Systematic Assessment of Tabular Data Synthesis

Abstract

Data synthesis has been advocated as an important approach for utilizing data while protecting data privacy. In recent years, a plethora of tabular data synthesis algorithms (*i.e.,* synthesizers) have been proposed. A comprehensive understanding of these synthesizers' strengths and weaknesses remains elusive due to the absence of principled evaluation metrics and head-to-head comparisons between state-of-the-art deep generative approaches and statistical methods. In this paper, we examine and critique existing evaluation metrics, and introduce a set of new metrics in terms of fidelity, privacy, and utility to address their limitations. Based on the proposed metrics, we also devise a unified objective for tuning, which can consistently improve the quality of synthetic data for all methods. We conducted extensive evaluations of 8 different types of synthesizers on 12 real-world datasets and identified some interesting findings, which offer new directions for privacy-preserving data synthesis.

1 Introduction

Data-driven decision-making has emerged as the prevailing approach to advance science, industrial applications, and governance, creating the necessity to share and publish tabular data. At the same time, growing concerns about the privacy breaches caused by data disclosure call for data publishing approaches that preserve privacy. One increasingly advocated and adopted approach to reduce privacy risks while sharing data is to release synthetic data. Ideally, synthetic data can effectively fit any data processing workflow designed for the original data without privacy concerns. Data synthesis initiatives have been promoted not only by the research community (Tao et al., 2021) but also among non-profit organizations (OECD, 2023) and government agencies (Benedetto et al., 2018).

In this paper, we study data synthesis algorithms for tabular data, which we call **synthesizers**. In recent years, a plethora of synthesizers have been proposed, which can be roughly categorized into two groups: statistical and deep generative. Statistical synthesizers use low-order marginals to create synthetic datasets that match real data distributions. They were the best-performing algorithms in NIST competitions (NIST, 2018; 2020). Deep generative synthesizers, on the other hand, learn the data distribution from real data and generate synthetic instances by sampling from the learned distribution. With the recent development in deep generative models (*e.g.,* diffusion models (Ho et al., 2020) and large language models (LLMs) (Vaswani et al., 2017; Radford et al., 2019)), new synthesizers are proposed to extend these successes to the realm of tabular data synthesis.

While recent state-of-the-art approaches achieve compelling results in synthesizing authentic tabular data, a comprehensive understanding of the strengths and weaknesses of different synthesizers remains elusive. In addition, there is a lack of principled and widely accepted evaluation metrics for data synthesis. It is known that evaluating synthesizers is inherently difficult (Theis et al., 2016), and qualitative evaluation of tabular data through visual inspection is also infeasible.

The above concerns motivate us to design a systematic evaluation framework for data synthesis to elucidate the current advancements in this field. Specifically, we examine, characterize, and critique the commonly used evaluation metrics, and propose a set of new metrics for data synthesis evaluation. Our assessments unfold along three main axes:

- *Fidelity.* To address the heterogeneity and high dimensionality of tabular data, we present a new fidelity metric based on Wasserstein distance. This metric offers a unified way to evaluate numerical, discrete, and mixed data distributions under the same criteria.
- *Privacy.* We identify the inadequacy of existing syntactic privacy metrics and the ineffectiveness of membership inference attacks by conducting comparison studies. We also propose a novel privacy metric called membership disclosure score to gauge the privacy risks of synthesizers.
- *Utility.* We advocate two tasks for assessing the utility of synthesizers: machine learning prediction and range (point) query. To eliminate the inconsistent performance caused by the choice of different machine learning models, we present a utility metric that quantifies the distributional shift between real and synthetic data.

SynMeter. We implement a systematic evaluation framework called SynMeter to support the assessment of data synthesis algorithms with the proposed metrics. Differing from the existing evaluations, SynMeter incorporates the model tuning phase, which eases hyperparameter selection and consistently improves the performance of synthesizers for fair comparison. Our code is publicly available[1], facilitating researchers to tune, assess, or benchmark new synthesis algorithms.

2 DATA SYNTHESIS EVALUATION

Given a dataset D sampled from an underlying distribution $\mathbb{D}$, we write $A \leftarrow \mathcal{T}(D)$ to denote that the synthesizer A is learned by running the training algorithm $\mathcal{T}$ on the dataset D. The synthesizer A then generates a synthetic dataset S to replace D for publishing. We consider three classes of desirable properties for synthesizers:

- **Fidelity**. As the substitute for real data, the distribution of the synthetic dataset should be close to $\mathbb{D}$. Since $\mathbb{D}$ is often unknown, fidelity is measured by the similarity between the input dataset D and the synthetic dataset S. If one partitions the input dataset D into a training set D_{train} and a test set D_{test}, one can measure fidelity as closeness to either D_{train} or D_{test}.
- **Privacy**. Using synthetic data is usually motivated by the desire to protect the input dataset. Some training algorithms $\mathcal{T}$ are designed to satisfy Differential Privacy (DP) (Dwork, 2006), we refer to these as DP synthesizers. (See Appendix E for the formal definition). However, satisfying DP under reasonable parameters may result in poor performance. Some synthesizers do not satisfy DP, and aim to protect privacy empirically. We call these Heuristically Private (HP) synthesizers. As a result, privacy metrics are essential for evaluating the privacy of HP synthesis algorithms.
- **Utility**. Synthetic data often replaces real datasets to perform specific downstream tasks. In these cases, the synthetic data may not necessarily need to preserve high fidelity, as long as it achieves good utility for these tasks. Hence, utility evaluation is useful to measure the effectiveness of synthesizers for common tasks.

3 EVALUATION METRICS FOR DATA SYNTHESIS ALGORITHMS

3.1 FIDELITY EVALUATION

Existing Metrics and Limitations. Existing fidelity metrics can be categorized into three groups: low-order statistics (McKenna et al., 2019), likelihood fitness (Xu et al., 2019), and evaluator-dependent metrics (Snoke et al., 2018). The main issue with low-order statistics is the lack of versatility. Each type of marginal distribution requires a specific statistical measure, complicating comprehensive comparisons across different attribute types. Likelihood fitness assesses how well synthetic data aligns with a known prior distribution. Although this is a natural approach for assessing fidelity, it becomes problematic when the prior distribution is unknown or complex, as is often the case in real-world datasets. Evaluator-dependent metrics, on the other hand, rely heavily on auxiliary evaluators (*e.g.,* thresholds or discriminators), which require careful calibration to ensure meaningful comparisons across diverse datasets and synthesizers. A more detailed discussion of existing fidelity metrics can be found in Appendix F.1.

Proposed Metric: Wasserstein Distance. We opt for Wasserstein distance to measure the distribution discrepancies between synthetic data and real data. Originating from optimal transport theory (Peyré & Cuturi, 2019), the Wasserstein distance provides a structure-aware measure of

---

[1]https://anonymous.4open.science/r/SynMeter

the minimal amount of work required to transform one distribution into another. Formally, Let $\mathbf{P} = (p_1, p_2, \ldots p_n)$ and $\mathbf{Q} = (q_1, q_2, \ldots q_n)$ be the two probability distributions, and $\mathbf{C}$ be a matrix of size $n \times n$ in which $\mathbf{C}_{ij} \geq 0$ is the cost of moving an element i of $\mathbf{P}$ to the element j of $\mathbf{Q}$ ($\mathbf{C}_{ii} = 0$ for all element i). The optimal transport plan $\mathbf{A}$ is:

$$
\min_{\mathbf{A}} \quad \langle \mathbf{C}, \mathbf{A} \rangle \\
\text{s.t. } \mathbf{A}\mathbb{1} = \mathbf{P}, \quad \mathbf{A}^\top \mathbb{1} = \mathbf{Q},
\tag{1}
$$

where $\langle \cdot, \cdot \rangle$ is inner product between two matrices, $\mathbb{1}$ denotes a vector of all ones. Let $\mathbf{A}^*$ be the solution to the above optimization problem, Wasserstein distance is defined as:

$$
\mathcal{W}(\mathbf{P}, \mathbf{Q}) = \langle \mathbf{C}, \mathbf{A}^* \rangle.
\tag{2}
$$

Now we can use Wasserstein distance to define the fidelity:

Definition 1 (Wasserstein-based Fidelity Metric). *Let v be a set of marginal variables, and $V = \{v\}$ is the collection of marginal variable sets. $f(v, D)$ is the marginal extraction function that derives the corresponding marginal distribution of v from distribution D. Let D and S be the empirical distribution of real and synthetic data, respectively. The fidelity of synthesis algorithm A is:*

$$
\text{Fidelity}(\mathsf{A}) \triangleq \frac{1}{|V|} \sum_{v \in V} \mathcal{W}(f(v, D), f(v, S)),
\tag{3}
$$

The smaller Wasserstein distance indicates the higher fidelity of the synthesizer A.

Determining Cost Matrix. The Wasserstein distance requires the predefined cost matrix $\mathbf{C}$, which encapsulates the "cost" of transitioning from one distribution element to another. For k-way marginal distributions $\mathbf{P}$ and $\mathbf{Q}$, the cost matrix is formulated by summing the pairwise distances between corresponding elements:

$$
\mathbf{C}_{ij} = \sum_{r=1}^{k} d(v_i^r, v_j^r).
\tag{4}
$$

Here, $v_i, v_j \in \mathbb{R}^k$ are the element located in i and j in k-way probability distributions. The distance $d(\cdot, \cdot)$ is tailored to the nature of the attributes, differing for numerical and categorical values:

$$
d(v_i^r, v_j^r) = \begin{cases} ||v_i^r - v_j^r||_1, & \text{if numerical} \\ \infty \ (\text{if } v_i^r \neq v_j^r), 1 \ (\text{if } v_i^r = v_j^r), & \text{if categorical} \end{cases}
\tag{5}
$$

We use l_1 distance for numerical values and consider the strict match for categorical attributes. It is also feasible to assign semantic distance for categorical attributes (Li et al., 2021), we omit it because it depends on the specific context and most synthesizers do not model the semantics in tabular data.

Merits of Wasserstein-based Fidelity Metric. Wasserstein distance offers several advantages for fidelity evaluations: (i) Faithfulness. It is a natural and structure-aware statistic measure for analyzing distribution discrepancies, generalizing existing metrics such as total variation distance and contingency similarity (Patki et al., 2016). (ii) Universality. It accommodates both numerical and categorical attributes and extends to any multivariate marginals under the same criterion, facilitating the evaluation of heterogeneous types of marginals.

3.2 PRIVACY EVALUATION

Existing Metrics and Limitations. A popular approach to assess privacy risk for HP synthesizers is to compare the similarity between input dataset and synthetic data, with higher similarity suggesting greater information leakage. We call these metrics *syntactic* because they consider only the input and synthetic datasets, and not the algorithm used to generate the synthetic data. The most popular syntactic privacy metric is Distance to Closest Records (DCR) (Zhao et al., 2021), which looks at the distribution of the distances from each synthetic data point to its nearest real one and uses the 5th percentile of this distribution as the privacy score. DCR and/or other similar metrics are widely used both in academia (Walia et al., 2020; Yale et al., 2019) and industry (AWS, 2022; Gretel, 2023), and have become the conventional privacy metrics for HP synthesizers (Ganev & De Cristofaro, 2023b).

We point out that syntactic privacy notions that are independent of the underlying algorithm are fundamentally flawed. For example, a synthesis algorithm that applies the same fixed perturbation to every record could produce a synthetic dataset that is quite different from the input dataset, resulting in a good privacy score under a syntactic metric, even though the input dataset could be easily reconstructed from the synthetic dataset.

Membership inference attacks (MIAs) have been widely used for empirical privacy evaluation in machine learning (especially classification models) (Shokri et al., 2017). A few MIAs against tabular data synthesis algorithms have been proposed: Groundhog (Stadler et al., 2022), TAPAS (Houssiau et al., 2022) and MODIAS (van Breugel et al., 2023). Our comparison studies in Section 5.2 demonstrate that these MIA algorithms are limited in effectiveness: they fail to distinguish different levels of privacy leakage in some situations. We also observe that the standard metrics in MIA literature (*i.e.,* TPR@lowFPR) still does not capture the maximum leakage among all records in the input. The detailed analysis of the inadequacy of existing privacy metrics is in Appendix F.2.

Proposed Metric: Membership Disclosure Score (MDS). We propose a new privacy evaluation metric to assess the membership disclosure risks of synthesizers, which is inspired by both DCR and MIAs. The intuition behind MDS is that the inclusion or exclusion of each record $x \in D$ during training may lead to different behaviors of the synthesizer A, which can be measured as a function of x, D, and A. We use the maximum value for any x as the measure of privacy leakage of applying A to D. Specifically, we first define the disclosure risk of one record as follows.

Definition 2 (Disclosure Risk of One Record). *Let O_D be the synthesizer A's output distribution when trained with dataset D, $\mathcal{M}$ is a distribution distance measurement, which is non-negativity and symmetric. The disclosure risk of record $x \in D$ is given by:*

$$\mathrm{DS}(x, \mathsf{A}, D) \triangleq \mathbb{E}_{H \subset D \setminus x} \big[\mathcal{M}(O_H \| O_{H \cup \{x\}}) \big], \tag{6}$$

where H is the subset of training instances that are i.i.d sampled from $D \setminus x$. The expectation is taken with respect to the i.i.d sampling of H and the randomness in the synthesis algorithm A.

Our privacy definition compares the difference between two expected output distributions for a given record x. Unfortunately, the above computation is intractable: even the synthesizer's output distribution is not analytically known. To simplify the situation, we instead instantiate $\mathcal{M}$ to measure the closeness between x and the empirical distribution of the synthetic data:

$$\widehat{\mathrm{DS}}(x, \mathsf{A}, D) \triangleq \mathbb{E}_{H \subset D \setminus x, S \sim O_H, S' \sim O_{H \cup \{x\}}} \big[|\mathrm{dist}(x, S) - \mathrm{dist}(x, S')| \big]. \tag{7}$$

Here, S is the synthetic dataset generated from O_H, $\mathrm{dist}(x, S)$ denotes the nearest distance (under l_1 norm) between record x and synthetic dataset S. (Empirically we find that the difference between using l_1 and l_2 distance is negligible.) However, directly computing Equation (7) is computationally expensive because it requires training models on paired subsets H and $H \cup \{x\}$ for every record x. To address this, we employ the shadow training technique commonly used in MIAs. Specifically, we train m synthesizers on independently sampled subsets $H_1, ..., H_m$ of equal size $|H_i| = \lfloor \frac{1}{2}|D| \rfloor$. To calculate the disclosure risk of x, we divide these models into two groups: one trained on subsets where $x \in H$, and the other where $x \notin H$. For each model trained on these subsets, we randomly generate n synthetic datasets and take the average nearest distance to x. By doing so, we only need to train m synthesizers and sample n synthetic datasets per synthesizer. Finally, we define the privacy risk of a synthesizer A on D to be the *maximum* disclosure risk across all training data:

Definition 3 (Membership Disclosure Score). *Let S be the sampled synthetic data from the synthesizer's output distribution O_H. The membership disclosure score of A is given by:*

$$\mathrm{MDS}(\mathsf{A}) \triangleq \max_{x \in D} \Big| \underbrace{\mathbb{E}_{H \subset D, S \sim O_{H \cup \{x\}}}[\mathrm{dist}(x, S)]}_{\text{closeness of } x \text{ when trained with } x} - \underbrace{\mathbb{E}_{H \subset D \setminus x, S' \sim O_H}[\mathrm{dist}(x, S')]}_{\text{closeness of } x \text{ when \textbf{not} trained with } x} \Big|, \tag{8}$$

In practice, we train 20 models and generate 100 synthetic datasets per model to compute MDS for all synthesizers. We analyze the effectiveness and efficiency of MDS in Section 5.2.

