576 A Preliminaries on Autoregressive Transformers

For **Perplexity.** Perplexity is a widely used metric for evaluating language models which encapsulates how well the model can predict a word. Formally, perplexity of a language model M is derived using the entropy formula as:

$$Perplexity(M) = 2^{H(L,M)} = 2^{-\sum_{x} L(x).log(M(x)))}$$
(1)

where L represents the ground-truth words. As seen, the perplexity is closely tied with the crossentropy loss of the model, i.e., H(L, M).

Parameter count. Contemporary autoregressive Transformer architectures can be divided into 582 three main components, namely, the input embedding layer, hidden layers, and the final (softmax) 583 projection layer. The embedding head often comprises look-up table based modules which map the 584 input language tokens to vectors. These vectors then enter a stack of multiple hidden layers a.k.a, the 585 decoder blocks. Each decoder block is made up of an attention layer and a feed-forward network. 586 Once the features are extracted by the stack of decoder blocks, the final prediction is generated 587 by passing through a final softmax projection layer. When counting the number of parameters in 588 an autoregressive Transformer, the total parameters enclosed in the hidden layers is dubbed the 589 590 decoder parameter count or equivalently, the non-embedding parameter count. These parameters are architecture dependent and do not change based on the underlying tokenization or the vocabulary 591 size. The embedding parameter count, however, accounts for the parameters enclosed in the input 592 593 embedding layer as well as the final softmax projection layer as they are both closely tied to the word embedding and vocabulary size. We visualize an autoregressive Transformer in Figure 17, where the 594 orange blocks contain the decoder parameters and grey blocks hold the embedding parameters. 595

596 **B** Experimental Setup

597 Datasets. We conduct experiments on two datasets, WikiText-103 and LM1B. The datasets are 598 tokenized using word-level and byte-pair encoding for models with Transformer-XL and GPT-2 599 backbones, respectively.

Training Setup. We adopt the open-source code by **[12]** and **[24]** to implement the GPT-2 and 600 Transformer-XL backbones, respectively. Table 2 encloses the hyperparameters used for training. We 601 follow the training hyperparameters, i.e., batch size, optimizer, learning rate values and scheduler, 602 provided in NVIDIA's open-source repository [24]. For each backbone and dataset, we use the same 603 training setup for all models generated by NAS. While hyperparameter optimization (HPO) is an 604 important and active area of research, due to the extremely high cost of NAS + HPO, the vast majority 605 606 of papers in NAS, including popular benchmarks [9, 28, 48], use the same training hyperparameters for all models. The setup for our training hyperparameters is also based on the evidence provided in 607 prior art in Transformer design [17, 27, 14] and NAS [38, 52, 6]. Specifically, for the range of model 608 sizes studied in this paper, prior work adopts the same batch size (see Table 2.1 in GPT-3 [3]), which 609 suggests there is no significant benefit in optimizing the batch size per architecture. The original 610 GPT-3 paper [3] also adopts the same learning rate scheduler for all models, regardless of their size. 611 Similarly, Authors of [17] show that the choice of learning rate scheduler does not have a significant 612 effect on final model performance, which further validates that exploration of the scheduler will not 613 alter the empirical findings in this paper. 614

Authors of [17] further provide a rule-of-thumb for setting the optimal learning rate (see Equation 615 D.1 of [17]). Adopting this rule shows that the changes in the value of the optimal learning rate 616 are negligible for the range of model sizes in our search space. We validate this by conducting an 617 experiment which aims to find the optimal learning rate per architecture. We sweep the learning rate 618 in the range [0.0001, 0.001, 0.01, 0.1] for 100 randomly sampled models from the GPT-2 backbone 619 and train them on WikiText103. The studied models span a wide range of configurations with 2 620 to 16 layers and 2M to 65M total parameters. We then pick the optimal learning rate for each 621 architecture, i.e., the one which results in the lowest perplexity. We remeasure the correlation between 622 newly obtained perplexities and the decoder parameter county proxy. Our learning rate optimization 623 experiment results in two important observations: 1) for the vast majority of the architectures (98%), 624 the optimal learning rate is equal to 0.01, i.e., the value used in all experiments (see Table 2), and 2) 625 the ranking of architectures after convergence remains largely unchanged, leading to a correlation 626 of 0.93 with decoder parameter count, compared to 0.96 when using the same learning rate for all 627

models. The above evidence suggests that the same training setup can be used for all architectures in the search-space, without affecting the results.

In this paper, each model is trained separately from scratch. In many scenarios, the user only needs to train one model from the Pareto-frontier, which is selected based on their needs for perplexity, latency, and memory. However, if the users are interested in multiple models, they can either train all models separately or create a supergraph enclosing all such configurations and train them all simultaneously using weight sharing as in [38] [47].

Evaluation. Validation perplexity is measured over a sequence length of 192 and 32 tokens for WikiText-103 and LM1B datasets, respectively. Inference latency and peak memory utilization are measured on the target hardware for a sequence length of 192, averaged over 10 measurements. We utilize PyTorch's native benchmarking interface for measuring the latency and memory utilization of

639 candidate architectures.

Table 2: LTS training hyperparameters for different backbones. Here, DO is the abbreviation used for dropout layers.

Backbone	Dataset	Tokenizer	# Vocab	Optim.	# Steps	Batch size	LR	Scheduler	Warmup	DO	Attn DO
Transformer-XL	WT103	Word	267735	LAMB 46	4e4	256	1e-2	Cosine	1e3	0.1	0.0
	LM1B	Word	267735	Adam	1e5	224	2.5e-4	Cosine	2e4	0.0	0.0
GPT-2	WT103	BPE	50257	LAMB 46	4e4	256	1e-2	Cosine	1e3	0.1	0.1
	LM1B	BPE	50257	LAMB 46	1e5	224	2.5e-4	Cosine	2e4	0.1	0.1

Search Setup. Evolutionary search is performed for 30 iterations with a population size of 100; the parent population accounts for 20 samples out of the total 100; 40 mutated samples are generated per iteration from a mutation probability of 0.3; and 40 samples are created using crossover.

643 C How Good is the Decoder Parameters Proxy for Pareto-frontier Search?

Before we use the decoder parameter count as a proxy for perplexity in the inner loop of paretofrontier search, we validate whether this proxy will actually help find pareto-frontiers which are close to the groundtruth. We first fully train all 1200 architectures sampled from the Transformer-XL backbone during evolutionary search (1). Using the validation perplexity obtained after full training, we rank all sampled architectures and extract the ground-truth pareto-frontier of perplexity versus latency. We train the models on the WikiText-103 dataset and benchmark Intel Xeon E5-2690 CPU as our target hardware platform for latency measurement in this experiment.

Figure Prepresents a scatter plot of the validation perplexity (after full training) versus latency for all sampled architectures during the search. The ground-truth pareto-frontier, by definition, is the lower convex hull of the dark navy dots, corresponding to models with the lowest validation perplexity for any given latency constraint. We mark the pareto-frontier points found by the training-free proxy with orange color. As shown, the architectures that were selected as the pareto-frontier by the proxy method are either on or very close to the ground-truth pareto-frontier.

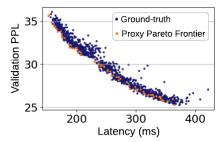


Figure 9: Perplexity versus latency pareto obtained from full training of 1200 architectures sampled during NAS on Transformer-XL backbone. Orange points are the pareto-frontier extracted using decoder parameter count proxy, which lies closely to the actual pareto-frontier. Decoder parameter count holds a SRC of 0.98 with the ground-truth perplexity after full training.

