# **Fine-tuning Diffusion Models with Limited Data**

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#### Abstract

Diffusion models have recently shown remarkable progress, demonstrating state-of-1 the-art image generation qualities. Like the other high-fidelity generative models, 2 diffusion models require a large amount of data and computing time for stable З training, which hinders the application of diffusion models for limited data settings. 4 To overcome this issue, one can employ a pre-trained diffusion model built on a 5 large-scale dataset and fine-tune it on a target dataset. Unfortunately, as we show 6 empirically, this easily results in overfitting. In this paper, we propose an efficient 7 fine-tuning algorithm for diffusion models that can efficiently and robustly train 8 on limited data settings. We first show that fine-tuning only the small subset of 9 the pre-trained parameters can efficiently learn the target dataset with much less 10 overfitting. Then we further introduce a lightweight adapter module that can be 11 attached to the pre-trained model with minimal overhead and show that fine-tuning 12 with our adapter module significantly improves the image generation quality. We 13 demonstrate the effectiveness of our method on various real-world image datasets. 14

#### 15 **1** Introduction

Diffusion models [35, 13] have become a mainstream approach in image synthesis, quickly taking 16 over the crown of Generative Adversarial Networks (GANs) [10] in the literature. Compared to 17 Variational Autoencoder (VAE) variants [20, 41, 5] or autoregressive models [42, 8] which are trained 18 to maximize likelihoods instead of directly optimizing image quality, diffusion models can be trained 19 to generate more realistic images with less number of parameters [13, 26]. Similar to the other 20 generative models, diffusion models require tons of data and training times to produce diverse images 21 of high quality. Even a simple diffusion model would require several GPU days to train on CIFAR-10 22 or ImageNet benchmark. This computational cost acts as a bottleneck, limiting the scalability of 23 diffusion models to applications where data are scarce. To resolve this issue common in high-fidelity 24 25 generative models, several approaches have been proposed. We offer a detailed review of recent 26 works in Appendix B. However, for diffusion models, except for fine-tuning methods for conditional generation [34, 9], there has been little work on fine-tuning pre-trained unconditional diffusion models 27 for target domain with limited data. 28

In this paper, we propose a novel fine-tuning algorithm for unconditional diffusion models under 29 limited data settings. This is a challenging task because it is prone to overfitting due to small data 30 and any regularization technique depending on conditional inputs is not available unlike conditional 31 settings [31]. A nave fine-tuning method of updating all weights easily results in overfitting, so 32 as done in existing transfer learning studies [44, 40, 24], a thorough study on which weights to 33 freeze and tune is required. Through empirical analysis, we first identify that the attention modules 34 common in the diffusion models are crucial for quick adaptation to the target domain, and fine-tuning 35 only the attention modules could significantly alleviate the overfitting. This is somewhat surprising 36 considering that the attention modules take only a small fraction (about 10%) of parameters in the 37 entire network for the diffusion model. Inspired by the adapter approach for language models [15], 38

Under review at the NeurIPS 2022 Workshop on Score-Based Methods. Do not distribute.

we further design a novel adapter module that can be attached to the pre-trained model and fine-tuned 39 with negligible additional parameters. Unlike the adapter module commonly applied for language 40 models, due to the nature of the diffusion models, our adapter module is time-aware, and we find 41 this time awareness is crucial for successful fine-tuning. Especially, we find that the adapter module 42 plays an important role under a large domain gap between source pre-training and target fine-tuning 43 data. Combining the idea of fine-tuning only the attention modules in the pre-trained model and 44 the fine-tuning with the adapter module, we present Adapter-Augmented Attention Fine-tuning 45  $(A^{3}FT)$  which efficiently learns on target tasks with limited data, converging faster with much less 46 overfitting than existing fine-tuning. We empirically demonstrate the effectiveness of our method on 47 real-world image synthesis tasks. 48

### 49 2 Methods



**Figure 1:** ImageNet pre-trained diffusion model fine-tuned with (left) 1000 CelebA images and (right) 400 Pokemon images. cFID is computed between the whole training dataset and 10K/5K samples from CelebA/Pokemon dataset, respectively. While naïve fine-tuning exhibit overfitting behavior, our methods, attention-block fine-tuning and A<sup>3</sup>FT, successfully mitigate overfitting. A<sup>3</sup>FT further achieves the best cFID.

