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# Ambient Diffusion mni: Training Good Models with Bad Data

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## Abstract

1 We show how to use low-quality, synthetic, and out-of-distribution images to  
2 improve the quality of a diffusion model. Typically, diffusion models are trained  
3 on curated datasets that emerge from highly filtered data pools from the Web and  
4 other sources. We show that there is immense value in the lower-quality images  
5 that are often discarded. We present Ambient Diffusion Omni, a simple, principled  
6 framework to train diffusion models that can extract signal from all available images  
7 during training. Our framework exploits two properties of natural images – spectral  
8 power law decay and locality. We first validate our framework by successfully  
9 training diffusion models with images synthetically corrupted by Gaussian blur,  
10 JPEG compression, and motion blur. We then use our framework to achieve state-  
11 of-the-art ImageNet FID and we show significant improvements in both image  
12 quality and diversity for text-to-image generative modeling. The core insight is  
13 that noise dampens the initial skew between the desired high-quality distribution  
14 and the mixed distribution we actually observe. We provide rigorous theoretical  
15 justification for our approach by analyzing the trade-off between learning from  
16 biased data versus limited unbiased data across diffusion times.

## 1 **Introduction**

18 Large-scale, high-quality training datasets have been a primary driver of recent progress in generative  
19 modeling. These datasets are typically assembled by filtering massive collections of images sourced  
20 from the web or proprietary databases [25, 43, 53, 58, 59]. The filtering process is crucial to the  
21 quality of the resulting models [13, 27, 25, 32, 27]. However, filtering strategies are often heuristic  
22 and inefficient, discarding large amounts of data [51, 43, 25, 13]. We demonstrate that the data  
23 typically rejected as low-quality holds significant, underutilized value.

24 Extracting meaningful information from degraded data requires algorithms that explicitly model the  
25 degradation process. In generative modeling, there is growing interest in approaches that learn to  
26 generate directly from degraded inputs [18, 17, 14, 15, 7, 47, 39, 52, 5, 1, 2, 55, 71, 46, 64, 45,  
27 11, 48]. A key limitation of existing methods is their reliance on knowing the exact form of the  
28 degradation. In real-world scenarios, image degradations—such as motion blur, sensor artifacts,  
29 poor lighting, and low resolution—are often complex and lack a well-defined analytical description,  
30 making this assumption unrealistic. Even within the same dataset, from ImageNet to internet scale  
31 text-to-image datasets, there are samples of varying qualities [28], as shown in Figures 3, 24, 27,  
32 25. Given access to this mixed-bag of datapoints, we would like to sample from a tilted continuous  
33 measure of high-quality images, without sacrificing the diversity present in the training points.

34 The training objective of diffusion models naturally decomposes sampling from a target distribution  
35 into a sequence of supervised learning tasks [30, 61, 62, 16, 19, 9, 10]. Due to the power-law structure

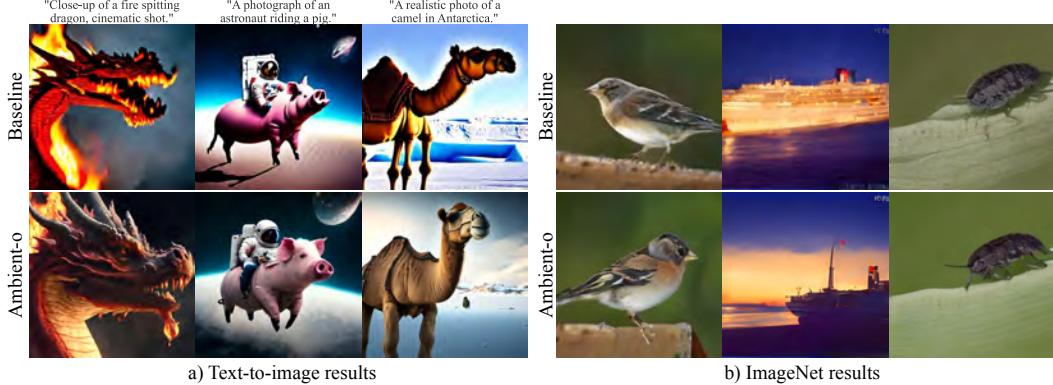


Figure 1: Effect of using Ambient-o for (a) training a text-to-image model (Micro-Diffusion [54]) and (b) a class-conditional model for ImageNet (EDM-2 [35]). All generations are initialized with the same noise. The baseline models are trained using all the data equally. Ambient-o changes the way the data is used during the diffusion process based on its quality. This leads to significant visual improvements without sacrificing diversity, as would happen with a filtering approach (see Fig. 29).

36 of natural image spectra [65], high diffusion times focus on generating globally coherent, semantically  
 37 meaningful content [22], while low diffusion times emphasize learning high-frequency details.  
 38 Our first key theoretical insight is that low-quality samples can still be valuable for training in the  
 39 high-noise regime. As noise increases, the diffusion process contracts distributional differences (see  
 40 Theorem B.2), reducing the mismatch between the high-quality target distribution and the available  
 41 mixed-quality data. At the same time, incorporating low-quality data increases the sample size,  
 42 reducing the variance of the learned estimator. Our analysis formalizes this bias-variance trade-off  
 43 and motivates a principled algorithm for training denoisers at high diffusion times using noisy,  
 44 heterogeneous data.  
 45 For low diffusion times, our algorithm leverages a second key property of natural images: locality. We  
 46 show a direct relationship between diffusion time and the optimal receptive field size for denoising.  
 47 Specifically, small image crops suffice at lower noise levels. This allows us to borrow high-frequency  
 48 details from out-of-distribution or synthetic images, as long as the marginal distributions of the crops  
 49 match those of the target data.  
 50 We introduce Ambient Diffusion Omni (Ambient-o), a simple and principled framework for training  
 51 diffusion models using arbitrarily corrupted and out-of-distribution data. Rather than filtering samples  
 52 based on binary ‘good’ or ‘bad’ labels, Ambient-o retains all data and modulates the training process  
 53 according to each sample’s utility. This enables the model to generate diverse outputs without  
 54 compromising image quality. Empirically, Ambient-o advances the state of the art in unconditional  
 55 generation on ImageNet and enhances diversity in text-conditional generation without sacrificing  
 56 fidelity. Theoretically, it achieves improved bounds for distribution learning by optimally balancing  
 57 the bias-variance trade-off: low-quality samples introduce bias, but their inclusion reduces variance  
 58 through increased sample size.

## 59 2 Background and Related Work

60 **Diffusion Modeling.** Diffusion models transform the problem of sampling from  $p_0$  into the problem  
 61 of learning *denoisers* for smoothed versions of  $p_0$  defined as  $p_t = p_0 \circledast \mathcal{N}(0, \sigma^2(t)\mathbf{I})$ . We typically  
 62 denote with  $X_0 \sim p_0$  the R.V. distributed according to the distribution of interest and  $X_t =$   
 63  $X_0 + \sigma(t)Z$ , the R.V. distributed according to  $p_t$ . The target is to estimate the set of optimal  $l_2$   
 64 denoisers, i.e., the set of the conditional expectations:  $\{\mathbb{E}[X_0|X_t = \cdot]\}_{t=1}^T$ . Typically, this can be  
 65 achieved through supervised learning by minimizing the following loss (or a re-parametrization of it):

$$J(\theta) = \mathbb{E}_{t \in \mathcal{U}[0, T]} \mathbb{E}_{x_0, x_t|t} \left[ \|h_\theta(x_t, t) - x_0\|^2 \right], \quad (2.1)$$

66 that is optimized over a function family  $\mathcal{H} = \{h_\theta : \theta \in \Theta\}$  parametrized by network parameters  $\theta$ .  
 67 For sufficiently expressive families, the minimizer is indeed:  $h_{\theta^*}(x, t) = \mathbb{E}[X_0|X_t = x]$ .

68 **Learning from noisy data.** The diffusion modeling framework described above assumes access  
 69 to samples from the distribution of interest  $p_0$ . An interesting variation of this problem is to learn  
 70 to sample from  $p_0$  given access to samples from a tilted measure  $\tilde{p}_0$  and a known degradation  
 71 model. In Ambient Diffusion [18], the goal is to sample from  $p_0$  given pairs  $(Ax_0, A)$  for a matrix  
 72  $A : \mathbb{R}^{m \times n}$ ,  $m < n$ , that is distributed according to a known density  $p(A)$ . The techniques in this  
 73 work were later generalized to accommodate additive Gaussian Noise [15, 17, 1] in the measurements.  
 74 More recently there have been efforts to further broaden the family of degradation models considered  
 75 through Expectation-Maximization approaches that involve multiple training runs [52, 5].

76 Recent work from [17] has shown that, at least for the Gaussian corruption model, leveraging the  
 77 low-quality data can tremendously increase the performance of the trained generative models. In  
 78 particular, the authors consider the setting where we have access to a few samples from  $p_0$ , let's  
 79 denote them  $\mathcal{D}_0\{x_0^{(i)}\}_{i=1}^{N_1}$  and many samples from  $p_{t_n}$ , let's denote them  $\mathcal{D}_{t_n}\{x_{t_n}^{(i)}\}_{i=1}^{N_2}$ , where  
 80  $p_{t_n} = p_0 \circledast \mathcal{N}(0, \sigma^2(t_n)\mathbf{I})$  is a smoothed version of  $p_0$  at a known noise level  $t_n$ . The clean samples  
 81 are used to learn denoisers for all noise levels  $t \in [0, T]$  while the noisy samples are used to learn  
 82 denoisers only for  $t \geq t_n$ , using the training objective:

$$J_{\text{ambient}}(\theta) = \mathbb{E}_{t \in \mathcal{U}(t_n, T)} \sum_{i=1}^{N_2} \mathbb{E}_{x_t | x_{t_n}^{(i)}} \left[ \left\| \alpha(t)h_\theta(x_t, t) + (1 - \alpha(t))x_t - x_{t_n}^{(i)} \right\|^2 \right], \quad (2.2)$$

83 with  $\alpha(t) = \frac{\sigma^2(t) - \sigma^2(t_n)}{\sigma^2(t)}$ . Note that the objective of equation 2.2 only requires samples from  $p_{t_n}$   
 84 (instead of  $p_0$ ) and can be used to train for all times  $t \geq t_n$ . This algorithm uses  $N_1 + N_2$  datapoints  
 85 to learn denoisers for  $t > t_n$  and only  $N_1$  datapoints to learn denoisers for  $t \leq t_n$ . The authors show  
 86 that even for  $N_1 \ll N_2$ , the model performs similarly to the setting of training with  $(N_1 + N_2)$   
 87 clean datapoints. The main limitation of this method and its related works is that the degradation  
 88 process needs to be known. However, in many applications, we have data from heterogeneous sources  
 89 and various qualities, but there is no analytic form or any prior on the corruption model.

90 **Data filtering.** One of the most crude, but widely used, approaches for dealing with heterogeneous  
 91 data sources is to remove the low-quality data and train only the high-quality subset [43, 25, 23].  
 92 While this yields better results than naively training on the entire distribution, it leads to a decrease in  
 93 diversity and relies on heuristics for optimizing the filtering. An alternative strategy is to train on the  
 94 entire distribution and then fine-tune on high-quality data [13, 54]. This approach better trades the  
 95 quality-diversity trade-off but still incurs a loss of diversity and is hard to calibrate.

96 **Training with synthetic data.** A lot of recent works have shown that synthetic data can improve the  
 97 generative capabilities of diffusion models when mixed properly with real data from the distribution  
 98 of interest [24, 3, 4]. In this work, we show that it helps significantly to view synthetic data as  
 99 corrupted versions of the samples from the real distribution and incorporate this perspective into the  
 100 training objective.

### 101 3 Method

102 We propose a new framework that extends beyond [17] to enable training generative models directly  
 103 from arbitrarily corrupted and out-of-distribution data, without requiring prior knowledge of the  
 104 degradation process. We begin by formalizing the setting of interest.

105 **Problem Setting.** We are given a dataset  $\mathcal{D} = \{w_0^{(i)}\}_{i=1}^N$  consisting of  $N$  datapoints. Each point  
 106 in  $\mathcal{D}$  is drawn from a mixture distribution  $\tilde{p}_0$ , which mixes  $p_0$  (the distribution of interest) and an  
 107 alternative distribution  $q_0$  that may contain various forms of degradation or out-of-distribution content.  
 108 We assume access to two labeled subsets,  $S_G, S_B$ , where points in  $S_G$  are known to come from the  
 109 clean distribution  $p_0$ , and points in  $S_B$  from the corrupted distribution  $q_0$ . While this assumption  
 110 simplifies the initial exposition, we relax it in Section G.1. We focus on the practically relevant  
 111 regime where  $|S_G| \ll |\mathcal{D}|$ —i.e., access to high-quality data is severely limited. The objective is to  
 112 learn a generative model that (approximately) samples from the clean distribution  $p_0$ , leveraging both  
 113 clean and corrupted samples in its training.

114 We now describe how degraded and out-of-distribution samples can be effectively leveraged during  
 115 training in both the high-noise and low-noise regimes of the diffusion process.

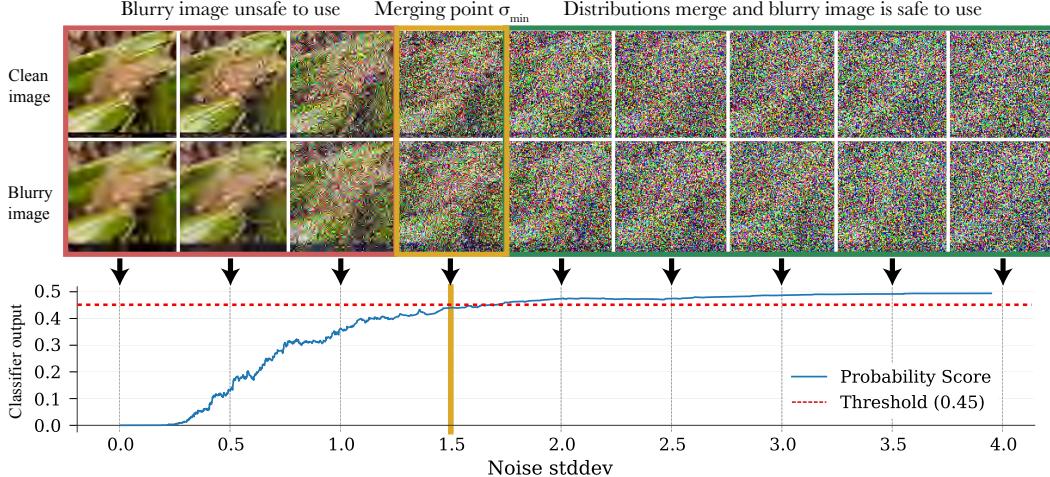


Figure 2: **A time-dependent classifier trained to distinguish noisy clean and blurry images** (blur kernel standard deviation  $\sigma_B = 0.6$ ). At low noise the classifier is able to perfectly identify the blurry images, and outputs a probability close to 0. As the noise increases and the information in the image is destroyed, the clean and blurry distributions converge and the classifier outputs a prediction close to 0.5. The red line plots the threshold (selected at  $\tau = 0.45$ ), which is crossed at  $\sigma_t = 1.64$ .

116 **3.1 Learning in the high-noise regime (leveraging low-quality data)**

117 **Addition of gaussian noise contracts distribution distances.** The first key idea of our method is  
 118 that, at high diffusion times  $t$ , the noised target distribution  $p_t$  and the noised corrupted distribution  
 119  $\tilde{p}_t$  become increasingly similar (Theorem B.2), effectively attenuating the discrepancy introduced  
 120 by corruption. This effect is illustrated in Figure 2 (top), where we compare a clean image and its  
 121 degraded counterpart (in this case, corrupted by Gaussian blur). As the diffusion time  $t$  increases, the  
 122 noised versions of both samples become visually indistinguishable. Consequently, samples from  $\tilde{p}_0$   
 123 can be leveraged to learn (the score of)  $p_t$ , for  $t > t_n^{\min}$ . We formalize this intuition in Section B, and  
 124 we also quantify that for large  $t$  there are statistical efficiency benefits for using a large sample from  
 125  $\tilde{p}_0$  versus a small sample from  $p_0$ .

126 **Heuristic selection of the noise level.** From the discussion so far, it follows that to use samples  
 127 from  $\tilde{p}_0$ , we need to assign them to a noise level  $t_n^{\min}$ . One can select this noise level empirically,  
 128 i.e. we can ablate this parameter by training different models and selecting the one that maximizes  
 129 the generative performance. However, this approach requires multiple trainings, which can be costly.  
 130 Instead, we can find the desired noise level in a principled way as detailed below.

131 **Training a classifier under additive Gaussian noise.** To identify the appropriate noise level, we  
 132 train a time-conditional classifier to distinguish between the noised distributions  $p_t$  and  $q_t$  across  
 133 various diffusion times  $t$ . We use a single neural network  $c_\theta^{\text{noise}}(x_t, t)$  that is conditioned on the  
 134 diffusion time  $t$ , following the approach of time-aware classifiers used in classifier guidance [21].  
 135 The classifier is trained using labeled samples from  $S_G$  (clean) and  $S_B$  (corrupted) via the following  
 136 objective:

$$J_{\text{noise}}(\theta) = \sum_{x_0 \in S_G} \mathbb{E}_{x_t|x_0} [-\log c_\theta^{\text{noise}}(x_t, t)] + \sum_{y_0 \in S_B} \mathbb{E}_{y_t|y_0} [-\log(1 - c_\theta^{\text{noise}}(y_t, t))] \quad (3.1)$$

137 **Annotation.** Once the classifier is trained, we use it to determine the minimal level of noise that must  
 138 be added to the low-quality distribution  $q_0$  so that it closely approximates a smoothed version of the  
 139 high-quality distribution  $p_0$ . Formally, we compute:

$$t_n^{\min} = \inf \left\{ t \in [0, T] : \frac{1}{|S_B|} \sum_{y_0 \in S_B} \mathbb{E}_{y_t|y_0} [c_\theta^{\text{noise}}(y_t, t)] > \tau \right\}, \quad (3.2)$$

140 for  $\tau = 0.5 - \epsilon$  and for some  $\epsilon > 0$ . Subsequently, we form the annotated dataset  $\mathcal{D}_{\text{annot}} =$   
 141  $\{(w_0^{(i)} + \sigma_{t_n^{\min}} Z^{(i)}, t_n^{\min})\}_{i=1}^N \cup \{(x_0, 0) | x_0 \in S_G\}$ , where the random variables  $Z^{(i)}$  are i.i.d. standard

142 normals. In particular, our annotated dataset indicates that we should only use the samples from  $\mathcal{D}$   
 143 for diffusion times  $t \geq t_n^{\min}$ , for which the distributions have approximately merged and hence it is  
 144 safe to use them. In fact, the optimal classifier assigns time  $t_n$  that corresponds to the first time for  
 145 which  $d_{\text{TV}}(p_t, q_t) \leq \epsilon$ .

