Domain Generalization by Learning and Removing Domain-specific Features

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Abstract

Deep Neural Networks (DNNs) suffer from domain shift when the test dataset follows a distribution different from the training dataset. Domain generalization aims to tackle this issue through learning a model that can generalize to unseen domains. In this paper, we propose a new approach that aims to explicitly remove domain-specific features for domain generalization. Following this approach, we propose a novel framework called Learning and Removing Domain-specific features for Generalization (LRDG) that learns a domain-invariant model by tactically removing domain-specific features from the input images. Specifically, we design a classifier to effectively learn domain-specific features for each source domain, respectively. We then develop an encoder-decoder network to map each input image into a new image space where the learned domain-specific features are removed. With the images output by the encoder-decoder network, another classifier is designed to learn the domain-invariant features to conduct image classification. Extensive experiments demonstrate that our framework achieves superior performance compared with the state-of-the-art methods.

1 Introduction

Deep Neural Networks (DNNs) have achieved great performance in computer vision tasks [26]. However, the performance would drop if the test dataset follows a distribution different from the training dataset. This issue is also known as domain shift [42]. Recent research has found that the DNNs tend to learn decision rules differently from humans [16, 21, 15]. For example, in ImageNet-based [37] image classification tasks, the Convolutional Neural Networks (CNNs) tend to learn local textures to discriminate objects, while we humans could use the knowledge of global object shapes as cues. The features learned by the DNNs may only belong to specific domains and are not generalized for other domains. For example, in real-world photos, objects belonging to the same category have similar textures, but in sketches [27], objects are only drawn by lines and contain no texture information. For a CNN that uses textures to discriminate objects in the photos, poor performance can be expected when it is applied to the sketches. This situation calls for the DNNs that can learn features invariant across domains instead of learning features that are domain-specific.

In this paper, we focus on the research topic of domain generalization and follow the multiple source domain generalization setting in the literature. Its goal is to train a model that can perform well on unseen domains. In this setting, we can access multiple labeled source domains and one or more unlabeled target domains. All the source and target domains share the same label space. During the training process, the source domains are available but the target domains are unseen. The target domains are only provided at the test phase.

One typical approach to domain generalization is to learn domain-invariant representations across domains [18, 30, 45, 3, 10, 13, 48, 31, 35]. This approach is based on the assumption that each

Submitted to 36th Conference on Neural Information Processing Systems (NeurIPS 2022). Do not distribute.

domain has its domain-specific features and all domains share domain-invariant features. For example, textures are domain-specific features for the photos but shapes are domain-invariant features for both photos and sketches. Previous works propose methods that seek to distill domain-invariant features. Although demonstrating promising performance, these methods do not clearly inform the deep networks that domain-specific features shall be effectively removed. Instead, it is only hoped that they would be removed through achieving the final goal of learning domain-invariant features. The lack of this clear guidance to the network may affect its learning efficacy. In this paper, we propose a new approach that aims to explicitly remove domain-specific features in order to achieve domain generalization. As indicated above, the CNNs tend to learn domain-specific features rather than domain-invariant features for classification. To prevent this from taking place, we actively remove domain-specific features and guide the CNNs to learn domain-invariant features for classification. Following this approach, we propose a novel framework: Learning and Removing Domain-specific features for Generalization (LRDG).

Our framework consists of domain-specific classifiers, an encoder-decoder network, and a domain-invariant classifier. Each domain-specific classifier can effectively learn domain-specific features from one source domain. Specifically, a domain-specific classifier is designed to discriminate the images across different classes within one particular source domain. At the same time, this classifier is required to be unable to discriminate the images across different classes within any other source domain. Each source domain therefore corresponds to one domain-specific classifier under this design. The encoder-decoder network in our framework maps the input images into a new image space where the domain-specific features are to be removed from the input images by utilizing the learned domain-specific classifiers. The transformed images are expected to contain much fewer domain-specific features compared with the original input images. The domain-invariant classifier is then appended to the encoder-decoder network and trained with the transformed images. By this design, the encoder-decoder network actively removes the domain-specific features and the domain-invariant classifier will be better guided to learn the domain-invariant features. Once trained, the encoder-decoder network and the domain-invariant classifier will be used for the classification of unseen target domains.

It is worth noting that our framework is different from the data augmentation based methods for domain generalization [46, 34, 49, 7]. Our framework aims to remove domain-specific features from the input images while data augmentation based methods generate various images with novel domain-specific features. Besides, our framework just transforms input images into a new image space and does not augment them to enlarge the training dataset.

We demonstrate the effectiveness of our framework with experiments on three benchmarks in domain generalization. Our framework consistently achieves state-of-the-art performance. We also experimentally verify that our framework effectively reduces the distribution difference among the source and target domains according to the generalization risk bound in the literature [2].

2 Proposed framework

Assuming that we are given N source domains $\mathcal{D}_s = \{D_s^1, D_s^2, \ldots, D_s^N\}$ with each domain following different distributions. For each domain (dataset), $D_s^i = \{(\mathbf{x}_j^i, y_j^i)\}_{j=1}^{n_i}$ where n_i is the number of samples in domain D_s^i, and $(\mathbf{x}_j^i, y_j^i)$ is the data-label pair for the jth sample in the ith domain. Following the literature, we assume that all source and target domains share the same label space. The goal of domain generalization is to use these source domains $\mathcal{D}_s$ to learn a model for the unseen target domain D_t.

Our work is inspired by recent work [32], where it uses a "lens" network (i.e. image-to-image translation network) to remove "shortcuts" (low-level visual features that a CNN can quickly learn, such as watermarks and color aberrations) from input images in a self-supervised learning task. Differently, our work focuses on removing domain-specific features from the input images for the domain generalization task. We use an encoder-decoder network similar to the "lens" network, but we design a different method to leverage the encoder-decoder network to remove the domain-specific features. In this section, we illustrate our framework in detail. We also provide theoretical analysis for our framework. Fig. 1 gives an overview of the entire framework.