#### 50 2.1 Naïve fine-tuning

Naïvely fine-tuning entire parameters of a pre-trained model with limited target data would be a straightforward approach, but it is well-known that this is prone to overfitting [45, 25]. As we empirically validate this for diffusion models in Fig. 1, the naïve fine-tuning causes overfitting in the early stage of training. In Fig. 3, we further verify that the quality and diversity of the images generated from the overfitted models are seriously damaged, and the models tend to memorize few images in target training data.

#### 57 2.2 Attention block fine-tuning

Most of the modern diffusion models employ U-Net [30] as a backbone architecture, which consists 58 of a stack of residual and attention blocks intertwined with skip connections. At a high level, a U-Net 59 is divided into an encoder and a decoder, where the encoder gradually downsamples images into 60 multi-scale features, and the decoder upsamples them back to the original sizes. Instead of fine-tuning 61 all the parameters, we fine-tune attention blocks while freezing residual blocks. As shown in Fig. 1, 62 the attention block fine-tuning works surprisingly well, significantly outperforming naïve fine-tuning. 63 Especially, attention block fine-tuning is not only more stabilized, but also achieves better image 64 quality in terms of cFID score [28]. Attention block tuning is more memory-efficient since it only 65 takes 10.3% of the total parameters. 66

#### 67 2.3 Time-aware adapter

While the attention block fine-tuning works well, as demonstrated by the adapter-based methods for 68 language models [15, 16], it is often beneficial to attach additional modules to the pre-trained model 69 for better adaptation to target data. Inspired by this, we develop a novel adapter module tailored for 70 diffusion models. Importantly, our adapter is *time-aware*, since the networks being used for diffusion 71 models should produce different outputs with respect to different time steps. As depicted in Fig. 2, 72 the time-aware adapter is placed between the attention block and its successive linear layer so as 73 to modulate the intermediate feature vector given the target data. Compared to the conventional 74 adapters, our adapter additionally takes time embedding vector  $t_{\text{embed}} \in \mathbb{R}^{d_t - 1}$  as an input along with feature tensor  $z_{\text{in}} \in \mathbb{R}^{c_z \times h_z \times w_z}$ , hence the name time-aware. A time-aware adapter is composed of 75 76 three submodules; a time-fusion module, a cross-attention module, and a time-scaling module. 77

**Time-fusion module** Time-fusion networks combines the time-embedding vector  $t_{embed}$  and an input feature vector  $z_{in}$  into another feature vector through feed-forward layers, which is then layer-normalized [1]. Refer to Appendix C.4 for details. The resulting feature vector  $z_{query} \in \mathbb{R}^{c_z \times h_z \times w_z}$  is fed into the crossattention module as a query. That is,

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$$z_{\text{query}} = \text{LN}(\text{FF}(z_{\text{in}}, t_{\text{embed}})),$$
 (1)

where  $LN(\cdot)$  denotes layer normalization and FF( $\cdot$ ) denotes feed-forward layers. Time-fusion modules use approximately 123K parameters ( $\approx 0.1\%$  of the pre-trained model).

91 **Cross-attention module** Cross-attention mod-92 ule takes  $z_{query}$  as a query, and  $z_{in}$  as both key 93 and value vectors with the same dimension. 94 We then apply channel-wise cross attention fol-95 lowed by layer normalization to produce an out-96 put tensor  $z_{out} \in \mathbb{R}^{c_z \times h_z \times w_z}$ .

97 
$$z_{\text{out}} = \text{LN}(\text{CrossAttn}(z_{\text{query}}, z_{\text{in}}, z_{\text{in}})).$$
 (2)

98 Cross-attention modules use approximately 99 1.6M parameters ( $\approx 1.3\%$  of the pre-trained 100 model).



**Figure 2:** Schematic for the time-aware adapter. Time-aware adapter is designed to fit inside an attention block. We introduce three adapter submodules: a time-fusion module, a cross-attention module, and a time-scaling module. Time-aware adapters take up to 5.4M parameters ( $\approx 4.5\%$  of the pre-trained diffusion model).