⁶⁵⁷ We define the mean average perplexity difference as a metric to evaluate the distance (d_{avg}) between ⁶⁵⁸ the proxy and ground-truth pareto-frontier:

$$d_{avg} = \frac{1}{N} \sum_{i=1}^{N} \frac{|p_i - p_{gt,i}|}{p_{gt,i}}$$
(2)

Here, p_i denotes the *i*-th point on the proxy pareto front and $p_{gt,i}$ is the closest point, in terms of latency, to p_i on the ground-truth pareto front. The mean average perplexity difference for Figure 9 is $d_{avg} = 0.6\%$. This low difference further validates the effectiveness of our zero-cost proxy in correctly ranking the sampled architectures and estimating the true pareto-frontier. In addition to the low distance between the pareto-frontier estimated using decoder parameter count proxy and the ground-truth, our zero-cost proxy holds a high SRC of 0.98 over the entire pareto, i.e., all 1200 sampled architectures.

We further study the decoder parameter proxy in scenarios where the range of model sizes provided for search is limited. We categorize the total 1200 sampled architectures into different bins based on the decoder parameters. Figure 10 demonstrates the SRC between decoder parameter count proxy and the validation perplexity after full training for different model sizes. The proposed proxy provides a highly accurate ranking of candidate architectures even when exploring a small range of model sizes.

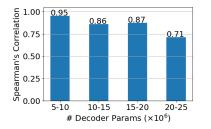


Figure 10: SRC between the decoder parameter count proxy and validation perplexity. Results are gathered on 1200 models grouped into four bins based on their decoder parameter count. Our proxy performs well even when exploring within a small range of model sizes.

671 D Analysis on Homogeneous Models

In this section, we evaluate the efficacy of the proposed proxies on the homogeneous search space, i.e., when all decoder layers have the same parameter configuration. In this scenario, the parameters are sampled from the valid ranges in Section 3 to construct one decoder block. This block is then replicated based on the selected n_{layer} to create the Transformer architecture. In what follows, we provide experimental results gathered on 100 randomly sampled Transformer models from the Transformer-XL backbone with homogeneous decoder blocks, trained on WikiText-103.

▶ Low-cost Proxies. Figure 11a demonstrates the SRC between various low-cost methods and the validation perplexity after full training. On the horizontal axis, we report the total computation required for each proxy in terms of FLOPs. Commensurate with the findings on the heterogeneous models, we observe a strong correlation between the low-cost proxies and validation perplexity, with decoder parameter count outperforming other proxies. Note that we omit the relu_log_det method from Figure 11a as it provides a low SRC of 0.42 due to heavy reliance on ReLU activations.

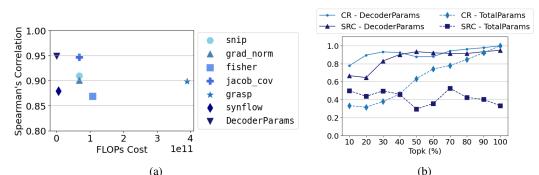


Figure 11: Experiments conducted on 100 randomly sampled Transformers with homogeneous decoder blocks, trained on WikiText-103. (a) SRC between ranking obtained from low-cost proxies and the ground-truth ranking after full training. The decoder parameter count obtains the best SRC with zero cost. (b) Performance of parameter count proxies. The decoder parameter count provides a very accurate ranking proxy with an SRC of 0.95 over all models.

▶ **Parameter Count.** As seen in Figure 11b, the total parameter count has a low SRC with the validation perplexity while the decoder parameter count provides an accurate proxy with an SRC of 0.95 over all architectures. These findings on the homogeneous search space are well-aligned with the observations in the heterogeneous space.

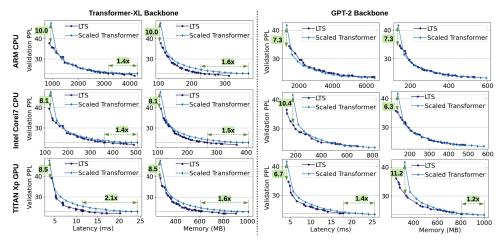


Figure 12: 2D visualization of the perplexity versus latency and memory pareto-frontier found by LTS and scaled backbone models with varying number of layers. All models are trained on the WikiText-103 dataset. The architectural parameters for all models are enclosed in Appendix H.

E How Does Model Topology Affect the Training-free Proxies?

Figure 13a shows the validation perplexity versus the aspect ratio of random architectures sampled from the Transformer-XL backbone and trained on WikiText-103. Here, the generated models span wide, shallow topologies (e.g., $d_{model}=1024$, $n_{layer}=3$) to narrow, deep topologies (e.g., $d_{model}=128$, $n_{layer}=35$). The maximum change in the validation perplexity for a given decoder parameter count is < 7% across wide range of aspect ratios ~ 8 - 323. Nevertheless, for the same decoder parameter count budget, the latency can vary by $1.3 \times$ and the peak memory utilization by $2.0 \times$ as shown in Figure 13b 13c, respectively.

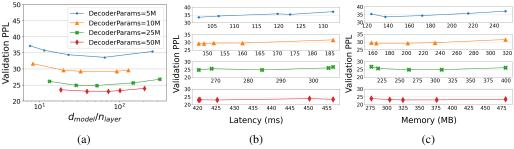


Figure 13: Validation perplexity after full training versus (a) the width-to-depth aspect ratio, (b) latency, and (c) peak memory utilization. Models are randomly generated from the Transformer-XL backbone and trained on WikiText-103. For a given decoder parameter count, we observe low variation in perplexity across different models, regardless of their topology. The topology, however, significantly affects the latency and peak memory utilization for models with the same perplexity.

For deeper architectures (more than 40 layers) with the Transformer-XL backbone, we observe an 696 increase in the validation perplexity, which results in a deviation from the pattern in Figure 13a. 697 This observation is associated with the inherent difficulty in training deeper architectures, which 698 can be mitigated with proposed techniques in the literature [39]. Nevertheless, such deep models 699 have a high latency, which makes them unsuitable for lightweight inference. For the purposes of 700 hardware-aware and efficient Transformer NAS, our search-space contains architectures with less 701 than 16 layers. In this scenario, the decoder parameter count proxy holds a very high correlation with 702 validation perplexity, regardless of the architecture topology as shown in Figure 13a 703

704 F 3D Pareto Visualization

Figure 14 visualizes the 3-dimensional pareto for the GPT-2 backbones. Here, the black and blue points denote the regular and pareto-frontier architectures, respectively. The pair of red dots are

architectures which match in both memory and decoder parameter count (\sim perplexity). However, 707 as shown, their latency differs by $2\times$. The pair of green points correspond to models with the 708 same decoder parameter count (\sim perplexity) and latency, while the memory still differs by 30MB, 709 which is non-negligible for memory-constrained application. In a 2-objective pareto-frontier search 710 of perplexity versus memory (or latency), each pair of red (or green) dots will result in similar 711 evaluations. While in reality, they have very different characteristics in terms of the overlooked metric. 712 This experiment validates the need for multi-objective pareto-frontier search, which simultaneously 713 takes into account multiple hardware performance metrics. 714

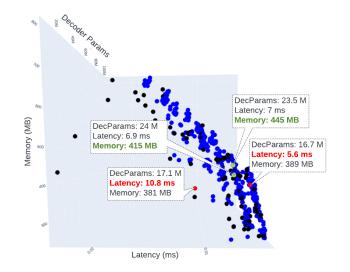


Figure 14: 3D visualization of our multi-objective NAS for the GPT-2 backbone on TITAN Xp GPU. Architectures with similar memory and decoder parameter count can result in drastically different runtimes (up to $2 \times$ difference). Similarly, architectures with similar decoder parameter count and latency may have different peak memory utilization. Therefore, it is important to perform multi-objective NAS where several hardware characteristics are simultaneously taken into account when extracting the pareto-frontier.

715 G LTS Performance Comparison on WikiText-103

We compare the pareto-frontier architectures found by LTS with the baseline after full training on the WikiText-103 dataset in Figure 12 Commensurate with the findings on the LM1B dataset, the NAS-generated models outperform the baselines in at least one of the three metrics, i.e., perplexity, latency, and peak memory utilization. We note that the gap between the baseline models and those obtained from NAS is larger when training on the LM1B dataset. This is due to the challenging nature of LM1B, which exceeds the WikiText-103 dataset size by $\sim 10\times$. Thus, it is harder for hand-crafted baseline models to compete with the optimized LTS architectures on LM1B.

