Informative Rewards and Generalization in Curriculum Learning

Abstract

Curriculum learning (CL) is central to human learning as much as reinforcement learning (RL) itself. However, CL agents trained using RL with function approximation produce limited generalization to later tasks in the curriculum. One contributing factor might be exploration itself. Exploration often induces the agent to visit task-irrelevant states, leading to training-induced non-stationarities. Thus, the value/policy networks utilize their limited capacity to fit targets for these irrelevant states. Consequently, this results in impaired generalization to later tasks. First, we propose to use an *online* distillation method to alleviate this problem in CL. We show that one can use a learned, informative reward function to minimize exploration and, consequently, non-stationarities during the distillation process. Second, we show that minimizing exploration improves capacity utilization as measured by feature rank. Finally, we illuminate the links between exploration, non-stationarity, capacity, and generalization in the CL setting. In conclusion, we see this as a crucial step toward improving the generalization of Deep RL methods in Curriculum learning.

1 Introduction

Deep Reinforcement Learning (DRL) has recently shown good results on various real-world problems (Akkaya et al., 2019; OpenAI, 2018; Silver et al., 2017; Tan et al., 2018; Becker-Ehmck et al., 2020). Many of these methods rely heavily on curricula (e.g., via self-play or automatic domain randomization). Considering the centrality of curricula to human learning (Skinner, 1958; Peterson, 2004; Dapena, 2002), it is natural to expect further advances from improved curriculum learning. Manually constructing a curriculum for each task is difficult, and automated curriculum learning methods have thus seen a resurgence in current research (Schmidhuber, 1991; Bengio et al., 2009; Schmidhuber, 2012; Portelas et al., 2020). However, these methods have still failed to reach their potential due to a host of reasons, including restricted task search spaces, limitations of exploration, and failure of models to continually learn and generalize to more complex tasks in an open-ended fashion (Wang et al., 2019; Jabri et al., 2019; Florensa et al., 2018).

Recent work suggests that the use of DRL in CL would produce limited generalization to downstream tasks not only due to non-stationarities inherent in DRL methods (Igl et al., 2021) but also the distribution shifts induced by the curricula themselves. Igl et al. (2021) identify policy updates, the consequent value updates and bootstrapping as three major sources of non-stationarity inherent to DRL. Kumar et al. (2020) show that bootstrapping, in particular, leads to a capacity loss in the neural networks used to approximate the policy or value. Lyle et al. (2022) ascribe this issue particularly to the non-stationarity in the target values as the policy improves during the learning process. These works show how an estimate of the rank of the feature matrix in the penultimate layer of the value network can be used to study this capacity loss phenomenon and attribute the impaired learning to

(a)	(b)

Figure 1: **Curriculum stages (a) and Effect of using informative rewards (b)**. The stages of the curriculum are depicted in (a). Plain curriculum learning involves only the first and last stage. To improve generalization, we propose to add an Inverse RL stage and an online distillation stage to help improve learned feature representations in the CL setting. We show that doing so improves results significantly in comparison with existing baselines to tackle non-stationarity and capacity issues in DRL. The figure on the right shows a comparison of results between stage 1 and stage 3. (The shaded regions depict the min-max envelope of 3 seeds) While the proximity baseline produces better generalization than other methods on the downstream task, we find that it has high variance in the distillation itself and only one seed performs as well as the other runs. However, as we expect, the proximity reward does minimize exploration, especially during the initial phases of the learning. We find that Jump-start RL, the proximity distillation and an engineered densely informative reward (based on manhattan distance) start showing returns within 20M samples.

the reduced discriminative power of the value networks. A lower feature rank would imply that the network cannot distinguish between as many states as it has the capacity for, i.e., the network suffers from state aliasing. However, we contend that this is not just because of the changing output values but also due to the diversity of inputs seen during exploration. This may sound counterintuitive since exploration is fundamental to learning. We argue that while exploration helps us learn what not to do, it is often unnecessary to model the failure modes given limited network capacity. In other words, in many cases it is simply sufficient to know something is wrong without knowing why. Furthermore, it could be detrimental if exploration induces the agent to alias states that are important for later tasks. Thus distillation methods can be used to relearn the task without spending too much capacity on known failure modes.

