LEARNING TO CLUSTER IN ORDER TO TRANSFER ACROSS DOMAINS AND TASKS

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ABSTRACT

This paper introduces a novel method to perform transfer learning across domains and tasks, formulating it as a problem of learning to cluster. The key insight is that, in addition to features, we can transfer similarity information and this is sufficient to learn a similarity function and clustering network to perform both domain adaptation and cross-task transfer learning. We begin by reducing categorical information to pair-wise constraints, which only considers whether two instances belong to the same class or not (pairwise semantic similarity). This similarity is category-agnostic and can be learned from data in the source domain using a similarity network. We then present two novel approaches for performing transfer learning using this similarity function. First, for unsupervised domain adaptation, we design a new loss function to regularize classification with a constrained clustering loss, hence learning a clustering network with the transferred similari ty metric generating the training inputs. Second, for cross-task learning (i.e., unsupervised clustering with unseen categories), we propose a framework to reconstruct and estimate the number of semantic clusters, again using the clustering network. Since the similarity network is noisy, the key is to use a robust clustering algorithm, and we show that our formulation is more robust than the alternative constrained and unconstrained clustering approaches. Using this method, we first show state of the art results for the challenge cross-task problem, applied on Omniglot and Imagenet. Our results show that we can reconstruct semantic clusters with high accuracy, compared to other constrained and unconstrained clustering approaches. We then evaluate the performance of cross-domain transfer using images from the Office-31 and SVHN-MNIST tasks and present top accuracy on both datasets. This is despite the fact that we perform no explicit domain adaptation, and if we combine our method with a domain adaptation loss we show further improvements.

1 INTRODUCTION

Supervised learning has made significant strides in the past decade, with substantial advancements arising from the use of deep neural networks. However, a large part of this success has come from the existence of extensive labeled datasets. In many situations, it is not practical to obtain such data due to the amount of effort required or when the task or data distributions change dynamically. To deal with these situations, the fields of transfer learning and domain adaptation have explored how to transfer learned knowledge across tasks or domains. Plenty of approaches have focused on cases where the distributions of the features and labels have changed, but the task is the same (e.g., classification across the same categories). Cross-task transfer learning strategies, on the other hand, have been widely adopted especially in the computer vision community where features learned by a deep neural network on a large classification task have been applied to a wide variety of other tasks (Donahue et al., 2014).

Most of the prior cross-task transfer learning works, however, require labeled target data to learn classifiers for the new task. If labels of the target data are absent, there is little choice other than to apply unsupervised approaches such as clustering on the target data with pre-trained feature representations. In this paper, we focus on the question of what can be transferred (besides features) to support both cross-domain and cross-task transfer learning. We address it with a learned similarity function as the most basic component of clustering. Then clustering can be realized using neural

networks combined with the similarity function, which can be successfully used to achieve both cross-task and cross-domain transfer.

The key idea is to formulate the clustering objective to use a learnable (and transferable) term, which in our proposed work is a *similarity prediction function*. Our proposed objective function can be easily combined with deep neural networks and optimized end-to-end. The features and clustering are optimized jointly, hence taking advantage of such side information in a robust way. . Using this method, we show that unsupervised learning can benefit from learning performed on a distinct task, and demonstrate the flexibility of further combining it with a classification loss and domain discrepancy loss.

In summary, we make several contributions. First, we propose to use predictive pairwise similarity as the knowledge that is transferred and formulate a learnable objective function to utilize the pairwise information in a fashion similar to constrained clustering. We then provide the methodologies to deploy the objective function in both cross-task and cross-domain scenarios with deep neural networks. The experimental results for cross-task learning on Omniglot and ImageNet show that we can achieve state of the art clustering results with predicted similarities. On the standard domain adaptation benchmark Office-31 dataset, we demonstrate improvements over state-of-art even when not performing any explicit domain adaptation, and further improvements if we do. Finally, on another domain adaptation task, SVHN-to-MNIST, our approach using Omniglot as the auxiliary dataset achieves top performance with large margin .

2 Related Work

Transfer Learning: Transfer learning aims to leverage the knowledge from the source domain to help to learn in the target domain, while only focus on the performance on the target domain. The type of transferred knowledge includes training instances, features, model parameters and relational knowledge (Pan & Yang, 2010). The pairwise similarity is the meta-knowledge we propose to transfer, which falls in between the last two types. The similarity prediction function is a neural network with learned parameters, while the output is the most simplified form of relational knowledge, i.e., only considering semantic similarity.

Cross-task Transfer Learning: The feature learned with ImageNet classification (Russakovsky et al., 2015) had boosted the performance of varied vision tasks in a supervised setting. For example, new classification task (Donahue et al., 2014; Yosinski et al., 2014), object detection (Girshick et al., 2014), semantic segmentation (Long et al., 2015a), and image captioning (Vinyals et al., 2015). The Translated Learning (Dai et al., 2009) has an unsupervised setting similar to ours, but it also focuses on transferring the feature. Our work explores another choice of information for transferring in an unsupervised setting.

Cross-domain Transfer Learning: It also called domain adaptation (Pan & Yang, 2010). Recently there is a large body of works address the domain shifting between image datasets by minimizing domain discrepancy (Tzeng et al., 2014; Long et al., 2015b; Ganin et al., 2016; Sun et al., 2016; Long et al., 2016; Sener et al., 2016b; Carlucci et al., 2017; Long et al., 2017; Zellinger et al., 2017). We addressed the problem in a complementary aspect that transfer extra information from the auxiliary dataset.

Constrained Clustering: Constrained clustering can be categorized by how the algorithm utilizes the pairwise information. The first type is using the constraints to learn the metric. For example, DML (Xing et al., 2003), ITML (Davis et al., 2007), SKMS (Anand et al., 2014), SKKm (Anand et al., 2014; Amid et al., 2016), and SKLR (Amid et al., 2016). This type of approach closely relate to metric learning and need a clustering algorithm like K-means in the second stage for doing actual clustering. The second type involves the constraints to formulate the clustering loss. For example, CSP (Wang et al., 2014) and COSC (Rangapuram & Hein, 2012). The third type use constraints for both metric learning and clustering objective, like MPCKMeans (Bilenko et al., 2004) and CECM (Antoine et al., 2012). The fourth group doesn't use constraints at all. The generic clustering algorithms like K-means (MacQueen et al., 1967), LCS (Chen & Cai, 2011), and LPNMF (Cai et al., 2009) are all belonged to this category. In above we only listed a small fraction of approaches because of the long list of works associated. *Our proposed clustering strategy belongs to the third type.* The constrained clustering methods above are initially applied to the semi-supervised setting that the ground-truth constraints

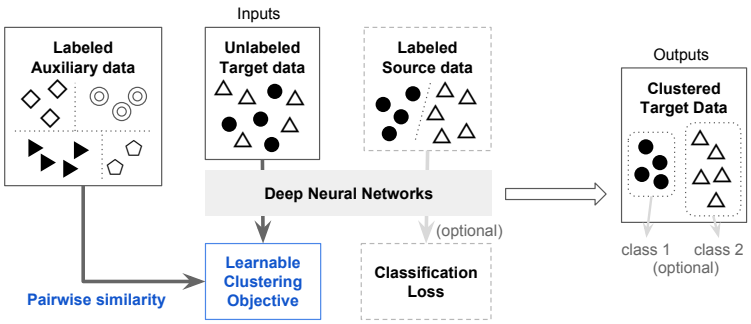

Figure 1: Overview of the transferring scheme with learnable clustering objective (LCO). The LCO and the pairwise similarity are the two key components of our approach and described in section 4. The dashed rectangles and light gray arrows are only available in cross-domain transferring. Details are described in section 3

are sparsely available. In our unsupervised setting, the ground-truth is unavailable but predicted constraints could be densely obtained. In our work, we include all the four types of algorithms in our transferring scheme for evaluation.