Merits of MDS. We emphasize that MDS is not syntactic. Specifically, MDS depends on an input dataset D and the synthesis algorithm A, but it is independent of any synthetic dataset generated by a single run of the synthesizer. We also note that MDS focuses on estimating membership privacy rather than other potential privacy risks. A detailed analysis of MDS is in Appendix G.

Figure 1: Overview of SynMeter.

Table 1: Performance improvements (%) with the proposed tuning objective.

Synthesizer	Fidelity ↑		Utility ↑	
	D_{Train}	D_{Test}	MLA	Query Error
MST	0.33	0.34	17.35	3.39
PrivSyn	1.60	2.92	12.08	1.12
TVAE	1.06	0.67	5.29	2.67
CTGAN	9.87	9.60	0.57	8.63
PATE-GAN	6.27	8.48	0.75	7.04
TabDDPM	13.62	13.65	13.67	11.95
TableDiffusion	11.34	10.95	8.32	7.86
GReaT	3.84	9.21	1.14	1.77

3.3 UTILITY EVALUATION

Existing Metrics and Limitations. Machine learning efficacy (Xu et al., 2019) has emerged as the predominant utility metric for data synthesis. It first chooses a machine learning model (*i.e.,* evaluator), then assesses the testing accuracy on real data after training the evaluator on synthetic datasets. However, there is no consensus on which evaluator should be used for evaluation. Different evaluators yield varying performance outcomes on synthetic data, and no single model consistently achieves the best performance across all datasets. (We show the case in Appendix F.3.)

Proposed Metrics: Machine Learning Affinity (MLA) and Query Error. To accurately reflect the performance degradation caused by the distribution shift of synthetic data (Lopes et al., 2021), we follow (Jordon et al., 2021) and measure the relative performance gap as the utility metric:

Definition 4 (Machine Learning Affinity). *Let $\mathcal{E}$ be a set of candidate machine learning models (i.e., evaluators), let $e_{D_{train}}$ and e_S be evaluators trained on real training data D_{train} and synthetic data S, $acc(e, D_{test})$ denotes the evaluator's accuracy (F1 score or RMSE) when performed on test dataset D_{test}. The MLA of synthesizer A is given by:*

$$\text{MLA}(\mathsf{A}) := \frac{1}{|\mathcal{E}|} \sum_{e \in \mathcal{E}} \left[\frac{acc(e_{D_{train}}, D_{test}) - acc(e_S, D_{test})}{acc(e_{D_{train}}, D_{test})} \right]. \tag{9}$$

A lower MLA score indicates a higher utility of synthetic data on the prediction task.

In addition to machine learning prediction, range/point queries are workhorses of statistical data analysis. However, these tasks are often overlooked when evaluating state-of-the-art synthesizers. We follow (McKenna et al., 2019) to define the query error as below:

Definition 5 (Query Error). *Consider a subset of k attributes $a = \{a_1, ..., a_k\}$ sampled from dataset D. For each attribute, if a_i is categorical, a value v_i is randomly chosen from its domain $\mathbb{R}(a_i)$, which forms the basis for a point query condition; for numerical attributes, two values s_i and d_i from $\mathbb{R}(a_i)$ are randomly sampled as the start and end points, to construct a range query condition. The final query $c \in \mathcal{C}$ combines k sub-queries and is executed on both real and synthetic data to obtain query frequency ratios $\mu_c^{D_{test}}$ and μ_c^S. The query error of synthesis A is defined as:*

$$\text{QueryError}(\mathsf{A}) := \frac{1}{|\mathcal{C}|} \sum_{c \in \mathcal{C}} \left[||\mu_c^{D_{test}} - \mu_c^S||_1 \right]. \tag{10}$$

4 A SYSTEMATIC EVALUATION FRAMEWORK FOR DATA SYNTHESIS

Tuning Objective. Most synthesizers do not provide guidelines for hyperparameter tuning. Instead, default settings are commonly used for evaluations. This practice can lead to suboptimal results and biased comparisons. To address this issue, we propose a simple tuning objective using proposed evaluation metrics to facilitate the hyperparameter selection:

$$\mathcal{L}(\mathsf{A}) = \alpha_1 \text{Fidelity}(\mathsf{A}) + \alpha_2 \text{MLA}(\mathsf{A}) + \alpha_3 \text{QueryError}(\mathsf{A}). \tag{11}$$

Since smaller values indicate better performance for all proposed metrics, we conduct a grid search on synthesizers and select the best hyperparameters that minimize $\mathcal{L}$ for evaluation. The privacy metric is excluded from model tuning, as we find empirically that incorporating MDS yields negligible improvements for synthesizers. We show how to set the coefficients (α_1, α_2, α_3) in Section 5.2.

SynMeter. We introduce a modular toolkit called SynMeter to assess data synthesis algorithms with proposed evaluation metrics. As depicted in Figure 1, SynMeter comprises four modules, and each module is implemented with an abstract interface for any synthesizer. (The detailed description of the evaluation pipeline is in Appendix A). We envisage that SynMeter can be used to (i) facilitate data owners to tune, train, and select different synthesizers for data publishing; and (ii) serve as a benchmark for data synthesis, providing systematic evaluation metrics for comparative studies.

5 EXPERIMENTS

We present a series of comprehensive experiments to answer the following question:

- **RQ1:** How effective are our proposed privacy metric and tuning objective?
- **RQ2:** How do the various synthesizers perform under our assessment? What are the new findings?
- **RQ3:** Why do these methods work well (or not so well) on certain aspects? How can our metrics help for in-depth analysis?

5.1 EXPERIMENTAL SETUPS

Datasets We use 12 real-world public datasets for evaluation. These datasets have various sizes, natures, attributes, and distributions. Table 2 provides the overall statistics of these datasets, and the detailed descriptions can be found in Appendix B.2.

Data Synthesis Algorithms. We study a wide range of HP and DP synthesizers. Specifically, we evaluate six types of HP synthesizers: the non-private version of MST (McKenna et al., 2021), the non-private version of PrivSyn (Zhang et al., 2021), CTGAN (Xu et al., 2019), TabDDPM (Kotelnikov et al., 2023), and GReaT (Borisov et al., 2023). For DP synthesizers, we assess four types: MST, PrivSyn, PATE-GAN (Jordon et al., 2018) and TableDiffusion (Truda, 2023). Detailed descriptions of these synthesizers are in Appendix B.3.

Note that our goal is not to benchmark all synthesizers but to focus on the best-known and broad spectrum of SOTA synthesizers. TabSyn (Zhang et al., 2024) is a recent diffusion-based model that is claimed to outperform TabDDPM. We found that once TabDDPM is tuned with SynMeter, it shows a similar performance as TabSyn under our assessment. Details are in Appendix C.6.

Implementation. During the evaluation, we first tune the synthesizers with the proposed tuning objective. Then, synthetic data are generated by the trained synthesizer for evaluation, where we test 20 times and report the mean and standard deviation as the final score. The hyperparameter search spaces of data synthesis algorithms are shown in Appendix D and the implementation details of the proposed metrics are in Appendix B.1.

5.2 EFFECTIVENESS OF MDS AND TUNING OBJECTIVE (RQ1)

Effectiveness of MDS. We compare MDS against the popular syntactic privacy metric DCR (Zhao et al., 2021), as well as three state-of-the-art MIAs: Groundhog (Stadler et al., 2022), TAPAS (Houssiau et al., 2022) and MODIAS (van Breugel et al., 2023). For DCR, we calculate the nearest distance of each synthetic record to real data, using the 5th percentile of the distance distribution as the privacy score. For MIAs, we follow Carlini et al. (2022) and use the true positive rate at 1% false positive rate (TPR@1%FPR) to measure the attack performance.

We conduct two proof-of-concept experiments to evaluate the effectiveness of MDS. First, we train a DP synthesizer (PATE-GAN) with varying levels of privacy protection by adjusting the privacy budget, and we measure the empirical privacy risk using these privacy metrics. Second, we train an HP synthesizer (TabDDPM) with different duplication ratios while keeping the size of the training dataset unchanged. Intuitively, a higher proportion of duplicate samples in the training set increases the memorization of the model, which in turn poses higher privacy risks (Carlini et al., 2023).

The results of both experiments are presented in Figure 2. DCR fails to distinguish between different levels of privacy risk in both scenarios and exhibits significant instability (indicated by large standard deviations). For MIAs, we observe an improvement in attack performance as the proportion of duplicates in the training set increases, especially for MODIAS. However, MIAs still struggle to capture privacy nuances with DP synthesizers. In contrast, MDS effectively detects privacy risks across

(a) Comparing privacy metrics on DP synthesizer.

(b) Comparing privacy metrics on HP synthesizer.

Figure 2: Effectiveness evaluation of MDS on Adult dataset. DCR and MDS use the left y-axis ("Privacy Score") whereas Groundhog, TAPAS and MODIAS utilize the right y-axis ("TPR@1%FPR") for comparison. Lower DCR scores and higher MIA/MDS scores indicate greater privacy risks. Only MDS can distinguish different levels of privacy risks.

(a) Impact of the number of shadow models.

(b) Impact of the number of synthetic datasets.

Figure 3: Stability evaluation of MDS on Adult dataset. We vary the number of shadow models and synthetic datasets used for computing MDS. The MDS of all three synthesizers can be accurately computed using 20 shadow models and 100 synthetic datasets.

all scenarios and demonstrates robustness as a reliable privacy metric, as evidenced by its lower standard deviation. Additional experiments on other existing privacy metrics are in Appendix C.4.

Stability and Efficiency of MDS. We validate the stability of MDS by varying the number of shadow models and synthetic datasets. Specifically, we compute the membership disclosure scores for three synthesizers using different quantities of shadow models and synthetic datasets, recording the mean and variance of the results, as depicted in Figure 3. Our results indicate that the variance of MDS decreases rapidly as the number of shadow models and synthetic datasets increases, with stable results achieved using 20 shadow models and 100 synthetic datasets. Although MDS requires training more shadow models compared to existing MIAs, previous study (Zhang et al., 2024) shows that tabular synthesizers can be trained in just a few minutes, with sampling taking only a few seconds. Therefore, MDS remains a practical and efficient solution for privacy assessment.

Effectiveness of Tuning Objective. Although the metrics in Equation (11) are based on different measurements, empirically we observe that their values consistently fall within the same range. Consequently, in our experiments, we set all three coefficients to $1/3$, as this configuration significantly improves the quality of synthetic data, as shown in Table 1. Interestingly, the tuning phase affects two types of synthesizers differently: statistical approaches show greater gains in utility than fidelity, while deep generative models exhibit the opposite trend. Additionally, the tuning phase proves especially beneficial for TabDDPM, resulting in notable improvements across both fidelity and utility metrics. We also evaluate alternative configurations in Appendix C.5, all of which demonstrate robust performance enhancements across all synthesizers.

5.3 OVERALL EVALUATION (RQ2)

Overview. Figure 4 and Figure 5 report the overview ranking results for HP and DP synthesizers, respectively. For HP synthesizers, TabDDPM exhibits superior fidelity and utility, albeit at the expense of compromising privacy. Statistical methods like PrivSyn achieve good fidelity while offering impressive privacy protection. Conversely, CTGAN, the most popular HP synthesizer, shows the least satisfactory results in synthetic data quality. For DP synthesizers, statistical methods remain effective in both fidelity and utility. The performance of deep generative models drops significantly to satisfy differential privacy. Even the strongest model (*i.e.,* TableDiffusion) underperforms statistical approaches by a large margin, which starkly contrasts with its performance in the HP context, indicating a pronounced impact of privacy constraints on deep generative models. The visualization of synthetic and real data is depicted in Figure 8 and Figure 9.

Fidelity Evaluation. We introduce two baselines to establish empirical lower and upper bounds for the proposed fidelity metric. The first baseline, HALF, randomly divides the real data into two equal parts, using one as the training dataset D and the other as the synthetic data S. Since both datasets are from the same distribution, this serves as the empirical upper bound of fidelity. The second baseline, HISTOGRAM, generates synthetic data using one-way marginals without accounting for correlations between attributes, making it the empirical lower bound of fidelity.

Figure 4: Average ranking comparison for six HP synthesizers (outer means higher rank and better performance). Each vertex is the average rank of the method across 12 datasets, and each axis is the evaluation metric. "Fidelity($D_{\text{train}}/D_{\text{test}}$)" denotes the fidelity evaluated on the training/test dataset. "MDS" is the proposed privacy metric, and "MLA" and "Query Error" are utility metrics.

Figure 5: Average ranking comparison for four DP synthesizers. All methods offer provable privacy guarantees so we remove the privacy axis for comparison.

Fidelity is evaluated by applying the Wasserstein distance to both the training dataset D_{train} (Table 3 and Table 4) and the test dataset D_{test} (Table 5 and Table 6). The results show that TabDDPM achieves near upper-bound fidelity, while statistical methods such as MST excel in the DP synthesizer category. Notably, all deep generative models experience a significant drop in fidelity when achieving differential privacy, whereas statistical methods maintain consistent performance.

Privacy Evaluation. We utilize SELF as the baseline to represent the lower bound of MDS. Specifically, SELF uses a direct copy of the real data as synthetic data, establishing the worst privacy protection. According to the definition of MDS, an ideal privacy-preserving synthesizer would achieve a score of 0, which is the upper bound of privacy evaluation.

Table 7 and Table 8 shows the privacy assessment results for HP synthesizers. In contrast to the fidelity evaluation, CTGAN, which exhibits the lowest fidelity performance, offers the impressive privacy protection against membership disclosure. Statistical methods like MST also show notable empirical privacy protections. However, the unsatisfied results of strong synthesis algorithms like TabDDPM and GReaT reveal their vulnerability to membership disclosure.

Utility Evaluation. The utility of data synthesis is assessed by performing downstream tasks on the synthetic datasets and measuring their performance using the proposed metrics, as shown in Table 9-12. For machine learning tasks, TabDDPM excels among HP synthesizers, contributing to its class-conditional framework that learns label dependencies during its training process. However, this advantage diminishes when adding random noise to ensure privacy, where MST takes the lead with its robust and superior performance. The outcomes for range (point) query tasks echo the results of fidelity evaluation, where TabDDPM shows superior performance in HP settings, and statistical methods (*e.g.,* MST) can surpass other methods under DP constraints.

5.4 In-depth Analysis (RQ3)

In this section, we delve into the underlying reasons for the observed performances. Specifically, we employ the proposed fidelity metrics as tools for analyzing the synthesizers' learning process and explore the impact of differing privacy budgets on DP synthesizers.

Why Does CTGAN Perform Poorly? Despite CTGAN is widely regarded as a strong synthesizer, our evaluation reveals that it produces the lowest-quality synthetic data. This discrepancy raises important questions about the reasons behind CTGAN's apparent underperformance. To investigate this, we scrutinize its learning trajectory, particularly evaluating the fidelity across different marginal types during training. As shown in Figure 6(a), both numerical and categorical marginals exhibit unexpected stagnation in improvement over training. This suggests that CTGAN's synthetic data

| (a) CTGAN | (b) TabDDPM |

Figure 6: Analyzing the learning process of CT-GAN and TabDDPM with proposed fidelity metrics on the Bean dataset.

Figure 7: Impact of privacy budget ϵ on Bean dataset. The lower score indicates higher fidelity/utility.

quality is heavily influenced by data preprocessing. Specifically, CTGAN relies on a variational Gaussian mixture model for numerical data and conditional sampling for categorical attributes. The model performs well when the data distribution is close to Gaussian; however, most tabular datasets are far more complex and deviate significantly from this assumption (Gorishniy et al., 2021). This mismatch largely explains CTGAN's suboptimal performance. Furthermore, this limitation may also account for CTGAN's strong empirical privacy protections. The model's difficulty in learning complex data structures results in outputs that are largely independent of any individual training sample, contributing to its good privacy protection.