**Time-scaling module** Motivated by Hong et al. [14], the time-scaling module computes the mixture factor  $\alpha_t \in [0, 1]^{c_z \times h_z \times w_z}$  that regulates the information generated by the time-aware adapter. Here, the mixture factor  $\alpha_t$  is also time-aware so that the effect of the adapter output can vary along time steps. The final output of the time-aware adapter is computed as

$$h_{\text{out}} = \text{FF}((1 - \alpha_t) \odot z_{\text{in}} + \alpha_t \odot z_{\text{out}}), \tag{3}$$

where  $\odot$  denotes the elementwise multiplication. Time-scaling modules use approximately 3.8M parameters ( $\approx 3.1\%$  of the pre-trained model).

#### **108 2.4 Adapter-augmented attention fine-tuning**

Combining the attention block fine-tuning and time-aware adapter, we present Adapter-Augmented Attention Fine-tuning  $(A^3FT)$  which fine-tunes attention blocks along with the time-aware adapter attached to the pre-trained model. We will demonstrate through experiments in Section 3, the timeaware adapter can seamlessly be trained with the attention blocks, leading to a significant performance

113 gain across datasets.

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<sup>&</sup>lt;sup>1</sup>For the time embedding vector, rather than introducing a new embedding network, we just reuse the time embedding vector of the pre-trained model.

#### 114 **3 Experiments**

Our method is tested on two datasets: CelebA [23] and Pokemon (pokemon.com). See Appendix C 115 for further experimental details. Table 1 summarizes our main results. We validate that naïve fine-116 tuning easily overfits to small-size training datasets yielding high cFID and KID. On the other hand, 117 attention-block fine-tuning largely outperforms naïve fine-tuning on both datasets. Further, with the 118 help of time-aware adapter, A<sup>3</sup>FT achieves the lowest cFID and KID score. In Fig. 3, we notice the 119 distinct difference in sample quality. While naïvely fine-tuned model produces relatively simple 120 images, attention-block fine-tuning and A<sup>3</sup>FT yield both diverse and high-quality images. We provide 121 122 the sampled images on CelebA in Appendix D.

**Table 1:** Sample quality evaluation on CelebA and Pokemon datasets. We report metrics computed after fine-tuning for 500 and 1000 epochs on CelebA and Pokemon datasets, respectively. A<sup>3</sup>FT surpasses naïve and attention-block fine-tuning in terms of cFID and KID.

Methods	$ImageNet \rightarrow CelebA$		ImageNet $\rightarrow$ Pokemon	
	cFID	KID	cFID	KID
Naïve fine-tuning Attention-block fine-tuning A <sup>3</sup> FT	15.746 7.922 6.843	0.010 0.005 <b>0.004</b>	57.505 39.835 <b>38.398</b>	0.025 0.013 0.012



**Figure 3:** Selected samples after fine-tuning 1000 epochs on Pokemon dataset: naïve fine-tuning (left; cFID 57.505), attention-block fine-tuning (middle; cFID 39.835), A<sup>3</sup>FT (right; cFID 38.398).

#### 123 4 Conclusion

In this paper, we empirically showed that naïvely fine-tuning diffusion models incurs overfitting in the early stage of training. As a solution, we discovered that fine-tuning only attention blocks can be a simple yet solid fine-tuning technique. To enhance the fine-tuning performance, we introduced the time-aware adapter that integrates a time-embedding vector so as to fit diffusion models. We further proposed a novel fine-tuning method, Adapter-Augmented Attention Fine-tuning, which fine-tunes attention blocks in conjunction with the time-aware adapter. Experiments validated that our approach enables faster and more stable fine-tuning with limited data as well as retaining high-quality samples.

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#### Background А 250

We provide a brief summary of diffusion models. We follow the standard formulation and nota-251 252 tions [35, 37, 13].