On the Transformer-XL backbone, the models on LTS pareto-frontier for the ARM CPU have, on average, 3.8% faster runtime and 20.7% less memory under the same validation perplexity budget. On the Corei7, the runtime and memory savings increase to 13.2% and 19.6%, respectively, while matching the baseline perplexity. We achieve our highest benefits on TITAN Xp GPU where the pareto-frontier of LTS has on average 31.8% lower latency and 21.5% less memory. Notably, the validation perplexity of the baseline 16-layer Transformer-XL base can be achieved with a lightweight model with $2.1 \times$ less latency while consuming $1.6 \times$ less memory at runtime.

On the GPT-2 backbone, LTS achieves 6.3 - 11.2 lower perplexity in the low-latency-and-memory regime. As we transition to larger models and higher latency, our results show that the GPT-2 architecture is nearly optimal on WikiText-103 when performing inference on a CPU. The benefits are more significant when targeting a GPU; For any given perplexity achieved by the baseline, LTS pareto-frontier on TITAN Xp delivers, on average, 9.0% lower latency and 4.5% lower memory. Therefore, the perplexity and memory of the baseline 16-layer GPT-2 can be achieved by a new model that runs $1.4 \times$ faster and consumes $1.2 \times$ less memory on TITAN Xp.

737 H Architecture Details

Tables 3, 4, 5, 6 enclose the architecture parameters for the baseline and NAS-generated models in Figure 8 for Transformer-XL and GPT-2 backbones. For each target hardware, the rows of the table are ordered based on increasing decoder parameter count (decreasing validation perplexity). For all models, $d_{head}=d_{model}/n_{head}$, the adaptive input embedding factor is set to k = 4, and $d_{embed}=d_{model}$.

742 I Transformer in other Domains

While our main focus in this paper is on autoregressive, decoder-only, Transformers used for language
 modeling, we perform preliminary experiments on Transformers used on other domains to investigate
 the applicability of parameter-based proxies for ranking.

Encoder-only Transformers. BERT [8] is a widely popular Transformer composed of encoder 746 blocks, which is used in a variety of tasks, e.g., question answering and language inference. The main 747 difference between BERT and the Transformers studied in this paper is the usage of bidirectional 748 versus causal attention. Specifically, the encoder blocks in BERT are trained to compute attention 749 between each input token and all surrounding tokens. In autoregressive models, however, attention 750 is only computed for tokens appearing prior to the current token. BERT is trained with a mixture 751 of masked language modeling and next sentence prediction objectives to ensure applicability to 752 language modeling as well as downstream language understanding tasks. We use the architectural 753 parameters described in Section $\overline{3}$ to construct the search space and randomly sample 300 models 754 from the BERT backbone. We then train all models on WikiText-103 for 40K steps following the 755 training setup provided in the original BERT paper [8] for the batch size, sequence length, optimizer, 756 757 learning rate, vocabulary size, and tokenizer. Figure 15 demonstrates the CR and SRC of encoder parameter count and test perplexity measured on various topk performing BERT models. As seen, 758 both the encoder and total parameter counts provide a highly accurate proxy for test perplexity of 759 BERT, achieving an SRC of 0.96 and 0.98, respectively. This trend suggests that parameter-based 760 proxies for NAS can be applicable to encoder-only search spaces as well. 761

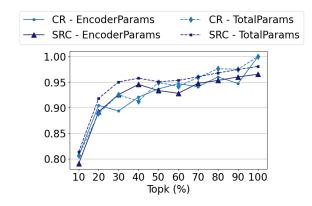


Figure 15: Performance of parameter count proxies on 300 randomly sampled models from the BERT backbone, trained on WikiText-103. Both encoder and total parameter counts provide a very accurate ranking proxy with an SRC of 0.96 and 0.98 over all models, respectively.

762 Encoder-Decoder Transformers. Transformers in this domain comprise both encoder and decoder layers with bidirectional and causal attention computation. This unique structure makes these 763 models suitable for sequence to sequence tasks such as Neural Machine Translation (NMT). Recent 764 work [14] shows that the performance of encoder-decoder Transformers also follows a scaling law 765 with model size. This power-law behavior between model size and performance can be leveraged to 766 develop training-free proxies for ranking these architectures during search. We test our hypothesis 767 by performing experiments on the open-source NMT benchmark by [50, 49] which consists of 2000 768 Transformers trained on various language pairs. The pre-trained Transformers in this benchmark have 769 770 homogeneous layers, i.e., the architectural parameters are the same for all layers and identical for the encoder and the decoder. In addition to architectural parameters, the search space for this benchmark 771 also includes various BPE tokenization and learning rates. We therefore pre-process the benchmark 772 by gathering all instances of Transformers for a fixed BPE, then for each given architecture we keep 773 774 the results corresponding to the best performing learning rate.

Figure 16 shows a heatmap of the SRC between parameter count proxies and perplexity as well 775 as the BLEU score. As seen, overall the ranking performance of total parameter count versus non-776 embedding parameter count, i.e., parameters enclosed in the encoder and decoder blocks, is largely 777 similar. On certain tasks, e.g., 'ja-en', 'so-en', and 'sw-en' the parameter count proxies perform 778 quite well, achieving a high SRC with both the BLEU score and perplexity. Interestingly, on 'so-en' 779 and 'sw-en', the parameter count and performance are inversely correlated, which may be due to the 780 limited training data for these language pairs which gives smaller models a leading advantage over 781 larger architectures. While these preliminary results show promise for parameter-based proxies in 782 NAS for NMT, there are several aspects that require further investigation in this domain, e.g., effect 783

of architectural heterogeneity and dataset size on the performance of these proxies. Studying these
 aspects may perhaps lead to a new formulation of training-free proxies for NMT and are out of scope

⁷⁸⁶ for this paper but pose an interesting future avenue of research.

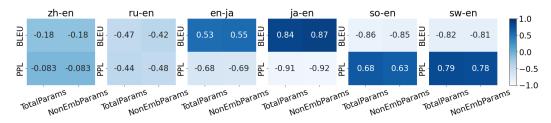


Figure 16: SRC between parameter count proxies and performance metrics, i.e., BLEU score and perplexity (PPL) for translation between various language pairs. The "NonEmbParams" label denotes the parameters enclosed in the encoder and decoder blocks only while the "TotalParams" label corresponds to the total parameter count including those in the embedding layers. Here, darker versus lighter colors show a high positive and negative correlation, respectively.

787 J Ethics Statement and Broader Impact

We provide an extremely lightweight method for NAS on autoregressive Transformers. Our work is likely to increase the adoption of NAS in the NLP domain, providing several prevalent benefits:

Firstly, a more widespread adoption of automated techniques, e.g., NAS eliminates the need for 790 laborious trials and error for manual design of Transformer architectures, freeing up hundreds of 791 hours of man-power as well as computational resources. Secondly, automating architecture design 792 can trigger generation of new models with superior performance, which benefits the ever-growing 793 applications of NLP in the everyday life. Finally, by making the search algorithm efficient, we ensure 794 it can be accessible to the general scientific public without need for any expensive mode training, 795 thereby minimizing the unwanted byproducts of the Deep Learning era such as the carbon footprint, 796 and power consumption. 797

While the benefits of automation in NLP are plenty, it can lead to potential side-effects that have not been yet fully unveiled. Since our work advances the use of NAS in the NLP design pipeline, there is need for careful scrutiny of the models which have been automatically designed with respect to aspects such as bias, misinformation, and nefarious activity, to name a few.

