

Training Cost Analysis is presented in Table 3. Early TDG methods (GI (Nasery et al., 2021), LSSAE (Qin et al., 2022), and DRAIN (ying Bai et al., 2022)) significantly increase training costs (see Yearbook and RMNIST for full costs). Even classifier-only W-Diff averages 81× the training cost. In contrast, our TEA only slightly increases cost by 33% over ERM in both TDG and CDGTD, being up to 60x more efficient that prior TDG/CDGTD baselines. 461

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4.3 Ablation Study and Analysis

Single Model Ablation results are shown in Table 4. The *Random Expert* average accuracies from randomly selected temporal experts, while *Last Expert* shows accuracies from the last domain experts. *Random Expert* performs worse than ERM, indicating that our method does not simply improve domain-agnostic convergence during fine-tuning. *Last Expert* outperforms *Random Expert*, demonstrating that our temporal finetuning enables the model to learn domain-specific distributions, achieving functional diversity among experts.

Weight Averaging Ablation are shown in Table 4. Recall that TEA optimizes two tradeoffs: (1) functional diversity vs. parameter similarity (with tem-

| Method | Yearbook | RMNIST | CLEAR-10 | CLEAR-100 | FMoW | HuffPost | Arxiv | Overall | Rel. Cost |
|--------|-------------|--------|----------|------------------|------------------|-------------------|-------|---------|-----------|
| | TDG setting | | | | | | | | |
| ERM | 0.02 | 0.02 | 0.30 | 1.58 | 2.34 | 3.05 | 7.92 | 2.18 | 1.00 |
| GI | 0.21 | 1.31 | 0.32* | 3.54* | 5.35* | 3.87* | 9.75* | 3.48 | 12.01 |
| LSSAE | 0.19 | 0.22 | 2.19 | 9.43 | 12.05 | - | - | - | 7.78 |
| TEA | 0.04 | 0.04 | 0.33 | 1.62 | 2.43 | 3.23 | 8.57 | 2.32 | 1.33 |
| | | | | CDGTD settin | g | | | | |
| IncERM | 0.02 | 0.02 | 0.30 | 1.58 | 2.34 | 3.03 | 7.95 | 2.18 | 1.00 |
| DRAIN | 0.05 | 0.13 | 0.33† | 1.75^{\dagger} | 2.45^{\dagger} | 3.07 [†] | 8.86 | 2.38 | 2.05 |
| EvoS | 0.07 | 0.07 | 0.38 | 1.67 | 2.56 | 3.08 | 9.04 | 2.41 | 1.80 |
| W-Diff | 3.12 | 6.74 | 3.47 | 32.35 | 65.31 | 13.18 | 77.93 | 28.87 | 81.01 |
| TEA | 0.04 | 0.04 | 0.32 | 1.64 | 2.46 | 3.19 | 8.65 | 2.33 | 1.33 |

Table 3: Training cost (hours on A40 GPU) for each method. Rel. Cost is the computational cost ratio vs. ERM/IncERM, averaged across all tasks. *GI without finetuning. [†]Classifier-only DRAIN.

| Configuration | Yearbook | RMNIST | FMoW | CLEAR-10 | CLEAR-100 | Huffpost | Arxiv | Overall |
|---------------------------|----------|--------|-------|----------|-----------|----------|-------|---------|
| Single Model | | | | | | | | |
| - ERM | 88.46 | 92.14 | 59.76 | 81.20 | 63.19 | 71.50 | 52.38 | 72.66 |
| - Random Expert | 87.46 | 82.29 | 59.37 | 81.63 | 63.26 | 71.34 | 52.05 | 71.06 |
| - Last Expert | 95.42 | 92.17 | 60.49 | 81.53 | 63.16 | 71.33 | 54.57 | 74.10 |
| Weight Averaging | | | | | | | | |
| - Only Temporal Experts | 95.41 | 92.64 | 60.54 | 82.12 | 66.32 | 71.43 | 53.79 | 74.61 |
| - Only Adaptive Averaging | 94.03 | 92.92 | 60.83 | 83.07 | 66.85 | 71.73 | 53.26 | 74.67 |
| Full TEA (ours) | 95.95 | 94.47 | 62.45 | 83.16 | 66.96 | 72.12 | 55.23 | 75.76 |

Table 4: Ablation study of TEA components under the TDG setting with OOD average accuracy (%).

| Coefficients | Yearbook | RMNIST | Arxiv | Overall |
|--------------|----------|--------|-------|---------|
| ERM | 88.46 | 92.14 | 52.38 | 72.66 |
| Correct | 95.95 | 94.47 | 55.23 | 75.76 |
| Reversed | 82.95 | 77.03 | 50.13 | 70.05 |

Table 5: Temporal Sanity Check with OOD Avg. Accuracy (%). Overall is averaged across the 7 benchmarks.



Figure 4: Visualization of averaging coefficients and accuracies of experts on target domain D_{S+1} .

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poral experts), and (2) bias vs. variance (with adaptive averaging). *Only Temporal Experts* uses uniform coefficients to average experts, optimizing only tradeoff 1, while *Only Adaptive Averaging* samples domain-agnostic weights then trains Time2Vec (Kazemi et al., 2019) for adaptive coefficients (detailed in supp.), optimizing only tradeoff 2. Both variants underperform full TEA, validating the necessity of both design choices.

Temporal Sanity Check are shown in Figure 4 and Table 5. Our adaptive averaging should increase coefficients for better-performing experts on future domains while decreasing coefficients for poor performers. Figure 4 confirms this design by showing higher coefficients for higher-performing models on domain D_{S+1} . Table 5 validates our design by showing that reversing coefficient order leads to worse OOD accuracy than ERM. 500

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5 Conclusion

This work addresses Temporal Domain Generalization (TDG), enabling models to generalize across temporal distribution shifts. We propose Temporal Expert Averaging (TEA), an efficient weight averaging framework for large-scale TDG. Based on theoretical insights, TEA uses constrained temporal finetuning to create functionally diverse yet parameter-similar experts, then adaptively averages them using coefficients derived from temporal dynamics of weight deviation principal components. Comprehensive evaluation demonstrates TEA's superior performance and efficiency across TDG and CDGTD settings. Since prior TDG work focuses on small-scale scenarios, we hope this encourages research on large-scale temporal generalization.

Limitations. Like prior TDG methods, our TEA relies on smooth distribution shift assumptions and cannot guarantee performance with abrupt shifts. Since most large-scale TDG benchmarks use discrete domains, we only explore discrete settings, though TEA could theoretically extend to Continuous Temporal Domain Generalization (CTDG).

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A **Experimental Setup Details**

A.1 Benchmark Introduction

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Huffpost (Ginosar et al., 2015) is a text classification benchmark comprising news headlines from The Huffington Post spanning 2012-2018. The task requires classifying headlines into 11 news categories: "Black Voices", "Business", "Comedy", "Crime", "Entertainment", "Impact", "Queer Voices", "Science", "Sports", "Tech", and "Travel". This temporal dataset captures evolving journalistic styles and content trends in digital media over six years. We adopt a temporal split using the first 4 years as training domains and the final 3 years as test domains for evaluating temporal generalization. Sample distributions across domains are detailed in Table 6.

