Self-Paced Contrastive Learning for Semi-supervised Medical Image Segmentation with Meta-labels

Abstract

Pre-training a recognition model with contrastive learning on a large dataset of unlabeled data has shown great potential to boost the performance of a downstream task, e.g., image classification. However, in domains such as medical imaging, collecting unlabeled data can be challenging and expensive. In this work, we propose to adapt contrastive learning to work with meta-label annotations, for improving the model's performance in medical image segmentation even when no additional unlabeled data is available. Meta-labels such as the location of a 2D slice in a 3D MRI scan or the type of device used, often come for free during the acquisition process. We use the meta-labels for pre-training the image encoder as well as to regularize a semi-supervised training, in which a reduced set of annotated data is used for training. Finally, to fully exploit the weak annotations, a self-paced learning approach is used to help the learning and discriminate useful labels from noise. Results on three different medical image segmentation datasets show that our approach: i) highly boosts the performance of a model trained on a few scans, ii) outperforms previous contrastive and semi-supervised approaches, and iii) reaches close to the performance of a model trained on the full data.

1 Introduction

Since the emergence of deep learning [24], there has been an active debate on the importance of pre-training neural networks. Precursor works [15] showed that pre-training a convolutional neural network with an unsupervised task (e.g., denoising autoencoders [47]) could help avoid local minima and lead to a better performance in the final supervised task. However, thanks to large datasets like ImageNet [11], the amount of labeled data for training has increased and, in such setting, pre-training often hinders performance [36]. This makes sense in light of recent studies showing, for instance, that symmetries in large networks induced many equivalent local minima [45, 33, 14]. Recently, contrastive learning has renewed interest in unsupervised pre-training [35]. Several works [7, 18, 9, 8, 58] have shown that pre-training with a contrastive loss can improve the performance of the subsequent supervised training, and perform even better than a network with supervised pre-training on ImageNet. While this has reopened the debate on the benefit of pre-training, it offers little help for domains where data is scarce such as medical imaging. In medical imaging, not only are labels expensive since they come from highly-trained experts such as radiologists, images are also hard to obtain due to the need for costly equipment (e.g., MRI or CT scanner) and privacy regulations.

Over the last years, a breadth of semi-supervised learning approaches have been proposed for medical image segmentation, including methods based on attention [30], adversarial learning [56], temporal ensembling [10, 52], co-training [38, 59], data augmentation [5, 57] and transformation consistency [4]. The common principle of these approaches is to add an unsupervised regularization loss using unlabeled images, which is optimized jointly with a standard supervised loss on a limited set of labeled images. Despite reducing significantly the amount of labeled data required for training, current semi-supervised learning methods still suffer from important drawbacks which impede their

use in various applications. Thus, a large number of unlabeled images is often necessary to properly learn the regularization prior. As mentioned before, this may be impossible in medical imaging scenarios where data is hard to obtain. Moreover, these methods also need a sufficient amount of labeled data, otherwise the training may collapse [34].

In a recent work, Chaitanya et al. [6] showed that unsupervised pre-training can be useful to learn a segmentation task with very few samples, by leveraging the meta information of medical images (e.g., the position of a 2D image in the 3D volume). While achieving impressive accuracy with as few as 2 volumes, this work has significant limitations. First, it relies on the strong assumption that the global or local representations of 2D images are similar if their locations within the volume or feature map are related. This assumption does not always hold in practice since volumes may not be well aligned, or due to the high variability of structures to segment. Second, it requires dividing the 2D images of a 3D volume in an arbitrary number of hard partitions that are contrasted, while the structure to segment typically varies gradually within the volume. Third, they do not exploit the full range of available meta data, for instance the patient ID or cycle phase of cardiac cine MRI, nor evaluate the benefit of combining several types of meta information in pre-training. Last, their approach leverages meta data only in pre-training, however this information could further boost performance if used while learning the final segmentation task, in a semi-supervised setting.

Our work addresses the limitations of current semi-supervised and self-supervised approaches for segmentation by proposing a novel self-paced contrastive learning method, which takes into account the noisiness of weak labels from meta data and exploits this data jointly with labeled images in a semi-supervised setting. The specific contributions of this paper are as follows:

- We propose, to our knowledge, the first self-paced strategy for contrastive learning which dynamically adapts the importance of individual samples in the contrastive loss. This helps the model deal with noisy weak labels that arise, for instance, from misaligned images or splitting a 3D volume in arbitrary partitions.
- We demonstrate the usefulness of a contrastive loss on meta-data for improving the performance of a final task, not only in pre-training but also as an additional loss in semi-supervised training.
- We show that combining multiple meta labels in our self-paced contrastive learning framework can improve performance on the final task, compared to using them independently. Our results also demonstrate the benefit of combining contrastive learning with temporal ensembling to further boost performance.

We empirically validate our contributions on three well-known medical imaging datasets, and show the proposed approach to outperform the contrastive learning method of [6] as well as several state-of-the-art semi-supervised learning methods for segmentation [48, 54, 56, 41, 39]. In the results, our approach obtains a performance close to fully supervised training with very few training scans.

2 Related work

We focus our presentation of previous works on two machine learning sub-fields that are most related to our current work: self-supervision, which includes contrastive learning, and self-paced learning.

