

FLEXROUND: LEARNABLE ROUNDING BY ELEMENT-WISE DIVISION FOR POST-TRAINING QUANTIZATION

Anonymous authors

Paper under double-blind review

ABSTRACT

Post-training Quantization (PTQ) has been gaining popularity for the deployment of deep neural networks on resource-limited devices since unlike quantization-aware training, neither a full training dataset nor end-to-end training is required at all. As PTQ schemes based on reconstructing each layer or block output turn out to be effective to enhance quantized model performance, recent works have developed algorithms to devise and learn a new weight-rounding scheme so as to better reconstruct each layer or block output. We notice that, however, such new rounding schemes are established on element-wise addition. In this work, we propose a simple yet effective new rounding mechanism for PTQ, coined *FlexRound*, via element-wise division to learn not only a common quantization grid size but also a different scale for each pre-trained weight. Thanks to the reciprocal rule of derivatives induced by element-wise division, FlexRound is inherently able to exploit the importance of a pre-trained weight when updating its corresponding scale, and thus, flexibly quantize a pre-trained weight depending on its own importance. We empirically validate the efficacy of FlexRound on a wide range of models and tasks. To the best of our knowledge, our work is the first to carry out comprehensive experiments on image classification, natural language understanding, and natural language generation in the *per-tensor* uniform PTQ setting. Our code will be open-sourced soon.

1 INTRODUCTION

Recent years have witnessed the unprecedented success of deep neural networks in a wide variety of domains including computer vision, natural language processing, automatic speech recognition, and so on. Although state-of-the-art deep neural networks surpass human-level performance, these neural networks cannot help requiring more and more computation cost and memory usage as networks become deeper and wider. In order to reduce the model size and accelerate inference operations, many researchers have attempted diverse compression techniques such as network quantization (Courbariaux et al., 2016) and network pruning (Han et al., 2016). In this paper, we concentrate on network quantization due to the advantage that INT4 or INT8 quantization allows us to accelerate quantized neural networks using off-the-shelf accelerators such as the NVIDIA A100 Tensor Core GPU (Wu et al., 2020) or ARM Cortex MCUs (Kim et al., 2021).

Network quantization techniques can be generally divided into two categories: quantization-aware training (QAT) and post-training quantization (PTQ). When quantizing neural networks via QAT (Jung et al., 2019; Jain et al., 2019; Zhao et al., 2020; Esser et al., 2020; Lee et al., 2021), the performance gap between a full-precision neural network and its quantized counterpart can be marginal. Yet, QAT requires end-to-end retraining or fine-tuning on a full training dataset, which often causes an enormous amount of time and resources to obtain a quantized neural network with competitive performance. Furthermore, a whole training dataset may not be available due to data privacy issues or demands to utilize legacy models. Such drawbacks of QAT are the reasons why

researchers recently pay more attention to PTQ (Zhao et al., 2019; Wang et al., 2020; Nahshan et al., 2021) that needs neither a full training dataset nor end-to-end learning at all.

PTQ had been initially performed via rounding-to-nearest scheme by minimizing the quantization error in the parameter space. Unfortunately, this approach suffers from severe performance degradation. Since it is reported that the loss degradation resulting from quantization can be approximated as the second-order error in Taylor Expansion by viewing quantized weights as perturbed weights, Nagel et al. (2020) and Li et al. (2021) substantiate that reconstructing each output of layer or block is equivalent to minimizing the approximation of loss degradation resulting from quantization under some assumptions. Accordingly, recent works (Nagel et al., 2020; Li et al., 2021; Hubara et al., 2021; Wei et al., 2022) have suggested to reconstruct each output of layer or block by devising and learning a new weight-rounding scheme, deviating from rounding-to-nearest, as an effort to preserve the performance of a full-precision model. However, all those new rounding schemes designed in existing studies either round or quantize pre-trained weights adaptively via element-wise addition.

Changing the perspective of a new rounding policy from element-wise addition to element-wise division, we propose a simple yet effective post-training weight quantization method called FlexRound, which flexibly quantizes pre-trained weights by learning how much each pre-trained weight should be divided by. Interestingly, thanks to the reciprocal rule of derivatives induced by element-wise division, FlexRound can inherently leverage pre-trained weights when updating an individual scale for every pre-trained weight. Specifically, we corroborate that a relatively wider range of discrete values needs to be explored when quantizing pre-trained weights of large magnitude. The rationale behind such an approach is that the magnitude of weight can be considered as its importance. Given that it is crucial to retain the knowledge of important weights even after quantization so as to maintain the performance of a pre-trained model, the constraints associated with quantizing weights of large absolute value should be relaxed compared to those of small absolute value (i.e., those important weights can be quantized to one of not only its two nearest discrete values but also discrete ones far from it). Accordingly, FlexRound quantizes pre-trained weights flexibly depending on each their own importance, thereby leading to better performance.

Our contributions are threefold:

- We propose FlexRound as a new rounding scheme for PTQ based on the principle of element-wise division to enable learning separate scales for all pre-trained weights as well as a common quantization grid size across a group (e.g., a channel or a layer).
- We demonstrate that such a new rounding scheme via element-wise division takes into consideration the importance of pre-trained weights when updating their corresponding scales so that FlexRound can quantize pre-trained weights of large magnitude (i.e., important pre-trained weights) more flexibly.
- To the best of our knowledge, we are the first to conduct extensive experiments in the form of *per-tensor* uniform PTQ reconstruction on various tasks including image classification, natural language understanding, and natural language generation. We verify the effectiveness of FlexRound using numerous models such as ResNet, MobileNetV2, BERT, GPT-Neo, and OPT.

2 RELATED WORK

Recently, many researchers have attempted to quantize a wide range of models for various tasks such as vision and language understanding/generation without any (re)training. OCS (Zhao et al., 2019) replicates channels entailing outliers, and then, halves outliers of those channels. Unfortunately, even though OCS explicitly addresses outliers, it still suffers from severe accuracy degradation when both weights and activations are quantized into low-bit. As an alternative solution, Wang et al. (2020) proposed Bit-Split that splits an integer into several bits and optimizes them separately. Although Wang et al. (2020) showed that the performance of Bit-Split is close to that of a full-precision model in the low-bit setting, Bit-Split may not be effective for certain architectures including MobileNetV2.

To overcome the limitations discussed above, Nagel et al. (2020) and Hubara et al. (2021) minimize the mean squared error (in a layer-by-layer fashion) between the full-precision layer’s output and its quantized layer’s output by inventing and learning a new weight-rounding mechanism dubbed as AdaRound and AdaQuant, respectively. As such a layer-wise reconstruction error minimization opens the door to 4-bit PTQ regime, Li et al. (2021) proposed block-wise reconstruction, titled BRECQ, to consider cross-layer dependency along with the possibility of fully quantizing MobileNetV2 into 4-bit. In addition to block-wise reconstruction, Wei et al. (2022) proposed QDrop that drops the quantization of activations at random during reconstruction to induce activation quantization to be synchronized with weight quantization. Both BRECQ and QDrop, however, are based on AdaRound, which requires numerous hyper-parameters for regularization while quantizing weights allows for rounding either up or down only at most. AdaQuant does not need any hyper-parameters and quantizes weights adaptively. AdaQuant, however, does not consider the magnitude of weights for quantization that turns out to be important as we discuss later.