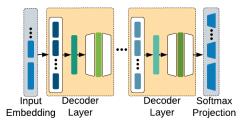


Figure 17: High-level visualization of different components in autoregressive Transformers. Here, the parameters enclosed in the orange blocks are counted as decoder parameters, while the parameters contained in the gray boxes denote the embedding parameter count.

	n _{layer}	d _{model}	n _{head}	d _{inner}	DecoderParams (M)
baseline	$\in [1, 16]$	512	8	2048	-
M1	2	512	[2, 2]	[1216, 1280]	3.2
M2	3	320	[2, 4, 2]	[1472, 2368, 3392]	5.5
M3	2	512	[2, 2]	[2560, 2176]	5.5
M4	2	512	[2, 2]	[3904, 1792]	6.5
	2				
M5		640	[2, 2]	[3520, 3456]	9.8
M6	2	832	[2, 2]	[3264, 3968]	13.1
M7	2	704	[8, 2]	[3904, 3968]	13.4
M8	2	960	[2, 2]	[3648, 3968]	15.9
M9	2	960	[2, 2]	[3904, 3968]	16.4
M10	3	960	[2, 2, 2]	[1856, 2368, 3392]	16.5
M11	3	960	[2, 4, 2]	[3328, 2368, 3200]	19.6
M11 M12	3	832	[2, 4, 2] [2, 2, 2]	[3904, 3968, 3008]	19.0
M13	3	960	[2, 2, 2]	[3904, 3584, 3456]	22.9
M14	3	960	[4, 2, 2]	[3648, 3584, 3584]	23.3
M15	3	960	[2, 2, 8]	[4032, 3968, 3904]	26.6
M16	4	896	[4, 2, 8, 2]	[3904, 3008, 3520, 3584]	29.7
M17	4	960	[2, 2, 2, 2]	[3840, 3904, 3520, 3072]	30.0
M18	4	960	[2, 2, 2, 2]	[4032, 3648, 3136, 4032]	31.0
1410	4	960	[2, 2, 4, 2]	[3904, 3968, 3840, 3584]	32.5
Way M20		960			35.7
A M20	4		[8, 8, 8, 4]	[4032, 3968, 2880, 3200]	
11/121	4	960	[8, 2, 4, 8]	[4032, 3584, 3840, 3584]	35.7
M22	5	960	[2, 2, 2, 2, 2]	[3904, 3968, 3264, 3456, 3200]	37.3
M23	5	960	[2, 2, 2, 8, 2]	[3904, 3648, 3136, 3648, 3840]	39.9
M24	6	960	[2, 2, 2, 2, 2, 8]	[3328, 2624, 3392, 2944, 3008, 3904]	42.5
M25	6	960	[2, 4, 2, 2, 2, 2]	[2112, 3840, 3328, 3264, 3968, 3648]	43.1
M26	6	960	[2, 2, 2, 2, 2, 2]	[3968, 3968, 3456, 3456, 3776, 2432]	44.8
		960			
M27	6		[2, 2, 4, 2, 8, 8]	[3584, 2624, 3392, 3968, 3008, 3328]	46.3
M28	6	960	[2, 4, 2, 2, 8, 2]	[3904, 3008, 3392, 3648, 3392, 3584]	46.4
M29	6	960	[8, 8, 2, 4, 2, 4]	[3904, 3648, 3136, 3648, 3200, 3840]	49.7
M30	6	960	[2, 4, 8, 4, 2, 8]	[3904, 3008, 3392, 3200, 3968, 3904]	49.7
M31	6	960	[8, 4, 8, 4, 2, 8]	[3904, 3648, 3392, 3200, 3968, 3840]	52.7
M32	8	896	[4, 2, 2, 4, 4, 2, 4, 8]	[3584, 3968, 3392, 3904, 2240, 1856, 2560, 3264]	53.1
M33	8	896	[4, 2, 2, 2, 4, 4, 4, 2]	[3584, 3584, 3520, 2368, 2752, 4032, 3520, 3264]	54.7
M34	8	960	[2, 4, 4, 4, 4, 8, 2, 2]	[3968, 3584, 3520, 3072, 3968, 4032, 1856, 3712]	62.5
M35	9	896	[4, 2, 4, 4, 8, 2, 8, 8, 2]	[3840, 3136, 3520, 2880, 3200, 3008, 3328, 2560, 3136]	63.4
	9				
M36		960	[4, 4, 8, 2, 2, 2, 8, 8, 2]	[2112, 3008, 3520, 3648, 3968, 4032, 1984, 3200, 3520]	68.0
M37	9	960	[8, 2, 4, 2, 8, 8, 8, 2, 2]	[3968, 3008, 3520, 3200, 3200, 4032, 1984, 2816, 3520]	69.8
M38	12	832	[2, 4, 4, 2, 2, 8, 8, 8, 4, 4, 2, 8]	[3136, 2112, 2112, 2368, 2752, 2432, 2432, 2176, 3456, 3712, 2880, 3712]	70.4
M39	12	832	[4, 4, 4, 2, 2, 8, 4, 8, 2, 8, 2, 8]	[3136, 3968, 2112, 2368, 3072, 2240, 2624, 2112, 3456, 3072, 2880, 3264]	72.1
M1	2	384	[2, 2]	[896, 2816]	3.4
M2	2	576	[2, 2]	[1792, 2816]	6.1
M3	2	832	[2, 2]	[1728, 1536]	6.5
M4	2	576	[2, 2]	[1408, 3776]	6.7
M4 M5	2	768			9.7
	2		[2, 2]	[2112, 3584]	
M6		768	[2, 2]	[3776, 1920]	9.7
M7	2	832	[2, 2]	[3776, 3392]	13.0
M8	2	960	[2, 4]	[1984, 3840]	13.0
M9	2	832	[2, 2]	[3968, 3584]	13.7
M10	2	960	[2, 2]	[3904, 3904]	16.2
M11	2	960	[8, 8]	[3968, 3584]	19.4
M12	3	960	[2, 2, 4]	[2176, 3840, 2880]	19.6
M12 M13	3	896		[2170, 3840, 2880] [2304, 3904, 3904]	19.0
M15 M14		890 960	[2, 2, 2]		22.8
	3		[2, 2, 4]	[3776, 2880, 3904]	
M15	3	960	[2, 8, 2]	[3840, 3840, 3904]	26.0
M16	3	960	[2, 2, 8]	[3968, 3904, 3904]	26.3
M17	3	960	[2, 8, 8]	[3904, 3840, 3904]	27.9
Li M17 M18 O M19	4	960	[2, 4, 2, 2]	[3904, 2112, 4032, 3584]	29.3
Ŭ M19	4	960	[2, 2, 2, 4]	[2112, 3840, 3904, 3904]	29.5
M20	4	960	[2, 2, 2, 4]	[3904, 3776, 3904, 3904]	32.9
M20 M21	4	960	[2, 2, 2, 4] [2, 4, 8, 4]	[3776, 3392, 3520, 3904]	33.6
M22	5	960	[2, 2, 2, 2, 2]	[3776, 1984, 3904, 3904, 3456]	35.8
M23	5	960	[2, 4, 2, 4, 2]	[3968, 3584, 3520, 3904, 3200]	39.3
M24	5	960	[2, 4, 4, 4, 2]	[3776, 3840, 3904, 3904, 3968]	42.2
M25	6	960	[2, 4, 2, 4, 2, 4]	[3776, 2112, 4032, 3584, 3200, 4032]	45.4
M26	6	960	[2, 4, 4, 2, 2, 4]	[3776, 3840, 3904, 3904, 3008, 2304]	45.4
M27	6	960	[2, 4, 2, 4, 4, 4]	[3776, 3840, 3904, 4032, 3648, 2432]	47.7
M28	6	960	[4, 2, 8, 4, 2, 2]	[3840, 3712, 3520, 4032, 3200, 4032]	49.7
M29	8	960			52.1
			[2, 2, 2, 4, 2, 4, 8, 2]	[3392, 1792, 3904, 3904, 3200, 2432, 1792, 2496]	
M30	7	960	[2, 2, 8, 4, 2, 2, 4]	[3776, 3840, 3904, 1856, 3072, 3648, 4032]	53.8
M31	8	960	[2, 2, 4, 4, 2, 4, 8, 2]	[3776, 3008, 4032, 3904, 3520, 3136, 1984, 3648]	60.5
M32	8	960	[8, 2, 2, 4, 8, 4, 4, 8]	[3776, 3008, 3904, 3904, 2176, 4032, 4032, 3648]	67.1
M33	9	960	[4, 2, 4, 4, 4, 4, 8, 8, 2]	[3840, 3136, 3520, 4032, 3200, 4032, 3648, 2112, 2368]	69.8
M34	9	960		[3520, 3008, 2880, 4032, 3200, 2432, 4032, 3904, 3136]	71.5
			[8, 2, 8, 8, 2, 4, 8, 2, 2] [2, 8, 2, 4, 2, 2, 4, 2, 2, 8, 8, 8, 4]	[3520, 3008, 2880, 4032, 3200, 2432, 4032, 3904, 3136] [3776, 2112, 1600, 3904, 3840, 2880, 2304, 3200, 2048, 2944, 2816, 3328, 3968]	71.5 73.3