Why Does TabDDPM Excel? One key finding of our evaluations is the TabDDPM's ability to synthesize high-quality tabular data. This challenges previous claims that deep generative models generally struggle for tabular data synthesis (Tao et al., 2021). We also use proposed fidelity metrics to analyze TabDDPM's learning process. As illustrated in Figure 6(b), the Wasserstein distance across all marginal distributions rapidly decreases, demonstrating the model's capacity to learn both numerical and categorical distributions. We attribute this success to the model's architecture: diffusion models have been shown to effectively minimize the Wasserstein distance between synthetic and real data (Kwon et al., 2022). This offers a methodological advantage over other generative models, which usually aim to minimize the Kullback-Leibler divergence. However, despite its strengths, TabDDPM presents significant privacy risks that have been largely overlooked in prior research. Directly applying differential privacy measures would severely degrade the quality of the synthetic data. Nevertheless, diffusion-based methods remain a promising frontier for tabular data synthesis.

Large Language Models Are Semantic-aware Synthesizers. We also notice that the recently emerged LLM-based synthesizer (*i.e.,* GReaT) also shows competitive performance, especially on datasets that consist of rich semantic attributes. For instance, GReaT achieves the best machine learning prediction performance on the Adult dataset, which contains detailed personal information (*e.g.,* age and relationship). However, this advantage diminishes when the semantic meaning of attributes is unclear, as evidenced by its weaker performance on the Phishing dataset, where attributes are preprocessed into integers. Given the rapid development of LLM and the inherent rich semantics of most tabular data, LLM-based methods may become a new paradigm for realistic data synthesis.

The Impact of Privacy Budget. To further analyze the impact of differential privacy on data synthesis, we run DP synthesizers with varying privacy budgets, and evaluate the fidelity and utility of the resulting synthetic data (see Figure 7). Our results show that statistical methods, such as MST, maintain robust performance even with a small privacy budget (*e.g.,* $\epsilon = 0.5$). In contrast, deep generative models typically require much larger privacy budgets (*e.g.,* $\epsilon = 8$) to achieve comparable results. These findings align with previous observations (Tao et al., 2021), which noted that statistical methods are more resilient to privacy constraints because they rely on the estimation of a small set of marginals. In comparison, deep generative models aim to capture the entire joint distribution, making them more susceptible to random perturbations.

6 RELATED WORK

Benchmarking DP Synthesizers. Several studies (Tao et al., 2021; Hu et al., 2024) have benchmarked DP synthesizers based on fidelity and utility. For fidelity, various statistical measurements are utilized based on the attribute types and k-way marginals. For example, Total Variation Distance (TVD) and the Kolmogorov-Smirnov Test (KST) are applied to assess univariate distribution similarity for categorical and numerical attributes, respectively. Correlation statistics such as Theil's

uncertainty coefficient (Zhao et al., 2021), Pearson correlation (Zhang et al., 2024), and the correlation ratio (Kotelnikov et al., 2023) are used for different types of two-way marginals (categorical, continuous, and mixed). For utility, machine learning performance is commonly employed as the primary downstream task.

Benchmarking HP Synthesizers. HP synthesizers are designed without incorporating differential privacy, which aims to protect privacy empirically (Xu et al., 2019; Solatorio & Dupriez, 2023). Several studies (Espinosa & Figueira, 2023; Chundawat et al., 2022) benchmark HP synthesizers based on fidelity and utility. These benchmarks directly employ existing fidelity metrics (as mentioned above) and evaluate utility using machine learning performance and anomaly detection tasks. However, privacy evaluation is completely overlooked in these studies (Espinosa & Figueira, 2023; Chundawat et al., 2022; Livieris et al., 2024; McLachlan et al., 2018), representing a major shortcoming in these benchmarks. In addition, they did not include the newly proposed deep generative synthesizers using diffusion models or LLMs, which we found to be very promising in our studies.

New Evaluation Toolbox and Metrics. Several studies (Qian et al., 2024; Lautrup et al., 2024; Houssiau et al., 2022) have developed toolboxes to facilitate the use of both HP and DP synthesizers. Specifically, Qian et al. (2024) introduced an out-of-the-box Python library that enables researchers and practitioners to perform data synthesis. However, this study focuses primarily on broad applicability and directly employs existing evaluation metrics without providing benchmark results or offering new insights. Houssiau et al. (2022) incorporated various privacy attacks, adopting membership inference attacks and attribute inference attacks from Stadler et al. (2022). However, the attack performance was relatively weak as a meaningful privacy measurement, and the evaluation was limited to three types of synthesizers. Recently, Ganev & De Cristofaro (2023a) critiqued existing privacy evaluation metrics (*e.g.,* DCR), highlighting that these ad-hoc metrics can be exploited for reconstruction attacks. However, the study did not clearly address the fundamental flaws in these metrics (discussion in Section 3.2) and did not introduce new and effective privacy metrics.

7 DISCUSSION AND KEY TAKEAWAYS

Data synthesis has been advocated as an important approach for utilizing data while protecting privacy. Despite the plethora of available data synthesizers, a comprehensive understanding of their strengths and weaknesses remains elusive. In this paper, we examine and critique existing metrics, and introduce a systematic framework as well as a new suite of evaluation criteria for assessing data synthesizers. We also provide a unified tuning objective that can consistently improve the performance of synthesizers and ensure that evaluation results are less affected by accidental choices of hyperparameters. Our results identify several guidelines for practitioners seeking the best performance for their task and facing the daunting task of selecting and configuring appropriate synthesizers:

- *Model tuning is indispensable.* Tuning hyperparameters can significantly improve synthetic data quality, especially for deep generative models.
- *Statistical methods should be preferred for applications where privacy is paramount.* MST and PrivSyn achieve the best fidelity among DP synthesizers, and they also offer good empirical privacy protection even in HP settings.
- *Diffusion models provide the best fidelity and utility.* Practitioners are suggested to use diffusion models (*e.g.,* TabDDPM) for tabular synthesis when the quality of synthetic data is the priority over privacy due to their impressive ability to generate highly authentic data.
- *Deep generative models can be tailored for specific tasks.* The flexible design spaces of deep generative models make them suitable for scenarios where the applications of the synthetic data are known in advance (*e.g.,* machine learning prediction). In addition, the LLM-based synthesizer, GReaT, is particularly effective at preserving semantic information in synthetic data.

Our systematic assessment shows that recently emerged generative models achieve impressive performance on tabular data synthesis and open up new directions in this field. At the same time, several critical challenges are also revealed such as privacy issues of diffusion models and performance gaps between DP and HP synthesizers. Our evaluation metrics and framework play a crucial role in elucidating the advancements in data synthesis and serve as a benchmark for future works.

REFERENCES

Ahmed Alaa, Boris Van Breugel, Evgeny S Saveliev, and Mihaela van der Schaar. How faithful is your synthetic data? sample-level metrics for evaluating and auditing generative models. In *International Conference on Machine Learning*, pp. 290–306, 2022.

Meenatchi Sundaram Muthu Selva Annamalai, Andrea Gadotti, and Luc Rocher. A linear reconstruction approach for attribute inference attacks against synthetic data. In *33rd USENIX Security Symposium*, pp. 2351–2368, 2024.

AWS. How to evaluate the quality of the synthetic data: measuring from the perspective of fidelity, utility, and privacy, 2022. https://aws.amazon.com/blogs/machine-learning/how-to-evaluate-the-quality-of-the-synthetic-data-measuring-from-the-perspective-of-fidelity-utility-and-privacy/.

Gary Benedetto, Martha Stinson, and John M Abowd. The creation and use of the sipp synthetic. *US Census Bureau*, 2018.

Nicolas Bonneel, Julien Rabin, Gabriel Peyré, and Hanspeter Pfister. Sliced and radon wasserstein barycenters of measures. *Journal of Mathematical Imaging and Vision*, 51:22–45, 2015.

Vadim Borisov, Kathrin Sessler, Tobias Leemann, Martin Pawelczyk, and Gjergji Kasneci. Language models are realistic tabular data generators. In *International Conference on Learning Representations*, 2023.

Olivier Bousquet and André Elisseeff. Stability and generalization. *The Journal of Machine Learning Research*, 2:499–526, 2002.

Nicholas Carlini, Steve Chien, Milad Nasr, Shuang Song, Andreas Terzis, and Florian Tramer. Membership inference attacks from first principles. In *2022 IEEE Symposium on Security and Privacy (SP)*, pp. 1897–1914, 2022.

Nicolas Carlini, Jamie Hayes, Milad Nasr, Matthew Jagielski, Vikash Sehwag, Florian Tramer, Borja Balle, Daphne Ippolito, and Eric Wallace. Extracting training data from diffusion models. In *32nd USENIX Security Symposium*, pp. 5253–5270, 2023.

Tianqi Chen and Carlos Guestrin. Xgboost: A scalable tree boosting system. In *Proceedings of the 22nd acm sigkdd international conference on knowledge discovery and data mining*, pp. 785–794, 2016.

Vikram S Chundawat, Ayush K Tarun, Murari Mandal, Mukund Lahoti, and Pratik Narang. A universal metric for robust evaluation of synthetic tabular data. *IEEE Transactions on Artificial Intelligence*, pp. 1–11, 2022.

Marco Cuturi. Sinkhorn distances: Lightspeed computation of optimal transport. In *Proceedings of the 26 th International Conference on Neural Information Processing Systems*, 2013.

Steven Diamond and Stephen Boyd. CVXPY: A Python-embedded modeling language for convex optimization. *Journal of Machine Learning Research*, 17(83):1–5, 2016.

Jinhao Duan, Fei Kong, Shiqi Wang, Xiaoshuang Shi, and Kaidi Xu. Are diffusion models vulnerable to membership inference attacks? In *International Conference on Machine Learning*, pp. 8717–8730, 2023.

Michael Duan, Anshuman Suri, Niloofar Mireshghallah, Sewon Min, Weijia Shi, Luke Zettlemoyer, Yulia Tsvetkov, Yejin Choi, David Evans, and Hannaneh Hajishirzi. Do membership inference attacks work on large language models? *arXiv preprint arXiv:2402.07841*, 2024.

Cynthia Dwork. Differential privacy. In *Automata, Languages and Programming*, pp. 1–12, 2006.

Cynthia Dwork and Aaron Roth. The algorithmic foundations of differential privacy. *Foundations and Trends® in Theoretical Computer Science*, 9(3–4):211–407, 2014.

Erica Espinosa and Alvaro Figueira. On the quality of synthetic generated tabular data. *Mathematics*, 11(15):3278, 2023.

Vitaly Feldman. Does learning require memorization? a short tale about a long tail. In *Proceedings of the 52nd Annual ACM SIGACT Symposium on Theory of Computing*, pp. 954–959, 2020.

Rémi Flamary, Nicolas Courty, Alexandre Gramfort, Mokhtar Z. Alaya, Aurélie Boisbunon, Stanislas Chambon, Laetitia Chapel, Adrien Corenflos, Kilian Fatras, Nemo Fournier, Léo Gautheron, Nathalie T. H. Gayraud, Hicham Janati, Alain Rakotomamonjy, Ievgen Redko, Antoine Rolet, Antony Schutz, Vivien Seguy, Danica J. Sutherland, Romain Tavenard, Alexander Tong, and Titouan Vayer. Pot: Python optimal transport. *The Journal of Machine Learning Research*, 22(1): 3571–3578, 2021.

Georgi Ganev and Emiliano De Cristofaro. On the inadequacy of similarity-based privacy metrics: Reconstruction attacks against" truly anonymous synthetic data". *arXiv preprint arXiv:2312.05114*, 2023a.

Georgi Ganev and Emiliano De Cristofaro. On the inadequacy of similarity-based privacy metrics: Reconstruction attacks against "truly anonymous synthetic data". *arXiv preprint arXiv:2312.05114*, 2023b.

Yury Gorishniy, Ivan Rubachev, Valentin Khrulkov, and Artem Babenko. Revisiting deep learning models for tabular data. In *Proceedings of the 35th International Conference on Neural Information Processing Systems*, pp. 18932–18943, 2021.

Gretel. Build smarter with the right data. fast. safe. accurate, 2023. https://gretel.ai/synthetics.

Ishaan Gulrajani, Faruk Ahmed, Martin Arjovsky, Vincent Dumoulin, and Aaron C Courville. Improved training of wasserstein gans. In *Proceedings of the 31th International Conference on Neural Information Processing Systems*, 2017.

Jonathan Ho, Ajay Jain, and Pieter Abbeel. Denoising diffusion probabilistic models. In *Proceedings of the 34th International Conference on Neural Information Processing Systems*, pp. 6840–6851, 2020.

Florimond Houssiau, James Jordon, Samuel N Cohen, Owen Daniel, Andrew Elliott, James Geddes, Callum Mole, Camila Rangel-Smith, and Lukasz Szpruch. Tapas: a toolbox for adversarial privacy auditing of synthetic data. *arXiv preprint arXiv:2211.06550*, 2022.

Yuzheng Hu, Fan Wu, Qinbin Li, Yunhui Long, Gonzalo Garrido, Chang Ge, Bolin Ding, David Forsyth, Bo Li, and Dawn Song. Sok: Privacy-preserving data synthesis. In *2024 IEEE Symposium on Security and Privacy (SP)*, pp. 2–2, 2024.

Bargav Jayaraman and David Evans. Are attribute inference attacks just imputation? In *Proceedings of the 2022 ACM SIGSAC Conference on Computer and Communications Security*, pp. 1569–1582, 2022.

James Jordon, Jinsung Yoon, and Mihaela Van Der Schaar. Pate-gan: Generating synthetic data with differential privacy guarantees. In *International conference on learning representations*, 2018.

James Jordon, Lukasz Szpruch, Florimond Houssiau, Mirko Bottarelli, Giovanni Cherubin, Carsten Maple, Samuel N. Cohen, and Adrian Weller. Synthetic data – what, why and how? *arXiv preprint arXiv:2205.03257*, 2021.

Jayoung Kim, Chaejeong Lee, and Noseong Park. Stasy: Score-based tabular data synthesis. In *International Conference on Learning Representations*, 2022.

Akim Kotelnikov, Dmitry Baranchuk, Ivan Rubachev, and Artem Babenko. Tabddpm: Modelling tabular data with diffusion models. In *International Conference on Machine Learning*, pp. 17564–17579, 2023.

Dohyun Kwon, Ying Fan, and Kangwook Lee. Score-based generative modeling secretly minimizes the wasserstein distance. In *Proceedings of the 36th International Conference on Neural Information Processing Systems*, 2022.

Anton Danholt Lautrup, Tobias Hyrup, Arthur Zimek, and Peter Schneider-Kamp. Syntheval: A framework for detailed utility and privacy evaluation of tabular synthetic data. *arXiv preprint arXiv:2404.15821*, 2024.

Chaejeong Lee, Jayoung Kim, and Noseong Park. Codi: Co-evolving contrastive diffusion models for mixed-type tabular synthesis. In *International Conference on Machine Learning*, pp. 18940–18956, 2023.

Ninghui Li, Tiancheng Li, and Suresh Venkatasubramanian. t-closeness: Privacy beyond k-anonymity and l-diversity. In *2007 IEEE 23rd international conference on data engineering*, pp. 106–115, 2007.

Ninghui Li, Wahbeh Qardaji, Dong Su, Yi Wu, and Weining Yang. Membership privacy: A unifying framework for privacy definitions. In *Proceedings of the 2013 ACM SIGSAC conference on Computer & communications security*, pp. 889–900, 2013.

