Federated learning for competing risk analysis in healthcare

Anonymous Author(s)

ABSTRACT

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Performing survival analysis on distributed healthcare data is an important research problem as the existing privacy laws and emerging data-sharing regulations prohibit the sharing of sensitive patient data across multiple institutions. The distributed healthcare survival data is typically heterogeneous, non-uniformly censored, and comes from patients with multi-morbidities (competing events), which may lead to biased and inaccurate risk predictions. To address these challenges, we propose federated learning for survival analysis with competing events. Specifically, (a) we propose a simple algorithm to estimate consistent federated pseudo values for survival analysis with competing events and censoring; and (b) we introduce a novel and flexible federated pseudo-value-based deep learning framework named FedCRA, where we employ a transformer-based model; named TransPseudo, to enable subject-specific prediction of the marginal risk of an event while preserving the data privacy. Extensive experiments on two real-world distributed CRA datasets with non-IID and non-uniform censoring properties and on synthetic data with different censoring settings demonstrate that our FedCRA framework with the TransPseudo model performs better than the federated learning framework with state-of-the-art CRA models.

CCS CONCEPTS

Mathematics of computing → Survival analysis;
 Computing methodologies → Distributed artificial intelligence;
 Security and privacy;

KEYWORDS

Survival analysis; Federated Learning; Competing Risks; Censoring

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1 INTRODUCTION

Multimorbidity, i.e., the presence of two or more chronic conditions in a person, is a prevalent and urgent problem in healthcare [7, 16], especially among older patients. In the United States, the prevalence of more than 2 morbidities was 59.6%, whereas the percentage was 92% among individuals over 65 years during 2013-14 [11]. Multimorbid patients face the risk of adverse outcomes, such as mortality,

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Figure 1: Challenges of Federated CRA in SEER dataset

due to different clinically significant diseases like cancer or heart disease. These outcomes, such as death from cancer or death from heart disease, are considered competing events, and their risks are referred to as competing risks [13, 19].

The standard survival analysis, also known as time-to-event analysis, ignores the competing risks or treats the competing events as censoring in the marginal risk prediction of the event of interest, leading to biased and inaccurate risk predictions. Recently, machine learning models have been developed for competing risk analysis [10, 13, 19, 25], which have shown promising improvement over traditional statistical CRA models [6, 7] and achieved state-of-theart performance. However, a limited amount of survival data are typically collected by a single medical center due to resource and privacy constraints, which is insufficient to develop an efficient machine learning-based survival model for accurate risk predictions. The National Cancer Institute took a great initiative to collect large-scale survival data of registered breast cancer patients from the hospitals of several regions in the USA through the Surveillance, Epidemiology, and End Results (SEER)¹ program. However, such initiatives are expensive and time-consuming, and far fewer. On the other hand, while collaborations across multiple medical centers to gather harmonized large-scale datasets is feasible, such collaborations are hindered by the strict privacy laws and regulations on user data sharing, such as Health Insurance Portability and Accountability Act (HIPAA) and European Union's General Data Protection Regulation (GDPR). To overcome the data sharing limitations from multiple institutions, Federated Learning (FL) [15] has been proposed as a viable solution, where instead of sharing data, models are shared and trained among multiple institutions. In this paper, we study the problem of solving the competing risk analysis problem under the federated learning settings (with the assumption that data sharing is infeasible) and propose a federated competing risk analysis (FedCRA) framework. We are inspired by the recent success of federated survival analysis [2, 18, 21, 24] in achieving performance close to the gold-standard centralized training.

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¹https://seer.cancer.gov/

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Even though CRA is a well-studied problem [10, 13, 19, 25], we 117 found no work on modeling competing risks in an FL setting, espe-118 119 cially on some real-world challenges of FedCRA including non-IID data, and non-uniform censoring. In this paper, we investigate the 120 following challenges in FedCRA and develop novel methods to pro-121 vide potential solutions to the problems. Challenge 1: Data Heterogeneity: The dissimilarities in patient demographics, event dis-123 tributions, and clinical histories among various collaborative med-124 125 ical centers result in non-IID data. Challenge 2: Non-Uniform 126 Censoring (NUC): Censoring, i.e., partial information of subjects' event status, is a key challenge in survival analysis that leads to 127 128 biased and inaccurate risk prediction [22]. This bias exacerbates in FL due to the non-uniformity of censoring distributions across 129 clients, as shown in Figure 1 (Subplot: KM estimate of the survival 130 estimate). Moreover, the censoring rate also varies across different 131 132 medical centers, leading to heterogeneous data distributions and sub-optimal performance of the local survival models. 133