3 THE TRANSFER LEARNING TASKS

To define the transfer learning problem addressed in this work, we follow the notations used by Pan & Yang (2010). The goal is to transfer knowledge from source data $S = (X_S, Y_S)$, where X_S is the set of data instances and Y_S is the corresponding categorical labels, to a target data noted as $T = (X_T, Y_T)$. The learning is unsupervised since Y_T is unknown. The scenario is divided into two cases. One is $\{Y_T\} \neq \{Y_S\}$, which means the set of categories are not the same and hence the transferring is across tasks. The second case is $\{Y_T\} = \{Y_S\}$, but with a domain shift. In another word, the marginal probability distributions of the input data are different, i.e. $P(X_T) \neq P(X_S)$. The latter is a cross-domain learning problem or called transductive learning. The domain adaptation approaches which have gained significant attention recently belong to the second scenario.

In order to align with common benchmarks for evaluating transfer learning performance, we further use the notion of an auxiliary dataset and split the source data into $S = S' \cup A$. $S' = (X'_S, Y'_S)$ is only presented in the cross-domain transfer scheme and has $\{Y'_S\} = \{Y_T\}$. The $A = (X_A, Y_A)$ is the auxiliary dataset which has a large amount of labeled data and potentially categories as well, and may or may not contain the categories of Y_T. For the cross task scenario, only A and unlabeled T are included, while cross-domain transfer involves A, S', and T. In the following sections we use the above notations and describe the two transfer learning tasks in detail. Figure 1 illustrates how our approach related to both tasks.

Transfer across tasks: If the target task has different categories, we cannot directly transfer the classifier from source to target, and there is no labeled target data to use for fine-tuning transferred features. Here we propose to first reduce the categorization problem to a surrogate same-task problem. We can directly apply transductive transfer learning (Pan & Yang, 2010) to the transformed task. The cluster structure in the target data are then reconstructed using the predictions in the transformed task. See figure 8 in the appendix for an illustration.

The source involves a labeled auxiliary dataset A and an unlabeled target dataset T. Y_T is the target that must be inferred. In this scenario the set of categories $\{Y_A\} \neq \{Y_T\}$, and Y_T is unknown. We first transform the problem of categorization into a pairwise similarity prediction problem. In other words, we specify a transformation function R such that $R(A) = (X_A^R, Y^R)$, and $X_A^R = \{(x_{A,i}, x_{A,j})\}_{\forall i,j}$ contains all pairs of data, where $\{Y^R\} = \{similar, dissimilar\}$. The transformation on the labeled auxiliary data is straightforward. It will be $similar$ if two data instances are from the same category, and vice versa. We then use it to learn a pairwise similarity prediction function $G(x_i, x_j) = y_{i,j}$. By applying G on T, we can obtain $G(x_{T,i}, x_{T,j}) = y_{T,i,j}$. The last step is to infer Y_T from $Y_T^R = \{y_{T,i,j}\}_{\forall i,j}$, which can be solved by using constrained clustering algorithms. Note that since

the actual Y_T is unknown, the algorithm only infers the indices of categories, which could be in arbitrary order. The resulting clusters are expected to contain coherent semantic categories.

Transfer across domains: The problem setting we consider here is the same as unsupervised domain adaptation. Following the standard evaluation procedure (Long et al., 2017; Ganin et al., 2016), the labeled datasets A is ImageNet and S' is one domain in the Office-31 dataset. The unlabeled T is another domain in Office-31. The backbone network is pre-trained using A, then fine-tuned with S' to learn the classifiers. To enhance the performance of the classifier on T, some strategies can be applied to minimize the domain discrepancy between the training source and target data.

4 THE LEARNABLE CLUSTERING OBJECTIVE (LCO)

The design of our learning objective is inspired from constrained clustering, which involves using pairwise information in their loss function. The pairwise information is called must-link/cannot-link constraints or similar/dissimilar pairs (we use the latter). Note that the information is binarized to one and zero for similar and dissimilar pairs, accordingly.

Although many constrained clustering algorithms been developed, few of them are scalable with respect to the number of pairwise relationships. Further, none of them can be easily integrated into deep neural networks. Inspired by the work of Hsu & Kira (2016), we construct a contrastive loss for clustering on the probability outputs of a softmax classifier. However, each output node does not have to map to a fixed category but instead each output node represents a probabilistic assignment of a data point to a cluster. The assignment between output nodes and clusters are formed stochastically during the optimization, and is guided by the pairwise similarity. If there is a similar pair, their output distribution should be similar, and vice-versa.

Specifically, we use the pair-wise KL-divergence to evaluate the distance between k cluster assignment distributions of two given input data, and use predicted similarity to construct the contrastive loss. Given a pair of data x_p, x_q, their corresponding output distributions are defined as $\mathcal{P} = f(x_p)$ and $\mathcal{Q} = f(x_q)$, while f is the neural network. The cost of a similar pair is described as :

$$\mathcal{L}(x_p, x_q)^+ = \mathcal{D}_{KL}(\mathcal{P}^\star || \mathcal{Q}) + \mathcal{D}_{KL}(\mathcal{Q}^\star || \mathcal{P}) \tag{1}$$

$$\mathcal{D}_{KL}(\mathcal{P}^\star || \mathcal{Q}) = \sum_{c=1}^{k} p_c log(\frac{p_c}{q_c}) \tag{2}$$

The cost $\mathcal{L}(x_p, x_q)^+$ is symmetric w.r.t. x_p, x_q, in which $\mathcal{P}^\star$ and $\mathcal{Q}^\star$ are alternatively assumed to be constant. Each KL-divergence factor $\mathcal{D}_{KL}(\mathcal{P}^\star || \mathcal{Q})$ becomes a unary function whose gradient is simply $\partial \mathcal{D}_{KL}(\mathcal{P}^\star || \mathcal{Q}) / \partial \mathcal{Q}$.

If x_p, x_q comes from a pair which is dissimilar, their output distributions are expected to be different, which can be defined as a hinge-loss function:

$$\mathcal{L}(x_p, x_q)^- = L_h(\mathcal{D}_{KL}(\mathcal{P}^\star || \mathcal{Q}), \sigma) + L_h(\mathcal{D}_{KL}(\mathcal{Q}^\star || \mathcal{P}), \sigma) \tag{3}$$

$$L_h(e, \sigma) = max(0, \sigma - e) \tag{4}$$

Given a pair of data with similarity prediction function $G(x_p, x_q) \in \{0, 1\}$, the total loss can be defined as a contrastive loss:

$$\mathcal{L}(x_p, x_q) = G(x_p, x_q)\mathcal{L}(x_p, x_q)^+ + (1 - G(x_p, x_q))\mathcal{L}(x_p, x_q)^- \tag{5}$$

We refer to equation 5 as LCO. Two special characteristics of the clustering criterion are worth mentioning: (1). There is no need to define cluster center. (2). There is no predefined metric applied on the feature representation. Instead, the divergence is calculated directly on the cluster assignment; therefore, both feature representation and clustering are jointly optimized using back-propagation through the deep neural networks.