As another line of post-training quantization (PTQ) research, some PTQ techniques are specialized in quantizing language models such as BERT and GPT-like models. Bondarenko et al. (2021) first applied PTQ to BERT by introducing per-embedding-group activation quantization scheme to deal with highly dynamic activation ranges. Yao et al. (2022) proposed ZeroQuant that quantizes BERT and GPT-3 in group-wise weight quantization manner driven by token-wise activation quantization via layer-by-layer knowledge distillation. Dettmers et al. (2022) quantizes large language models like OPT with vector-wise weight quantization and mixed-precision decomposition with FP16 activation. All those methods do not consider per-tensor weight quantization which is useful for highly parallelized computing systems.

Most of the aforementioned PTQ studies are targeted to either vision models or language models only, but not to both. Most experimental results in the above PTQ works are conducted via channel-wise/group-wise/vector-wise weight quantization at the expense of reduced parallelism. To the best of our knowledge, our work is the first to carry out extensive experiments on diverse tasks ranging from computer vision to natural language processing assuming a per-tensor uniform PTQ setting.

3 METHODOLOGY

In this section, we first present the notations used in the paper, describe the concept and design of FlexRound for per-tensor uniform post-training quantization (PTQ) reconstruction, and then, scrutinize how FlexRound can leverage the importance of a pre-trained weight.

3.1 PRELIMINARIES

Notations. A scalar, a vector, and a matrix (or a tensor) are expressed as a non-bold letter, a small bold letter and a capital bold letter (e.g. s , \mathbf{s} and \mathbf{S}) respectively. $\widehat{\mathbf{W}}$ indicates the quantized counterpart of \mathbf{W} . The input to a convolutional or fully-connected layer is denoted as \mathbf{X} if all previous layers are intact or as $\widetilde{\mathbf{X}}$ if all previous layers are quantized. The (i, j) element of a matrix \mathbf{W} is represented as $W_{(i,j)}$. We let \odot and $/$ indicate element-wise product and element-wise division, respectively, similar to the broadcasting process in Python Numpy. $\lfloor \cdot \rfloor$ and $\lfloor \cdot \rfloor$ express the rounding function and the floor function. $\|\cdot\|_F$ represents the Frobenius norm.

PTQ Background. The conventional uniform PTQ approach is to quantize pre-trained weights \mathbf{W} to be $\widehat{\mathbf{W}} = s_1 \left\lfloor \frac{\mathbf{W}}{s_1} \right\rfloor$ via rounding-to-nearest and to minimize $\|\mathbf{W} - \widehat{\mathbf{W}}\|_F^2$ with respect to the quantization grid size s_1 , but the minimization of quantization error in the parameter space is not equivalent to that of the final task loss. On the grounds that Li et al. (2021) proves that the loss degradation resulting from quantization can be approximated as the quadratic form of the network output and its Hessian matrix, several existing studies have strove to minimize $\|\mathbf{W}\mathbf{X} - \widehat{\mathbf{W}}\widetilde{\mathbf{X}}\|_F^2$ layer-by-layer or block-by-block with respect to continuous variables \mathbf{V} with only a small amount

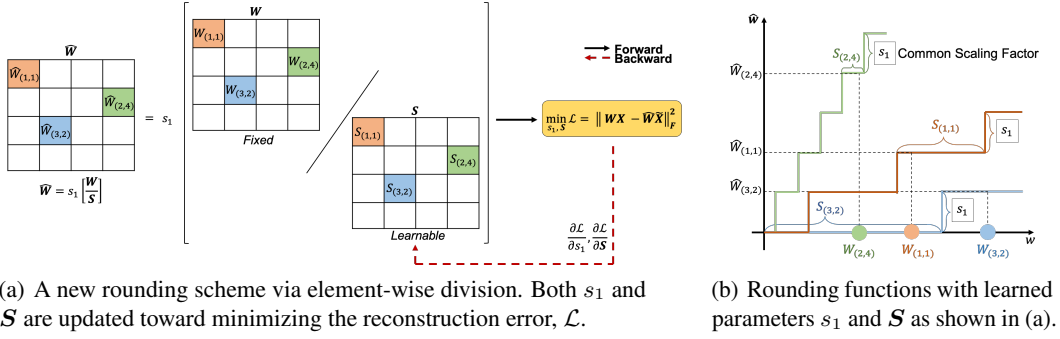


Figure 1: Illustration of FlexRound in the per-tensor uniform PTQ reconstruction. As seen in (b), FlexRound flexibly quantizes pre-trained weights by observing $W_{(2,4)} < W_{(3,2)}$ but $\widehat{W}_{(2,4)} > \widehat{W}_{(3,2)}$.

of data, where \widehat{W} is either $s_1(\lfloor \frac{W}{s_1} \rfloor + h(\mathbf{V}))$ with a certain function $h(\cdot)$ (Nagel et al., 2020) or $s_1 \lfloor \frac{W+\mathbf{V}}{s_1} \rfloor$ (Hubara et al., 2021). However, all these aforementioned rounding mechanisms are founded on element-wise addition.

3.2 FLEXROUND

Unlike prior works based on element-wise addition, we exploit element-wise division for quantizing pre-trained weights. We can formulate our proposed weight-rounding scheme via element-wise division as follows:

$$\widehat{W} = s_1 \left\lfloor \frac{W}{S} \right\rfloor, \quad (1)$$

where the shape of S is equal to that of W while all entries of S as well as the quantization grid size s_1 are positive and learnable. Similarly to preceding studies, both s_1 and S are updated as an attempt to minimize $\|W\mathbf{X} - \widehat{W}\mathbf{X}\|_F^2$.

Eq. 1 implies that the basic formula of FlexRound supports per-tensor uniform PTQ. Notice that although FlexRound can adopt a per-channel weight quantization scheme simply by replacing a scalar s_1 with a vector s_1 , since we show later that per-tensor uniform PTQ (using FlexRound) is enough to provide the accuracy of a full-precision model, we set a single quantization grid size s_1 for each layer (per-tensor quantization schemes facilitate higher parallelism for implementation compared to per-channel quantization schemes (Nagel et al., 2021)). From now on, thus, we study only the per-tensor uniform PTQ reconstruction. The overall procedure of FlexRound is described in Figure 1.

Now let us discuss how to design S . Let $W \in \mathbb{R}^{C_{out} \times C_{in}}$ in the case of a fully-connected layer and $W \in \mathbb{R}^{C_{out} \times C_{in} \times H \times W}$ in the case of a convolutional layer. We first start formulating S as $S = s_1 \odot S_2$ where $S_2 \in \mathbb{R}_{>0}^{C_{out} \times C_{in}}$ in the case of a fully-connected layer and $S_2 \in \mathbb{R}_{>0}^{C_{out} \times C_{in} \times H \times W}$ in the case of a convolutional layer while all elements of S_2 are learnable. Then, motivated by a wide acknowledgement that the statistics of output channels can vary greatly (Nagel et al., 2019; Lou et al., 2020), we account for the variation of output channel’s statistics by complementing S with an additional learnable tensor s_3 , where $s_3 \in \mathbb{R}_{>0}^{C_{out} \times 1}$ in the case of a fully-connected layer and $s_3 \in \mathbb{R}_{>0}^{C_{out} \times 1 \times 1 \times 1}$ in the case of a convolutional layer. For a convolutional layer, S is additionally complemented by another learnable tensor s_4 , where $s_4 \in \mathbb{R}_{>0}^{1 \times C_{in} \times 1 \times 1}$. Consequently, S is formulated as $s_1 \odot S_2 \odot s_3$ for a fully-connected layer as displayed in Figure 2 and $s_1 \odot S_2 \odot s_3 \odot s_4$ for a convolutional layer.