Self-supervision and contrastive learning Self-supervision is a form of unsupervised learning where a pretext task is used to pre-train a model so to better perform a downstream task. Examples of pretext tasks are learning to sort a sequence [26, 51], predicting rotations [17, 16], solving a jigsaw puzzle [31] and many others [13, 55, 12, 44, 23]. Most of these methods can improve performance on the downstream task when labeled data for training is scarce. However, when a large and general enough dataset of labeled images like ImageNet [11] is available, a simple supervised pre-training can provide better results [20, 32]. Recently, unsupervised contrastive learning [7, 18, 8] was shown to boost performance even when learning a downstream task on a large dataset, and to improve over a model pre-trained in a supervised manner on a large dataset. This approach is based on the simple idea of enforcing similarity in the representation of two examples from the same class (positive pairs), and increase representation dissimilarity on pairs from different classes (negative pairs) [35, 46]. In images, positive pairs are typically defined as two transformed versions of the same image, for instance using a geometric or color transformation, while negative ones are any other pair of images [7–9, 18].

In a recent work, Khosla et al. [22] showed that, when combined with true semantic labels, a contrastive learning based pre-train and fine-tune pipeline performed surprisingly well, outperforming conventional training with cross-entropy in some cases. The work in [58] extended this idea to

pixel-level tasks like semantic segmentation, clustering the representations of pixels in an image according to their labels. Applying a similar strategy to medical image segmentation, Chaitanya et al. [6] leveraged meta-labels from 3D scans in a local and global contrastive learning framework to improve performance when training with limited data. However, positive and negative pairs in their contrastive loss are defined using noisy "weak" labels, arising for example from misaligned images or an arbitrary partitioning of 3D volumes, which may lead to learning sub-optimal representations. Moreover, their approach only exploits meta-labels in pre-training instead of considering them jointly with labeled images in a semi-supervised strategy. Our work extends this recent approach with a self-paced learning method that adapts the importance of positive pairs dynamically during training, and focuses the learning on the most reliable ones. In contrast to [6], we also exploit contrastive learning as regularization loss in semi-supervised training and show that further improvements can be achieved when combining it with a temporal ensembling strategy like Mean Teacher [10, 52].

Self-paced learning A sub-category of Curriculum Learning (CL) [1], Self-paced Learning (SPL) is inspired by the learning process of humans that gradually incorporates easy to hard samples in training [25]. The effectiveness of such strategy has been validated in various computer vision tasks [49, 21, 53]. Jiang et al. [21] proposed an SPL method considering both the difficulty and diversity of training examples, which outperformed conventional SPL methods that ignore diversity. Zhang et al. [53] incorporated SPL in a DNN fine-tuning process for object detection to cope with data ambiguity and guide the learning in complex scenarios. The usefulness of SPL when training with a limited budget or when the training data is corrupted by noise was also studied in recent work [50]. So far, the application of SPL to image segmentation remains limited. Wang et al. [49] presented an SPL method for lung nodule segmentation where the uncertainty of each sample prediction in the loss is controlled by the SPL regularizer. Related to our work, Wang et al. [29] proposed a margin preserving contrastive learning framework for domain adaptation that uses a self-paced strategy in self-training. Compared to this approach, which uses SPL *outside* the contrastive loss to select confident pseudo-labels for self-training, our method incorporates it *within* the loss via importance weights that are learned jointly with network parameters.

3 Proposed method

In this section, we present our self-paced contrastive learning approach for segmentation that leverages intrinsic meta information extracted from medical volumetric images. Our method effectively pre-trains a segmentation model with a self-paced variant of contrastive learning that is more robust to noisy annotations. The same approach is also used to further boost the segmentation accuracy in semi-supervised setting, where only very limited pixel-wised annotations are used. In the following subsections, we detail the formulation of the proposed approach.

3.1 Contrastive learning with meta labels

Given a batch of N images from a dataset $\mathcal{D}_u$ of unlabeled images, unsupervised contrastive learning approaches [7, 19, 35] aim at finding a feature extractor $f(\cdot)$ that gives similar representations for two augmented instances of the same image and differentiating those from two different images, regardless of their true classes. This can be achieved by creating an augmented set of samples indexed by $i \in I \equiv 1, \ldots, 2N$, with two augmented samples for each original image in the batch and then optimizing the following loss:

$$\mathcal{L}_{\text{unsupCon}} \; = \; \frac{1}{2N} \sum_{i=1}^{2N} - \log \frac{\exp\left(\mathbf{z}_i^{\mathsf{T}} \mathbf{z}_{j(i)}/\tau\right)}{\sum_{a \in \mathcal{A}(i)} \exp\left(\mathbf{z}_i^{\mathsf{T}} \mathbf{z}_a/\tau\right)} \tag{1}$$

In this loss, $\mathbf{z}_i = \frac{f(\mathbf{x}_i)}{\|f(\mathbf{x}_i)\|}$ is the L_2-normalized representation of an image $\mathbf{x}_i$ in the augmented batch (i.e., the *anchor*) and $j(i)$ is the index of the other augmented sample from the same original image as $\mathbf{x}_i$ (i.e., the *positive*). $\mathcal{A}(i) \equiv I \setminus i$ contains all indexes of the augmented set except i, and has a size of $2N-1$. Finally, τ is a small temperature factor that helps the gradient descent optimization by smoothing the landscape of the loss.