 Table 3: Detailed architectural parameters for all models in Figure 8 with Transformer-XL backbone.

 n_{layer} d_{model} DecoderParams (M)

 DecoderParams (M)

 $\frac{n_{layer}}{Cl | 6l | 5l | 2}$ $\frac{n_{bead}}{2048}$

		nlayer	dmodel	n _{head}	dinner	DecoderParams (M)
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	baseline	∈[1,16]	8	2048	512	-
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M1	2	384	[2, 2]	[1152, 2432]	3.3
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M2	2	576	[2, 2]	[2048, 1728]	5.1
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M3	2	512	[2, 2]	[2368, 3072]	6.2
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M4	2	448	[8, 2]	[2944, 3008]	6.8
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M5	2	832	[8, 2]	[3264, 3072]	13.2
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	M6	2	768	[2, 2]	[3968, 4032]	13.3
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M7	2	896	[8, 4]	[4032, 2880]	15.8
MI0 2 960 [4,8] [3968,3648] 18.3 M11 3 960 [2,2,2] [3584,3072,2624] 19.7 M12 3 896 [2,2,2] [3840,2880,3840] 20.7 M13 3 896 [8,4,8] [4032,2112,3392] 22.9 M14 3 960 [4,2,2] [3840,3008,3840] 23.0 M15 3 960 [2,2,8] [3584,4032,4032] 26.1 M17 3 960 [8,2,8] [4032,4032,3340] 26.6 M17 3 960 [8,4,8] [4032,4032,350] 27.8 M18 3 960 [8,4,8] [4032,4032,350] 24.4 M19 4 896 [4,4,8,8] [4032,3008,3328,390] 36.4 M21 4 960 [4,2,4,4] [3840,3008,3328,390] 36.4 M22 4 960 [2,2,8,8] [4032,3068,3904,3304,3302] 39.0 M24 5 960 [2,4,2,4,4] <td>M8</td> <td>2</td> <td>960</td> <td>[2, 2]</td> <td>[3840, 3968]</td> <td>16.2</td>	M8	2	960	[2, 2]	[3840, 3968]	16.2
$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	M9	2	960	[4, 8]	[3968, 3008]	17.1
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M10	2	960	[4, 8]	[3968, 3648]	18.3
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M11	3	960	[2, 2, 2]	[3584, 3072, 2624]	19.7
M14 3 960 [4, 2, 2] [3840, 3008, 3840] 23.0 M15 3 960 [2, 2, 8] [3584, 4032, 4032] 26.1 M16 3 960 [2, 2, 8] [4032, 4032, 3520] 27.8 M17 3 960 [8, 2, 8] [4032, 4032, 3520] 27.8 M18 3 960 [8, 4, 8] [4032, 4032, 3523, 3520] 22.4 M19 4 896 [4, 4, 8, 8] [4032, 4032, 3523, 3520] 32.4 M20 4 960 [4, 2, 4, 8] [3840, 3008, 3328, 3584] 33.2 M21 4 960 [4, 2, 4, 4] [3840, 3008, 3329, 2496, 4032] 39.0 M22 4 960 [2, 2, 4, 4] [3840, 3008, 3328, 3904, 3840] 36.4 M23 5 960 [2, 2, 4, 4] [3968, 3968, 3840, 4032, 3732] 39.0 M24 5 960 [2, 4, 2, 2, 8] [3840, 3008, 3840, 3322, 2752] 39.7 M25 5 960 [2, 4, 2, 2, 8] [3840, 3008, 3840, 3324, 39	M12	3	896	[2, 2, 2]	[3840, 2880, 3840]	20.7
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M13	3	896	[8, 4, 8]	[4032, 2112, 3392]	22.9
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M14	3	960	[4, 2, 2]	[3840, 3008, 3840]	23.0
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M15	3	960	[2, 2, 8]	[3584, 4032, 4032]	26.1
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M16	3	960	[2, 2, 8]	[4032, 4032, 3840]	26.6
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M17	3	960	[8, 2, 8]	[4032, 4032, 3520]	27.8
M20 4 960 [4, 2, 8, 8] [3840, 3008, 3328, 3584] 33.2 M21 4 960 [4, 2, 4, 4] [3840, 3008, 3323, 3584] 33.2 M21 4 960 [4, 2, 4, 4] [3840, 4003, 3329, 3904, 4032] 34.7 M22 4 960 [4, 2, 4, 4, 8] [4032, 3964, 4032, 3904, 4032] 39.0 M23 5 960 [4, 2, 4, 4, 8] [3840, 3008, 3322, 2496, 4032] 39.0 M24 5 960 [2, 2, 4, 4, 4] [3968, 3968, 3840, 4032, 3732, 4032, 2752] 39.7 M25 5 960 [2, 4, 2, 2, 8] [3968, 3968, 3840, 4032, 3732, 4032, 3752] 39.7 M26 5 960 [4, 2, 8, 8, 8] [3840, 3008, 3840, 302, 3904, 3904] 43.4 M26 5 960 [4, 2, 2, 8, 8] [3840, 3008, 3840, 3328, 3904, 3904] 45.5 M28 6 896 [2, 2, 4, 4, 2, 2] [3840, 3008, 3840, 3328, 3904, 3328, 3904] 45.5 M29 6 896 [2, 4, 4, 2, 2] [3840, 3068, 3840, 3328, 3904, 3328, 3904] 45.5	M18	3	960	[8, 4, 8]	[4032, 4032, 4032]	29.4
M20 4 960 [4, 2, 8, 8] [3840, 3008, 3328, 3584] 33.2 M21 4 960 [4, 2, 4, 4] [3840, 3008, 3323, 3584] 33.2 M21 4 960 [4, 2, 4, 4] [3840, 4003, 3329, 3904, 4032] 34.7 M22 4 960 [4, 2, 4, 4, 8] [4032, 3964, 4032, 3904, 4032] 39.0 M23 5 960 [4, 2, 4, 4, 8] [3840, 3008, 3322, 2496, 4032] 39.0 M24 5 960 [2, 2, 4, 4, 4] [3968, 3968, 3840, 4032, 3732, 4032, 2752] 39.7 M25 5 960 [2, 4, 2, 2, 8] [3968, 3968, 3840, 4032, 3732, 4032, 3752] 39.7 M26 5 960 [4, 2, 8, 8, 8] [3840, 3008, 3840, 302, 3904, 3904] 43.4 M26 5 960 [4, 2, 2, 8, 8] [3840, 3008, 3840, 3328, 3904, 3904] 45.5 M28 6 896 [2, 2, 4, 4, 2, 2] [3840, 3008, 3840, 3328, 3904, 3328, 3904] 45.5 M29 6 896 [2, 4, 4, 2, 2] [3840, 3068, 3840, 3328, 3904, 3328, 3904] 45.5	🖌 M19	4	896	[4, 4, 8, 8]	[4032, 3456, 3328, 3392]	32.4