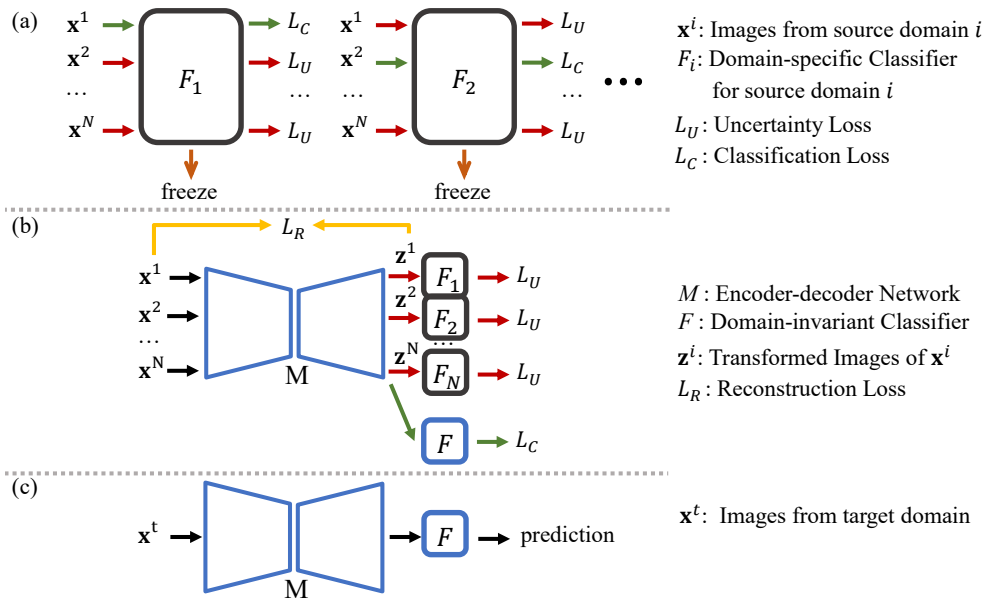


Figure 1: An overview of the proposed framework LRDG. (a) Training domain-specific classifiers for each source domain. The domain-specific classifier F_i is trained with the classification loss L_C on the source domain i and the uncertainty loss L_U on the remaining source domains. After training, the weights of the domain-specific classifiers are frozen. (b) The encoder-decoder network M is trained with the reconstruction loss L_R and the uncertainty loss L_U through domain-specific classifiers. Meanwhile, the domain-invariant classifier F is trained with the classification loss L_C on the transformed images. (c) At the testing phase, the encoder-decoder network M and the domain-invariant classifier F are used for classifying images of the target domain.

2.1 Learning domain-specific features

Our framework starts by training N individual domain-specific classifiers $\mathcal{F}_S = \{F_1, F_2, \ldots, F_N\}$ in which the ith classifier F_i is designed to only use the domain-specific features from the ith source domain D_s^i to discriminate images. The domain-specific classifiers $\mathcal{F}_S$ should not use domain-invariant features as cues. In other words, F_i is expected to be able to effectively discriminate images within D_s^i but it should be difficult for F_i to discriminate images within any other domain. Domains excluding D_s^i are used to maximize the classification uncertainty or adversarially increase the difficulty of classification for F_i. The classification performance of F_i on domains excluding D_s^i should be similar to a random guess.

Specifically, the classifier F_i is trained by minimizing a classification loss $\mathcal{L}_C^{F_S}$ on D_s^i,

$$\arg\min_{\theta_i} \mathbb{E}_{D_s^i \sim \mathcal{D}_s}[\mathbb{E}_{(\mathbf{x}_j^i, y_j^i) \sim D_s^i}[L_C(F_i(\mathbf{x}_j^i; \theta_i), y_j^i)]], \tag{1}$$

and maximizing an uncertainty loss $\mathcal{L}_U^{F_S}$ on the remaining domains $\{D_s^1, \ldots, D_s^{i-1}, D_s^{i+1}, \ldots, D_s^N\}$,

$$\arg\max_{\theta_i} \mathbb{E}_{D_s^k \sim \mathcal{D}_s, k \neq i}[\mathbb{E}_{(\mathbf{x}_j^k, y_j^k) \sim D_s^k}[L_U(F_i(\mathbf{x}_j^k; \theta_i))]], \tag{2}$$

where θ_i denotes the parameters of the classifier F_i. L_C and L_U are the classification loss function and the uncertainty loss function, respectively. We use cross-entropy loss as the classification loss. For the uncertainty loss, since we aim to make the prediction similar to a random guess, we use entropy loss:

$$L_U(F_i(\mathbf{x}_j^k; \theta_i)) = -\sum_{l=1}^{C} p(y = l | F_i(\mathbf{x}_j^k; \theta_i)) \log p(y = l | F_i(\mathbf{x}_j^k; \theta_i)), \tag{3}$$

where C is the number of classes and $p(y = l | F_i(\mathbf{x}_j^k; \theta_i))$ denotes the probability of $\mathbf{x}_j^k$ belonging to class l. Least likely loss [32] is also an alternative of the entropy loss. The classifier first predicts an

image and obtains the probabilities of all the classes. The class with the lowest probability is called least likely class. This image is assigned with a label of this class. Then we train the classifier to predict the least likely class. The least likely loss is

$$L_U(F_i(\mathbf{x}_j^k;\theta_i)) = L_C(F_i(\mathbf{x}_j^k;\theta_i), \hat{y}_j^k),\ where\ \hat{y}_j^k = \arg\min_y p(y|F_i(\mathbf{x}_j^k;\theta_i)). \tag{4}$$

However, experiments show that the entropy loss can better achieve the classification randomness than the least likely loss, so we use entropy loss as the default uncertainty loss.

After training, we freeze the parameters θ of these classifiers $\mathcal{F}_S$ and use them to learn domain-invariant features.

2.2 Removing domain-specific features

To remove domain-specific features from the input images, we utilize an encoder-decoder network M that maps the images into a new image space $\mathcal{Z}$. The output images are fed into the domain-specific classifiers $\mathcal{F}_S$ and a new domain-invariant classifier F.