This approach works well when a large dataset of unlabeled images is available. However, as the number of available images is small in our case, we also leverage meta-labels from the structure of the data in our contrastive learning framework. Following [6], we consider the 2D slices of a given set of M 3D volumetric scans as our training data, and extract various meta labels for each 2D image,

e.g., patient ID, position of the slice in the volume, etc. More generally, we suppose that each image $\mathbf{x}_i$ has set of K meta labels denoted as $y_i^k \in \{1, \ldots, C_k\}$, where C_k is the number of class label for meta information $k \in \{1, \ldots, K\}$. The contrastive loss for the meta-label k is then defined as:

$$\mathcal{L}_{\text{con}}^k = \frac{1}{2N} \sum_{i=1}^{2N} \frac{1}{|\mathcal{P}^k(i)|} \sum_{j \in \mathcal{P}^k(i)} \underbrace{-\log \frac{\exp\left(\mathbf{z}_i^\mathsf{T} \mathbf{z}_j / \tau\right)}{\sum_{a \in \mathcal{A}(i)} \exp\left(\mathbf{z}_i^\mathsf{T} \mathbf{z}_a / \tau\right)}}_{\ell_{ij}} \tag{2}$$

where $\mathcal{P}^k(i) = \{j \in I \,|\, y_j^k = y_i^k\} \cup \{j(i)\}$ are the indexes of augmented samples with same label as $\mathbf{x}_i$ or coming from the same original image. By minimizing this loss, the feature extractor learns to group together representations with the same class and push away those from different ones.

In medical image segmentation, encoder-decoder based networks such as U-Net [43] and its variants are widely utilized thanks to their symmetric design and appealing performance on various dataset. Such network $F(\cdot)$ decomposes in two parts, an encoder $E(\cdot)$ that summarizes the global context of an input 2D slice into a low-dimensional representation, and a decoder $D(\cdot)$ that takes as input the representation and gradually recovers its spatial resolution using side information such as skip connections or pooling indexes. Previous work on contrastive learning showed that pre-training both the encoder and decoder separately helped the downstream segmentation task [6]. In preliminary experiments, we found that pre-training the decoder gave marginal improvements and thus focused our method on the encoder. Specifically, we consider the features of the encoder as a single vector $E(\mathbf{x}) \in \mathbb{R}^d$ and use a shallow non-linear projector $g(\cdot)$ called *head* to obtain the final normalized embedding $\mathbf{z}_i = \frac{g(E(\mathbf{x}_i))}{\|g(E(\mathbf{x}_i))\|}$.

3.2 Self-paced learning to mitigate noisy meta labels

The supervised contrastive loss of Equ. (2) can actually hurt the learning of representations in pre-training if the positive pairs are obtained with "weak" or noisy labels. For instance, if using patient ID as meta-label, we will force the encoder to cluster the representations of all 2D slices in a 3D volume, *including* those containing mainly background noise. Likewise, grouping together the slices in the same partition of two volumes hinders pre-training if the volumes are not fully aligned and/or their partitions cover different regions of the structure to segment.

To overcome this problem, we propose a self-paced strategy for contrastive learning which assigns an importance weight $w_{ij} \in [0, 1]$ to the specific loss of each positive pair (i, j), defined as l_{ij} in Equ. (3). A self-paced regularization term $R_\gamma(w_{ij})$, controlled by the learning pace parameter γ, is added to give a greater importance (i.e., larger w_{ij}) to pairs that are more confident (i.e., smaller ℓ_{ij}), and vice-versa. The learning pace γ is increased over training so that high-confidence pairs are considered in the beginning and then less-confident ones are gradually added as training progresses. We achieve this by defining the following self-paced contrastive loss optimized over both encoder parameters and importance weights:

$$\mathcal{L}_{\text{SP-con}}^k = \frac{1}{2N} \sum_{i=1}^{2N} \frac{1}{|\mathcal{P}^k(i)|} \sum_{j \in \mathcal{P}^k(i)} w_{ij}\, \ell_{ij} + R_\gamma(w_{ij}) \tag{3}$$

Following standard SPL approaches [21], we define the regularizer R_γ such that the weights are monotone decreasing with respect to the loss l_{ij} (i.e., harder examples are given less importance) and monotone increasing with respect to the learning pace (i.e., a larger γ increases the weights). In this work, we consider two regularizer functions, based on hard thresholding and linear imputation:

$$R_\gamma^{\text{hard}}(w_{ij}) = -\gamma\, w_{ij}\,; \qquad R_\gamma^{\text{linear}}(w_{ij}) = \gamma\big(\tfrac{1}{2} w_{ij}^2 - w_{ij}\big). \tag{4}$$

Optimization process We minimize the loss in Equ. (3) by optimizing alternatively with respect to the encoder parameters θ_E or importance weights w_{ij}, while keeping the other fixed. With fixed w_{ij}, we update θ_E via stochastic gradient descent where the gradient is given b

$$\nabla_{\theta_E} \mathcal{L}_{\text{SP-con}}^k = \frac{1}{2N} \sum_{i=1}^{2N} \frac{1}{|\mathcal{P}^k(i)|} \sum_{j \in \mathcal{P}^k(i)} w_{ij}\big(\nabla_{\theta_E} \ell_{ij}\big). \tag{5}$$