4.1 THE PAIRWISE SIMILARITY PREDICTION NETWORK

Although there is no restriction of how G should be constructed, we choose deep convolution neural networks due to their efficiency in vision tasks. We design a network architecture inspired from

Zagoruyko & Komodakis (2015). While they use it to predict the image patch similarity, we use it to predict image-level semantic similarity. However, the Siamese architecture used in Zagoruyko & Komodakis (2015) is not efficient in both training and inference, especially when pairwise information is dense. Therefore, instead of using Siamese architecture, we keep the single column backbone but add a *pair-enumeration layer* on top of the feature extraction network. The pair-enumeration layer enumerates all pairs of feature vectors within a mini-batch and concatenates the features. Suppose the input of the layer is $10 * 512$ with the mini-batch size 10 and the feature dimension 512; then the output of the pair-enumeration layer will be $100 * 1024$.

We illustrate the full architecture in appendix figure 2. We add one hidden fully connected layer on top of the enumeration layer and a binary classifier at the end. We use the standard cross-entropy loss and train it end-to-end. The supervision for training was obtained by converting the ground-truth category labels into binary similarity, i.e., if two samples are from the same class then their label will be *similar*, otherwise *dissimilar*. The inference is also end-to-end, and it outputs predictions among all similarity pairs in a mini-batch. The output probability $g \in [0, 1]$ with 1 means more similar. We binarize g at 0.5 to obtain discrete similarity predictions. In the following sections, we simplified the notation of the pairwise similarity prediction network as G. Once G is learned, it is then used as a static function in our experiments.

4.2 THE OBJECTIVE FUNCTION WITH DENSE SIMILARITY PREDICTION

Since the pairwise prediction of a mini-batch can be densely obtained from G , to efficiently utilize the pair-wise information without forwarding each data multiple times we also combine the pair-enumeration layer described in section 4.1 with equation 5. In this case the outputs of softmax are enumerated in pairs. Let D be the set of all tuples (p, q), while p and q are the indices of a sample in a mini-batch. The dense clustering loss $\mathcal{L}_d$ for a mini-batch is calculated by:

$$\mathcal{L}_d = \sum_{\forall (p,q) \in D} \mathcal{L}(x_p, x_q). \tag{6}$$

4.3 COMBINING WITH OTHER OBJECTIVES

In the cross-domain case, we further have labeled source data. Therefore, we simultaneously use LCO for T while using classification loss for S'. The overall training procedure is similar to previous domain adaptation approaches in that both source and target data are mixed in a mini-batch, but different losses are applied. We denote the source domain images in a mini-batch b as X_{b^S} and the target domain images X_{b^T} with its set of dense pairs D_{b^T}. The loss function $\mathcal{L}_{cd}$ for cross-domain transfer in a mini-batch can then be formulated as:

$$\mathcal{L}_{cd} = \mathcal{L}_{cls} + \mathcal{L}_{cluster} \tag{7}$$

$$\mathcal{L}_{cls} = \frac{1}{|b^S|} \sum_{\forall x_i \in X_{b^S}} CrossEntropyLoss(f(x_i)). \tag{8}$$

$$\mathcal{L}_{cluster} = \frac{1}{|b^T|^2} \sum_{\forall (i,j) \in D_{b^T}} \mathcal{L}(x_i, x_j). \tag{9}$$

The $\mathcal{L}_{cluster}$ and $\mathcal{L}_{cls}$ share the same outputs from network f. Although $\mathcal{L}_{cluster}$ does not force the mapping between clusters and categories, $\mathcal{L}_{cls}$ does. Therefore the learned classifier can be applied on target data directly and picks the maximum probability for the predicted class. Note that in our loss function, there is no term to explicitly match the feature distribution between source and target; it merely transfers more knowledge in the form of constraints to regularize the learning of the classifier. There is also no requirement for the architecture to utilize hidden layers. Therefore our approach has large flexibility to be combined with other domain adaptation strategies, which we will demonstrate in the experiments.

5 EXPERIMENTS

5.1 UNSUPERVISED CROSS-TASK TRANSFER LEARNING

5.1.1 SETUP

The **Omniglot** dataset (Lake et al., 2015) contains 1623 different handwritten characters and each of them has 20 images drawn by different people. The characters are from 50 different alphabets and were separated to 30 background sets $Omniglot_{bg}$ and 20 evaluation sets $Omniglot_{eval}$ by the author. We use the $Omniglot_{bg}$ as the auxiliary dataset and the $Omniglot_{eval}$ as the target data. The total number of characters in $Omniglot_{bg}$ is 964, which can be regarded as the number of categories available to learn the semantic similarity.

The G function has a backbone neural network with four 3x3 convolution layers followed by 2x2 max-pooling with stride 2. The architecture is illustrated in appendix figure 2. All hidden layers are followed by batch normalization (Ioffe & Szegedy, 2015) and rectified linear unit. To prepare the inputs for training, the images from $Omniglot_{bg}$ were resized to 32x32 and normalized to zero mean with unit standard deviation. Each mini-batch has size of 100 and is sampled from random 20 characters to make sure the amount of similar pairs is reasonable. After pair enumeration, there are 10000 pairs subject to the loss function, which is a two-class cross entropy loss. The ground-truth similarity is obtained by converting the categorical labels. The loss of G is optimized by stochastic gradient decent and is the only part trained in a supervised manner in this section.

The Constrained Clustering Networks (CCN) is used to reconstruct the semantic clusters in the target dataset. We called the neural network as CCN if it only uses the LCO for the loss. The network has four 3x3 convolution layers followed by 2x2 max-pooling with stride 2, one hidden fully-connected layer, and one cluster assignment layer which is also fully connected. The number of output nodes in the last layer is equal to the number of potential cluster in target data. The output distribution is enumerated in pairs before sending to LCO. The network is randomly initialized, trained end-to-end, and be optimized by stochastic gradient decent with randomly sampled 100 images per mini-batch. Note the G function used by LCO is fixed during the optimization. The input data preparation is the same as above, except now the data is from $Omniglot_{eval}$. Specifically, during the training, the same mini-batch is given to both G and CCN. The dense pairwise similarity predictions from G are sent to LCO and are then fully utilized. The only hyper-parameter in LCO is the σ, and we set it to 2 for all our experiments. Appendix figure 3 illustrates the network.

$Omniglot_{eval}$ contains 20 alphabets and each one can be used as a standalone dataset. The 20 target datasets contain a varied number (20 to 47) of characters. Therefore we can evaluate the reconstruction performance under a varied number of ground-truth clusters. We tested the situations when the number of character (K) in an alphabet is known and unknown. When K is known, we set the target number of clusters in the clustering algorithm equal to true number of characters. If K is unknown, the common practice is to set it to a large number so that the data from different categories will not be forced to be in the same cluster. In the experiment, we simply set K to 100, which is much larger than the largest dataset (47).