146 **From arbitrary corruption to additive Gaussian noise.** The afore-described approach reduces  
 147 our problem of learning from data with arbitrary corruption to the setting of learning from data  
 148 corrupted with additive Gaussian noise. The price we pay for this reduction is the information loss  
 149 due to the extra noise we add to the samples during the annotation stage. We can now extend the  
 150 objective function (2.2) to train our diffusion model. Suppose our annotated dataset is comprised of  
 151 samples  $\{(x_{t_i^{\min}}^{(i)}, t_i^{\min})\}$ . Then our objective becomes:

$$J_{\text{ambient-o}}(\theta) = \mathbb{E}_{t \in \mathcal{U}[0, T]} \sum_{i: t_i^{\min} < t} \mathbb{E}_{x_t | x_{t_i^{\min}}^{(i)}} \left[ \left\| \alpha(t, t_i^{\min}) h_{\theta}(x_t, t) + (1 - \alpha(t, t_i^{\min})) x_t - x_{t_i^{\min}}^{(i)} \right\|^2 \right],$$

152 where  $\alpha(t, t_i^{\min}) = \frac{\sigma^2(t) - \sigma^2(t_i^{\min})}{\sigma^2(t)}$ .

153 Moreover, the method is particularly well-suited to certain types of corruptions but is less effective  
 154 for others. Because the addition of Gaussian noise suppresses high-frequency components—due  
 155 to the spectral power law of natural images—our approach is most effective for corruptions that  
 156 primarily degrade high frequencies (e.g., blur). In contrast, degradations that affect low-frequency  
 157 content—such as color shifts, contrast reduction, or fog-like occlusions—are more challenging. This  
 158 limitation is illustrated in Figure 9: masked images, for example, require significantly more noise to  
 159 become usable compared to high-frequency corruptions like blur. In the extreme, the method reduces  
 160 to a filtering approach, as infinite noise nullifies all information in the corrupted samples.

### 161 3.2 Learning in the low-noise regime (synthetic and out-of-distribution data)

162 So far, our algorithm implicitly results in varying amounts of training data across diffusion noise  
 163 levels. At high noise, the model can leverage abundant low-quality data, whereas at low noise levels,  
 164 it must rely solely on the limited set of high-quality samples. We now extend the algorithm to enable  
 165 the use of synthetic and out-of-distribution data for learning denoisers at low-noise diffusion times.

166 To achieve this, we leverage another fundamental property of natural images: *locality*. At low  
 167 diffusion times, the denoising task can be solved using only a small local region of the image, without  
 168 requiring full spatial context. We validate this hypothesis experimentally in the Experiments Section  
 169 (Figures 11, 12, 13, 14), where we show that there is a mapping between diffusion time  $t$  and the  
 170 crop size needed to perform the denoising optimally at this diffusion time. Intuitively, the higher the  
 171 noise, the more context is required to accurately reconstruct the image. Conversely, for lower noise,  
 172 the local information within a small neighborhood suffices to achieve effective denoising. We use  
 173  $\text{crop}(t)$  to denote the minimal crop size needed to perform optimal denoising at time  $t$ . If there are  
 174 two distributions  $p_0$  and  $\tilde{p}_0$  that agree on their marginals (i.e. crops), they can be used interchangeably  
 175 for low-diffusion times. Note that the distributions don't have to agree globally, they only have to  
 176 agree on a local (patch) level. Formally, let  $A(t)$  be a random patch selector of size  $\text{crop}(t)$ . Let also  
 177  $p_0, \tilde{p}_0$  two distributions that satisfy:

$$A(t) \# p_0 = A(t) \# \tilde{p}_0, \quad (3.3)$$

178 where  $A(t) \# p_0$  denotes the pushforward measure<sup>1</sup> of  $p_0$  under  $A(t)$ . Then, the cropped portions  
 179 of the tilted distributions provide equivalent information to the crops of the original distribution for  
 180 denoising.

181 **Training a crops classifier.** Note that the condition of Equation (3.3) can be trivially satisfied if  $A(t)$   
 182 masks all the pixels or even if  $A(t)$  just selects a single pixel. We are interested in finding what is  
 183 the maximum crop size for which this condition is approximately true. Once again, we can use a  
 184 classifier to solve this task. The input to the classifier,  $c_{\theta}^{\text{crops}}$ , is a crop of an image that either arises  
 185 from  $p_0$  or  $\tilde{p}_0$ , and the classifier needs to classify between these two cases.

<sup>1</sup>Given measure spaces  $(X_1, \Sigma_1)$  and  $(X_2, \Sigma_2)$ , a measurable function  $f : X_1 \rightarrow X_2$ , and a probability  
 measure  $p : \Sigma_1 \rightarrow [0, \infty)$ , the pushforward measure  $f \# p$  is defined as  $(f \# p)(B) := p(f^{-1}(B)) \forall B \in \Sigma_2$ .

186 **Annotation and training using the trained classifier.** Once the classifier is trained, we are now  
 187 interested in finding the biggest crop size for which the distributions  $p_0, \tilde{p}_0$  cannot be confidently  
 188 distinguished. Formally,

$$t_n^{\max} = \sup \left\{ t \in [0, T] : \frac{1}{|S_B|} \sum_{y_0 \in S_B} [c_{\theta}^{\text{crops}}(A(t)(y_t))] > \tau \right\}, \quad (3.4)$$

189 for  $\tau = 0.5 - \epsilon$  and for some small  $\epsilon > 0$ <sup>2</sup>. For times  $t \leq t_n^{\max}$ , the out-of-distribution images from  
 190  $\tilde{p}_0$  can be used with the regular diffusion objective as images from  $p_0$ , as for these times the denoiser  
 191 only looks at crops and at the crop level the distributions have converged.

192 **The donut paradox.** Each sample can be used for  $t \geq t_i^{\min}$  and for  $t \leq t_i^{\max}$ , but not for  $t \in$   
 193  $(t_i^{\max}, t_i^{\min})$ . We call this the *donut paradox* as there is a hole in the middle of the diffusion trajectory  
 194 for which we have fewer available data. These times do not have enough noise for the distributions  
 195 to merge globally, but also the required receptive field for denoising is big enough so that there are  
 196 differences on a crop level. We show an example of this effect in Figure 10.

Table 1: ImageNet results with and without classifier-free guidance.

ImageNet-512	Train FID ↓				Test FID ↓				Model Size	
	FID		FIDv2		FID		FIDv2			
	no CFG	w/ CFG	no CFG	w/ CFG	no CFG	w/ CFG	no CFG	w/ CFG	Mparams	NFE
EDM2-XS	<b>3.57</b>	2.91	<b>103.39</b>	79.94	3.77	3.68	115.16	93.86	125	63
Ambient-o-XS	3.59	<b>2.89</b>	107.26	<b>79.56</b>	<b>3.69</b>	<b>3.58</b>	<b>115.02</b>	<b>92.96</b>	125	63
EDM2-XXL	1.91 (1.93)	1.81	42.84	33.09	2.88	2.73	56.42	46.22	1523	63
Ambient-o-XXL	1.99	1.87	43.38	33.34	2.81	2.68	56.40	46.02	1523	63
Ambient-o-XXL+crops	<b>1.91</b>	<b>1.80</b>	<b>42.84</b>	<b>32.63</b>	<b>2.78</b>	<b>2.53</b>	<b>56.39</b>	<b>45.78</b>	1523	63

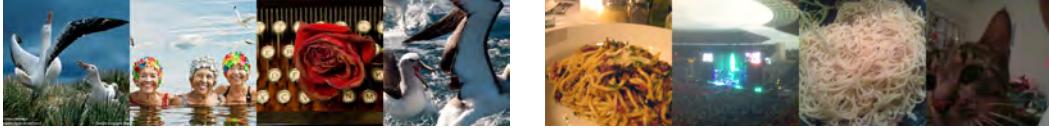


Figure 3: Results using CLIP to obtain the high-quality and the low-quality sets of ImageNet.

## 197 4 Experiments

198 **Controlled experiments to show utility from low-quality data.** To verify our method, we first  
 199 do synthetic experiments on artificially corrupted data. We use EDM [34] as our baseline, and we  
 200 train networks on CIFAR-10 and FFHQ. For the first experiments, we only use the high-noise part of  
 201 our Ambient-o method (Section 3.1). We underline that for all of our experiments, we only change  
 202 the way we use the data, and we keep all the optimization and network hyperparameters as is. We  
 203 compare against using all the data as equal (despite the corruption) and the filtering strategy of  
 204 only training on the clean samples. For evaluation, we measure FID [29] with respect to the full  
 205 uncorrupted dataset (which is not available during training).

206 For the blurring experiments, we use a Gaussian kernel with standard deviation  $\sigma_B =$   
 207  $0.4, 0.6, 0.8, 1.0$ , and we corrupt 90% of the data. We show some corrupted images in Appendix  
 208 Figure 5a. To obtain annotations, we train a blurry vs clean image classifier under noise, as explained  
 209 in Section 3.1. For the experiments in the main paper, we use a balanced dataset for the training  
 210 of the classifier. We ablate the effect of having fewer training samples for the classifier training in  
 211 Appendix Section F where we show that reducing the number of clean samples available for classifier  
 212 training leads to a small drop in performance. Once equipped with the trained classifier, each sample  
 213 is annotated on its own based on the amount of noise that is needed to confuse the classifier (sample  
 214 dependent annotation). We present our results in Table 2a. As shown, for all corruption strengths,  
 215 Ambient Omni, significantly outperforms the two baseline methods. In the one to the last column of  
 216 Table 2a, we further show the average annotation of the classifier. As expected, the average assigned  
 217 noise level increases as the corruption intensifies.

<sup>2</sup>We subtract an  $\epsilon$  to allow for approximate mixing of the two distributions and hence smaller annotation times.

Table 2: In a controlled experiment with restricted access only to 10% of the clean dataset, our method of Ambient-o uses corrupted and out-of-distribution data to improve performance.

(a) Gaussian blurred data at different levels.				(b) Additional out-of-distribution data.				
Method	Parameters Values ( $\sigma_B$ )	$\bar{\sigma}_{t_n}^{\min}$	FID	Source Data	Additional Data	Method	$\bar{\sigma}_{t_n}^{\max}$	FID
<b>Only Clean (10%)</b>	-	-	8.79	Dogs (10%)	None	-	-	12.08
<b>All data</b>	1.0	45.32			Cats	Fixed $\sigma$	0.2	11.14
	0.8	28.26			Cats	Fixed $\sigma$	0.1	9.85
	0.6	11.42			Cats	Fixed $\sigma$	0.05	10.66
	0.4	2.47			Cats	Fixed $\sigma$	0.025	12.07
<b>Ambient-o</b>	1.0	2.84	<b>6.16</b>	Cats (10%)	Cats	Classifier	0.09	<b>8.92</b>
	0.8	1.93	<b>6.00</b>		Procedural	Classifier	0.042	<b>10.98</b>
	0.6	1.38	<b>5.34</b>	Cats (10%)	None	-	-	5.20
	0.4	0.22	<b>2.44</b>		Dogs	Classifier	0.13	5.11
					Wildlife	Classifier	0.08	<b>4.89</b>

218 **Controlled experiments to show utility from out-of-distribution images.** We now want to validate  
 219 the method developed in Section 3.2 for leveraging out-of-distribution data. To start with, we want to  
 220 find the mapping between diffusion times and the size of the receptive field required for an optimal  
 221 denoising prediction. To do so, we take a pre-trained denoising diffusion model and measure the  
 222 denoising loss at a given location as we increase the size of the context. We provide the corresponding  
 223 plot in the Supplemental Figures 13, 11. The main finding is that while providing more context  
 224 always leads to a decrease in the average loss, for sufficiently small noise levels, the loss nearly  
 225 plateaus before the full image context is provided. That implies that the perfect denoiser for a given  
 226 noise level only needs to look at a localized part of the image.

227 Equipped with the mapping between diffusion times and crop sizes, we now proceed to a fun  
 228 experiment. Specifically, we show that it is possible to use images of cats to improve a generative  
 229 model for dogs (!) and vice-versa. The cats here represent out-of-distribution data that can be used  
 230 to improve the performance in the distribution of interest (in our toy example, dogs distribution).  
 231 To perform this experiment, we train a classifier that discriminates between cats and dog images by  
 232 looking at crops of various sizes (Section 3.2). Figure 18 shows the predictions of an  $8 \times 8$  crops-  
 233 classifier for an image of a cat, illustrating that there are a number of crops that are misclassified  
 234 as crops from a dog image. We report results for this experiment in Table 2b and we observe  
 235 improvements in FID arising from using out-of-distribution data. Beyond natural images, we show  
 236 that it is even possible to use procedurally generated data from Shaders [6] to (slightly) improve the  
 237 performance. Figure 19 shows an example of such an image and the corresponding predictions of  
 238 a crops classifier. Table 2b contains more results and ablations between annotating all the out-of-  
 239 distribution at a single noise level vs. sample-dependent annotations.

240 **Corruptions of natural datasets – ImageNet results.** Up to this point, our corrupted data has  
 241 been artificially constructed to study our method in a controlled setting. However, it turns out that  
 242 even in real datasets such as ImageNet, there are images with significant degradations such as heavy  
 243 blur, low lighting, and low contrast, and also images with fantastic detail, clear lightning, and sharp  
 244 contrast. Here, the high-quality and the low-quality sets are not given and hence we have to estimate  
 245 them. We opt to use the CLIP-IQA quality metric [66] to separate ImageNet into high-quality (top  
 246 10% CLIP-IQA) and low-quality (bottom 90% CLIP-IQA) sets. Figure 3 shows some of the top  
 247 and bottom quality images according to our metric. Given the high-quality and low-quality sets, we  
 248 are now back to the previous setting where we can use the developed Ambient-o methodology. We  
 249 underline that there is a rich literature regarding quality-assessment methods [69, 68, 49, 67].

250 We use Ambient-o to refer to our method that uses low-quality data at high diffusion times (Section 4)  
 251 and Ambient-o+crops to refer to the extended version of our method that uses crops from potentially  
 252 low-quality images at low-diffusion times. Perhaps surprisingly, there are images in ImageNet that  
 253 have lower global quality but high-quality crops that we can use for low-noise. We present results in  
 254 Table 1, where we show the best FID [29] and  $FD_{DINOv2}$  obtained by different methods. We show the  
 255 highest and lowest quality crops, alongside their associated full images, of ImageNet according to  
 256 CLIP in Figure 15.

257 As shown in the Table, our method leads to state-of-the-art FID scores, improving over the previous  
 258 state-of-the-art baseline EDM-2 [35] at both the low and high parameter count settings. The benefits  
 259 are more pronounced when we measure test FID as our method memorizes significantly less due  
 260 to the addition of noise during the annotation stage of our pipeline (Section 3.1). Beyond FID, we

261 provide qualitative results in Figure 1 (bottom) and Appendix Figures 7, 8. We further show that the  
 262 quality of the generated images measured by CLIP increased compared to the baseline in Appendix  
 263 Table 5. The observed improvements are proof that the ability to learn from data with heterogeneous  
 264 qualities can be truly impactful for realistic settings beyond synthetic corruptions typically studied in  
 265 prior work.

266 **Text-to-image results.** For our final set of experiments, we show how Ambient-o can be used to  
 267 improve the performance of text-to-image diffusion models. We use the code-base of MicroDiffusion  
 268 [54], as it is open-data and trainable with modest compute ( $\approx 2$  days on 8-H100 GPUs). Sehwag et al.  
 269 [54] use four main datasets to train their model: Conceptual Captions (12M) [56], Segment Anything  
 270 (11M) [41], JourneyDB (4.2M) [63], and DiffusionDB (10.7M) [70]. Of these four, DiffusionDB is  
 271 of significantly lower quality than the others as it contains solely synthetic data from an outdated  
 272 diffusion model. This presents an opportunity for the use of our method. Can we use this lower-quality  
 273 data and improve the performance of the trained network?

274 We set  $\sigma_{\min} = 2$  for all samples from DiffusionDB and  $\sigma_{\min} = 0$  for all other datasets and we train a  
 275 diffusion model with Ambient-o. We note that we did not ablate this hyperparameter and it is quite  
 276 likely that improved results would be obtained by tuning it or by training a high-quality vs low-quality  
 277 data classifier for the annotation. Despite that, our trained model achieves a remarkable FID of **10.61**  
 278 in COCO, significantly improving the baseline FID of 12.37 (Table 4). We present qualitative results  
 279 in Figure 1 and GPT-4o evaluations on DrawBench and PartiPrompt in Figure 23. Ambient-o and  
 280 baseline generations for different prompts can be found in Figure 1.