183 As can be seen, the gradient of low-confidence pairs (i, j) will be scaled down by their weight w_{ij},
184 thus these pairs will contribute less to the learning. Then, given a fixed θ_E we compute the optimal
185 weights w_{ij}^* by solving the following problem:

$$w_{ij}^* = \arg\min_{w_{ij} \in [0,1]} w_{ij}\, \ell_{ij} + R_\gamma(w_{ij}) \tag{6}$$

186 The following theorem gives the optimal solution for the hard and linear SPL regularization strategies.

187 **Theorem 1.** *Given the definitions of R_γ^{hard} and $R_\gamma^{\mathrm{linear}}$ in Equ. (4), the closed-form solutions to Equ.*
188 *(6) are given by*

$$w_{ij}^{\mathrm{hard}} = \left\{ \begin{array}{ll} 1, & \mathit{if}\ \ell_{ij} \leq \gamma \\ 0, & \mathit{else} \end{array} \right. ; \qquad w_{ij}^{\mathrm{linear}} = \max\left(1 - \frac{1}{\gamma}\ell_{ij},\, 0\right). \tag{7}$$

189 *Proof.* For the hard regularizer R_γ^{hard} the problem becomes

$$\min_{w_{ij} \in [0,1]} w_{ij}\, \ell_{ij} - \gamma\, w_{ij} = (\ell_{ij} - \gamma)w_{ij} \tag{8}$$

190 If $\ell_{ij} - \gamma \geq 0$, since we are minimizing, the optimum is obviously $w_{ij} = 0$. Else, if $\ell_{ij} - \gamma < 0$, the
191 minimum is achieved for $w_{ij} = 1$. Combining these two results gives the hard threshold of Equ. (7).

192 A similar approach is used for the linear regularizer R_γ^{hard}. In this case, the problem to solve is

$$\min_{w_{ij} \in [0,1]} w_{ij}\, \ell_{ij} + \gamma\left(\tfrac{1}{2}w_{ij}^2 - w_{ij}\right) = \tfrac{\gamma}{2}w_{ij}^2 + (\ell_{ij} - \gamma)\, w_{ij} \tag{9}$$

193 If $l_{ij} \geq \gamma$, since $w_{ij} \geq 0$, the minimum is reached for $w_{ij} = 0$. Else, if $\ell_{ij} < \gamma$, we find the optimum
194 by deriving the function w.r.t. w_{ij} and setting the result to zero, giving

$$w_{ij} = 1 - \frac{1}{\gamma}\ell_{ij}. \tag{10}$$

195 Since both γ and ℓ_{ij} are non-negative, we have that $w_{ij} \in [0, 1]$, hence it is a valid solution.
196 Considering both cases simultaneously, we therefore get the linear rule of Equ. (7). □

197 These update rules in Equ. (7) can be explained intuitively. For a given γ, the hard threshold rule only
198 considers confident pairs with $\ell_{ij} \geq \gamma$ and ignores the others. In contrast, the linear rule, weights
199 each pair proportionally to γ and the inverse of ℓ_{ij}, emphasizing more confident ones.

200 **Selecting the learning pace parameter** One of the main challenges in self-paced learning methods
201 is selecting the learning pace parameter γ. If γ is too small, all pairs will be ignored and there will be
202 no learning. Conversely, if γ is too large, all pairs will be considered regardless of their confidence,
203 which corresponds to having no self-paced learning. The following theorem provides insights on how
204 to set this parameter during training.

205 **Theorem 2.** *The loss ℓ_{ij} related to a given pair (i, j) in the SPL objective of Equ. (3) is bounded by*
206 $\log(|\mathcal{A}(i)| - 1) - 2/\tau \leq l_{ij} \leq \log(|\mathcal{A}(i)| - 1) + 2/\tau.$

207 *Proof.* We start by rewriting l_{ij} equivalently as

$$l_{ij} = \log \frac{\sum_{a \in \mathcal{A}(i)} \exp\left(\mathbf{z}_i^\mathsf{T} \mathbf{z}_a / \tau\right)}{\exp\left(\mathbf{z}_i^\mathsf{T} \mathbf{z}_j / \tau\right)} = \log\left(1 + \sum_{a \in \mathcal{A}(i) \setminus j} \frac{\exp\left(\mathbf{z}_i^\mathsf{T} \mathbf{z}_a / \tau\right)}{\exp\left(\mathbf{z}_i^\mathsf{T} \mathbf{z}_j / \tau\right)}\right) \tag{11}$$

208 Since the representation vectors $\mathbf{z}_i$ are L_2-normalized, their dot product is a cosine similarity falling
209 in the range $[-1, 1]$. To minimize l_{ij}, we then need to minimize the dot product in the numerator
210 inside the sum and maximize the one in the denominator, which corresponds to

$$l_{ij}^{\min} = \log\left(1 + (|\mathcal{A}(i)| - 1)\frac{e^{-1/\tau}}{e^{1/\tau}}\right) = \log\left(1 + (|\mathcal{A}(i)| - 1)e^{-2/\tau}\right) \approx \log\left(|\mathcal{A}(i)| - 1\right) - 2/\tau. \tag{12}$$

211 Similarly, we maximize l_{ij} by doing the opposite:

$$l_{ij}^{\max} = \log\left(1 + (|\mathcal{A}(i)| - 1)\frac{e^{1/\tau}}{e^{-1/\tau}}\right) = \log\left(1 + (|\mathcal{A}(i)| - 1)e^{2/\tau}\right) \approx \log\left(|\mathcal{A}(i)| - 1\right) + 2/\tau. \tag{13}$$

212 □

213 This theorem tell us that using $\gamma = l_{ij}^{\max}$ guarantees that all pairs are used in the loss, for both the
214 hard and the linear SPL regularizers. Additionally, when using the hard regularizer, R_γ^{hard}, $\gamma = l_{ij}^{\min}$
215 is the minimum learning pace so that at least one pair can be selected.