Ninghui Li, Min Lyu, Dong Su, and Weining Yang. *Differential privacy: From theory to practice*. Synthesis Lectures on Information Security, Privacy, & Trust. Morgan & Claypool Publishers, 2016.

Zitao Li, Trung Dang, Tianhao Wang, and Ninghui Li. Mgd: a utility metric for private data publication. In *Proceedings of the 8th International Conference on Networking, Systems and Security*, pp. 106–119, 2021.

Ioannis E Livieris, Nikos Alimpertis, George Domalis, and Dimitris Tsakalidis. An evaluation framework for synthetic data generation models. In *IFIP International Conference on Artificial Intelligence Applications and Innovations*, pp. 320–335, 2024.

Raphael Gontijo Lopes, Sylvia J Smullin, Ekin Dogus Cubuk, and Ethan Dyer. Tradeoffs in data augmentation: An empirical study. In *International Conference on Learning Representations*, 2021.

Ashwin Machanavajjhala, Johannes Gehrke, Daniel Kifer, and Muthuramakrishnan Venkitasubramaniam. l-diversity: Privacy beyond k-anonymity. In *Proceedings of the 22nd International Conference on Data Engineering*, pp. 24, 2006.

Ryan McKenna, Daniel Sheldon, and Gerome Miklau. Graphical-model based estimation and inference for differential privacy. In *International Conference on Machine Learning*, pp. 4435–4444, 2019.

Ryan McKenna, Gerome Miklau, and Daniel Sheldon. Winning the nist contest: A scalable and general approach to differentially private synthetic data. *arXiv preprint arXiv:2108.04978*, 2021.

Scott McLachlan, Kudakwashe Dube, Thomas Gallagher, Bridget J. Daley, and Jason A. Walonoski. The aten framework for creating the realistic synthetic electronic health record. In *International Conference on Health Informatics*, 2018.

NIST. Differential privacy synthetic data challenge, 2018. https://www.nist.gov/ctl/p scr/open-innovation-prize-challenges/past-prize-challenges/2018 -differential-privacy-synthetic.

NIST. Differential privacy temporal map challenge, 2020. https://www.nist.gov/ctl/p scr/open-innovation-prize-challenges/past-prize-challenges/2020 -differential-privacy-temporal.

OECD. Emerging privacy-enhancing technologies, 2023. https://www.oecd-ilibrary. org/content/paper/bf121be4-en.

Nicolas Papernot, Shuang Song, Ilya Mironov, Ananth Raghunathan, Kunal Talwar, and Ulfar Erlingsson. Scalable private learning with pate. In *International Conference on Learning Representations*, 2018.

Neha Patki, Roy Wedge, and Kalyan Veeramachaneni. The synthetic data vault. In *IEEE International Conference on Data Science and Advanced Analytics*, pp. 399–410, 2016.

Gabriel Peyré and Marco Cuturi. Computational optimal transport: With applications to data science. *Foundations and Trends® in Machine Learning*, 11(5-6):355–607, 2019.

Therese D Pigott. A review of methods for missing data. *Educational research and evaluation*, 7 (4):353–383, 2001.

Liudmila Prokhorenkova, Gleb Gusev, Aleksandr Vorobev, Anna Veronika Dorogush, and Andrey Gulin. Catboost: unbiased boosting with categorical features. In *Proceedings of the 32nd International Conference on Neural Information Processing Systems*, 2018.

Zhaozhi Qian, Rob Davis, and Mihaela van der Schaar. Synthcity: a benchmark framework for diverse use cases of tabular synthetic data. *Advances in Neural Information Processing Systems*, 36, 2024.

Alec Radford, Jeffrey Wu, Rewon Child, David Luan, Dario Amodei, and Ilya Sutskever. Language models are unsupervised multitask learners. *OpenAI blog*, 1(8):9, 2019.

Reza Shokri, Marco Stronati, Congzheng Song, and Vitaly Shmatikov. Membership inference attacks against machine learning models. In *2017 IEEE symposium on security and privacy (SP)*, pp. 3–18, 2017.

Joshua Snoke, Gillian M Raab, Beata Nowok, Chris Dibben, and Aleksandra Slavkovic. General and specific utility measures for synthetic data. *Journal of the Royal Statistical Society Series A: Statistics in Society*, 181(3):663–688, 2018.

Aivin V. Solatorio and Olivier Dupriez. Realtabformer: Generating realistic relational and tabular data using transformers. *arXiv preprint arXiv:2302.02041*, 2023.

Theresa Stadler, Bristena Oprisanu, and Carmela Troncoso. Synthetic data – anonymisation groundhog day. In *31st USENIX Security Symposium*, pp. 1451–1468, 2022.

Latanya Sweeney. k-anonymity: A model for protecting privacy. *International journal of uncertainty, fuzziness and knowledge-based systems*, 10(05):557–570, 2002.

Yuchao Tao, Ryan McKenna, Michael Hay, Ashwin Machanavajjhala, and Gerome Miklau. Benchmarking differentially private synthetic data generation algorithms. *arXiv preprint arXiv:2112.09238*, 2021.

L. Theis, A. van den Oord, and M. Bethge. A note on the evaluation of generative models. In *ICLR*, 2016.

Gianluca Truda. Generating tabular datasets under differential privacy. *arXiv preprint arXiv:2308.14784*, 2023.

Boris van Breugel, Hao Sun, Zhaozhi Qian, and Mihaela van der Schaar. Membership inference attacks against synthetic data through overfitting detection. In Francisco J. R. Ruiz, Jennifer G. Dy, and Jan-Willem van de Meent (eds.), *International Conference on Artificial Intelligence and Statistics*, pp. 3493–3514, 2023.

Laurens Van der Maaten and Geoffrey Hinton. Visualizing data using t-sne. *Journal of machine learning research*, 9(11), 2008.

Ashish Vaswani, Noam Shazeer, Niki Parmar, Jakob Uszkoreit, Llion Jones, Aidan N Gomez, Łukasz Kaiser, and Illia Polosukhin. Attention is all you need. In *Proceedings of the 31th International Conference on Neural Information Processing Systems*, 2017.

Manhar Walia, Brendan Tierney, and Susan Mckeever. Synthesising tabular data using wasserstein conditional gans with gradient penalty (wcgan-gp). In *Irish Conference on Artificial Intelligence and Cognitive Science*, 2020.

Lei Xu, Maria Skoularidou, Alfredo Cuesta-Infante, and Kalyan Veeramachaneni. Modeling tabular data using conditional gan. In *Proceedings of the 33rd International Conference on Neural Information Processing Systems*, pp. 7335–7345, 2019.

Andrew Yale, Saloni Dash, Ritik Dutta, Isabelle Guyon, Adrien Pavao, and Kristin P Bennett. Assessing privacy and quality of synthetic health data. In *Proceedings of the Conference on Artificial Intelligence for Data Discovery and Reuse*, pp. 1–4, 2019.

Chiyuan Zhang, Daphne Ippolito, Katherine Lee, Matthew Jagielski, Florian Tramèr, and Nicholas Carlini. Counterfactual memorization in neural language models. In *Proceedings of the 37th International Conference on Neural Information Processing Systems*, 2023.

Hengrui Zhang, Jiani Zhang, Balasubramaniam Srinivasan, Zhengyuan Shen, Xiao Qin, Christos Faloutsos, Huzefa Rangwala, and George Karypis. Mixed-type tabular data synthesis with score-based diffusion in latent space. In *International Conference on Learning Representations*, 2024.

Zhikun Zhang, Tianhao Wang, Ninghui Li, Jean Honorio, Michael Backes, Shibo He, Jiming Chen, and Yang Zhang. PrivSyn: Differentially private data synthesis. In *30th USENIX Security Symposium*, pp. 929–946, 2021.

Zilong Zhao, Aditya Kunar, Robert Birke, and Lydia Y. Chen. Ctab-gan: Effective table data synthesizing. In *Proceedings of The 13th Asian Conference on Machine Learning*, pp. 97–112, 2021.

A   EVALUATION PIPELINES

The SynMeter pipeline consists of four phases: data preparation, model tuning, model training, and model evaluation.

The *data preparation* phase preprocesses data for learning algorithms[2]. In this phase, statistical methods select low-dimensional marginals to serve as compact representations for capturing data distributions. Deep generative models apply standard data processing techniques like data encoding and normalization.

The goal of *model tuning* phase is to select the optimal hyperparameters for data synthesizers. We use the proposed tuning objective in Equation (11) for hyperparameter selections.

The *model training* phase focuses on model learning with tuned hyperparameters. Various generative models implement different architectures and optimization objectives.

In the *model evaluation* phase, the trained model samples some synthetic data, which are used for evaluation. Specifically, we assess the fidelity, privacy, and utility of synthesizers via the proposed metrics.

B   DETAILS OF EXPERIMENTAL SETUPS

B.1   IMPLEMENTATION DETAILS

Wasserstein-based Fidelity Metric.   The computation of Wasserstein distance involves solving the linear programming problem in Equation 1 and selecting proper marginal distributions. We compute the Wasserstein distance of all the one-way and two-way marginals and use the mean as the final fidelity score. The real dataset D can be designated as either D_{train} or D_{test} to evaluate the fidelity of synthesizers on training data or test data.

There are many open-source libraries like CVXPY (Diamond & Boyd, 2016) and POT (Flamary et al., 2021) that can be used to solve linear programming reasonably fast. However, when the cost matrix becomes rather large and dense, directly calculating the metric can be computationally expensive. Several options are provided to address this problem: (i) Sinkhorn distance (Cuturi, 2013) provides a fast approximation to the Wasserstein distance by penalizing the objective with an entropy term. (ii) Sliced-Wasserstein distance (Bonneel et al., 2015), which uses Radon transform to linearly project data into one dimension, can be efficiently computed. (iii) Reducing the size of the cost matrix by randomly sampling a small set of points from the probability densities. In practice, we find that sampling is both efficient and effective. We randomly sample half of the synthetic data when $n > 5,000$ and use the POT library to compute the Wasserstein distance as the fidelity scores.

Membership Disclosure Score (MDS).   We follow previous work (Carlini et al., 2022) and use shadow models to compute MDS. Specifically, we trained the synthesizer using half of the dataset and kept the other half as non-members for each shadow model. Once the synthesizer was trained, we randomly generated 100 synthetic datasets with the same size of training data and calculated the average closeness difference as the disclosure score. The MDS is computed as the maximum disclosure score across all records.

Utility Metrics.   For machine learning affinity (MLA), we utilize eight machine learning models to compute MLA: SVM, Logistic Regression (or Ridge Regression), Decision Tree, Random Forest, Multilayer Perceptron (MLP), XGBoost (Chen & Guestrin, 2016), CatBoost (Prokhorenkova et al., 2018), and Transformers (Gorishniy et al., 2021). Each model is extensively tuned on real training data to ensure optimal hyperparameters. Performance on classification and regression is evaluated by the F1 score and RMSE, respectively. For query error, we randomly construct 1,000 3-way query conditions and conduct range (point) queries for both synthetic and real data.

---

[2]Here we assume no missing values in the original data. The missing values problem has been extensively studied (Pigott, 2001), which is orthogonal to data synthesis.

Table 2: Statistics of datasets. # Num stands for the number of numerical columns, and # Cat stands for the number of categorical columns.

Dataset	# Train	# Validation	# Test	# Num	# Cat	Task type
Adult	20838	5210	6513	6	9	Binclass
Shoppers	7891	1973	2466	10	8	Binclass
Phishing	7075	1769	2211	0	31	Binclass
Magic	12172	3044	3804	10	1	Binclass
Faults	1241	311	389	24	4	Multiclass(7)
Bean	8710	2178	2723	16	1	Multiclass(7)
Obesity	1350	338	423	8	9	Multiclass(7)
Robot	3491	873	1092	24	1	Multiclass(4)
Abalone	2672	668	836	8	1	Regression
News	25372	6343	7929	46	14	Regression
Insurance	856	214	268	3	4	Regression
Wine	3134	784	980	12	0	Regression

B.2 DATASETS

We use 12 real-world datasets for evaluations. These datasets have various sizes, natures, attributes, and distributions. We explicitly divide datasets into training and test with a ratio of 8:2, then split 20% of the training dataset as the validation set, which is used for model tuning. The statistics of the datasets are presented in Table 2. Below is a detailed introduction to each dataset:

- **Adult**[3] is to predict whether income exceeds 50K/yr based on census data.
- **Shoppers**[4] is to analyze the intention of online shoppers.
- **Phishing**[5] is to predict if a webpage is a phishing site. The dataset consists of important features for predicting phishing sites, including information about webpage transactions.
- **Magic**[6] is to simulate the registration of high-energy gamma particles in the atmospheric telescope.
- **Faults**[7] is the fault detection dataset, which classified steel plates faults into 7 different types.
- **Bean**[8] predicts the type of dray bean based on form, shape, and structure.
- **Obesity**[9] is to estimate the obesity level based on eating habits and physical condition of individuals from Mexico, Peru, and Columbia.
- **Robot**[10] is a multi-class classification dataset collected as the robot moves around the room, following the wall using ultrasound sensors.
- **Abalone**[11] is to predict the age of abalone from physical measurements.
- **News**[12] is to predict the number of shares in social networks (popularity).
- **Insurance**[13] is for prediction on the yearly medical cover cost. The dataset contains a person's medical information.
- **Wine**[14] collects physicochemical tests on wine.

---

[3] https://archive.ics.uci.edu/dataset/2/adult
[4] https://archive.ics.uci.edu/dataset/468/online+shoppers+purchasing+intention+dataset
[5] https://archive.ics.uci.edu/dataset/468/online+shoppers+purchasing+intention+dataset
[6] https://archive.ics.uci.edu/dataset/159/magic+gamma+telescope
[7] https://archive.ics.uci.edu/dataset/198/steel+plates+faults
[8] https://archive.ics.uci.edu/dataset/602/dry+bean+dataset
[9] https://archive.ics.uci.edu/dataset/544/estimation+of+obesity+levels+based+on+eating+habits+and+physical+condition
[10] https://archive.ics.uci.edu/dataset/194/wall+following+robot+navigation+data
[11] https://archive.ics.uci.edu/dataset/1/abalone
[12] https://archive.ics.uci.edu/dataset/332/online+news+popularity
[13] https://www.kaggle.com/datasets/tejashvi14/medical-insurance-premium-prediction
[14] https://archive.ics.uci.edu/dataset/186/wine+quality

Figure 8: Visualization comparison of HP synthesizers on Bean dataset with t-SNE (Van der Maaten & Hinton, 2008). Real data are in blue and synthetic data are in orange.

B.3 USED DATA SYNTHESIS ALGORITHMS

We study a wide range of state-of-the-art synthesizers, from statistical methods to deep generative models. We select them as they are either generally considered to perform best in practice (McKenna et al., 2021; Zhang et al., 2021), widely used (Xu et al., 2019; Papernot et al., 2018), or recently emerged (Kotelnikov et al., 2023; Borisov et al., 2023; Truda, 2023). These synthesizers can be categorized into two groups: heuristic private (HP) and differentially private (DP) synthesizers.

HP Synthesizers. Synthesizers in this category are developed without integrating DP:

- **CTGAN** (Xu et al., 2019) is one of the most widely used HP synthesis algorithms. It utilizes generative adversarial networks to learn tabular data distributions. Training techniques like conditional generation and Wasserstein loss (Gulrajani et al., 2017) are used.
- **TVAE** (Xu et al., 2019) is the state-of-the-art variational autoencoder for tabular data synthesizer, which uses mode-specific normalization to tackle the non-Gaussian problems of continuous distributions.
- **TabDDPM** (Kotelnikov et al., 2023) is the state-of-the-art diffusion model for data synthesis. It leverages the Gaussian diffusion process and the multinomial diffusion process to model continuous and discrete distributions respectively.
- **GReaT** Borisov et al. (2023) utilizes the large language model (LLM) for data synthesis. It converts records to textual representations for LLM and generates synthetic data with prompts.