Unlike the training of the domain-specific classifier F_i where the source domain D_s^i is used for minimizing the classification loss, on the contrary, the source domain D_s^i in this step is used to maximize the uncertainty loss $\mathcal{L}_U^M$

$$\arg\max_{\theta_M} \mathbb{E}_{D_s^i\sim\mathcal{D}_s}[\mathbb{E}_{(\mathbf{x}_j^i,y_j^i)\sim D_s^i}[L_U(F_i(M(\mathbf{x}_j^i;\theta_M);\theta_i))]]. \tag{5}$$

The parameters θ_i of F_i are frozen and the parameters θ_M of the encoder-decoder network M are trained. Maximizing the uncertainty loss forces the output image $\mathbf{z}_i = M(\mathbf{x}_i)$ to contain a minimum amount of domain-specific features. In doing so, the encoder-decoder network can remove the domain-specific features in the input images $\mathbf{x}$ and retain domain-invariant features in the output images $\mathbf{z}$.

To maintain the overall similarity between the input and output images, we add a reconstruction loss $\mathcal{L}_R^M$ for the encoder-decoder network,

$$\arg\min_{\theta_M} \mathbb{E}_{D_s^i\sim\mathcal{D}_s}[\mathbb{E}_{(\mathbf{x}_j^i,y_j^i)\sim D_s^i}[L_R(M(\mathbf{x}_j^i;\theta_M),\mathbf{x}_j^i)]], \tag{6}$$

where L_R is the reconstruction loss function. We use pixel-wise l_2 loss as the default reconstruction loss for its simplicity and reasonably good performance. Other reconstruction losses could also be employed, such as pixel-wise l_1 loss and perceptual losses [24]. Detailed discussion is available in the supplementary material.

We then minimize the classification loss $\mathcal{L}_C^{FM}$ by training the domain-invariant classifier F on all source domains

$$\arg\min_{\theta_M,\theta_F} \mathbb{E}_{D_s^i\sim\mathcal{D}_s}[\mathbb{E}_{(\mathbf{x}_j^i,y_j^i)\sim D_s^i}[L_C(F(M(\mathbf{x}_j^i;\theta_M);\theta_F),y_j^i)]], \tag{7}$$

where θ_F are the parameters of the domain-invariant classifier F. This classification loss $\mathcal{L}_C^{FM}$ also updates the encoder-decoder network to prevent the encoder-decoder network from losing the domain-invariant features due to the uncertainty loss. The uncertainty loss also has the potential to remove domain-invariant features if it is difficult to separate the domain-specific features from domain-invariant features.

Overall, when training domain-specific classifiers we optimize

$$\mathcal{L}_1 = \mathcal{L}_C^{F_S} + \lambda_1\mathcal{L}_U^{F_S}, \tag{8}$$

and when learning domain-invariant features, we optimize

$$\mathcal{L}_2 = \mathcal{L}_C^{FM} + \lambda_2\mathcal{L}_U^M + \lambda_3\mathcal{L}_R^M, \tag{9}$$

where λ_1, λ_2 and λ_3 are hyperparameters that control the relative weight of these losses.

For convenience, we denote the encoder-decoder network M and the domain-invariant classifier F as a domain-invariant model. At the testing phase, the domain-invariant model is used for classifying images of the target domain.

2.3 Explanation of LRDG with respect to existing theory

We first introduce the generalization risk bound for domain generalization [2] and then further explain the effectiveness of our framework with respect to this.

Theoretically, the corresponding task for a domain is defined as a deterministic true labeling function f, where $f : \mathcal{X} \to \mathcal{Y}$. $\mathcal{X}$ and $\mathcal{Y}$ are the input space and the label space, respectively. We denote the space of the candidate hypothesis as $\mathcal{H}$, where a hypothesis $h : \mathcal{X} \to \mathcal{Y}$. The risk of the hypothesis h on a domain $\mathcal{D}$ is defined as:

$$\mathcal{R}[h] = \mathbb{E}_{x\sim\mathcal{D}}[\mathcal{L}(h(x) - f(x))], \tag{10}$$

where $\mathcal{L} : \mathcal{Y} \times \mathcal{Y} \to \mathcal{R}_+$ measures the difference between the hypothesis and the true labeling function.

Following [2], for the source domains $\{\mathcal{D}_s^1, \mathcal{D}_s^2, \ldots, \mathcal{D}_s^N\}$, we define the convex hull Λ_S of the source domains as a set of mixture source distributions: $\Lambda_S = \{\bar{\mathcal{D}} : \bar{\mathcal{D}}(\cdot) = \sum_{i=1}^N \pi_i \mathcal{D}_s^i(\cdot), 0 \leq \pi_i \leq 1, \sum_{i=1}^N \pi_i = 1\}$. We also define $\bar{\mathcal{D}}_t \in \Lambda_S$ as the closest domain to the target domain $\mathcal{D}_t$. $\bar{\mathcal{D}}_t$ is given by $\arg\min_{\pi_1,\ldots,\pi_N} d_{\mathcal{H}}[\mathcal{D}_t, \sum_{i=1}^N \pi_i \mathcal{D}_s^i]$, where $d_{\mathcal{H}}[\cdot,\cdot]$ is $\mathcal{H}$-divergence [25] that quantifies the distribution difference of two domains. We use the following generalization risk bound [2] for the target domain $\mathcal{D}_t$.

Theorem 1 [2]. Given the previous setting, the following inequality holds for the risk $\mathcal{R}_t[h], \forall h \in \mathcal{H}$ for any domain $\mathcal{D}_t$:

$$\mathcal{R}_t[h] \leq \sum_{i=1}^N \pi_i \mathcal{R}_s^i[h] + \frac{\gamma + \epsilon}{2} + \lambda_\pi, \tag{11}$$

where $\gamma = d_{\mathcal{H}}[\mathcal{D}_t, \bar{\mathcal{D}}_t]$, $\epsilon = \sup_{i,j\in[N]} d_{\mathcal{H}}[\mathcal{D}_s^i, \mathcal{D}_s^j]$ and λ_π is the minimum sum of the risks achieved by some $h \in \mathcal{H}$ on $\mathcal{D}_t$ and $\bar{\mathcal{D}}_t$. γ measures the distribution difference between the source domains and the target domain. ϵ is the maximum pairwise $\mathcal{H}$-divergence among source domains. Theorem 1 shows that the upper bound for the target depends on γ and ϵ.