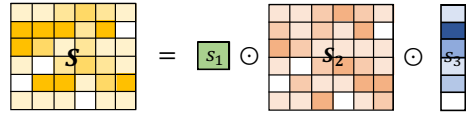


Figure 2: Formation of S for a linear layer.

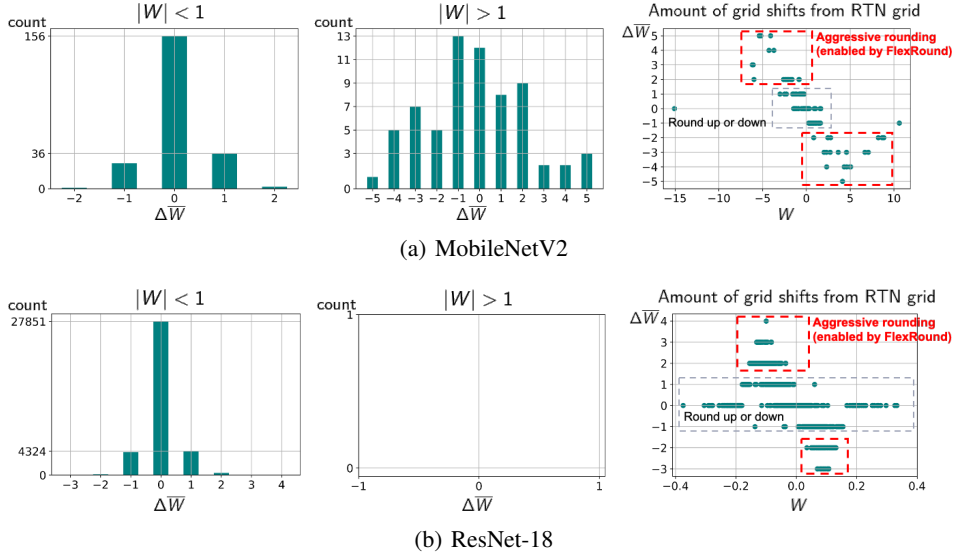


Figure 3: Weight updates through FlexRound of the first convolutional layer in the first block of (a) MobileNetV2 and (b) ResNet-18, after quantizing pre-trained weights into 4-bit (by FlexRound) while activations are kept in full-precision.

Accordingly, quantization process for FlexRound can be expressed as

$$\widehat{W} = \begin{cases} s_1 \left\lfloor \frac{W}{s_1 \odot S_2 \odot s_3} \right\rfloor & \text{if } W \text{ is a fully-connected layer} \\ s_1 \left\lfloor \frac{W}{s_1 \odot S_2 \odot s_3 \odot s_4} \right\rfloor & \text{if } W \text{ is a convolutional layer} \end{cases} \quad (2)$$

where all entries of S_2 , s_3 , and s_4 are initialized to be ones and updated to minimize $\|W X - \widehat{W} \widetilde{X}\|_F^2$ (with respect to s_1 , S_2 , s_3 , and s_4) subject to the constraint that all elements of s_1 , S_2 , s_3 , and s_4 are positive.

Since s_1 , S_2 , s_3 , and s_4 are all learnable and FlexRound does not need any explicit regularization terms, no additional hyper-parameter is necessary, and thus, FlexRound would be convenient for practitioners. Moreover, as all entries of s_1 , S_2 , s_3 , and s_4 are positive and FlexRound is based on element-wise division, FlexRound encourages \widehat{W} to employ the same sign as W . Hence, FlexRound prevents extreme changes of weights through quantization process, which could occur when a rounding scheme relies on an element-wise addition technique.

3.3 LEVERAGING THE IMPORTANCE OF A PRE-TRAINED WEIGHT

As we discussed previously, either element-wise addition or element-wise division is effective to produce a better rounding scheme than a rounding to the nearest scheme. In order to investigate the difference between element-wise addition and element-wise division, it would be instructive to analyze the gradient of the reconstruction error $\mathcal{L} = \|W X - \widehat{W} \widetilde{X}\|_F^2$ with respect to S' (where S' is $S_2 \odot s_3$ for a fully-connected layer and $S_2 \odot s_3 \odot s_4$ for a convolutional layer). Through analysis, unlike element-wise addition, we show that element-wise division enables $\frac{\partial \mathcal{L}}{\partial S'}$ to leverage the importance of pre-trained weights W , as follows¹:

Using the straight-through estimator (Bengio et al., 2013), for every i and j , $\left| \frac{\partial \mathcal{L}}{\partial S'_{(i,j)}} \right|$ is directly proportional to $\left| W_{(i,j)} \frac{\partial \mathcal{L}}{\partial \widehat{W}_{(i,j)}} \right|$, which implies that $S'_{(i,j)}$ is (partially) affected by $W_{(i,j)}$. As a result,

¹For simplicity, we take into account the case of a fully-connected layer.

$\overline{W}_{(i,j)} = \left\lfloor \frac{W_{(i,j)}}{s_1 \odot S'_{(i,j)}} \right\rfloor$ can also be updated and influenced by $W_{(i,j)}$ as well. In other words, as the magnitude of a pre-trained weight $W_{(i,j)}$ is larger, the chance of $\overline{W}_{(i,j)}$ receiving a larger update becomes higher during the PTQ reconstruction. In light of the fact that the magnitude of a weight can be regarded as a metric to measure importance during compressing a neural network (Han et al., 2015; Zhu & Gupta, 2017), if the goal is to enhance model accuracy after quantization, it would be reasonable to have less important (that is, smaller magnitude) weights rounded either up or down only while allowing more important (i.e., exhibiting larger magnitude) weights to be quantized to one of the two closest quantization grids or more.

Figure 3 presents the amount of weight updates through FlexRound for MobileNetV2 and ResNet-18. On the left side and the center side of Figure 3, histograms describe the change of $\overline{W}_{(i,j)}$ grouped for small pre-trained weights ($|W| < 1$, left) and large pre-trained weights ($|W| > 1$, center). On the right side, scatter plots show the amount of grid shifts from the grids obtainable by the rounding-to-nearest (RTN) scheme. We note that MobileNetV2 and ResNet-18 are quantized distinctively due to FlexRound. For example, in the case of MobileNetV2 as illustrated in Figure 3(a), the change of $\overline{W}_{(i,j)}$ attained by minimizing \mathcal{L} is more aggressive (i.e., rounding can be deviated by more than one-step up or one-step down) when the absolute value of $W_{(i,j)}$ is larger than one, which means that FlexRound more flexibly quantizes pre-trained weights of large magnitude as illustrated in red dotted squares in Figure 3(a). The amount of aggressively rounded weights in the first convolutional layer of the first block of MobileNetV2 is around 12.8% of the total. For ResNet-18, however, there are no pre-trained weights whose magnitudes are larger than one. Thus, most pre-trained weights are rounded either up or down as shown in Figure 3(b) (e.g., only about 1.5% weights are rounded aggressively in the first convolutional layer of the first block of ResNet-18). Different rounding results by FlexRound, AdaRound, and AdaQuant are visually compared in Appendix A.