		4	960	[4, 2, 8, 8]	[3840, 3008, 3328, 3584]	33.2
	≦ M21	4	960	[4, 2, 4, 4]	[3840, 4032, 3904, 4032]	34.7
	☐ M22	4	960	[2, 2, 8, 8]	[4032, 3968, 3904, 3840]	36.4
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M23	5	960	[4, 2, 4, 4, 8]	[3840, 3008, 3392, 2496, 4032]	39.0
	M24	5	960	[2, 2, 4, 4, 4]	[3968, 4032, 3328, 4032, 2752]	39.7
	M25	5	960	[2, 4, 2, 2, 8]	[3968, 3968, 3840, 4032, 3904]	43.4
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M26	5	960		[3840, 3008, 3840, 3328, 3968]	43.8
	M27	5	960	[8, 2, 8, 8, 4]	[4032, 3008, 3840, 3904, 3968]	45.3
	M28	6	896	[2, 2, 4, 4, 2, 2]	[3840, 3968, 3840, 3328, 3904, 3904]	45.5
	M29	6	896	[8, 4, 8, 4, 8, 8]	[3328, 2112, 3392, 3904, 3328, 3264]	46.2
M32 6 960 [2,4,8,8,4,2] [3840,396,3840,3328,4032,3776] 52.4 M33 6 960 [4,8,8,4,2] [3840,396,3840,3322,328,906,3776] 53.1 M34 6 960 [4,8,8,8,4,4] [3840,3840,3392,328,906,3776] 53.9 M35 7 960 [4,8,8,8,8,2,8] [3840,3968,3840,3392,3840,3328,3712] 53.9 M35 7 960 [4, 2, 8, 8, 2, 8] [3840,3968,3840,3328,3062,328,4032] 64.7 M36 8 960 [4, 2, 8, 8, 4, 8] [3840,3968,3840,3328,3072,3328,4032] 70.1 M37 10 896 [8, 8, 8, 2, 8, 2, 2, 2, 8, 2] [3840,3072,340,2560,3048,3328,3072,3328,4032,3072] 70.1 M37 10 896 [8, 8, 8, 4, 8, 8, 4, 2] [2752,3456,2880,3004,322,3264,3136] 74.2 M38 9 960 [8, 8, 8, 4, 8, 8, 4, 2] [2752,3456,2860,3904,372,3264,336] 74.4 M39 10 896 [8, 4, 8, 8, 8, 2, 8, 2] [4032,3008,3840,2560,3904,3904,3072,3264,2368,2496] 75.4	M30	6	960	[4, 2, 2, 4, 2, 8]	[3840, 3008, 3840, 3904, 4032, 3392]	49.1
	M31	6	960	[4, 8, 8, 4, 8, 4]	[3072, 3584, 3392, 3840, 3328, 3712]	51.3
	M32	6	960	[2, 4, 8, 8, 4, 2]	[3840, 3968, 3840, 3328, 4032, 3776]	52.4
M35 7 960 [4], 8, 8, 8, 8, 2, 8] [3840, 3968, 3840, 3328, 3968, 3328, 4052] 64.7 M36 8 960 [4], 2, 8, 8, 8, 4, 8, 8] [3840, 3968, 3840, 3328, 3072, 3328, 4052] 70.1 M37 10 896 [8, 8, 2, 2, 2, 2, 8, 2] [3840, 3072, 3840, 2560, 3648, 3328, 3840, 3008, 2880, 3328] 74.2 M38 9 960 [8, 8, 8, 4, 8, 8, 4, 2] [2752, 3456, 2880, 3004, 2752, 3204, 4136] 74.4 M39 10 896 [8, 4, 8, 8, 2, 2, 4, 8] [4032, 3008, 3840, 2560, 3904, 3904, 3072, 3264, 2368, 2496] 75.4	M33	6	960	[4, 8, 8, 8, 4, 4]	[3840, 3584, 3392, 3328, 3968, 3776]	53.1
M36 8 960 [4, 2, 8, 8, 4, 8, 8] [3840, 3968, 3840, 3328, 3072, 3328, 4032, 3072] 70.1 M37 10 896 [8, 8, 8, 2, 8, 2, 2, 2, 8, 2] [3840, 3072, 3340, 2560, 3648, 3328, 3600, 3008, 2880, 3328] 74.2 M38 9 960 [8, 8, 8, 4, 4, 8, 8, 4, 2] [2752, 3456, 2880, 3904, 4732, 3264, 3136] 74.4 M39 10 896 [8, 4, 8, 8, 8, 2, 8, 2, 4, 8] [4032, 3008, 3840, 2560, 3904, 3904, 3072, 3264, 2368, 2496] 75.4	M34	6	960	[4, 8, 8, 8, 8, 8, 2]	[3840, 3840, 3392, 3840, 3328, 3712]	53.9
M36 8 960 [4, 2, 8, 8, 8, 4, 8, 8] [3840, 3968, 3840, 3328, 3072, 3328, 4032, 3072] 70.1 M37 10 896 [8, 8, 8, 2, 8, 2, 2, 2, 8, 2] [3840, 3072, 340, 2560, 3648, 3328, 3007, 3328, 4032, 3072] 74.2 M38 9 900 [8, 8, 8, 4, 8, 8, 4, 2] [2752, 3456, 2880, 3904, 2520, 3044, 3322, 3024, 3136] 74.4 M39 10 896 [8, 4, 8, 8, 8, 2, 8, 2, 4, 8] [4032, 3008, 3840, 2560, 3904, 3904, 3027, 3264, 2368, 2496] 75.4	M35	7	960	[4, 8, 8, 8, 8, 8, 2, 8]	[3840, 3968, 3840, 3328, 3968, 3328, 4032]	64.7
M37 10 896 [8, 8, 8, 2, 8, 2, 2, 8, 2] [3840, 3072, 3840, 2560, 3648, 3328, 3840, 3008, 2880, 30328] 74.2 M38 9 960 [8, 8, 8, 4, 4, 8, 8, 4, 2] [2752, 3456, 2880, 3904, 2752, 3904, 4032, 3264, 3136] 74.4 M39 10 896 [8, 4, 8, 8, 8, 2, 4, 8] [4032, 3008, 3840, 2560, 3904, 3904, 3072, 3264, 2368, 2496] 75.4	M36	8	960			70.1
M38 9 960 [8, 8, 8, 4, 4, 8, 8, 4, 2] [2752, 3456, 2880, 3904, 2752, 3904, 4032, 3264, 3136] 74.4 M39 10 896 [8, 4, 8, 8, 8, 2, 8, 2, 4, 8] [4032, 3008, 3840, 2560, 3904, 3072, 3264, 2368, 2496] 75.4	M37	10	896		[3840, 3072, 3840, 2560, 3648, 3328, 3840, 3008, 2880, 3328]	74.2
	M38	9	960		[2752, 3456, 2880, 3904, 2752, 3904, 4032, 3264, 3136]	74.4
	M39	10	896	[8, 4, 8, 8, 8, 2, 8, 2, 4, 8]	[4032, 3008, 3840, 2560, 3904, 3904, 3072, 3264, 2368, 2496]	75.4
	M40	12	832		[3840, 2816, 2112, 3584, 3648, 2432, 2304, 3008, 2880, 1664, 2432, 3776]	77.7

 Table 4: Detailed architectural parameters for all models in Figure 8 with Transformer-XL backbone.

 naver
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 dmoded
 DecoderParams (M)

Table 5: Detailed architectural parameters for all models in Figure 8 with GPT-2 backbone.

