On the Relationship Between Structure in Natural Language and Models of Sequential Decision Processes

Abstract

Human language is marked by powerful semantics, rich structure, and incredible flexibility, making it a hallmark of intelligent behaviour, setting humans apart from other animals. It affects the decisions we make and actions we take—allowing realisation of our thoughts and reasoning capabilities as tangible functions in the world. While AI has made great advances both in sequential decision-making using Markov Decision Processes (MDPs) and in Natural Language Processing (NLP), there is still work to be done to realise the potential offered by language, when used to inform the decision-making processes of artificial agents. In this paper, we explore how the different functional elements of natural language– such as verbs, nouns and adjectives—relate to decision process formalisms of varying complexity and structure. We attempt to determine which elements of language can be usefully grounded to a particular class of decision process and how partial observability changes the usability of language information. Our work gives insights into how more complex, structured models can capture linguistic concepts, where simple MDPs cannot. We argue that the rich structure of natural language indicates that reinforcement learning should focus on richer, more highly structured models of decision-making.

1. Introduction

Artificial Intelligence (AI) is concerned with designing agents that exhibit intelligent behaviour. These agents are typically formulated as systems able to perceive their environment via sensors, tasked with selecting actions that they execute, to maximise their utility function. This problem has historically been approached from a sequential decision making perspective, focused on designing agents that exhibit intelligent decision-making capabilities over time. Markov Decision Processes (MDPs) (Puterman, 1990) are widely used to model such problems, and many derived classes (with increasing structure and complexity) have been defined to tractably handle more complex settings.

Language is considered a hallmark of human intelligence— one of the key characteristics that sets us apart from other animals species. The use of language has allowed for the transmission, storage and evolution of knowledge for humans. Moreover, language allows to describe our world, motives and reasoning; thus enabling transfer of knowledge to individuals encountering a new scenario, enabling us to learn new concepts when needed. However, human language is vastly complex. It is marked by semantics, pragmatics, rich syntactic structure, and levels of ambiguity, and the problem of having a computer understand (or generate) it fluently is still unsolved. Language could be considered the most obvious element of high intelligence that differentiates us from other animals. Therefore, the integration of natural language and decision-making models is of particular interest to researchers aiming to create integrated, general-purpose intelligent agents.

There has been a growing interest within the community in integrating language information and decision-making agents in the context of Reinforcement Learning (RL) (Luketina et al., 2019), with marked gains in performance from using language in RL. However, there has been relatively little investigation into how the form and structure of the decision process modeled by MDPs—of which there are several classes of varying structure and complexity—might be reflected in the natural language appropriate for communicating with an agent solving one. In this work we consider the following question: what parts of speech are appropriate for communicating about what classes of MDPs? As our tasks and models grow increasingly more complex, does the spectrum of language required also broaden?

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Preliminary work. Under review by the International Conference on Machine Learning (ICML). Do not distribute.

2. Background

2.1. Classes of Markov Decision Processes

In its simplest form, a Markov Decision Process (MDP) (Puterman, 1990) is specified by the tuple (S, A, T, R, γ), where S denotes a set of states, A denotes a set of actions the agent can take, $T : S \times A \rightarrow \Delta(S)$ denotes a transition probability distribution that represents the probability of transitioning to state $s' \in S$ when action $a \in A$ is taken while in state $s \in S$, R denotes a task-specific reward function and γ denotes a discount factor. An agent solving an MDP is typically tasked with finding a policy π, mapping states to actions, that maximies the discounted cumulative rewards obtained over time, that is $\sum_{t=0}^{\infty} \gamma^t r_t$ where r_t is the reward obtained at time t. In hierarchical reinforcement learning (Barto and Mahadevan, 2003), the agent is able to structure its policy to introduce higher-level, temporally abstract, actions, often called *options* (Sutton et al., 1999).

MDPs model the special case where the agent is able to perceive, at every timestep, all the information it requires to decide which action to take. In the more general case, the agent's sensors at each timestep only offer a limited view of the environment state. Partially Observable Markov Decision Processes (**POMDP**) (Kaelbling et al., 1998) model this case by extending the MDP tuple to be $(S, A, T, R, \Omega, O, \gamma)$ where the set Ω represents the set of observations that the agent can get and $O : S \times A \rightarrow \Delta(\Omega)$ is the observation function such that $O(s, a, z) = p(z|s, a)$, i.e. when the agent in state $s \in S$ executes action $a \in A$, $O(s, a, z)$ is the probability of getting the observation $z \in \Omega$; the agent never has direct access to S. The remaining elements are defined as in the MDP case.