Proposed Solutions: To address the challenges in federated CRA, we propose first-of-its-kind federated pseudo-values-based deep learning framework, **FedCRA**, to solve CRA in an FL manner. We also propose a novel client-specific Transformer-based CRA model, **TransPseudo**. FedCRA jointly trains TransPseudo models in a federated framework to learn a global updated model without sharing raw data, which is further used to predict the probability of an event at or before time *t* due to cause *k*, i.e., cause-specific cumulative incidence function (**CIF**), given the covariates for a patient in a client. *We introduce federated pseudo-values to efficiently handle non-uniform censoring and account for the heterogeneity in event time and censoring distribution*. Our federated pseudo values preserve patient data privacy since they are derived from aggregated summary statistics (containing no identifying information) instead of raw data.



Figure 2: Benefit of participating in our FedCRA framework (TransPseudo-Federated). Our federated pseudo value-based TransPseudo model shows improvement in average C-Index performance over the local DeepHit and local TranPseudo models on distributed non-IID SEER datasets for all three clients (WEST, CENTRAL, and EAST regions).

We show in figure 2 that all decentralized clients can improve their prediction accuracy for CRA by participating in our FedCRA framework, thus, improving patients' outcomes. We also conduct extensive experiments on multiple realistic federated settings with real CRA data: SEER [19] and eICU [17] as well as on several synthetic datasets with different censoring settings to demonstrate the efficacy of our FedCRA framework to improve the model's performance preserving data privacy and to address data heterogeneity and non-uniform censoring. We show that our proposed FedCRA 175

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framework achieves close performance to the gold-standard centralized training on centrally aggregated data. Moreover, FedCRA performs better than the FL framework with SOTA CRA models.

2 PROPOSED FEDCRA FRAMEWORK

The recent success of pseudo value-based deep neural networks in standard survival analysis [20, 22], CRA [19] and federated survival analysis (FSA) [21] has motivated us to develop a pseudo-valuebased deep learning model for solving CRA in a federated manner. However, federated CRA is a more intricate problem due to the complex interaction between covariates and competing events and the real-world challenges in federated CRA, such as non-IID data and non-uniform censoring. As a result, simple deep neural networks need more learning capacity for obtaining accurate predictions and satisfactory performance in federated CRA. On the other hand, the transformer-based model has a strong learning capacity and has achieved SOTA performance in a wide range of tasks [8, 25], which motivates us to design transformer-based models for performing complex CRA in an FL manner. Therefore, we propose an FL framework for CRA; we call it FedCRA, where we first derive the pseudo values in a federated fashion and use them as response variables (ground truth) in our proposed client-specific Transformer-based models, TransPseudo. Then we conduct federated training with the TransPseudo models for learning the global model parameters.

Federated Pseudo Values for CIF: Due to censoring, i.e., incomplete event status or ground truth, the direct application of standard regression or classification techniques becomes infeasible. Pseudo values can be considered the natural replacement for the incompletely observed CIF [4], thus, can be used to efficiently handle censoring [1, 19, 26]. The traditional Jackknife pseudo values, computed on local client data, exhibit local consistency but suffer from global inconsistency due to heterogeneity in the event and censoring distributions of the clients. Computing pseudo values on merged data in a central server from clients can address the problem; however, data privacy laws and regulations make it infeasible. Moreover, the pseudo values, requiring leave-one-out computation for each subject in a sample, become computationally expensive and infeasible for federated CRA as the number of clients and sample size increases. To overcome these challenges, we introduce a novel federated pseudo values derivation approach for federated CRA, which uses the summary statistics from the clients instead of raw data that do not disclose the patient identifying information and, thus, preserve the data privacy. The leave-one-out computation required for pseudo values derivation is performed in parallel on the clients, reducing computational complexity and enabling scalability for FL. Furthermore, our federated pseudo values are directly derived from the estimate of global CIF, incorporating global information on the time-to-event distribution to account for the heterogeneity in client data. The federated pseudo values derivation approach is described as follows.