All constrained clustering algorithms can be used to reconstruct the semantic clusters for our problem. Since there are mis-predictions in G, robustness to noise is the most important factor. Here we include all four types of constrained clustering introduced in section 2 as the baselines. We provide the full set of pairwise constraints to all algorithms including ours. In other words, given an alphabet of 20 characters, it will contains 400 images and 16000 predicted similarities from G (note that G makes predictions for both orders of a pair and for self pairs). The full pairwise similarities were presented to all algorithms in random order, while we empirically found it has no noticeable effect on results. We pick the baseline approaches based on code availability and scalability with respect to the number of pairwise constraints. Therefore we have shown results for K-means (MacQueen et al., 1967), LPNMF (Cai et al., 2009), LSC (Chen & Cai, 2011), ITML (Davis et al., 2007), SKKm (Anand et al., 2014), SKLR (Amid et al., 2016), SKMS (Anand et al., 2014), CSP (Wang et al., 2014) , and MPCK-means (Bilenko et al., 2004) as our baselines. We use the default parameters for each algorithm provided by original author except for K, the number of cluster. We use the same normalized images used in CCN for all algorithms.

Table 1: Unsupervised cross-task transferring from $Omniglot_{bg}$ to $Omniglot_{eval}$. The performance is averaged across 20 alphabets which have 20 to 47 letters. The ACC and NMI without brackets has the number of cluster equal to ground-truth. The "(100)" means the algorithms use $K = 100$. The characteristics of how each algorithm utilizes the pairwise constraints are marked in the "Constraints used in" column, where metric stands for the metric learning of feature representation.

Method	Constraints used in Metric	Constraints used in Clustering	ACC	ACC (100)	NMI	NMI (100)
K-means			21.7%	18.9%	0.353	0.464
LPNMF			22.2%	16.3%	0.372	0.498
LSC			23.6%	18.0%	0.376	0.500
ITML	o		56.7%	47.2%	0.674	0.727
SKMS	o		-	45.5%	-	0.693
SKKm	o		62.4%	46.9%	0.770	0.781
SKLR	o		66.9%	46.8%	0.791	0.760
CSP		o	62.5%	65.4%	0.812	0.812
MPCK-means	o	o	81.9%	53.9%	0.871	0.816
CCN (Ours)	o	o	**82.4%**	**78.1%**	**0.889**	**0.874**

The evaluation uses two clustering metrics. The first is normalized-mutual information (NMI) (Strehl & Ghosh, 2002) which is widely used for clustering. The second one is the clustering accuracy (ACC) (Yang et al., 2010). The ACC metric first finds the one-to-one matching between predicted clusters and ground-truth labels, and then calculates the classification accuracy based on the mapping. All data outside the matched clusters will be regarded as mis-predictions. To get high ACC, the algorithm has to generate coherent clusters where each cluster includes most of the data in a category; otherwise the score drops quickly. Therefore ACC provides better discrimination to evaluate whether the semantic clusters have been reconstructed well.

5.1.2 Results and Discussions

The results are summarized in table 1, which reports the average performance over the 20 alphabets. Our approach achieved the top performance on both metrics. The CCN demonstrates promising robustness on the challenging scenario of unknown K. It achieved 78.1% average accuracy. Compared with 82.4% when K is known, CCN has a relatively small drop. If comparing it with the second best algorithm, CSP, which is 65.4%, CCN outperforms it with a large gap. The classical approach MPCK-means works surprisingly well when the number of clusters is known, but its performance dropped dramatically from 81.9% to 53.9% when $K = 100$. If we look at the performance of 20 individual alphabets (appendix table 3), CCN achieved 94% clustering accuracy on *Old Church Slavonic Cyrillic*, which has 45 characters. Therefore the results show the feasibility of reconstructing semantic clusters using only noisy similarity predictions.

When to use the semantic similarity? The experiments in table 1 show a clear trend that utilizing the pairwise constraints jointly for both metric learning and minimizing the clustering loss achieves the best performance, including both MPCK-means and CCN. In the case of unknown number of clusters, where we set $K = 100$, the algorithms that use constraints to optimize clustering loss have better robustness, for example, CSP and CCN. The group (ITML, SKMS, SKKm, and SKLR) that only use constraints for metric learning significantly outperform the group that does not use it (K-means, LPNMF, LSC). However, their performance are still far behind CCN. Our results confirm the importance of jointly optimizing the metric and clustering.

The robustness of the algorithm against noisy similarity prediction is the key factor to enable the cross-task transfer framework. To our best knowledge, table 1 is the first comprehensive robustness comparisons using the predicted constraints learned from real data instead of converting from ground-truth labels. The accuracy of G in our experiment were shown in appendix table 5 and demonstrate the reasonable performance of G which is on par with Matching-Net (Vinyals et al., 2016). After binarizing the prediction at 0.5 probability, the similar pair precision, similar pair recall, dissimilar pair precision, and dissimilar pair recall among the 659 characters are $(0.392, 0.927, 0.999, 0.995)$, accordingly. The binarized predictions are better than uniform random guess $(0.002, 0.500, 0.998, 0.500)$,

but are still noisy. Therefore it is very challenging for constrained clustering. The visualization of the robustness range of CCN are provided in the appendix E, and shows that the robustness is related to the large amount of pairs involved in a mini-batch. We hypothesize that during the optimization, the gradients from wrongly predicted pairs are canceled out by each other or by the correctly predicted pairs. Therefore the overall gradient still moves the solution towards a better clustering result. Finding the reason of robustness is not the focus of this paper so we leave it to future work.

How to predict K? Inferring the number of clusters (NC) is a hard problem, but with the pairwise similarity information it becomes feasible. For evaluation, we compute the difference between the number of dominant clusters (NDC) and the true number of categories (NC^{gt}) in a dataset. We use a naive definition for NDC, which is the number of clusters that have size larger than expected size when data is sampled uniformly. In other words, $NDC = \sum_{i=1}^{K} [C_i >= E[C_i]]$, where $[\cdot]$ is an Iverson Bracket and C_i is the size of cluster i. For example, $E[C_i]$ will be 10 if the alphabet has 1000 images and $K = 100$. Then the average difference ($ADif$) is calculated by $ADif = \frac{1}{|D|} \sum_{d \in D} |NDC_d - NC_d^{gt}|$, where d (i.e., alphabet) is a dataset in D. A smaller $ADif$ indicates a better estimate of K. CCN achieves a score of 6.35 (see appendix table 4). We compare this with the baseline approach SKMS (Anand et al., 2014), which does not require a given K and supports a pipeline to estimate K automatically (therefore we only put it in to the column $K = 100$ in table 1.). SKMS gets 16.3. Furthermore, 10 out of 20 datasets from CCN's prediction have a difference between NDC_d and NC_d^{gt} smaller or equal to 3, which shows the feasibility of estimating K with predicted similarity.

5.1.3 Experiment on the ImageNet dataset

We applied the same scheme on the ImageNet dataset. The 1000-class dataset is separated into 882-class ($ImageNet_{882}$) and 118-class ($ImageNet_{118}$) subsets as the random split in Vinyals et al. (2016). We use $ImageNet_{882}$ for A and 30 classes ($\sim$39k images) are randomly sampled from $ImageNet_{118}$ for T. The difference from section 5.1.1 is that here uses the Resnet-18 for both G and CCN, and the weights of backbone are pre-trained with $ImageNet_{882}$. Since the amount of pair is high and is not feasible to feed into other constrained clustering algorithms, we compare CCN with K-means, LSC , and LPNMF. We use the output from the average pooling layer of Resnet-18 as the input to these clustering algorithms. CCN gives the top performance with average ACC 73.8% when K is known, and 65.2% when the number of cluster is unknown, which outperforms the second (34.5% by K-means) with a large margin. The resuls demonstrate our approach is scalable to large dataset. The full comparison is in appendix table 6. And the performance of G is provided in appendix table 7.

