Subgroup Generalization and Fairness of Graph Neural Networks

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Abstract

Despite enormous successful applications of graph neural networks (GNNs) re-1 cently, theoretical understandings of their generalization ability, especially for 2 node-level tasks where data are not independent and identically-distributed (IID), 3 have been sparse. The theoretical investigation of the generalization performance 4 is beneficial for understanding fundamental issues (such as fairness) of GNN 5 models and designing better learning methods. In this paper, we present a novel 6 PAC-Bayesian analysis for GNNs under a non-IID semi-supervised learning setup. 7 8 Moreover, we analyze the generalization performances on different subgroups of unlabeled nodes, which allows us to further study an accuracy-(dis)parity-style 9 (un)fairness of GNNs from a theoretical perspective. Under reasonable assump-10 tions, we demonstrate that the distance between a test subgroup and the training 11 set can be a key factor affecting the GNN performance on that subgroup, which 12 calls special attention to the training node selection for fair learning. Experiments 13 across multiple GNN models and datasets support our theoretical results. 14

15 **1 Introduction**

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Graph Neural Networks (GNNs) [11, 30, 16] are a family of machine learning models that can be
used to model non-Euclidean data as well as inter-related samples in a flexible way. Recent years have
witnessed enormous successful applications of GNNs in various areas, such as drug discovery [14],
computer vision [24], transportation forecasting [42], recommender systems [41], etc. Depending
on the type of prediction target, the application tasks can be roughly categorized into node-level,
edge-level, subgraph-level, and graph-level tasks [39].

In contrast to the huge empirical success in practice, theoretical understandings of the generalization 22 23 ability of GNNs have been rather limited. Among the existing literature, some studies [9, 10, 21] focus on the analysis of graph-level tasks where each sample is an entire graph and the training data 24 are IID samples of graphs. A very limited number of studies [31, 36] explore GNN generalization 25 for node-level tasks but they assume the training nodes (and their associated neighborhoods) are IID 26 27 samples, which does not align with the commonly seen graph-based semi-supervised learning setups. 28 Baranwal et al. [3] investigate GNN generalization under a specific data generating mechanism. 29 In this work, our first contribution is to provide a novel PAC-Bayesian analysis for the generalization

ability of GNNs on node-level tasks with non-IID assumptions about training nodes. In particular, we assume the node features are fixed and the node labels are independently sampled from distributions conditioned on the node features. We also assume the training set and the test set can be chosen as arbitrary subsets of nodes on the graph. We first prove two general PAC-Bayesian generalization

bounds (Theorem 1 and Theorem 2) under this non-IID setup, and then derive a generalization bound
 for GNN (Theorem 3) in terms of characteristics of the GNN models and the node features.

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Notably, the generalization error is influenced by the distance of the aggregated node features between 36 the test nodes and the training nodes. This implies that, given a fixed training set, test nodes that are 37 "far away" from all the training nodes may suffer from larger generalization errors, which leads to an 38 accuracy-disparity unfairness. In reality, these nodes may reside in small isolated clusters, or they are 39 on the boundaries of large communities. We conduct empirical experiments using multiple benchmark 40 datasets and investigate the test accuracy of four popular GNN models on different subgroups. Results 41 42 indicate there is indeed a significant disparity in test accuracy among these subgroups. We summarize the contributions of this work as follows. (1) We establish a novel PAC-Bayesian 43

we summarize the control buddens of this work as follows. (1) we establish a novel rAC-Dayesian
 analysis for graph-based semi-supervised learning with non-IID training nodes. (2) We provide a
 subgroup generalization bound for GNNs under this setup. (3) As an implication of the derived
 generalization bound, we predict that there would be an accuracy disparity across different subgroups

47 of test nodes. (4) We empirically verify the existence of accuracy-disparity unfairness of GNNs.

48 2 Related Work

49 2.1 Generalization of Graph Neural Networks

The majority of existing literature that aim to develop theoretical understandings of GNNs have 50 focused on the expressive power of GNNs (see Sato [29] for a survey along this line), while the 51 number of studies trying to understand the generalizability of GNNs is rather limited. Among 52 them, some [9, 10, 21] focus on graph-level tasks, the analyses of which cannot be easily applied 53 to node-level tasks. As far as we know, Scarselli et al. [31], Verma and Zhang [36], Baranwal et al. 54 55 [3] are the only existing studies investigating the generalization of GNNs on node-level tasks, even though node-level tasks are more common in reality. Scarselli et al. [31] present an upper bound of 56 the VC-dimension of GNNs; Verma and Zhang [36] derive a stability-based generalization bound for 57 a single-layer GCN [16] model. Yet, both Scarselli et al. [31] and Verma and Zhang [36] (implicitly) 58 assume that the training nodes are IID samples from a certain distribution, which does not align 59 with the common practice of node-level semi-supervised learning. Baranwal et al. [3] investigate the 60 generalization of graph convolution under a specific data generating mechanism, i.e., the contextual 61 stochastic block model [8]. Our work presents the first generalization analysis of GNNs for non-IID 62 node-level tasks without strong assumptions on the data generating mechanism. 63