First, each client transforms the inputs, i.e., event time and status, into summary statistics, such as the number of subjects at risk at time t_0 ; (R_{0k}) , number of events (d_k) , number of subjects experienced event r; (d_{rk}) and number of censored (c_k) at a vector of unique time points (τ_k) in the local data. Clients send the summary statistics to the global server, where the server aggregates the summary statistics at the union of the vector of unique time points of

clients, $\tau = \bigcup_k \tau_k$, to form a global partial table. The global partial 233 table contains the total number of subjects at risk at time $t_0 \in \tau$, 234 R₀ = $\sum_{k=1}^{K} R_{0k}$, the total number of events, $d = \sum_{k=1}^{K} d_k$, the total number of subjects who experienced event r; $d_r = \sum_{k=1}^{K} d_{rk}$ and 235 236 237 the total number of censored, $c = \sum_{k=1}^{K} c_k$ at the vector of unique time points τ . The server fills up the partial table by computing the 238 239 number of subjects at risk at subsequent time points $(t_1, t_2, ..)$ using 240 the formula: $R_{t_j} = R_{t_{j-1}} - R_{t_{j-1}} - d_{t_{j-1}} - c_{t_{j-1}}$. Then, the server com-241 pute the global survival function as $\hat{S}_G(t) = \prod_{t_j \in \tau \leq t} (1 - \frac{d_{t_j}}{R_{t_j}})$ 242 243 and the global CIF as $\hat{F}_{Gr}(t) = \sum_{t_j \in \tau \leq t} \hat{S}_G(t) \frac{d_{rt_j}}{R_{t_i}}$. The global 244 server sends the global partial table and the global CIF to the 245 clients. Clients first create leave-one-out global partial tables by 246 omitting the *i*th subjects from the risk set $R(t_0)$ and from d, d_r, c 247 at which time point the event or censoring occurred (denoted as 248 $d^{-ik}, d_r^{-ik}, c^{-ik}$). Then clients fill the risk set at the subsequent 249 $d^{-ik}, d_r^{-ik}, c^{-ik}$). Then clients fill the risk set at the subsequent time points in the leave-one-out global partial table using the fol-lowing formula: $R_{tj}^{-ik} = R_{tj-1}^{-ik} - d_{tj-1}^{-ik} - c_{tj-1}^{-ik}$, where $t_j \in \tau$. Using the complete table, clients compute the leave-one-out global CIF as $\hat{F}_{Gr}^{-ik}(t) = \sum_{t_j \in \tau \le t} \hat{S}_{G}^{-ik}(t) \frac{d_{rtj}^{-ik}}{R_{rj}^{-ik}}$. Finally, each client computes the pseudo values for their subjects using the following equation: $J_{ikr}(t) = n\hat{F}_{Gr}(t) - (n-1)\hat{F}_{Gr}^{-ik}(t); i = 1, 2, ..., n_k, k = 1, 2, ..., K$. Here, n is the total number of subjects of all clients i.e. $n = \sum_{k=1}^{K} n_k$ and 250 251 252 253 254 255 256 257 *n* is the total number of subjects of all clients, i.e., $n = \sum_{i=1}^{K} n_k$ and 258 t can be a pre-specified single time point or a vector of time points, 259 Υ (provided by the user). $\hat{F}_{Gr}(t)$ is the AJ estimate of the global CIF 260 for event *r* at time *t* and $\hat{F}_{Gr}^{-ik}(t)$ is the leave-one-out AJ estimate of 261 the global CIF, obtained by omitting i^{th} subject from client k. For a 262 subject *i* in client *k*, pseudo values are calculated for all *R* causes 263 at a vector of pre-specified time points, Y. Our federated pseudo 264 values are directly derived from the consistent estimate of global 265 cumulative incidence function $F_r^G(t)$ [5] and can be shown to be 266 consistent by following the lemma 2 in [9]. 267

Federated Training: Our FedCRA framework employs our pro-268 posed client-specific TransPseudo models that communicate with a 269 global server. During each communication round, the global server 270 sends the clients a global TransCRA model represented by w^v . The 271 local clients then update their local models by incorporating the global model parameters and training their models using their re-273 spective local data. The newly trained local models denoted as 274 Δw_k^v , are then sent back to the global server. Using a standard FL 275 algorithm, FedAvg [15], the global server aggregates the updates 276 from the local models to update the global model. Subsequently, 277 the updated global model is sent back to the local clients by the 278 global server. This process is repeated for a specified number of 279 communication rounds, denoted as V. Once the V rounds are com-280 pleted, the globally updated model is utilized to make personalized 281 CIF predictions. 282