Arxiv (Ginosar et al., 2015) is a text classification 842 benchmark containing paper titles and their corresponding primary categories spanning 2007-2022. The task requires classifying research papers into one of 172 categories based solely on their titles. This temporal dataset reflects the dynamic evolution of research fields, with changing academic trends and emerging disciplines captured across the 16-year timespan. We adopt a temporal split 850 using the first 9 years as training domains and the final 7 years as test domains for evaluating temporal generalization. Sample distributions across domains are presented in Table 7.

Yearbook dataset, sourced from Yao et al. (2022a) and built upon the MIT-licensed Portraits dataset (Ginosar et al., 2015), comprises 32×32 grayscale yearbook portraits from 128 American high schools across 27 states. Spanning eight decades (1930-2013), this temporal dataset captures the evolution of fashion trends and societal changes, making it particularly suitable for evaluating algorithmic performance on temporal domain shift. We formulate the task as binary gender classification, partitioning the timeline into 4-year intervals to create 21 distinct domains. Following standard practice, we allocate the initial 16 domains for training and reserve the final 5 domains for outof-domain evaluation. Sample distributions across domains are detailed in Table 8.

Rotated MNIST (RMNIST) derives from the clas-871 sic MNIST dataset (Deng, 2012) by systemati-872 cally applying rotational transformations from 0° to 80° in 10° increments, creating 9 sequential domains that simulate temporal distribution shift. 875

This benchmark evaluates 10-class digit classification performance on 28×28 grayscale images under gradually increasing rotational distortion. We adopt a 6-3 domain split, utilizing the initial six domains for model training and evaluating generalization on the final three domains.

FMoW (Ginosar et al., 2015) contains 224×224 RGB satellite imagery spanning 2002-2017 across 200 countries. This temporal benchmark captures natural evolution in visual features driven by human development and environmental changes over time. The classification task involves predicting functional land use across 62 categories, ranging from residential areas to industrial facilities. We partition the dataset temporally with each year constituting a distinct domain, yielding 16 total domains. Training utilizes the first 13 domains, while the final 3 domains serve as out-of-distribution test sets. Domain-wise sample distributions are provided in Table 9.

CLEAR-10&100 (Lin et al., 2022) contain useruploaded images from 2007-2014 with natural temporal shifts of visual concepts. Samples are organized into 10 chronologically ordered domains. CLEAR-10 comprises 10 classes with 3,000 samples per domain (300 per class), while CLEAR-100 contains 100 classes with 10,000 samples per domain (100 per class). We set the image input shape as (224, 224, 3) and use the first 5 domains as source domains and the final 5 domains as target domains for temporal generalization evaluation.

| Domain | Year | Training Split | Validation Split | All |
|--------|-----------|----------------|------------------|-------|
| 1 | 2012 | 6701 | 744 | 7446 |
| 2 | 2013 | 7492 | 832 | 8325 |
| 3 | 2014 | 9539 | 1059 | 10599 |
| 4 | 2015 | 11826 | 1313 | 13140 |
| 5 | 2016 | 10548 | 1172 | 11721 |
| 6 | 2017 | 7907 | 878 | 8786 |
| 7 | 2018 | 3501 | 388 | 3890 |
| Total | 2012-2018 | 57514 | 6386 | 63907 |

Table 6: Domain Sizes for Huffpost (Yao et al., 2022a)

A.2 Method Configurations

Huffpost (Yao et al., 2022a) uses pretrained Distil-BERT base model (Sanh et al., 2019) as the backbone. All baseline methods are trained on 90% randomly split training data from source domains for 50 epochs with learning rate 2e-5 (except A-GEM which uses 1e-7). Other baseline configurations follow Xie et al. (2024c,b).

| Domain | Year | Training Split | Validation Split | All |
|--------|-----------|----------------|------------------|---------|
| 1 | 2007 | 131550 | 14616 | 146167 |
| 2 | 2008 | 62460 | 6939 | 69400 |
| 3 | 2009 | 206244 | 22916 | 229161 |
| 4 | 2010 | 50665 | 5629 | 56295 |
| 5 | 2011 | 55741 | 6193 | 61935 |
| 6 | 2012 | 51678 | 5741 | 57420 |
| 7 | 2013 | 64951 | 7216 | 72168 |
| 8 | 2014 | 79498 | 8833 | 88332 |
| 9 | 2015 | 193979 | 21553 | 215533 |
| 10 | 2016 | 120682 | 13409 | 134092 |
| 11 | 2017 | 111024 | 12336 | 123361 |
| 12 | 2018 | 123891 | 13765 | 137657 |
| 13 | 2019 | 142767 | 15862 | 158630 |
| 14 | 2020 | 166014 | 18445 | 184460 |
| 15 | 2021 | 201241 | 22360 | 223602 |
| 16 | 2022 | 89765 | 9973 | 99739 |
| Total | 2007-2022 | 1852150 | 205786 | 2057952 |

Table 7: Domain Size for Arxiv (Yao et al., 2022a)

| Domain | Interval | Training Split | Validation Split | All |
|--------|-------------|----------------|------------------|-------|
| 1 | 1930 - 1933 | 758 | 87 | 845 |
| 2 | 1934 - 1937 | 1149 | 130 | 1279 |
| 3 | 1938 – 1941 | 949 | 108 | 1057 |
| 4 | 1942 - 1945 | 2353 | 263 | 2616 |
| 5 | 1946 – 1949 | 1229 | 138 | 1367 |
| 6 | 1950 – 1953 | 1082 | 122 | 1204 |
| 7 | 1954 – 1957 | 1646 | 185 | 1831 |
| 8 | 1958 – 1961 | 1295 | 146 | 1441 |
| 9 | 1962 - 1965 | 1468 | 166 | 1634 |
| 10 | 1966 – 1969 | 2227 | 249 | 2476 |
| 11 | 1970 – 1973 | 1634 | 183 | 1817 |
| 12 | 1974 – 1977 | 2238 | 250 | 2488 |
| 13 | 1978 – 1981 | 1553 | 175 | 1728 |
| 14 | 1982 – 1985 | 2331 | 261 | 2592 |
| 15 | 1986 – 1989 | 1792 | 201 | 1993 |
| 16 | 1990 - 1993 | 1729 | 195 | 1924 |
| 17 | 1994 – 1997 | 1882 | 211 | 2093 |
| 18 | 1998 - 2001 | 2136 | 239 | 2375 |
| 19 | 2002 - 2005 | 1868 | 210 | 2078 |
| 20 | 2006 - 2009 | 1010 | 114 | 1124 |
| 21 | 2010 - 2013 | 1102 | 125 | 1227 |
| Total | 1930 - 2013 | 33431 | 3758 | 37189 |

Table 8: Domain Sizes for Yearbook (Yao et al., 2022a)