A diffusion model is a class of latent variable models with a Markov chain of latent variables 253 describing the generative process. Given a data  $\mathbf{x}_0 \sim p_{\text{data}}(\mathbf{x}) := q(\mathbf{x})$ , a forward process injects a 254 series of Markovian Gaussian noises with a sequence of controlled variances  $\{\beta_t\}_{t=1}^{\hat{T}}$  over T steps, 255 until the perturbed data  $\mathbf{x}_T$  is nearly isotropic Gaussian distributed: 256

$$q(\mathbf{x}_t|\mathbf{x}_{t-1}) := \mathcal{N}(\mathbf{x}_t; \sqrt{1 - \beta_t} \mathbf{x}_{t-1}, \beta_t \mathbf{I}) \text{ for } t = 1, \dots, T-1, \quad q(\mathbf{x}_T|\mathbf{x}_0) \approx \mathcal{N}(\mathbf{x}_T; \mathbf{0}, \mathbf{I}).$$
(4)

Reversing the forward process, a backward diffusion process will bring an isotropic Gaussian noise 258  $\mathbf{x}_T \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$  to a sample from the data distribution  $\mathbf{x}_0 \sim q(\mathbf{x}_0)$ . Since the backward process 259  $q(\mathbf{x}_t|\mathbf{x}_{t-1})$  is intractable, we introduce an approximate backward process defined with the model 260  $p_{\theta}(\mathbf{x}_t | \mathbf{x}_{t-1})$  parameterized by  $\theta$ : 261

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$$p_{\theta}(\mathbf{x}_{t-1}|\mathbf{x}_t) := \mathcal{N}(\mathbf{x}_{t-1}; \boldsymbol{\mu}_{\theta}(\mathbf{x}_t, t), \boldsymbol{\Sigma}_{\theta}(\mathbf{x}_t, t)) \text{ for } t = 1, \dots, T.$$
(5)

Then we can optimize the parameter  $\theta$  by maximizing the variational lower-bound, or minimizing the 263 negative of the variational lower bound. 264

$$\mathcal{L}_{\text{vlb}} := \mathbb{E}_{q(\mathbf{x}_{0:T})} \left[ -\log \frac{p_{\theta}(\mathbf{x}_{0:T})}{q(\mathbf{x}_{1:T}|\mathbf{x}_{0})} \right] \ge \mathbb{E}_{q(\mathbf{x}_{0})} \left[ -\log p_{\theta}(\mathbf{x}_{0}) \right].$$
(6)

By Bayes' rule and Markov property, one can easily derive that 266

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$$q(\mathbf{x}_{t-1}|\mathbf{x}_t, \mathbf{x}_0) = \mathcal{N}(\mathbf{x}_{t-1}; \tilde{\boldsymbol{\mu}}_t(\mathbf{x}_t, \mathbf{x}_0), \beta_t \mathbf{I})$$
(7)

$$\tilde{\boldsymbol{\mu}}_{t}(\mathbf{x}_{t}, \mathbf{x}_{0}) := \frac{\sqrt{\bar{\alpha}_{t-1}}\beta_{t}}{1 - \bar{\alpha}_{t}} \mathbf{x}_{0} + \frac{\sqrt{\alpha_{t}}(1 - \bar{\alpha}_{t-1})}{1 - \bar{\alpha}_{t}} \mathbf{x}_{t}, \quad \tilde{\beta}_{t} := \frac{1 - \bar{\alpha}_{t-1}}{1 - \bar{\alpha}_{t}} \beta_{t}, \quad \bar{\alpha}_{t} := \prod_{i=1}^{\iota} (1 - \beta_{i}), \quad (8)$$

and the variational objective (6) boils down to 269

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$$\mathcal{L}_{\text{vlb}} \equiv \mathbb{E}_{t,\mathbf{x}_0} \left[ \frac{1}{2||\boldsymbol{\Sigma}_{\theta}(\mathbf{x}_t, t)||^2} || \tilde{\boldsymbol{\mu}}_t(\mathbf{x}_t, \mathbf{x}_0) - \boldsymbol{\mu}_{\theta}(\mathbf{x}_t, t) ||^2 \right],\tag{9}$$

where  $\equiv$  denotes the equality up to a constant. Employing reparameterization for Gaussians [20], Ho 271 et al. [13] proposes to further simplify the objective as 272

$$\mathcal{L}_{\text{simple}} \equiv \mathbb{E}_{t,\mathbf{x}_{0},\boldsymbol{\epsilon}_{t}} \left[ ||\boldsymbol{\epsilon}_{t} - \boldsymbol{\epsilon}_{\theta}(\mathbf{x}_{t},t)||^{2} \right], \tag{10}$$

where we parameterize the noise  $\epsilon_{\theta}$  instead of the mean  $\mu_{\theta}$  and the scaling factors  $\|\Sigma_{\theta}(\mathbf{x}_t, t)\|^2$  are 274 discarded to have uniform loss weights for all time steps.<sup>2</sup> 275