Proposed TransPseudo Model: Our TransPseudo model adapts the FT-Transformer (Feature Tokenizer + Transformer) architecture [8] and uses covariates as input and predicts CIF via federated pseudo values as response variables (ground truth). First, a Feature Tokenizer transforms the inputs X (both numerical and categorical covariates) into embeddings $T \in \mathbb{R}^{P \times q}$. The embeddings of all covariates (both numeric and categorical) are stacked to create an

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embedding matrix T. Then, a transformer module first appends the output token [OT] embedding to the embedding matrix T. After that a stack of L Transformer layers $F_1, F_2, ..., F_L$ are applied as: $T_i = F_i(T_{i-1})$ where $T_0 = stack[[OT], T]$. TransPseudo model predicts the CIF using the final representation of the output token [OT] as $\hat{F}(\tau) = Sigmoid(Linear(ReLU(LayerNorm(T_{\tau}^{[OT]})))).$ See the paper [8] for the details of the transformer module. We introduce a pseudo-value-based binary cross-entropy (PBC) loss for FedCRA with *R* competing events. The loss $L_k^{PBC}(t)$ for client *k* at time *t* is defined as, $L_k^{PBC}(t) = \frac{1}{n_k * R} \sum_{r=1}^R \sum_{i=1}^{n_k} - [\mathbb{I}(J_{ikr}(t) > 1)]$ $0.5)log\hat{F}(t|x_{ikr}) + (1 - \mathbb{I}(J_{ikr}(t) > 0.5))log(1 - \hat{F}(t|x_{ikr}))].$ where $\hat{F}(t|x_{ikr})$ and $J_{ikr}(t)$ respectively are the predicted CIF and the pseudo values at time point t for i^{th} individual in client k. Note that t can be a prespecified single time point or a vector of time points, Υ , where pseudo values are calculated based on the research interest. If we calculate the loss for a vector of time points, then the final loss is $\sum_{t} L_{k}^{PBC}(t)$.

3 EXPERIMENTS

We conduct extensive experiments to answer the following research questions. **Q1**: What are the advantages of employing federated pseudo values as opposed to traditional Jackknife pseudo values in the FedCRA framework? **Q2**: How does our FedCRA perform on real-world distributed CRA data with non-independent and identically distributed (Non-IID) and Non-uniform censoring properties compared to the FL framework with the state-of-the-art CRA approaches? **Q3**: How robust is the FedCRA framework under different types and amounts of censoring?

Synthetic datasets with different censoring mechanisms: To replicate different censoring scenarios in FL, we generate 5 distributed synthetic CRA datasets with different censoring mechanisms, such as (a) time censoring (TC), (b) interim censoring (IC), (c) case censoring (CC) with 25%, 50%, and 75% censoring [21], considering 10 decentralized clients assumed each client to have different covariate distributions (non-IID). To construct these datasets, we generate 12 numerical covariates from a multivariate normal distribution with mean *mu* and variance σ^2 . Additionally, we generate two binary variables from a binomial distribution with probability *p*. Survival times are generated from exponential distribution considering the linear and nonlinear interaction among covariates.

SEER Data: The Surveillance, Epidemiology, and End Results (SEER) ² program of the National Cancer Institute collected data from breast cancer patients registered at multiple hospitals in the United States to provide cancer statistics in the United States. The dataset contains 6 competing events and 28366 patients, out of which 23.2% patients died of cervical cancer (**CC**), 2.6% died due to other cancers (**OCN**), 2.4% died of cardiovascular disease (**CVD**), 1.1% died due to chronic medical disease (**CMD**), 0.6% died of infectious disease (**ID**), and 1.8% died due to other causes (**OCS**) [19]. To replicate a realistic distributed CRA data scenario with non-uniform censoring (NUC) for FL, we first partitioned the SEER data into 3 clients based on the regions of the hospitals: West, Central, and East. Next, we chose a fixed number of subjects for all clients based on the minimum number of censored and uncensored subjects in

²https://seer.cancer.gov/

the clients. Then, we varied the censoring percentages chosen from
[0.2, 0.3, 0.4, 0.50, 0.55] for each client and adjusted the number
of uncensored subjects by subtracting the number of selected censored subjects from the total fixed number of subjects. This setup
enables us to evaluate FL models in a geographically distributed
data environment and under non-uniform censoring settings.