4 EXPERIMENTS

In this section, we present experimental results for benchmark datasets and network models in computer vision and natural language processing tasks. We first empirically confirm that additional tensors s_3 and s_4 introduced in Section 3.2 implement distinct contributions in the per-tensor uniform post-training quantization (PTQ) setting. Then, we compare the performance of FlexRound with that of some state-of-the-art PTQ approaches in the following cases: image classification on the ImageNet (Russakovsky et al., 2015) dataset with the ResNet (He et al., 2016) and MobileNetV2 (Sandler et al., 2018) architectures (Section 4.2), natural language understanding (NLU) on the GLUE (Wang et al., 2018) benchmark with the BERT (Devlin et al., 2018) and GPT-Neo (Black et al., 2021) architectures (Section 4.3), and natural language generation (NLG) on WikiText2 (Merity et al., 2016) and Penn Treebank (PTB) (Marcus et al., 1993) with the GPT-Neo and OPT (Zhang et al., 2022) architectures (Section 4.3). For brevity, we let “B + X” and “Q + X” indicate that a certain rounding scheme ‘X’ is performed in the experimental setup described in BRECQ (Li et al., 2021) or QDrop (Wei et al., 2022), respectively (an experimental setup includes the definition of a block unit for reconstruction error minimization or how much the probability of dropping the quantization of activations is). As introduced in BRECQ and QDrop, we also utilize the LSQ technique (Esser et al., 2020) when updating an activation step size for activation quantization. Throughout our comprehensive experiments, we verify that FlexRound can achieve competitive performance with a full-precision model for the above tasks even in the *per-tensor* uniform PTQ reconstruction, which has not been introduced previously. All experimental results in this section are conducted by our own implementation based on open-source codes.

4.1 ABLATION STUDY

To justify the introduction of s_3 and s_4 on FlexRound in the per-tensor uniform PTQ setting, we investigate the impact of s_3 and s_4 on the performance of FlexRound using the ImageNet dataset with pre-trained weights quantized into 2-bit (activations are not quantized). As shown in the last

Table 1: Top-1/Top-5 accuracy (%) on ImageNet by ResNet-18, ResNet-50, and MobileNetV2 with only weights quantized into 2-bit. “B + X” denotes the implementation of X in the setting of BRECCQ.

Method	ResNet-18	ResNet-50	MobileNetV2
B + AdaQuant	1.13/4.10	0.12/0.60	0.10/0.50
B + AdaRound	63.01/85.20	68.31/88.98	33.10/60.58
B + FlexRound without s_3, s_4	63.19/85.08	70.00/89.82	34.75/62.51
B + FlexRound with s_3, s_4	63.73/85.41	70.57/90.07	38.09/64.90

Table 2: Top-1/Top-5 accuracy (%) for ResNet-18, ResNet-50, and MobileNetV2 on ImageNet when only weights are quantized. “B + X” expresses the implementation of X in the BRECCQ’s setting.

Method	# Bits (W./A.)	ResNet-18	ResNet-50	MobileNetV2
Full-precision	32/32	71.00/89.97	76.63/93.04	72.62/90.67
B + AdaQuant	4/32	67.50/87.75	72.79/90.77	15.17/32.89
B + AdaRound	4/32	70.18/89.38	75.86/92.62	69.46/88.85
B + FlexRound (Ours)	4/32	70.28/89.44	75.95/92.68	70.82/89.67
B + AdaQuant	3/32	57.09/80.82	52.13/75.22	0.20/0.79
B + AdaRound	3/32	68.79/88.62	74.31/91.81	62.51/84.52
B + FlexRound (Ours)	3/32	68.65/88.54	74.38/91.81	66.87/87.56
B + AdaQuant	2/32	0.23/0.92	0.10/0.50	0.10/0.50
B + AdaRound	2/32	61.99/84.81	48.47/77.09	39.57/66.18
B + FlexRound (Ours)	2/32	62.57/84.84	63.67/85.72	46.04/72.48

two rows in Table 1, the presence of s_3 and s_4 enhances the accuracy for all models. Interestingly, FlexRound outperforms both AdaQuant and AdaRound even without s_3 and s_4 , which would support our claim that a new rounding scheme, shifted from element-wise addition to element-wise division, is the key to improving quantization quality significantly.

4.2 RESNET-18, RESNET-50, AND MOBILENETV2 ON IMAGENET

In this subsection, we quantize ResNet-18, ResNet-50, and MobileNetV2 in the low-bit PTQ reconstruction with 1024 randomly sampled images. Linear symmetric per-tensor quantization format is assumed to quantize weights and/or activations. For FlexRound, the output of each layer or block is reconstructed during $5k$ iterations while all learnable parameters (i.e., s_1, S_2, s_3 , and s_4) are updated by using one learning rate (e.g., $4e-4$ for the ResNet models quantized by 3-bit or 4-bit, or $1e-3$ for the ResNet models quantized by 2-bit and MobileNetv2). The first and last layers are quantized into 8-bit and the batch normalization layer is folded into convolution, as done in Li et al. (2021). Our experiments are performed based on full-precision pre-trained models available from [the BRECCQ \(Li et al., 2021\) github repository²](#), and we report the median over five random trials.

Assuming the quantization of weights only, we compare FlexRound with AdaRound and AdaQuant that utilize the principle of element-wise addition to decide rounding operations. Table 6 shows that FlexRound consistently outperforms those two addition-based rounding policies. Note that the performance of AdaQuant is inferior to that of AdaRound in Table 6. Correspondingly, FlexRound would be compared to AdaRound only to save space hereafter. Table 7 provides model accuracy when AdaRound and FlexRound (to quantize both weights and activations) are associated with the settings of BRECCQ or QDrop. In Table 7, it should be noted that FlexRound is particularly successful for MobileNetV2 incorporating weights of large magnitude, for the reason that we explained in Section 3.3. It is also interesting to see that even when both weights and activations of the ResNet

²<https://github.com/yhhhli/BRECCQ>

Table 3: Top-1/Top-5 accuracy (%) for ResNet-18, ResNet-50, and MobileNetV2 on ImageNet when both weights and activations are quantized. “B + X” and “Q + Y” represent the implementation of X in the BRECCQ’s setting and that of Y in the QDrop’s setting, respectively.