The basic MDP and POMDP formalisms are essentially *unstructured*: while they specify the form of the decision process, they do not impose any further structure or complexity on the form of the states, actions, and observations available to the agent. These formalisms have been extended to describe more structured decision processes. We consider the following types of structure in this paper:

Factored Factored MDPs (Guestrin et al., 2003; Koller and Parr, 2000) and Factored POMDPs (Williams et al., 2005; Katt et al., 2019) introduce structure into the state space by modeling the state as a vector of state variables $s = \{s_1, s_2, ..., s_n\}$. These variables can typically be partitioned in *factors* $s_{z_j} \subset \{s_1, s_2, ..., s_n\}$. This factorisation can be found naturally when modeling natural systems where state variables have clear semantics. This factored representation is also reflected in the transition function that can be written as the product of such factors z_j, which satisfy the conditional independence property, i.e. $P_{z_j}(s'|s, a) = P_{z_j}(s'|s_{z_j}, a)$.

Object Oriented Object-Oriented MDPs (**OO-MDP**) (Diuk et al., 2008) and POMDPs (**OO-POMDPs**) (Wandzel et al., 2019) further structure the state space by introducing the concepts of objects and object classes. Each object class is defined by a set of attributes (state variables), and each object instance has a state defined by assigning values to these attributes. The state of the entire environment is the union of the state of its constituent objects, thus allowing a more efficient, and understandable representation.

Parameterised Actions Parameterised Action MDPs (**PAMDP**) (Masson et al.) extend the set of actions A to have actions parameterised by a vector $x \in \mathbb{R}^{m_a}$. An action selection by the agent is then a pair (a, x), which specifies the discrete actions as well as its parametrisation (for example, to kick a ball with a certain amount of force, or to move at a certain velocity). We know of no existing use of PA-POMDPs, but the extension of the model to the POMDP case is straightforward.

Decentralised Decentralised MDPs (**Dec-MDP**) (Bernstein et al., 2002) and POMDPs (**Dec-POMDP**) (Nair et al., 2003) extend the MDP and POMDP formalisms to model the multi-agent case, in environments consisting of multiple agents—that together are maximizing the same reward function—selects its actions in a decentralised manner. This allows modelling of each agent's policy in the world in a decentralised manner, while allowing centralised execution of multiple agents' actions.

2.2. Syntactic Categories in Language

Syntactic categories, also known as parts-of-speech (POS), are classes of words that have semantic tendencies—for example, nouns describe *objects* while adjectives refer to *properties*. They are broadly categorised into closed class (e.g., determiners such as *"a, the"* or prepositions such as *"on, at"*, that are rarely coined or expanded as times change) and open class (e.g., verbs such as *"zoom, fax"* or nouns like *"Macbook, Roomba"* that are continually created as needed). There are four main open classes i.e., **nouns, verbs, adjectives, adverbs** each of which are subcategorised. We refer readers to the supplementary material for a full overview of parts-of-speech and the 45 categories as annotated by the Penn Tree Bank (Marcus et al., 1993). POS categories are important for several language understanding tasks, since they reveal important information about properties of the word, as well as its context. For example, for words that have different POS tags in different concepts (e.g., *"dash"* as a verb versus *"dash"* as a noun), knowing their POS tags, could help resolve ambiguity to understand the meaning of the sentence.

Tag	Description	Example
CC	coordinating conjunction	*and, or, if*
V	verb	*move, push, pull*
IN	preposition	*above, below, on*
NN	common noun	*wall, location*
NNP	proper noun	*Taxi, Agent*
ADJ	adjective	*blue, round, small*
EX	existential 'there'	*there*
MD	modal	*can, should*
ADV	adverb	*quickly, slowly*
PRP	personal pronoun	*your, their*

Table 1. Parts of speech (as tagged by the PTB) for word classes important to decision making.