216 **The complete SPL loss** To exploit the information in all available meta-labels, our final loss
217 combines the contrastive losses $\mathcal{L}_{\mathrm{SP\text{-}con}}^k$ for meta-labels $k = 1, \ldots, K$:

$$\mathcal{L}_{\mathrm{SP\text{-}con}} = \sum_{k=1}^{K} \lambda_k \, \mathcal{L}_{\mathrm{SP\text{-}con}}^k \tag{14}$$

218 Here, $\lambda_k \geq 0$ is a coefficient controlling the relative importance of the kth meta-label in the final
219 loss, which is determined by grid search on a separate validation set.

3.3 Semi-supervised segmentation with contrastive learning

221 In previous work [6], contrastive learning has mostly been used for pre-training the model. Here,
222 we show that it can further boost results in a semi-supervised setting, where training with a limited
223 set of samples. In semi-supervised setting, in addition to the unlabeled images $\mathcal{D}_u$, a small amount
224 of pixelwise-annotated images $\mathcal{D}_l$ are also available. To incorporate the knowledge from meta
225 information in a semi-supervised setting, we modify our self-paced contrastive loss as

$$\mathcal{L}_{\mathrm{semi\text{-}sup}} = \mathcal{L}_{\mathrm{sup}} + \lambda_{\mathrm{reg}} \, \mathcal{L}_{\mathrm{reg}} + \lambda_{\mathrm{SP}} \, \mathcal{L}_{\mathrm{SP\text{-}con}}, \tag{15}$$

226 where $\mathcal{L}_{\mathrm{sup}}$ is the loss computed on labeled data (cross-entropy loss in our work), $\mathcal{L}_{\mathrm{reg}}$ is the
227 regularization loss normally used in semi-supervised approaches (in our experiments we use Mean
228 Teacher) and $\mathcal{L}_{\mathrm{SP\text{-}con}}$ is our self-paced contrastive loss. Last, λ_{reg} and λ_{sp} are weights balancing the
229 different loss terms which are determined by grid search.

4 Experimental setup

231 To assess the performance of the proposed self-paced contrastive learning, we carry out extensive
232 experiments on three clinically-relevant benchmark datasets with different experimental settings.
233 In this section we briefly describe the used datasets and some implementation details. For further
234 information please refer to the Suppl. Material.

4.1 Datasets

236 Three clinically-relevant benchmark datasets for medical image segmentation are used for our
237 experiments: the Automated Cardiac Diagnosis Challenge (ACDC) dataset [2], the Prostate MR
238 Image Segmentation 2012 Challenge (PROMISE12) dataset [27], and Multi-Modality Whole Heart
239 Segmentation Challenge (MMWHS) dataset [60]. These three datasets contain different anatomic
240 structures and present different acquisition resolutions. For the contrastive loss, we exploit meta-
241 labels on slice position and patient identity. Additionally, for ACDC, we consider the cardiac phase
242 (i.e., systole or diastole) as a third source of meta-data. For all datasets, we split images into training,
243 validation and test sets, which remain unchanged during all experiments. We train the model with
244 only a few scans of the training data as labeled data (the rest of the data is used without annotations as
245 in a semi-supervised setting) and report results in terms of 3D DSC metric [3] on the test set. Details
246 on training set split, data pre-processing, augmentation methods and evaluation metrics can be found
247 in the Suppl. Material.

248 For all dataset, we report the segmentation performance by varying the number of labeled scans
249 across experiments. For ACDC dataset, labeled scans ranges from 1 to 4, representing 0.5% to 2% of
250 all available data. For PROMISE12, we use 3 to 7 scans, representing 6% to 14% of the whole data.
251 For MMWHS, we use 1 and 2 annotated scans, corresponding to 10% - 20% of training data.

4.2 Network architecture and optimization parameters

253 We use `PyTorch` [37] as our training framework and employ the U-Net architecture [43] as our
254 segmentation network. Network parameters are optimized using stochastic gradient descent (SGD)
255 with a RAdam optimizer [28]. We provide the detailed training hyper-parameters in the Suppl.
256 Material. For the pre-training process, we obtain representations by projecting the encoder's output to

Figure 1: Self-paced strategy for γ. (a) Evolution of γ; (b) Expectation of w_{ij} over training epochs.

Table 1: Performance on ACDC for hard and linear SP strategy and different values of p.

| | | ACDC | | |
SP type	p	1 scan	2 scans	4 scans
Linear	$^1/_2$	**74.40%**	**80.34%**	**81.86%**
	1	72.06%	79.54%	81.03%
	2	59.72%	70.36%	80.05%
Hard	$^1/_2$	64.42%	78.26%	80.07%
	1	**72.01%**	**79.80%**	**80.24%**
	2	71.86%	72.14%	76.19%

a vector of size 256, using a simple MLP network with one hidden layer and LeaklyReLU activation function. Our proposed self-paced contrastive learning objective (Equ. (3)) involves a learning pace parameter γ set as

$$\gamma = \gamma_{\text{start}} + (\gamma_{\text{end}} - \gamma_{\text{start}}) \times \left(\frac{\texttt{cur\_epoch}}{\texttt{max\_epoch}}\right)^p \tag{16}$$

where γ_{start}, γ_{end} are hyper-parameters controlling the importance weights in the beginning and the end of training, and $\texttt{cur\_epoch}$, $\texttt{max\_epoch}$ are the current training epoch and the total number of training epochs respectively. p controls how fast γ increases during the optimization procedure.