5.2 Unsupervised Cross-Domain Transfer Learning

5.2.1 Setup

Office-31 (Saenko et al., 2010) has images from 31 categories of office objects. The 4652 images are obtained from three domains: Amazon, DSLR, and Webcam. The dataset is the standard benchmark for evaluating domain adaptation performance in computer vision. We experiment with all six combinations: $A \rightarrow W$, $A \rightarrow D$, $D \rightarrow A$, $D \rightarrow W$, $W \rightarrow A$, $W \rightarrow D$, and report the average accuracy based on five random experiments for each setting.

The G function uses the ImageNet pre-trained Resnet-18 as the backbone network. The semantic similarity is trained with 1000 categories in ImageNet. The training process is the same as section 5.1.1 except the images are resized to 224.

We follow the standard protocols using deep neural networks (Long et al., 2017; Ganin et al., 2016) for unsupervised domain adaptation. The backbone network is pre-trained with ImageNet. Appendix figure 4 and 7 illustrates the scheme. During the training, all source data and target data are used. Each mini-batch is constructed by 32 labeled samples from source and 96 unlabeled samples from target. Since the target dataset has no label and could only be randomly sampled, it is crucial to have sufficient mini-batch size to make similar pairs be sampled. The loss function used in our approach is equation (7) and is optimized by stochastic gradient decent. The LCO and DANN (RevGrad) with ResNet backbone are implemented with Torch. We use the code from original author for JAN. Both DANN and JAN use a 256-dimension bottleneck feature layer.

Table 2: Unsupervised cross-domain transfer (domain adaptation) on Office-31 dataset. The backbone network used here is the Resnet-18 (He et al., 2016) pre-trained with ImageNet.

	A → W	D → W	W → D	A → D	D → A	W → A	Avg
Source-Only	66.8	92.8	96.8	67.1	51.4	53.0	71.3
DANN (Ganin et al., 2016)	73.2	97.0	99.0	69.3	58.0	57.8	75.7
JAN (Long et al., 2017)	74.5	94.1	**99.6**	**75.9**	58.7	59.0	76.9
LCO (ours)	76.7	97.3	98.2	71.2	61.0	60.5	77.5
LCO+DANN	**78.2**	**97.4**	98.6	73.5	**62.8**	**60.6**	**78.5**

5.2.2 Results and Discussions

The results are summarized in table 2. Our approach (LCO) demonstrates a strong performance boost for the unsupervised cross-domain transfer problem. It reaches 77.5% average accuracy which gained 6.2 points from the 71.3% source-only baseline. Although our approach merely transfers more information from the auxiliary dataset, it outperforms the strong approach DANN (75.7%), and state-of-the-art JAN (76.9%). When combining DANN with LCO, the performance is further boosted. This indicates that LCO helps mitigate the transfer problem in a certain way that is orthogonal to minimizing the domain discrepancy. We observe the same trend when using a deeper backbone network, i.e, ResNet-34. In such a case the average accuracy achieved is 77.9%, 81.1% and 82% for source-only, LCO and LCO+DANN, respectively, though we used exactly the same G as before (with ResNet-18 backbone for G). This indicates that the information carried in the similarity predictions is not equivalent to transferring features with deeper networks. Appendix table 8 summarizes the effect of transferring the feature of deeper network. More discussions are in appendix D. And the performance of G is provided in appendix table 9 to show that even the prediction contains significant noise, our approach still benefit from it.

5.2.3 Experiments on SVHN-to-MNIST

We also evaluated LCO on another widely compared scenario, which uses color Street View House Numbers images (SVHN) (Netzer et al., 2011) as S', the gray-scale hand-written digits (MNIST) (LeCun, 1998) as T. For learn the G, we use the $Omniglot_{bg}$ as A. Our experimental setting is similar to Sener et al. (2016a). The performance gain from source-only in our approach is +37.1%, which wins a large margin from the +23.9% of LTR (Sener et al., 2016a). Our 89.1% accuracy also achieves the top performance. The full comparison is presented in appendix table 10.

6 Conclusion and Outlook

In this paper, we demonstrated the usefulness of transferring information in the form of pairwise similarity predictions. Such information can be transferred as a function and utilized by a loss formulation inspired from constrained clustering, but implemented more robustly within a neural network that can jointly optimize both features and clustering outputs based on these noisy predictions. The experiments for both cross-task and cross-domain transfer learning show strong benefits of using the semantic similarity predictions resulting in new state of the art results across several datasets. This is true even without explicit domain adaptation for the cross-domain task, and if we add a domain discrepancy loss the benefits increase further.

There are two key factors determining the performance of the proposed framework. The first is the robustness of the constrained clustering and second is the performance of the similarity prediction function. We show the robustness empirically, but we do not explore other choices for learning G. For example, applying domain adaptation for G would be a significant extension. Furthermore, the generalizability of our approach is actually controlled by G. If G can be used across modalities such as vision and language, information could be easily transfered across a wider range of task domains. We leave these aspects for future work.

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APPENDICES

A THE DIAGRAM OF NETWORKS

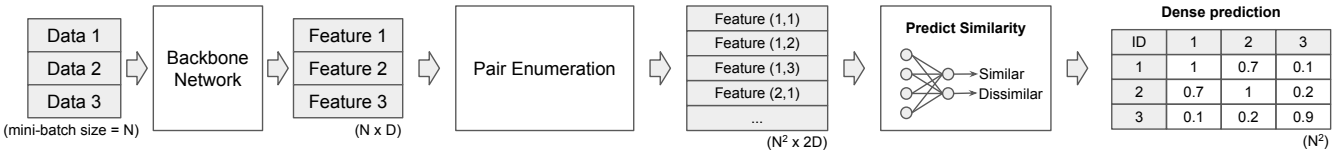

Figure 2: The similarity prediction network

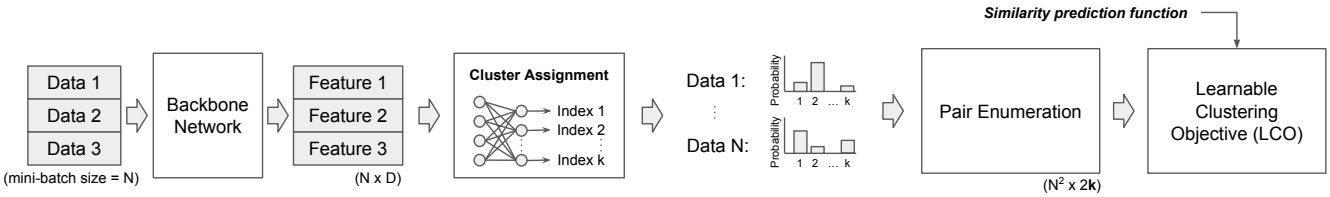

Figure 3: The constrained clustering network used for cross task transferring. The cluster assignment block contains two fully connected layers and has the number of output node equal to k.