TEA for Huffpost uses the same DistilBERT back-915 bone. Under TDG setting, TEA first trains on all 916 source domain training splits using ERM for 45 917 epochs with learning rate 2e-5 during the pretrain-918 ing stage, then performs temporal finetuning for 919 5 epochs on each domain in reverse temporal or-920 der (from 2015 to 2012) using SI with learning 921 rate 5e-6 and constraint strength $c_{si} = 0.1$. Under CDGTD setting, we adopt 47-epoch incremental 923 ERM training on each domain (from 2012 to 2015) with learning rate 2e-5, followed by 30 temporal 925 finetuning epochs on each domain in reverse tempo-927 ral order (from 2015 to 2012) using SI with learning rate 5e-6 and constraint strength $c_{si} = 0.1$. Note 928 that temporal finetuning under CDGTD uses only 10% of the data, so the total training cost remains 47+30×0.1=50 epochs. During temporal finetun-931

| Domain | Year | Training Split | Validation Split | All |
|--------|-----------|----------------|------------------|--------|
| 1 | 2002 | 1676 | 227 | 1903 |
| 2 | 2003 | 2279 | 276 | 2555 |
| 3 | 2004 | 1755 | 240 | 1995 |
| 4 | 2005 | 2512 | 324 | 2836 |
| 5 | 2006 | 3155 | 406 | 3561 |
| 6 | 2007 | 1497 | 190 | 1687 |
| 7 | 2008 | 2261 | 298 | 2559 |
| 8 | 2009 | 7439 | 935 | 8374 |
| 9 | 2010 | 18957 | 2456 | 21413 |
| 10 | 2011 | 22111 | 2837 | 24948 |
| 11 | 2012 | 24704 | 3138 | 27842 |
| 12 | 2013 | 3465 | 385 | 3850 |
| 13 | 2014 | 5572 | 620 | 6192 |
| 14 | 2015 | 8885 | 988 | 9873 |
| 15 | 2016 | 14363 | 1596 | 15959 |
| 16 | 2017 | 5534 | 615 | 6149 |
| Total | 2002-2017 | 126165 | 15531 | 141696 |

Table 9: Domain Sizes for FMoW (Yao et al., 2022a)

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ing on each domain, we sample model weights at K = 5 evenly spaced training steps and uniformly average them to obtain expert model weights. For PCA on expert deviations, we use the top 10 principal components. For ARIMA estimation, we employ an ARIMA(1,1,1) model. When computing averaging coefficients, we set the sharpness hyperparameter r = 5.

Arxiv (Yao et al., 2022a) also uses pretrained DistilBERT base model (Sanh et al., 2019) as the backbone. All baseline methods are trained on 90% randomly split training data from source domains for 5 epochs with learning rate 2e-5 (except A-GEM which uses 1e-6). Other baseline configurations follow Xie et al. (2024c,b).

TEA for Arxiv uses the same DistilBERT backbone. Under TDG setting, TEA first trains on all source domain training splits using ERM for 4 epochs with learning rate 2e-5 during the pretraining stage, then performs temporal finetuning for 1 epoch on each domain in reverse temporal order (from 2015 to 2007) using SI with learning rate 5e-6 and constraint strength $c_{si} = 0.1$. Under CDGTD setting, we adopt 4-epoch incremental ERM training on each domain (from 2007 to 2015) with learning rate 2e-5, followed by 10 temporal finetuning epochs on each domain in reverse temporal order (from 2015 to 2007) using SI with learning rate 5e-6 and constraint strength $c_{si} = 0.1$. Note that temporal finetuning under CDGTD uses only 10% of the data, so the total training cost remains $4+10\times0.1=5$ epochs. During temporal finetuning on each domain, we sample model weights at K = 5 evenly spaced training steps and uniformly average them to obtain expert

967model weights. For PCA on expert deviations, we968use the top 10 principal components. For ARIMA969estimation, we employ an ARIMA(1,1,1) model.970When computing averaging coefficients, we set the971sharpness hyperparameter r = 5.

Yearbook (Yao et al., 2022a) uses a 4-layer convolutional network from Yao et al. (2022a). All baseline methods are trained on 90% randomly split
training data from source domains for 50 epochs
with learning rate 1e-3. Other baseline configurations follow Xie et al. (2024c,b).

TEA for Yearbook uses the same 4-layer convolu-978 tional network from Yao et al. (2022a). Under TDG 979 setting, TEA first trains on all source domain training splits using ERM for 40 epochs with learning 981 rate 1e-3 during the pretraining stage, then per-982 forms temporal finetuning for 10 epochs on each domain in reverse temporal order (from D_{16} to D₁) using SI with learning rate 5e-4 and constraint strength $c_{si} = 0.1$. Under CDGTD setting, we adopt 48-epoch incremental ERM training on each 987 domain (from D_1 to D_{16}) with learning rate 1e-3, followed by 20 temporal finetuning epochs on each domain in reverse temporal order (from D₁₆ to D_1) using SI with learning rate 5e-4 and constraint strength $c_{si} = 0.1$. Note that temporal finetuning 992 993 under CDGTD uses only 10% of the data, so the total training cost remains 48+20×0.1=50 epochs. 994 During temporal finetuning on each domain, we 995 sample model weights at K = 5 evenly spaced training steps and uniformly average them to obtain expert model weights. For PCA on expert deviations, we use the top 10 principal components. For 999 ARIMA estimation, we employ an ARIMA(1,1,1)1000 model. When computing averaging coefficients, 1001 we set the sharpness hyperparameter r = 5.

> **RMNIST** adopts the ConvNet in Qin et al. (2022). All baseline methods are trained on 90% randomly split training data from source domains for 50 epochs with learning rate 1e-3 (except A-GEM which uses 1e-5). Other baseline configurations follow Xie et al. (2024c,b).

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TEA for RMNIST uses the same ConvNet. Un-1009 der TDG setting, TEA first trains on all source 1010 domain training splits using ERM for 40 epochs 1011 with learning rate 1e-3 during the pretraining stage, 1012 1013 then performs temporal finetuning for 10 epochs on each domain in reverse temporal order (from 1014 D_6 to D_1) using SI with learning rate 2e-4 and con-1015 straint strength $c_{si} = 0.1$. Under CDGTD setting, we adopt 48-epoch incremental ERM training on 1017

each domain (from D_1 to D_6) with learning rate 1018 1e-3, followed by 20 temporal finetuning epochs on 1019 each domain in reverse temporal order (from D₆ to 1020 D_1) using SI with learning rate 2e-4 and constraint 1021 strength $c_{si} = 0.1$. Note that temporal finetuning 1022 under CDGTD uses only 10% of the data, so the 1023 total training cost remains $48+20\times0.1=50$ epochs. 1024 During temporal finetuning on each domain, we 1025 sample model weights at K = 5 evenly spaced 1026 training steps and uniformly average them to obtain 1027 expert model weights. For PCA on expert devia-1028 tions, we use the top 10 principal components. For 1029 ARIMA estimation, we employ an ARIMA(1,1,1)1030 model. When computing averaging coefficients, 1031 we set the sharpness hyperparameter r = 5. 1032

FMoW (Yao et al., 2022a) adopts a DenseNet-121 (Huang et al., 2017) backbone pretrained on ImageNet (Deng et al., 2009). All baseline methods are trained on 90% randomly split training data from source domains for 25 epochs with learning rate 2e-4 (except A-GEM which uses 1e-6). Other baseline configurations follow Xie et al. (2024c,b). 1033