	n _{layer}	d _{mode1}	n _{head}	d _{inner}	DecoderParams (M)
baseline	$\in [1, 16]$	8	2048	512	-
M1	3	256	[2, 2, 2]	[3072, 3776, 3904]	6.3
M2	2	448	[2, 2]	[3456, 3776]	8.1
M3	2	448	[2, 4]	[4032, 3904]	8.7
M4	3	384	[2, 2, 2]	[3072, 2176, 4032]	8.9
M5	2	576	[2, 2]	[3456, 3584]	10.8
M6	4	448	[2, 2, 2, 2]	[4032, 3904, 1920, 3072]	14.8
M7	4	512	[2, 2, 4, 2]	[3904, 3136, 1280, 2624]	15.4
M8	2	832	[8, 2]	[3456, 3584]	17.3
M9	2	960	[2, 8]	[3456, 3648]	21.0
M10	2	960	[2, 2]	[3968, 3584]	21.9
M11	5	640	[2, 2, 2, 2, 2]	[4032, 2560, 2176, 2304, 3136]	26.4
M12	3	832	[2, 8, 4]	[3840, 3840, 3776]	27.4
M13	5	704	[2, 2, 2, 4, 4]	[2368, 3648, 1856, 3712, 3200]	30.8
M14	3	960	[2, 2, 2]	[3584, 3648, 4032]	32.7
M15	3	960	[2, 2, 2]	[3904, 3520, 4032]	33.1
M16	6	640	[2, 2, 2, 2, 2, 2, 2]	[2624, 2560, 2880, 3776, 3648, 3840]	34.6
M17	4	896	[2, 2, 4, 2]	[4032, 3712, 3328, 3072]	38.2
≏ M18	5	832	[2, 2, 2, 4, 4]	[3392, 3648, 2880, 3712, 3200]	41.9
× M19	4	960	[2, 2, 4, 2]	[3904, 3136, 3328, 3776]	42.0
d M18 M19 M20 M21	4	960	[8, 8, 2, 4]	[3904, 3712, 4032, 3776]	44.4
≧ M21	6	832	[2, 2, 4, 2, 2, 2]	[3904, 3456, 4032, 1792, 3072, 2496]	47.9
H M22	5	896	[4, 2, 2, 2, 4]	[3968, 3200, 3840, 3328, 3648]	48.3
M23	5	960	[2, 2, 2, 2, 2]	[3904, 3264, 3328, 3776, 3392]	52.4
M24	5	960	[2, 2, 4, 2, 2]	[3584, 3456, 3776, 2944, 4032]	52.7
M25	5	960	[2, 8, 2, 4, 2]	[3904, 3648, 4032, 3776, 3968]	55.6
M26	6	960	[8, 8, 2, 2, 2, 2]	[3904, 2560, 2880, 3776, 2240, 3840]	59.1
M27	6	960	[2, 2, 2, 4, 2, 2]	[2496, 3456, 3328, 3904, 3968, 2944]	60.8
M28	6	960	[4, 2, 4, 4, 2, 8]	[4032, 3456, 3328, 3776, 4032, 2752]	63.2
M29	6	960	[2, 2, 2, 4, 4, 4]	[3968, 3648, 3840, 3776, 3584, 2624]	63.4
M30	7	960	[2, 2, 2, 4, 2, 4, 2]	[3904, 2368, 4032, 3008, 3520, 2944, 2496]	68.7
M31	7	960	[2, 2, 4, 2, 2, 2, 4]	[3072, 3648, 3520, 3584, 3136, 1984, 3584]	69.1
M32	7	960	[4, 2, 2, 2, 8, 2, 2]	[3712, 3648, 3584, 3520, 2752, 3008, 3392]	71.2
M33	8	960	[2, 4, 4, 2, 2, 2, 2, 2]	[3904, 2816, 3072, 1920, 3328, 3456, 2304, 2368]	74.1
M34	8	960	[2, 2, 2, 4, 2, 2, 8, 2]	[3520, 2368, 4032, 1792, 3200, 3776, 3200, 3648]	78.6
M35	8	960	[4, 2, 4, 4, 8, 8, 4, 2]	[3520, 3712, 3328, 3776, 3200, 2752, 3200, 2112]	78.7
M36	8	960	[8, 4, 2, 8, 2, 2, 2, 2]	[3520, 3840, 3328, 3776, 3200, 3776, 3968, 3648]	85.4
M37	10	960		[3648, 2560, 3776, 1792, 3968, 2752, 3200, 2368, 4032, 2368]	95.5
M38	10	960		[3840, 2240, 3328, 3776, 3648, 3200, 2944, 2368, 3968, 2880]	98.8
M39	10	960		[3840, 2240, 3328, 3776, 3200, 3200, 3968, 2368, 3968, 2816]	99.8