64 2.2 Fairness of Machine Learning on Graphs

The fairness issues of machine learning on graphs start to receive research attention recently. Fol-65 lowing conventional machine learning fairness literature, the majority of previous work along this 66 line [1, 5–7, 18, 27, 33, 43] concerns about fairness with respect to a given sensitive attribute, such as 67 gender or race, which defines protected groups. In practice, the fairness issues of learning on graphs 68 are much more complicated due to the asymmetric nature of the graph-structured data. However, 69 only a few studies [15] investigate the unfairness caused by the graph structure without knowing a 70 sensitive feature. Moreover, in a node-level semi-supervised learning task, the non-IID sampling of 71 training nodes brings additional uncertainty to the fairness of the learned models. This work is the 72 first to present a learning theoretic analysis under this setup, which in turn suggests how the graph 73 structure and the selection of training nodes may influence the fairness of machine learning on graphs. 74

75 2.3 PAC-Bayesian Analysis

PAC-Bayesian analysis [22] has become one of the most powerful theoretical framework to analyze 76 the generalization ability of machine learning models. We will briefly introduce the background in 77 Section 3.2, and refer the readers to a recent tutorial [12] for a systematic overview of PAC-Bayesian 78 analysis. We note that Liao et al. [21] recently present a PAC-Bayesian generalization bound for 79 GNNs on IID graph-level tasks. Both Liao et al. [21] and this work utilize results from Neyshabur et al. 80 [25], a PAC-Bayesian analysis for ReLU-activated neural networks, in part of our proofs. Compared 81 to Neyshabur et al. [25], the key contribution of Liao et al. [21] is the derivation of perturbation 82 bounds of two types of GNN architectures; while the key contribution of this work is the novel 83 analysis under the setup of non-IID node-level tasks. There is also an existing work of PAC-Bayesian 84 analysis for transductive semi-supervised learning [4]. But it is different from our problem setup and, 85 in particular, it cannot be used to analyze the generalization on subgroups. 86

87 **3** Preliminaries

In this section, we first formulate the problem of node-level semi-supervised learning. We also
 provide a brief introduction of the PAC-Bayesian framework.

90 3.1 The Problem Formulation and Notations

91 Semi-supervised node classification. Let $G = (V, E) \in \mathcal{G}_N$ be an undirected graph, with 92 $V = \{1, 2, ..., N\}$ being the set of N nodes and $E \subseteq V \times V$ being the set of edges. And \mathcal{G}_N 93 is the space of all undirected graphs with N nodes. The nodes are associated with node features 94 $X \in \mathbb{R}^{N \times D}$ and node labels $y \in \{1, 2, ..., K\}^N$.

In this work, we focus on the transductive node classification setting [40], where the node features X and the graph G are observed prior to learning, and every quantity of interest in the analysis will be conditioned on X and G. Without loss of generality, we treat X and G as fixed throughout our analysis and the randomness comes from the labels y. In particular, we assume that for each node $i \in V$, its label y_i is generated from an unknown conditional distribution $\Pr(y_i | Z_i)$, where Z = g(X, G) and $g : \mathbb{R}^{N \times D} \times \mathcal{G}_N \to \mathbb{R}^{N \times D'}$ is an aggregation function that aggregates the features over (multi-hop) local neighborhoods¹. We also assume that the node labels are generated independently conditional on their respective aggregated features Z_i 's.

Given a small set of the labeled nodes, $V_0 \subseteq V$, the task of node-level semi-supervised learning to learn a classifier $h : \mathbb{R}^{N \times D} \times \mathcal{G}_N \to \mathbb{R}^{N \times K}$ from a function family \mathcal{H} and perform it on the remaining unlabeled nodes. Given a classifier h, the classification for a node i is obtained by

$$\hat{y}_i = \operatorname*{argmax}_{k \in \{1, \dots, K\}} h_i(X, G)[k],$$

where $h_i(X,G)$ is the *i*-th row of the output of h(X,G) and $h_i(X,G)[k]$ refers to the *k*-th element of $h_i(X,G)$.

Subgroups. In Section 4, we will present an analysis of the GNN generalization performance on any subgroup of the set of unlabeled nodes, $V \setminus V_0$. Note that the analysis on any subgroup is a stronger result than that on the entire unlabeled set, as the entire set is a subset. Later we will show that the analysis on subgroups (rather than on the entire set) further allows us to investigate the accuracy disparity across subgroups. We denote a collection of subgroups of interest as $V_1, V_2, \ldots, V_M \subseteq$ $V \setminus V_0$. In practice, a subgroup can be defined based on an attribute of the nodes (e.g., a gender group), certain graph-based properties, or an arbitrary partition of the nodes. We also define the size of each subgroup as $N_m := |V_m|, m = 0, \ldots, M$.