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TEA for FMoW uses the same DenseNet-1040 121 (Huang et al., 2017). Under TDG setting, TEA 1041 first trains on all source domain training splits using 1042 ERM for 20 epochs with learning rate 2e-4 during 1043 the pretraining stage, then performs temporal fine-1044 tuning for 5 epochs on each domain in reverse tem-1045 poral order (from D_{13} to D_1) using SI with learning 1046 rate 7e-5 and constraint strength $c_{si} = 0.1$. Under 1047 CDGTD setting, we adopt 23-epoch incremental 1048 ERM training on each domain (from D_1 to D_{13}) 1049 with learning rate 2e-4, followed by 20 temporal 1050 finetuning epochs on each domain in reverse tem-1051 poral order (from D_{13} to D_1) using SI with learning 1052 rate 2e-5 and constraint strength $c_{si} = 0.1$. Note 1053 that temporal finetuning under CDGTD uses only 1054 10% of the data, so the total training cost remains 1055 $23+20\times0.1=25$ epochs. During temporal finetun-1056 ing on each domain, we sample model weights at 1057 K = 5 evenly spaced training steps and uniformly 1058 average them to obtain expert model weights. For 1059 PCA on expert deviations, we use the top 10 prin-1060 cipal components. For ARIMA estimation, we 1061 employ an ARIMA(1,1,1) model. When comput-1062 ing averaging coefficients, we set the sharpness 1063 hyperparameter r = 1. 1064

CLEAR-10 (Lin et al., 2022) adopts a ResNet-18 (He et al., 2016). All baseline methods are trained on 90% randomly split training data from source domains for 50 epochs with batch size 128

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and learning rate 1e-3 (except A-GEM which uses 1e-6). Other baseline configurations follow the FMoW configurations from Xie et al. (2024c,b).

TEA for CLEAR-10 uses the same ResNet-18 (He 1072 et al., 2016). Batch size is 128. Under TDG set-1073 ting, TEA first trains on all source domain training 1074 splits using ERM for 45 epochs with learning rate 1075 1e-3 during the pretraining stage, then performs 1076 temporal finetuning for 5 epochs on each domain 1077 in reverse temporal order (from D_5 to D_1) using 1078 SI with learning rate 1e-4 and constraint strength 1079 $c_{si} = 0.1$. Under CDGTD setting, we adopt 49epoch incremental ERM training on each domain 1081 (from D_1 to D_5) with learning rate 1e-3, followed 1083 by 10 temporal finetuning epochs on each domain in reverse temporal order (from D_5 to D_1) using 1084 SI with learning rate 1e-4 and constraint strength 1085 $c_{si} = 0.1$. Note that temporal finetuning under 1086 CDGTD uses only 10% of the data, so the total 1087 training cost remains 49+10×0.1=50 epochs. During temporal finetuning on each domain, we sample 1089 model weights at K = 5 evenly spaced training 1090 steps and uniformly average them to obtain expert 1091 model weights. For PCA on expert deviations, we use the top 10 principal components. For ARIMA 1093 estimation, we employ an ARIMA(1,1,1) model. When computing averaging coefficients, we set the 1095 1096 sharpness hyperparameter r = 0.5.

> **CLEAR-100** (Lin et al., 2022) adopts a ResNet-50 (He et al., 2016). All baseline methods are trained on 90% randomly split training data from source domains for 50 epochs with batch size 128 and learning rate 5e-4 (except A-GEM which uses 1e-6). Other baseline configurations follow the FMoW configurations from Xie et al. (2024c,b).

TEA for CLEAR-100 uses the same ResNet-1104 1105 50 (He et al., 2016). Batch size is 128. Under TDG setting, TEA first trains on all source 1106 domain training splits using ERM for 45 epochs 1107 with learning rate 5e-4 during the pretraining stage, 1108 then performs temporal finetuning for 5 epochs on 1109 each domain in reverse temporal order (from D_5 1110 to D₁) using SI with learning rate 1e-4 and con-1111 straint strength $c_{si} = 0.1$. Under CDGTD setting, 1112 we adopt 49-epoch incremental ERM training on 1113 each domain (from D_1 to D_5) with learning rate 5e-1114 1115 4, followed by 10 temporal finetuning epochs on each domain in reverse temporal order (from D_5 to 1116 D₁) using SI with learning rate 1e-4 and constraint 1117 strength $c_{si} = 0.1$. Note that temporal finetuning 1118 under CDGTD uses only 10% of the data, so the 1119

total training cost remains $49+10\times0.1=50$ epochs. 1120 During temporal finetuning on each domain, we 1121 sample model weights at K = 5 evenly spaced 1122 training steps and uniformly average them to obtain 1123 expert model weights. For PCA on expert devia-1124 tions, we use the top 10 principal components. For 1125 ARIMA estimation, we employ an ARIMA(1,1,1)1126 model. When computing averaging coefficients, 1127 we set the sharpness hyperparameter r = 0.5. 1128

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A.3 Ablation Details

Ablation study of TEA components examines four variants: Random Expert, Last Expert, Only Temporal Experts, and Only Adaptive Averaging. The first three involve simple modifications to specific TEA components, while Only Adaptive Averaging represents a more substantially different variant. We briefly describe the first three below and detail Only Adaptive Averaging in the following section:

- **Random Expert**: Randomly selects expert models and reports the average performance across multiple runs, which effectively equals the average performance of all experts.
- Last Expert: Uses only the expert from the final domain.
- Only Temporal Experts: Identical to TEA except for using uniform averaging coefficients (1/S) instead of adaptive coefficients to average all expert weights.

Only Adaptive Averaging shown in 5 aims to use base weights without temporal fine-tuning to achieve functional diversity, capturing temporal shift patterns solely through adaptive weight averaging in the coefficients. This variant cannot be implemented by simply removing TEA components, as our averaging coefficient estimation relies on shift patterns from experts corresponding to different temporal domains. Without temporal differences between base weights, we cannot use TEA's principal component trajectory-based coefficient estimation. Therefore, we adopt a training-based generation approach instead.

We first sample base weights. Following SWA (Izmailov et al., 2018), we randomly sample S weights from the training process, which we call "snapshots". A key challenge arises with normalization layers: on TDG tasks, freezing normalization layers leads to underfitting, while optimizing them results in snapshots with



Figure 5: An overview of our *Only Adaptive Averaging* ablation. (a) When optimizing the selector network in *Only Adaptive Averaging*, we use output averaging as a proxy task, utilizing the estimated coefficients to average the outputs of all snapshots. (b) During inference, we perform weight averaging with the optimized selector network.

different normalization parameters and statistics. 1168 Since weight averaging is highly sensitive to 1169 normalization differences, excessive variation 1170 causes poor performance in the averaged model. 1171 We address this using a "late sampling" strategy, 1172 as we observe that normalization becomes 1173 sufficiently good during intermediate training 1174 stages. Specifically, we freeze the normalization 1175 layers during the final epoch of each task and 1176 sample K snapshots $\{\theta_k\}_{k=1}^K$ within this last 1177 epoch (noted as K as we use all domain as a 1178 unified domain and set K = S for fair ablation). 1179 We then generate adaptive averaging coefficients 1180 through a training-based approach. Specifically, 1181 we use a Time2Vec (Kazemi et al., 2019) module 1182 with a 2-layer MLP as the selector network ϕ to 1183 generate averaging coefficients. After sampling 1184 the snapshots, we randomly select samples with 1185 timestamps from the training domains and train the 1186 selector network to combine the outputs of these 1187 snapshots. We formulate this training process as: 1188

$$\phi^* = \arg\min_{\phi} \sum_{i \in [1,S]} \sum_{(x,t,y) \sim D_i} \ell\left(\sum_{k=1}^K \phi(t)_k \cdot f(x,\theta_k), y\right)$$

s.t. $\{\theta_k\}_{k=1}^K \sim \mathcal{S}_{ls}(\arg\min_{\theta} \sum_{i \in [1,S]} \sum_{(X,\cdot,Y) \sim D_i} \ell(f(X,\theta),Y)$

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where S_{ls} is the snapshot sampling process with late sampling strategy. We use Adam optimizer for optimizing the selector network with learning rate as 1e-4, batch size as 1 and training steps as 2000.