Exploration in RL is exponentially hard with respect to the task horizon. Lee et al. (2021) learn a proximity function from expert demonstrations in goal-reaching tasks and use the differences of the function as a notion of progress to produce a reward function. Progress towards the goal is immediately positively reinforced, making it a densely informative reward. They show that such a function easily generalizes to unseen states and is particularly useful for imitation learning in data-limited regimes. Building on this work, we find that such learned informative reward functions act as an inductive bias for RL agents in learning representations that generalize well to more complex downstream tasks in CL. Ideally, a maximally informative reward illuminates the optimal action for a state immediately, reducing the task horizon to 1. This reduces the task complexity to be quadratic in the horizon, reducing the number of states the agent visits while learning the task. This suggests a simple way to reduce non-stationarity by minimizing the states visited by the agent. Thus, we attempt to learn such an informative reward function from demonstrations. We then use this learned reward to train an agent with minimal non-stationarity. Fig. 1 gives a brief overview of our setting.

Finally to summarize our contributions, we show that online distillation via exploration minimizing rewards improves generalization to downstream tasks in a curriculum. Second, we find that this is related to improved utilization of capacity as measured by the rank of the features in the penultimate layer of the value network. Finally, we elucidate the links between exploration, non-stationarity, capacity and generalization in the curriculum learning setting.

2 Background

In the following section, we describe related work, explain how our method differs from prior work and provide a short summary of the work we build upon.

Proximity functions for generalizable imitation. Lee et al. (2021) improve generalization to unseen states in Imitation Learning (IL) by learning a proximity function. Essentially, they show that learning a temporal distance measure from expert demonstrations, helps the learned reward function to extract more information from the limited demonstrations, enabling it to generalize better to *unseen states*. Furthermore, they compare the IL performance in settings where the demonstrations are limited in diversity and show that their method outperforms other IL methods, including those that learn from observations and also demonstrations in some cases. In our work, we use their proximity function as an informative reward for online policy distillation in CL, to minimize exploration, and consequently non-stationarity. And we show that distillation using such informative rewards produces policies that generalize to *unseen environments* (particularly ones containing unseen objects and action consequences) as opposed to rewards that generalize to unseen states. We also use more complex procedurally generated grid worlds and adapt their method to work in our setting.

Non-stationarity and generalization. Generalization impairment due to non-stationarity has already been well studied in both Supervised Learning (Ash and Adams, 2019) and Reinforcement Learning (Igl et al., 2021; Fedus et al., 2020; Lyle et al., 2022; Steinparz et al., 2022). Igl et al. (2021) propose iterated network distillation as a solution to tackle any non-stationarity that arises in the context of DRL. However, using iterated distillation can erase information about failure modes that are learned by the policy during the early stages of training. This is because later distillation stages rely on replay-buffer data that may no longer contain the initial learning phases. While it is okay to lose the detailed modelling of the failure modes, we still need to know what not to do. Furthermore, naive distillation could force the network to overfit to the training task (By making strong assumptions given the limited data) and consequently impair generalization to more complex downstream tasks. Our generalization experiments suggest this is indeed the case. Hence, we propose to use an online distillation by learning an exploration-minimizing reward function that provides both positive and negative reinforcement, i.e. the agent learns both what to do and what to avoid.

Measuring network capacity using feature rank. Kumar et al. (2020) showed that it is possible to observe the adverse effects of bootstrapping by looking at the rank of the features in the penultimate layer of the value network. Lyle et al. (2022) use similar methods to show that this is due to distribution shifts (concept shifts in particular). First, using the ability to fit random targets, they show in the supervised setting that networks iteratively trained on randomly sampled conditional target label distributions (concept shifts) exhibit increasing loss with further iterations (negative forward transfer). However, when the network is sufficiently large (over-parametrized regime), they show that this effect is reversed, and positive forward transfer is observed. Furthermore, Lyle et al. (2022) shows that we are usually in the under-parametrized regime in DRL, and the networks exhibit the expected *negative* forward transfer to random targets. Second, they use a feature rank measure to show a positive correlation between training performance and feature rank and find that methods that *use a dense reward improve feature rank* and performance. While our results corroborate these findings, we further find that it is not merely the reward's density but rather the reward's informativeness that significantly improves the feature rank. Furthermore, we show that informative rewards reduce the number of irrelevant states visited by the agent, leading to better capacity utilization and feature rank. We also go on to demonstrate this impact in the curriculum learning setting, where we obtain significant improvement in generalization compared with methods that merely alleviate distribution shifts using distillation. Furthermore, we also use a slightly different version of feature rank that not only considers non-zero singular values but rather the uniformity of the singular values by using an entropy formula (Roy and Vetterli, 2007). Lyle et al. (2022) adapt a method from continual learning, which they call InFeR. InFeR adds multiple linear heads to the penultimate layer and trains these heads to predict the same values that the entire architecture does at the initialization point. This tends to behave as a regularization that prevents the rank from collapsing lower than the number of heads used. While this method does work as intended, as our results corroborate, they also show that preventing the feature rank from collapsing is insufficient for improving generalization to downstream tasks.