116 **Margin loss on each subgroup.** Now we can define the *empirical* and *expected margin loss* of any 117 classifier $h \in \mathcal{H}$ on each subgroup $V_m, m = 0, 1, ..., M$. Given a sample of observed node labels 118 y_i 's, the empirical margin loss of h on V_m for a margin $\gamma \ge 0$ is defined as

$$\widehat{\mathcal{L}}_{m}^{\gamma}(h) := \frac{1}{N_{m}} \sum_{i \in V_{m}} \mathbb{1}\left[h_{i}(X, G)[y_{i}] \le \gamma + \max_{k \neq y_{i}} h_{i}(X, G)[k]\right],\tag{1}$$

where $\mathbb{1}[\cdot]$ is the indicator function. The expected margin loss is the expectation of Eq. (1), i.e.,

$$\mathcal{L}_{m}^{\gamma}(h) := \mathbb{E}_{y_{i} \sim \Pr(y|Z_{i}), i \in V_{m}} \mathcal{L}_{m}^{\gamma}(h).$$
⁽²⁾

To simplify the notation, we define $y^m := \{y_i\}_{i \in V_m}, \forall m = 0, ..., M$, so that Eq. (2) can be written as $\mathcal{L}_m^{\gamma}(h) = \mathbb{E}_{y^m} \widehat{\mathcal{L}}_m^{\gamma}(h)$. We note that the classification *risk* and *empirical risk* of *h* on V_m are respectively equal to $\mathcal{L}_m^0(h)$ and $\widehat{\mathcal{L}}_m^0(h)$.

123 3.2 The PAC-Bayesian Framework

The PAC-Bayesian framework [22] is an approach to analyze the generalization ability of a stochastic predictor drawn from a distribution Q over the predictor family \mathcal{H} that is learned from the training

¹An example is $g_i(X,G) = \frac{1}{|\mathcal{N}(i)|+1} \left(X_i + \sum_{j \in \mathcal{N}(i)} X_j \right)$, where $g_i(X,G)$ is the *i*-th row of the output of g(X,G) and $\mathcal{N}(i) := \{j \mid (i,j) \in E\}$ is the set of 1-hop neighbors of node *i*. The aggregation function *g* can also be defined to aggregate over multiple-hop neighbors.

data. For any stochastic classifier distribution Q and m = 0, ..., M, slightly overloading the notation, we denote the empirical margin loss of Q on V_m as $\hat{\mathcal{L}}_m^{\gamma}(Q)$, and the corresponding expected margin

loss as $\mathcal{L}_m^{\gamma}(Q)$. And they are given by

$$\widehat{\mathcal{L}}_m^{\gamma}(Q) := \mathbb{E}_{h \sim Q} \widehat{\mathcal{L}}_m^{\gamma}(h), \quad \mathcal{L}_m^{\gamma}(Q) := \mathbb{E}_{h \sim Q} \mathcal{L}_m^{\gamma}(h).$$

In general, a PAC-Bayesian analysis aims to bound the generalization gap between $\mathcal{L}_m^{\gamma}(Q)$ and $\hat{\mathcal{L}}_m^{\gamma}(Q)$. The analysis is usually done by first proving that, for any "prior" distribution² P over \mathcal{H} that is independent of the training data, the generalization gap can be controlled by the discrepancy between P and Q; the analysis is then followed by careful choices of P to get concrete upper bounds of the generalization gap. While the PAC-Bayesian framework is built on top of stochastic predictors, there exist standard techniques [19] that can be used to derive generalization bounds for deterministic predictors from PAC-Bayesian bounds.

Finally, we introduce two divergence of distributions that will be used in the analysis. We denote the total variation (TV) divergence between two distributions Q and P as $D_{\text{TV}}(Q||P) := \frac{1}{2} \int |\frac{dQ}{dP} - 1|dP$,

and the Kullback-Leibler (KL) divergence as $D_{\mathrm{KL}}(Q\|P) := \int \ln \frac{dQ}{dP} dQ$.

139 4 Analysis

As we mentioned in Section 2.3, existing PAC-Bayesian analyses cannot be directly applied to the non-IID semi-supervised learning setup where we care about the generalization (disparity) across different subgroups of the unlabeled samples. In this section, we first present general PAC-Bayesian theorems for subgroup generalization under our problem setup; then we derive a generalization bound for GNNs and discuss implications of the bounds.

145 4.1 General PAC-Bayesian Theorems for Subgroup Generalization

146 Stochastic classifier bound. We first present the general PAC-Bayesian theorem (Theorem 1) for 147 subgroup generalization of stochastic classifiers. The generalization bound depends on a notion of 148 expected loss discrepancy between two subgroups as defined below.

Definition 1 (Expected Loss Discrepancy). *Given a distribution* P over \mathcal{H} , for any $\lambda > 0$ and $\gamma \ge 0$, for any two subgroups V_m and $V_{m'}$ ($0 \le m, m' \le M$), define the expected loss discrepancy between V_m and V_0 with respect to (P, γ, λ) as

$$D_{m,m'}^{\gamma}(P;\lambda) := \ln \mathbb{E}_{h\sim P} e^{\lambda \phi \left(\mathcal{L}_{m}^{\gamma/2}(h) - \mathcal{L}_{m'}^{\gamma}(h)\right)},$$

where $\mathcal{L}_m^{\gamma/2}(h)$ and $\mathcal{L}_{m'}^{\gamma}(h)$ follow the definition of Eq. (2), and we define $\phi(x) := \max(0, x)$.

Intuitively, $D_{m,m'}^{\gamma}(P;\lambda)$ captures the difference of the expected loss between V_m and $V_{m'}$ in an average sense (over P). Note that $D_{m,m'}^{\gamma}(P;\lambda)$ is asymmetric in terms of V_m and $V_{m'}$, and can be negative if the loss on V_m is mostly smaller than that on $V_{m'}$.