We show that our framework can effectively lower the value of this generalization risk bound for a given domain generalization task. Recall that our encoder-decoder network maps the input images into a new image space. We denote the mapped source domains as $\{\widehat{\mathcal{D}}_s^1, \widehat{\mathcal{D}}_s^2, \ldots, \widehat{\mathcal{D}}_s^N\}$ and the mapped target domain as $\widehat{\mathcal{D}}_t$. With the domain-specific classifiers, the domain-specific features are removed from the source domains and the mapped source domains tend to have common domain-invariant features. As a result, the mapped source domains $\{\widehat{\mathcal{D}}_s^1, \widehat{\mathcal{D}}_s^2, \ldots, \widehat{\mathcal{D}}_s^N\}$ will have smaller distribution difference than the raw source domains, i.e. $d_{\mathcal{H}}[\widehat{\mathcal{D}}_s^i, \widehat{\mathcal{D}}_s^j] \leq d_{\mathcal{H}}[\mathcal{D}_s^i, \mathcal{D}_s^j]$. ϵ in Eq. 11 is therefore reduced. After removing the domain-specific features for each source domain, the mapped target domain $\widehat{\mathcal{D}}_t$ is closer to the mapped source domains, so our framework also reduces γ in Eq. 11. Concerning Theorem 1, these changes provide a principled explanation and warrant to the effectiveness of the proposed framework. We will demonstrate these changes in the experiment section (Sec. 3.3).

3 Experiments

We evaluate our framework on three benchmark datasets and compare the performance with previous methods. After that, we study the domain divergence among the source and target domains.

3.1 Datasets and settings

Datasets. We evaluate our framework on three object recognition datasets for domain generalization. PACS [27] contains four domains: Photo (**P**), Art Painting (**A**), Cartoon (**C**) and Sketch (**S**) with each domain covering seven categories including dog, elephant, giraffe, guitar, horse, house, and person. VLCS [42] also has four domains: PASCAL VOC 2007 (**V**), LabelMe (**L**), Caltech (**C**) and Sun (**S**) and images belong to five categories of bird, chair, car, dog, and person. Office-Home [43] has images from 65 categories over four domains including Art (**A**), Clipart (**C**), Product (**P**), and Real-World (**R**). For each dataset, following the literature, the experimental protocol is to consider three domains as the source domains and the remaining one as the target domain.

Networks and loss functions. We use U-net [36] for the encoder-decoder network. Following the standard setting in the domain generalization literature [12, 48, 22], we use AlexNet [26], ResNet18 [20] and ResNet50 [20] as backbones for the domain-specific classifiers and the domain-invariant classifier. We use AlexNet for PACS and VLCS, ResNet18 for PACS and Office-Home and ResNet50 for PACS. The AlexNet and ResNet are pre-trained by ImageNet [37] for all experiments. We use the standard cross-entropy loss as the classification loss L_C. For the uncertainty loss L_U, we choose the entropy loss, and for the reconstruction loss L_R, we utilize the pixel-wise l_2 loss. A detailed analysis of the loss functions is available in the supplementary material.

Training setting. The encoder-decoder network, the domain-specific classifiers, and the domain-invariant classifier are all trained with Stochastic Gradient Descent. The source datasets are split into a training set and a validation set. The learning rates are decided by the validation set. We set $\lambda_1 = 1$ for all the experiments. We give equal weight to the classification loss and the uncertainty loss for training the domain-specific classifiers. For λ_2 and λ_3, we follow the literature [12, 4] and directly use the leave-one-domain-out cross-validation to select their values.

Methods for comparison. We compare our framework with previous domain generalization works including domain-invariant based methods [30, 44, 10, 48, 13, 31, 35] and other state-of-the-art methods [14, 4, 8, 28, 12, 49, 34, 22, 7, 47, 9] including data augmentation based methods [34, 49, 7], meta-learning based methods [4, 28, 12], etc. The baseline is defined as the method of empirical risk minimization (ERM). It trains a classifier by minimizing the classification loss on all source domains.

3.2 Main results

PACS contains four domains of Art painting, Cartoon, Photo, and Sketch. These datasets have large domain gaps. The classification results of previous methods and our framework are shown in Table 1. Averagely, our framework consistently achieves the best performance in all three backbones compared with previous works. Especially on Sketch, the accuracy of our framework is average 3% better than the previous SOTA methods, showing superior performance. Our framework also obtains the best performance on Art painting in AlexNet and maintains the highest accuracy on Cartoon in ResNet50 (ours: 85.78% vs. SOTA: 83.40%). This indicates that removing the domain-specific features from the input images is an effective method for domain generalization.

Table 1: Comparison with existing methods on PACS.

AlexNet											
Target	Baseline	CIDDG [30]	JiGen [8]	Epi-FCR [28]	MASF [12]	PAR [44]	DMG [10]	ER [48]	MetaVIB [13]	RSC [22]	LRDG (ours)
A	61.13	62.70	67.63	64.70	70.35	68.70	64.65	71.34	71.94	71.62	**72.01**
C	68.77	69.73	71.71	72.30	72.46	70.50	69.88	70.29	73.17	**75.11**	72.97
P	87.96	78.65	89.00	86.10	90.68	90.40	87.31	89.92	**91.93**	90.88	89.50
S	58.63	64.45	65.18	65.00	67.33	64.60	71.42	71.15	65.94	66.62	**74.86**
Avg.	69.12	68.88	73.38	72.00	75.21	73.54	73.32	75.67	75.74	76.05	**77.33**

ResNet18											
Target	Baseline	Epi-FCR [28]	MASF [12]	DMG [10]	ER [48]	MixStyle [49]	SagNet [34]	Stylized [7]	StableNet [47]	RSC [22]	LRDG (ours)
A	77.95	82.10	80.29	76.90	80.70	**84.10**	83.58	82.73	81.74	83.43	81.88
C	74.24	77.00	77.17	**80.38**	76.40	78.80	77.66	77.97	79.91	80.31	80.20
P	95.89	93.90	94.99	93.35	**96.65**	96.10	95.47	94.95	96.53	95.99	95.21
S	70.11	73.00	71.69	75.21	71.77	75.90	76.30	81.61	80.50	80.85	**84.65**
Avg.	79.54	81.50	81.03	81.46	81.38	83.70	83.25	84.32	84.69	85.15	**85.48**

