RL-DARTS: Differentiable Architecture Search for Reinforcement Learning

Abstract

Recently, Differentiable Architecture Search (DARTS) has become one of the most popular Neural Architecture Search (NAS) methods successfully applied in supervised learning (SL). However, its applications in other domains, in particular for reinforcement learning (RL), has seldom been studied. This is due in part to RL possessing a significantly different optimization paradigm than SL, especially with regards to the notion of replay data, which is continually generated via inference in RL. In this paper, we introduce RL-DARTS, one of the first applications of end-to-end DARTS in RL to search for convolutional cells, applied to the challenging, infinitely procedurally generated Procgen benchmark. We demonstrate that the benefits of DARTS become amplified when applied to RL, namely search efficiency in terms of time and compute, as well as simplicity in integration with complex preexisting RL code via simply replacing the image encoder with a DARTS supernet, compatible with both off-policy and on-policy RL algorithms. At the same time however, we provide one of the first extensive studies of DARTS outside of the standard fixed dataset setting in SL via RL-DARTS. We show that throughout training, the supernet gradually learns better cells, leading to alternative architectures which can be highly competitive against manually designed policies, but also verify previous design choices for RL policies.

1 Introduction and Motivation

Over the last decade, recent advancements in deep reinforcement learning have heavily focused on algorithmic improvements (Hessel et al., 2018; Wang et al., 2016), data augmentation (Raileanu et al., 2020; Kostrikov et al., 2020), infrastructure upgrades (Espeholt et al., 2018; Horgan et al., 2018), and even hyperparameter tuning (Zhang et al., 2021; Faust et al., 2019). Automating such methods for RL have given rise to the field of Automated Reinforcement Learning (AutoRL). Surprisingly however, one relatively underdeveloped and unexplored area is in automating large-scale policy architecture design.

Recently, works in larger-scale RL suggest that designing a policy's architecture can be just as important as the algorithm or quality of data, if not more, for various metrics such as generalization, transferrability, and efficiency. One surprising phenomenon found on Procgen (Cobbe et al., 2020), a procedural generation benchmark for RL, was that "IMPALA-CNN", a residual convolutional architecture from (Espeholt et al., 2018), could substantially outperform "NatureCNN", the standard 3-layer convolutional architecture used for Atari (Mnih et al., 2013), in both generalization and sample complexity under limited and infinite data regimes respectively (Cobbe et al., 2019). Furthermore, in robotics subfields such as grasping (Kalashnikov et al., 2018; Rao et al., 2020), cameras collect very detailed real-world images (ex: 472 x 472, 4x larger than ImageNet (Russakovsky et al., 2015)) for observations which require deep image encoder architectures, consisting of more than 15 convolutions. As such RL policy networks gradually become larger and more sophisticated, so does the need for understanding and automating such designs.

Many efficient Neural Architecture Search (NAS) methods utilize the *one-shot* setup, where only one set of shared weight parameters is trained through an ensemble of models, otherwise known as a *supernet*. Differentiable Architecture Search (Liu et al., 2019), trains the supernet by inserting architecture selection variables inside the network in a continuous relaxation approach, in order to be differentiable with respect to a loss. These architecture search parameters are then used to select a final discretized perception module to be retrained from scratch in an evaluation phase.

The differentiable aspect of DARTS is highly attractive to RL, which possess two complications which SL does not:

1. RL is an ***entire system***. In most RL algorithms involving auto-differentiation, there are multiple different phases: a *collection/exploration phase* which collects environment data via forward passes/inference of a policy, in addition to a *training phase* which updates parameters for potentially multiple network components (e.g. both the policy and value function in policy gradient methods). There can also even be a separate *evaluation phase* (disjoint from evaluation in NAS) different from the collection phase (e.g. using argmax greedy evaluation instead of the stochastic actor, for both Q-learning and policy gradient methods). Such phases are also commonly distributed over different machines, adding an extra layer of complexity via inter-machine communication.

2. RL training curves **possess considerably more variance and noise** than SL curves, with a much larger room for error due to sensitivity to hyperparameters (Andrychowicz et al., 2020), which originally led to the criterion of reporting mean and standard deviation for 3 seeded runs (Henderson et al., 2018). In fact, this noise can be nearly *unbounded*, as in many cases, an unlucky and catastrophic seeded training run can simply lead to a trivial reward even with an optimal architecture. Such noise may potentially be problematic for fast convergence for blackbox/evolutionary optimization methods. Furthermore, the RL **loss contains important information not conveyed by just pure reward** (e.g. value function error and entropy penalty, as well as potentially exploration/novelty bonuses), whereas information may be lost when simply summarizing all progress to a single scalar point of data.