¹⁵⁶ For stochastic classifiers, we have the following Theorem 1. Proof can be found in Appendix A.1.

Theorem 1 (Subgroup Generalization of Stochastic Classifiers). For any $0 < m \le M$, for any $\lambda > 0$ and $\gamma \ge 0$, for any "prior" distribution P on H that is independent of the training data on V_0 , with probability at least $1 - \delta$ over the sample of y^m , for any Q on H, we have³

$$\mathcal{L}_{m}^{\gamma/2}(Q) \leq \widehat{\mathcal{L}}_{0}^{\gamma}(Q) + \frac{1}{\lambda} \left(D_{\mathrm{TV}}(Q \| P) + \ln \frac{2}{\delta} + \frac{\lambda^{2}}{4N_{0}} + D_{m,0}^{\gamma}(P;\lambda) \right).$$
(3)

Theorem 1 can be viewed as an adaptation of a result by Alquier et al. [2] from the IID supervised setting to our non-IID semi-supervised setting. The terms $D_{\text{TV}}(Q||P), \ln \frac{2}{\delta}$, and $\frac{\lambda^2}{4N_0}$ are

²The distribution is called "prior" in the sense that it doesn't depend on training data. "Prior" and "posterior" in PAC-Bayesian are different with those in conventional Bayesian statistics. See Guedj [12] for details.

³Theorem 1 also holds when we substitute $\mathcal{L}_m^{\gamma/2}(h)$ and $\mathcal{L}_m^{\gamma/2}(Q)$ as $\mathcal{L}_m^{\gamma}(h)$ and $\mathcal{L}_m^{\gamma}(Q)$ respectively. But we state the theorem in this form to ease the development of the later analysis.

commonly seen in PAC-Bayesian analysis for IID supervised setting. In particular, when setting $\lambda = \Theta(\sqrt{N_0}), \frac{1}{\lambda} \left(\ln \frac{2}{\delta} + \frac{\lambda^2}{4N_0} \right)$ vanishes as the training size N_0 grows. The divergence between Qand $P, D_{\text{TV}}(Q \| P)$, is usually considered as a measurement of the model complexity [12]. And there will be a trade-off between the training loss, $\hat{\mathcal{L}}_0^{\gamma}(Q)$, and the complexity (how far can the learned "posterior" Q go from the "prior" P).

Uniquely for the non-IID semi-supervised setting, there is an extra term $D_{m,0}^{\gamma}(P;\lambda)$, which is the expected loss discrepancy between the target test subgroup V_m and the training set V_0 . Note that this quantity is independent of the training labels y^0 . Not surprisingly, it is difficult to give generalization guarantees if the expected loss on V_m is much larger than that on V_0 for any stochastic classifier Pindependent of training data. We have to make some assumptions about the relationship between V_m

and V_0 to obtain a meaningful bound on $\frac{1}{\lambda}D_{m,0}^{\gamma}(P;\lambda)$, which we will discuss in details in Section 4.2.

Deterministic classifier bound. Utilizing standard techniques in PAC-Bayesian analysis [19, 22, 25], we can convert the bound for stochastic classifiers in Theorem 1 to a bound for deterministic classifiers as stated in Theorem 2 below (see Appendix A.2 for the proof).

Theorem 2 (Subgroup Generalization of Deterministic Classifiers). Let \tilde{h} be any classifier in \mathcal{H} . For any $0 < m \leq M$, for any $\lambda > 0$ and $\gamma \geq 0$, for any "prior" distribution P on \mathcal{H} that is independent of the training data on V_0 , with probability at least $1 - \delta$ over the sample of y^m , with probability at least $1 - \delta$ over the sample of y^m , for any Q on \mathcal{H} such that $\operatorname{Pr}_{h\sim Q}\left(\max_{i\in V_0\cup V_m}|h_i(X,G)-\tilde{h}_i(X,G)|_{\infty}<\frac{\gamma}{8}\right) > \frac{1}{2}$, we have

$$\mathcal{L}_{m}^{0}(\tilde{h}) \leq \widehat{\mathcal{L}}_{0}^{\gamma}(\tilde{h}) + \frac{1}{\lambda} \left(2\sqrt{D_{\mathrm{KL}}(Q\|P) + 1} + \ln\frac{2}{\delta} + \frac{\lambda^{2}}{4N_{0}} + D_{m,0}^{\gamma/2}(P;\lambda) \right).$$
(4)

Theorem 1 and 2 are not specific to GNNs and hold for any (respectively stochastic and deterministic) classifier under the semi-supervised setup. In Section 4.2, we will apply Theorem 2 to obtain a

subgroup generalization bound that explicitly depends on the characteristics of GNNs and the data.

184 4.2 Subgroup Generalization Bound for Graph Neural Networks

The GNN model. We consider GNNs where the node feature aggregation step and the prediction step are separate. In particular, we assume the GNN classifier takes the form of $h_i(X, G) =$ $f(g_i(X, G); W_1, W_2, ..., W_L)$, where g is an aggregation function as we described in Section 3.1 and f is a ReLU-activated L-layer Multi-Layer Perceptron (MLP) with $W_1, ..., W_L$ as parameters for each layer⁴. Denote the largest width of all the hidden layers as b.