ResNet50											
Target	Baseline	MASF [12]	Metareg [4]	DSON [39]	DMG [10]	ER [48]	RSC [22]	MatchDG [31]	SWAD [9]	Fishr [35]	LRDG (ours)
A	86.08	82.89	87.20	87.04	82.57	87.51	87.89	85.61	**89.30**	88.40	86.57
C	77.31	80.49	79.20	80.62	78.11	79.31	82.16	82.12	83.40	78.70	**85.78**
P	96.62	95.01	97.60	95.99	94.49	**98.25**	97.92	97.94	97.30	97.00	95.57
S	77.49	72.29	70.30	82.90	78.32	76.30	83.35	78.76	82.50	77.80	**86.59**
Avg.	84.37	82.67	83.60	86.64	83.37	85.34	87.83	86.11	88.10	85.50	**88.63**

VLCS dataset also contains four domains. Table 2 shows the classification accuracy of the domain generalization methods using the AlexNet backbone. It can be seen that our framework obtains comparable performance to the best-performing methods, and also outperforms prior approaches on LabelMe and Sun. For Office-Home, the ResNet18 is used as the backbone. The classification performance is shown in Table 3. Our framework outperforms previous methods and achieves the best

average performance. Besides, our framework obtains the best performance on Art (more than 1% improvement compared with the SOTA), demonstrating that removing the domain-specific features can significantly improve the generalization performance.

Table 2: Comparison with existing methods on VLCS using AlexNet backbone.

Target	Baseline	CIDDG [30]	JiGen [8]	Epi-FCR [28]	MASF [12]	ER [48]	MetaVIB [13]	Stylized [7]	RSC [22]	LRDG (ours)
V	66.27	64.38	70.62	67.10	69.14	73.24	70.28	68.18	**73.93**	68.95
L	61.81	63.06	60.90	64.30	64.90	58.26	62.66	60.77	61.86	**65.53**
C	96.17	88.83	96.93	94.10	94.78	96.92	97.37	96.86	**97.61**	96.85
S	63.78	62.10	64.30	65.90	67.64	69.10	67.85	63.42	68.32	**69.27**
Avg.	72.01	69.59	73.19	72.90	74.11	74.38	74.54	72.31	**75.43**	75.15

Table 3: Comparison with existing methods on Office-Home using ResNet18 backbones.

Target	Baseline	D-SAMs [14]	JiGen [8]	DSON [39]	MixStyle [49]	SagNet [34]	Stylized [7]	RSC [22]	LRDG (ours)
A	52.23	58.03	53.04	59.37	58.70	60.20	58.71	58.42	**61.73**
C	46.20	44.37	47.51	45.70	**53.40**	45.38	52.33	47.90	52.43
P	70.14	69.22	71.47	71.84	**74.20**	70.42	72.95	71.63	72.96
R	73.07	71.45	72.79	74.68	**75.90**	73.38	75.00	74.54	75.89
Avg.	60.41	60.77	61.20	62.90	65.50	62.34	64.75	63.12	**65.75**

3.3 Domain divergence

In this section, we investigate the distribution difference among the source domains and the target domain to demonstrate that our framework can effectively reduce domain divergence.

3.3.1 Source domain divergence

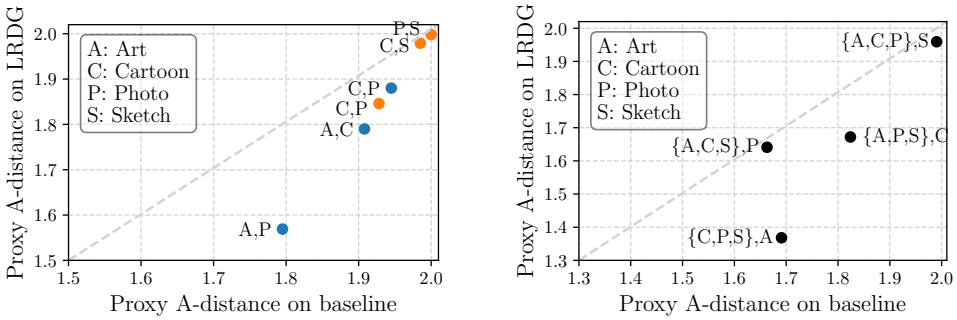
To investigate the distribution difference among the source domains, we compute the $\mathcal{H}$-divergence. Following the works of [6, 5], we can approximate the $\mathcal{H}$-divergence by a learning algorithm to discriminate between pairwise source domains. For example, with source domains $\mathcal{D}_s^i$ and $\mathcal{D}_s^j$, we label the samples of $\mathcal{D}_s^i$ by 1, and the samples of $\mathcal{D}_s^j$ by 0. We then train a classifier (e.g. linear SVM) to discriminate between these two domains. Given a test error ε of this classifier, the Proxy A-distance (PAD) defined as $2(1-2\varepsilon)$ can approximate the $\mathcal{H}$-divergence.

We follow the method from [19, 11, 1] to compute the PAD. For a pair of source domains, we combine these domains and construct a new dataset. This dataset is randomly split into two subsets of equal size. One subset is used for training and the other one is used for test. We train a collection of linear SVMs (with different values of regularization parameters) on the training set and compute the errors ε of all the SVMs on the test dataset. The lowest error ε is used to compute the PAD.

Fig. 2a compares the PAD of the raw source domains and the mapped source domains. The experiments are conducted on PACS with AlexNet backbone. For the raw source domains, we extract features from the baseline model (i.e. the last pooling layer of the AlexNet) to train the linear SVMs, while for the mapped source domains, we use features from our domain-invariant classifier. In the figure, each dot represents a pair of source domains (e.g. Art and Photo). It has two values: the PAD of the source domain pair obtained upon the baseline model (x axis) and the PAD of the same pair computed upon our framework (y axis). All the dots are below the diagonal meaning that the PAD values of the mapped pairwise source domains are lower than the raw pairwise source domains. With our framework, the mapped source domains become harder to be distinguished, indicating that removing the domain-specific features reduces the distribution difference among source domains. This also proves that ϵ in the generalization risk bound (Eq. 11) is reduced by our framework.