Method	# Bits (W./A.)	ResNet-18	ResNet-50	MobileNetV2
Full-precision	32/32	71.00/89.97	76.63/93.04	72.62/90.67
B + AdaRound	4/4	69.18/88.85	74.44/91.80	61.05/83.30
B + FlexRound (Ours)	4/4	69.32/88.83	74.56/91.87	63.74/85.01
Q + AdaRound	4/4	69.20/88.96	74.90/92.15	65.42/86.23
Q + FlexRound (Ours)	4/4	69.26/88.81	75.08/92.20	66.66/87.21
B + AdaRound	3/3	64.83/86.12	67.01/87.28	3.74/11.54
B + FlexRound (Ours)	3/3	64.99/85.93	68.29/87.89	25.43/48.28
Q + AdaRound	3/3	65.71/86.96	70.49/89.93	39.86/66.00
Q + FlexRound (Ours)	3/3	65.43/86.60	70.74/89.78	51.49/76.90

Table 4: Performance of BERT_{Base}, BERT_{Large}, on the GLUE benchmark. For evaluation metrics, matched and mismatched accuracies are reported for MNLI, F1 score and accuracy are reported for QQP, Mathews correlation is reported for CoLA, Pearson and Spearman correlations are reported for STS-B, and accuracy is reported for the others. “Q + X” indicates the implementation of X in the QDrop’s setting.

Dataset	Method	BERT _{BASE}	BERT _{LARGE}	GPT-Neo _{125M}	GPT-Neo _{1.3B}	GPT-Neo _{2.7B}
MNLI	Full-precision	84.49/85.20	86.05/85.98	79.11/79.63	85.12/86.04	86.36/87.02
	Q+AdaRound	83.69/84.61	85.75/85.86	72.67/74.11	84.90/85.82	86.33/86.75
	Q+FlexRound (Ours)	84.53/84.98	85.93/85.99	72.94/74.24	85.56/86.14	86.41/86.89
QQP	Full-precision	88.06/91.08	88.66/91.59	85.20/88.99	88.26/91.28	88.62/91.50
	Q+AdaRound	87.65/90.58	87.48/90.62	72.97/79.35	87.98/91.04	88.38/91.27
	Q+FlexRound (Ours)	87.81/90.83	88.38/91.31	73.75/80.65	88.27/91.18	88.60/91.39
QNLI	Full-precision	91.25	92.13	85.15	91.36	92.46
	Q+AdaRound	91.16	92.24	80.87	91.40	92.04
	Q+FlexRound (Ours)	91.16	92.04	80.52	91.54	92.50
SST-2	Full-precision	93.00	92.78	89.91	93.35	94.50
	Q+AdaRound	92.66	93.00	84.75	92.55	93.81
	Q+FlexRound (Ours)	92.43	93.58	83.03	93.12	94.04
CoLA	Full-precision	58.55	63.57	37.83	57.42	58.88
	Q+AdaRound	56.79	54.30	20.15	58.93	57.14
	Q+FlexRound (Ours)	57.53	60.57	21.59	59.30	57.37
STS-B	Full-precision	88.52/88.20	88.98/88.89	79.87/80.12	88.94/88.90	89.75/89.82
	Q+AdaRound	88.00/87.53	86.87/86.69	68.55/68.25	88.97/88.77	89.03/ 88.91
	Q+FlexRound (Ours)	88.29/87.91	88.82/88.76	67.65/ 68.34	88.82/88.58	89.06/88.69
MRPC	Full-precision	85.05	85.54	80.15	85.05	87.99
	Q+AdaRound	81.62	82.35	75.25	84.80	85.78
	Q+FlexRound (Ours)	84.07	84.31	75.49	85.05	86.76
RTE	Full-precision	64.62	71.19	64.98	76.17	80.87
	Q+AdaRound	63.54	66.79	62.82	75.09	80.51
	Q+FlexRound (Ours)	64.62	68.95	62.82	76.17	81.23

models are quantized into 4-bit under the per-tensor uniform PTQ setting, the performance degradation (compared to a full-precision pre-trained model) is negligible (less than 1.5%) in Table 7.

4.3 LANGUAGE MODELS

All language models we consider in this paper are based on the structure of Transformers (Vaswani et al., 2017). To quantize Transformers into 8-bit, we apply linear asymmetric per-tensor quantization scheme for both weights and activations, while reconstruction (for PTQ) is considered for each Transformer layer that includes attention sublayers and feedforward sublayers. All weights are

Table 5: Performance of GPT-Neo_{125M}, GPT-Neo_{1.3B}, GPT-Neo_{2.7B}, OPT_{125M}, OPT_{1.3B} and OPT_{2.7B} on the WikiText2 and PTB datasets. The perplexity (PPL) is employed as a performance metric. The lower PPL, the better. “Q + X” means the implementation of X in the QDrop’s setting.

Dataset	Method	GPT-Neo _{125M}	GPT-Neo _{1.3B}	GPT-Neo _{2.7B}	OPT _{125M}	OPT _{1.3B}	OPT _{2.7B}
WikiText2	Full-precision	31.54	15.40	13.35	56.08	29.76	26.13
	Q+AdaRound	35.60	15.75	13.95	226.48	40.40	47.48
	Q+FlexRound (Ours)	33.44	15.68	13.80	66.07	40.01	40.38
PTB	Full-precision	64.63	31.51	27.22	129.90	76.06	68.81
	Q+AdaRound	70.16	31.97	28.24	220.01	103.15	120.37
	Q+FlexRound (Ours)	66.62	31.74	27.68	145.45	101.81	106.88

quantized into 8-bit except the last randomly initialized layer. As for activation quantization, on-the-fly (static) quantization is conducted before every fully-connected layer except the inputs of the softmax layer and the normalization layer that remain to be of full-precision as in Zafrir et al. (2019) and Zhang et al. (2020).

BERT and GPT-Neo on GLUE We evaluate the natural language understanding (NLU) performance of FlexRound using various models including BERT_{Base}, BERT_{Large}, GPT-Neo_{125M}, GPT-Neo_{1.3B} and GPT-Neo_{2.7B} on the GLUE benchmark. The learning rate applied to all learnable parameters (s_1 , S_2 , and s_3) is selected to be $2e-4$ for BERT and to be $3e-4$ for GPT-Neo. Reconstruction process is performed by using 1024 random samples for $20K$ iterations. For all experiments, the batch size is 64 and maximum sequence length of all experiments is 128. We utilize pre-trained language models (PLMs) and datasets available from the HuggingFace (Wolf et al., 2020) repository³. Further experimental details are referred to Appendix C. In Table 4, we report the performance of ‘Q + AdaRound’ and ‘Q + FlexRound’ that are potentially promising as shown in Table 7. We can notice that ‘Q + FlexRound’ yields better NLU scores than ‘Q + AdaRound’ for most NLU tasks. In particular, for the MNLI and QQP datasets, ‘Q + FlexRound’ can achieve comparable or even superior performance to a full-precision model in the per-tensor uniform PTQ setting except GPT-Neo_{125M}.

GPT-Neo and OPT on WikiText2 and PTB We test the natural language generation (NLG) performance of FlexRound on the WikiText2 and PTB datasets. PLMs (for NLG) are quantized by FlexRound (in a per-tensor quantization manner) while a small amount of data of downstream tasks are used for reconstruction and evaluation. Specifically, PLMs include GPT-Neo_{125M}, GPT-Neo_{1.3B}, GPT-Neo_{2.7B}, OPT_{125M}, OPT_{1.3B} and OPT_{2.7B}, while 256 downstream task data samples are chosen at random for reconstruction. More details on the experimental setup are provided in Appendix D. Table 5 presents the results of GPT-Neo and OPT on NLG tasks and it is clear that ‘Q + FlexRound’ is superior to ‘Q + AdaRound’ for all models and NLG tasks. Note that for GPT-Neo, ‘Q + FlexRound’ can achieve the similar performance of a full-precision PLM even in the per-tensor uniform PTQ setting, while some previous attempts rely on group-wise or vector-wise quantization (Yao et al., 2022; Dettmers et al., 2022).