¹⁹⁰ **Upper-bounding** $D_{m,0}^{\gamma}(P;\lambda)$. To derive the generalization guarantee, we first upper-bound the ¹⁹¹ expected loss discrepancy $D_{m,0}^{\gamma}(P;\lambda)$ by making two assumptions on the data. We first assume that ¹⁹² the label distributions conditional on aggregated features are smooth (Assumption 1).

- Assumption 1 (Smoothness of Data Distribution). Assume there exist c-Lipschitz continuous func-
- tions $\eta_1, \eta_2, \ldots, \eta_K : \mathbb{R}^{D'} \to [0, 1]$, such that, for any node $i \in V$,

$$\Pr(y_i = k \mid g_i(X, G)) = \eta_k(g_i(X, G)), \forall k = 1, \dots, K.$$

- We also need to characterize the relationship between a target subgroup V_m and the training set V_0 .
- For this purpose, we define the distance from V_m to V_0 and the concept of *near set* below.
- 197 **Definition 2** (Distance To Training Set and Near Set). For each $0 < m \le M$, define the distance
- 198 from the subgroup V_m to the training set V_0 as

$$\epsilon_m := \max_{j \in V_m} \min_{i \in V_0} \|g_i(X, G) - g_j(X, G)\|_2.$$

199 Further, for each $i \in V_0$, define the near set of i with respect to V_m as

$$V_m^{(i)} := \{ j \in V_m \mid \|g_i(X,G) - g_j(X,G)\|_2 \le \epsilon_m \}.$$

200 Clearly,

$$V_m = \bigcup_{i \in V_0} V_m^{(i)}.$$

⁴SGC [38] and APPNP [17] are special cases of GNNs in this form.

- Then, with the Assumption 2 below, we can bound the expected loss discrepancy $D_{m,0}^{\gamma}(P;\lambda)$ with 201 the following Lemma 1 (see the proof in Appendix A.3). 202
- **Assumption 2** (Equal-Sized and Disjoint Near Sets). For any $0 < m \leq M$, assume the near sets of 203 each $i \in V_0$ with respect to V_m are disjoint and have the same size $s_m \in \mathbb{N}^+$. 204
- 205

Lemma 1 (Bound for $D_{m,0}^{\gamma}(P;\lambda)$). Under Assumption 1 and 2, for any $0 < m \leq M$, any $\lambda > 0$ and $\gamma \geq 0$, assume the prior P on \mathcal{H} is defined by sampling the vectorized MLP parameters from $\mathcal{N}(0,\sigma^2 I)$ for some $\sigma^2 \leq \frac{(\gamma/4\epsilon_m)^{2/L}}{2b(\ln 2bL+\lambda)}$. we have 206

207

$$D_{m,0}^{\gamma}(P;\lambda) \le \ln 2 + \lambda c K \epsilon_m.$$
(5)

Intuitively, what we need to bound $D_{m,0}^{\gamma}(P;\lambda)$ is that the training set V_0 is "representative" for V_m . 208 This is reasonable in practice as it's natural to select the training samples according to the distribution 209 of the population. Specifically, Assumption 2 assumes that V_m can be split into equal-sized partitions 210 indexed by the training samples. The elements of each partition $V_m^{(i)}$ are close to the corresponding training sample *i* but not so close to training samples other than *i*. This assumption is stronger than 211 212 needed to obtain a meaningful bound on $D_{m,0}^{\gamma}(P;\lambda)$, and we can relax it by only assuming that most 213 samples in V_m have proportional "close representatives" in V_0 . But we keep Assumption 2 in this 214 work, as it is intuitively clear and significantly eases the analysis and notations. 215

The bound (5) suggests that the closer between V_m and V_0 (smaller ϵ_m), the smaller the expected 216 loss discrepancy. 217

Bound for GNNs. Finally, with an additional assumption (Assumption 3) that the maximum L2 218

norm of aggregated node features does not grow too fast in terms of the number of training samples, 219

- we obtain a subgroup generalization bound for GNNs in Theorem 3. The proof of Theorem 3 can be 220 found in Appendix A.4. 221
- **Assumption 3.** Define $B_m := \max_{i \in V_0 \cup V_m} \|g_i(X, G)\|_2$, and assume $B_m = o(N_0^{1/4})$. 222
- **Theorem 3** (Subgroup Generalization Bound for GNNs). Let \tilde{h} be any classifier in \mathcal{H} with parameters 223

 $\{W_l\}_{l=1}^L$. Under Assumptions 1, 2, and 3, for any $0 < m \le M$, $\gamma \ge 0$ and large enough N_0 , with 224 probability at least $1 - \delta$ over the sample of y^m , we have 225

$$\mathcal{L}_{m}^{0}(\tilde{h}) \leq \widehat{\mathcal{L}}_{0}^{\gamma}(\tilde{h}) + O\left(cK\epsilon_{m} + \frac{2\sqrt{b\sum_{l=1}^{L} \|\widetilde{W}_{l}\|_{F}^{2}}}{N_{0}^{1/4}(\gamma/8)^{1/L}}(\epsilon_{m})^{1/L} + \frac{1}{N_{0}^{1/2}}\ln\frac{N_{0}}{\delta}\right).$$
(6)