3.3.2 Source-Target domain divergence

We also investigate the distribution difference between the source domains and the target domain. Specifically, we measure the domain divergence between the target domain and the closest mixture



(a) (b)

Figure 2: Proxy A-distances (PAD) on PACS. *x* axis: PAD computed upon the baseline model; *y* axis: PAD computed upon our framework. **(a)** Proxy A-distances (PAD) of pairwise source domains. *Blue dots*: PAD of pairwise source domains among Art, Cartoon, and Photo (Sketch as target domain). *Orange dots*: PAD of pairwise source domains among Cartoon, Photo, and Sketch (Art as target domain). **(b)** Proxy A-distances (PAD) of pairwise source-target domains. For a target domain (e.g. Art), the source domain is the closest mixture source domain (e.g. mixture of Cartoon, Photo, and Sketch) to the target domain. The PAD is computed with the mixture source domain and the target domain.

source domain $\bar{\mathcal{D}}_t$ to the target domain. To obtain this mixture source domain, as defined in Sec. 2.3, we need to find π_i for each source domain D_s^i, so that $\bar{\mathcal{D}}_t = \sum_{i=1}^N \pi_i \mathcal{D}_s^i$, where $0 \leq \pi_i \leq 1$ and $\sum_{i=1}^N \pi_i = 1$. Because π_i can be any real value in the interval of $[0, 1]$, traversing all values to find the desired π_i is impossible. Therefore, We limit the values of π_i to the set of $\{0, 0.1, 0.2, \cdots, 0.9, 1\}$ (11 values in total), and find the setting of $\{\pi_i\}_{i=1}^N$ that can obtain $\bar{\mathcal{D}}_t$. We traverse all possible settings of $\{\pi_i\}_{i=1}^N$ and obtain all possible mixture source domains $\bar{\mathcal{D}} = \sum_{i=1}^N \pi_i \mathcal{D}_s^i$. For each setting of $\{\pi_i\}_{i=1}^N$, we random sample $\pi_i n_t$ samples from each source domain $\mathcal{D}_s^i$ and concatenate all these samples into a mixture source dataset. n_t is the number of samples in the target domain. By this design, each mixture source domain has an equal number of samples to the target domain. Similar to Sec. 3.3.1, we also train classifiers (i.e. linear SVMs) to discriminate between each mixture source domain and the target domain. The linear SVMs are trained on image features extracted from the baseline model. We then use the test error to compute the PAD between each mixture source dataset and the target dataset. The mixture source domain with the lowest PAD is the closest mixture source domain $\bar{\mathcal{D}}_t$ to the target domain. The detailed settings of π_i for the closest mixture source domains to the corresponding target domains on PACS are listed in Table 4. For convenience, we denote the closest mixture source domain $\bar{\mathcal{D}}_t$ and the target domain D_t together as a source-target domain pair.

Fig. 2b shows the PAD of the raw source-target domains and the mapped source-target domains. Similar to Sec. 3.3.1, for the raw source-target domains, we extract features from the baseline model to train the linear SVMs. To compute the PAD of the mapped source-target domains, we extracted image features from our domain-invariant classifier to train the linear SVMs. In the figure, each dot represents a source-target domain pair (e.g. {Cartoon, Photo, Sketch}, Art). We can see that all the dots are below the diagonal. The PAD values of the mapped source-target pairs are lower than the raw source-target pairs. This indicates that the distribution difference between the source domains and the target domain is reduced by our framework. γ in the generalization risk bound (Eq. 11) is therefore reduced. Removing the domain-specific features from the source domains can also reduce the distribution difference between the source domains and the target domain.

Table 4: The settings of π_i for the closest mixture source domains to the corresponding target domains on PACS.

Source			Target
D_s^1: π_1	D_s^2: π_2	D_s^3: π_3	D_t
Cartoon: 0.2	Photo: 0.8	Sketch: 0	Art
Art: 0.5	Photo: 0.3	Sketch: 0.2	Cartoon
Art: 0.7	Cartoon: 0.3	Sketch: 0	Photo
Art: 0.1	Cartoon: 0.6	Photo: 0.3	Sketch

In summary, our framework can reduce the distribution difference not only among source domains but also between the source domains and the target domain. This also demonstrates that our framework can effectively lower the value of the generalization risk bound by reducing ϵ and γ.

4 Related work

Domain generalization is a challenging task that requires models to be well performed on unseen domains. One common approach is to learn domain-invariant features among the source domains. Muandet et al. [33] propose to reduce the domain dissimilarity by a kernel-based method. Ghifary et al. [18] reduce dataset bias by extracting features that are shared among domains with a multi-task autoencoder network. Li et al. [29] utilize the Maximum Mean Discrepancy (MMD) on adversarial autoencoders to align the distributions across source domains. Li et al. [30] design an end-to-end conditional invariant deep neural network that minimizes the discrepancy of conditional distributions across domains. Arjovsky et al. [3] develop Invariant Risk Minimization (IRM) that uses a causal mechanism to obtain the optimal invariant classifier upon the representation space. Chattopadhyay et al. [10] propose to learn domain-specific binary masks to balance the domain-invariant and domain-specific features for the prediction of unseen target domains. Zhao et al. [48] propose an entropy regularization method to learn the domain-invariant conditional distributions by using classification loss and domain adversarial loss. Du et al. [13] develop a probabilistic meta-learning method that learns domain-invariant representations with meta variational information bottleneck principle derived from variational bounds of mutual information. Mahajan et al. [31] assume that domains are generated by mixing causal and non-causal features and the same object from different domains should have similar representations. Based on this, they propose a new method called MatchDG to build a domain-invariant classifier by matching similar inputs. Rame et al. [35] match the gradients among source domains to minimize domain invariance.

Recent papers demonstrate that CNNs tend to classify objects based on features from superficial local textures and backgrounds, while humans rely on global object shapes for classification [23, 17]. To address this issue, some methods aim to capture the global object shapes from the images. These methods are proposed based on the assumption that the local textures and backgrounds are the domain-specific features, and the global object shapes are the domain-invariant features. Wang et al. [45] extract semantic representations by penalizing features extracted with gray-level co-occurrence matrix (GLCM) which are sensitive to texture. Wang et al. [44] penalize the earlier layers of CNNs from learning local representations and make the CNNs rely on the global representations for classification.