Minimizing exploration for bootstrapping RL. Jump-Start RL (JSRL) (Uchendu et al., 2022) is a recent method that proposes to accelerate RL by producing a starting state distribution very close to the goal state and then moving away from the goal during training. They mainly address the offline RL, followed by the online fine-tuning setting (i.e., the task doesn't change or increase in complexity). They show that using a guiding policy during the online fine-tuning in the limited data regime produces significantly better than other IL and RL baselines. However, they do not directly address the transfer problem in curriculum learning. We show that JSRL indeed transfers well because of its ability to reduce exploration, but it does not perform as well as exploration minimizing rewards.

Informative reward functions. RUDDER (Arjona-Medina et al., 2019; Patil et al., 2022; Dinu et al., 2022; Holzleitner et al., 2020; Widrich et al., 2021) learns to assign credit such that the expected sum of future rewards is zero under the current policy. RUDDER uses a lessons buffer to store trajectories from the current policy or an expert to learn a reward redistribution that satisfies *return equivalence*. Return equivalence ensures that the reward redistribution does not modify the task specified by the original MDP. In contrast, we relax this constraint but rely on the generalization ability of neural networks to capture the task definition from the expert trajectories. While we lose guarantees that the learned reward accurately represents the task defined by the original reward function, we argue that for most real-world tasks that matter to us, it is incredibly hard to define a reward function that accurately represents the desired behavior. Hence, we can justify relaxing this constraint, allowing us to redefine the reward solely to make learning easier/minimize states visited. Furthermore, in our setting, we consider only goal-reaching tasks in the curriculum and do not require return equivalence. Hence, our experiments use the proximity function as our informative reward function.

Thus, we conclude that the problem we address hasn't been dealt with in prior work and our results provide a novel insight into the problem of improving generalization in CL.

3 Methodology

In this section, first, we formalize the problem setting, then we discuss how we learn the informative reward, and finally, we describe the baselines used to substantiate our claims.

3.1 Preliminaries

Here, we formalize our problem setting. We define the MDP M as the six tuple $(S, A, R, P, \rho_0, \gamma)$, where S and A are the state and action spaces respectively. $R : S \times A \times S \to \mathbb{R}$ is a scalar reward function. $P(s_{t+1} \mid s_t, a_t)$ represents the transition probability distribution. ρ_0 is the initial state distribution and $\gamma \in [0, 1)$ is a discount factor commonly used to ensure that the discounted sum of rewards converges given an infinite horizon. For the experiments, however, we use a fixed horizon H. A policy $\pi_\theta(a_t \mid s_t)$ is the distribution of actions taken by an agent in each state s_t of the MDP, which is commonly approximated using a deep neural network parametrized by θ. The learned informative reward function $R_\phi^{inf}(s_t, a_t, s_{t+1})$, is parametrized by ϕ. It suffices to say that an informative reward is one that tells the agent what to do at every state immediately, i.e. moving temporally closer to the goal produces a positive reward without delay and negative otherwise. In other words, we expect that the reward captures the notion of *progress* towards the goal. Such a reward would ensure that visiting task-irrelevant states is immediately penalized.

We assume we have a minimal curriculum of two task MDPs M_1 and M_2. Both of them are assumed to be goal reaching tasks and M_2 is a more complicated version of M_1, in that:

    a) It contains objects that are not seen, and or necessitates actions that are not used in M_1.

    b) Only agents which solve M_1 are even capable of solving M_2 in a reasonable time frame.

Hence, our assumption ensures that M_2 as defined necessitates a CL method (barring the use of manually engineered rewards). So test for generalization, we train the agent first Furthermore, we consider complex enough environments to test the generalization capacity of the networks in a meaningful fashion. Ideally, we want the environment to be complex enough for it to possess diverse task-irrelevant information and to also induce the state aliasing effect. For simpler environments, we

169 find all baselines have very similar performances, making it difficult to analyse the phenomenon that
170 we are interested in. Hence, this concludes our discussion of how we frame the problem and why we
171 do so this way.