DP Synthesizers. These methods are either inherently designed with DP or are adaptations of HP models with additional mechanisms to offer provable privacy guarantees:

- **MST** (McKenna et al., 2021) is the state-of-the-art DP synthesizer, which uses probabilistic graphical models McKenna et al. (2019) to learn the dependence of low-dimensional marginals. It won the NIST Differential Privacy Synthetic Data Challenge NIST (2018). Discrete binning is applied for numerical attributes.
- **PrivSyn** (Zhang et al., 2021) is a non-parametric DP synthesizer, which iteratively updates the synthetic dataset to make it match the target noise marginals. This method also shows strong performance in NIST competitions (NIST, 2018; 2020). Discretization is also used for modeling numerical attributes.
- **PATE-GAN** (Jordon et al., 2018) shares a similar architecture with CTGAN, but leverages the Private Aggregation of Teacher Ensembles (PATE) (Papernot et al., 2018) to offer DP guarantees.
- **TableDiffusion** (Truda, 2023) is a newly proposed diffusion model for data synthesis, which uses Differentially Private Stochastic Gradient Descent (DP-SGD) to enforce privacy.

All DP synthesizers can be adapted to the HP scenario either by using their HP counterparts[15] (*i.e.,* CTGAN for PATE-GAN, TabDDPM for TableDiffusion) or by setting the privacy budget to infinity (*i.e.,* MST and PrivSyn). However, some HP synthesizers, such as TVAE and GReaT, do not have corresponding DP variants. Thus, we only assess their performance within the context of HP models.

MST ($\epsilon = 1$)	PrivSyn ($\epsilon = 1$)	PATE-GAN ($\epsilon = 1$)	TableDiffusion ($\epsilon = 1$)

Figure 9: Visualization comparison of DP synthesizers on Bean dataset with t-SNE. Real data are in blue and synthetic data are in orange.

C ADDITIONAL EXPERIMENTS AND RESULTS

C.1 FIDELITY RESULTS

Here we include the complete fidelity results in our evaluation. The fidelity evaluation on train data is shown in Table 5 and Table 4. The fidelity evaluation on test data is demonstrated in Table 5 and Table 6. It is observed that TabDDPM outperforms other HP synthesizers on most datasets, and statistical methods (*i.e.,* MST and PrivSyn) achieve the best performance when DP is required.

Table 3: Fidelity evaluation (lower score indicates better fidelity) of synthesizers on training data D_{train} of first six datasets. The privacy budget ϵ of HP synthesizers is ∞ (the top part), and the budget for DP synthesizers is 1 (the middle part). HALF and HISTOGRAM are the baselines that serve as the empirical upper/lower bound of the fidelity for HP synthesizers. The best result is in bold.

	Adult	Shoppers	Phishing	Magic	Faults	Bean
MST	$0.186_{\pm.010}$	$0.092_{\pm.002}$	$0.019_{\pm.001}$	$0.037_{\pm.002}$	$0.056_{\pm.002}$	$0.040_{\pm.002}$
PrivSyn	$0.024_{\pm.001}$	$0.030_{\pm.001}$	$\mathbf{0.010_{\pm.001}}$	$0.015_{\pm.003}$	$0.064_{\pm.006}$	$0.035_{\pm.002}$
TVAE	$0.085_{\pm.002}$	$0.156_{\pm.001}$	$0.024_{\pm.001}$	$0.021_{\pm.003}$	$0.055_{\pm.007}$	$0.047_{\pm.006}$
CTGAN	$0.059_{\pm.001}$	$0.062_{\pm.001}$	$0.062_{\pm.002}$	$0.157_{\pm.006}$	$0.133_{\pm.004}$	$0.139_{\pm.005}$
TabDDPM	$\mathbf{0.020_{\pm.001}}$	$\mathbf{0.022_{\pm.001}}$	$0.015_{\pm.001}$	$\mathbf{0.011_{\pm.003}}$	$\mathbf{0.026_{\pm.002}}$	$\mathbf{0.015_{\pm.002}}$
GReaT	$0.050_{\pm.002}$	$0.049_{\pm.003}$	$0.076_{\pm.002}$	$0.037_{\pm.003}$	$0.050_{\pm.006}$	$0.020_{\pm.001}$
MST ($\epsilon = 1$)	$0.198_{\pm.013}$	$0.103_{\pm.002}$	$\mathbf{0.023_{\pm.001}}$	$\mathbf{0.042_{\pm.003}}$	$\mathbf{0.086_{\pm.003}}$	$\mathbf{0.048_{\pm.004}}$
PrivSyn ($\epsilon = 1$)	$\mathbf{0.045_{\pm.002}}$	$\mathbf{0.077_{\pm.005}}$	$0.033_{\pm.002}$	$0.052_{\pm.003}$	$0.228_{\pm.007}$	$0.142_{\pm.007}$
PATE-GAN ($\epsilon = 1$)	$0.139_{\pm.001}$	$0.176_{\pm.002}$	$0.173_{\pm.002}$	$0.153_{\pm.005}$	$0.204_{\pm.003}$	$0.520_{\pm.006}$
TableDiffusion ($\epsilon = 1$)	$0.180_{\pm.002}$	$0.209_{\pm.002}$	$0.123_{\pm.002}$	$0.132_{\pm.003}$	$0.369_{\pm.002}$	$0.148_{\pm.005}$
HALF (upper bound)	$0.020_{\pm.002}$	$0.018_{\pm.001}$	$0.010_{\pm.002}$	$0.011_{\pm.004}$	$0.017_{\pm.002}$	$0.015_{\pm.004}$
HISTOGRAM (lower bound)	$0.213_{\pm.013}$	$0.101_{\pm.003}$	$0.027_{\pm.001}$	$0.051_{\pm.003}$	$0.081_{\pm.002}$	$0.087_{\pm.002}$

Table 4: Fidelity evaluation (lower score indicates better fidelity) of synthesizers on training data D_{train} of last six datasets. The privacy budget ϵ of HP synthesizers is ∞ (the top part), and the budget for DP synthesizers is 1 (the middle part). HALF and HISTOGRAM are the baselines that serve as the empirical upper/lower bound of the fidelity for HP synthesizers. The best result is in bold.

	Obesity	Robot	Abalone	News	Insurance	Wine
MST	$0.041_{\pm.001}$	$0.050_{\pm.002}$	$0.037_{\pm.002}$	$0.060_{\pm.001}$	$0.038_{\pm.005}$	$0.066_{\pm.001}$
PrivSyn	$0.034_{\pm.002}$	$0.065_{\pm.012}$	$0.024_{\pm.004}$	$\mathbf{0.018_{\pm.001}}$	$0.033_{\pm.002}$	$0.017_{\pm.000}$
TVAE	$0.055_{\pm.004}$	$0.053_{\pm.001}$	$0.048_{\pm.003}$	$0.081_{\pm.001}$	$0.078_{\pm.007}$	$0.039_{\pm.000}$
CTGAN	$0.072_{\pm.002}$	$0.106_{\pm.003}$	$0.049_{\pm.004}$	$0.040_{\pm.001}$	$0.090_{\pm.004}$	$0.033_{\pm.001}$
TabDDPM	$\mathbf{0.017_{\pm.001}}$	$\mathbf{0.015_{\pm.002}}$	$\mathbf{0.015_{\pm.004}}$	$0.034_{\pm.001}$	$\mathbf{0.028_{\pm.005}}$	$\mathbf{0.011_{\pm.000}}$
GReaT[1]	$0.055_{\pm.005}$	$0.055_{\pm.003}$	$0.022_{\pm.005}$	-	$0.094_{\pm.004}$	$0.019_{\pm.001}$
MST ($\epsilon = 1$)	$\mathbf{0.063_{\pm.001}}$	$\mathbf{0.065_{\pm.001}}$	$\mathbf{0.052_{\pm.003}}$	$\mathbf{0.062_{\pm.002}}$	$\mathbf{0.071_{\pm.002}}$	$\mathbf{0.068_{\pm.001}}$
PrivSyn ($\epsilon = 1$)	$0.167_{\pm.009}$	$0.169_{\pm.021}$	$0.127_{\pm.009}$	$0.070_{\pm.002}$	$0.124_{\pm.006}$	$0.156_{\pm.004}$
PATE-GAN ($\epsilon = 1$)	$0.086_{\pm.003}$	$0.477_{\pm.002}$	$0.331_{\pm.005}$	$0.065_{\pm.002}$	$0.385_{\pm.003}$	$0.251_{\pm.000}$
TableDiffusion ($\epsilon = 1$)	$0.347_{\pm.003}$	$0.203_{\pm.001}$	$0.232_{\pm.005}$	$0.135_{\pm.001}$	$0.343_{\pm.002}$	$0.108_{\pm.001}$
HALF (upper bound)	$0.017_{\pm.003}$	$0.010_{\pm.001}$	$0.012_{\pm.004}$	$0.009_{\pm.001}$	$0.026_{\pm.004}$	$0.006_{\pm.000}$
HISTOGRAM (lower bound)	$0.051_{\pm.001}$	$0.061_{\pm.002}$	$0.069_{\pm.001}$	$0.063_{\pm.002}$	$0.046_{\pm.002}$	$0.068_{\pm.000}$

[1]GReaT cannot be applied to the News dataset because of the maximum length limit of large language models.

---

[15]Although these paired models are quite different in the numbers of neural network layers, preprocessing, and learning strategies, they belong to the same type of generative model. Thus we call them "counterparts".

Table 5: Fidelity evaluation (*i.e.,* Wasserstein distance) of data synthesis algorithms on test data D_{test} of the first six datasets. `HALF` and `HISTOGRAM` are the baselines that serve as the empirical upper and lower bounds of the fidelity for HP synthesizers. The low score indicates the synthesizer can generate high-quality synthetic data. The best result is in bold.

	Adult	Shoppers	Phishing	Magic	Faults	Bean
MST	$0.172_{\pm.004}$	$0.098_{\pm.002}$	$0.026_{\pm.001}$	$0.039_{\pm.002}$	$0.089_{\pm.006}$	$0.044_{\pm.003}$
PrivSyn	$0.025_{\pm.001}$	$0.041_{\pm.003}$	$\mathbf{0.017_{\pm.002}}$	$0.015_{\pm.002}$	$0.079_{\pm.007}$	$0.037_{\pm.003}$
TVAE	$0.086_{\pm.002}$	$0.154_{\pm.002}$	$0.028_{\pm.002}$	$0.020_{\pm.003}$	$0.081_{\pm.016}$	$0.050_{\pm.004}$
CTGAN	$0.061_{\pm.003}$	$0.061_{\pm.002}$	$0.069_{\pm.001}$	$0.150_{\pm.004}$	$0.133_{\pm.007}$	$0.139_{\pm.005}$
TabDDPM	$\mathbf{0.021_{\pm.001}}$	$\mathbf{0.031_{\pm.001}}$	$0.019_{\pm.001}$	$\mathbf{0.012_{\pm.002}}$	$\mathbf{0.058_{\pm.008}}$	$\mathbf{0.016_{\pm.003}}$
GReaT	$0.052_{\pm.002}$	$0.056_{\pm.004}$	$0.072_{\pm.002}$	$0.039_{\pm.003}$	$0.063_{\pm.007}$	$0.021_{\pm.004}$
MST ($\epsilon = 1$)	$0.179_{\pm.004}$	$0.103_{\pm.001}$	$\mathbf{0.028_{\pm.001}}$	$0.042_{\pm.004}$	$\mathbf{0.112_{\pm.005}}$	$\mathbf{0.048_{\pm.003}}$
PrivSyn ($\epsilon = 1$)	$\mathbf{0.049_{\pm.002}}$	$\mathbf{0.084_{\pm.002}}$	$0.030_{\pm.003}$	$\mathbf{0.031_{\pm.003}}$	$0.236_{\pm.017}$	$0.128_{\pm.010}$
PATE-GAN ($\epsilon = 1$)	$0.139_{\pm.002}$	$0.171_{\pm.002}$	$0.173_{\pm.002}$	$0.155_{\pm.005}$	$0.215_{\pm.004}$	$0.523_{\pm.004}$
TableDiffusion ($\epsilon = 1$)	$0.179_{\pm.002}$	$0.210_{\pm.002}$	$0.121_{\pm.002}$	$0.132_{\pm.005}$	$0.390_{\pm.004}$	$0.149_{\pm.004}$
`HALF` (upper bound)	$0.022_{\pm.002}$	$0.023_{\pm.002}$	$0.016_{\pm.003}$	$0.011_{\pm.003}$	$0.042_{\pm.005}$	$0.015_{\pm.003}$
`HISTOGRAM` (lower bound)	$0.199_{\pm.017}$	$0.101_{\pm.001}$	$0.030_{\pm.001}$	$0.048_{\pm.002}$	$0.113_{\pm.006}$	$0.080_{\pm.003}$

Table 6: Fidelity evaluation (*i.e.,* Wasserstein distance) of data synthesis algorithms on test data D_{test} of the last six datasets. `HALF` and `HISTOGRAM` are the baselines that serve as the empirical upper and lower bounds of the fidelity for HP synthesizers. The low score indicates the synthesizer can generate high-quality synthetic data. The best result is in bold.

	Obesity	Robot	Abalone	News	Insurance	Wine
MST	$0.062_{\pm.003}$	$0.055_{\pm.003}$	$0.062_{\pm.008}$	$0.050_{\pm.004}$	$0.083_{\pm.009}$	$0.075_{\pm.002}$
PrivSyn	$0.053_{\pm.005}$	$0.054_{\pm.004}$	$\mathbf{0.032_{\pm.005}}$	$\mathbf{0.018_{\pm.001}}$	$0.074_{\pm.006}$	$0.022_{\pm.001}$
TVAE	$0.059_{\pm.003}$	$0.059_{\pm.007}$	$0.046_{\pm.005}$	$0.079_{\pm.001}$	$0.118_{\pm.009}$	$0.045_{\pm.001}$
CTGAN	$0.085_{\pm.004}$	$0.109_{\pm.009}$	$0.066_{\pm.005}$	$0.040_{\pm.001}$	$0.116_{\pm.008}$	$0.034_{\pm.001}$
TabDDPM	$\mathbf{0.043_{\pm.003}}$	$\mathbf{0.028_{\pm.004}}$	$0.034_{\pm.010}$	$0.032_{\pm.001}$	$\mathbf{0.070_{\pm.009}}$	$\mathbf{0.017_{\pm.001}}$
GReaT	$0.062_{\pm.008}$	$0.058_{\pm.006}$	$0.037_{\pm.004}$	-	$0.107_{\pm.010}$	$0.024_{\pm.001}$
MST ($\epsilon = 1$)	$\mathbf{0.075_{\pm.004}}$	$\mathbf{0.072_{\pm.007}}$	$\mathbf{0.080_{\pm.010}}$	$0.051_{\pm.002}$	$\mathbf{0.093_{\pm.006}}$	$\mathbf{0.075_{\pm.001}}$
PrivSyn ($\epsilon = 1$)	$0.154_{\pm.013}$	$0.177_{\pm.011}$	$0.111_{\pm.011}$	$\mathbf{0.044_{\pm.001}}$	$0.152_{\pm.011}$	$0.130_{\pm.005}$
PATE-GAN ($\epsilon = 1$)	$0.089_{\pm.004}$	$0.478_{\pm.007}$	$0.353_{\pm.009}$	$0.061_{\pm.002}$	$0.386_{\pm.011}$	$0.250_{\pm.003}$
TableDiffusion ($\epsilon = 1$)	$0.338_{\pm.005}$	$0.203_{\pm.002}$	$0.226_{\pm.007}$	$0.128_{\pm.001}$	$0.366_{\pm.008}$	$0.098_{\pm.001}$
`HALF` (upper bound)	$0.041_{\pm.006}$	$0.023_{\pm.005}$	$0.028_{\pm.007}$	$0.010_{\pm.002}$	$0.060_{\pm.007}$	$0.014_{\pm.001}$
`HISTOGRAM` (lower bound)	$0.066_{\pm.002}$	$0.065_{\pm.002}$	$0.094_{\pm.009}$	$0.059_{\pm.006}$	$0.081_{\pm.004}$	$0.076_{\pm.001}$

C.2 PRIVACY REUSLTS

The complete privacy results in our evaluation are shown in Table 7 and Table 8.