5 Conclusion

In this work, we propose a new approach that aims to explicitly remove domain-specific features for domain generalization. Following this approach, we develop a novel domain generalization framework that learns domain-invariant features by actively removing domain-specific features from the input images. We also experimentally verify the reduced domain divergence among source domains and target domains brought by our approach. Experiments show that our framework achieves strong performance on various datasets compared with existing domain generalization methods.

Despite the advantages of our framework, it has some potential limitations to be further addressed. We need to train the same number of domain-specific classifiers as the source domains. When there are more source domains, more computational resources will be required to train the domain-specific classifiers. This may be addressed by designing a novel domain-specific classifier that can learn domain-specific features of multiple source domains simultaneously. Another limitation of our framework is that it cannot remove the domain-specific features of the unseen target domain. These domain-specific features should also be removed since they would negatively affect the classification performance. For example, our framework performs slightly worse than the baseline when Photo is the target domain (as shown in Table 1). This may be because Photo contains rich domain-specific features compared with the source domains, and our framework would make incorrect predictions due to these domain-specific features. As the target domain is not available during training, how to remove domain-specific features from the target domain will be another challenging issue to research.

References

[1] Hana Ajakan, Pascal Germain, Hugo Larochelle, François Laviolette, and Mario Marchand. Domain-adversarial neural networks. *arXiv preprint arXiv:1412.4446*, 2014.

[2] Isabela Albuquerque, João Monteiro, Mohammad Darvishi, Tiago H Falk, and Ioannis Mitliagkas. Generalizing to unseen domains via distribution matching. *arXiv preprint arXiv:1911.00804*, 2019.

[3] Martin Arjovsky, Léon Bottou, Ishaan Gulrajani, and David Lopez-Paz. Invariant risk minimization. *arXiv preprint arXiv:1907.02893*, 2019.

[4] Yogesh Balaji, Swami Sankaranarayanan, and Rama Chellappa. Metareg: Towards domain generalization using meta-regularization. In *Proceedings of the 32nd International Conference on Neural Information Processing Systems*, pages 1006–1016, 2018.

[5] Shai Ben-David, John Blitzer, Koby Crammer, Alex Kulesza, Fernando Pereira, and Jennifer Wortman Vaughan. A theory of learning from different domains. *Machine learning*, 79(1):151–175, 2010.

[6] Shai Ben-David, John Blitzer, Koby Crammer, Fernando Pereira, et al. Analysis of representations for domain adaptation. *Advances in neural information processing systems*, 19:137, 2007.

[7] Francesco Cappio Borlino, Antonio D'Innocente, and Tatiana Tommasi. Rethinking domain generalization baselines. In *2020 25th International Conference on Pattern Recognition (ICPR)*, pages 9227–9233. IEEE, 2021.

[8] Fabio M Carlucci, Antonio D'Innocente, Silvia Bucci, Barbara Caputo, and Tatiana Tommasi. Domain generalization by solving jigsaw puzzles. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pages 2229–2238, 2019.

[9] Junbum Cha, Sanghyuk Chun, Kyungjae Lee, Han-Cheol Cho, Seunghyun Park, Yunsung Lee, and Sungrae Park. Swad: Domain generalization by seeking flat minima. *Advances in Neural Information Processing Systems*, 34, 2021.

[10] Prithvijit Chattopadhyay, Yogesh Balaji, and Judy Hoffman. Learning to balance specificity and invariance for in and out of domain generalization. In *European Conference on Computer Vision*, pages 301–318. Springer, 2020.

[11] Minmin Chen, Zhixiang Xu, Kilian Weinberger, and Fei Sha. Marginalized denoising autoencoders for domain adaptation. In *ICML*, 2012.

[12] Qi Dou, Daniel Coelho de Castro, Konstantinos Kamnitsas, and Ben Glocker. Domain generalization via model-agnostic learning of semantic features. In *Advances in Neural Information Processing Systems*, pages 6450–6461, 2019.

[13] Yingjun Du, Jun Xu, Huan Xiong, Qiang Qiu, Xiantong Zhen, Cees GM Snoek, and Ling Shao. Learning to learn with variational information bottleneck for domain generalization. In *European Conference on Computer Vision*, pages 200–216. Springer, 2020.

[14] Antonio D'Innocente and Barbara Caputo. Domain generalization with domain-specific aggregation modules. In *German Conference on Pattern Recognition*, pages 187–198. Springer, 2018.

[15] Robert Geirhos, Jörn-Henrik Jacobsen, Claudio Michaelis, Richard Zemel, Wieland Brendel, Matthias Bethge, and Felix A Wichmann. Shortcut learning in deep neural networks. *Nature Machine Intelligence*, 2(11):665–673, 2020.

[16] Robert Geirhos, Patricia Rubisch, Claudio Michaelis, Matthias Bethge, Felix A Wichmann, and Wieland Brendel. Imagenet-trained cnns are biased towards texture; increasing shape bias improves accuracy and robustness. In *International Conference on Learning Representations*, 2018.

[17] Robert Geirhos, Patricia Rubisch, Claudio Michaelis, Matthias Bethge, Felix A Wichmann, and Wieland Brendel. Imagenet-trained cnns are biased towards texture; increasing shape bias improves accuracy and robustness. In *International Conference on Learning Representations*, 2019.

[18] Muhammad Ghifary, W Bastiaan Kleijn, Mengjie Zhang, and David Balduzzi. Domain generalization for object recognition with multi-task autoencoders. In *Proceedings of the IEEE international conference on computer vision*, pages 2551–2559, 2015.

[19] Xavier Glorot, Antoine Bordes, and Yoshua Bengio. Domain adaptation for large-scale sentiment classification: A deep learning approach. In *ICML*, 2011.

[20] Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 770–778, 2016.

[21] Katherine Hermann, Ting Chen, and Simon Kornblith. The origins and prevalence of texture bias in convolutional neural networks. *Advances in Neural Information Processing Systems*, 33, 2020.

[22] Zeyi Huang, Haohan Wang, Eric P. Xing, and Dong Huang. Self-challenging improves cross-domain generalization. In *ECCV*, 2020.

[23] Jason Jo and Yoshua Bengio. Measuring the tendency of cnns to learn surface statistical regularities. *arXiv preprint arXiv:1711.11561*, 2017.