281 As an additional ablation, we compared our method with the recipe of doing a final fine-tuning  
 282 on the highest-quality subset, as done in the works of [54, 13]. Compared to this baseline, our  
 283 method obtained slightly worse COCO FID (10.61 vs 10.27) but obtained much greater diversity,  
 284 as seen visually in Figure 29 and quantitatively through  $> 13\%$  increases in DINO Vendi Diversity  
 285 on prompts from DiffDB (3.22 vs 3.65.). This corroborates our intuition that data filtration leads to  
 286 decreased diversity. Ambient-o uses all the data but can strike a fine balance between high-quality  
 287 and diverse generation.

(a) Measuring fidelity and prompt alignment of  
 generated images on COCO dataset.

Method	FID-30K (↓)	Clip-FD-30K (↓)	Clip-score (↑)
Baseline	12.37	10.07	0.345
Ambient-o	<b>10.61</b>	<b>9.40</b>	<b>0.348</b>

(b) Measuring performance on the GenEval benchmark.

Method	Overall	Objects				Color attribution	
		Single	Two	Counting	Colors		
Baseline	0.44	0.97	0.33	0.35	0.82	0.06	0.14
Ambient-o	<b>0.47</b>	0.97	<b>0.40</b>	<b>0.36</b>	0.82	<b>0.11</b>	0.14

Figure 4: Quantitative benefits of Ambient-o on COCO [44] zero-shot generation and GenEval [26].

## 288 5 Conclusion

289 Is it possible to get good generative models from bad data? Our framework extracts value from  
 290 low-quality, synthetic, and out-of-distribution sources. At a time when the ever-growing data demands  
 291 of GenAI are at odds with the need for quality control, Ambient-o lights a path for both to be achieved  
 292 simultaneously.

## 293 References

- 294 [1] Asad Aali, Marius Arvinte, Sidharth Kumar, and Jonathan I Tamir. “Solving Inverse Prob-  
 295 lems with Score-Based Generative Priors learned from Noisy Data”. In: *arXiv preprint*  
 296 *arXiv:2305.01166* (2023) (cit. on pp. 1, 3).
- 297 [2] Asad Aali, Giannis Daras, Brett Levac, Sidharth Kumar, Alex Dimakis, and Jon Tamir. “Am-  
 298 bient Diffusion Posterior Sampling: Solving Inverse Problems with Diffusion Models Trained on  
 299 Corrupted Data”. In: *The Thirteenth International Conference on Learning Representations*.  
 300 2025. URL: <https://openreview.net/forum?id=qeXcMutEZY> (cit. on p. 1).
- 301 [3] Sina Alemdammad, Josue Casco-Rodriguez, Lorenzo Luzi, Ahmed Imtiaz Humayun, Hossein  
 302 Babaei, Daniel LeJeune, Ali Siahkoohi, and Richard G Baraniuk. “Self-consuming generative  
 303 models go mad”. In: *arXiv preprint arXiv:2307.01850 4* (2023), p. 14 (cit. on p. 3).

304 [4] Sina Alemohammad, Ahmed Imtiaz Humayun, Shruti Agarwal, John Collomosse, and  
 305 Richard Baraniuk. “Self-improving diffusion models with synthetic data”. In: *arXiv preprint*  
 306 *arXiv:2408.16333* (2024) (cit. on p. 3).

307 [5] Weimin Bai, Yifei Wang, Wenzheng Chen, and He Sun. “An Expectation-Maximization  
 308 Algorithm for Training Clean Diffusion Models from Corrupted Observations”. In: *arXiv*  
 309 *preprint arXiv:2407.01014* (2024) (cit. on pp. 1, 3).

310 [6] Manel Baradad, Chun-Fu Chen, Jonas Wulff, Tongzhou Wang, Rogerio Feris, Antonio Torralba,  
 311 and Phillip Isola. “Procedural Image Programs for Representation Learning”. In: *Advances in*  
 312 *Neural Information Processing Systems*. Ed. by Alice H. Oh, Alekh Agarwal, Danielle Belgrave,  
 313 and Kyunghyun Cho. 2022. URL: <https://openreview.net/forum?id=wJwHTgIoEOP>  
 314 (cit. on p. 7).

315 [7] Ashish Bora, Eric Price, and Alexandros G Dimakis. “AmbientGAN: Generative models from  
 316 lossy measurements”. In: *International conference on learning representations*. 2018 (cit. on  
 317 p. 1).

318 [8] Zdravko I Botev, Joseph F Grotowski, and Dirk P Kroese. “Kernel density estimation via  
 319 diffusion”. In: (2010) (cit. on p. 13).

320 [9] Sitan Chen, Sinho Chewi, Jerry Li, Yuanzhi Li, Adil Salim, and Anru R Zhang. “Sampling is  
 321 as easy as learning the score: theory for diffusion models with minimal data assumptions”. In:  
 322 *arXiv preprint arXiv:2209.11215* (2022) (cit. on p. 1).

323 [10] Sitan Chen, Giannis Daras, and Alex Dimakis. “Restoration-Degradation Beyond Linear  
 324 Diffusions: A Non-Asymptotic Analysis For DDIM-type Samplers”. In: *Proceedings of the*  
 325 *40th International Conference on Machine Learning*. Ed. by Andreas Krause, Emma Brun-  
 326 skill, Kyunghyun Cho, Barbara Engelhardt, Sivan Sabato, and Jonathan Scarlett. Vol. 202.  
 327 *Proceedings of Machine Learning Research*. PMLR, 23–29 Jul 2023, pp. 4462–4484. URL:  
 328 <https://proceedings.mlr.press/v202/chen23e.html> (cit. on p. 1).

329 [11] Tianyu Chen, Yasi Zhang, Zhendong Wang, Ying Nian Wu, Oscar Leong, and Mingyuan Zhou.  
 330 *Denoising Score Distillation: From Noisy Diffusion Pretraining to One-Step High-Quality*  
 331 *Generation*. 2025. *arXiv: 2503.07578 [cs.LG]*. URL: <https://arxiv.org/abs/2503.07578> (cit. on p. 1).

333 [12] Yunjey Choi, Youngjung Uh, Jaejun Yoo, and Jung-Woo Ha. “StarGAN v2: Diverse image  
 334 synthesis for multiple domains”. In: *Proceedings of the IEEE/CVF Conference on Computer*  
 335 *Vision and Pattern Recognition*. 2020, pp. 8188–8197 (cit. on p. 21).

336 [13] Xiaoliang Dai et al. *Emu: Enhancing Image Generation Models Using Photogenic Needles in*  
 337 *a Haystack*. 2023. *arXiv: 2309.15807 [cs.CV]* (cit. on pp. 1, 3, 8).

338 [14] Giannis Daras, Yeshwanth Cherapanamjeri, and Constantinos Costis Daskalakis. “How Much  
 339 is a Noisy Image Worth? Data Scaling Laws for Ambient Diffusion.” In: *The Thirteenth*  
 340 *International Conference on Learning Representations*. 2025. URL: <https://openreview.net/forum?id=qZwtPEw2qN> (cit. on p. 1).

342 [15] Giannis Daras, Yuval Dagan, Alexandros G Dimakis, and Constantinos Daskalakis. “Consistent  
 343 diffusion models: Mitigating sampling drift by learning to be consistent”. In: *arXiv preprint*  
 344 *arXiv:2302.09057* (2023) (cit. on pp. 1, 3).

345 [16] Giannis Daras, Mauricio Delbracio, Hossein Talebi, Alex Dimakis, and Peyman Milanfar.  
 346 “Soft Diffusion: Score Matching with General Corruptions”. In: *Transactions on Machine*  
 347 *Learning Research* (2023). ISSN: 2835-8856. URL: <https://openreview.net/forum?id=W98rebBx1Q> (cit. on p. 1).

349 [17] Giannis Daras, Alexandros G Dimakis, and Constantinos Daskalakis. “Consistent Diffusion  
 350 Meets Tweedie: Training Exact Ambient Diffusion Models with Noisy Data”. In: *arXiv preprint*  
 351 *arXiv:2404.10177* (2024) (cit. on pp. 1, 3).

352 [18] Giannis Daras, Kulin Shah, Yuval Dagan, Aravind Gollakota, Alex Dimakis, and Adam Klivans.  
 353 “Ambient Diffusion: Learning Clean Distributions from Corrupted Data”. In: *Thirty-seventh*  
 354 *Conference on Neural Information Processing Systems*. 2023. URL: <https://openreview.net/forum?id=wBJBLy9kBY> (cit. on pp. 1, 3).

356 [19] Mauricio Delbracio and Peyman Milanfar. “Inversion by direct iteration: An alternative to  
 357 denoising diffusion for image restoration”. In: *arXiv preprint arXiv:2303.11435* (2023) (cit. on  
 358 p. 1).

359 [20] Jia Deng, Wei Dong, Richard Socher, Li-Jia Li, Kai Li, and Li Fei-Fei. “ImageNet: A large-  
 360 scale hierarchical image database”. In: *2009 IEEE Conference on Computer Vision and Pattern*  
 361 *Recognition*. 2009, pp. 248–255. DOI: [10.1109/CVPR.2009.5206848](https://doi.org/10.1109/CVPR.2009.5206848) (cit. on p. 21).

362 [21] Prafulla Dhariwal and Alexander Nichol. “Diffusion models beat gans on image synthesis”. In: *Advances in neural information processing systems* 34 (2021), pp. 8780–8794 (cit. on p. 4).

363 [22] Sander Dieleman. *Diffusion is spectral autoregression*. 2024. URL: <https://sander.ai/2024/09/02/spectral-autoregression.html> (cit. on p. 2).

364 [23] Logan Engstrom, Andrew Ilyas, Benjamin Chen, Axel Feldmann, William Moses, and  
 365 Aleksander Madry. “Optimizing ml training with metagradient descent”. In: *arXiv preprint*  
 366 *arXiv:2503.13751* (2025) (cit. on p. 3).

367 [24] Damien Ferbach, Quentin Bertrand, Avishek Joey Bose, and Gauthier Gidel. “Self-consuming  
 368 generative models with curated data provably optimize human preferences”. In: *arXiv preprint*  
 369 *arXiv:2407.09499* (2024) (cit. on p. 3).

370 [25] Samir Yitzhak Gadre, Gabriel Ilharco, Alex Fang, Jonathan Hayase, Georgios Smyrnis, Thao  
 371 Nguyen, Ryan Marten, Mitchell Wortsman, Dhruba Ghosh, Jieyu Zhang, et al. “DataComp: In  
 372 search of the next generation of multimodal datasets”. In: *arXiv preprint arXiv:2304.14108*  
 373 (2023) (cit. on pp. 1, 3).

374 [26] Dhruba Ghosh, Hanna Hajishirzi, and Ludwig Schmidt. *GenEval: An Object-Focused Frame-  
 375 work for Evaluating Text-to-Image Alignment*. 2023. arXiv: [2310.11513](https://arxiv.org/abs/2310.11513) [cs.CV]. URL:  
 376 <https://arxiv.org/abs/2310.11513> (cit. on p. 8).

377 [27] Sachin Goyal, Pratyush Maini, Zachary C Lipton, Aditi Raghunathan, and J Zico Kolter.  
 378 “Scaling Laws for Data Filtering–Data Curation cannot be Compute Agnostic”. In: *Proceedings*  
 379 *of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*. 2024, pp. 22702–  
 380 22711 (cit. on p. 1).

381 [28] Dan Hendrycks and Thomas Dietterich. “Benchmarking neural network robustness to common  
 382 corruptions and perturbations”. In: *arXiv preprint arXiv:1903.12261* (2019) (cit. on p. 1).

383 [29] Martin Heusel, Hubert Ramsauer, Thomas Unterthiner, Bernhard Nessler, and Sepp Hochreiter.  
 384 “Gans trained by a two time-scale update rule converge to a local nash equilibrium”. In: *Advances in neural information processing systems* 30 (2017) (cit. on pp. 6, 7).

385 [30] Jonathan Ho, Ajay Jain, and Pieter Abbeel. “Denoising diffusion probabilistic models”. In: *Advances in Neural Information Processing Systems* 33 (2020), pp. 6840–6851 (cit. on p. 1).

386 [31] Robert A. Jacobs, Michael I. Jordan, Steven J. Nowlan, and Geoffrey E. Hinton. “Adap-  
 387 tive Mixtures of Local Experts”. In: *Neural Computation* 3.1 (Mar. 1991). \_eprint:  
 388 <https://direct.mit.edu/neco/article-pdf/3/1/79/812104/neco.1991.3.1.79.pdf>, pp. 79–87. ISSN:  
 389 0899-7667. DOI: [10.1162/neco.1991.3.1.79](https://doi.org/10.1162/neco.1991.3.1.79). URL: <https://doi.org/10.1162/neco.1991.3.1.79> (cit. on p. 22).

390 [32] Yiding Jiang, Allan Zhou, Zhili Feng, Sadhika Malladi, and J Zico Kolter. “Adaptive data opti-  
 391 mization: Dynamic sample selection with scaling laws”. In: *arXiv preprint arXiv:2410.11820*  
 392 (2024) (cit. on p. 1).

393 [33] Mason Kamb and Surya Ganguli. “An analytic theory of creativity in convolutional diffusion  
 394 models”. In: *arXiv preprint arXiv:2412.20292* (2024) (cit. on p. 13).

395 [34] Tero Karras, Miika Aittala, Timo Aila, and Samuli Laine. “Elucidating the design space of  
 396 diffusion-based generative models”. In: *arXiv preprint arXiv:2206.00364* (2022) (cit. on pp. 6,  
 397 21).

398 [35] Tero Karras, Miika Aittala, Jaakko Lehtinen, Janne Hellsten, Timo Aila, and Samuli Laine.  
 399 “Analyzing and Improving the Training Dynamics of Diffusion Models”. In: *Proc. CVPR*. 2024  
 400 (cit. on pp. 2, 7, 19–21).

401 [36] Tero Karras, Samuli Laine, and Timo Aila. “A style-based generator architecture for generative  
 402 adversarial networks”. In: *Proceedings of the IEEE/CVF Conference on Computer Vision and*  
 403 *Pattern Recognition*. 2019, pp. 4401–4410 (cit. on p. 21).

404 [37] Sergey Kastryulin, Dzhamil Zakirov, and Denis Prokopenko. *PyTorch Image Quality:  
 405 Metrics and Measure for Image Quality Assessment*. Open-source software available  
 406 at <https://github.com/photosynthesis-team/piq>. 2019. URL: <https://github.com/photosynthesis-team/piq> (cit. on p. 18).

407 [38] Sergey Kastryulin, Jamil Zakirov, Denis Prokopenko, and Dmitry V. Dylov. *PyTorch Image  
 408 Quality: Metrics for Image Quality Assessment*. 2022. DOI: [10.48550/ARXIV.2208.14818](https://doi.org/10.48550/ARXIV.2208.14818).  
 409 URL: <https://arxiv.org/abs/2208.14818> (cit. on p. 18).

416 [39] Varun A Kelkar, Rucha Deshpande, Arindam Banerjee, and Mark A Anastasio. “Ambient-  
 417 Flow: Invertible generative models from incomplete, noisy measurements”. In: *arXiv preprint*  
 418 *arXiv:2309.04856* (2023) (cit. on p. 1).

419 [40] Diederik P Kingma and Jimmy Ba. “Adam: A Method for Stochastic Optimization”. In: *arXiv*  
 420 *preprint arXiv:1412.6980* (2014) (cit. on pp. 21, 22).

421 [41] Alexander Kirillov, Eric Mintun, Nikhila Ravi, Hanzi Mao, Chloe Rolland, Laura Gustafson,  
 422 Tete Xiao, Spencer Whitehead, Alexander C. Berg, Wan-Yen Lo, Piotr Dollár, and Ross  
 423 Girshick. *Segment Anything*. 2023. arXiv: [2304.02643 \[cs.CV\]](https://arxiv.org/abs/2304.02643). URL: <https://arxiv.org/abs/2304.02643> (cit. on pp. 8, 21).

425 [42] Alex Krizhevsky and Geoffrey Hinton. “Learning multiple layers of features from tiny images”.  
 426 In: (2009) (cit. on p. 21).

427 [43] Jeffrey Li et al. *DataComp-LM: In search of the next generation of training sets for language*  
 428 *models*. 2024. arXiv: [2406.11794 \[cs.LG\]](https://arxiv.org/abs/2406.11794) (cit. on pp. 1, 3).

429 [44] Tsung-Yi Lin, Michael Maire, Serge Belongie, Lubomir Bourdev, Ross Girshick, James Hays,  
 430 Pietro Perona, Deva Ramanan, C. Lawrence Zitnick, and Piotr Dollár. *Microsoft COCO: Common Objects in Context*. 2015. arXiv: [1405.0312 \[cs.CV\]](https://arxiv.org/abs/1405.0312). URL: <https://arxiv.org/abs/1405.0312> (cit. on p. 8).

433 [45] Yvette Y Lin, Angela F Gao, and Katherine L Bouman. “IMAGING AN EVOLVING BLACK  
 434 HOLE BY LEVERAGING SHARED STRUCTURE”. In: *ICASSP* (2024) (cit. on p. 1).

435 [46] Zeyuan Liu, Zhihe Yang, Jiawei Xu, Rui Yang, Jiafei Lyu, Baoxiang Wang, Yunjian Xu, and  
 436 Xiu Li. “ADG: Ambient Diffusion-Guided Dataset Recovery for Corruption-Robust Offline  
 437 Reinforcement Learning”. In: *arXiv preprint arXiv:2505.23871* (2025) (cit. on p. 1).

438 [47] Haoye Lu, Qifan Wu, and Yaoliang Yu. “SFBD: A Method for Training Diffusion Models with  
 439 Noisy Data”. In: *Frontiers in Probabilistic Inference: Learning meets Sampling*. 2025. URL:  
 440 <https://openreview.net/forum?id=6HN14zuHRb> (cit. on p. 1).