5 CONCLUSION

We propose a new rounding scheme, named *FlexRound*, for post-training quantization under the principle of element-wise division, to enable learning both a common quantization grid size and an individual scale for each pre-trained weight. We validate that FlexRound can flexibly quantizes pre-trained weights by exploiting their magnitude as a metric to measure importance. Consequently, FlexRound can achieve comparable performance to a full-precision model even in the per-tensor uniform PTQ setting. As a future work, we plan to quantize large language models beyond 6.7B parameters in the per-tensor uniform PTQ setting.

³<https://github.com/huggingface/transformers>

REFERENCES

- Yoshua Bengio, Nicholas Leonard, and Aaron Courville. Estimating or propagating gradients through stochastic neurons for conditional computation. *arXiv preprint arXiv:1308.3432*, 2013.
- Sid Black, Leo Gao, Phil Wang, Connor Leahy, and Stella Biderman. GPT-Neo: Large Scale Autoregressive Language Modeling with Mesh-Tensorflow, March 2021. URL <https://doi.org/10.5281/zenodo.5297715>. If you use this software, please cite it using these metadata.
- Yelysei Bondarenko, Markus Nagel, and Tijmen Blankevoort. Understanding and overcoming the challenges of efficient transformer quantization. In *Proceedings of the 2021 Conference on Empirical Methods in Natural Language Processing*, pp. 7947–7969. Association for Computational Linguistics, November 2021. doi: 10.18653/v1/2021.emnlp-main.627. URL <https://aclanthology.org/2021.emnlp-main.627>.
- Matthieu Courbariaux, Itay Hubara, Daniel Soudry, Ran El-Yaniv, and Yoshua Bengio. Binarized neural networks: Training deep neural networks with weights and activations constrained to+ 1 or-1. *arXiv preprint arXiv:1602.02830*, 2016.
- Tim Dettmers, Mike Lewis, Younes Belkada, and Luke Zettlemoyer. Llm.int8(): 8-bit matrix multiplication for transformers at scale. *arXiv preprint arXiv:2208.07339*, 2022.
- Jacob Devlin, Ming-Wei Chang, Kenton Lee, and Kristina Toutanova. Bert: Pre-training of deep bidirectional transformers for language understanding. *arXiv preprint arXiv:1810.04805*, 2018.
- Steven K. Esser, Jeffrey L. McKinstry, Deepika Bablani, Rathinakumar Appuswamy, and Dharmendra S. Modha. Learned step size quantization. In *International Conference on Learning Representations*, 2020. URL <https://openreview.net/forum?id=rkgO66VKDS>.
- Song Han, Jeff Pool, John Tran, and William Dally. Learning both weights and connections for efficient neural network. *Advances in neural information processing systems*, 28, 2015.
- Song Han, Huizi Mao, and William J. Dally. Deep compression: Compressing deep neural networks with pruning, trained quantization and huffman coding. In *International Conference on Learning Representations*, 2016. URL <https://arxiv.org/pdf/1510.00149.pdf>.
- Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pp. 770–778, 2016.
- Itay Hubara, Yury Nahshan, Yair Hanani, Ron Banner, and Daniel Soudry. Accurate post training quantization with small calibration sets. In *Proceedings of the 38th International Conference on Machine Learning*, volume 139 of *Proceedings of Machine Learning Research*, pp. 4466–4475. PMLR, 2021. URL <https://proceedings.mlr.press/v139/hubara21a.html>.
- Sambhav R Jain, Albert Gural, Michael Wu, and Chris H Dick. Trained quantization thresholds for accurate and efficient fixed-point inference of deep neural networks. *arXiv preprint arXiv:1903.08066*, 2019.
- Sangil Jung, Changyong Son, Seohyung Lee, Jinwoo Son, Jae-Joon Han, Youngjun Kwak, Sung Ju Hwang, and Changkyu Choi. Learning to quantize deep networks by optimizing quantization intervals with task loss. In *The IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, pp. 4350–4359, 2019.
- Sumin Kim, Gunju Park, and Youngmin Yi. Performance evaluation of int8 quantized inference on mobile gpus. *IEEE Access*, 9:164245–164255, 2021.

- Jung Hyun Lee, Jihun Yun, Sung Ju Hwang, and Eunho Yang. Cluster-promoting quantization with bit-drop for minimizing network quantization loss. In *2021 IEEE/CVF International Conference on Computer Vision (ICCV)*, pp. 5350–5359. IEEE Computer Society, 2021. URL <https://doi.ieeecomputersociety.org/10.1109/ICCV48922.2021.00532>.
- Yuhang Li, Ruihao Gong, Xu Tan, Yang Yang, Peng Hu, Qi Zhang, Fengwei Yu, Wei Wang, and Shi Gu. BRECQ: Pushing the limit of post-training quantization by block reconstruction. In *International Conference on Learning Representations*, 2021. URL <https://openreview.net/forum?id=POWv6hDd9XH>.
- Qian Lou, Feng Guo, Minje Kim, Lantao Liu, and Lei Jiang. Autoq: Automated kernel-wise neural network quantization. In *International Conference on Learning Representations*, 2020. URL <https://openreview.net/forum?id=rygfnn4twS>.
- Mitchell P. Marcus, Beatrice Santorini, and Mary Ann Marcinkiewicz. Building a large annotated corpus of English: The Penn Treebank. *Computational Linguistics*, 19(2):313–330, 1993. URL <https://www.aclweb.org/anthology/J93-2004>.
- Stephen Merity, Caiming Xiong, James Bradbury, and Richard Socher. Pointer sentinel mixture models, 2016.
- Markus Nagel, Mart van Baalen, Tijmen Blankevoort, and Max Welling. Data-free quantization through weight equalization and bias correction. In *Proceedings of the IEEE/CVF International Conference on Computer Vision*, pp. 1325–1334, 2019.
- Markus Nagel, Rana Ali Amjad, Mart Van Baalen, Christos Louizos, and Tijmen Blankevoort. Up or down? Adaptive rounding for post-training quantization. In *Proceedings of the 37th International Conference on Machine Learning*, volume 119 of *Proceedings of Machine Learning Research*, pp. 7197–7206. PMLR, 2020. URL <https://proceedings.mlr.press/v119/nagel20a.html>.
- Markus Nagel, Marios Fournarakis, Rana Ali Amjad, Yelysei Bondarenko, Mart van Baalen, and Tijmen Blankevoort. A white paper on neural network quantization. *arXiv preprint arXiv:2106.08295*, 2021.
- Yury Nahshan, Brian Chmiel, Chaim Baskin, Evgenii Zheltonozhskii, Ron Banner, Alex M Bronstein, and Avi Mendelson. Loss aware post-training quantization. *Machine Learning*, 110(11):3245–3262, 2021.
- Pranav Rajpurkar, Jian Zhang, Konstantin Lopyrev, and Percy Liang. SQuAD: 100,000+ Questions for Machine Comprehension of Text. *arXiv e-prints*, art. arXiv:1606.05250, 2016.
- Olga Russakovsky, Jia Deng, Hao Su, Jonathan Krause, Sanjeev Satheesh, Sean Ma, Zhiheng Huang, Andrej Karpathy, Aditya Khosla, Michael Bernstein, et al. Imagenet large scale visual recognition challenge. *International journal of computer vision*, 115(3):211–252, 2015.
- Mark Sandler, Andrew Howard, Menglong Zhu, Andrey Zhmoginov, and Liang-Chieh Chen. Mobilenetv2: Inverted residuals and linear bottlenecks. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pp. 4510–4520, 2018.
- Ashish Vaswani, Noam Shazeer, Niki Parmar, Jakob Uszkoreit, Llion Jones, Aidan N Gomez, Łukasz Kaiser, and Illia Polosukhin. Attention is all you need. *Advances in neural information processing systems*, 30, 2017.
- Alex Wang, Amanpreet Singh, Julian Michael, Felix Hill, Omer Levy, and Samuel R Bowman. Glue: A multi-task benchmark and analysis platform for natural language understanding. *arXiv preprint arXiv:1804.07461*, 2018.