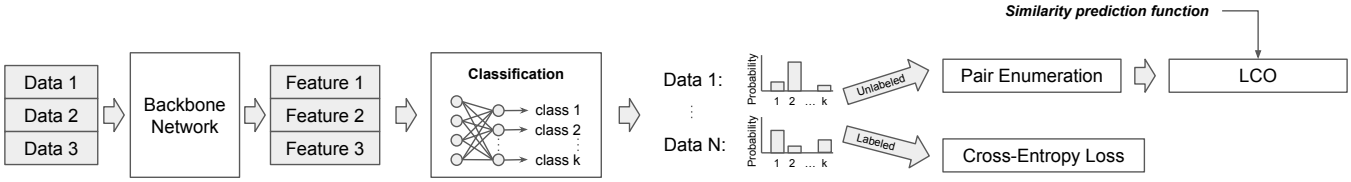

Figure 4: The network for cross domain transferring with constrained clustering loss (LCO).

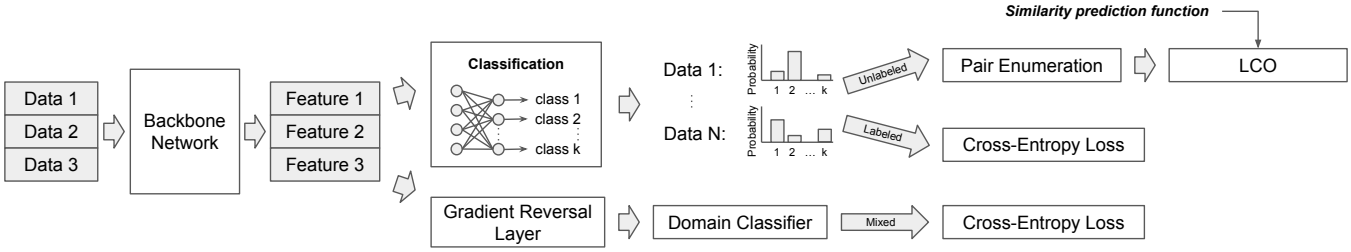

Figure 5: The network for cross domain transferring combined LCO and DANN.

B THE COMPARISON OF EXPERIMENT SETTINGS

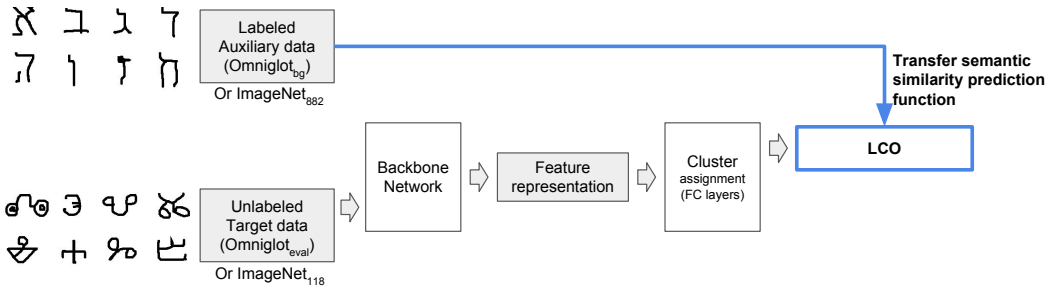

Figure 6: The diagram of cross-task transferring experiment. Two experiments follow this flow: $Omniglot_{bg}$ to $Omniglot_{eval}$, and $ImageNet_{882}$ to $ImageNet_{118}$. Both has exclusive classes between source and target domain. For the ImageNet experiment, the backbone network is initialized with the weights pre-trained with $ImageNet_{882}$.

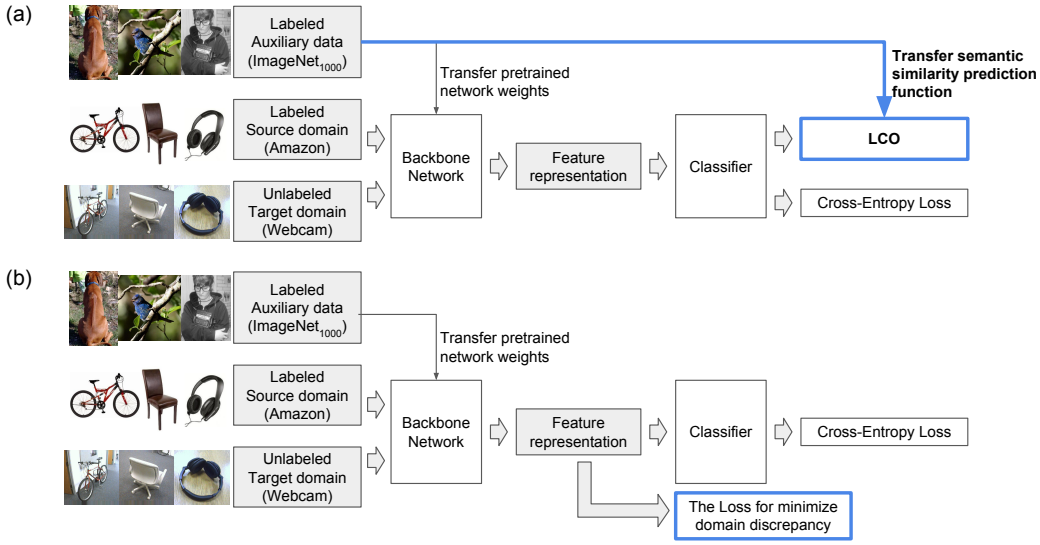

Figure 7: The comparison between domain adaptation approaches (a) Transferring semantic similarity from auxiliary data, and (b) Minimizing the domain discrepancy. The diagram uses office-31 benchmark as the scenario of transferring.

C SUPPLEMENTARY FOR UNSUPERVISED CROSS TASK TRANSFER LEARNING

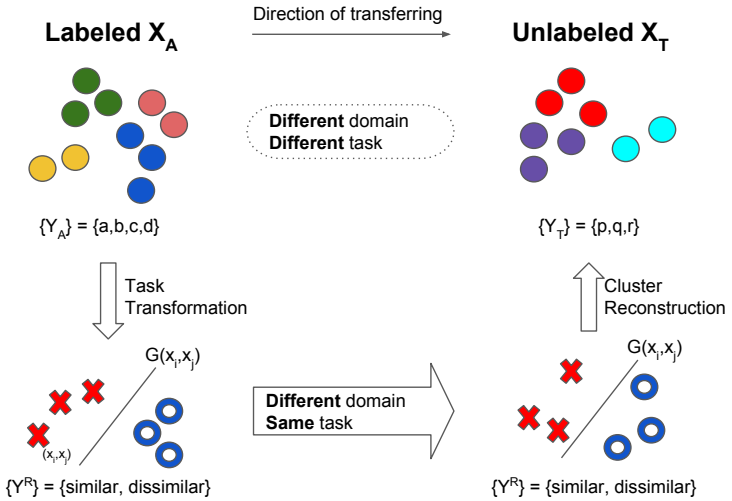

Figure 8: The concept for reconstructing clusters of unseen categories. The colors represent data of different categories. The hollow circle and cross symbol represent similar and dissimilar data pairs. The proposed approach follows the arrows in counter-clockwise direction. For detailed explanation please see section 3.