eICU Data: The eICU dataset is a widely used public clinical 355 dataset obtained from the eICU Collaborative Research Database 356 357 [17], where data are collected from patients admitted to the ICU 358 setting and gathered from multiple hospitals in the United States. We extracted 17342 patients who were diagnosed with one or more 359 of the following four diseases: cancer (CN), liver disease (LV), im-360 munosuppression (IM), and diabetes (DI). Death from each disease 361 is considered a competing event, and we only consider the death of 362 patients diagnosed with a single disease as an event. We imputed 363 the missing values using Multivariate Imputation by Chained Equa-364 tions (MICE) [23] separately for each client. To simulate real-world 365 non-IID distributed CRA data, we partitioned the eICU dataset 366 into 4 clients based on the region of the hospital: (1) Midwest, (2) 367 Northeast, (3) South, and (4) West. 368

Experimental Setup: To evaluate the performance of the models, we consider three training setups: (1) *Gold standard centralized training:* models are trained on combined training data shared from clients to the server, (2) *Local training:* clients' own data are used to train their models locally, and (3) *Federated training:* clients
communicate with a global server by sharing their models instead of raw training data to update a global model.

Evaluation Criteria: In both centralized and federated settings,
we use the combined test data from clients to evaluate the models.
We also use the client's local test data to evaluate the locally trained
models as well as federated trained local models (training of updated
global model by FL on local client data). We use the time-dependent
concordance index (C-Index) [3] as our evaluation metric and use
pycox [12] package to compute them.

383 Implementation Details: Each client's data is randomly split 384 into 80% training and 20% test data. We use 10% or 20% of the training data as validation sets. We ran the experiment 5 times with 385 different random initialization or a different set of censoring per-386 centages (for SEER) and reported the average performance with cor-387 responding standard deviation. We train our proposed TransPseudo 388 models using the Adam optimizer [14] with an early stopping cri-389 terion based on the best validation loss. We use a learning rate 390 scheduler and select the batch size from [512, 1024]. For a central-391 ized setting, the models are trained up to 500 epochs with a patience 392 393 of 10. For the federated settings, we perform a hyperparameter tuning to select the best learning rate, the number of local epochs, and 394 total communication rounds. Based on the hyper-parameter tuning, 395 396 we choose the learning rate, the number of local epochs, and total 397 communication rounds 0.0001, 20, and 20, respectively. To obtain the prediction of CIF, we use Sigmoid activation function in the 398 final output layer. We set 10^{th} to 99^{th} percentile of the time horizon 399 with an interval of 10 for SEER and Synthetic datasets and [10, 20, 400 40, 80, 160, 320, 740] for eICU dataset, as the pre-specified time 401 points for calculating pseudo values and evaluating the models. 402

Models Comparison: We compare our proposed FL framework FedCRA with our proposed client-specific models, TransPseudo,

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to FL framework with three state-of-the-art CRA models: i) Statistical model, Cause-specific Cox proportional hazard model (**CS-CoxPH**) [6] ii) Deep-learning-based model, **DeepHit** [13], and iii) Transformer-based model, **SurvTRACE** [25].

4 RESULTS AND DISCUSSION

Jackknife pseudo values vs. federated pseudo values: To show the effectiveness of employing our proposed federated pseudo values in our FedCRA framework as opposed to the traditional jackknife pseudo values, we evaluate and compare the performance of federated trained and locally trained TransPseudo models using both pseudo values on the combined test set and the local test sets of distributed SEER and eICU datasets. Table 1 demonstrates that the TransPseudo model with our proposed federated pseudo values shows up to 9% improvement over the traditional Jackknife pseudo values in terms of C-Index.

Table 1: Comparing federated and Jackknife pseudo values using TransPseudo model

Dataset	Combined test data	local test data				
	Federated Training	local Training	Federated Training			
	Jackknife Fed. Pseudo	Jackknife Fed. Pseudo	Jackknife Fed. Pseudo			
SEER	0.72 (0.032) 0.83 (0.019)	0.80 (0.011) 0.86 (0.007)	0.80 (0.018) 0.91 (0.017)			
eICU	0.74 (0.006) 0.83 (0.008)	0.75 (0.035) 0.83 (0.016)	0.79 (0.019) 0.87 (0.017)			