After training ϕ^* , we use it during inference to

generate averaging coefficients for the K = S 1195 snapshots: $\alpha^{OAA} = \{\alpha_k^{OAA}\}_{k=1}^K = \phi^*(t_f).$ 1196

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B Additional Discussion

TDG's Value for NLP Community. On one hand, 1198 Temporal Domain Generalization (TDG) (Ortiz-1199 Jiménez et al., 2019; Mancini et al., 2019; Wang 1200 et al., 2020; ying Bai et al., 2022; Nasery et al., 1201 2021; Zeng et al., 2023; Wang et al., 2022; Xie et al., 2024c,a; Yong et al., 2023; Xie et al., 2024b) 1203 has broad application prospects in NLP tasks, as 1204 temporal distribution shifts are prevalent in NLP, 1205 such as lexical changes over time and evolving un-1206 derstanding of specific expressions (e.g., memes) 1207 across time periods. Particularly in the large lan-1208 guage model era, TDG's low-resource general-1209 ization nature can reduce the expensive compu-1210 tational and data costs required for LLM retrain-1211 ing or fine-tuning. On the other hand, TDG has 1212 already been widely recognized as a valuable di-1213 rection by the relevant community, with numer-1214 ous papers published in top-tier conferences, in-1215 cluding our baselines: GI (NeurIPS'21) (Nasery 1216 et al., 2021), LSSAE (ICML'22) (Oin et al., 2022), 1217 DRAIN (ICLR'23) (ying Bai et al., 2022), EvoS 1218 (NeurIPS'23) (Xie et al., 2024c), and W-Diff 1219 (NeurIPS'24) (Xie et al., 2024b). 1220

Continual Learning. TDG shares similar data con-
figurations with continual learning (Zenke et al.,
2017; Lopez-Paz and Ranzato, 2017; Shin et al.,122112211222

2017; Chaudhry et al., 2018), and our main bench-1224 marks (Yao et al., 2022a; Lin et al., 2022)were orig-1225 inally introduced for continual learning. However, 1226 TDG and continual learning differ significantly 1227 in their objectives. Standard continual learning primarily focuses on the past, addressing whether 1229 learning new tasks causes catastrophic forgetting of 1230 previous knowledge. In contrast, TDG focuses on 1231 the future, concerned with leveraging past knowl-1232 edge to enhance generalization to future domains. 1233 We incorporate representative continual learning 1234 baselines including EWC (Kirkpatrick et al., 2017), 1235 SI (Zenke et al., 2017), and A-GEM (Chaudhry 1236 et al., 2018), which show no significant generaliza-1237 tion improvement on future domains. 1238

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Continual Domain Generalization over Temporal Drift (CDGTD) can be viewed as an intersection of standard TDG and continual learning. This represents a reasonable application direction, requiring models to both retain past knowledge and generalize well to future domains. However, this does not diminish the importance of standard TDG, as the core challenge of TDG-how to utilize temporal shift patterns in past data for better future generalization-is orthogonal to CDGTD's additional constraint of sequential domain access. Moreover, CDGTD may complicate the exploration of temporal generalization capabilities by introducing an additional variable. Therefore, we consider both standard TDG and CDGTD equally important, with no priority distinction.

Large Language Models (LLMs). While LLMs (OpenAI, 2023; Touvron et al., 2023; Guo et al., 2025) achieve good generalization through training on massive datasets, this does not conflict with TDG. TDG fundamentally targets lowresource scenarios and has considerable practical value when large training datasets are unavailable. Conversely, in cases of relatively smooth temporal distribution shifts, applying TDG with limited data is more data-efficient than brute-force generalization through massive training. Furthermore, regardless of how much data LLMs are trained on, TDG can be further applied to enhance temporal generalization capabilities. Notably, TDG application to LLMs is particularly promising as it can effectively reduce LLM training costs. However, TDG is still far from being applicable to LLMs, primarily due to scaling limitations. This highlights the value of our work as a solid step toward LLM-scale TDG.

1274 **Temporal Reasoning** (Xiong et al., 2024; Yuan

et al., 2024; Fatemi et al., 2024; Chu et al., 2023). 1275 While this may sound related to TDG, the primary 1276 connection is that both contain "temporal" in their 1277 names. Temporal reasoning focuses on enabling 1278 models to understand explicit temporal relation-1279 ships at the individual sample level, whereas TDG 1280 aims to adapt models to implicit temporal distribu-1281 tion shifts at the dataset level. Temporal reasoning 1282 could potentially improve TDG performance, but 1283 this remains unexplored. 1284

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C Theoretical Analysis

C.1 Notations

We denote \mathcal{X} the input space, \mathcal{Y} the label space, and $\ell : \mathcal{Y}^2 \to \mathbb{R}^+$ a loss function. We have a sequence of domains $\{D_i\}$ indexed by timestamps $t_i \in \mathcal{T}$, where \mathcal{T} is a totally ordered set representing time. Each domain D_i has a distribution p_i . For the training (source) domains $\{D_i\}_{i=1}^S$, we have timestamps $t_1 < t_2 < \ldots < t_S$ in \mathcal{T} , and corresponding distributions p_1, p_2, \ldots, p_S . For simplicity, we will use p_i to refer to the joint, posterior, and marginal distributions of (X, Y) at time t. We note $f_i : \mathcal{X} \to \mathcal{Y}$ as the labeling function at time t_i . We assume there is no noise in the data: f_i is defined on $\mathcal{X}_i \triangleq \{x \in \mathcal{X} \mid p_i(x) > 0\}$ by $\forall (x, y) \sim p_i, f_i(x) = y$.

C.2 Temporal Domain Generalization

We consider a neural network (NN) $f(\cdot, \theta) : \mathcal{X} \to \mathcal{Y}$ made of a fixed architecture f with weights θ . Given observations from source domains at times t_1, t_2, \ldots, t_S , we seek θ minimizing the target generalization error at a future time $t_f > t_S$:

$$\mathcal{E}_f(\theta) = \mathbb{E}_{(x,y) \sim p_f}[\ell(f(x,\theta), y)]. \tag{7}$$

 $f(\cdot, \theta)$ should approximate f_f on \mathcal{X}_f . This is challenging in the TDG setup because we only have data from earlier timestamps, which are related yet different from the future target domain.