Table 7: Privacy evaluation (lower score means better empirical privacy protection) of HP synthesizers on the first six datasets. `SELF` is the baseline that serves as the empirical lower bound of MDS (the upper bound of MDS is 0 by definition). The best result is in bold.

	Adult	Shoppers	Phishing	Magic	Faults	Bean
MST	$\mathbf{0.031_{\pm.001}}$	$0.012_{\pm.002}$	$0.038_{\pm.003}$	$0.008_{\pm.001}$	$0.030_{\pm.002}$	$0.015_{\pm.003}$
PrivSyn	$0.046_{\pm.002}$	$\mathbf{0.005_{\pm.001}}$	$0.017_{\pm.003}$	$\mathbf{0.005_{\pm.002}}$	$\mathbf{0.004_{\pm.001}}$	$\mathbf{0.006_{\pm.003}}$
TVAE	$0.192_{\pm.003}$	$0.050_{\pm.002}$	$\mathbf{0.016_{\pm.001}}$	$0.016_{\pm.005}$	$0.037_{\pm.002}$	$0.029_{\pm.001}$
CTGAN	$0.131_{\pm.002}$	$0.018_{\pm.003}$	$0.125_{\pm.002}$	$0.012_{\pm.003}$	$0.011_{\pm.004}$	$0.028_{\pm.001}$
TabDDPM	$0.204_{\pm.001}$	$0.019_{\pm.002}$	$0.082_{\pm.003}$	$0.015_{\pm.001}$	$0.092_{\pm.002}$	$0.020_{\pm.003}$
GReaT	$0.199_{\pm.002}$	$0.044_{\pm.003}$	$0.091_{\pm.001}$	$0.011_{\pm.002}$	$0.099_{\pm.003}$	$0.016_{\pm.004}$
`SELF` (lower bound)	$0.733_{\pm.000}$	$0.094_{\pm.000}$	$0.125_{\pm.000}$	$0.199_{\pm.000}$	$0.209_{\pm.000}$	$0.273_{\pm.000}$

C.3 UTILITY RESULTS

Table 9 and Table 10 present the results of MLA and Table 11 and Table 12 presents the query error results for different synthesizers. Similar to the results of fidelity evaluation, TabDDPM demon-

Table 8: Privacy evaluation (lower score means better empirical privacy protection) of HP synthesizers on the last six datasets. SELF is the baseline that serves as the empirical lower bound of MDS (the upper bound of MDS is 0 by definition). The best result is in bold.

	Obesity	Robot	Abalone	News	Insurance	Wine
MST	$\mathbf{0.013}_{\pm.001}$	$\mathbf{0.008}_{\pm.001}$	$0.030_{\pm.002}$	$0.043_{\pm.003}$	$\mathbf{0.006}_{\pm.001}$	$0.030_{\pm.002}$
PrivSyn	$0.027_{\pm.002}$	$0.012_{\pm.001}$	$\mathbf{0.012}_{\pm.003}$	$0.005_{\pm.002}$	$0.013_{\pm.001}$	$\mathbf{0.008}_{\pm.003}$
TVAE	$0.104_{\pm.003}$	$0.039_{\pm.002}$	$0.035_{\pm.001}$	$\mathbf{0.004}_{\pm.003}$	$0.036_{\pm.002}$	$0.019_{\pm.001}$
CTGAN	$0.026_{\pm.001}$	$0.033_{\pm.003}$	$0.024_{\pm.002}$	$0.007_{\pm.005}$	$0.009_{\pm.003}$	$0.013_{\pm.001}$
TabDDPM	$0.333_{\pm.001}$	$0.113_{\pm.002}$	$0.120_{\pm.003}$	$0.008_{\pm.001}$	$0.027_{\pm.002}$	$0.075_{\pm.003}$
GReaT	$0.263_{\pm.002}$	$0.039_{\pm.003}$	$0.130_{\pm.001}$	-	$0.072_{\pm.002}$	$0.034_{\pm.003}$
SELF (lower bound)	$0.671_{\pm.000}$	$0.338_{\pm.000}$	$0.285_{\pm.000}$	$0.068_{\pm.000}$	$0.078_{\pm.000}$	$0.346_{\pm.000}$

strates strong performance among HP synthesizers, while statistical methods outperform other approaches among DP synthesizers.

Table 9: Utility evaluation (*i.e.,* MLA) of data synthesis on the first six datasets. The lower value means better utility. The privacy budget ϵ of HP synthesizers is set as ∞ (the top part), and the budget for DP synthesizers is set as 1 (the bottom part). The best result of each category is in bold.

	Adult	Shoppers	Phishing	Magic	Faults	Bean
MST	$0.086_{\pm.001}$	$0.193_{\pm.002}$	$0.037_{\pm.003}$	$0.073_{\pm.001}$	$0.255_{\pm.002}$	$0.035_{\pm.003}$
PrivSyn	$0.120_{\pm.003}$	$0.040_{\pm.001}$	$0.057_{\pm.002}$	$0.085_{\pm.003}$	$0.532_{\pm.001}$	$0.039_{\pm.002}$
TVAE	$0.035_{\pm.002}$	$0.011_{\pm.003}$	$0.031_{\pm.001}$	$0.075_{\pm.002}$	$0.217_{\pm.003}$	$0.059_{\pm.001}$
CTGAN	$0.039_{\pm.003}$	$0.031_{\pm.002}$	$0.068_{\pm.001}$	$0.154_{\pm.003}$	$0.525_{\pm.002}$	$0.103_{\pm.001}$
TabDDPM	$0.014_{\pm.001}$	$\mathbf{0.006}_{\pm.002}$	$\mathbf{0.007}_{\pm.003}$	$\mathbf{0.007}_{\pm.001}$	$\mathbf{0.085}_{\pm.002}$	$\mathbf{0.003}_{\pm.003}$
GReaT	$\mathbf{0.009}_{\pm.002}$	$0.009_{\pm.003}$	$0.020_{\pm.001}$	$0.033_{\pm.002}$	$0.183_{\pm.003}$	$0.017_{\pm.001}$
MST ($\epsilon = 1$)	$\mathbf{0.101}_{\pm.003}$	$\mathbf{0.048}_{\pm.001}$	$\mathbf{0.041}_{\pm.002}$	$\mathbf{0.093}_{\pm.003}$	$\mathbf{0.489}_{\pm.001}$	$\mathbf{0.054}_{\pm.002}$
PrivSyn ($\epsilon = 1$)	$0.120_{\pm.002}$	$0.177_{\pm.003}$	$0.085_{\pm.001}$	$0.217_{\pm.002}$	$0.753_{\pm.003}$	$0.466_{\pm.001}$
PATE-GAN ($\epsilon = 1$)	$0.126_{\pm.001}$	$0.135_{\pm.002}$	$0.530_{\pm.003}$	$0.394_{\pm.001}$	$0.781_{\pm.002}$	$0.781_{\pm.003}$
TableDiffusion ($\epsilon = 1$)	$0.198_{\pm.002}$	$0.135_{\pm.003}$	$0.074_{\pm.001}$	$0.133_{\pm.002}$	$0.904_{\pm.003}$	$0.981_{\pm.001}$

Table 10: Utility evaluation (*i.e.,* MLA) of data synthesis on the last six datasets. The lower value means better utility. The privacy budget ϵ of HP synthesizers is set as ∞ (the top part), and the budget for DP synthesizers is set as 1 (the bottom part). The best result of each category is in bold.

	Obesity	Robot	Abalone	News	Insurance	Wine
MST	$0.332_{\pm.001}$	$0.146_{\pm.002}$	$0.096_{\pm.003}$	$0.498_{\pm.001}$	$0.270_{\pm.002}$	$0.347_{\pm.003}$
PrivSyn	$0.604_{\pm.003}$	$0.406_{\pm.001}$	$0.210_{\pm.002}$	$1.992_{\pm.003}$	$0.518_{\pm.001}$	$0.201_{\pm.002}$
TVAE	$0.294_{\pm.002}$	$0.128_{\pm.003}$	$0.245_{\pm.001}$	$0.147_{\pm.002}$	$0.336_{\pm.003}$	$0.091_{\pm.001}$
CTGAN	$0.893_{\pm.003}$	$0.434_{\pm.002}$	$0.282_{\pm.001}$	$0.104_{\pm.003}$	$1.700_{\pm.002}$	$0.222_{\pm.001}$
TabDDPM	$\mathbf{0.021}_{\pm.001}$	$\mathbf{0.011}_{\pm.002}$	$\mathbf{0.043}_{\pm.003}$	$\mathbf{0.047}_{\pm.001}$	$\mathbf{0.140}_{\pm.002}$	$\mathbf{0.047}_{\pm.003}$
GReaT	$0.117_{\pm.002}$	$0.050_{\pm.003}$	$0.038_{\pm.001}$	-	$0.292_{\pm.002}$	$0.083_{\pm.003}$
MST ($\epsilon = 1$)	$\mathbf{0.531}_{\pm.003}$	$\mathbf{0.245}_{\pm.001}$	$\mathbf{0.241}_{\pm.002}$	$1.072_{\pm.003}$	$\mathbf{1.366}_{\pm.001}$	$0.340_{\pm.002}$
PrivSyn ($\epsilon = 1$)	$0.821_{\pm.002}$	$0.608_{\pm.003}$	$0.624_{\pm.001}$	$4.538_{\pm.002}$	$1.878_{\pm.003}$	$\mathbf{0.302}_{\pm.001}$
PATE-GAN ($\epsilon = 1$)	$0.877_{\pm.001}$	$0.755_{\pm.002}$	$2.119_{\pm.003}$	$0.259_{\pm.001}$	$2.325_{\pm.002}$	$0.405_{\pm.003}$
TableDiffusion ($\epsilon = 1$)	$0.968_{\pm.002}$	$0.439_{\pm.003}$	$0.287_{\pm.001}$	$\mathbf{0.781}_{\pm.002}$	$2.503_{\pm.003}$	$0.489_{\pm.001}$

C.4 COMPARISON OF DIFFERENT PRIVACY METRICS

We compare the efficacy of different privacy metrics by conducting proof-of-concept experiments. Specifically, we consider the following popular privacy metrics:

- **DCR** (Zhao et al., 2021) measures the distance between the synthetic record and its closest real neighbor. The 5th percentile of the distance distribution represents the privacy score (a higher score means better privacy). We also utilize the worst-case (nearest distance) of DCR for comparison.

Table 11: Utility evaluation (*i.e.,* query error) of data synthesis on the first six datasets. A lower value means a smaller query error. The privacy budget ϵ of HP synthesizers is ∞ (the top part), and the budget for DP synthesizers is 1 (the bottom part). The best result of each category is in bold.

	Adult	Shoppers	Phishing	Magic	Faults	Bean
MST	$0.056_{\pm.018}$	$0.044_{\pm.005}$	$\mathbf{0.009_{\pm.001}}$	$0.035_{\pm.004}$	$0.041_{\pm.003}$	$0.036_{\pm.003}$
PrivSyn	$0.009_{\pm.002}$	$0.011_{\pm.006}$	$0.011_{\pm.002}$	$0.011_{\pm.002}$	$0.027_{\pm.004}$	$0.034_{\pm.002}$
TVAE	$0.025_{\pm.005}$	$0.034_{\pm.006}$	$0.018_{\pm.000}$	$0.014_{\pm.002}$	$0.026_{\pm.003}$	$0.019_{\pm.001}$
CTGAN	$0.015_{\pm.001}$	$0.017_{\pm.001}$	$0.051_{\pm.002}$	$0.037_{\pm.002}$	$0.047_{\pm.006}$	$0.030_{\pm.003}$
TabDDPM	$\mathbf{0.006_{\pm.001}}$	$\mathbf{0.008_{\pm.001}}$	$0.012_{\pm.001}$	$\mathbf{0.006_{\pm.001}}$		
GReaT	$0.014_{\pm.002}$	$0.014_{\pm.004}$	$0.049_{\pm.002}$	$0.029_{\pm.003}$	$0.028_{\pm.003}$	$0.011_{\pm.001}$
MST ($\epsilon = 1$)	$0.071_{\pm.014}$	$0.052_{\pm.017}$	$\mathbf{0.012_{\pm.001}}$	$0.036_{\pm.003}$	$\mathbf{0.045_{\pm.002}}$	$\mathbf{0.037_{\pm.002}}$
PrivSyn ($\epsilon = 1$)	$\mathbf{0.010_{\pm.001}}$	$0.027_{\pm.007}$	$0.016_{\pm.002}$	$\mathbf{0.025_{\pm.003}}$	$0.100_{\pm.006}$	$0.048_{\pm.004}$
PATE-GAN ($\epsilon = 1$)	$0.028_{\pm.004}$	$\mathbf{0.024_{\pm.002}}$	$0.117_{\pm.009}$	$0.058_{\pm.005}$	$0.088_{\pm.009}$	$0.191_{\pm.017}$
TableDiffusion ($\epsilon = 1$)	$0.057_{\pm.006}$	$0.054_{\pm.005}$	$0.071_{\pm.007}$	$0.074_{\pm.011}$	$0.119_{\pm.009}$	$0.052_{\pm.007}$

Table 12: Utility evaluation (*i.e.,* query error) of data synthesis on the last six datasets. A lower value means a smaller query error. The privacy budget ϵ of HP synthesizers is ∞ (the top part), and the budget for DP synthesizers is 1 (the bottom part). The best result of each category is in bold.