5 Results

In this section, we first compare the hard and linear regularization strategy for SPL on ACDC. Then, we evaluate all components of our method in a comprehensive ablation study with a reduced set of training data on the three different datasets. Finally, we compare our method with the most promising approaches for semantic segmentation in medical imaging, with reduced training data.

5.1 Hard vs. linear self-paced regularization

Table 1 reports the validation score for the hard and linear SPL training with different p in Equ. (16), and different numbers of annotated scans on the ACDC dataset. We observe that both SPL strategies (R_γ^{hard} and R_γ^{linear}) effectively help to improve the performance, however the linear strategy always leads to a higher improvement. This is probably because the hard strategy only employs binary weights, i.e., $w_{ij} \in \{0,1\}$, whereas the linear strategy gradually increases w_{ij} and therefore provides a smoother optimization.

In Fig. 1 (a), we plot the value of γ over epochs for different values of p, and show in (b) the corresponding expectation of w_{ij} for all positive pairs. We observe that, for a large p, γ tends to be small for most of the training and mainly increases in the very end of the process, resulting in small w_{ij} for positive pairs. In contrast, when $p = ^1/_2$, we see a rapid increase of weights w_{ij} during training, which results in higher segmentation scores. This observation is inline with the findings from [42] and [40] on different tasks, where raising rapidly the self-paced rate in the first half of the training benefits the generalization performance. In the Suppl. Material, we also present a concrete evaluation of w_{ij} for three different scans during model optimization, corresponding to the four orange star markers in Fig. 1 (b). Since we found out that R_γ^{linear} strategy works better than R_γ^{hard}, we will use R_γ^{linear} for all following experiments.

5.2 Ablation study

Table 2 summarizes the 3D DSC performance on test set for the three dataset with very limited labeled data. At the top of the table, we report the number of labeled scans used and, for every result, we also give in parenthesis the standard deviation computed with 3 different random seeds for the initialization of the parameters. In the second and third columns of the table we provide the loss used for the pre-training, if any, and the loss for the downstream training.

Upper and lower bounds We present results for a *Baseline* which uses only the annotated scans with cross-entropy as standard supervised loss $\mathcal{L}_{\mathrm{sup}}$, and for *Full Supervision* where the same loss is used with all available data and associated annotations (175 for ACDC, 40 for Prostate and 10 for MMWHS). These two rows represent lower and upper bounds on the expected performance of the different variants of our approach.

Unsupervised contrastsive loss We evaluate the performance of pre-training the network encoder with *Unsupervised Contrastive* loss as in [7], where two augmented versions of the same image are considered as a positive pair. In all datasets, this loss improves over our baseline model, although the improvement is limited because the amount of unlabeled data available is still reduced compare to the settings of previous work on unsupervised contrastive learning [7, 18, 9, 8, 58]. We also add our self-paced learning strategy on top of this contrastive loss, and call this modified model *Unsupervised Contrastive + SP*. As meta-labels may be noisy, performance is increased in almost all experiments, especially when fewer labels are available.

Pre-training contrastive loss on meta-data We report the performance of a model pre-trained with a *Contrastive* loss on meta-labels. The meta labels are 3D slice location $\mathcal{L}_{\mathrm{con}}^1$, patient identity $\mathcal{L}_{\mathrm{con}}^2$ and cardiac phase $\mathcal{L}_{\mathrm{con}}^3$ (only for ACDC). We find that that slice position always gives the highest accuracy among all meta-labels, and largely outperforms the unsupervised contrastive loss. While all meta-labels increase performance compared to unsupervised contrastive loss, their combination leads to the best results in most cases.

Pre-training self-paced contrastive loss on meta-data Next, we evaluate the model pre-trained with a Self-Paced Contrastive loss on meta-labels (*SP-Con (pre-train)*). As with the unsupervised contrastive loss, the self-paced approach also successfully improves the segmentation quality compared to treating all positive pairs equally.

Semi-supervised We report the performance of a model without any pre-training, but using the unlabeled data during training as in a semi-supervised training with our proposed self-paced contrastive loss (*SP-Con (semi-sup)*). It can be seen that performance is inferior to Contrastive pre-training on meta-data, however the improvement is still quite relevant and, in most cases, superior to unsupervised pre-training.

Pre-trained and semi-supervised Our next subsection reports results for the combination of Self-Paced Contrastive learning used for both pre-training and semi-supervised training (*SP-Con (both)*). Although the loss is the same, its use during pre-training and as additional regularization in a semi-supervised setting brings additional improvements.

Pre-trained and semi-supervised with Mean Teacher We then evaluate the model using both pre-training and semi-supervised (as the previous) but with an additional Mean-Teacher for semi-supervision (*SP-Con (both) + Mean-Teacher*). By combining our approach with a simple Mean-Teacher method, our results on all datasets are further boosted, approaching the performance of fully supervised training but using a very low number of annotated scans. This is the model that we will use in the comparison with the state-of-the-art.