The differences between domains at different timestamps are due to distribution shifts (i.e., the fact that $p_i(X, Y) \neq p_j(X, Y)$ for $i \neq j$), which can be decomposed into:

- **Diversity shift:** when marginal distributions differ over time (i.e., $p_i(X) \neq p_j(X)$)
- Correlation shift: when posterior distributions differ over time (i.e., $p_i(Y|X) \neq 1319$ $p_j(Y|X)$ and $f_i \neq f_j$) 1320

The weights are typically learned on source domain data $\{D_1, D_2, \ldots, D_S\}$ from timestamps $\{t_1, t_2, \ldots, t_S\}$ (each composed of n_i i.i.d. samples from $p_i(X, Y)$) with a configuration c, which contains all other configurations and sources of randomness in learning. We call $l_{\mathcal{T}} =$ $\{D_1, D_2, \ldots, D_S, c\}$ a learning procedure, and explicitly write $\theta(l_{\mathcal{T}})$ to refer to the weights obtained after stochastic minimization of the appropriate objective function. Specific to our TEA, we define $l_i = \{D_1, D_2, \ldots, D_S, t_i, c\}$ as a temporal expert learning procedure to get expert model $\theta_i = \theta(l_i)$ which is designed to excels on domain D_i while also using data from other domains.

C.3 Temporal Expert Averaging

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We study the benefits of combining S individual member weights $\{\theta_i\}_{i=1}^S \triangleq \{\theta(l_i)\}_{i=1}^S$ obtained from S different domains at timestamps $\{t_1, t_2, \ldots, t_S\}$. Each weight θ_i corresponds to an expert model that is more proficient for domain D_i (though not necessarily trained exclusively on that domain).

Unlike traditional weight averaging (Cha et al., 2021; Rame et al., 2022; Wortsman et al., 2022) that uses equal coefficients, for temporal domain generalization, we propose a temporally-weighted averaging scheme that assigns different importance to experts based on their relevance to the target future domain.

Temporal Expert Averaging (TEA) is defined as:

$$f_{\text{TEA}} \triangleq f(\cdot, \theta_{\text{TEA}}),$$

$$\theta_{\text{TEA}} \triangleq \sum_{i=1}^{S} \alpha_i \left(\{t_i\}_{i=1}^{S}, \{\theta_i\}_{i=1}^{S}, t_f \right) \cdot \theta_i. \quad (8)$$

where the coefficients $\{\alpha_i\}_{i=1}^S$ satisfy $\sum_{i=1}^S \alpha_i = 1$ and $\alpha_i \ge 0$ for all *i*. These coefficients are determined based on the temporal shift among the source domain experts $\{\theta_i\}_{i=1}^S$ and temporal information $\{t_i\}_{i=1}^S$ and t_f .

C.4 TEA loss derivation

Following Rame et al. (2022), we decompose TEA's error leveraging the similarity between WA and functional ensembling (ENS) (Lakshminarayanan et al., 2017; Dietterich, 2000), a more traditional way to combine a collection of weights. We also use Mean Squared Error as ℓ for simplicity. For TDG setting, we define Temporal ENS (T-ENS) with coefficients $\{\alpha_i\}_{i=1}^S$ as

$$f_{\text{T-ENS}} \triangleq \sum_{i=1}^{S} \alpha_i f(\cdot, \theta_i).$$
 (9) 1367

Lemma 1 establishes that f_{TEA} approximates $f_{\text{T-ENS}}$ to first order when $\{\theta_i\}_{i=1}^S$ are close in weight space.

Lemma 1 (TWA and T-ENS). Given $\{\theta_i\}_{i=1}^{S}$ with learning procedures for different temporal experts. Denoting $\Delta_{\{\theta\}} = \max_{i=1}^{S} \|\theta_i - \theta_{TEA}\|_2, \forall (x, y) \in \mathcal{X} \times \mathcal{Y}$:

$$f_{TEA}(x) = f_{T-ENS}(x) + O(\Delta_{\{\theta\}}^2) \qquad (10)$$

$$\ell(f_{TEA}(x), y) = \ell(f_{T-ENS}(x), y) + O(\Delta_{\{\theta\}}^2).$$
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Proof. This proof has two components:

- to establish the functional approximation, it performs Taylor expansion of the models' predictions at the first order.
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- to establish the loss approximation, it performs Taylor expansion of the loss at the first order.

Functional approximation With a Taylor expansion at the first order of the models' predictions w.r.t. parameters θ :

$$f_{\theta_i} = f_{\text{TEA}} + \nabla f|_{\text{TEA}} \Delta_i + O\left(\|\Delta_i\|_2^2\right)$$
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 $f_{\text{T-ENS}} - f_{\text{TEA}}$

=

$$= \sum_{i=1}^{S} \alpha_i \nabla f|_{\text{TEA}} \Delta_i + \sum_{i=1}^{S} \alpha_i O\left(\|\Delta_i\|_2^2\right),$$
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where
$$\Delta_i = \theta_i - \theta_{\text{TWA}}$$
. 1391

Note that unlike in the equal weighting case, we 1392 don't have $\sum_{i=1}^{S} \Delta_i = 0$ for weighted averaging. 1393 Instead, we have $\sum_{i=1}^{S} \alpha_i \Delta_i = 0$. Therefore: 1394

$$f_{\text{T-ENS}} - f_{\text{TEA}}$$
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$$=\sum_{i=1}^{S} \alpha_i \nabla f|_{\text{TEA}} \Delta_i + \sum_{i=1}^{S} \alpha_i O\left(\|\Delta_i\|_2^2\right)$$
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$$= \nabla f|_{\text{TWA}} \sum_{i=1}^{S} \alpha_i \Delta_i + O\left(\sum_{i=1}^{S} \alpha_i \|\Delta_i\|_2^2\right)$$
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$$= O\left(\sum_{i=1}^{S} \alpha_i \|\Delta_i\|_2^2\right)$$
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1399 Since $\Delta_i \leq \Delta_{\{\theta\}}$ for all i, and $\sum_{i=1}^{S} \alpha_i = 1$, we have:

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$$f_{\text{T-ENS}} - f_{\text{TEA}} = O\left(\sum_{i=1}^{S} \alpha_i \Delta_{\{\theta\}}^2\right)$$

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$$= O\left(\Delta_{\{\theta\}}^2 \sum_{i=1}^{n} \alpha_i\right)$$

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$$= O\left(\Delta_{\{\theta\}}^2\right)$$

Loss approximation. With a Taylor expansion at the zeroth order of the loss w.r.t. its first input and injecting the functional approximation:

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$$\ell(f_{\text{T-ENS}}(x); y) = \ell(f_{\text{TWA}}(x); y)$$
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$$+ O(||f_{\text{T-ENS}}(x) - f_{\text{TEA}}(x)||_2)$$