3.2 Learning informative rewards

173 Here, we describe how we can learn the informative reward we need to minimize exploration. Lee
174 et al. (2021) define the proximity function $f_\phi(s_t)$, as an exponential of the temporal distance $(T - t)$
175 to the goal $f_\phi(s_t) \sim \delta^{(T-t)}, \delta \in (0, 1)$, i.e. 1 if close to the goal and 0 if far away. This corresponds
176 to a value function when the goal has a reward 1, using a discount $\gamma = \delta$. Hence, this method is
177 similar to RUDDER's notion of informativeness, which also proposes taking a difference of the value
178 function. They take differences of such a function as a reward $R_\phi^{inf}(s_t, a_t, s_{t+1}) = f_\phi(s_{t+1}) - f_\phi(s_t)$.
179 Hence, their reward corresponds to the notion of *progress* towards the goal and helps us to minimize
180 exploration.

Additionally, Lee et al. (2021) use an ensemble of proximity functions and add an uncertainty penalty
to prevent the agent from visiting states where the proximity function variance is high.

$$R_\phi^{inf}(s_t, a_t, s_{t+1}) = f_\phi(s_{t+1}) - f_\phi(s_t) - \lambda.U_\phi(s_{t+1})$$

Furthermore, they continue training the proximity function to estimate 0 for the student's states since
the limited expert trajectories are not sufficient to learn such a function fully on states not visited by
the expert. Hence, they propose the following loss:

$$\mathcal{L}_\phi = \mathbb{E}_{\tau_i^e \sim \mathcal{D}^e, s_t \sim \tau_i^e} \left[f_\phi(s_t) - \delta^{(T_i - t)} \right]^2 + \mathbb{E}_{\tau \sim \pi_\theta, s_t \sim \tau} \left[f_\phi(s_t) \right]^2,$$

where $\mathcal{D}^e$ is the expert dataset and τ_i^e is a trajectory sampled from it. Unlike IL, we have access to
the goal termination conditions for both tasks, to make use of during the online distillation. Hence,
we modify this loss function to include successful samples from the student to expedite learning on
the procedurally generated environments that we use.

$$\mathcal{L}_\phi = \mathbb{E}_{\tau_i^e \sim \{\mathcal{D}^e, \mathcal{D}_s^{\pi_\theta}\}, s_t \sim \tau_i^e} \left[f_\phi(s_t) - \delta^{(T_i - t)} \right]^2 + \mathbb{E}_{\tau \sim \pi_\theta, s_t \sim \tau} \left[f_\phi(s_t) \right]^2,$$

181 where $\mathcal{D}_s^{\pi_\theta}$ is the set of successful trajectories sampled by the student π_θ. To conclude, we use
182 the proximity function as our informative reward function, since it captures this notion of *progress*
183 towards the goal. Any path that leads to failure modes or irrelevant states would produce an immediate
184 negative reward and consequently allow our agent to avoid visiting such states.

3.3 Baselines and Implementation

186 In this section we describe the baselines we chose, how we adapted them to the CL setting and finally
187 why we chose them. To evaluate the advantages of using an exploration-minimizing reward for
188 improving transfer in CL, we consider three diverse baselines apart from *Sparse*, which is vanilla CL
189 (because it uses a sparse reward to train on M_1). It involves simply training an RL agent on M_1 and
190 transferring it to M_2.

191 First, we have ITER (Igl et al., 2021) which is explicitly designed to handle non-stationarity in DRL
192 via iterated distillation. Their distillation process combines both offline loss terms with a behavioral
193 cloning (BC) term, where the BC terms are annealed to zero over the distillation process. We can see
194 this as offline distillation in contrast. The student is then hot-swapped with the teacher during training
195 on M_1 and thus at the end of training, we have an agent that has experienced less non-stationarity
196 overall. We then transfer this agent to the more complex tasks corresponding to M_2 to evaluate how
197 well it transfers. We specifically chose this baseline because it addresses non-stationarity without
198 addressing exploration. This should help us rule out that it is purely a problem of non-stationarity.