441 [48] Haoye Lu, Qifan Wu, and Yaoliang Yu. *Stochastic Forward-Backward Deconvolution: Training*  
 442 *Diffusion Models with Finite Noisy Datasets*. 2025. arXiv: [2502.05446 \[cs.LG\]](https://arxiv.org/abs/2502.05446). URL:  
 443 <https://arxiv.org/abs/2502.05446> (cit. on p. 1).

444 [49] Anish Mittal, Rajiv Soundararajan, and Alan C Bovik. “Making a “completely blind” image  
 445 quality analyzer”. In: *IEEE Signal processing letters* 20.3 (2012), pp. 209–212 (cit. on p. 7).

446 [50] William Peebles and Saining Xie. *Scalable Diffusion Models with Transformers*. 2023. arXiv:  
 447 [2212.09748 \[cs.CV\]](https://arxiv.org/abs/2212.09748). URL: <https://arxiv.org/abs/2212.09748> (cit. on p. 22).

448 [51] Guilherme Penedo, Hynek Kydlíček, Anton Lozhkov, Margaret Mitchell, Colin Raffel, Leandro  
 449 Von Werra, Thomas Wolf, et al. “The FineWeb Datasets: Decanting the Web for the Finest  
 450 Text Data at Scale”. In: *arXiv preprint arXiv:2406.17557* (2024) (cit. on p. 1).

451 [52] François Rozet, Gérôme Andry, François Lanusse, and Gilles Louppe. “Learning Diffusion  
 452 Priors from Observations by Expectation Maximization”. In: *arXiv preprint arXiv:2405.13712*  
 453 (2024) (cit. on pp. 1, 3).

454 [53] Christoph Schuhmann, Romain Beaumont, Richard Vencu, Cade Gordon, Ross Wightman,  
 455 Mehdi Cherti, Theo Coombes, Aarush Katta, Clayton Mullis, Mitchell Wortsman, et al. “Laion-  
 456 5b: An open large-scale dataset for training next generation image-text models”. In: *Advances*  
 457 *in Neural Information Processing Systems* 35 (2022), pp. 25278–25294 (cit. on p. 1).

458 [54] Vikash Sehwag, Xianghao Kong, Jingtao Li, Michael Spranger, and Lingjuan Lyu. “Stretch-  
 459 ing Each Dollar: Diffusion Training from Scratch on a Micro-Budget”. In: *arXiv preprint*  
 460 *arXiv:2407.15811* (2024) (cit. on pp. 2, 3, 8, 21, 22).

461 [55] Kulin Shah, Alkis Kalavasis, Adam R. Klivans, and Giannis Daras. *Does Generation Require*  
 462 *Memorization? Creative Diffusion Models using Ambient Diffusion*. 2025. arXiv: [2502.21278 \[cs.LG\]](https://arxiv.org/abs/2502.21278) (cit. on p. 1).

464 [56] Piyush Sharma, Nan Ding, Sebastian Goodman, and Radu Soricut. “Conceptual Captions:  
 465 A Cleaned, Hypernymed, Image Alt-text Dataset For Automatic Image Captioning”. In: *Proceedings of the 56th Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers)*. Ed. by Iryna Gurevych and Yusuke Miyao. Melbourne, Australia:  
 466 Association for Computational Linguistics, July 2018, pp. 2556–2565. DOI: [10.18653/v1-P18-1238](https://doi.org/10.18653/v1-P18-1238). URL: <https://aclanthology.org/P18-1238/> (cit. on pp. 8, 21).

470 [57] Noam Shazeer, Azalia Mirhoseini, Krzysztof Maziarz, Andy Davis, Quoc Le, Geoffrey Hinton, and Jeff Dean. *Outrageously Large Neural Networks: The Sparsely-Gated Mixture-of-Experts Layer*. 2017. arXiv: [1701.06538 \[cs.LG\]](https://arxiv.org/abs/1701.06538). URL: <https://arxiv.org/abs/1701.06538> (cit. on p. 22).

471 [58] Gowthami Somepalli, Vasu Singla, Micah Goldblum, Jonas Geiping, and Tom Goldstein. “Diffusion Art or Digital Forgery? Investigating Data Replication in Diffusion Models”. In: *arXiv preprint arXiv:2212.03860* (2022) (cit. on p. 1).

472 [59] Gowthami Somepalli, Vasu Singla, Micah Goldblum, Jonas Geiping, and Tom Goldstein. “Understanding and Mitigating Copying in Diffusion Models”. In: *arXiv preprint arXiv:2305.20086* (2023) (cit. on p. 1).

473 [60] Jiaming Song, Chenlin Meng, and Stefano Ermon. “Denoising diffusion implicit models”. In: *arXiv preprint arXiv:2010.02502* (2020) (cit. on p. 21).

474 [61] Yang Song and Stefano Ermon. “Generative modeling by estimating gradients of the data distribution”. In: *Advances in Neural Information Processing Systems* 32 (2019) (cit. on p. 1).

475 [62] Yang Song, Jascha Sohl-Dickstein, Diederik P Kingma, Abhishek Kumar, Stefano Ermon, and Ben Poole. “Score-based generative modeling through stochastic differential equations”. In: *arXiv preprint arXiv:2011.13456* (2020) (cit. on p. 1).

476 [63] Keqiang Sun, Junting Pan, Yuying Ge, Hao Li, Haodong Duan, Xiaoshi Wu, Renrui Zhang, Aojun Zhou, Zipeng Qin, Yi Wang, Jifeng Dai, Yu Qiao, Limin Wang, and Hongsheng Li. *JourneyDB: A Benchmark for Generative Image Understanding*. 2023. arXiv: [2307.00716 \[cs.CV\]](https://arxiv.org/abs/2307.00716). URL: <https://arxiv.org/abs/2307.00716> (cit. on pp. 8, 21).

477 [64] Ayush Tewari, Tianwei Yin, George Cazenavette, Semon Rezhikov, Josh Tenenbaum, Frédo Durand, Bill Freeman, and Vincent Sitzmann. “Diffusion with forward models: Solving stochastic inverse problems without direct supervision”. In: *Advances in Neural Information Processing Systems* 36 (2023), pp. 12349–12362 (cit. on p. 1).

478 [65] Antonio Torralba, Phillip Isola, and William T Freeman. *Foundations of computer vision*. MIT Press, 2024 (cit. on p. 2).

479 [66] Jianyi Wang, Kelvin CK Chan, and Chen Change Loy. “Exploring CLIP for Assessing the Look and Feel of Images”. In: *AAAI*. 2023 (cit. on pp. 7, 21).

480 [67] Jianyi Wang, Kelvin CK Chan, and Chen Change Loy. “Exploring clip for assessing the look and feel of images”. In: *Proceedings of the AAAI conference on artificial intelligence*. Vol. 37. 2. 2023, pp. 2555–2563 (cit. on p. 7).

481 [68] Zhou Wang, Alan C Bovik, Hamid R Sheikh, and Eero P Simoncelli. “Image quality assessment: from error visibility to structural similarity”. In: *IEEE transactions on image processing* 13.4 (2004), pp. 600–612 (cit. on p. 7).

482 [69] Zhou Wang, Eero P Simoncelli, and Alan C Bovik. “Multiscale structural similarity for image quality assessment”. In: *The Thirly-Seventh Asilomar Conference on Signals, Systems & Computers*, 2003. Vol. 2. Ieee. 2003, pp. 1398–1402 (cit. on p. 7).

483 [70] Zijie J Wang, Evan Montoya, David Munechika, Haoyang Yang, Benjamin Hoover, and Duen Horng Chau. “DiffusionDB: A Large-scale Prompt Gallery Dataset for Text-to-Image Generative Models”. In: *arXiv preprint arXiv:2210.14896* (2022) (cit. on pp. 8, 21).

484 [71] Yasi Zhang, Tianyu Chen, Zhendong Wang, Ying Nian Wu, Mingyuan Zhou, and Oscar Leong. “Restoration Score Distillation: From Corrupted Diffusion Pretraining to One-Step High-Quality Generation”. In: *arXiv preprint arXiv:2505.13377* (2025) (cit. on p. 1).

514 **A Limitations and Future Work**

515 Our work opens several avenues for improvement. On the theoretical side, we aim to establish  
 516 matching lower bounds to demonstrate that learning from the mixture distribution becomes provably  
 517 optimal beyond a certain noise threshold. Algorithmically, while our method performs well under  
 518 high-frequency corruptions, it remains an open question whether more effective training strategies  
 519 could be used for different types of corruptions (e.g., masking). Moreover, real-world datasets often  
 520 exhibit patch-wise heterogeneity—for example, facial regions are frequently blurred for privacy,  
 521 leading to uneven corruption across image crops. We plan to investigate patch-level noise annotations  
 522 to better capture this structure in future work. Computationally, the full-version of our algorithm  
 523 requires the training of classifiers for annotations that increases the runtime. This overhead can be

524 avoided by using hand-picked annotation times based on quality proxies as done in our synthetic data  
 525 experiment. Finally, we believe the true potential of Ambient-o lies in scientific applications, where  
 526 data often arises from heterogeneous measurement processes.

## 527 B Theory

528 We study the 1-d case, but all our claims easily extend to any dimension. We compare two algorithms:

529 **Algorithm 1.** Algorithm 1 trains a diffusion model using access to  $n_1$  samples from a target density  
 530  $p_0$ , assumed to be supported in  $[0, 1]$  and be  $\lambda_1$ -Lipschitz.

531 **Algorithm 2.** Algorithm 2 trains a diffusion model using access to  $n_1 + n_2$  samples from a density  
 532  $\tilde{p}_0$  that is a mixture of the a target density  $p_0$  and another density  $q_0$ , assumed to be supported in  $[0, 1]$   
 533 and be  $\lambda_2$ -Lipschitz:  $\tilde{p}_0 = \frac{n_1}{n_1+n_2}p_0 + \frac{n_2}{n_1+n_2}q_0$ .

534 We want to compare how well these algorithms estimate the distribution  $p_t := p_0 \circledast \mathcal{N}(0, \sigma_t^2)$ . We  
 535 use  $\hat{p}_t^{(1)}, \hat{p}_t^{(2)}$  to denote the estimates obtained for  $p_t$  by Algorithms 1 and 2 respectively.

536 **Diffusion modeling is Gaussian kernel density estimation.** We start by making a connection  
 537 between the optimal solution to the diffusion modeling objective and kernel density estimation. Given  
 538 a finite dataset  $\{W^{(i)}\}_{i=1}^n$ , the optimal solution to the diffusion modeling objective should match the  
 539 empirical density at time  $t$ , which is:

$$\hat{p}_t(x) = \frac{1}{n\sigma_t} \sum_{i=1}^n \phi\left(\frac{W^{(i)} - x}{\sigma_t}\right), \quad (\text{B.1})$$

540 where  $\phi(u) = \frac{1}{\sqrt{2\pi}}e^{-u^2/2}$  is the Gaussian kernel. We observe that equation B.1 is identical to a  
 541 Gaussian kernel density estimate, given samples  $\{W^{(i)}\}_{i=1}^n$ .<sup>3</sup>

542 We establish the following result for Gaussian kernel density estimation.

543 **Theorem B.1** (Gaussian Kernel Density Estimation). *Let  $\{W^{(i)}\}_{i=1}^n$  be a set of  $n$  independent  
 544 samples from a  $\lambda$ -Lipschitz density  $p$ . Let  $\hat{p}$  be the empirical density,  $p_\sigma := p \circledast \mathcal{N}(0, \sigma^2)$  and  
 545  $\hat{p}_\sigma = \hat{p} \circledast \mathcal{N}(0, \sigma^2)$ . Then, with probability at least  $1 - \delta$  with respect to the sample randomness,*

$$d_{\text{TV}}(p_\sigma, \hat{p}_\sigma) \lesssim \frac{1}{n} + \frac{1}{\sigma^2 n} + \sqrt{\frac{\log n + \log(1 \vee \lambda) + \log 2/\delta}{\sigma^2 n}}. \quad (\text{B.2})$$

546 The proof of this result is given in the Appendix.

547 **Comparing the performance of Algorithms 1 and 2.** Applying Theorem B.1 directly to the  $p_0$   
 548 density, we immediately get that the estimate  $\hat{p}_t^{(1)}(x)$  obtained by Algorithm 1 satisfies:

$$d_{\text{TV}}(p_t, \hat{p}_t^{(1)}) \lesssim \frac{1}{n_1} + \frac{1}{\sigma_t^2 n_1} + \sqrt{\frac{\log n_1 + \log(1 \vee \lambda_1) + \log 2/\delta}{\sigma_t^2 n_1}}. \quad (\text{B.3})$$

549 Let us now see what we get by applying Theorem B.1 to Algorithm 2, which uses samples from the  
 550 tilted distribution  $\tilde{p}_0$ . Since this distribution is  $\left(\frac{n_1}{n_1+n_2}\lambda_1 + \frac{n_2}{n_1+n_2}\lambda_2\right)$ -Lipschitz, we get that:

$$d_{\text{TV}}(\tilde{p}_t, \hat{p}_t^{(2)}) \lesssim \frac{1}{(n_1 + n_2)} + \frac{1}{\sigma_t^2 (n_1 + n_2)} + \sqrt{\frac{\log(n_1 + n_2) + \log(1 \vee \frac{n_1}{n_1+n_2}\lambda_1 + \frac{n_2}{n_1+n_2}\lambda_2) + \log 2/\delta}{\sigma_t^2 (n_1 + n_2)}},$$

551 where  $\tilde{p}_t := \tilde{p}_0 \circledast \mathcal{N}(0, \sigma_t^2)$ .

552 Further, we have that:  $d_{\text{TV}}(p_t, \hat{p}_t^{(2)}) \leq d_{\text{TV}}(\tilde{p}_t, p_t) + d_{\text{TV}}(\tilde{p}_t, \hat{p}_t^{(2)})$ . We already have a bound for  
 553 the second term. To bound the first term, we prove the following theorem.

<sup>3</sup>This connection has been observed in prior works too, e.g., see [33, 8].

**Theorem B.2** (Distance contraction under noise). *Consider distributions  $P$  and  $Q$  supported on a subset of  $\mathbb{R}^d$  with diameter  $D$ . Then*

$$d_{\text{TV}}(P \circledast \mathcal{N}(0, \sigma^2 \mathbf{I}), Q \circledast \mathcal{N}(0, \sigma^2 \mathbf{I})) \leq d_{\text{TV}}(P, Q) \cdot \frac{D}{2\sigma}.$$

554 Applying this theorem we get that:  $d_{\text{TV}}(\tilde{p}_t, p_t) \leq \frac{1}{2\sigma_t} d_{\text{TV}}(\tilde{p}_0, p_0) \leq \frac{1}{2\sigma_t} \cdot \frac{n_2}{n_1+n_2} d_{\text{TV}}(p_0, q_0)$ , where  
555 for the second inequality we used that  $d_{\text{TV}}(p_0, \tilde{p}_0) \leq \frac{n_2}{n_1+n_2} d_{\text{TV}}(p_0, q_0)$ .

557 Putting everything together, Algorithm (2) achieves an estimation error:

$$d_{\text{TV}}(p_t, \hat{p}_t^{(2)}) \lesssim \frac{1}{(n_1+n_2)} + \frac{1}{\sigma_t^2(n_1+n_2)} + \sqrt{\frac{\log(n_1+n_2) + \log(1 \vee \frac{n_1}{n_1+n_2} \lambda_1 + \frac{n_2}{n_1+n_2} \lambda_2) + \log 2/\delta}{\sigma_t^2(n_1+n_2)}} + \frac{n_2}{\sigma_t(n_1+n_2)} d_{\text{TV}}(p_0, q_0).$$

558 Comparing this with the bound obtained in Equation B.3, we see that if  $n_2$  is sufficiently larger than  
559  $n_1$  or if  $\lambda_2 \leq \lambda_1$ , there is a  $t_n^{\min}$  such that for any  $t \geq t_n^{\min}$ , the upper-bound obtained by Algorithm  
560 2 is better than the upper-bound obtained by Algorithm 1. That implies that for high-diffusion times,  
561 using biased data might be helpful for learning, as the bias term (final term) decays with the amount  
562 of noise. Going back to equation B, note that the switching point  $t \geq t_n^{\min}$  depends on the distance  
563  $d_{\text{TV}}(\tilde{p}_t, p_t)$  that decays as shown in Theorem B.2. Once this distance becomes small enough, our  
564 computations above suggest that we benefit from biased data. The classifier of Section 3.1, if optimal,  
565 exactly tracks the distance  $d_{\text{TV}}(\tilde{p}_t, p_t)$  and, as a result, tracks the switching point.

## 566 C Theoretical Results

### 567 C.1 Kernel Estimation

568 **Assumption C.1.** The density  $p$  is  $\lambda$  lipschitz.

569 Let  $\{X^{(i)}\}_{i=1}^n$  a set of  $n$  independent samples from a density  $p$  that satisfies Assumption C.1. Let  $\hat{p}$   
570 be the empirical density on those samples.