2.3. Different Syntax for Different Languages

We should note that, although the four main POS categories seem like fundamental syntactic constructs, some languages (like Riau Indonesian or Tongan) do not even make a distinction between nouns and verbs (Broschart, 1997). There also exist languages devoid of a certain class e.g., adjectives in Korean, where words that would normally be adjectives in English translate to a subclass of verbs in Korean (*"beautiful"→ "to be beautiful"*). Thus, although the different languages vary in the syntactic categories they cover, their functionality can be replicated, albeit at a cost (e.g., larger number of words).

3. Language Elements for Describing Decision Processes

We now draw connections between *which* part-of-speech elements can be related to each particular model class, each of which varies in complexity from the others. We summarise these insights in Table 2.

Unstructured MDPs   This is the base formalism for decision processes in AI and the one that provides the least structure. In the most general case, the state representation is entangled or completely unstructured and, hence, tying nouns to elements of the model can be difficult. However, it is possible to relate **proper nouns** to states that have certain characteristics such as goal states. Actions can be referred to using **intransitive verbs**—as there is no concept of an object to apply the action on. Conditional statements and connecting words i.e., **conjunctions** like *"and, or"* can be used to tie together specifications of parts of the MDP. **Prepositions** denoting order relations, such as *"before, after"* could be used to describe ordering a sequence of actions or sub-policies. **Determiners** such as *"more, less, equal"*, **cardinal quantities** and **comparative adjectives/adverbs** can be used to specify rewards.

Factored MDPs   In addition to the elements above, **proper nouns** can be used to name factors. These nouns are unique in the sense that no two factors are the same. As nouns, we can qualify them by using **adjectives** that can specify properties of the factor such a particular setting of the factor. For instance, if we consider the coordinates of a robot (x, y) to be "location", "*home* location" could be the coordinates $(0, 0)$.

OO-MDPs   Object classes in OO-MDPs create the possibility of using **common nouns**. In this way, we can use **determiners** such as *"a, the"* to talk about a specific instance of an object or about any object of a class. As before, **adjectives** can qualify object instances. In this way, we can map qualified nouns to instances with particular attributes—e.g. *the red ball*. With different numbers of objects, we can use **quantifiers** such as *"there is/are, all"*. Specific instances of an object can be specified by **proper nouns**. Given the existence of objects, **transitive verbs** can be mapped to actions that affect objects, in this way information about the dynamics of the world can be represented with more complex constructs as the transition function relates to the objects' state.

PAMDPs   In this class of MDPs, we have actions that are parameterized, thus calling for **adverbs** as a way to qualify action (**verbs**). In this way, we can now realise actions that corresponds to verb phrases such as "*to go up slowly*".

Dec-MDPs   In these models, we have referential expressions, in order to denote concepts of oneself and other existing entities in the world for multi-agent environments. Therefore **pronouns** (e.g., personal, possessive) come into play.

Unstructured POMDPs   In these models, the important difference is the presence of partial observability. Part-of-speech that relate to MDPs are still pertinent here. However, we can use POS elements that can convey facts and uncertainty about the world such as **modal verbs** like *"could, should"* that allow to specify information about the world. Facts are necessary in partial observable domains in order to reduce the uncertainty the agent has about the state of the world.

Factored POMDPs   Along with the above POMDP elements, **proper nouns** can be used, in the same way as in Factored MDPs. Similarly, **adjectives** can specify properties of state variables, that differentiate them from other states.

OO-POMDPs   In OO-POMDPs, we need to express facts about the objects. Therefore, **prepositions** that denote order such as *"in, at, on, below, above"* can be used to state

MDP	V	CC	IN	Quant	NN	NNP	ADJ	EX	MD	ADV	PRP
MDP	√	√	√								
Factored MDP	√	√	√	√	√						
OO-MDP	√	√	√	√	√	√	√				
Unstructured POMDP	√	√	√					√	√		
Factored POMDP	√	√	√	√	√			√	√		
OO-POMDP	√	√	√	√	√	√	√	√	√		
LTL-MDP	√	√	√							√	
Dec-MDP	√	√	√								√
Dec-POMDP	√	√	√					√	√		√
Dec-OO-POMDP	√	√	√	√	√	√	√	√	√		√

Table 2. Differences in complexities in different classes of MDPs. Each row shows a class of MDPs while columns show POS categories that can be used to ground to existing parts of each model, as enumerated in Section 3.

relative order among object instances' states. For instance, if we instantiate an object class *"cup"*, we can use specify facts about an object class: *the cup should be in the kitchen*.