Comparing model performance on real-world distributed CRA datasets: Table 2 shows that our TransPseudo model outperforms CS-CoxPH, DeepHit, and SurvTRACE by 10.2%, 5.5%, and 5.8% in the centralized setting, $8.0\%,\,3.5\%,\,and\,4.1\%$ in local training, and 11.8%, 3.5% 8.5% in federated setting evaluated on the local test set of SEER data, respectively. DeepHit and TransPseudo perform similarly in the federated setting evaluated on the combined test set of SEER data. However, TransPseudo outperforms CS-CoxPH and SurvTRACE by 4.7% and 2.3%. Our TransPseudo model, compared to CS-CoxPH, DeepHit, and SurvTRACE, respectively, obtains 9.8%, 20.8%, and 6.5% better C-Index in the centralized setting, 15.5%, 16.5%, and 11.8% in local training, 5.5%, 14% and 6.5% in federated setting evaluated on the combined test set of eICU data and 12.3%, 8.7% and 12% in federated setting evaluated on the local test set of eICU data. Our findings highlight the effectiveness of TransPseudo in improving the local performance of the models and suggest the potential of FL for CRA.

Comparing model performance on various censoring settings: Table 3 demonstrates that our TransPseudo model achieves 9.3% and 5.6% overall improvement over the DeepHit and Surv-TRACE models, respectively, in the centralized setting evaluated on the combined test set of synthetic datasets with different censoring mechanisms, such as time censoring (TC), Interim Censoring (IC) and Case Censoring (CC). In the federated settings, our TransCRA model outperforms DeepHit by 5.8% and shows similar performance as the SurvTRACE model. The results support the effectiveness of using federated pseudo values in the TransPseudo model to handle different types of censoring.

Limitations: While our TransPseudo provides accurate predictions, they require more computational time and resources for training than the simple DNN and statistical models, such as DeepHit and CS-CoxPH. The model is unsuitable for datasets with many features,

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Table 2: C-Index comparison of the models on the SEER and eICU datasets

Setup	↓ Model		SEER					eICU			
	$Event \rightarrow$	СС	OCN	CVD	CMD	ID	OCS	CN	LV	IM	DI
Centralized (Combined Test Data)	CS-CoxPH	0.79 (0.015)	0.78 (0.010)	0.80 (0.007)	0.84 (0.023)	0.68 (0.207)	0.77 (0.026)	0.80 (0.001)	0.71 (0.117)	0.72 (0.008)	0.80 (0.000)
	DeepHit	0.88 (0.010)	0.85 (0.018)	0.82 (0.018)	0.76 (0.046)	0.81 (0.107)	0.82 (0.022)	0.71 (0.022)	0.65 (0.071)	0.56 (0.058)	0.67 (0.026)
	SurvTRACE	0.84 (0.028)	0.83 (0.025)	0.83 (0.026)	0.79 (0.051)	0.83 (0.080)	0.80 (0.067)	0.77 (0.015)	0.82 (0.035)	0.76 (0.021)	0.81 (0.006)
	TransPseudo	0.87 (0.006)	0.88 (0.027)	0.88 (0.018)	0.89 (0.065)	0.89 (0.064)	0.86 (0.010)	0.82(0.018)	0.89 (0.028)	0.82 (0.034)	0.89 (0.014)
Federated (Combined Test Data)	CS-CoxPH	0.79 (0.013)	0.79 (0.007)	0.80 (0.009)	0.84 (0.022)	0.75 (0.027)	0.76 (0.031)	0.79 (0.001)	0.80 (0.004)	0.70 (0.007)	0.80 (0.000)
	DeepHit	0.83 (0.008)	0.83 (0.030)	0.86 (0.014)	0.84 (0.049)	0.87 (0.038)	0.82 (0.028)	0.71 (0.024)	0.68 (0.022)	0.59 (0.021)	0.77 (0.019)
	SurvTRACE	0.82 (0.007)	0.81 (0.025)	0.82 (0.017)	0.78 (0.078)	0.84 (0.058)	0.80 (0.051)	0.75 (0.009)	0.80 (0.034)	0.72 (0.043)	0.78 (0.008)
	TransPseudo	0.80 (0.007)	0.82 (0.041)	0.83 (0.013)	0.87 (0.034)	0.86 (0.073)	0.83 (0.021)	0.81(0.021)	0.87 (0.027)	0.83 (0.012)	0.80 (0.014)
Local	CS-CoxPH	0.79 (0.033)	0.79 (0.047)	0.81 (0.040)	0.84 (0.042)	0.68 (0.119)	0.78 (0.056)	0.69 (0.012)	0.63 (0.035)	0.61 (0.051)	0.80 (0.017)
Training (Local	DeepHit	0.87 (0.007)	0.82 (0.028)	0.83 (0.017)	0.78 (0.076)	0.83 (0.065)	0.83 (0.033)	0.67 (0.039)	0.67 (0.049)	0.56 (0.063)	0.79 (0.007)
	SurvTRACE	0.84 (0.028)	0.83 (0.025)	0.83 (0.026)	0.79 (0.051)	0.83 (0.080)	0.80 (0.067)	0.70 (0.030)	0.67 (0.009)	0.71 (0.037)	0.80 (0.010)
Test Data)	TransPseudo	0.88 (0.004)	0.87 (0.017)	0.86 (0.019)	0.91 (0.020)	0.84 (0.021)	0.81 (0.025)	0.86 (0.029)	0.78 (0.061)	0.82 (0.014)	0.89 (0.010)
Local Federated	CS-CoxPH	0.79 (0.028)	0.79 (0.040)	0.80 (0.042)	0.84 (0.037)	0.74 (0.105)	0.77 (0.052)	0.76 (0.000)	0.73 (0.005)	0.68 (0.007)	0.82 (0.001)
	DeepHit	0.88 (0.009)	0.85 (0.022)	0.88 (0.020)	0.86 (0.056)	0.90 (0.040)	0.86 (0.027)	0.83 (0.012)	0.79 (0.021)	0.71 (0.052)	0.80 (0.017)
(Local	SurvTRACE	0.87 (0.002)	0.82 (0.035)	0.81 (0.026)	0.79 (0.048)	0.83 (0.091)	0.81 (0.049)	0.76 (0.059)	0.69 (0.031)	0.76 (0.042)	0.79 (0.006)
Test Data)	TransPseudo	0.87 (0.014)	0.91 (0.021)	0.91 (0.018)	0.95 (0.022)	0.91 (0.061)	0.89 (0.020)	0.89 (0.007)	0.82 (0.036)	0.88 (0.029)	0.89 (0.002)