571 We are interested in bounding the total variation distance between  $p_\sigma := p \circledast \mathcal{N}(0, \sigma^2)$  and  $\hat{p}_\sigma =$   
572  $\hat{p} \circledast \mathcal{N}(0, \sigma^2)$ . In particular,

$$\hat{p}_\sigma(x) = \frac{1}{n\sigma} \sum_{i=1}^n \phi\left(\frac{X^{(i)} - x}{\sigma}\right), \quad (\text{C.1})$$

573 where  $\phi(u) = \frac{1}{\sqrt{2\pi}} e^{-u^2/2}$  is the Gaussian kernel. We want to argue that the TV distance between  
574  $p_\sigma$  and  $\hat{p}_\sigma$  is small given sufficiently many samples  $n$ . For simplicity, let's fix the support of  $p$  to be  
575  $[0, 1]$ . We have:

$$d_{\text{TV}}(p_\sigma, \hat{p}_\sigma) = \frac{1}{2} \int_0^1 |p_\sigma(x) - \hat{p}_\sigma(x)| dx = \sum_{l=0}^{L-1} \int_{l/L}^{(l+1)/L} |p_\sigma(x) - \hat{p}_\sigma(x)| dx \quad (\text{C.2})$$

576 Now let us look at one of the terms of the summation.

$$\int_{l/L}^{(l+1)/L} |p_\sigma(x) - \hat{p}_\sigma(x)| dx = \int_{l/L}^{(l+1)/L} |p_\sigma(x) - p_\sigma(l/L) + p_\sigma(l/L) - \hat{p}_\sigma(x)| dx \quad (\text{C.3})$$

$$\leq \int_{l/L}^{(l+1)/L} |p_\sigma(x) - p_\sigma(l/L)| dx + \int_{l/L}^{(l+1)/L} |p_\sigma(l/L) - \hat{p}_\sigma(x)| dx. \quad (\text{C.4})$$

577 We first work on the first term. Using Lemma C.6:

$$\int_{l/L}^{(l+1)/L} |p_\sigma(x) - p_\sigma(l/L)| dx \leq \lambda \int_{l/L}^{(l+1)/L} |x - l/L| dx \quad (\text{C.5})$$

$$= \frac{\lambda}{2L^2}. \quad (\text{C.6})$$

578 Next, we work on the second term.

$$\int_{l/L}^{(l+1)/L} |p_\sigma(l/L) - \hat{p}_\sigma(x)| dx = \int_{l/L}^{(l+1)/L} |p_\sigma(l/L) - \hat{p}_\sigma(l/L) + \hat{p}_\sigma(l/L) - \hat{p}_\sigma(x)| dx \quad (\text{C.7})$$

$$\leq \int_{l/L}^{(l+1)/L} |p_\sigma(l/L) - \hat{p}_\sigma(l/L)| dx + \int_{l/L}^{(l+1)/L} |\hat{p}_\sigma(l/L) - \hat{p}_\sigma(x)| dx. \quad (\text{C.8})$$

579 According to Lemma C.5, we have that  $\hat{p}_\sigma$  is  $\hat{\lambda} = \frac{1}{\sigma^2 \sqrt{2\pi e}}$  Lipschitz. Then, the second term becomes:

$$\int_{l/L}^{(l+1)/L} |\hat{p}_\sigma(l/L) - \hat{p}_\sigma(x)| dx \leq \hat{\lambda} \int_{l/L}^{(l+1)/L} |l/L - x| dx = \frac{\hat{\lambda}}{2L^2}. \quad (\text{C.9})$$

580 It remains to bound the following term

$$\int_{l/L}^{(l+1)/L} |p_\sigma(l/L) - \hat{p}_\sigma(l/L)| dx = \frac{|p_\sigma(l/L) - \hat{p}_\sigma(l/L)|}{L} \quad (\text{C.10})$$

581 We will be applying Hoeffding's Inequality, stated below:

582 **Theorem C.2** (Hoeffding's Inequality). *Let  $Y_1, \dots, Y_n$  be independent random variables in  $[a, b]$  with  
583 mean  $\mu$ . Then,*

$$\Pr \left( \left| \frac{1}{n} \sum_{i=1}^n Y_i - \mu \right| \geq t \right) \leq 2 \exp \left( -2nt^2/(b-a)^2 \right). \quad (\text{C.11})$$

584 Recall that  $\hat{p}_\sigma$  can be written as

$$\hat{p}_\sigma(x) = \frac{1}{n} \sum_{i=1}^n \frac{\phi((X^{(i)} - x)/\sigma)}{\sigma} = \frac{1}{n} \sum_{i=1}^n Y_i, \quad (\text{C.12})$$

585 in terms of the random variables  $Y_i := \frac{\phi((X^{(i)} - x)/\sigma)}{\sigma}$ . These random variables are supported in  
586  $\left[0, \frac{1}{\sqrt{2\pi\sigma^2}}\right]$ . So, for any  $x$ , we have that:

$$\Pr (|\hat{p}_\sigma(x) - \mathbb{E}[\hat{p}_\sigma(x)]| \geq t) \leq 2 \exp (-4\pi\sigma^2 nt^2). \quad (\text{C.13})$$

587 Taking  $t = \sqrt{\frac{\log(2L/\delta)}{4\pi\sigma^2 n}}$  and using the above inequality and the union bound, we have that, with  
588 probability at least  $1 - \delta$ , for all  $l \in \{0, 1, \dots, L-1\}$ :

$$|\hat{p}_\sigma(l/L) - \mathbb{E}[\hat{p}_\sigma(l/L)]| \leq \sqrt{\frac{\log(2L/\delta)}{4\pi\sigma^2 n}}. \quad (\text{C.14})$$

589 Let us now compute the expected value of  $\hat{p}_\sigma(x)$ .

$$\mathbb{E}[\hat{p}_\sigma(x)] = \mathbb{E} \left[ \frac{1}{n\sigma} \sum_{i=1}^n \phi \left( \frac{X^{(i)} - x}{\sigma} \right) \right] \quad (\text{C.15})$$

$$= \frac{1}{n\sigma} \sum_{i=1}^n \mathbb{E} \left[ \phi \left( \frac{X^{(i)} - x}{\sigma} \right) \right] \quad (\text{C.16})$$

$$= \frac{1}{\sigma} \int p(u) \phi \left( \frac{x-u}{\sigma} \right) du \equiv (p \circledast \mathcal{N}(0, \sigma^2))(x) = p_\sigma(x). \quad (\text{C.17})$$

590 Combining equation C.14 and equation C.17, we get:

$$|\hat{p}_\sigma(l/L) - p_\sigma(x)| \leq \sqrt{\frac{\log(2L/\delta)}{4\pi\sigma^2 n}}. \quad (\text{C.18})$$

Putting everything together we have:

$$d_{\text{TV}}(p_\sigma, \hat{p}_\sigma) \leq \frac{\lambda}{2L} + \frac{1}{2L\sigma^2\sqrt{2\pi e}} + \sqrt{\frac{\log(2L/\delta)}{4\pi\sigma^2 n}}.$$

Choosing  $L = n \cdot \max\{\lambda, 1\}$  we get that:

$$d_{\text{TV}}(p_\sigma, \hat{p}_\sigma) \lesssim \frac{1}{n} + \frac{1}{\sigma^2 n} + \sqrt{\frac{\log n + \log(1 \vee \lambda) + \log 2/\delta}{\sigma^2 n}}.$$

591 **C.2 Evolution of parameters under noise**

592 *Proof of theorem B.2:* We will use the following facts:

593 *Fact 1* (Direct corollary of the optimal coupling theorem). There exists a coupling  $\gamma$  of  $P$  and  $Q$ ,  
594 which samples a pair of random variables  $(X, Y) \sim \gamma$  such that  $\Pr_{\gamma}[X \neq Y] = d_{\text{TV}}(P, Q)$ .

595 *Fact 2.* For any  $x, y \in \mathbb{R}^d$ :  $d_{\text{TV}}(\mathcal{N}(x, \sigma^2 \mathbf{I}), \mathcal{N}(y, \sigma^2 \mathbf{I})) \leq \|x - y\|/2\sigma$

*Proof.* The KL divergence between  $\mathcal{N}(\mu_1, \Sigma_1)$  and  $\mathcal{N}(\mu_2, \Sigma_2)$  is

$$\text{KL}(\mathcal{N}(\mu_1, \Sigma_1), \mathcal{N}(\mu_2, \Sigma_2)) = \frac{1}{2} \left( \text{tr}(\Sigma_2^{-1} \Sigma_1) + (\mu_2 - \mu_1) \Sigma_2^{-1} (\mu_2 - \mu_1) - d + \log \frac{|\Sigma_2|}{|\Sigma_1|} \right).$$

Applying this general result to our case:

$$\text{KL}(\mathcal{N}(x, \sigma^2 \mathbf{I}), \mathcal{N}(y, \sigma^2 \mathbf{I})) = \frac{1}{2} \left( \frac{\|x - y\|^2}{\sigma^2} \right).$$

596 We conclude by applying Pinsker's inequality.  $\square$

597 A corollary of Fact 2 and the optimal coupling theorem is the following:

598 *Fact 3.* Fix arbitrary  $x, y \in \mathbb{R}^d$ . There exists a coupling  $\gamma_{x,y}$  of  $\mathcal{N}(0, \sigma^2 \mathbf{I})$  and  $\mathcal{N}(0, \sigma^2 \mathbf{I})$ , which  
599 samples a pair of random variables  $(Z, Z') \sim \gamma_{x,y}$  such that  $\Pr_{\gamma_{x,y}}[x + Z \neq y + Z'] = \|x - y\|/2\sigma$ .

600 Now let us denote by  $\tilde{P} = P \circledast \mathcal{N}(0, \sigma^2 \mathbf{I})$  and  $\tilde{Q} = Q \circledast \mathcal{N}(0, \sigma^2 \mathbf{I})$ . To establish our claim in the  
601 theorem statement, it suffices to exhibit a coupling  $\tilde{\gamma}$  of  $\tilde{P}$  and  $\tilde{Q}$  which samples a pair of random  
602 variables  $(\tilde{X}, \tilde{Y}) \sim \tilde{\gamma}$  such that:  $\Pr_{\tilde{\gamma}}[\tilde{X} \neq \tilde{Y}] \leq d_{\text{TV}}(P, Q) \cdot \frac{D}{2\sigma}$ . We define coupling  $\tilde{\gamma}$  as follows:

- 603 1. Sample  $(X, Y) \sim \gamma$  (as specified in Fact 1); then
- 604 2. sample  $(Z, Z') \sim \gamma_{X,Y}$  (as specified in Fact 3); then
- 605 3. output  $(\tilde{X}, \tilde{Y}) := (X + Z, Y + Z')$ .

606 Let us argue the following:

607 **Lemma C.3.** *The afore-described sampling procedure  $\tilde{\gamma}$  is a valid coupling of  $\tilde{P}$  and  $\tilde{Q}$ .*

608 *Proof.* We need to establish that the marginals of  $\tilde{\gamma}$  are  $\tilde{P}$  and  $\tilde{Q}$ . We will only show that for  
609  $(\tilde{X}, \tilde{Y}) \sim \tilde{\gamma}$  according to the afore-described sampling procedure, the marginal distribution of  $\tilde{X}$  is  
610  $\tilde{P}$ , as the proof for  $\tilde{Y}$  is identical. Since  $\gamma$  is a coupling of  $P$  and  $Q$ , for  $(X, Y) \sim \gamma$ , the marginal  
611 distribution of  $X$  is  $P$ . By Fact 3, conditioning on any value of  $X$  and  $Y$ , the marginal distribution of  
612  $Z$  is  $\mathcal{N}(0, \sigma^2 \mathbf{I})$ . Thus,  $\tilde{X} = X + Z$ , where  $X \sim P$  and independently  $Z \sim \mathcal{N}(0, \sigma^2 \mathbf{I})$ , and thus the  
613 distribution of  $\tilde{X}$  is  $\tilde{P}$ .  $\square$

614 **Lemma C.4.** *Under the afore-described coupling  $\tilde{\gamma}$ :  $\Pr_{\tilde{\gamma}}[\tilde{X} \neq \tilde{Y}] \leq d_{\text{TV}}(P, Q) \cdot \frac{D}{2\sigma}$ .*

615 *Proof.* Notice that, when  $X = Y$ , by Fact 3,  $Z = Z'$  with probability 1, and therefore  $\tilde{X} = \tilde{Y}$ . So  
616 for event  $\tilde{X} \neq \tilde{Y}$  to happen, it must be that  $X \neq Y$  happens and, conditioning on this event, that  
617  $X + Z \neq Y + Z'$  happens. By Fact 1,  $\Pr_{\gamma}[X \neq Y] = d_{\text{TV}}(P, Q)$ . By Fact 3, for any realization of  
618  $(X, Y)$ ,  $\Pr_{\gamma_{X, Y}}[X + Z \neq Y + Z'] = \frac{\|X - Y\|}{2\sigma} \leq \frac{D}{2\sigma}$ , where we used that  $P$  and  $Q$  are supported on  
619 a set with diameter  $D$ . Putting the above together, the claim follows.  $\square$

620  $\square$

### 621 C.3 Auxiliary Lemmas

622 **Lemma C.5** (Lipschitzness of the empirical density). *For a collection of points  $X^{(1)}, \dots, X^{(n)}$   
623 consider the function  $\hat{p}_{\sigma}(x) = \frac{1}{n\sigma} \sum_{i=1}^n \phi\left(\frac{X^{(i)} - x}{\sigma}\right)$ , where  $\phi(u) = \frac{1}{\sqrt{2\pi}} e^{-u^2/2}$  is the Gaussian  
624 kernel. Then  $p_{\sigma}$  is  $\left(\frac{1}{\sigma^2 \sqrt{2\pi e}}\right)$ -Lipschitz.*

625 *Proof.* Let us compute the derivative of  $\hat{p}_{\sigma}$ :

$$\hat{p}'_{\sigma}(x) = \frac{1}{n\sigma} \sum_{i=1}^n \frac{d}{dx} \phi\left(\frac{x - X^{(i)}}{\sigma}\right) \quad (\text{C.19})$$

$$= \frac{1}{\sqrt{2\pi} n \sigma} \sum_{i=1}^n \exp\left(-(X^{(i)} - x)^2 / (2\sigma^2)\right) \frac{X^{(i)} - x}{\sigma^2} \quad (\text{C.20})$$

$$\leq \frac{1}{\sqrt{2\pi} \sigma^2} \max_u \exp(-u^2/2) u \quad (\text{C.21})$$

$$\leq \frac{1}{\sigma^2 \sqrt{2\pi e}}. \quad (\text{C.22})$$

626  $\square$

627 **Lemma C.6** (Lipschitzness of a density convolved with a Gaussian). *Let  $p$  be a density that is  
628  $\lambda$ -Lipschitz. Let  $p_{\sigma} = p \otimes \mathcal{N}(0, \sigma^2 I)$ . Then,  $p_{\sigma}$  is also  $\lambda$ -Lipschitz.*

629 *Proof.* Let us denote with  $\phi_{\sigma}(\cdot)$  the Gaussian density with variance  $\sigma^2$ . We have that:

$$p_{\sigma}(x) - p_{\sigma}(y) = \int (p(x - \tau) - p(y - \tau)) \phi_{\sigma}(\tau) d\tau \Rightarrow \quad (\text{C.23})$$

$$|p_{\sigma}(x) - p_{\sigma}(y)| \leq \int |p(x - \tau) - p(y - \tau)| \phi_{\sigma}(\tau) d\tau \quad (\text{C.24})$$

$$\leq \lambda |x - y| \cdot \int \phi_{\sigma}(\tau) d\tau \quad (\text{C.25})$$

$$= \lambda |x - y|. \quad (\text{C.26})$$

630  $\square$

## 631 D Additional Results

### 632 D.1 CIFAR-10 controlled corruptions

633 Figures 5a, 5b and 6 show gaussian blur, motion blur, and JPEG corrupted CIFAR-10 images  
634 respectively at different levels of severity. Appendix Table 3 shows results for JPEG compressed  
635 data at different levels of compression. We also tested our method for motion blurred data with high  
636 severity, visualized in the last row of Appendix Figure 6), obtaining a best FID of 5.85 (compared to  
637 8.79 of training on only the clean data).



(a) CIFAR-10 images corrupted with blur at increasing levels ( $\sigma_B = 0.4, 0.6, 1.0$ ).



(b) CIFAR-10 images corrupted with JPEG at compression rates: 25%, 18%, 15% respectively.

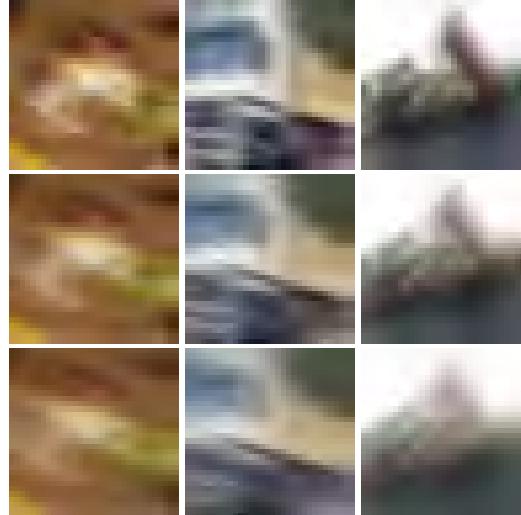
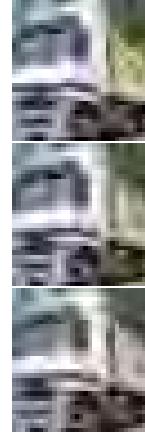


Figure 6: CIFAR-10 images corrupted with motion blur at increasing levels of corruption.

## 638 D.2 FFHQ-64x64 controlled corruptions

639 In Appendix 4 we show additional results for learning from blurred data on the FFHQ dataset.  
640 Similarly to the main paper, we observe that our Ambient-o algorithm leads to improvements over  
641 just using the high-quality data that are inversely proportional to the corruption level.

## 642 D.3 ImageNet results

643 In the main paper, we used FID as a way to measure the quality of generated images. However, FID  
644 is computed with respect to the test dataset that might also have samples of poor quality. Further,  
645 during FID computation, quality and diversity are entangled. To disentangle the two, we generate  
646 images using the EDM-2 baseline and our Ambient-o model and we use CLIP to evaluate the quality  
647 of the generated image (through the CLIP-IQA metric implemented in the PIQ package [38, 37]). We  
648 present results and win-rates in Table 5. As shown, Ambient-o achieves a better per-image quality  
649 compared to the baseline despite using exactly the same model, hyperparameters, and optimization  
650 algorithm. The difference comes solely from better use of the available data.