199 Second, we have InFeR, Initial Feature Regularization Lyle et al. (2022), where they adapt a method
200 based on Benjamin et al. (2018) designed to tackle catastrophic forgetting. They apply an l_2 penalty
201 on outputs from a set of auxiliary network heads such that the outputs do not change from their values
202 at the start of training. This restricts the network from the rank collapse phenomenon (Kumar et al.,
203 2020) (see Fig. 4) as the penultimate features are forced to have projections along each independently
204 initialized linear head layer. We performed a hyperparameter search to identify the combination of the

number of heads, an amplification term β and a loss weight α that achieves comparable performance on M_1. Then we transfer this agent to M_2 where we use plain PPO to evaluate the learned features. We chose this baseline because it addresses network capacity directly, without dealing with either non-stationarity or exploration. This helps us rule out whether it is purely a capacity problem.

Third, we consider the method proposed by Uchendu et al. (2022), which we described in Section 2. We modify their approach slightly. They consider two settings, one where the roll in is randomly sampled from $[0, H)$ and another where a roll in schedule is fixed a priori to decrease during the training. We start with a fixed roll in set to a constant $R = 10$ and then reduce the roll in for the next episode by 1 if the agent solves the previous episode or increase by 1 if it fails. And we restrict the roll in value to lie in $(0, R]$. Using this, we have a natural curriculum for the roll in which is decided by the performance of the agent directly. We thus train an agent in such a fashion on M_1 and then transfer the learned weights to a plain PPO agent on M_2. We chose this baseline because it directly attempts to minimize exploration, without dealing with capacity. But it does add additional non-stationarity to the task in the form of a moving initial state distribution. This should also help us understand to what extent the problem is a result of exploration.

Finally, for all baselines and experiments, we train using an actor-critic method, PPO, which uses function approximators to approximate both the value and the policy.

4 Experiments and results

In this section, we describe the three major experiments we perform and discuss the results thus obtained.

First, we construct challenging curricula using the `MiniGrid` environment (Chevalier-Boisvert et al., 2022). In our case, for the first task M_1, we consider the `MiniGrid-MultiRoom-N2-v0` environment (2-*room*), which consists of two procedurally generated rooms in a 13×13 grid with the agent in the first room and a green goal square in the second room. To reach the goal, the agent needs to learn to navigate to the door, open it, and then move to the goal square within a horizon of 40 steps. For M_2, we consider a set of 6 different, more difficult versions of the 2-room environment, as shown in Fig. 2. To make the tasks moderately challenging, for each of the environments, we set the horizon based on the number of rooms, with 20 steps per room. Hence, all the 2-room environments have a horizon for 40 and the 3-room environments have a horizon of 60. Thus, the first experiment involves one of standard curriculum learning. We use a particular method to train on M_1 and then evaluate generalization to M_2 by initializing the agent with the weights trained on M_1. We always train three seeds and transfer the best performing seed. Thus, our first experiment (see Fig. 3) tests how well each method above generalizes to the downstream task. Fig. 3 shows that online distillation with an exploration minimizing reward produces the best downstream generalization in comparison with all other methods. Furthermore, we see that methods which indirectly reduce exploration like JSRL come next. Methods which reduce non-stationarity like ITER come next. This suggests that reducing exploration directly is more useful in our setting, but there is some improvement to be gained from addressing non-stationarity directly as well. Finally, the vanilla CL baseline, sparse performs somewhat better than the InFeR baseline which regularizes a capacity measure (feature rank) showing that directly regularizing feature rank can have a detrimental effect for transfer as it would be easy for a network to memorize irrelevant information from the states.

Second, we count the number of times that the agents visit a randomly sampled square in 2-room environment while training using the respective methods (see Fig. 4(a)). As expected, methods which directly aim to minimize exploration do in fact reduce the diversity of states visited by the agent during the course of learning and other methods do not have a noticeable effect on exploration.

Third, we measure the feature rank using an entropy based measure Roy and Vetterli (2007) of the features in the penultimate layer using states sampled from a vanilla RL expert trained on 2-room. Here, we find that the feature rank regularization methods indeed work in avoiding the rank collapse phenomenon (see Fig. 4(b)). Furthermore, we find that an exploration minimizing reward (proximity) does prevent rank collapse to an extent and also leads to much higher feature rank after training. This is likely because it reduces state aliasing, as the reward is informative and helps distinguish between states. Furthermore, JSRL, which also indirectly minimizes exploration, has a very low feature rank because it sees only states from a very small distribution near the goal initially. But despite having additional non-stationarity in the form of a moving initial state distribution ρ_0, it still achieves a

high feature rank at the end of training, and we consequently see that methods which achieve higher
feature rank naturally tend to perform better than ones that don't on downstream tasks.