Next, we investigate the qualitative implications of our theoretical results. 226

4.3 Implications for Fairness of Graph Neural Networks 227

Accuracy-disparity style of unfairness. One merit of our analysis is that we can apply Theorem 3 228 on different subgroups of the unlabeled nodes and compare the subgroup generalization bounds. This 229 allows us to study the accuracy disparity across subgroups from a theoretical perspective. 230

A major factor that affects the generalization bound (6) is ϵ_m , the distance from the target subgroup 231 V_m to the training set V_0 . The generalization bound (6) suggests that there is a better generalization 232 guarantee for subgroups that are closer to the training set. In other words, it is unfair for subgroups 233 that are far away from the training set. While our theoretical analysis only provides an upper bound 234 for the generalization error, in Section 5, we empirically verify that the test performances of GNN 235 models do present accuracy disparity across subgroups with varying distances to the training set. 236

Moreover, when more domain knowledge about the particular learning task and data is available, 237 we can further investigate the factors that affect ϵ_m and identify potential fairness issues. As an 238 example, the geodesic distance (length of shortest-path on the graph) between two nodes may be a 239 good indicator for the similarity of their aggregated features. Below we discuss two such scenarios. 240

Smoothing effect of feature aggregation in GNNs. Many existing GNN models are known to have a 241 smoothing effect on the aggregated node features [20]. As a result, nodes with a shorter geodesic 242 distance are likely to have more similar aggregated features. 243

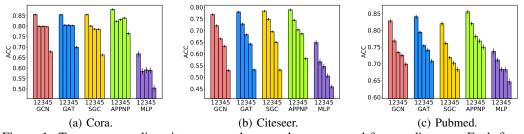


Figure 1: Test accuracy disparity across subgroups by aggregated-feature distance. Each figure corresponds to a dataset, and each bar cluster corresponds to a model. Bars labeled 1 to 5 represent subgroups with increasing distance to training set. Results are averaged over 40 independent trials with different random splits of the data, and the error bar represents the standard error of the mean.

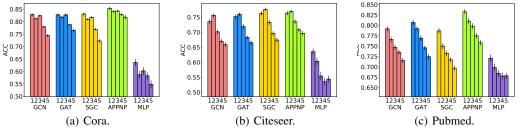


Figure 2: Test accuracy disparity across subgroups by geodesic distance. The experiment and plot settings are the same as Figure 1, except for the bars labeled from 1 to 5 here represent subgroups with increasing shortest-path distance to training set.

Homophily. Many real-world graph-structured data present a homophily property [23], i.e., connected 244 nodes tend to share similar attributes. In this case, again, nodes with a shorter distance on the graph 245 tend to have more similar aggregated features. 246

Impact of training data selection. Another implication of the theoretical results is that the selection 247 of the training set plays an important role on the fairness of the learned GNN models. First, at a 248 population level, if the training set of choice leaves part of the unlabeled set far away, there will 249 likely be a large accuracy disparity. Second, a key ingredient in the proof of Lemma 1 is that the 250 predictions of the model on two nodes are more likely to be the same if they are close in terms of the 251 aggregated node features. This suggests that, when the shortest-path distance is a good indicator for 252 the similarity of the aggregated features, training nodes with higher *closeness centrality*⁵ may have a 253 higher impact on the behaviour of the learned model. More generally, the influence of training nodes 254 on the learned model may be relevant to their positions on the graph. 255

5 **Experiments** 256

In this section, we empirically verify the accuracy disparity suggested by our theoretical results. 257

General setup. We experiment on 4 popular GNN models, GCN [16], GAT [35], SGC [38], and 258 APPNP [17], as well as a MLP model for reference. For all the models, we use the implementations 259 in Deep Graph Library [37]. 40 independent trails are carried out for each experiment. 260

5.1 Accuracy Disparity Across Subgroups 261

Subgroups. We examine the accuracy disparity with *three types of* subgroups as described below. 262

Subgroup by aggregated-feature distance. In order to directly investigate the effect of ϵ_m on the 263 generalization bound (6), we first split the test nodes into subgroups by their distance to the training set 264

in terms of the aggregated features. As the GCN and GAT models are all two-layer GNNs, we use the 265

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two-step aggregated features to calculate the distance. In particular, denote the adjacency matrix of the graph G as $A \in \{0, 1\}^{N \times N}$ and the corresponding degree matrix as D, where D is a $N \times N$ diagonal 267

⁵Closeness centrality of node *i* is defined as $1/\sum_{j \in V \setminus \{i\}} d(i, j)$, where $d(\cdot, \cdot)$ is the shortest-path distance.