Table 3: Results for learning from JPEG compressed data on CIFAR-10.

Method	Dataset	Clean (%)	Corrupted (%)	JPEG Compression (Q)	$\bar{\sigma}_{t_n}^{\min}$	FID
<b>Only Clean</b>	Cifar-10	10	0	—	—	8.79
<b>Ambient Omni</b>	Cifar-10	10	90	15%	1.60	6.67
				18%	1.40	6.43
				25%	1.27	6.34
				50%	1.03	5.94
				75%	0.81	5.57
				90%	0.63	4.72

Table 4: Results for learning from blurred data, FFHQ.

Method	Dataset	Clean (%)	Corrupted (%)	Parameters Values ( $\sigma_B$ )	$\bar{\sigma}_{t_n}^{\min}$	FID
<b>Only Clean</b>	FFHQ	10	0	-	-	5.12
<b>Ambient Omni</b>	FFHQ	10	90	0.8	2.89	4.95

## 651 E Ambient diffusion implementation details and loss ablations

652 Similar to the EDM-2 [35] paper, we use a pre-condition weight to balance the importance of different  
 653 diffusion times. Specifically, we modulate the EDM2 weight  $\lambda(\sigma)$  by a factor:

$$\lambda_{\text{amb}}(\sigma, \sigma_{\min}) = \sigma^4 / (\sigma^2 - \sigma_{\min}^2)^2 \quad (\text{E.1})$$

654 for our ambient loss based on a similar analysis to [35]. We further use a buffer zone around the  
 655 annotation time of each sample to ensure that the loss doesn't have singularities due to divisions by 0.  
 656 We ablate the precondition term and the buffer size in Appendix Table 6.

657 For our ablations, we focus on the setting of training with 10% clean data and 90% corrupted data  
 658 with Gaussian blur of  $\sigma_B = 0.6$ . Using no ambient pre-conditioning and no buffer, we obtain an  
 659 FID of 5.56. In the same setting, adding the ambient pre-conditioning weight  $\lambda_{\text{amb}}(\sigma, \sigma_{\min})$  improves  
 660 FID by 0.13 points. Next, we ablate two strategies to mitigate the impact of the singularity of  
 661  $\lambda_{\text{amb}}(\sigma, \sigma_{\min})$  at  $\sigma = \sigma_{\min}$ . The first strategy clips the ambient pre-conditioning weight at a specified  
 662 maximum value  $\lambda_{\text{amb}}^{\text{MAX}}$ , but still trains for  $\sigma$  arbitrarily close to  $\sigma_{\min}$ . The second strategy also specifies  
 663 a maximum value, but imposes a buffer

$$\sigma > \sqrt{1 + \frac{1}{\lambda_{\text{amb}}^{\text{MAX}} - 1} \sigma_{\min}} \quad (\text{E.2})$$

664 that restricts training to noise levels  $\sigma$  such that  $\lambda_{\text{amb}}(\sigma, \sigma_{\min}) \leq \lambda_{\text{amb}}^{\text{MAX}}$ . Clipping the ambient weight  
 665 to  $\lambda_{\text{amb}}^{\text{MAX}} = 2.0$  minimally improves FID to 5.35, but clipping to 4.0 significantly worsens it to  
 666 5.69. Adding a buffer at  $\lambda_{\text{amb}}^{\text{MAX}} = 2.0$  slightly worsens FID to 5.40, but slackening the buffer to 4.0  
 667 minimally improves FID to 5.34. We opt for the buffering strategy in favor of the clipping strategy  
 668 since performance appears convex in the buffer parameter, and because it obtains the best FID.

## 669 F Annotation ablations

670 We ablate the choice of using a fixed annotation vs sample-adaptive annotations in Appendix Table  
 671 7. We find that using sample-adaptive annotations achieves improved results. Nevertheless, both  
 672 annotation methods yield improvements over the training on filtered data and the training on every-  
 673 thing baselines. To show that our method works for more corruption types, we perform an equivalent  
 674 experiment with JPEG compressed data at different compression ratios and we achieve similar results,  
 675 presented in Appendix Table 3. We ablate the impact of the amount of training data and the number  
 676 of training iterations on the classifier annotations in Appendix Section F. We show results for motion  
 677 blur (Figure 6 and Section D.1) and for the FFHQ dataset (Table 4).

Table 5: Additional comparison between EDM-2 XXL and our Ambient-o model using the CLIP IQA metric for image quality assesment. Ambient-o leads to improved scores despite using the exact same architecture, data and hyperparameters. For this experiment, we use the models with guidance optimized for DINO FD since they are the ones producing the higher quality images.

Metric	EDM-2 [35] XXL	Ambient-o XXL crops
Average CLIP IQA score	0.69	<b>0.71</b>
Median CLIP IQA score	0.79	<b>0.80</b>
Win-rate	47.98%	<b>52.02%</b>

Table 6: Ablation study of ambient weight and stability buffer on Cifar-10 with 10% clean data and 90% corrupted data with blur of 0.6.

Method	FID $\downarrow$
<i>No ambient preconditioning weight and no buffer:</i>	
$\lambda_{\text{amb}}(\sigma, \sigma_{\min}) = 1 \& \sigma > \sigma_{\min}$	5.49
<i>Adding ambient preconditioning weight:</i>	
+ Weight $\lambda_{\text{amb}}(\sigma, \sigma_{\min}) = \sigma^4 / (\sigma^2 - \sigma_{\min}^2)^2$	5.36
<i>Adding stability buffer/clipping:</i>	
+ Clip $\lambda_{\text{amb}}(\sigma, \sigma_{\min})$ at 2.0	5.35
+ Clip $\lambda_{\text{amb}}(\sigma, \sigma_{\min})$ at 4.0	5.69
+ Buffer $\lambda_{\text{amb}}(\sigma, \sigma_{\min})$ at 2.0 i.e. $\sigma > \sqrt{2}\sigma_{\min}$	5.40
+ Buffer $\lambda_{\text{amb}}(\sigma, \sigma_{\min})$ at 4.0 i.e. $\sigma > (2/\sqrt{3})\sigma_{\min}$	<b>5.34</b>

678 **Balanced vs unbalanced data:** We ablate the impact of classifier training data on the setting of  
679 CIFAR-10 with 10% clean data and 90% corrupted data with gaussian blur with  $\sigma_B = 0.6$ . When  
680 annotating with a classifier trained on the same unbalanced dataset we train the diffusion model on  
681 we obtained a best FID of 6.04, compared to the 5.34 obtained if we train on a balanced dataset.

682 **Training iterations:** We ablate the impact of classifier training iterations on the setting of CIFAR-10  
683 with 10% clean data and 90% corrupted data with JPEG compression at compression rate of 18%,  
684 training the classifier with a balanced dataset. We report minute variations in the best FID, obtaining  
685 6.50, 6.58, and 6.49 when training the classifier for 5e6, 10e6, and 15e6 images worth of training  
686 respectively.

Table 7: Comparison with baselines for training with data corrupted by Gaussian Blur at different levels. The dataset used in this experiment is CIFAR-10.

Method	Clean (%)	Corrupted (%)	Parameters Values ( $\sigma_B$ )	$\bar{\sigma}_{t_n}^{\min}$	FID
<b>Only Clean</b>	10	0	-	-	8.79
<b>No annotations</b>	10	90	1.0		45.32
			0.8		28.26
			0.4	0	2.47
<b>Single annotation</b>	10	90	1.0	2.32	6.95
			0.8	1.89	6.66
			0.4	0.00	2.47
<b>Classifier annotations</b>	10	90	1.0	2.84	6.16
			0.8	1.93	6.00
			0.4	0.22	2.44

687 **G Training Details**

688 **G.1 Formation of the high-quality and low-quality sets.**

689 In the theoretical problem setting we assumed the existence of a good set  $S_G$  from the clean  
690 distribution and a bad set  $S_B$  from the corrupted distribution. In practice, we do not actually possess  
691 these sets initially, but we can construct them so long as we have access to a measure of "quality".  
692 Given a function on images which tells us whether its good enough to generate or not e.g. CLIP-IQA  
693 quality [66] greater than some threshold, we can define our good set  $S_G$  as the good enough images  
694 and  $S_B$  as the complement. From this point on we can apply the methodology of ambient-o as  
695 developed, either employing classifier annotations as in our pixel diffusion experiments, or fixed  
696 annotations as in our large scale ImageNet and text-to-image experiments.

697 **G.2 Datasets**

698 **CIFAR-10.** CIFAR-10 [42] consists of 60,000 32x32 images of ten classes (airplane, automobile,  
699 bird, cat, deer, dog, frog, horse, ship, and truck).

700 **FFHQ.** FFHQ [36] consists of 70,000 512x512 images of faces from Flickr. We used the dataset at  
701 64x64 resolution for our experiments.

702 **AFHQ.** AFHQ [12] consists of 5,653 images of cats, 5,239 images of dogs and 5,000 images of  
703 wildlife, for a total of 15,892 images.

704 **ImageNet.** ImageNet [20] consists of 1,281,167 images of variable resolution from 1000 classes.

705 **Conceptual Captions.** Conceptual Captions [56] consists of 12M (image url, caption) pairs.

706 **Segment Anything.** Segment Anything [41] consists of 11.1M high-resolution images annotated  
707 with segmentation masks. Since the original dataset did not have real captions, we use the same  
708 LLaVA generated captions created by the MicroDiffusion [54] paper.

709 **JourneyDB.** JourneyDB consists of 4.4M synthetic image-caption pairs from Midjourney [63].

710 **DiffusionDB.** DiffusionDB consists of 14M synthetic image-caption pairs, mostly generated from  
711 Stable Diffusion models [70]. We use the same 10.7M quality-filtered subset created by the MicroD-  
712 iffusion paper [54].

713 **G.3 Diffusion model training**

714 **CIFAR-10.** We use the EDM [34] codebase as a reference to train class-conditional diffusion  
715 models on CIFAR-10. The architecture is a Diffusion U-Net [60] with ~55M parameters. We use  
716 the Adam optimizer [40] with learning rate 0.001, batch size 512, and no weight decay. While the  
717 original EDM paper trained for  $200 \times 10^6$  images worth of training, when training with corrupted  
718 data we saw best results around  $20 \times 10^6$  images. On a single 8xV100 node we achieved a throughput  
719 of 0.8s per 1k images, for an average of 4.4h per training run.

720 **FFHQ.** Same as for CIFAR-10, except learning was set to  $2e - 4$ , we trained for a maximum of  
721  $100 \times 10^6$  images worth of training, and saw best results around  $30 \times 10^6$  images worth.

722 **AFHQ.** Same as FFHQ.

723 **ImageNet.** We use the EDM2 [35] codebase as a reference to train class-conditional diffusion  
724 models on ImageNet. The architecture is a Diffusion U-Net [60] with ~125M parameters. We use  
725 the Adam optimizer [40] with reference learning rate 0.012, batch size 2048, and no weight decay.  
726 Same as the original codebase, we trained for ~2B worth of images. On 32 H200 GPUs, XS models  
727 took ~3 days to train, while XXL models took ~7 days.

728 **MicroDiffusion.** We use the MicroDiffusion codebase [54] as a reference to train text-to-image  
 729 models on an academic budget. We follow their recipe exactly, changing only the standard denoising  
 730 diffusion loss to the ambient diffusion loss. The architecture is a Diffusion Transformer [50] utilizing  
 731 Mixture-of-Experiments (MoE) feedforward layers [57, 31], with  $\sim 1.1\text{B}$  parameters. We use the  
 732 AdamW optimizer [40] with reference learning rates  $2.4e-4$  /  $8e-5$  /  $8e-5$  /  $8e-5$  for each of the  
 733 four phases and batch size 2048 for all phases. On 8 H200 GPUs, training takes  $\sim 2$  days to train.

734 **G.4 Classifier training**

735 Classifier training is done using the same optimization recipe (optimizer, learning rate, batch size,  
 736 etc.) as diffusion model training, except we change the architecture to an encoder-only "Half-Unet",  
 737 simply by removing the decoder half of the original UNet architecture. The training of the classifier  
 738 is substantially shorter compared to the diffusion training since classification is task is easier than  
 739 generation.

740 **H Additional Figures**

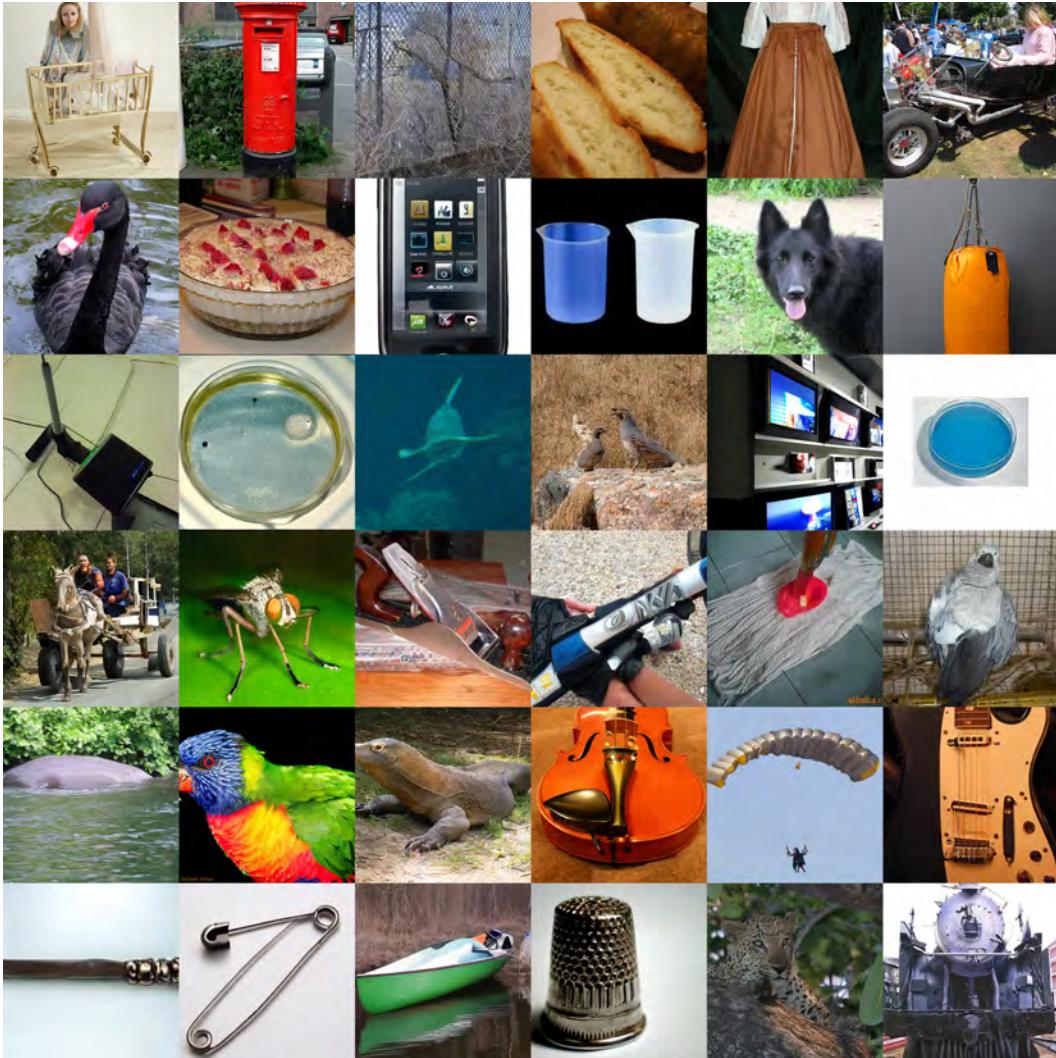


Figure 7: Uncurated generations from our Ambient-o XXL model trained on ImageNet.

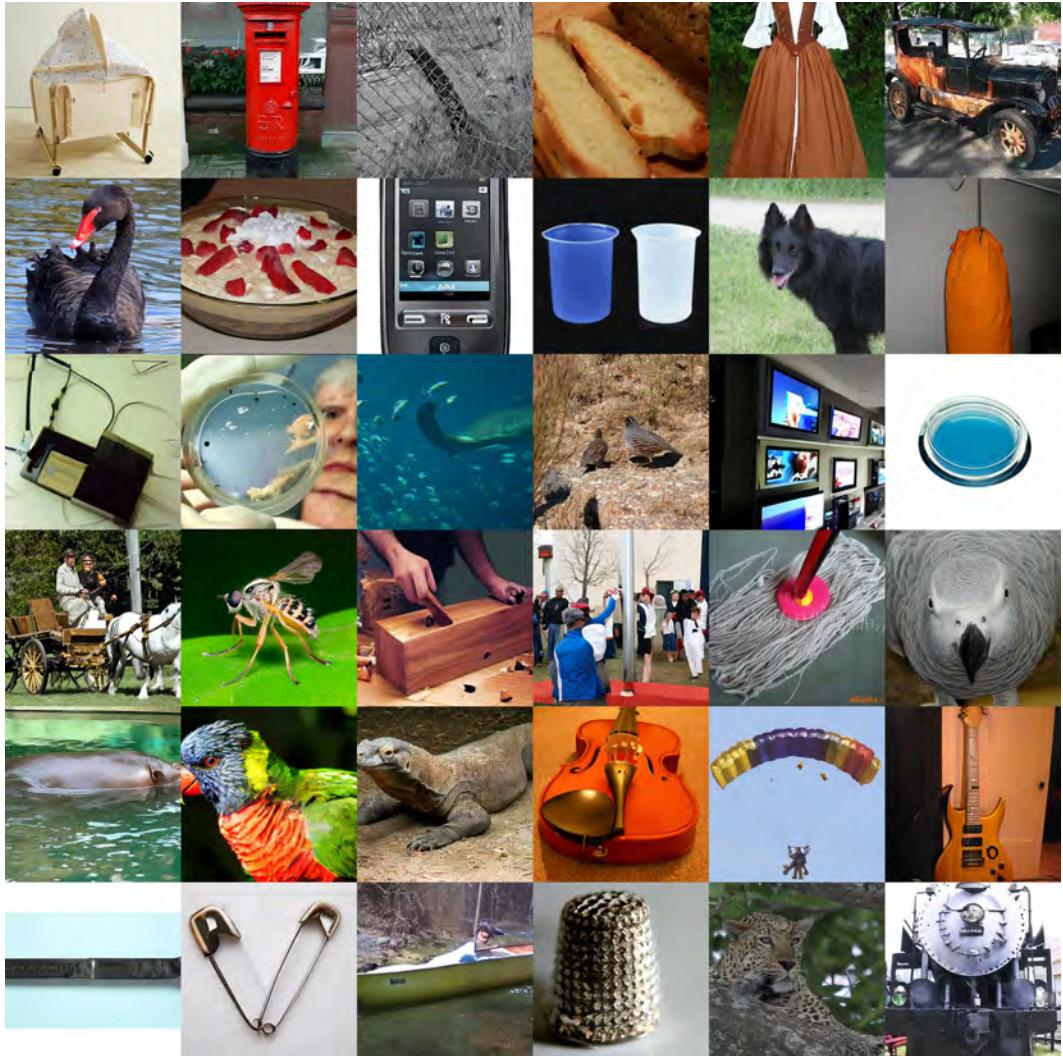


Figure 8: Uncurated generations from our Ambient-o+crops XXL model trained on ImageNet.