	Obesity	Robot	Abalone	News	Insurance	Wine
MST	$0.035_{\pm.007}$	$0.049_{\pm.005}$	$0.040_{\pm.004}$	$0.033_{\pm.005}$	$0.039_{\pm.004}$	$0.042_{\pm.005}$
PrivSyn	$0.027_{\pm.006}$	$0.029_{\pm.003}$	$0.014_{\pm.001}$	$\mathbf{0.010_{\pm.005}}$	$0.035_{\pm.007}$	$0.013_{\pm.002}$
TVAE	$0.027_{\pm.003}$	$0.020_{\pm.001}$	$0.016_{\pm.002}$	$0.030_{\pm.006}$	$0.050_{\pm.009}$	$0.028_{\pm.004}$
CTGAN	$0.037_{\pm.004}$	$0.033_{\pm.004}$	$0.036_{\pm.005}$	$0.018_{\pm.003}$	$0.055_{\pm.006}$	$0.016_{\pm.003}$
TabDDPM	$\mathbf{0.017_{\pm.003}}$	$\mathbf{0.008_{\pm.001}}$	$\mathbf{0.011_{\pm.003}}$	$0.017_{\pm.002}$	$\mathbf{0.027_{\pm.007}}$	$\mathbf{0.010_{\pm.001}}$
GReaT	$0.030_{\pm.003}$	$0.014_{\pm.001}$	$0.019_{\pm.003}$	-	$0.041_{\pm.007}$	$0.013_{\pm.001}$
MST ($\epsilon = 1$)	$0.043_{\pm.005}$	$\mathbf{0.050_{\pm.008}}$	$0.041_{\pm.003}$	$0.043_{\pm.004}$	$\mathbf{0.033_{\pm.004}}$	$\mathbf{0.045_{\pm.004}}$
PrivSyn ($\epsilon = 1$)	$0.060_{\pm.004}$	$0.095_{\pm.002}$	$0.051_{\pm.003}$	$\mathbf{0.027_{\pm.005}}$	$0.062_{\pm.007}$	$0.064_{\pm.008}$
PATE-GAN ($\epsilon = 1$)	$\mathbf{0.037_{\pm.001}}$	$0.150_{\pm.023}$	$0.223_{\pm.032}$	$0.029_{\pm.003}$	$0.138_{\pm.011}$	$0.158_{\pm.013}$
TableDiffusion ($\epsilon = 1$)	$0.108_{\pm.010}$	$0.071_{\pm.012}$	$0.085_{\pm.010}$	$0.050_{\pm.003}$	$0.195_{\pm.011}$	$0.048_{\pm.006}$

- **NNDR** (Zhao et al., 2021) calculates the distance ratio between the closest and second closest real neighbor to synthetic data. The 5th percentile (or nearest distance) determines the privacy score, where higher values indicate better privacy.
- **Groundhog** (Stadler et al., 2022) first calculates statistics (*e.g.,* histogram, correlations, *etc.*) from synthetic data as features. It then uses these features to train shadow models to form a binary classification for membership attack.
- **TAPAS** (Houssiau et al., 2022) leverages the counting queries as features and training a random forest classifier for membership attack.
- **DOMIAS** (van Breugel et al., 2023) is the state-of-the-art MIA for data synthesis, which utilizes the additional reference dataset to calibrate the density estimation of output distributions, and determines the membership via likelihood ratio hypothesis.

We randomly divide the dataset into two disjoint subsets: a training set D_t and a reference set D_r, where $|D_t| = |D_r|$ and they share the same data distribution. Each synthesis algorithm is trained on D_t and generates the synthetic data D, while the reference data D_r remains unused during the synthesis process. Different treatments are applied for different metrics: (i) For syntactic metrics (*i.e.,* DCR and NNDR), we compute the privacy score by treating either D_t or D_r as the real data. Unless a synthesizer provides very good privacy, it is expected that the privacy leakage on D_r is significantly smaller than that on D_t, since the synthetic data is generated using D_t and is independent of D_r. (ii) For MIAs and MDS, training dataset D_t and synthesis algorithm A are utilized to compute the privacy leakage. Table 13 presents the scores of different privacy metrics for various HP synthesizers on the Adult dataset. We have the following observations:

- *Syntactic metrics are not stable.* The standard deviations of syntactic metrics are quite large compared to their mean values. This instability is pronounced when using the nearest distance as the score, representing the worst-case assessment. This arises because syntactic metrics fail to account for the inherent randomness of the synthesis process.

Table 13: Comparison of privacy metrics for HP synthesizers on Adult dataset. D_t, D_r, and S are the training, reference, and synthetic data. A is the synthesis algorithm. Syntactic privacy metrics (DCR and NNDR) are highly unstable and are unable to provide meaningful privacy measures. MIAs (Groundhog, TAPAS and MODIAS) fail to distinguish the different levels of privacy risks of synthesizers.

Privacy Metric	Metric Input	MST ($\epsilon = \infty$)	PrivSyn ($\epsilon = \infty$)	TVAE	CTGAN	TabDDPM	GReaT
DCR (5th percentile distance)	D_t, S	$0.535_{\pm.121}$	$0.520_{\pm.182}$	$0.493_{\pm.116}$	$0.533_{\pm.103}$	$0.409_{\pm.181}$	$0.437_{\pm.122}$
	D_r, S	$0.527_{\pm.146}$	$0.531_{\pm.194}$	$0.487_{\pm.158}$	$0.479_{\pm.146}$	$0.446_{\pm.175}$	$0.502_{\pm.201}$
DCR (Nearest distance)	D_t, S	$0.102_{\pm.078}$	$0.110_{\pm.084}$	$0.124_{\pm.109}$	$0.105_{\pm.883}$	$0.081_{\pm.077}$	$0.082_{\pm.069}$
	D_r, S	$0.117_{\pm.096}$	$0.104_{\pm.083}$	$0.132_{\pm.105}$	$0.129_{\pm.094}$	$0.102_{\pm.080}$	$0.094_{\pm.067}$
NNDR (5th percentile distance)	D_t, S	$0.753_{\pm.226}$	$0.737_{\pm.204}$	$0.740_{\pm.218}$	$0.733_{\pm.135}$	$0.834_{\pm.129}$	$0.835_{\pm.105}$
	D_r, S	$0.750_{\pm.223}$	$0.703_{\pm.205}$	$0.714_{\pm.187}$	$0.802_{\pm.103}$	$0.881_{\pm.101}$	$0.795_{\pm.117}$
NNDR (Nearest distance)	D_t, S	$0.532_{\pm.274}$	$0.508_{\pm.315}$	$0.496_{\pm.229}$	$0.517_{\pm.284}$	$0.542_{\pm.247}$	$0.522_{\pm.203}$
	D_r, S	$0.530_{\pm.298}$	$0.498_{\pm.304}$	$0.504_{\pm.209}$	$0.539_{\pm.263}$	$0.547_{\pm.229}$	$0.512_{\pm.255}$
Groundhog (TPR@1%FPR)	D_t, A	$0.010_{\pm.002}$	$0.011_{\pm.001}$	$0.010_{\pm.003}$	$0.010_{\pm.002}$	$0.015_{\pm.003}$	$0.013_{\pm.002}$
TAPAS (TPR@1%FPR)	D_t, A	$0.012_{\pm.001}$	$0.013_{\pm.001}$	$0.011_{\pm.002}$	$0.009_{\pm.001}$	$0.030_{\pm.002}$	$0.020_{\pm.001}$
MODIAS (TPR@1%FPR)	D_t, A	$0.011_{\pm.001}$	$0.011_{\pm.001}$	$0.010_{\pm.002}$	$0.008_{\pm.001}$	$0.035_{\pm.002}$	$0.022_{\pm.001}$
MDS (ours)	D_t, A	$0.031_{\pm.001}$	$0.046_{\pm.002}$	$0.192_{\pm.003}$	$0.131_{\pm.002}$	$0.204_{\pm.001}$	$0.199_{\pm.001}$

- *Syntactic metrics are improper privacy measurements.* When using training data D_t or reference data D_r as real data to compute DCR and NNDR, the score differences are very small compared to their standard deviations. We note that for a good privacy metric, only when a synthesizer provides a very strong privacy guarantee, would we expect the two scores to be very similar. Since it is impossible that all HP synthesizers can provide such a high level of strong privacy guarantee, we assert this is because these syntactic metrics do not provide a good measure of privacy.
- *MIAs fail to distinguish different levels of privacy.* Experimental results show that the performance of MI attacks is relatively low for most synthesizers. We attribute the failure to the inherent randomness of synthesizers and synthetic datasets, which make it difficult to capture reliable signals to determine the membership.
- *MDS is a reliable privacy metric.* It is observed that the variance of MDS is very small, indicating its robustness for assessing data synthesizers. Additionally, MDS can also detect subtle differences in privacy leakage across various HP synthesizers.

C.5 IMPACT OF MODEL TUNING PHASE

Here, we present the results of various coefficient combinations during the tuning phase, as shown in Table 14. The results demonstrate that our tuning objective is highly robust to different coefficient assignments, with all combinations showing a significant improvement over the default settings. Additionally, we note that practitioners can adjust these coefficients based on specific application needs to enhance certain characteristics of the synthetic data. For example, one may want to increase α_2 to improve the quality of synthetic data for model selection tasks.

However, we also observed that no single coefficient configuration maximizes model performance across all three metrics. We believe this is because each metric emphasizes a different aspect of synthetic data quality. For instance, MLA is designed to maximize machine learning performance, specifically focusing on the correlation with label columns. In contrast, the fidelity metric evaluates the overall distributional similarity between real and synthetic data, which is independent of downstream tasks.

C.6 PERFORMANCE OF TABSYN

We include TabSyn (Zhang et al., 2024), the most recent HP synthesis algorithm for comparison. TabSyn first trains an autoencoder to capture inter-column relations and then employs a latent diffusion model for tabular data synthesis. We compare it with TabDDPM (Kotelnikov et al., 2023), as both algorithms are diffusion-based synthesizers, and TabDDPM has demonstrated impressive performance in our assessments.

Table 14: Average performance improvements (%) on fidelity and utility for TabDDPM when training with the proposed tuning objective in Equation (11).

			Fidelity ↑		Utility ↑	
α_1	α_2	α_3	D_{Train}	D_{Test}	MLA	Query Error
0	1/2	1/2	10.57	10.01	8.45	7.90
1/4	1/2	1/4	11.17	10.48	8.30	7.21
1/4	1/4	1/2	11.24	10.33	8.08	7.91
1/3	1/3	1/3	11.34	10.95	8.32	7.86
1/2	1/4	1/4	12.16	10.98	7.64	7.06
1/2	0	1/2	11.34	10.23	7.15	7.65
1/2	1/2	0	10.38	9.97	8.62	7.17

Figure 10: Performance behaviors of HP synthesizers on Magic dataset. "LR" denotes Linear Regression, "DT" is Decision Tree, and "RF" means Random Forest.

Both synthesizers are tuned using SynMeter and evaluated with our proposed metrics. As shown in Table 15, TabSyn and TabDDPM exhibit comparable performance across fidelity, privacy, and utility metrics, with neither emerging as a clear winner in any category. It is worth noting that Zhang et al. (2024) reported superior performance for TabSyn over TabDDPM. We attribute this to the possibility that TabDDPM was not optimally tuned in previous evaluations.

Table 15: Performance comparison between TabDDPM and TabSyn. The best result is in bold.

	Synthesizer	Adult	Shoppers	Phishing	Magic	Faults	Bean	Obesity	Robot	Abalone	News	Insurance	Wine
Fidelity (D_{train})	TabDDPM	**0.020**±.001	**0.022**±.001	**0.015**±.001	**0.011**±.003	**0.026**±.002	**0.015**±.002	**0.017**±.001	**0.015**±.002	**0.015**±.004	0.034±.001	0.028±.005	**0.011**±.000
	TabSyn	0.025±.003	0.030±.005	0.018±.003	0.012±.004	0.034±.003	0.033±.008	0.028±.003	0.045±.002	0.020±.005	**0.012**±.002	**0.026**±.003	0.021±.000
Fidelity (D_{test})	TabDDPM	**0.021**±.001	**0.031**±.001	**0.019**±.001	**0.012**±.002	0.058±.001	**0.016**±.003	**0.043**±.003	**0.028**±.004	0.034±.010	0.032±.001	0.070±.009	**0.017**±.001
	TabSyn	0.028±.002	0.035±.001	0.023±.001	0.014±.002	**0.057**±.012	0.033±.007	0.047±.006	**0.012**±.001	**0.020**±.006	**0.012**±.001	**0.067**±.008	0.028±.000
Privacy (MDS)	TabDDPM	0.204±.001	0.019±.002	0.082±.003	**0.015**±.001	0.092±.002	0.020±.003	0.333±.001	0.113±.002	0.120±.003	**0.008**±.001	0.027±.002	**0.075**±.003
	TabSyn	**0.202**±.001	**0.017**±.002	0.088±.002	0.029±.001	0.100±.003	0.021±.003	0.183±.002	0.062±.001	0.102±.002	0.026±.003	**0.019**±.002	0.124±.002
Utility (MLA)	TabDDPM	0.014±.001	0.006±.002	0.007±.003	0.007±.001	0.085±.002	0.003±.003	0.021±.001	0.011±.002	0.043±.003	0.047±.001	0.140±.002	0.047±.003
	TabSyn	0.014±.001	0.006±.002	0.025±.003	0.005±.001	0.118±.002	0.005±.001	0.075±.001	0.086±.002	0.017±.001	0.009±.003	0.033±.001	0.082±.002
Utility (QueryError)	TabDDPM	0.006±.001	0.008±.001	0.012±.001	0.006±.001	0.021±.002	0.006±.001	0.017±.003	0.008±.001	0.011±.003	0.017±.002	0.027±.007	0.010±.001
	TabSyn	0.005±.001	0.009±.001	0.016±.001	0.007±.001	0.018±.003	0.009±.001	0.020±.002	0.017±.003	0.009±.002	0.005±.001	0.027±.006	0.016±.001

D HYPERPARAMETER SEARCH SPACES

In this paper, we evaluate the following synthesizers: MST (McKenna et al., 2019), PrivSyn (Zhang et al., 2021), TVAE (Xu et al., 2019), CTGAN (Xu et al., 2019), TabDDPM (Kotelnikov et al., 2023), GReaT (Borisov et al., 2023), PATE-GAN (Jordon et al., 2018), and TableDiffusion (Truda, 2023). The hyperparameter search spaces of these synthesizers are shown in Table 16 to Table 23.

Table 16: MST (McKenna et al., 2019) hyperparameters search space.

Parameter	Distribution
Number of two-way marginals	$\text{Int}[10, 50]$
Number of three-way marginals	$\text{Int}[5, 20]$
Number of bins	$\text{Int}[5, 20]$
Maximum number of iterations	$\text{Int}[3000, 5000]$
Number of tuning trials	50

E DIFFERENTIALLY PRIVATE DATA SYNTHESIS

Definition 6 (Differential Privacy (Dwork, 2006)). *A randomized mechanism $\mathcal{M} : D \to \mathcal{R}$ is (ε, δ)-differentially private if for any two neighboring datasets $D, D' \in D$ and $S \subseteq \mathcal{R}$, it holds:*

$$\Pr[\mathcal{M}(D) \in S] \le e^{\varepsilon} \Pr[\mathcal{M}(D') \in S] + \delta \qquad (12)$$

Table 17: PrivSyn (Zhang et al., 2021) hyperparameters search space.

Parameter	Distribution
Number of bins	$\text{Int}[5, 20]$
Maximum number of iterations	$\text{Int}[10, 100]$
Number of tuning trials	50

Table 18: TVAE (Xu et al., 2019) hyperparameters search space.

Parameter	Distribution
Number of epochs	$\text{Int}[100, 500]$
Batch size	$\text{Int}[500, 5000]$
Loss factor	$\text{Float}[1, 5]$
Embedding dimension	$\text{Int}[128, 512]$
Compression dimension	$\text{Int}[128, 512]$
Decompression dimension	$\text{Int}[128, 512]$
L_2 regularization	$\text{LogUniform}[1e\text{-}6, 1e\text{-}3]$
Number of tuning trials	50

This definition requires that, on any two neighboring input databases, the difference in the output distributions of the randomized algorithm $\mathcal{M}$ is bounded by e^ϵ (*i.e.*, ϵ is the privacy budget), except with a small failure probability δ. This failure probability δ is usually assumed to be cryptographically small: in this paper, it is set to $\delta = 1 \cdot 10^{-9}$.

An important property of DP is given by the *post-processing* theorem, which lets us use the output of DP mechanisms freely without worrying about further privacy leakage.