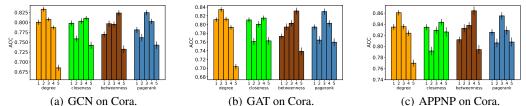


Figure 3: Test accuracy disparity across subgroups by node centrality. Each figure corresponds to the results of a pair of model and dataset, and each bar cluster corresponds to the subgroups defined by a certain centrality metric. In each cluster, the bars labeled from 1 to 5 represent subgroups with decreasing node centrality. Other settings are the same as Figure 1.

matrix with $D_{ii} = \sum_{j=1}^{N} A_{ij}, \forall i = 1, ..., N$. Given the feature matrix $X \in \mathbb{R}^{N \times D}$, The two-step aggregated features are obtained by $Z = (D+I)^{-1}(A+I)(D+I)^{-1}(A+I)X$. For each test node *i*, we define its aggregated-feature distance to the training set V_0 as $d_i = \min_{j \in V_0} ||Z_i - Z_j||_2$. Then we sort the test nodes according to this distance and split them into 5 equal-sized subgroups.

Subgroup by geodesic distance. As we discussed in Section 4.3, the geodesic distance on the graph may correlate with the aggregated-feature distance. So we also define subgroups based on the geodesic distance. We split the subgroups similarly by replacing S_i of each test node i as the minimum of the geodesic distances from i to each training node on the graph.

Subgroup by node centrality. Lastly, we also define subgroups based on 4 types of node centrality scores (degree, closeness, betweenness, and PageRank) of the test nodes. We split the subgroups by replacing S_i of each test node *i* as the centrality score of *i*. The purpose of this setup is to rule out a potential confounding factor that test nodes close to the training set may have high centrality scores.

Experiment setup. Following common GNN experiment setup [32], we randomly select 20 nodes
in each class for training, 500 nodes for validation, and 1,000 nodes for testing. Once training is done,
we report the test accuracy on subgroups defined by aggregated-feature distance, geodesic distance,
and node centrality in Figure 1, 2, and 3 respectively⁶.

Experiment results. First, as shown in Figure 1, there is a clear trend that the accuracy of a test subgroup decreases as the aggregated-feature distance between the test subgroup and the training set increases. And the trend is consistent for all 4 GNN models on all the datasets we test on (except for APPNP on Cora). This result verifies the existence of accuracy disparity suggested by Theorem 3.

Second, we observe in Figure 2 that there is a similar trend when we split subgroups by the geodesic distance. This suggests that the geodesic distance on the graph can be used as a simpler indicator in practice for machine learning fairness on real-world graph-structured data. Using such a classical network metric as an indicator also helps us connect graph-based machine learning to network theory, especially to understandings about social networks, to better analyze fairness issues of machine learning on social networks, where high-stake decisions related to human subjects may be involved.

Furthermore, as in Figure 3, there is no monotonic trend for test accuracy when we split subgroups by node centrality. This suggests that it is indeed the distance between the test subgroup and the training nodes, rather than the centrality of the test nodes alone, that influences the generalization error.

Finally, it is intriguing that, in both Figure 1 and 2, the test accuracy of MLP (which does not use the 297 graph structure) also decreases as the distance of a subgroup to the training set increases. This result 298 is perhaps not surprising if the subgroups were defined by distance on the original node features, as 299 MLP can be viewed as a special GNN where the feature aggregation function is an identity mapping, 300 so the "aggregated features" for MLP essentially equal to the original features. Our theoretical 301 analysis can then be similarly applied to MLP. The question is why there is also an accuracy disparity 302 w.r.t. the aggregated-feature distance and the geodesic distance. We suspect this is because these 303 304 datasets present homophily, i.e., original (non-aggregated) features of geodesically closer nodes tend to be more similar. As a result, a subgroup with smaller geodesic distance may also have closer node 305 features to the training set. To verify this hypothesis, we repeat the experiments in Figure 1, but with 306

⁶The main paper reports the results on selected datasets (Cora, Citeseer, and Pubmed for subgroups by aggregated-feature & geodesic distance, and Cora for node centrality. Results on more datasets are in Appendix C.

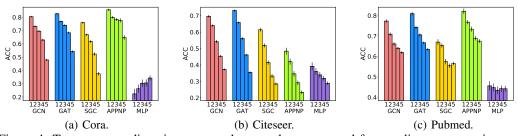


Figure 4: Test accuracy disparity across subgroups by aggregated-feature distance, experimented with noisy features. The experiment and plot settings are the same as Figure 1, except for the node features are perturbed by independent noises such that they are less homophilious.

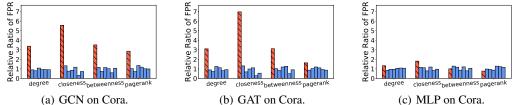


Figure 5: Relative ratio between the FPR under biased training node selection and the FPR under uniform training node selection. Each bar in each cluster corresponds to a class (there are 7 classes in total). The red shaded bar indicates the class with high centrality training nodes under the biased setup. Each cluster corresponds to a centrality metric being used for the biased node selection.

independent noises added to node features such that they become less homophilious. As in Figure 4, the decreasing pattern of test accuracy across subgroups remains for the 4 GNNs on all datasets;

while for MLP, the pattern disappears on Cora and Pubmed and becomes less sharp on Citeseer.

310 5.2 Impact of Biased Training Node Selection

In all the previous experiments, we follow the standard GNN training setup where 20 training nodes are uniformly sampled for each class. Next we investigate the impact if the selection of training nodes is biased, verifying our discussions in Section 4.3. We will demonstrate that the node centrality scores of the training nodes play an important role in the learned GNN model.