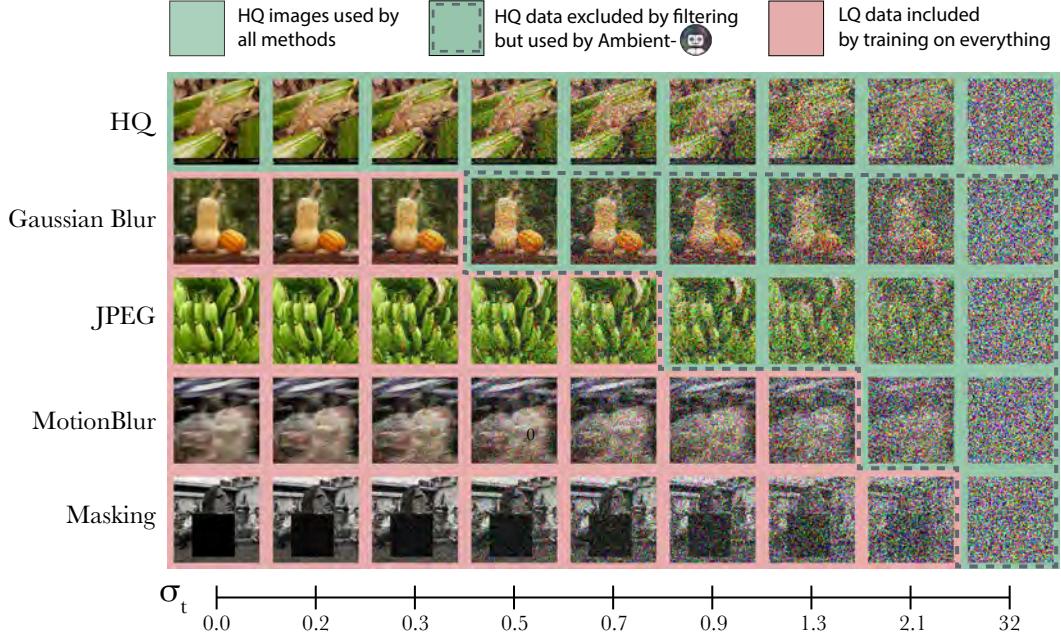


Figure 9: **Visual summary of our method for using low-quality data at high-noise.** We see how the various corrupted images become indistinguishable from the High Quality (HQ) after a minimum noise level. These noisy versions of Low Quality (LQ) images are actually high-quality data, which filtering approaches discard, but Ambient Omni uses.

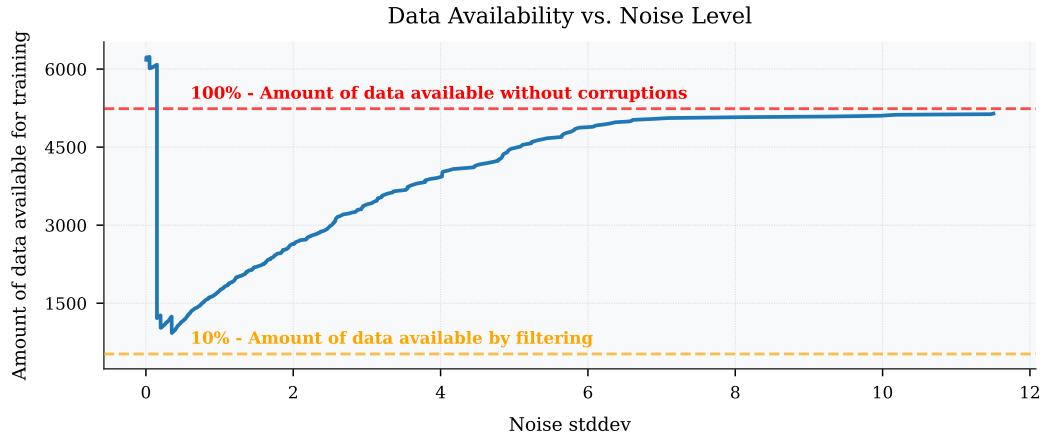


Figure 10: Amount of samples available at each noise level when training a generative model for dogs in the following setting: (1) we have 10% of the dogs dataset uncorrupted, (2) we have the other 90% of the dogs dataset corrupted with gaussian blur with  $\sigma_B = 0.6$ , and (3) we have 100% of the clean dataset of cats. At low noise levels, we can train on both the high quality dogs and a lot of the cats, resulting in  $> 100\%$  of samples available relative to the original dogs dataset size. As the noise level starts to increase, we stop being able to use the out-of-distribution cat samples, but start gaining some blurry dog samples. As the noise level approaches the maximum all the blurry dogs become available for training, such that the amount of data available approaches 100%.

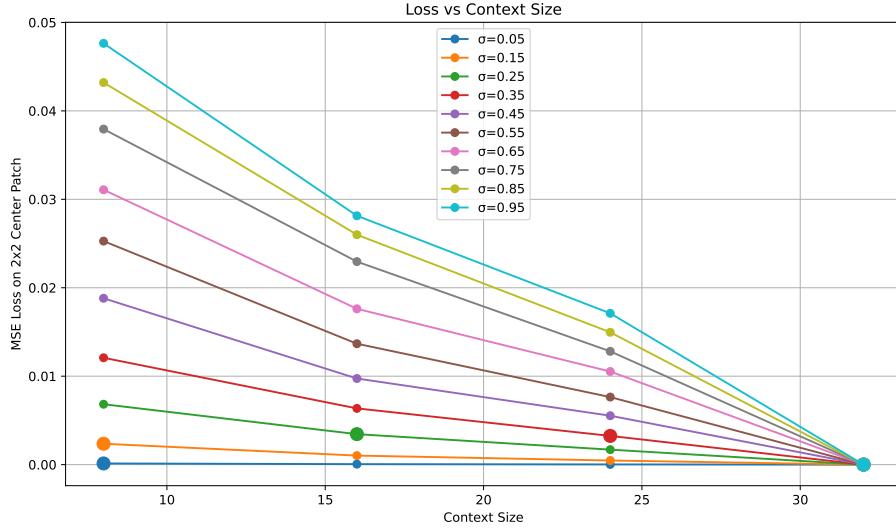


Figure 11: ImageNet-512x512: denoising loss of an optimally trained model, measured at  $2 \times 2$  center patch, as we increase the context size given to the model (horizontal axis) and the noise level (different curves). As expected, for higher noise, more context is needed for optimal denoising. The large dot on each curve marks the point where the loss nearly plateaus.

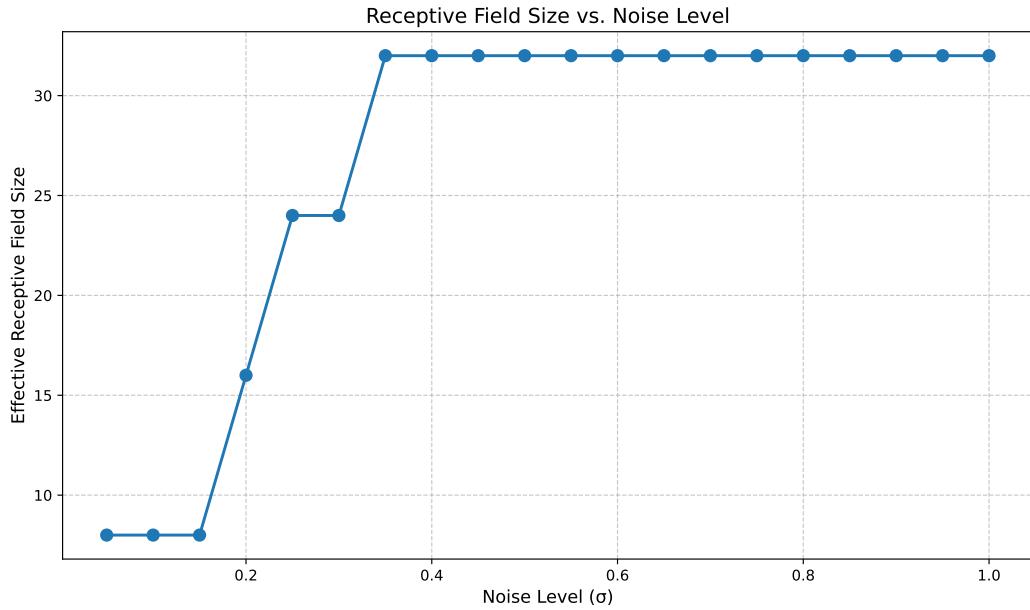


Figure 12: ImageNet-512x512: context size needed to be within  $\epsilon = 1e - 3$  of the optimal loss for different noise levels. As expected, for higher noise, more context is needed for optimal denoising.

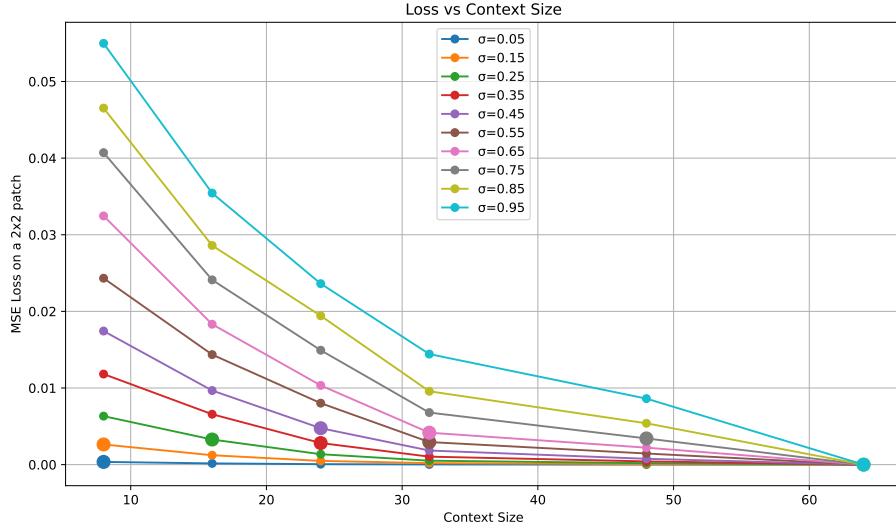


Figure 13: FFHQ: denoising loss of an optimally trained model, measured at  $2 \times 2$  center patch, as we increase the context size given to the model (horizontal axis) and the noise level (different curves). As expected, for higher noise, more context is needed for optimal denoising. The large dot on each curve marks the point where the loss nearly plateaus.

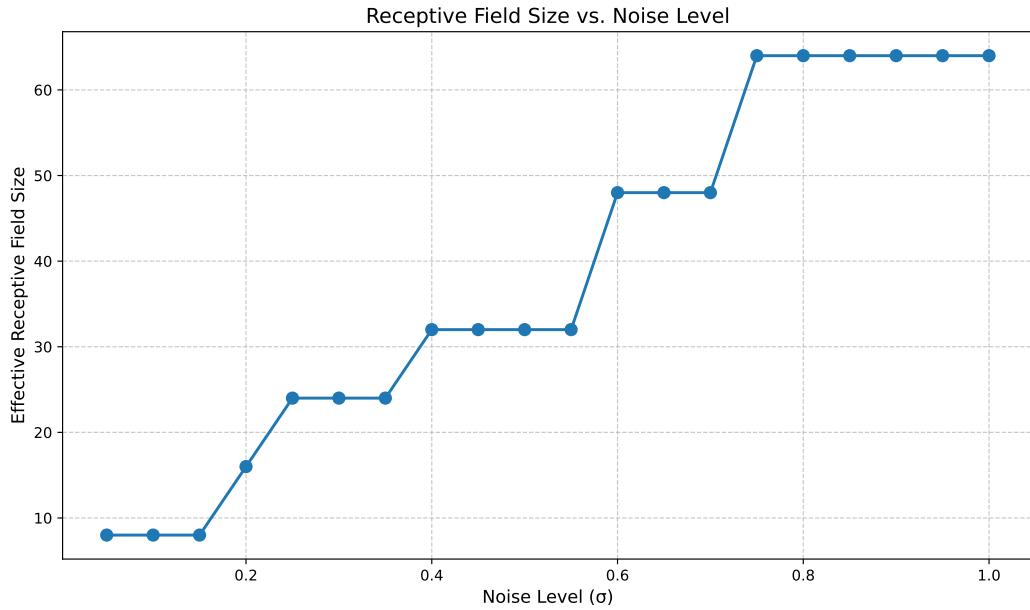


Figure 14: FFHQ: context size needed to be within  $\epsilon = 1e - 3$  of the optimal loss for different noise levels. As expected, for higher noise, more context is needed for optimal denoising.

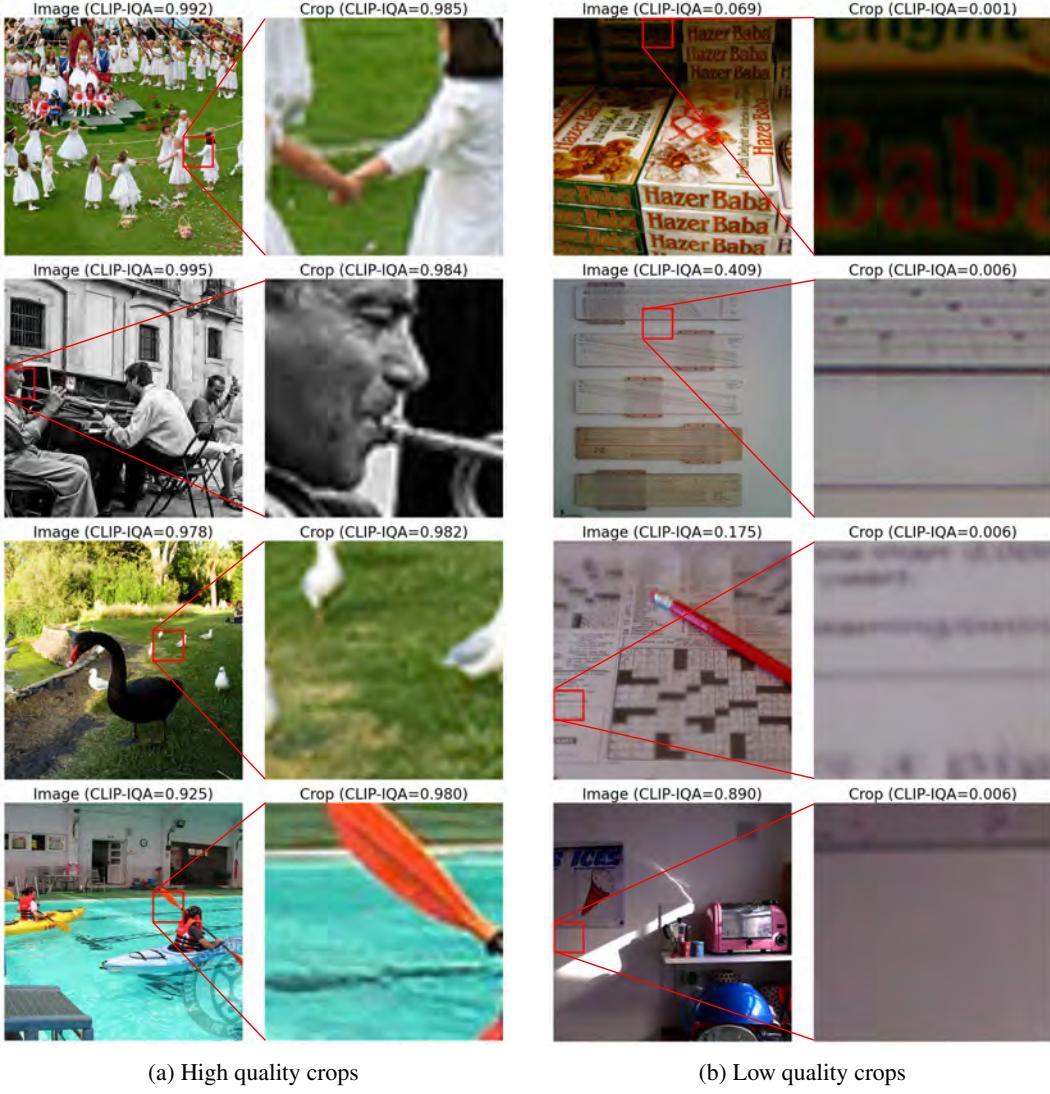


Figure 15: Results using CLIP to find (a) high-quality and (b) low-quality crops on ImageNet.