- Peisong Wang, Qiang Chen, Xiangyu He, and Jian Cheng. Towards accurate post-training network quantization via bit-split and stitching. In *International Conference on Machine Learning*, pp. 9847–9856. PMLR, 2020.
- Xiuying Wei, Ruihao Gong, Yuhang Li, Xianglong Liu, and Fengwei Yu. QDrop: Randomly dropping quantization for extremely low-bit post-training quantization. In *International Conference on Learning Representations*, 2022. URL <https://openreview.net/forum?id=ySQH0oDyp7>.
- Thomas Wolf, Lysandre Debut, Victor Sanh, Julien Chaumond, Clement Delangue, Anthony Moi, Pierric Cistac, Tim Rault, Remi Louf, Morgan Funtowicz, Joe Davison, Sam Shleifer, Patrick von Platen, Clara Ma, Yacine Jernite, Julien Plu, Canwen Xu, Teven Le Scao, Sylvain Gugger, Mariama Drame, Quentin Lhoest, and Alexander Rush. Transformers: State-of-the-art natural language processing. In *Proceedings of the 2020 Conference on Empirical Methods in Natural Language Processing: System Demonstrations*, pp. 38–45, Online, October 2020. Association for Computational Linguistics. doi: 10.18653/v1/2020.emnlp-demos.6. URL <https://aclanthology.org/2020.emnlp-demos.6>.
- Hao Wu, Patrick Judd, Xiaojie Zhang, Mikhail Isaev, and Paulius Micikevicius. Integer quantization for deep learning inference: Principles and empirical evaluation. *arXiv preprint arXiv:2004.09602*, 2020.
- Zhewei Yao, Reza Yazdani Aminabadi, Minjia Zhang, Xiaoxia Wu, Conglong Li, and Yuxiong He. Zeroquant: Efficient and affordable post-training quantization for large-scale transformers. *arXiv preprint arXiv:2206.01861*, 2022.
- Ofir Zafrir, Guy Boudoukh, Peter Izsak, and Moshe Wasserblat. Q8bert: Quantized 8bit bert. In *2019 Fifth Workshop on Energy Efficient Machine Learning and Cognitive Computing-NeurIPS Edition (EMC2-NIPS)*, pp. 36–39. IEEE, 2019.
- Susan Zhang, Stephen Roller, Naman Goyal, Mikel Artetxe, Moya Chen, Shuohui Chen, Christopher Dewan, Mona Diab, Xian Li, Xi Victoria Lin, et al. Opt: Open pre-trained transformer language models. *arXiv preprint arXiv:2205.01068*, 2022.
- Wei Zhang, Lu Hou, Yichun Yin, Lifeng Shang, Xiao Chen, Xin Jiang, and Qun Liu. Ternarybert: Distillation-aware ultra-low bit bert. *arXiv preprint arXiv:2009.12812*, 2020.
- Ritchie Zhao, Yuwei Hu, Jordan Dotzel, Chris De Sa, and Zhiru Zhang. Improving neural network quantization without retraining using outlier channel splitting. In *International conference on machine learning*, pp. 7543–7552. PMLR, 2019.
- Xiandong Zhao, Ying Wang, Xuyi Cai, Cheng Liu, and Lei Zhang. Linear symmetric quantization of neural networks for low-precision integer hardware. In *International Conference on Learning Representations*, 2020. URL <https://openreview.net/forum?id=H11Bj2VFPS>.
- Michael Zhu and Suyog Gupta. To prune, or not to prune: exploring the efficacy of pruning for model compression. *arXiv preprint arXiv:1710.01878*, 2017.

A COMPARISON OF FLEXROUND TO ADAROUND AND ADAQUANT

Figure 4 shows that the comparison of FlexRound to AdaRound and AdaQuant. As seen in Figure 4(a), FlexRound can quantize pre-trained weights more flexibly than AdaRound and AdaQuant. As weights of large magnitude are not quantized aggressively in the middle of Figure 4(a) compared to the right of Figure 4(a), AdaQuant quantizes weights of large importance marginally, which seems to make it difficult for AdaQuant to quantize MobileNetV2 into 4-bit.

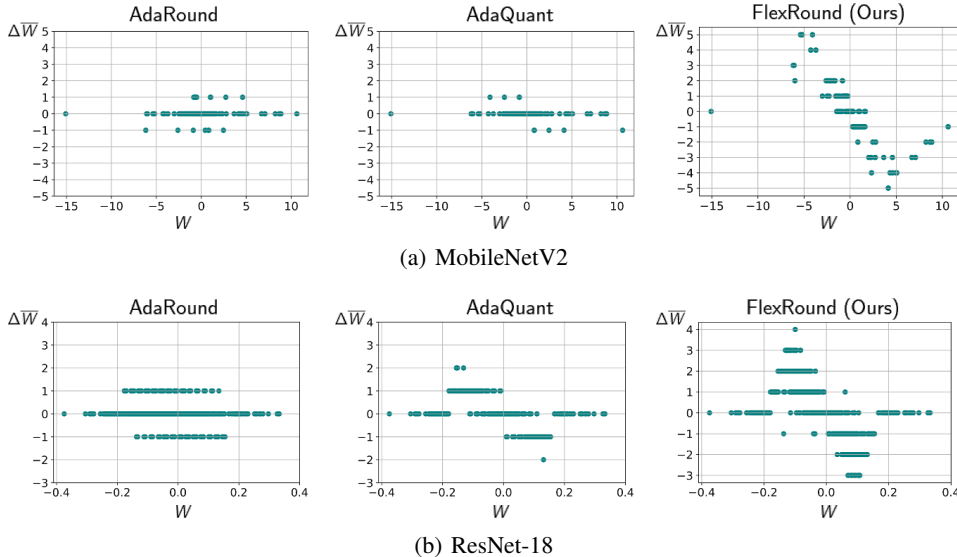


Figure 4: Scatter plot of the amount of grid shifts from rounding-to-nearest grid in the first layer of the first block in MobileNetV2 and ResNet-18 when only weights are quantized into 4-bit.