Dec-POMDPs   Analogously to the observable case, we have that in this case we need to specify facts about other agents' state and policies. As in OO-POMDPs, **prepositions** are important to provide both spatial information about the agents and temporal information—e.g. *"before, after"*—when ordering and coordination among agents' policies is required.

Non-Markovian Policies   Through the combination of conditional statements and **temporal prepositions** such as *"until, before, after"*, it is possible to specify instructions for a task which relates to further structure in the action space of the model. These instructions can be related to (sub-)policies in any of the models we have discussed thus far. However, these may be Non-Markovian given that the use of prepositions such as "until" implicitly requires the agent to record past actions and states in order to determine if a condition is satisfied. Linear Temporal Logic (LTL) has been used in several works (Ding et al., 2011; Oh et al.) that use **LTL-MDPs** in order to handle such dependencies.

4. Discussion and Conclusions

We have attempted to use insights from syntactic constructs in natural languages to characterise the differences in the forms of language useful for communicating with agents using different classes of decision-making models. We posit that the richness of language has its roots in the richness of the decision process that the agent using the language is solving. From the parallels drawn in the previous section, we can see how much of language can be (partially) related to elements of the different MDP classes, which in turn, suggests the different kinds of structure and abstractions that humans might be implicitly using to tractably solve their own decision problems. This in turn suggests that the form of language used to describe a task has the potential to aid

in automatically determining the structure and abstraction necessary for an agents to solve that task.

Moreover, we wish to emphasize that our exploration shows that much of human's use of language is used for conveying factual information about objects and object classes, which strongly suggests that human decision processes are both partially observable and highly structured. However, the flexible nature of language, both in the way that new elements—such as those of the open classes of syntactic elements—can be defined based on known elements and how verbs and nouns can be qualified in new ways, could result from the flexibility with which we can generate new abstractions to handle new problems and better handle partial observability.

Current RL research does not use highly structured and partially observable models—many current efforts go into designing algorithms with as little structural bias as possible. The richness of human language—and its clear links to richer, more structured representations—suggests that RL research should perhaps focus instead on highly structured formalisms, especially for research on grounding language in RL.

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5. Supplementary Material

Tag	Description	Example	Tag	Description	Example	Tag	Description	Example
CC	coordinating conjunction	*and, but, or*	PDT	predeterminer	*all, both*	VBP	verb non-3sg present	*eat*
CD	cardinal number	*one, two*	POS	possessive ending	*'s*	VBZ	verb 3sg pres	*eats*
DT	determiner	*a, the*	PRP	personal pronoun	*I, you, he*	WDT	wh-determ.	*which, that*
EX	existential 'there'	*there*	PRP$	possess. pronoun	*your, one's*	WP	wh-pronoun	*what, who*
FW	foreign word	*mea culpa*	RB	adverb	*quickly*	WP$	wh-possess.	*whose*
IN	preposition/ subordin-conj	*of, in, by*	RBR	comparative adverb	*faster*	WRB	wh-adverb	*how, where*
JJ	adjective	*yellow*	RBS	superlatv. adverb	*fastest*	$	dollar sign	*$*
JJR	comparative adj	*bigger*	RP	particle	*up, off*	#	pound sign	*#*
JJS	superlative adj	*wildest*	SYM	symbol	*+,%, &*	"	left quote	*' or "*
LS	list item marker	*1, 2, One*	TO	"to"	*to*	"	right quote	*' or "*
MD	modal	*can, should*	UH	interjection	*ah, oops*	(	left paren	*[, (, {, <*
NN	sing or mass noun	*llama*	VB	verb base form	*eat*	)	right paren	*],), }, >*
NNS	noun, plural	*llamas*	VBD	verb past tense	*ate*	,	comma	*,*
NNP	proper noun, sing.	*IBM*	VBG	verb gerund	*eating*	.	sent-end punc	*. ! ?*
NNPS	proper noun, plu.	*Carolinas*	VBN	verb past part.	*eaten*	:	sent-mid punc	*: ; ... – -*

Figure 8.1 Penn Treebank part-of-speech tags (including punctuation).