Figure 2: **Multiroom curriculum.** We first train the agent using various methods on 2-room and evaluate the generalization capability of the learned policy under those methods by transferring to 6 different, more complex settings that involve picking up/dropping keys, boxes, balls and avoiding lava. While merely adding a room can be seen as an extrapolation of the original 2-room setting, all the tasks involve objects *(lava, key, box, ball)* and or actions *(pick, avoid, drop)* that the agent has never seen or taken before and hence measure generalization in a challenging way. Furthermore, the environments are procedurally generated every episode making this a challenging test.

Figure 3: **Generalization to downstream tasks** Generalization results after training an agent on the plain 2-room environment M_1 using 5 different methods and transferring that agent to 6 complex downstream tasks with differing difficulties representing M_2 (see Fig. 2). We find that the proximity baseline, where we use a proximity function to minimize exploration generalizes well to even the most complex environments involving unseen objects such as lava, keys, balls and boxes. JSRL, which also minimizes exploration by rolling in with a guide policy performs slightly worse. ITER, which uses offline distillation (Combining BC and Offline RL terms) is the next best, showing that while minimizing exploration helps the best, minimizing non-stationarity is still useful. The vanilla CL baseline, sparse performs better than InFeR, which explicitly regularizes network capacity (feature rank). This shows that regularizing feature rank is not as powerful as directly minimizing exploration or non-stationarity. This makes intuitive sense, since a network may find it easy to buff up its feature rank by memorizing irrelevant state information. Finally random is a vanilla PPO baseline which fails to learn all but the first task showing that our choices of M_2, indeed require training on M_1 and are challenging choices to evaluate generalization in CL. (Note: the shaded area corresponds to min-max envelope of 3 seeds per run)

Figure 4: **State visitation counts (a) and Mean feature rank (b)** In (a), we show the number of times the agent visits a randomly sampled square on the grid during a particular episode. We see that using an informative reward significantly reduces the number of times the agent visits the chosen square, which is mostly not going to lie on the shortest path to the goal. Furthermore, we see that while JSRL minimizes this measure, it only succeeds in the initial stages due to the role in taking it towards the goal, which leads to episode termination lowering its chances of visiting our chosen square. Other methods do not reduce exploration. In (b), we show a measure of the feature rank in the penultimate layer of the value network for data collected from a vanilla RL expert in 2-room. We see that using an informative reward reduces the initial drop in the feature rank due to zero rewards in the sparse setting. Furthermore, we observe that the feature rank is improved not because the reward is dense (Dense Gaussian noise reward is worse than the sparse reward) but because the reward is informative of the task and reduces exploration. We also note the correlation between the higher variance in state visitation and the feature rank, especially for the sparse reward, and the trend seems to hold within the seeds as well. We can see the feature rank drops very low immediately for JSRL because the starting state distribution is very limited and as the rolling in is reduced, the feature rank catches up to its real value once the roll in fades away. And finally, we also see that the InFeR regularization directly prevents the feature rank from dropping too low.

5   Conclusion

Informative reward functions simplify the exploration problem, minimizing non-stationarity and improving generalization to downstream tasks. While they do also improve capacity utilization as measured by penultimate layer feature rank measures, we find that such measures, when directly optimized for, stop being good measures. To summarize our main experimental findings: First, we find that online distillation via exploration minimizing Inverse RL is effective in improving generalization to later tasks in the curriculum and, in particular, more effective than other methods that directly target non-stationarity or capacity measures. Second, we found that this is linked to improved capacity utilization by visualizing the penultimate layer feature ranks, showing that feature ranks are good capacity measures only when they are not optimized for improvement. Finally, we directly validated that the improvements in generalization do relate to exploration minimization by measuring state visitation counts.

Limitations and future outlook.   First, while our method improves upon other curriculum learning baselines, the curriculum still needs to be provided manually and we do not address the problem of curriculum generation. Furthermore, while capacity is efficiently utilized, we do not have a way of increasing capacity on the fly, apart from initializing the retraining process with a larger network. On the flip side, the online distillation using a learned reward function makes it agnostic to the RL algorithm used. This makes our method complementary to improvements in RL algorithms. Although we use complex visual environments with procedural generation, our analysis only covers goal reaching tasks in discrete environments. Furthermore, the proximity function is not an ideal way to minimize exploration for online distillation as it does not always produce students which perform better than the teachers, but for the purpose of our experiments (since we take the best performing seed out of 3), we found it sufficient. Identifying the ideal way to learn such exploration minimizing rewards is left for future work.

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