Table 3: The breakdown results of each alphabet in $Omniglot_{eval}$. The unsupervised cross task transferring experiment is described in section 5.1. This table shows the clustering accuracy with $K = 100$ to simulate the situation of unknown number of cluster.

Alphabet	K-means	LPNMF	LSC	ITML	SKMS	SKKm	SKLR	CSP	MPCK-means	CCN
Angelic	24%	26%	27%	48%	78%	40%	38%	72%	50%	**82%**
Atemayar_Qelisayer	19%	14%	17%	51%	61%	51%	44%	61%	50%	**82%**
Atlantean	19%	15%	19%	57%	72%	55%	51%	**77%**	47%	72%
Aurek_Besh	23%	18%	21%	45%	49%	44%	45%	76%	71%	**90%**
Avesta	22%	18%	19%	47%	29%	39%	38%	65%	52%	**76%**
Ge_ez	19%	17%	17%	56%	58%	47%	42%	72%	55%	**82%**
Glagolitic	22%	19%	21%	42%	38%	58%	62%	66%	61%	**85%**
Gurmukhi	15%	13%	15%	44%	26%	54%	48%	60%	56%	**80%**
Kannada	18%	14%	16%	48%	37%	46%	53%	60%	48%	**62%**
Keble	20%	14%	18%	44%	60%	46%	44%	75%	68%	**90%**
Malayalam	18%	15%	16%	36%	24%	49%	52%	50%	54%	**72%**
Manipuri	17%	15%	16%	49%	40%	53%	54%	66%	62%	**85%**
Mongolian	18%	18%	19%	50%	40%	37%	48%	75%	57%	**86%**
Old_Church_Slavonic_Cyrillic	19%	16%	19%	42%	41%	52%	67%	71%	67%	**94%**
Oriya	15%	13%	14%	46%	40%	54%	45%	57%	52%	**67%**
Sylheti	14%	13%	14%	49%	32%	35%	37%	59%	43%	**64%**
Syriac_Serto	20%	18%	19%	55%	70%	42%	35%	70%	47%	**73%**
Tengwar	18%	18%	18%	51%	44%	49%	40%	61%	44%	**66%**
Tibetan	18%	14%	16%	44%	31%	47%	54%	59%	55%	**84%**
ULOG	20%	18%	18%	41%	41%	40%	41%	56%	38%	**70%**
Average	19%	16%	18%	47%	46%	47%	47%	65%	54%	**78%**

Table 4: Estimate the number of character for 20 datasets in $Omniglot_{eval}$. The bold number means the prediction has error smaller or equal to 3. The $ADif$ is defined in section 5.1.2.

Alphabet	True #class	SKMS	CCN (K=100)
Angelic	20	16	26
Atemayar_Qelisayer	26	17	34
Atlantean	26	21	41
Aurek_Besh	26	14	**28**
Avesta	26	8	32
Ge_ez	26	18	32
Glagolitic	45	18	**45**
Gurmukhi	45	12	**43**
Kannada	41	19	**44**
Keble	26	16	**28**
Malayalam	47	12	**47**
Manipuri	40	17	**41**
Mongolian	30	**28**	36
Old_Church_Slavonic_Cyrillic	45	23	**45**
Oriya	46	22	**49**
Sylheti	28	11	50
Syriac_Serto	23	19	38
Tengwar	25	12	41
Tibetan	42	15	**42**
ULOG	26	15	40
$ADif$		16.3	6.35

Table 5: The performance of the similarity prediction function used in section 5.1. We leverage the N-way test which commonly used in one-shot learning evaluation. The similarity is learned with $Omniglot_{bg}$ and has N-way test with $Omniglot_{eval}$ and MNIST. The experiment settings follow Vinyals et al. (2016). The raw probability output (without binarization) from our G is used to find the nearest exemplar in the N-way test.

	Omniglot-eval		MNIST
Method	5-way	20-way	10-way
Siamese-Nets (Koch et al., 2015)	0.967	0.880	0.703
Match-Net (Vinyals et al., 2016)	**0.981**	**0.938**	**0.720**
Ours	0.979	0.935	**0.720**

Table 6: Unsupervised cross-task transfer learning on ImageNet. The values are the average of three random subsets in $ImageNet_{118}$. Each subset has 30 classes. The "(100)" means $K = 100$. All methods use the features (outputs of average pooling) from Resnet-18 pre-trained with $ImageNet_{882}$ classification.

Method	ACC	ACC(100)	NMI	NMI(100)
K-means	71.9%	34.5%	0.713	0.671
LSC	73.3%	33.5%	0.733	0.655
LPNMF	43.0%	21.8%	0.526	0.500
CCN (ours)	**73.8%**	**65.2%**	**0.750**	**0.715**

Table 7: The performance of similarity prediction function (G, trained with $ImageNet_{882}$) applied on three subset of $ImageNet_{118}$. Each subset contains 30 random classes of $ImageNet_{118}$. The predictions are binarized at 0.5 to calculate the precision and recall. Random*: The expected performance when classes are uniformly distributed and make uniform random guess for similarity. It is an approximation since the number of images in each class is only roughly equal in ImageNet. We sampled 12M pairs for each set to collect the statistics. Sampling more pairs has no noticeable change to the values.

Set	Similar Precision	Similar Recall	Dissimilar Precision	Dissimilar Recall
Random*	0.033	0.500	0.967	0.500
Set A	0.840	0.664	0.983	0.994
Set B	0.825	0.631	0.981	0.993
Set C	0.771	0.671	0.983	0.990
Average	0.812	0.655	0.982	0.992

D SUPPLEMENTARY FOR UNSUPERVISED CROSS DOMAIN TRANSFER LEARNING

D.1 MORE DISCUSSION FOR OFFICE-31 EXPERIMENTS

Note that our experiments (appendix table 8) also show that simply using deeper pre-trained networks produces a significant performance boost by itself. Specifically, using Resnet-50 increases the performance 8.4 points from Alexnet, which surpasses the 6.2 points gained by using one of the state-of-the-art domain adaptation algorithms (JAN (Long et al., 2017)). If we regard pre-training with deeper networks as transferring more information, our approach is similar in this aspect since both transfer more information from the auxiliary dataset. In this case, memory limitations precluded the application of LCO to such models, and multi-GPU implementations for this problem is an area of future work.

Table 8: The performance of unsupervised transfer across domains on Office-31 dataset. The backbone networks in the comparison have different number of convolutional layers. The AlexNet has 5 layers and the ResNets have 18$\sim$50 layers. SO is the abbreviate of source-only. The first two rows are directly copied from Long et al. (2017). The feature learned with deeper networks generalize better across domains.

	A $\rightarrow$ W	D $\rightarrow$ W	W $\rightarrow$ D	A $\rightarrow$ D	D $\rightarrow$ A	W $\rightarrow$ A	Avg	Gain
AlexNet SO	61.6	95.4	99.0	63.8	51.1	49.8	70.1	-
AlexNet (JAN-A)	**75.2**	96.6	**99.6**	72.8	57.5	56.3	76.3	+6.2
Resnet-18 SO	66.8	92.8	96.8	67.1	51.4	53.0	71.3	+1.2
Resnet-34 SO	73.1	96.4	98.8	73.8	**63.2**	**62.1**	77.9	+7.8
Resnet-50 SO	74.3	**96.8**	98.8	**79.5**	61.2	60.6	**78.5**	**+8.4**

Table 9: The performance of similarity prediction function (G, trained with $ImageNet_{882}$) applied on three domains of Office-31 dataset. Total 1.4M pairs are examined to calculate the table.