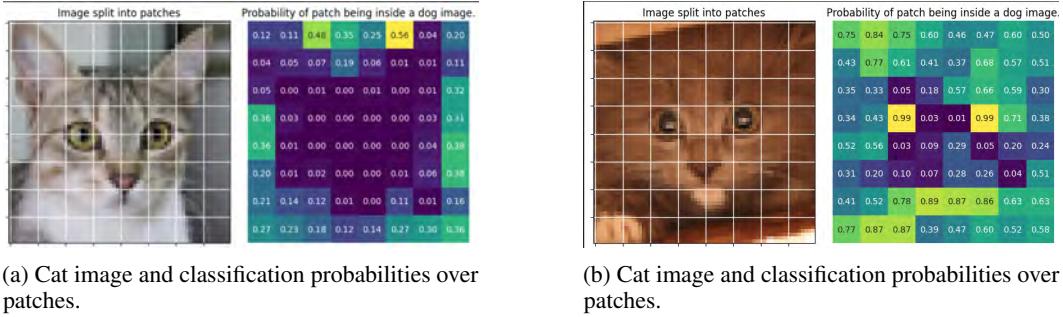
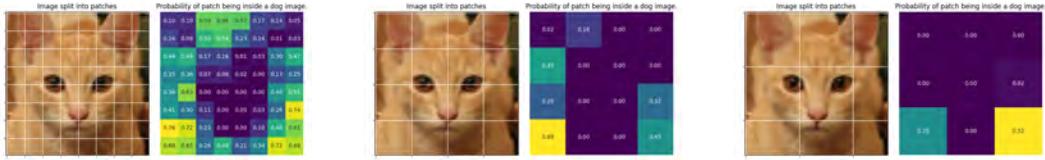


Figure 16: Two examples of cats from the AFHQ dataset. We partition each cat into non overlapping patches and we compute the probabilities of the patch belonging to an image of a dog using a cats vs dogs classifier trained on patches. The cat on the right has a lot more patches that could belong to a dog image according to the classifier, possibly due to the color or the texture of the fur.



(a) Cat annotated by a cats vs. dogs classifier that operates with crops of size 8.

(b) Cat annotated by a cats vs. dogs classifier that operates with crops of size 16.

(c) Cat annotated by a cats vs. dogs classifier that operates with crops of size 24.

Figure 17: Patch-based annotations of a cat image from AFHQ using cats vs. dogs classifiers trained on different patch sizes.

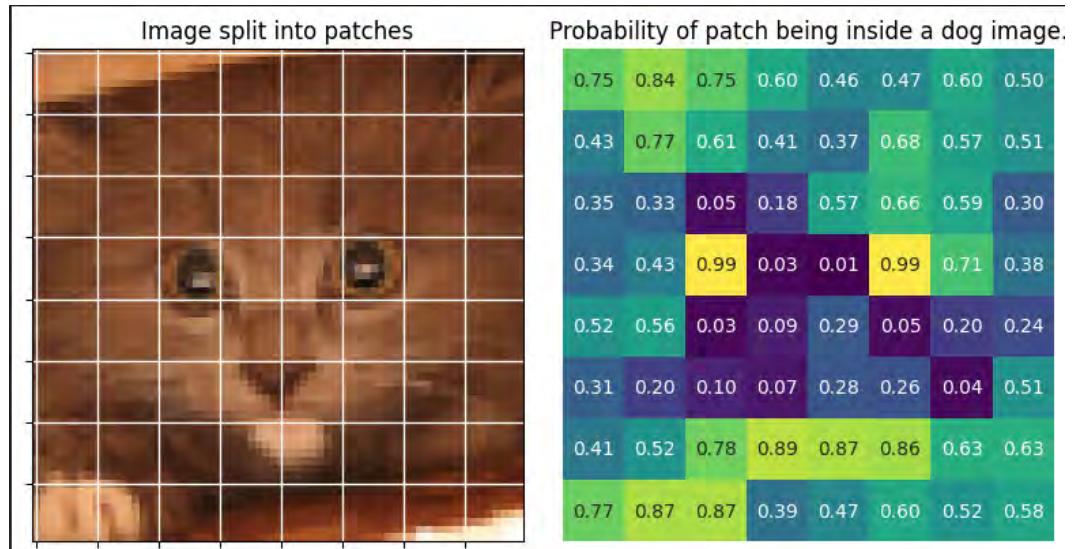


Figure 18: Patch level probabilities for dogness in a cat image.

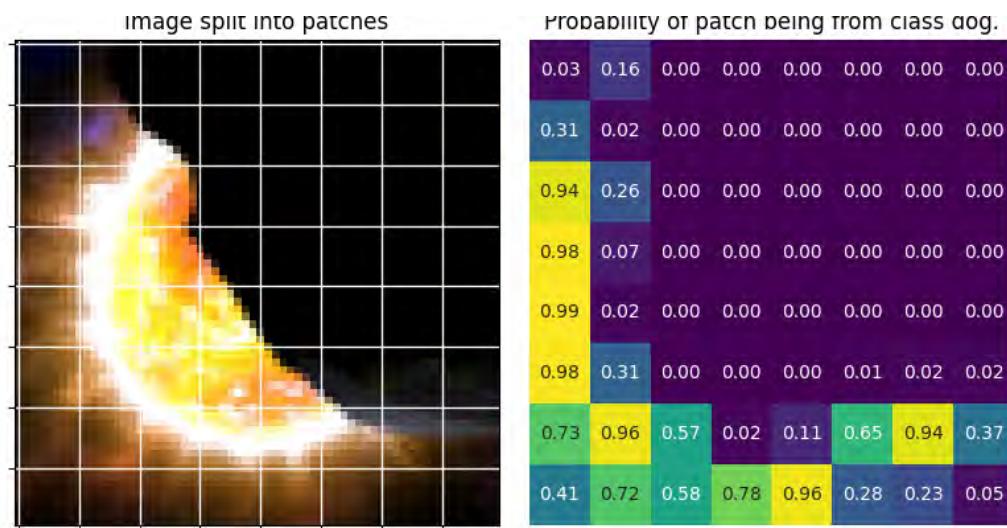
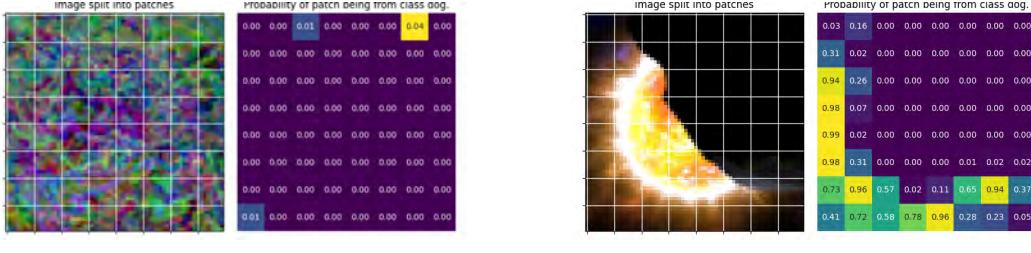


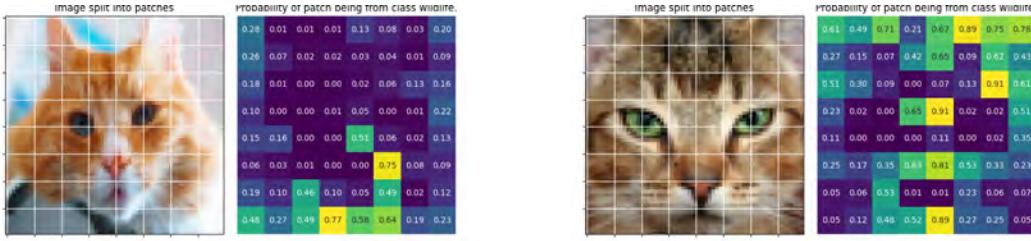
Figure 19: Patch level probabilities for dogness in a synthetic image (procedural program). The cat has more useful patches than this non-realistic procedural program.



(a) Synthetic image and classification probabilities over patches.

(b) Synthetic image and classification probabilities over patches.

Figure 20: Two examples of procedurally generated images. We partition each image into non overlapping patches and we compute the probabilities of the patch belonging to an image of a dog using a synthetic image vs dogs classifier trained on patches. The image on the right has a lot more patches that could belong to a dog image according to the classifier, possibly due to the color or the texture.



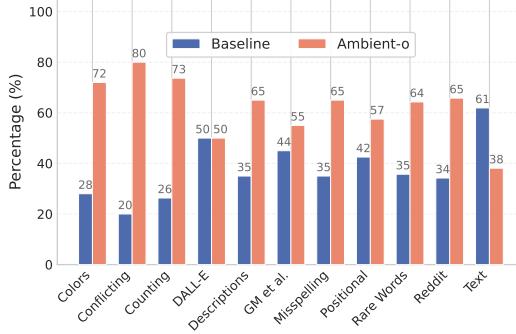
(a) Cat image and classification probabilities over patches.

(b) Cat image and classification probabilities over patches.

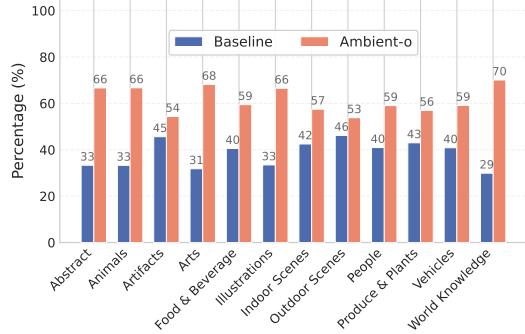
Figure 21: Two examples of cat images. We partition each image into nonoverlapping patches and we compute the probabilities of the patch belonging to an image of wildlife using a cats vs wildlife classifier trained on patches. The image on the right has a lot more patches that could belong to a wildlife image according to the classifier, possibly due to the color or the texture.



Figure 22: Example batch.



(a) DrawBench

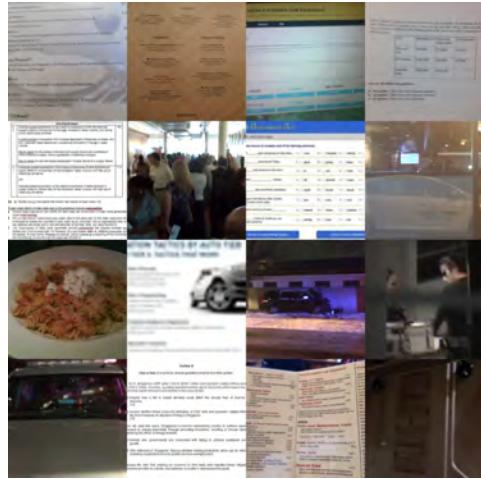


(b) PartiPrompts

Figure 23: Assessing image quality with GPT-4o on DrawBench and PartiPrompts.



(a) Highest quality images from CC12M according to CLIP.

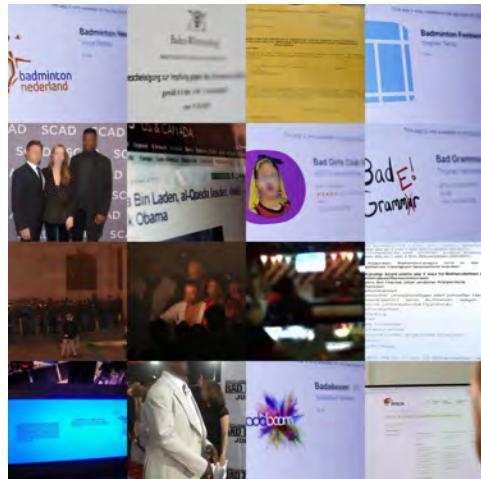


(b) Lowest quality images from CC12M according to CLIP.

Figure 24: CLIP annotations for quality of images from CC12M.



(a) Highest quality images from SA1B according to CLIP.

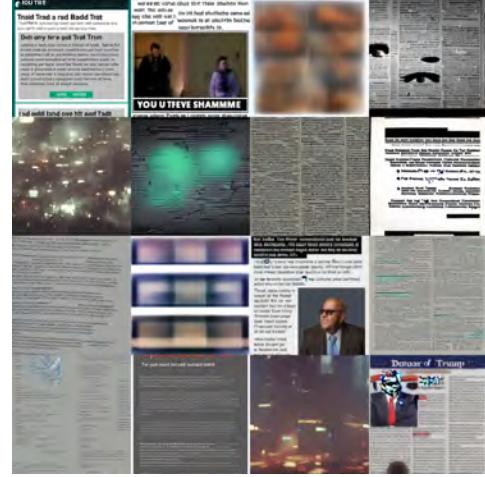


(b) Lowest quality images from SA1B according to CLIP.

Figure 25: CLIP annotations for quality of images from SA1B.



(a) Highest quality images from DiffDB according to CLIP.



(b) Lowest quality images from DiffDB according to CLIP.

Figure 26: CLIP annotations for quality of images from DiffDB.



(a) Highest quality images from JDB according to CLIP.



(b) Lowest quality images from JDB according to CLIP.

Figure 27: CLIP annotations for quality of images from JDB.

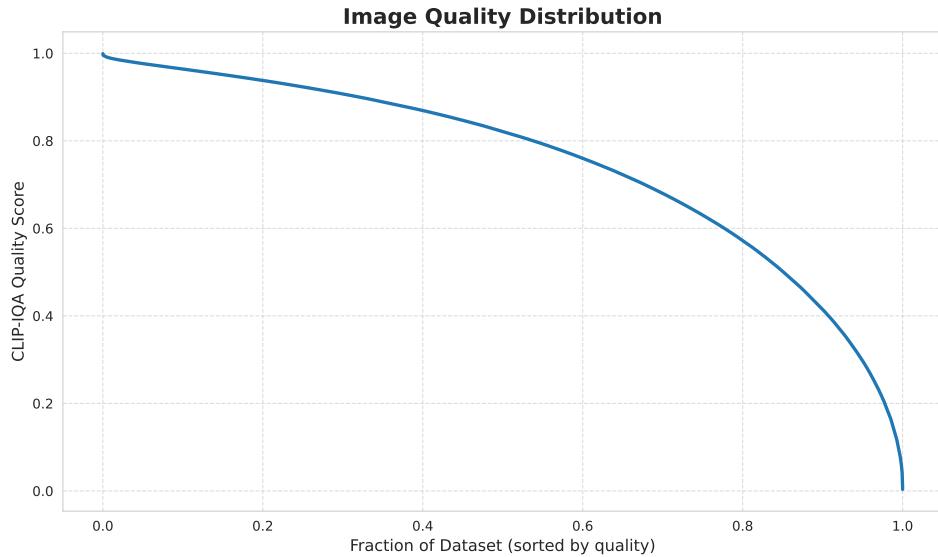


Figure 28: Distribution of image qualities according to CLIP for ImageNet-512.



Figure 29: **Examples of mode collapse.** Left: baseline model finetuned on a high-quality subset. Right: Ambient-o model using all the data. As shown, finetuning decreases output diversity.

741 **NeurIPS Paper Checklist**

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743 Question: Do the main claims made in the abstract and introduction accurately reflect the  
744 paper's contributions and scope?

745 Answer: **[Yes]**

746 Justification: Our method does not use any information about the type of corruption, and  
747 our experiments show it generalizes to low quality data found in the wild, not just a few  
748 artificially controlled corruptions.

749 Guidelines:

- 750 • The answer NA means that the abstract and introduction do not include the claims  
751 made in the paper.
- 752 • The abstract and/or introduction should clearly state the claims made, including the  
753 contributions made in the paper and important assumptions and limitations. A No or  
754 NA answer to this question will not be perceived well by the reviewers.
- 755 • The claims made should match theoretical and experimental results, and reflect how  
756 much the results can be expected to generalize to other settings.
- 757 • It is fine to include aspirational goals as motivation as long as it is clear that these goals  
758 are not attained by the paper.

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760 Question: Does the paper discuss the limitations of the work performed by the authors?

761 Answer: **[Yes]**

762 Justification: We openly discuss the limitations of our approach, such as:

- 763 (a) The high and low quality distributions never *perfectly* merge, so our method always  
764 introduces a (small) distribution error compared to filtering.
- 765 (b) Our method does not work well with certain corruption types, such as masking. These  
766 "ill-suited" corruptions require a very large amount of noise to merge, such that they  
767 are effectively never used during training and our method reduces to filtering in these  
768 cases.

769 Guidelines:

- 770 • The answer NA means that the paper has no limitation while the answer No means that  
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775 model well-specification, asymptotic approximations only holding locally). The authors  
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798 a complete (and correct) proof?

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800 Justification: Our theorems include all premises and assumptions used to prove the result.  
801 Informal proofs are found in the main text, referencing formal proofs in the appendix.

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805 referenced.
- 806 • All assumptions should be clearly stated or referenced in the statement of any theorems.
- 807 • The proofs can either appear in the main paper or the supplemental material, but if  
808 they appear in the supplemental material, the authors are encouraged to provide a short  
809 proof sketch to provide intuition.
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- 812 • Theorems and Lemmas that the proof relies upon should be properly referenced.

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819 produce our experiments is included in the paper (either in the main text or the appendix).  
820 Additionally, we will make the training and evaluation code public after acceptance of the  
821 paper.

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830 For example, if the contribution is a novel architecture, describing the architecture fully  
831 might suffice, or if the contribution is a specific model and empirical evaluation, it may  
832 be necessary to either make it possible for others to replicate the model with the same  
833 dataset, or provide access to the model. In general, releasing code and data is often  
834 one good way to accomplish this, but reproducibility can also be provided via detailed  
835 instructions for how to replicate the results, access to a hosted model (e.g., in the case  
836 of a large language model), releasing of a model checkpoint, or other means that are  
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