5.3 Comparison with the state-of-the-art

We compare our method with other approaches that aim to improve training with few annotated images/scans. Table 3 presents results in terms of 3D DSC score for approaches based on data augmentation [54], pre-training the weights on both encoder and decoder of the model [6] and various semi-supervised learning methods [48, 56, 41, 39]. For a more detailed explanation of the experimental setup of each method, see Suppl. Material. To have a fair comparison, for all methods, we used grid search on the validation set to tune the hyper-parameters. For most methods, the improvement with respect to the baseline trained with only the supervised loss is quite limited and varies depending on the dataset and the number of annotated scans used. For instance, *Adversarial training* performs quite well on the PROMISE12 dataset (scans in this dataset exhibit more variability in term of intensity contrast), but not so well on ACDC. Likewise, *Mean-Teacher* does not perform well for 1 and 2 annotated scans in ACDC but, when increasing the scans to 4, it outperforms most of the other methods. Global and local *Contrastive* loss using meta-data manages to obtain an excellent improvement on all datasets. However, our approach still yields substantial improvements with respect to that method. This is due to our proposed self-paced learning strategy, as well as the combined use of the contrastive loss for pre-training and semi-supervised learning.

Table 2: 3D DSC performance (and standard deviation) for different components and approaches on three medical image datasets with a few labelled scans.

Method	Pretrain	Train		ACDC			PROMISE12			MMWHS	
				1 scan	2 scans	4 scans	3 scans	5 scans	7 scans	1 scan	2 scans
Baseline	–	$\mathcal{L}_{\text{sup}}$		57.53 (1.18)	67.06 (0.68)	75.64 (0.15)	35.02 (2.59)	59.03 (1.25)	72.81 (1.08)	70.94 (0.84)	80.25 (0.38)
Full Supervision (*all labels*)	–	$\mathcal{L}_{\text{sup}}$			88.06 (0.20)			89.70 (0.51)			88.27 (1.23)
Unsup. Con.	$\mathcal{L}_{\text{con}}^{\text{unsup.}}$	$\mathcal{L}_{\text{sup}}$		65.14 (2.53)	72.88 (3.00)	76.56 (1.34)	38.74 (8.47)	60.99 (5.20)	75.28 (1.72)	74.12 (1.45)	80.57 (2.50)
Unsup. Con. + SP	$\mathcal{L}_{\text{SP}}^{\text{unsup.}}$	$\mathcal{L}_{\text{sup}}$		67.35 (1.98)	75.11 (0.92)	76.87 (0.84)	40.21 (6.63)	67.37 (0.99)	75.14 (0.50)	74.30 (1.81)	80.71 (0.83)
Contrastive	$\mathcal{L}_{\text{con}}^1$	$\mathcal{L}_{\text{sup}}$		70.57 (0.96)	78.59 (0.79)	79.60 (0.49)	57.44 (4.89)	75.21 (1.94)	80.02 (1.28)	76.53 (1.79)	83.05 (2.68)
	$\mathcal{L}_{\text{con}}^2$			63.63 (1.80)	73.30 (1.25)	76.83 (0.91)	55.50 (3.83)	69.95 (1.06)	78.93 (0.63)	74.71 (0.29)	82.41 (0.33)
	$\mathcal{L}_{\text{con}}^3$			64.52 (1.34)	76.81 (0.97)	77.66 (0.56)	–	–	–	–	–
SP-Con (*pre-train*)	$\mathcal{L}_{\text{SP}}^1$	$\mathcal{L}_{\text{sup}}$		73.99 (1.27)	81.01 (1.44)	82.83 (0.26)	58.81 (2.35)	75.28 (1.49)	80.71 (1.27)	77.20 (0.87)	82.87 (0.39)
	$\mathcal{L}_{\text{SP}}^2$			69.26 (1.69)	76.34 (0.60)	78.34 (0.42)	56.80 (1.59)	69.75 (0.47)	79.02 (0.18)	76.67 (0.48)	83.10 (1.51)
	$\mathcal{L}_{\text{SP}}^3$			65.18 (1.50)	79.05 (.026)	81.04 (0.16)	–	–	–	–	–
SP-Con (*semi-sup*)	–	$\mathcal{L}_{\text{sup}}+$ $\mathcal{L}_{\text{SP}}^1$		67.34 (0.74)	73.74 (0.51)	77.27 (0.12)	54.50 (1.53)	70.49 (1.33)	76.95 (0.81)	73.82 (0.68)	81.63 (0.39)
		$\mathcal{L}_{\text{SP}}^2$		60.82 (0.98)	68.06 (1.09)	77.10 (0.35)	41.67 (1.59)	61.04 (1.46)	75.98 (0.98)	73.43 (1.33)	78.08 (1.88)
		$\mathcal{L}_{\text{SP}}^3$		62.52 (0.46)	68.39 (0.26)	77.24 (0.17)	–	–	–	–	–
SP-Con (*both*)	$\mathcal{L}_{\text{SP}}^1$	$\mathcal{L}_{\text{sup}}+$ $\mathcal{L}_{\text{SP}}^1$		75.66 (1.94)	80.37 (0.36)	82.35 (0.58)	68.79 (2.63)	77.38 (1.90)	80.55 (0.75)	76.58 (1.00)	82.69 (0.39)
	$\mathcal{L}_{\text{SP}}^2$	$\mathcal{L}_{\text{SP}}^2$		70.47 (0.93)	76.58 (0.45)	78.37 (0.22)	56.68 (2.64)	72.21 (1.32)	77.28 (1.86)	75.33 (0.62)	82.39 (0.27)
	$\mathcal{L}_{\text{SP}}^3$	$\mathcal{L}_{\text{SP}}^3$		70.08 (0.96)	78.70 (0.51)	80.19 (0.28)	–	–	–	–	–
SP-Con (*both*) + Mean Teacher	$\mathcal{L}_{\text{SP}}^1$	$\mathcal{L}_{\text{sup}}$ $\mathcal{L}_{\text{MT}}+$ $\mathcal{L}_{\text{SP}}^1$		78.76 (0.26)	82.14 (0.19)	84.42 (0.18)	74.06 (1.13)	82.50 (0.91)	84.14 (0.35)	78.82 (0.34)	84.90 (0.58)
	$\mathcal{L}_{\text{SP}}^2$	$\mathcal{L}_{\text{SP}}^2$		75.30 (0.68)	79.67 (0.26)	82.65 (0.32)	61.39 (1.33)	77.74 (1.07)	83.92 (0.39)	75.94 (0.90)	84.57 (0.61)
	$\mathcal{L}_{\text{SP}}^3$	$\mathcal{L}_{\text{SP}}^3$		73.94 (0.54)	81.29 (0.09)	83.21 (0.05)	–	–	–	–	–
	$\mathcal{L}_{\text{SP}}^{1-3}$	$\mathcal{L}_{\text{SP}}^{1-3}$		79.80 (0.33)	83.20 (0.25)	84.84 (0.15)	74.47 (0.36)	83.78 (0.30)	84.52 (0.17)	78.97 (0.52)	84.87 (0.11)