We choose a "dominant class" and construct a manipulated training set. For each class, we still sample 20 training nodes but in a biased way. For the dominant class, the sample is biased towards nodes of high centrality; while for other classes, the sample is biased towards nodes of low centrality. We evaluate the relative ratio of False Positive Rate (FPR) for each class between the setup using manipulated training set and the setup using uniformly sampled training set.

As shown in Figure 5, compared to MLP, the GNN models have significantly worse FPR for the dominant class when the training nodes are biased. This is because, after feature aggregation, there will be a larger proportion of test nodes that are closer to the training nodes of higher centrality. And the learned GNN model will be heavily biased towards the training labels of these nodes.

324 6 Discussion and Conclusion

We present a novel PAC-Bayesian analysis for the generalization ability of GNNs on node-level 325 semi-supervised learning tasks. As far as we know, this is the first generalization bound for GNNs 326 for non-IID node-level tasks without strong assumptions on the data generating mechanism. One 327 advantage of our analysis is that it can be applied to arbitrary subgroups of the test nodes, which 328 allows us to investigate an accuracy-disparity style of fairness for GNNs. Both the theoretical and 329 empirical results suggest that there is an accuracy disparity across subgroups of test nodes that have 330 varying distance to the training set, and nodes with larger geodesic distance to the training nodes suffer 331 from a lower classification accuracy. In reality, these nodes are likely to reside in underrepresented 332 marginalized communities or on the boundaries of large communities. In the future, we would like to 333 utilize our theoretical results to analyze other potential factors of the fairness of GNNs. 334

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451 Checklist

452	1. For all authors
453 454	(a) Do the main claims made in the abstract and introduction accurately reflect the paper's contributions and scope? [Yes]
455	(b) Did you describe the limitations of your work? [Yes]
456	(c) Did you discuss any potential negative societal impacts of your work? [Yes]
457 458	(d) Have you read the ethics review guidelines and ensured that your paper conforms to them? [Yes]
459	2. If you are including theoretical results
460	(a) Did you state the full set of assumptions of all theoretical results? [Yes]
461 462	(b) Did you include complete proofs of all theoretical results? [Yes] Proofs are provided in the appendix.
463	3. If you ran experiments
464 465 466	(a) Did you include the code, data, and instructions needed to reproduce the main experimental results (either in the supplemental material or as a URL)? [Yes] In the supplemental material.
467 468	(b) Did you specify all the training details (e.g., data splits, hyperparameters, how they were chosen)? [Yes]
469 470	(c) Did you report error bars (e.g., with respect to the random seed after running experi- ments multiple times)? [Yes]
471 472 473	(d) Did you include the total amount of compute and the type of resources used (e.g., type of GPUs, internal cluster, or cloud provider)? [No] The experiments in this study are not computationally expensive and the resources are less of interest.

 using/curating? [N/A] We are using widely-used benchmark datasets. (e) Did you discuss whether the data you are using/curating contains personally identifiable information or offensive content? [No] The benchmark datasets are already anonymized and widely used by the research community. 5. If you used crowdsourcing or conducted research with human subjects (a) Did you include the full text of instructions given to participants and screenshots, if applicable? [N/A] (b) Did you describe any potential participant risks, with links to Institutional Review Board (IRB) approvals, if applicable? [N/A] (c) Did you include the estimated hourly wage paid to participants and the total amount 	474	4. If you are using existing assets (e.g., code, data, models) or curating/releasing new assets
 (b) Did you mention the license of the assets? [No] Both the Deep Graph Library and benchmark datasets are commonly used in the community. (c) Did you include any new assets either in the supplemental material or as a URL? [Yes] We included our code in the supplemental material. (d) Did you discuss whether and how consent was obtained from people whose data you're using/curating? [N/A] We are using widely-used benchmark datasets. (e) Did you discuss whether the data you are using/curating contains personally identifiable information or offensive content? [No] The benchmark datasets are already anonymized and widely used by the research community. 5. If you used crowdsourcing or conducted research with human subjects (a) Did you include the full text of instructions given to participants and screenshots, if applicable? [N/A] (b) Did you describe any potential participant risks, with links to Institutional Review Board (IRB) approvals, if applicable? [N/A] (c) Did you include the estimated hourly wage paid to participants and the total amount 	475	
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 (c) Did you include any new assets either in the supplemental material or as a URL? [Yes] We included our code in the supplemental material. (d) Did you discuss whether and how consent was obtained from people whose data you're using/curating? [N/A] We are using widely-used benchmark datasets. (e) Did you discuss whether the data you are using/curating contains personally identifiable information or offensive content? [No] The benchmark datasets are already anonymized and widely used by the research community. 5. If you used crowdsourcing or conducted research with human subjects (a) Did you include the full text of instructions given to participants and screenshots, if applicable? [N/A] (b) Did you describe any potential participant risks, with links to Institutional Review Board (IRB) approvals, if applicable? [N/A] (c) Did you include the estimated hourly wage paid to participants and the total amount 	477	
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	490	Board (IRB) approvals, if applicable? [N/A]
492 spent on participant compensation? [N/A]	491	
	492	spent on participant compensation? [N/A]