baseline	$n_{layer} \in [1, 16]$	d _{model} 1024	n _{head} 12	3072	DecoderParams (M
M1	2	512	[2, 2]	[1920, 1920]	6.0
M2	3	320 576	[8, 2, 4]	[1920, 1920, 3712]	6.1
M3 M4	2 3	384	[2, 2] [2, 8, 2]	[1344, 3200] [3840, 2368, 3328]	7.9 9.1
M5	5	384	[4, 4, 2, 4, 4]	[2880, 1920, 960, 2496, 1280]	10.3
M6	2	768	[2, 2]	[1600, 2240]	10.6
M7	5	320	[4, 2, 2, 4, 2]	[1344, 2240, 3776, 3008, 3648]	11.0
M8	3	768	[2, 2, 4]	[1856, 1792, 1920]	15.7
M9	3	704	[2, 2, 2]	[3136, 2112, 1920]	16.1
M10 M11	2 6	960 448	[4, 2] [4, 4, 2, 2, 4, 2]	[3584, 2304] [3072, 2112, 4032, 2688, 1600, 3072]	18.7 19.7
M11 M12	3	960	[4, 4, 2, 2, 4, 2] [4, 4, 2]	[2368, 2560, 2048]	24.5
M12 M13	4	704	[4, 8, 4, 2]	[3008, 3776, 2560, 3648]	26.3
M14	5	704	[4, 2, 4, 2, 8]	[3584, 3136, 3776, 3072, 1856]	31.7
M15	3	960	[2, 2, 2]	[3392, 3648, 3840]	32.0
M16	4	960	[4, 2, 8, 2]	[2048, 3328, 1984, 1856]	32.5
M17	7	704	[2, 4, 4, 4, 8, 2, 2]	[3008, 2560, 1920, 1856, 2112, 1728, 3136]	36.9
M18 M19	4	960	[2, 2, 4, 8]	[3392, 3456, 2432, 2304]	37.0
	5 5	832 960	[4, 4, 4, 4, 4]	[3840, 1920, 4032, 3072, 3968] [2560, 2048, 3648, 1728, 2304]	41.9 42.1
M20 M21	5	960	[8, 4, 2, 2, 4] [4, 4, 2, 2, 2]	[2560, 2048, 3648, 1728, 2304] [3072, 2240, 1984, 2176, 3520]	43.4
M22	5	960	[2, 4, 4, 4, 2]	[2496, 3648, 3328, 3392, 2112]	47.2
M23	6	832	[4, 2, 4, 4, 2, 4]	[2496, 3200, 1664, 3904, 3520, 3840]	47.7
M24	6	960	[8, 2, 2, 2, 8, 4]	[2304, 3328, 3456, 1856, 1792, 2112]	50.7
M25	5	960	[4, 8, 2, 4, 4]	[3264, 2688, 4032, 3968, 3712]	52.4
M26	6	960	[2, 4, 4, 2, 2, 2]	[3008, 2624, 4032, 2688, 3520, 2624]	57.7
M27	6	960	[2, 4, 4, 2, 8, 2]	[2304, 3648, 3328, 3648, 3904, 1728]	57.8
M28	6	960 960	[4, 4, 2, 4, 2, 2] [2, 2, 2, 8, 4, 8, 4]	[3072, 2368, 4032, 4032, 3776, 3264]	61.6
M29 M30	7 7	960 960	[2, 2, 2, 8, 4, 8, 4] [2, 4, 4, 4, 4, 2, 2]	[3008, 2304, 1920, 1984, 3520, 2816, 3712] [3200, 4032, 2048, 2624, 2112, 2752, 2880]	62.9 63.6
M31	7	960	[2, 4, 4, 4, 4, 2, 2]	[3584, 3648, 3328, 3392, 3200, 1984, 3200]	68.8
M32	7	960	[2, 4, 8, 8, 2, 2, 8]	[3008, 3648, 3584, 3648, 3008, 1728, 3712]	68.8
M33	7	960	[4, 4, 2, 4, 4, 8, 4]	[3584, 3840, 3328, 3392, 3136, 2944, 2496]	69.5
M34	8	960	[8, 2, 2, 8, 2, 2, 8, 2]	[3008, 3648, 1792, 1984, 3008, 2816, 3712, 3520]	74.7
M35	8	960	[2, 2, 2, 2, 8, 4, 4, 2]	[3008, 2304, 1792, 3008, 3520, 2880, 3712, 3456]	75.1
M36	8	960	[2, 2, 2, 2, 2, 2, 2, 4, 8]	[3008, 1792, 3840, 3392, 3520, 3136, 3712, 3520]	79.4
M37 M38	9 11	960 832	[2, 2, 4, 4, 8, 8, 4, 2, 4]	[1664, 1792, 2240, 3904, 3648, 3264, 2176, 3712, 1856] [2072, 2368, 4032, 2068, 1664, 2068, 2176, 2624, 3840, 2176, 2112]	79.9 83.8
M39	9	960	$\begin{matrix} [8, 4, 2, 4, 4, 2, 8, 4, 4, 8, 8] \\ [4, 2, 4, 8, 2, 2, 4, 2, 4] \end{matrix}$	[3072, 2368, 4032, 3968, 1664, 3968, 2176, 2624, 3840, 2176, 2112] [2496, 3648, 3328, 3392, 3648, 1728, 2880, 3520, 2368]	85.1
M40	9	960	[4, 2, 4, 8, 4, 2, 4, 2, 4]	[3072, 2816, 4032, 2560, 3648, 1728, 3840, 3264, 3456]	87.8
M41	10	960	[8, 2, 4, 4, 2, 2, 4, 8, 2, 4]	[3648, 1792, 2432, 1856, 3392, 2304, 3776, 2944, 3136, 3904]	93.0
M42	10	960	[8, 2, 2, 4, 2, 2, 2, 4, 2, 2]	[3264, 2048, 3520, 3904, 3840, 3840, 2624, 3072, 3776, 2304]	98.8
M43	12	896	[4, 4, 4, 2, 4, 2, 4, 8, 8, 2, 4, 2]	[2048, 3136, 4032, 1792, 3584, 1728, 3136, 3008, 2560, 3200, 3648, 1728]	98.9
M44	10	960	[4, 2, 8, 4, 2, 8, 4, 4, 4, 2]	[3584, 3968, 3328, 3904, 2368, 2112, 3904, 3520, 3328, 2688]	99.8
M45 M1	10	960 384	[8, 2, 4, 4, 4, 4, 4, 2, 2, 8]	[2688, 3200, 3840, 3392, 3520, 3136, 3392, 3520, 2880, 3200] [3840, 2432]	99.9 6.0
M2	3	320	[2, 2, 2]	[2176, 3072, 2496]	6.2
M3	2	512	[2, 2]	[1408, 2624]	6.2
M4	3	384	[2, 2, 2]	[3264, 3456, 3584]	9.7
M5	2	576	[2, 2]	[3136, 3648]	10.5
M6	3	448	[2, 2, 2]	[4032, 3648, 4032]	12.9
M7	4	448	[2, 2, 4, 4]	[3072, 3648, 4032, 1792]	14.5
M8 M0	2	768 576	[2, 2]	[3968, 3328]	15.9
M9 M10	4 2	960	[2, 2, 2, 2]	[3072, 2752, 3456, 3136] [3840, 3264]	19.6 21.0
M10 M11	4	900 640	[2, 2] [2, 2, 2, 2]	[3840, 3204] [2176, 3648, 3584, 1920]	21.0
M12	3	960	[2, 2, 2, 2]	[2176, 3264, 2432]	26.2
M13	4	768	[2, 2, 2, 2]	[3584, 2112, 3392, 1920]	26.4
M14	4	768	[2, 2, 2, 2]	[3584, 2560, 3776, 1536]	27.1
M15	4	832	[2, 2, 2, 2]	[3904, 1984, 3392, 3136]	31.8
M15 M16 M17	3	960	[2, 2, 2]	[3968, 4032, 2880]	32.0
	5	768 960	[2, 2, 4, 2, 2]	[3648, 3072, 3392, 1984, 2944] [3136, 1984, 3202, 2044]	34.9
M18 M19	4 4	960 960	[2, 2, 2, 2] [2, 2, 2, 4]	[3136, 1984, 3392, 2944] [3968, 3456, 3584, 3136]	36.8 42.0
M20	6	768	[4, 2, 2, 4] [4, 2, 2, 4, 2, 4]	[3584, 2112, 3456, 3136, 3840, 2560]	42.0
M21	7	768	[2, 4, 2, 4, 4, 4, 2]	[2624, 1984, 2496, 3968, 2880, 2112, 4032]	47.5
M22	5	960	[2, 2, 4, 2, 4]	[2176, 3264, 3392, 3008, 3328]	47.6
M23	6	960	[4, 4, 2, 4, 2, 2]	[2048, 2624, 3520, 1984, 2880, 2624]	52.3
M24	6	960	[2, 4, 4, 4, 2, 2]	[1792, 3456, 2752, 2240, 1664, 3840]	52.4
M25	6	960	[4, 2, 2, 2, 4, 4]	[2176, 1664, 3648, 3136, 3968, 3904]	57.7
M26 M27	7 7	960 806	[2, 2, 4, 4, 2, 2, 8]	[2816, 1792, 3968, 1728, 1664, 3328, 2944] [3904, 3264, 3328, 3968, 1728, 2624, 4032]	60.9 63.5
M27 M28	7	896 960	[2, 2, 4, 2, 2, 2, 2] [4, 2, 4, 2, 2, 2, 2]	[3904, 3264, 3328, 3968, 1728, 2624, 4032] [3584, 2560, 1792, 1920, 3968, 2112, 3968]	63.5 64.1
M28 M29	8	960 960	[4, 2, 4, 2, 2, 2, 2] [2, 2, 2, 4, 2, 2, 2, 4]	[3328, 2432, 2624, 2752, 1664, 2240, 2304, 2816]	68.3
M30	7	960	[4, 2, 4, 2, 2, 2, 2]	[3904, 2304, 2368, 3584, 3264, 2880, 3904]	68.5
M31	8	960	[4, 2, 4, 2, 2, 4, 2, 4]	[2560, 3648, 2624, 2112, 3328, 2112, 1792, 3328]	70.9
M32	8	960	[4, 4, 4, 2, 2, 4, 2, 4]	[2560, 2304, 2624, 4032, 2688, 2624, 3840, 2816]	74.7
M33	9	960	[2, 4, 2, 4, 2, 4, 2, 2, 4]	[3072, 3264, 2944, 1984, 2880, 3520, 2112, 2624, 1728]	79.6
	10	896	[2, 2, 4, 2, 2, 2, 2, 2, 4, 2]	[2816, 3264, 3584, 1792, 3136, 3584, 2240, 2240, 1920, 2752]	81.2
M34			[8, 2, 2, 2, 4, 4, 2, 4, 4]	[3904, 3648, 2432, 3136, 3264, 2816, 2240, 3072, 3840]	87.7
M35	9	960			
	9 10 10	960 960 960	$\begin{bmatrix} 0, 2, 2, 2, 4, 4, 2, 4, 4 \end{bmatrix}$ $\begin{bmatrix} 4, 4, 2, 2, 4, 4, 2, 4, 4, 2 \end{bmatrix}$ $\begin{bmatrix} 4, 2, 4, 2, 2, 2, 2, 4, 4, 2 \end{bmatrix}$	[2176, 3264, 2752, 3136, 3968, 3520, 3776, 3328, 1728, 2496] [3904, 2112, 2496, 3968, 3968, 2624, 3904, 2304, 3200, 3840]	94.9 99.0

 Table 6: Detailed architectural parameters for all models in Figure 8 with GPT-2 backbone.