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$$\ell(f_{\text{T-ENS}}(x); y) = \ell(f_{\text{TEA}}(x); y) + O\left(\Delta_{\{\theta\}}^2\right)$$

where

$$\mathcal{B} = \left(\sum_{i=1}^{S} \alpha_i \cdot bias_i\right)^2, \ bias_i = y - \bar{f}_i(x),$$
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$$\mathcal{V} = \sum_{i=1}^{S} \alpha_i^2 \cdot var_i, \ var_i = \mathbb{E}_{l_i} \left[dev_i^2 \right],$$
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$$\mathcal{C} = \sum_{i \neq j} \alpha_i \alpha_j \operatorname{cov}_{i,j}, \ \operatorname{cov}_{i,j} = \mathbb{E}_{\{l_i, l_j\}} \left[\operatorname{dev}_i \cdot \operatorname{dev}_j \right],$$
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with
$$dev_i = f(x, \theta(l_i)) - \bar{f}_i(x),$$
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$$\bar{\Delta}^2 = \mathbb{E}[\Delta_{\{\theta\}}^2] \text{ with } \Delta_{\{\theta\}} = \max_{i=1}^S \|\theta_i - \theta_{TWA}\|_2.$$
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Proof. Following Rame et al. (2022), we use the he bias-variance decomposition in Kohavi et al. (1996) with $f_{\text{T-ENS}} \triangleq \sum_{i=1}^{S} \alpha_i f(\cdot, \theta(l_i))$ to decompose the expected generalization error: 1441

$$\mathbb{E}_{\mathbf{l}}[\mathcal{E}_f(\{\theta(l_i)\}_{i=1}^S)]$$
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$$= \mathbb{E}_f[\operatorname{Bias}\{f_{\text{T-ENS}}|(x,y)\}^2 + \operatorname{Var}\{f_{\text{T-ENS}}|x\}],$$
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where bias term becomes:

C.5 Bias-variance-covariance-locality Decomposition for TEA

We can derive the following decomposition of 1413 TEA's expected test error in the future domain. The 1414 expectation is over the joint distribution describing 1415 the S learning procedures $\{l_i\}_{i=1}^S$. (Note that in 1416 the temporal domain generalization (TDG) setting, 1417 models from different timestamps may have differ-1418 ent biases and variances due to the evolution of 1419 data distributions over time. This temporal hetero-1420 geneity is a key characteristic that distinguishes 1421 TDG from standard DG.) 1422

Proposition 1 (Bias-variance-covariance-locality 1423 decomposition for temporal weight averaging). De-1424 noting $\bar{f}_i(x) = \mathbb{E}_{l_i}[f(x, \theta(l_i))]$ as the expected 1425 prediction of an expert model for timestamp t_i , 1426 $\mathbb{E}_f = \mathbb{E}_{(x,y)\sim p_f}$ and $\mathbf{l} = \{l_1,\ldots,l_S\}$, the ex-1427 pected generalization error on future domain t_f 1428 of $\theta_{TWA} = \sum_{i=1}^{S} \alpha_i \cdot \theta_i$ over the joint distribution 1429 1430 of the learning procedures is:

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$$\mathbb{E}_{\mathbf{l}}[\mathcal{E}_f(\theta_{TEA})] = \mathbb{E}_f\left[\mathcal{B} + \mathcal{V} + \mathcal{C}\right] + O(\bar{\Delta}^2), \quad (11)$$

 $Bias\{f_{T-ENS}|(x,y)\}$ 1445

$$= y - \mathbb{E}_{\mathbf{l}}\left[\sum_{i=1}^{S} \alpha_i f(x, \theta(l_i))\right]$$
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$$= y - \sum_{i=1}^{S} \alpha_i \mathbb{E}_{\mathbf{l}}[f(x, \theta(l_i))]$$
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$$= y - \sum_{i=1}^{S} \alpha_i \bar{f}_i(x)$$
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$$=\sum_{i=1}^{S}\alpha_i(y-\bar{f}_i(x))$$
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$$=\sum_{i=1}^{S} \alpha_i \mathrm{bias}_i(x, y)$$
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Thus, the squared bias term is:

$$\operatorname{Bias}\{f_{\text{T-ENS}}|(x,y)\}^2 = \left(\sum_{i=1}^{S} \alpha_i \operatorname{bias}_i\right)^2$$
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For the variance term, denoting $dev_i = 1453$ $f(x, \theta(l_i)) - \bar{f}_i(x)$, we have: 1454

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$$\begin{aligned} \operatorname{Var} &\{ f_{\text{T-ENS}} | x \} \\ &= \mathbb{E}_{\mathbf{l}} \left[\left(\sum_{i=1}^{S} \alpha_{i} f(x, \theta(l_{i})) - \mathbb{E}_{\mathbf{l}} \left[\sum_{i=1}^{S} \alpha_{i} f(x, \theta(l_{i})) \right] \right) \\ &= \mathbb{E}_{\mathbf{l}} \left[\left(\sum_{i=1}^{S} \alpha_{i} (f(x, \theta(l_{i})) - \bar{f}_{i}(x)) \right)^{2} \right] \\ &= \mathbb{E}_{\mathbf{l}} \left[\sum_{i=1}^{S} \sum_{j=1}^{S} \alpha_{i} \alpha_{j} \cdot \operatorname{dev}_{i} \cdot \operatorname{dev}_{j} \right] \\ &= \sum_{i=1}^{S} \alpha_{i}^{2} \mathbb{E}_{\mathbf{l}} [\operatorname{dev}_{i}^{2}] + \sum_{i \neq j} \alpha_{i} \alpha_{j} \mathbb{E}_{\mathbf{l}} [\operatorname{dev}_{i} \cdot \operatorname{dev}_{j}] \\ &= \sum_{i=1}^{S} \alpha_{i}^{2} \operatorname{var}_{i} + \sum_{i \neq j} \alpha_{i} \alpha_{j} \operatorname{cov}_{i,j} \end{aligned}$$

1456i=1 $i \neq j$ 1456Combination with Lemma 1 We recall that per1457our adapted Lemma 1:

$$\ell(f_{\mathsf{TEA}}(x), y) = \ell(f_{\mathsf{T-ENS}}(x), y) + O(\Delta^2_{\{\theta\}}).$$

Taking the expectation over the learning procedures and combining all terms:

1461
$$\mathbb{E}[\mathcal{E}_f(\theta_{\text{TEA}})] = \mathbb{E}_f \left[\left(\sum_{i=1}^{S} \alpha_i \text{bias}_i \right)^2 \right] + \mathbb{E}_f \left[\sum_{i=1}^{S} \alpha_i^2 \text{var}_i \right]$$

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$$+ \mathbb{E}_{f} \left[\sum_{i=1}^{m} \alpha_{i}^{-} \operatorname{var}_{i} \right]$$
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$$+ \mathbb{E}_{f} \left[\sum_{i \neq j} \alpha_{i} \alpha_{j} \operatorname{cov}_{i,j} \right]$$

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C.6 Theoretical Insights for TEA

From Equation 11, we can see that generalization error can be reduced by minimizing bias \mathcal{B} , variance \mathcal{V} , covariance \mathcal{C} , and locality $\overline{\Delta}^2$. However, due to the complexity of real-world data and models, finding an optimal analytical solution is nearly impossible. Nevertheless, similar to Rame et al. (2022), we can derive practical insights for designing TEA by analyzing the relationships between these four terms, model properties, and averaging coefficients.