While Ho et al. [13] demonstrated that using fixed variance schedules for the model distributions 276 empirically working well, that is, setting  $\Sigma_{\theta}(\mathbf{x}_t, t) = \sigma_t^2 \mathbf{I}$ , Nichol and Dhariwal [26] later showed 277 that one can improve upon fixed variance with the variances parameterized by weighting vector v, 278  $\Sigma_{\theta}(\mathbf{x}_t, t) = \exp(v \log \beta_t + (1 - v) \log \dot{\beta}_t)$ . Since the simplified objective (10) dropping the scaling 279 factors does not contain the variance terms, Nichol and Dhariwal [26] proposed to optimize a hybrid 280 objective defined as 281 282

$$\mathcal{L}_{\text{hybrid}} = \mathcal{L}_{\text{simple}} + \lambda \mathcal{L}_{\text{vlb}}, \qquad (11)$$

for some  $\lambda > 0$ , together with cosine annealing variance scheduling which is specifically tailored for 283 the low-resolution images (e.g.,  $64 \times 64$  or  $32 \times 32$  images). We follow the training scheme and model 284 architecture described in Nichol and Dhariwal [26] throughout our experiments. 285

<sup>&</sup>lt;sup>2</sup>Of note, not only straight-forward, the simple loss resembles the score matching loss in noise-conditioned score networks [37]. Forward and reverse processes each can be mapped to noise conditional score matching and Langevin dynamics. Such connection laid the groundwork for score-based continuous diffusion models [6, 38, 12]. The uniform weighting is reported to enhance image quality while sacrificing the log-likelihood values of generated images [13].

#### 286 **B** Related works

**Generative models for image synthesis** Generative models for image synthesis are largely categorized into likelihood-based approaches [20, 41, 5, 42, 8] and GANS [10, 18, 3]. Diffusion models have recently gained popularity due to their ability to generate high-quality images [36, 13, 6]. Most modern generative models use deep neural networks requiring a large amount of training data, so they usually suffer from overfitting when trained with limited data.

**Image synthesis with limited data** Multiple works have been proposed to improve the performance 292 of image synthesis when the number of data is limited. For GAN-based methods, Karras et al. 293 [17], Zhao et al. [47] propose data augmentation techniques to prevent discriminator overfitting. 294 Liu et al. [22] propose a lightweight network architecture suitable for small datasets. Meanwhile, 295 leveraging pre-trained models on larger data and fine-tuning them on smaller data sets is becoming as 296 297 popular as in other fields. Mo et al. [24] show that freezing discriminators in GAN fine-tuning gives 298 stable results. Ojha et al. [27] constrain the adapted model to share latent space with the source model. Zhao et al. [46] shows that the low-level filters of pre-trained GANs are helpful in learning limited 299 training data even when they are perceptually distant from the target data. Sauer et al. [33], Kumari 300 et al. [21] used pre-trained models as feature extractors for a discriminator and show the effectiveness 301 of faster and more stable convergence. However, fine-tuning with limited data for unconditional 302 diffusion models is still less explored yet. 303

Fine-tuning for diffusion models Recently, a high-performance pre-trained diffusion model has 304 been published [29, 32]. As of now, few pioneering works investigate fine-tuning diffusion models; 305 Giannone et al. [9] proposing few-shot learning diffusion models that can quickly learn conditional 306 generative model for a set of images, and Ruiz et al. [31] proposing a prompt-like approach for text-307 to-image diffusion models. Wang et al. [43] propose two-stage finetuning scheme for image-to-image 308 309 translation. However, these works focus on conditional generation and fine-tune the pre-trained 310 model without network modification. To the best of our knowledge, our method is the first one to study module-level effects for fine-tuning an unconditional diffusion model with limited data. 311

Adapter-based method for transfer learning In a natural language processing task, Houlsby et al. [15] proposed a memory-efficient method for transformers that only updates adapter modules while freezing other weights during fine-tuning. The adapter-based method requires only a small number of additional parameters, so it is efficient when adapting to a variety of tasks. Karimi Mahabadi et al. [16] developed a more compact and faster adapter module based on matrix factorization and weight sharing. Chen et al. [4], Sung et al. [40] adopt the adapter method for the vision task and showed effectiveness on reducing memory and training time.