Table 3: Model comparison on different censoring settings

Setup	Model	тс	IC	CC25	CC50	CC75
Centralized	DeepHit	0.68 (0.009)	0.68 (0.012)	0.65 (0.004)	0.67 (0.007)	0.72 (0.007)
	SurvTRACE	0.72 (0.014)	0.69 (0.015)	0.67 (0.006)	0.67 (0.009)	0.67 (0.008)
	TransPseudo	0.79 (0.005)	0.79 (0.005)	0.75 (0.009)	0.80 (0.004)	0.82 (0.008)
Federated	DeepHit	0.66 (0.007)	0.66 (0.006)	0.65 (0.006)	0.65 (0.009)	0.65 (0.002)
	SurvTRACE	0.70 (0.004)	0.68 (0.005)	0.67 (0.009)	0.68 (0.007)	0.71 (0.009)
	TransPseudo	0.72 (0.008)	0.71 (0.009)	0.68 (0.006)	0.71 (0.011)	0.76 (0.007)

especially in the cross-device FL, where resource constraint is an important issue. The computational burden of our model comes from the quadratic complexity of the vanilla Multi-Head Self-Attention (MHSA) with respect to the number of features. Gorishniy et al. [8] suggest efficiently approximating the MHSA or distilling the Transformer models with feature tokenizer into simpler architectures for better inference. Our federated pseudo values address data heterogeneity in terms of non-IID time-to-event/censoring distributions. However, feature distributions are still different, i.e., non-IID across the clients, which requires a specialized FL algorithm.

5 CONCLUSION

Competing risk analysis (CRA) is an important problem ignored in the existing federated survival analysis. In this paper, we proposed a first-of-its-kind pseudo-value-based federated framework for CRA, **FedCRA**, to estimate the subject-specific CIF in the presence of competing events and censoring. We also proposed a transformerbased model- TransPseudo for CRA. We introduce a federated pseudo values derivation approach that allows us to analyze the CRA data in a federated framework preserving privacy. We conduct experiments on real and synthetic distributed CRA data with non-IID, non-uniform censoring properties and show that our FedCRA framework is better than FL framework with SOTA CRA models.

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