[24] Justin Johnson, Alexandre Alahi, and Li Fei-Fei. Perceptual losses for real-time style transfer and super-resolution. In *European conference on computer vision*, pages 694–711. Springer, 2016.

[25] Daniel Kifer, Shai Ben-David, and Johannes Gehrke. Detecting change in data streams. In *VLDB*, volume 4, pages 180–191. Toronto, Canada, 2004.

[26] Alex Krizhevsky, Ilya Sutskever, and Geoffrey E Hinton. Imagenet classification with deep convolutional neural networks. *Communications of the ACM*, 60(6):84–90, 2017.

[27] Da Li, Yongxin Yang, Yi-Zhe Song, and Timothy M Hospedales. Deeper, broader and artier domain generalization. In *Proceedings of the IEEE international conference on computer vision*, pages 5542–5550, 2017.

[28] Da Li, Jianshu Zhang, Yongxin Yang, Cong Liu, Yi-Zhe Song, and Timothy M Hospedales. Episodic training for domain generalization. In *Proceedings of the IEEE International Conference on Computer Vision*, pages 1446–1455, 2019.

[29] Haoliang Li, Sinno Jialin Pan, Shiqi Wang, and Alex C Kot. Domain generalization with adversarial feature learning. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pages 5400–5409, 2018.

[30] Ya Li, Xinmei Tian, Mingming Gong, Yajing Liu, Tongliang Liu, Kun Zhang, and Dacheng Tao. Deep domain generalization via conditional invariant adversarial networks. In *Proceedings of the European Conference on Computer Vision (ECCV)*, pages 624–639, 2018.

[31] Divyat Mahajan, Shruti Tople, and Amit Sharma. Domain generalization using causal matching. In *International Conference on Machine Learning*, pages 7313–7324. PMLR, 2021.

[32] Matthias Minderer, Olivier Bachem, Neil Houlsby, and Michael Tschannen. Automatic shortcut removal for self-supervised representation learning. *International Conference on Machine Learning*, 2020.

[33] Krikamol Muandet, David Balduzzi, and Bernhard Schölkopf. Domain generalization via invariant feature representation. In *International Conference on Machine Learning*, pages 10–18. PMLR, 2013.

[34] Hyeonseob Nam, HyunJae Lee, Jongchan Park, Wonjun Yoon, and Donggeun Yoo. Reducing domain gap by reducing style bias. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 8690–8699, 2021.

[35] Alexandre Rame, Corentin Dancette, and Matthieu Cord. Fishr: Invariant gradient variances for out-of-distribution generalization. *arXiv preprint arXiv:2109.02934*, 2021.

[36] Olaf Ronneberger, Philipp Fischer, and Thomas Brox. U-net: Convolutional networks for biomedical image segmentation. In *International Conference on Medical image computing and computer-assisted intervention*, pages 234–241. Springer, 2015.

[37] Olga Russakovsky, Jia Deng, Hao Su, Jonathan Krause, Sanjeev Satheesh, Sean Ma, Zhiheng Huang, Andrej Karpathy, Aditya Khosla, Michael Bernstein, et al. Imagenet large scale visual recognition challenge. *International journal of computer vision*, 115(3):211–252, 2015.

[38] Ramprasaath R Selvaraju, Michael Cogswell, Abhishek Das, Ramakrishna Vedantam, Devi Parikh, and Dhruv Batra. Grad-cam: Visual explanations from deep networks via gradient-based localization. In *Proceedings of the IEEE international conference on computer vision*, pages 618–626, 2017.

[39] Seonguk Seo, Yumin Suh, Dongwan Kim, Geeho Kim, Jongwoo Han, and Bohyung Han. Learning to optimize domain specific normalization for domain generalization. In *Computer Vision–ECCV 2020: 16th European Conference, Glasgow, UK, August 23–28, 2020, Proceedings, Part XXII 16*, pages 68–83. Springer, 2020.

[40] Karen Simonyan and Andrew Zisserman. Very deep convolutional networks for large-scale image recognition. *arXiv preprint arXiv:1409.1556*, 2014.

[41] Jost Tobias Springenberg, Alexey Dosovitskiy, Thomas Brox, and Martin Riedmiller. Striving for simplicity: The all convolutional net. *ICLR (workshop track)*, 2015.

[42] Antonio Torralba and Alexei A Efros. Unbiased look at dataset bias. In *CVPR 2011*, pages 1521–1528. IEEE, 2011.

[43] Hemanth Venkateswara, Jose Eusebio, Shayok Chakraborty, and Sethuraman Panchanathan. Deep hashing network for unsupervised domain adaptation. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pages 5018–5027, 2017.

[44] Haohan Wang, Songwei Ge, Zachary Lipton, and Eric P Xing. Learning robust global representations by penalizing local predictive power. In *Advances in Neural Information Processing Systems*, pages 10506–10518, 2019.

[45] Haohan Wang, Zexue He, and Eric P. Xing. Learning robust representations by projecting superficial statistics out. In *International Conference on Learning Representations*, 2019.

[46] Zhenlin Xu, Deyi Liu, Junlin Yang, Colin Raffel, and Marc Niethammer. Robust and generalizable visual representation learning via random convolutions. In *International Conference on Learning Representations*, 2020.

[47] Xingxuan Zhang, Peng Cui, Renzhe Xu, Linjun Zhou, Yue He, and Zheyan Shen. Deep stable learning for out-of-distribution generalization. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 5372–5382, 2021.

[48] Shanshan Zhao, Mingming Gong, Tongliang Liu, Huan Fu, and Dacheng Tao. Domain generalization via entropy regularization. *Advances in Neural Information Processing Systems*, 33, 2020.

[49] Kaiyang Zhou, Yongxin Yang, Yu Qiao, and Tao Xiang. Domain generalization with mixstyle. In *International Conference on Learning Representations*, 2021.

Checklist

1. For all authors...
   (a) Do the main claims made in the abstract and introduction accurately reflect the paper's contributions and scope? [Yes]
   (b) Did you describe the limitations of your work? [Yes] See Section 5.
   (c) Did you discuss any potential negative societal impacts of your work? [N/A]
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