 $+ O(\bar{\Delta}^2)$

1477Insight 1 Tradeoff between Functional Diversity1478and Parameter Similarity among Experts. Covari-1479ance C reduction necessitates functional diversity1480among experts, while the locality constraint $\overline{\Delta}^2$ 1481demands parameter similarity among experts.

The covariance term increases when the predictions of $\{f(\cdot, \theta(l_i))\}_{i=1}^S$ are correlated, suggesting

that DiWA's (Rame et al., 2022) approach to reduce covariance by encouraging functional diversity remains effective. However, the locality term $\overline{\Delta}^2$ simultaneously constrains the weights to remain close in parameter space. This tradeoff suggests that when training these expert models, we should find an appropriate balance between encouraging diverse predictions and maintaining parameter similarity. 1484

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Insight 2 Tradeoff between Bias and Variance via Averaging Coefficients. Reducing variance V requires averaging weights evenly, while reducing bias \mathcal{B} demands concentrating coefficients on experts with lower bias magnitudes on future data.

Insight 2 is obtained by introducing 2 assumptions specific to the TDG for further discussion about bias and variance.

Assumption 1 (Ordered Bias Magnitudes). The models can be ordered by expected bias magnitudes on future domains such that $\mathbb{E}_f \left[bias_{m_1}^2 \right] \geq \mathbb{E}_f \left[bias_{m_1}^2 \right] \geq \cdots \geq \mathbb{E}_f \left[bias_{m_S}^2 \right]$, with $\{m_j\}_{j=1}^S$ being a permutation of $\{i\}_{i=1}^S$.

Assumption 2 (Equal Variance Experts). The variance of each expert's prediction is equal across all experts, such that $\mathbb{E}_f[var_i] = v$ for all $i \in \{1, 2, ..., M\}$.

Lemma 2 (Optimal Averaging Coefficients for Bias Minimization). Let the bias of model i be:

$$b_i(x,y) = \operatorname{bias}_i(x,y), \sigma_i^2 := \mathbb{E}_f\left[b_i^2\right],$$
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and define the root-mean-square magnitude:

$$\sigma_i = \sqrt{\sigma_i^2} \quad (i = 1, \dots, S).$$
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According to Assumption 1, magnitudes are ordered $\sigma_{m_1} \ge \sigma_{m_2} \ge \cdots \ge \sigma_{m_S}$, where $\{m_j\}_{j=1}^S$ is a permutation of $\{1, \ldots, S\}$. For convex weights $\boldsymbol{\alpha} \in \Delta^S := \{\alpha_i \ge 0, \sum_{i=1}^S \alpha_i = 1\}$, consider the combined bias loss:

$$L(\boldsymbol{\alpha}) := \mathbb{E}_f \left[\left(\sum_{i=1}^{S} \alpha_i b_i \right)^2 \right].$$
(12)

If **no** information is available on the pairwise bias covariances $\Sigma_{ij} := \mathbb{E}_f[b_ib_j], (i \neq j)$, then the minimax problem:

$$\min_{\boldsymbol{\alpha} \in \Delta^S} \max_{\Sigma \text{ s.t. } \operatorname{diag}(\Sigma) = \boldsymbol{\sigma}^2} L(\boldsymbol{\alpha})$$
(13) 1524

is solved by:

$$\alpha_{m_S}^{\star} = 1, \quad \alpha_i^{\star} = 0 \text{ for } i \neq m_S$$
 (14) 1526

with $L(\boldsymbol{\alpha}^{\star}) = \sigma_{m_S}^2$. 1527

1528Proof. We can write $L(\alpha) = \alpha^{\top} \Sigma \alpha$ with un-1529known positive-semidefinite matrix Σ satisfying1530 $\Sigma_{ii} = \sigma_i^2$. By the Cauchy-Schwarz inequality,1531 $|\Sigma_{ij}| \leq \sigma_i \sigma_j$. The worst case occurs when all1532covariances reach the extreme value $\Sigma_{ij} = \sigma_i \sigma_j$,1533yielding:

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$$\max_{\Sigma} L(\boldsymbol{\alpha}) = \left(\sum_{i=1}^{S} \alpha_i \sigma_i\right)^2.$$
(15)

Since $\sum_{i} \alpha_i \sigma_i$ is a convex combination of the ordered set $\{\sigma_{m_j}\}$, its minimum over the simplex Δ^S is attained by placing all weight on the smallest RMS magnitude σ_{m_S} , which gives the stated α^* and the minimax value $L(\alpha^*) = \sigma_{m_S}^2$.

Lemma 3 (Optimal Averaging Coefficients for Variance Minimization). Consider the variance term with equal variances $\mathbb{E}_f[var_i] = v$ for all $i \in \{1, ..., S\}$:

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$$\mathbb{E}_f\left[\mathcal{V}\right] = v \sum_{i=1}^{S} \alpha_i^2. \tag{16}$$

1545 For averaging coefficients $\alpha \in \Delta^S := \{\alpha_i \geq 0, \sum_{i=1}^{S} \alpha_i = 1\}$, the variance term is minimized 1547 when weights are distributed equally across all 1548 models:

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$$\alpha_i^{\star} = \frac{1}{S} \text{ for all } i \tag{17}$$

1550 with optimal variance $v \cdot \frac{1}{S}$.

1551 *Proof.* We seek to minimize $\sum_{i=1}^{S} \alpha_i^2$ subject to 1552 the constraints $\sum_{i=1}^{S} \alpha_i = 1$ and $\alpha_i \ge 0$. By the 1553 Cauchy-Schwarz inequality:

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$$\left(\sum_{i=1}^{S} \alpha_i\right)^2 \le S \sum_{i=1}^{S} \alpha_i^2, \tag{18}$$

1555 with equality if and only if all α_i are equal. Since 1556 $\sum_{i=1}^{S} \alpha_i = 1$, we have:

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$$1 = \left(\sum_{i=1}^{S} \alpha_i\right)^2 \le S \sum_{i=1}^{S} \alpha_i^2, \qquad (19)$$

1558 which implies $\sum_{i=1}^{S} \alpha_i^2 \ge \frac{1}{S}$. Equality is achieved 1559 when $\alpha_i = \frac{1}{S}$ for all *i*, giving the optimal solution. 1560 In summary, Lemma 2 indicates that optimizing the bias term requires concentrating weight on experts with smaller bias magnitude on future domains, while Lemma 3 suggests that minimizing variance requires the opposite approach—distributing weight as evenly as possible across all experts. This creates a fundamental tradeoff between bias and variance in the selection of averaging coefficients. 1561

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Discussion about Assumptions. Assumption 1 is similar to the smooth distribution shift assumption used by most prior TDG methods (ying Bai et al., 2022; Zeng et al., 2023; Nasery et al., 2021; Xie et al., 2024b,c), allowing us to model distribution change and leverage temporal information to predict future parameter or feature. Assumption 2 is reasonable when all experts share the same architecture, optimization procedure and hyperparameters, differing only in the specific temporal domains they've been optimized to excel in.

D Additional Results

We show the coefficients vs. D_{S+1} accuracy across 1582 all benchmarks in Figure 6. 1583



Figure 6: Visualization of averaging coefficients and accuracies of experts on target domain D_{S+1} .