B RESNET-18, RESNET-50, AND MOBILENETV2 ON IMAGENET WITH PRE-TRAINED MODELS FROM THE OFFICIAL PYTORCH REPOSITORY

Table 6: Top-1/Top-5 accuracy (%) for ResNet-18, ResNet-50, and MobileNetV2 on ImageNet when only weights are quantized. “B + X” expresses the implementation of X in the BRECQ’s setting.

Method	# Bits (W./A.)	ResNet-18	ResNet-50	MobileNetV2
Full-precision	32/32	69.76/89.08	76.15/92.87	71.88/90.29
B + AdaQuant	4/32	67.55/87.73	74.09/91.77	0.48/0.53
B + AdaRound	4/32	69.15/88.70	75.51/92.73	67.76/88.12
B + FlexRound (Ours)	4/32	69.21/88.76	75.59/92.63	69.56/89.02
B + AdaQuant	3/32	60.75/83.41	66.19/87.08	0.10/0.52
B + AdaRound	3/32	67.98/88.17	74.51/92.20	60.18/83.52
B + FlexRound (Ours)	3/32	68.02/88.03	74.61/92.11	64.85/86.38
B + AdaQuant	2/32	1.13/4.10	0.12/0.60	0.10/0.50
B + AdaRound	2/32	63.01/85.20	68.31/88.98	33.10/60.58
B + FlexRound (Ours)	2/32	63.73/85.41	70.57/90.07	38.09/64.90

Table 7: Top-1/Top-5 accuracy (%) for ResNet-18, ResNet-50, and MobileNetV2 on ImageNet when both weights and activations are quantized. “B + X” and “Q + Y” represent the implementation of X in the BRECCQ’s setting and that of Y in the QDrop’s setting, respectively.

Method	# Bits (W./A.)	ResNet-18	ResNet-50	MobileNetV2
Full-precision	32/32	69.76/89.08	76.15/92.87	71.88/90.29
B + AdaRound	4/4	68.32/88.13	74.28/92.02	28.46/52.60
B + FlexRound (Ours)	4/4	68.34/88.19	74.42/92.04	55.25/78.61
Q + AdaRound	4/4	68.19/88.18	74.68/92.02	56.68/80.95
Q + FlexRound (Ours)	4/4	68.23/88.22	74.83/92.11	61.56/84.18
B + AdaRound	3/3	64.44/85.73	68.80/88.79	2.11/7.24
B + FlexRound (Ours)	3/3	64.61/85.85	69.62/89.19	8.80/21.79
Q + AdaRound	3/3	65.33/86.60	71.80/90.72	32.41/59.27
Q + FlexRound (Ours)	3/3	65.28/86.49	71.84/90.48	41.51/68.02

C BERT AND GPT-NEO ON GLUE

The experimental setting of ‘Q + AdaRound’ follows Wei et al. (2022). To investigate the natural language understanding performance of FlexRound from BERT⁴ to GPT-Neo⁵, we directly fine-tune pre-trained models on the GLUE⁶ dataset. For BERT, we use uncased models. Hyper-parameter selection for fine-tuning a pre-trained model is given in Table 8. We use ADAM optimizer as default for all methods and models. In the QDrop’s setting, the probability of dropping activation quantization is set to 0.5.

Table 8: Hyper-parameter selection for fine-tuning BERT_{Base}, BERT_{Large}, GPT-Neo_{125M}, GPT-Neo_{1.3B}, and GPT-Neo_{2.7B} on the GLUE benchmark.

Configuration	BERT _{Base}	BERT _{Large}	GPT-Neo _{125M}	GPT-Neo _{1.3B}	GPT-Neo _{2.7B}
Learning Rate	2e-5	2e-5	2e-5	2e-5	1e-5
Batch Size	32	32	32	32	16
Epoch			3		
Max Sequence Length			128		
Weight Decay			0.01		

D GPT-NEO AND OPT ON WIKITEXT2 AND PTB

To evaluate FlexRound for natural language generation tasks, we utilize the WikiText2⁷ and PTB⁸ datasets. Table 9 reports the learning rate, the batch size, and the number of iterations for ‘Q + FlexRound’. The experimental setting of ‘Q + AdaRound’ follows Wei et al. (2022) except the number of iterations; we employ 15k iterations for GPT-Neo and 20k iterations for OPT⁹. The batch size for ‘Q + AdaRound’ is same as that for ‘Q + FlexRound’. We use ADAM optimizer as default for all methods and models. The probability of dropping activation quantization is set to 0.5 in the QDrop’s setting.

⁴<https://huggingface.co/bert-base-uncased>

⁵<https://huggingface.co/EleutherAI/gpt-neo-1.3B>

⁶<https://huggingface.co/datasets/glue>

⁷<https://huggingface.co/datasets/wikitext>

⁸https://huggingface.co/datasets/ptb_text_only

⁹<https://huggingface.co/facebook/opt-1.3b>

Table 9: Hyper-parameter selection for ‘Q + FlexRound’ in Table 5.

Dataset	Configuration	GPT-Neo _{125M}	GPT-Neo _{1.3B}	GPT-Neo _{2.7B}	OPT _{125M}	OPT _{1.3B}	OPT _{2.7B}
WikiText2	Learning rate	2e-3	6e-4	4e-4	1e-3	9e-5	8e-5
	Batch size	32	16	8	32	16	8
	Iteration	15k	15k	15k	5k	5k	5k
PTB	Learning rate	4e-3	4e-3	2e-3	8e-4	1e-3	5e-3
	Batch size	32	16	8	32	16	8
	Iteration	15k	15k	15k	5k	5k	5k

E BERT ON SQUAD

Table 10 additionally shows the performance of FlexRound on the SQuADv1 (Rajpurkar et al., 2016)¹⁰ dataset for the BERT models. For experimental details, Both BERT_{Base} and BERT_{Large} are uncased models. For ‘Q + FlexRound’, the learning rate is set to 1e-4 for both models. For both ‘Q + AdaRound’ and ‘Q + FlexRound’, the batch size and the number of iterations for reconstruction are 64 and 20k respectively. We use ADAM optimizer as default for all methods and models. The other experimental setting of ‘Q + AdaRound’ follows Wei et al. (2022). Table 11 shows the hyper-parameter selection for fine-tuning. Both BERT_{Base} and BERT_{Large} are using the same configuration. The other setting for fine-tuning is the same as HuggingFace repository.

Table 10: F1 score for BERT_{Base} and BERT_{Large} on SQuADv1 dataset when both weights and activations are quantized into 8-bit. ‘‘Q + X’’ represent the implementation of X in the QDrop’s setting.

Method	# Bits (W./A.)	BERT _{Base}	BERT _{Large}
Full-precision	32/32	87.05	89.31
Q + AdaRound	8/8	86.90	88.89
Q + FlexRound (Ours)	8/8	87.25	89.25

Table 11: Hyper-parameter selection for fine-tuning BERT_{Base} and BERT_{Large} on SQuADv1 dataset.

Learning rate	Batch size	Epoch	Maximum sequence length	Document stride
1e-4	32	4	384	128

¹⁰<https://huggingface.co/datasets/squad>