Domain	Similar Precision	Similar Recall	Dissimilar Precision	Dissimilar Recall
Amazon	0.194	0.696	0.988	0.894
DSLR	0.196	0.882	0.995	0.858
Webcam	0.213	0.865	0.994	0.876

Table 10: The unsupervised transferring across domain (S': SVHN, T: MNIST A: $Omniglot_{bg}$) without pre-trained backbone network weights. Our setup is similar to Sener et al. (2016a) and Ganin et al. (2016) therefore has a similar source-only performance.

Method		SVHN->MNIST	Gain
Ganin et al. (2016)	Source-Only	54.9	-
	DANN	73.9	+19.0
Sener et al. (2016a)	Source-Only	54.9	-
	LTR	78.8	+23.9
Saito et al. (2017)	Source-Only	70.1	-
	ATDA	86.2	+16.1
Tzeng et al. (2017)	Source-Only	60.1	-
	ADDA	76.0	+15.9
Ours	Source-Only	52.0	-
	LCO	**89.1**	**+37.1**

Table 11: The performance of similarity prediction function (G, trained with $Omniglot_{bg}$) applied on MNIST dataset. Total 5M pairs are sampled to calculate the table.

	Similar Precision	Similar Recall	Dissimilar Precision	Dissimilar Recall
Random	0.100	0.500	0.900	0.500
MNIST	0.782	0.509	0.946	0.984

E ROBUSTNESS ANALYSIS OF CONSTRAINED CLUSTERING NETWORK

E.1 SETUP

To quickly explore the large combination of factors that may affect the clustering, we use a small dataset (MNIST) and a small network which has two convolution layers followed by two fully connected layers. The MNIST dataset is a dataset of handwritten digits that contains 60k training and 10k testing images with size 28x28. Only the training set is used in this section and the raw pixels, which were normalized to zero mean and unit standard deviation, were fed into networks directly.

The networks was randomly initialized and the clustering training was run five times under each combination of factors with showing the best final results, as is usual in the random restart regime. The mini-batch size was set to 256, thus up to 65536 pairs were presented to the LCO per mini-batch if using full density (D=1). There were 235 mini-batches in an epoch and the optimization proceeded for 15 epochs. The clustering loss was minimized by stochastic gradient descent with learning rate 0.1 and momentum 0.9. The predicted cluster was assigned at the end by forwarding samples through the clustering networks. The best result in the five runs was reported.

To simulate different performance of the similarity prediction, the label of pairs were flipped according to the designated recall. For example, to simulate a 90% recall of similar pair, 10% of the ground truth similar pair in a mini-batch were flipped. The precision of similar/dissimilar pairs is a function of the recall of both type of pairs, thus controlling the recall is sufficient for the evaluation. The recalls for both similar and dissimilar pairs were gradually reduced from one to zero at intervals of 0.1.

E.2 DISCUSSION

The resulting performance w.r.t different values of recall, density, and number of clusters is visualized in Figure 9. The bright color means high NMI score and is desired. The larger the bright region, the more robust the clustering is against the noise of similarity prediction. The ACC score shows almost the same trend and is thus not shown here.

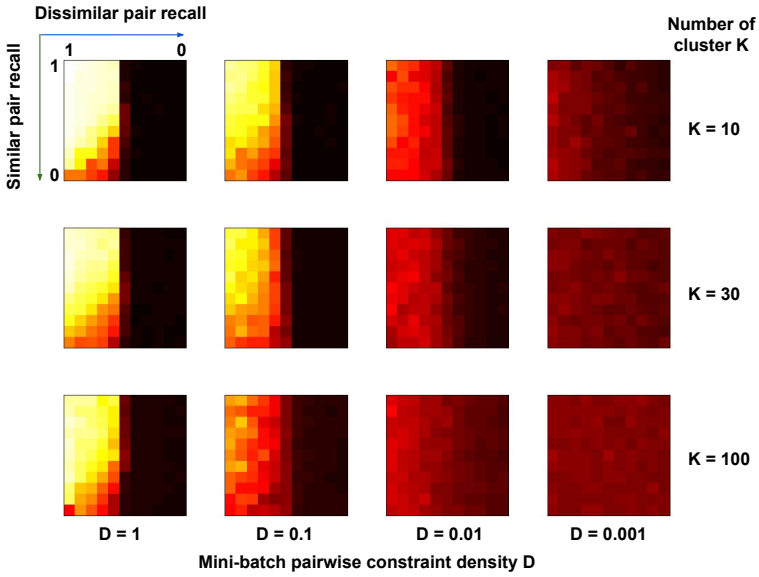

Figure 9: The clustering performance with different pairwise density and number of clusters. A bright color means that the NMI score is close to 1 while black corresponds to 0. The density is defined as a ratio compared to the total number of pair-wise combinations in a mini-batch. The number of clusters defines the final softmax output dimensionality. In each sub-figure, we show how the scores change w.r.t. the similar pair recall and dissimiliar pair recall.

How does similarity prediction affect clustering? Looking at the top-left heat map in figure 9, which has $D = 1$ and 10 cluster, it can be observed that the NMI score is very robust to low similar pair recall, even lower than 0.5. For recall of dissimilar pairs, the effect of recall is divided at the 0.5 value: the clustering performance can be very robust to noise in dissimilar pairs if the recall is greater than 0.5; however, it can completely fail if recall is below 0.5. For similar pairs, the clustering works on a wide range of recalls when the recall of dissimilar pairs is high.

In practical terms, robustness to the recall of similar pairs is desirable because it is much easier to predict dissimilar pairs than similar pairs in real scenarios. In a dataset with 10 categories e.g. Cifar-10, we can easily get 90% recall for dissimilar pairs with purely random guess if the number of class is known, while the recall for similar pairs will be 10%.

How does the density of the constraints affect clustering? We argue that the density of pairwise relationships is the key factor to improving the robustness of clustering. The density $D = 1$ means that every pair in a mini-batch is utilized by the clustering loss. For density $D = 0.1$, it means only 1 out of 10 possible constraints is used. We could regard the higher density as better utilization of the pairwise information in a mini-batch, thus more learning instances contribute to the gradients at once. Consider a scenario where there is one sample associated with 5 true similar pairs and 3 false similar pairs. In such a case, the gradients introduced by the false similar pairs have a higher chance to be overridden by true similar pairs within the mini-batch, thus the loss can converge faster and is less affected by errors. In Figure 9, we could see when density decreases, the size of the bright region shrinks significantly.

In our implementation, enumerating the full pairwise relationships introduces negligible overhead in computation time using GPU. Although there is overhead for memory consumption, it is limited because only the vector of predicted distributions has to be enumerated for calculating the clustering loss.

The effect of vary number of Cluster In the MNIST experiments, the number of categories is 10. We augment the softmax output number up to 100. The rows of figure 9 show that even when the number of output categories is significant larger than the number of true object categories, e.g. $100 > 10$, the clustering performance NMI score only degrades slightly.