Table 3: 3D DSC performance (and standard deviation) of our method and other approaches on three medical image datasets with few labelled scans. Bold red-colored values are the best performing methods, underlined blue-colored ones correspond to the second best performing method.

Method	ACDC			PROMISE12			MMWHS	
	1 scan	2 scans	4 scans	3 scans	5 scans	7 scans	1 scan	2 scans
Entropy Min. [48]	60.47 (1.03)	69.81 (0.99)	76.19 (1.21)	53.47 (5.70)	65.66 (0.42)	73.52 (2.71)	72.28 (0.58)	78.39 (1.54)
Mix-up [54]	60.87 (1.28)	67.45 (1.04)	76.18 (0.49)	41.38 (2.80)	64.55 (1.93)	73.56 (0.61)	71.50 (0.54)	80.12 (0.84)
Adv. Training [56]	63.05 (0.80)	70.68 (0.27)	75.89 (0.94)	_61.58_ (2.10)	71.00 (1.20)	_81.05_ (1.34)	73.47 (1.42)	80.40 (0.93)
Mean Teacher [41]	62.85 (0.67)	72.84 (0.22)	79.12 (0.08)	52.96 (1.97)	68.38 (2.04)	77.37 (0.87)	72.36 (1.35)	81.01 (0.57)
Discrete MI [39]	69.27 (1.41)	77.74 (0.42)	80.06 (0.24)	47.77 (3.58)	68.29 (2.35)	77.63 (1.13)	72.38 (1.04)	82.45 (1.36)
Contrastive [6]	_70.05_ (2.66)	_79.11_ (2.02)	_81.25_ (2.15)	61.15 (2.95)	_74.62_ (1.69)	80.08 (1.39)	_76.45_ (0.62)	_82.93_ (0.42)
Our Method	**79.80** (0.33)	**83.20** (0.25)	**84.84** (0.15)	**74.47** (0.36)	**83.78** (0.30)	**84.52** (0.17)	**78.97** (0.52)	**84.87** (0.11)

6 Discussion and conclusion

In this paper, we presented a technique based on contrastive loss with meta-labels that can highly improve the performance of a segmentation model for medical images when unlabeled data is scarce. It was shown that, with a reduced amount of unlabeled images, unsupervised contrastive loss is not very effective. Instead, in the context of medical images, additional meta-data is freely available and, if properly used, can greatly boost performance. We have presented results on three well known datasets in the field, and have shown that the accuracy of contrastive loss with meta-labels can be boosted by the use of self-paced learning. Our self-paced contrastive learning method can be used during pre-training, as well as a regularization during training, and the combination of the two further boosts results. Finally, we have compared our approach with the state-of-the-art in semi-supervised learning and have shown that the simple combination of our approach with multiple meta-data and a simple semi-supervised approach as Mean Teacher is more effective than previous approaches. While using a single scan, our method can approach fully supervised training.

Social impact and limitations The proposed method can have an effective and practical impact in terms of medical imaging analysis in hospitals and health centers. As shown in our experiments, it produces an accurate medical image segmentation with a very reduced set of annotated data. This has the potential of helping radiologists and other clinicians using medical images, which can contribute to a better diagnosis and reduced costs. While our empirical evaluation has shown excellent results with a very limited data, using fewer annotated images also increases chances of over-fitting some outliers in the data and produce erroneous or misleading results. Further studies about the reliability of medical image segmentation with reduced images is therefore recommended.

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