### 319 C Experimental Details

#### 320 C.1 Configurations

Our algorithm is implemented in Python 3.9.5 and Pytorch 1.10.2. All experiments are performed on four NVIDIA Tesla V100s.

#### 323 C.2 Setting

We present detailed experimental settings for experiment results reproduction. For all experiments, we use the ImageNet  $64 \times 64$  pre-trained model ( $\approx 120M$  parameters) in Nichol and Dhariwal [26]. Our model consists of a total of 15 attention blocks and 30 residual blocks. Input images go under four downsampling steps, each with [2C, 2C, 2C, 4C] channels where C = 128, and then upsampled via four symmetric steps. The pre-trained model employs multi-head attention blocks with 4 heads.

We employ Adam [19] for all experiments, with a learning rate of  $2 \cdot 10^{-4}$  and epsilon of  $1 \cdot 10^{-8}$ . We set the batch size to 128 and 5 for fine-tuning and sampling, respectively. Opposed to Nichol and Dhariwal [26], we do not use neither dropout [39] nor exponential moving average over model parameters.

To fine-tune diffusion models, we use the hybrid loss in (11) with cosine beta scheduling such that  $(\beta_1, \beta_2) = (1 \cdot 10^{-4}, 2 \cdot 10^{-2})$ . We set diffusion timesteps as T = 1000.

We fine-tune the pre-trained model with 1000 CelebA images and 400 Pokemon images. Evaluation metrics are computed between the whole training dataset and 10K/5K samples from CelebA/Pokemon dataset.

#### 338 C.3 Metrics

Since quantifying image generation performance remains a challenge, metrics must be carefully chosen. We use two different evaluation metrics: (i) clean Fréchet Inception Distance (cFID) [28] and (ii) Kernel Inception Distance (KID) [2]. While FID [11] is a popular choice for capturing both image fidelity and diversity, Parmar et al. [28] points out that FID is inconsistent with image resizing and quantization. To resolve such an issue, we use cFID by default. Due to our relatively small dataset size, we also implement KID which is proven to be unbiased and asymptotically normal. Metrics are computed between the whole training dataset and generated images.

#### 346 C.4 Time-aware adapter

In this section, we review a detailed structure of the time-aware adapter. In conventional adapter-based methods [15, 16], independent adapters are employed across all blocks. In Houlsby et al. [15] and Karimi Mahabadi et al. [16], every single transformer layer needs two separate adapters so that the number of adapters needed grows as to the number of layers. We alleviate such an issue using a weight-sharing technique. We let the same adapter submodule fit into several attention blocks.

We build two time-fusion modules which integrate into attention blocks with 384 and 512 channels. 352 Time-fusion module first match the dimension of two inputs,  $t_{embed}$  and  $z_{in}$ . The time-embedding 353 vector  $t_{embed}$  goes through two linear layers to match the dimension of  $z_{in}$ , and we add such two 354 vectors before passing on to the final linear layer. Similarly, we build only two cross-attention 355 modules which are attached to attention blocks with 384 and 512 channels. We implement vanilla 356 single-head attention operation. Importantly, we construct separate time-scaling modules for all 357 attention blocks analogous to conventional NLP adapters. This is because we want to regulate the 358 information from time-aware adapter in a block-wise manner. Time-scaling module is merely an 359 MLP with two fully connected layers with SiLU activation [7]. 360

## **D** Additional results



**Figure 4:** Selected samples after fine-tuning for 1500 epochs on CelebA dataset: (top) naïve fine-tuning, (middle) attention-block fine-tuning, (bottom)  $A^3FT$ .