Theorem 1 (Post-Processing). *Let $\mathcal{M} : D \rightarrow \mathcal{R}$ be an (ε, δ)-DP mechanism and $f : \mathcal{R} \rightarrow \mathcal{R}'$. Then $f \circ \mathcal{M} : D \rightarrow \mathcal{R}'$ also satisfies (ε, δ)-DP.*

Now we can use DP and the post-processing theorem to define differentially private data synthesis:

Definition 7 (Differentially Privacy Data Synthesis). *Given a dataset D sampled from some underlying distribution $\mathbb{D}$, we write $\mathsf{A} \leftarrow \mathcal{T}(D)$ to denote that the synthesizer A is learned by running the training algorithm $\mathcal{T}$ on the training set D. If the training algorithm $\mathcal{T}$ satisfies DP, then we call it differentially private data synthesis.*

That is, the probability that the adversary can infer if a given synthesizer A was fit on D or D', *i.e.*, $\mathsf{A} \sim \mathcal{T}(D)$ or $\mathsf{A} \sim \mathcal{T}(D')$, is bounded by the ϵ parameter. The guarantees of the overall data synthesis algorithm then follow from the post-processing theorem, as the synthetic dataset is simply sampled from the fitted synthesizer.

F   DISCUSSION OF EXISTING EVALUATION METRICS

F.1   EXISTING FIDELITY METRICS AND LIMITATIONS

Low-order Statistics. Marginals are the workhorses of statistical data analysis and well-established statistics for one(two)-way marginals have been used to assess the quality of synthetic data.

Distribution Measurements. Total Variation Distance (TVD) and Kolmogorov-Smirnov Test (KST) are used to measure the univariate distribution similarity for categorical and numerical attributes, respectively. The main problem with this approach is the lack of versatility. Each type of marginal requires a distinct statistical measure, which complicates the ability to perform a comprehensive comparison across various attribute types.

Correlation Statistics. Some researchers use correlation difference, *i.e.,* the difference of correlation scores on synthetic and real data, to measure the pairwise distribution similarity. Popular correlation

Table 19: CTGAN (Xu et al., 2019) hyperparameters search space.

Parameter	Distribution
Number of epochs	$\text{Int}[100, 500]$
Batch size	$\text{Int}[500, 5000]$
Embedding dimension	$\text{Int}[128, 512]$
Generator dimension	$\text{Int}[128, 512]$
Discriminator dimension	$\text{Int}[128, 512]$
Learning rate of generator	$\text{LogUniform}[1e\text{-}5, 1e\text{-}3]$
Learning rate of discriminator	$\text{LogUniform}[1e\text{-}5, 1e\text{-}3]$
Number of tuning trials	50

Table 20: TabDDPM (Kotelnikov et al., 2023) hyperparameters search space.

Parameter	Distribution
Number of layers	$\text{Int}[2, 8]$
Embedding dimension	$\text{Int}[128, 512]$
Number of diffusion timesteps	$\text{Int}[100, 10000]$
Number of training iterations	$\text{Int}[5000, 30000]$
Learning rate of discriminator	$\text{LogUniform}[1e\text{-}5, 3e\text{-}3]$
Number of tuning trials	50

statistics like Theil's uncertainty coefficient (Zhao et al., 2021), Pearson correlation (Zhang et al., 2024), and the correlation ratio (Kotelnikov et al., 2023) are applied for different types of two-way marginals (categorical, continuous, and mixed). In addition to the lack of universality, this approach also suffers from the problem that correlation scores capture only limited information about the data distribution. Two attributes may have the same correlation score both in the real data and in the synthetic data, yet their underlying distributions diverge significantly—a phenomenon known as the scale invariance of correlation statistics[16].

Likelihood Fitness. Xu et al. (2019) assume the input data are generated from some known probabilistic models (*e.g.,* Bayesian networks), thus the likelihood of synthetic data can be derived by fitting them to the priors. While likelihood fitness can naturally reflect the closeness of synthetic data to the assumed prior distribution, it is only feasible for data whose priors are known, which is inaccessible for most real-world complex datasets.

Evaluator-dependent Metrics. Probabilistic mean squared error (pMSE) (Snoke et al., 2018) employs a logistic regression discriminator to distinguish between synthetic and real data, using relative prediction confidence as the fidelity metric. The effectiveness of pMSE highly relies on the choice of auxiliary discriminator, which requires careful calibration to ensure meaningful comparisons across different datasets and synthesizers. Alaa et al. (2022) propose α-Precision and β-Recall to quantify how faithful the synthetic data is. Specifically, α-Precision defines fidelity as the proportion that the synthetic samples are covered by real data, and β-Recall evaluates the coverage of the synthetic data. However, previous studies (Zhang et al., 2024) find that α-Precision and β-Recall exhibit a predominantly negative correlation, and it's unclear which one should be used for fidelity evaluation.

F.2 EXISTING PRIVACY METRICS AND LIMITATIONS

Syntactic Privacy Metrics. Researchers propose to measure the empirical privacy risk of synthetic data by comparing an input dataset with the output dataset generated by the synthesizer, typically using the distances between data records. For example, the Distance to Closest Records (DCR) (Zhao et al., 2021) metric looks at the distribution of the distances from each synthetic data point to its nearest real one, and uses the 5th percentile (or the mean) of this distribution as the privacy score.

---

[16]https://en.wikipedia.org/wiki/Pearson_correlation_coefficient#Mathematical_properties

Table 21: GReaT (Borisov et al., 2023) hyperparameters search space.

Parameter	Distribution
Temperature	$\text{Float}[0.6, 0.9]$
Number of fine-tuning epochs	$\text{Int}[100, 300]$
Number of training iterations	$\text{Int}[5000, 30000]$
Batch size	$\text{Int}[8, 32]$
Number of tuning trials	20

Table 22: PATE-GAN (Jordon et al., 2018) hyperparameters search space.

Parameter	Distribution
Number of teachers	$\text{Int}[5, 20]$
Number of generator layers	$\text{Int}[1, 3]$
Number of discriminator layers	$\text{Int}[1, 3]$
Generator dimension	$\text{Int}[50, 200]$
Discriminator dimension	$\text{Int}[50, 200]$
Number of iterations	$\text{Int}[1000, 5000]$
Learning rate	$\text{LogUniform}[1e\text{-}5, 1e\text{-}3]$
Number of tuning trials	50

A small score is interpreted as indicating that the synthetic dataset is too close (similar) to real data, signaling a high risk of information leakage. There are other variations of DCR, *e.g.,* using the minimum distance instead of the 5th percentile, or using, for each record, the ratio of the closest distance and the second closest distance. However, these variations result in highly unstable measurements because of the inherent randomness of synthetic data. DCR and/or other similar metrics are widely used both in academia (Yale et al., 2019) and industry (AWS, 2022; Gretel, 2023), and have become the conventional privacy evaluation metrics for HP synthesizers (Jordon et al., 2021).

We note that metrics such as DCR are computed based on a pair of datasets: the input real dataset, and the output synthetic dataset. They do not depend on the synthesis algorithm at all. We call such metrics **syntactic**. We also note that when researchers were studying privacy properties of data anonymizers, syntactic privacy metrics such as k-anonymity (Sweeney, 2002), ℓ-diversity (Machanavajjhala et al., 2006), and t-closeness (Li et al., 2007) were introduced. Similarly, these metrics consider only the anonymized dataset (and not the algorithm generating the dataset) when measuring privacy. Over the last decade and a half, the community gradually recognized the limitations of such syntactic privacy metrics and adopted privacy notions such as differential privacy (Dwork, 2006), which defines privacy as a property of the data processing algorithm, instead of the property of a particular output.

Limitations of DCR. We use the DCR as an example to show the limitations of such syntactic privacy metrics as it's the most widely-used metric in the literature. First, DCR *overestimates* the privacy risks when data points are naturally clustered close together. As illustrated by discussions about differential privacy (Dwork & Roth, 2014; Li et al., 2016), leaking information regarding an individual should not be considered a privacy violation if the leakage can occur even if the individual's data is not used. Analogously, having some synthetic data very close to real ones does *not* mean worse privacy if this situation can occur even if each data point is removed. Consider, for example, a dataset that is a mixture of two Gaussians with small standard deviations. A good synthetic dataset is likely to follow the same distribution, and has many data points very close to the real ones. DCR interprets this closeness as a high privacy risk, overlooking the fact that the influence of any individual training instance on synthetic data is insignificant.

Second, DCR measures privacy loss using the 5th percentile (or mean) proximity to real data, which fails to bound the *worst-case* privacy leakage among all records. When measuring the privacy leakage across different individuals, one needs to ensure that the worst-case leakage is bounded, so that every individual's privacy is protected. It is unacceptable to use a mechanism that sacrifices the

Table 23: TableDiffusion (Truda, 2023) hyperparameters search space.

Parameter	Distribution
Number of layers	$\text{Int}[1, 6]$
Number of diffusion timesteps	$\text{Int}[3, 20]$
Number of epochs	$\text{Int}[5, 20]$
Batch size	$\text{Int}[128, 1024]$
Noise prediction	$\{\text{True, False}\}$
Learning rate	$\text{LogUniform}[1e\text{-}4, 1e\text{-}2]$
Number of tuning trials	50

privacy of some individuals even though the protection averaged over the population is good. This point is illustrated by the fact that the re-identification of one or a few individuals is commonly accepted as privacy breaches (Li et al., 2013).

Membership Inference Attack on Data Synthesis. MIA have been widely used as an empirical privacy metric in machine learning, which has been extensively studied on discriminative models (Shokri et al., 2017; Carlini et al., 2022). For generative models like diffusion models (Duan et al., 2023) and LLM (Duan et al., 2024), studies mainly focus both on the *white-box* setting (where an adversary has full access to the trained model) and on the *black-box* setting (where an adversary has exact knowledge of the specifications of the generative model). In the realm of data synthesis, Annamalai et al. (2024) claim that the *non-box* setting should be considered in practice: the adversary has access to the synthetic dataset but no information about the underlying generative model or even the specifications of the synthetic data generation algorithm. Stadler et al. (2022) perform the first non-box membership inference attack called Groundhog, which utilizes handcrafted features extracted from synthetic data distribution to train shadow models. While the attack against a small minority of records can be useful to measure theoretical risks, they may not be necessarily relevant in practice especially if the adversary does not have a precise way to recognize vulnerable outliers. DOMIAS (van Breugel et al., 2023) utilizes the additional reference dataset to calibrate the density estimation of output distributions and achieve state-of-the-art performance for data synthesis. However, as shown in Section 5.2, DOMIAS is still insufficient the distinguish nuances of privacy risks on all scenarios. As a result, current research on data synthesis rarely uses MIA for privacy evaluation (Qian et al., 2024).

F.3 LIMITATIONS OF MACHINE LEARNING EFFICACY

To show the instability issue of machine learning efficacy, we compare the performance of different machine learning models on the Adult dataset, as illustrated in Figure 10. We can see the performance of various data synthesizers fluctuates significantly across different machine learning models, and such variations in performance underscore the impact of the choice of evaluation models. For instance, while PrivSyn is ranked third when evaluated using linear regression, it falls to fifth when assessed with decision trees. Such variations indicate that machine learning efficacy fails to provide a stable and consistent measure for evaluating the utility of synthetic data in prediction tasks. Moreover, directly averaging the performance across all models also fails to capture nuanced performance differences. For instance, the mean performance of PrivSyn and TVAE appears nearly identical (0.8 vs. 0.802), whereas MLA more effectively differentiates their relative performance degradation (0.085 vs. 0.075), providing a more reliable assessment.

G DISCUSSION OF PROPOSED PRIVACY METRIC

Comparison with Syntactic Privacy Metrics. We use DCR as an example to show how the proposed membership disclosure score (MDS) addresses the drawbacks of syntactic metrics. First, MDS addresses DCR's over-estimating leakage issue by quantifying how much including each record x *changes* the distance between x and the closest synthetic data. If including x results in records much closer to x to be generated, then the disclosure risk is high. Conversely, if records close to x are generated regardless of whether x is included, then the disclosure risk for x is low.

Therefore, MDS follows a distinguishing game designed to mirror the DP definition, rather than relying on the density of data points. Additionally, MDS uses the maximum disclosure risk among all records, providing a stable *worst-case* privacy measurement.

Comparison with MIAs. Both membership disclosure score (MDS) and membership inference attacks (MIAs) measure privacy risks by assessing the influence of discrepancies observed in the synthesizer when trained with or without certain records. Additionally, MDS incorporates shadow model techniques (Shokri et al., 2017) to estimate the influence for all data records, which is the standard approach in MIAs. However, unlike MIAs, MDS directly assesses the privacy risks of training data without relying on the construction of the membership inference security game (Carlini et al., 2022). Consequently, MDS's privacy estimation does not depend on the effectiveness of one specific attack algorithm, offering greater flexibility in evaluating various types of data synthesizers.

Connections to Related Work. The definition of the proposed MDS aligns closely with concepts of memorization in neural networks (Feldman, 2020; Zhang et al., 2023) and the leave-one-out notion of stability in machine learning (Bousquet & Elisseeff, 2002). However, it diverges in three crucial ways: (i) We measure the worst-case discourse risk as the privacy metric, whereas other studies focus on the difference of individuals or average cases. (ii) Our work specifically addresses privacy concerns in data synthesis, as opposed to other studies that explore discriminative models like classification. (iii) Our approach emphasizes the discrepancy caused by the presence or absence of target data in training, in contrast to other works that highlight performance gains from adding samples to the training set.

Limitations of MDS. Although MDS provides a straightforward way to assess the privacy risk of data synthesis, it may not apply to all synthesizers. Pathological synthesizers exist for which MDS is inappropriate. One example of such a synthesizer is the one that simply adds the same large constant to each record in the input dataset. In datasets where the records are far apart, this results in a large MDS (meaning low disclosure risks) yet completely reveals the dataset, assuming that the mechanism of the synthesizer is known and deterministic. However, most (if not all) practical synthesizers are randomization algorithms, *i.e.,* they learn the (noise) distribution of the input records and then synthesize from the distribution. In summary, whenever syntactic privacy metric (like DCR) is used as a heuristic privacy metric, we believe that it is better to use MDS instead.

We also note that MDS focuses specifically on membership privacy (Li et al., 2013) and does not address all potential privacy risks associated with synthetic datasets. For instance, attribute inference attacks (Annamalai et al., 2024) and reconstruction attacks (Jayaraman & Evans, 2022) pose serious privacy threats to synthetic data, which MDS is not designed to capture.

In addition, MDS requires training multiple shadow models to estimate the disclosure risks. This can pose a challenge when assessing large-scale tabular synthesis models like GReaT, which involve fine-tuning entire LLMs. However, existing MIAs (Stadler et al., 2022; van Breugel et al., 2023) also rely on shadow modeling to compute privacy scores. Thus, MDS remains a practical and feasible solution for privacy assessment in most tabular datasets and synthesis algorithms.

H MISLEADING STATEMENTS FROM PREVIOUS WORK

We find that some statements in the literature may be misleading or even incorrect due to limitations of evaluation metrics or methodologies. We highlight some of them below:

- Extensive studies (Zhao et al., 2021; Lee et al., 2023; Zhang et al., 2024) use Distance to Closest Records (DCR) to evaluate the privacy of synthetic data and assert their models are safe. However, in this paper, we show that DCR fails to serve as an adequate measure of privacy. We also show that many recently introduced HP methods exhibit significant privacy risks, which are often ignored by the community.
- Kotelnikov et al. (2023) show that the machine learning performance on TabDDPM is even better than that on real data, which implies that synthetic data can be a perfect (even better) substitute for real data. However, this statement may be incorrect due to inadequate model tuning and improper data shuffling practices. Our evaluations show that even simple models, such as linear regression, can achieve better performance on real data than on high-quality synthetic data.

- Some studies (Kim et al., 2022; Jordon et al., 2018) prioritize machine learning efficacy as the primary (if not only) fidelity evaluation metric. This approach is problematic because data synthesis can be *biased* to label attributes, and a high machine learning efficacy score does not necessarily equate to high fidelity in synthetic data.