DARTS solves (1) as it integrates naturally within the RL system with **minimal modifications** to the code and pipeline, by simply replacing the image encoder in standard RL algorithms. For (2), architecture search parameters in the DARTS supernet are joint trained alongside weight parameters, and can thus also use information from multiple auxiliary losses, which can be much richer signals than potentially sparse rewards. We represent this approach in Figure 1.

However, a few subtle peculiarities arise when applying DARTS to RL. While DARTS in SL focuses mostly on bilevel optimization and generalization rather than training the supernet, as almost any network, even an MLP, can obtain 100% training accuracy (Zhang et al., 2017), a core major focus in RL is still on the training procedure itself, in order to improve sample complexity and asymptotic rewards. However, it is nonobvious that a DARTS supernet can *even train* with so many different moving parts in RL. This is especially because using a differentiable loss (ex: Bellman error) as the search objective is a double-edged sword in RL, as loss is defined with **respect to the replay buffer, whose data**

Figure 1: Representation of our method, in which a DARTS supernet is simply inserted into the network components of a standard RL training pipeline, which may potentially be highly distributed.

is collected by the policy itself via inference on the architecture. In SL, the data distribution is independent of the architecture, and the loss (e.g. cross-entropy or negative log-likelihood) is strongly correlated or even equivalent to the objective (e.g. accuracy or density estimation (Parmar et al., 2018)). However **in RL, a bad architecture could lead to a poor initial distribution of data, and thus a local optimum where the loss is zero while the policy is still poor.** This is inherently due to the fact that the data in the replay buffer may not sufficiently cover the state and action space of the entire environment, and is common in cases such as sparse reward problems. This issue occurs even if the replay buffer data is fixed, which is the basis of offline RL (Levine et al., 2020).

The other question occurs during the *discretization* phase of DARTS, as any continuous relaxation method must deal with *integrality gaps* when rounding back to a discrete space, with this gap dependent on the optimization landscape. At the core of multiple discretization procedures (Liu et al., 2019; Chu et al., 2020c; Hundt et al., 2019) lies the idea of op selection based on edge weights. However, RL's optimization landscape is significantly different (Ilyas et al., 2020; Ahmed et al., 2019) from SL, and thus **even if the supernet trains in RL, it is unclear if e.g. DARTS's default**

discretization procedure leads to a better discrete cell, which is the original goal of DARTS and NAS in general.

In this paper, we carefully analyze the extent at which DARTS can optimize perception modules for RL environments. While there is a rich series of active study on the theoretical and empirical behavior of DARTS optimization in SL (Wang et al., 2021b; Chen & Hsieh, 2020; Li et al., 2021), **our work is one of the first to study its optimization in RL, a completely different paradigm.** In summary, our contributions are:

- We demonstrate DARTS can be integrated with existing RL algorithms in a minimally invasive and easy-to-use manner, agnostic to the specific pipeline. Remarkably, on the challenging Procgen benchmark featuring infinite data, the DARTS supernet is able to train from scratch and efficiently produce similar training curves as baselines using both on-policy (PPO) and off-policy (Rainbow) methods, both of which require inference on the network.

- Due to the common issue of integrality gaps between supernet cells and discrete cells, we verify both qualitatively via visualizations and quantitatively via rewards, that discretized cells start with suboptimal architectures and gradually evolve to better architectures. However, we also demonstrate how this can fail, especially if the corresponding supernet fails to train, with further extensive ablations in the Appendix.

- By evaluating the final discrete cells at the end of supernet training, we discover that many environments benefit from learned, custom-tailored architectures, suggesting that human-designed architectures can be suboptimal. Furthermore, we find that joint-training a supernet on multiple environments can potentially produce a single transferrable cell. This opens up questions for future study, as large-scale RL can potentially benefit from more applications of NAS techniques.

2 RELATED WORKS

Most previous AutoRL methods can be thought of in terms of blackbox and evolutionary methods. For NAS on RL, these include (Song et al., 2021; Gaier & Ha, 2019; Stanley & Miikkulainen, 2002) which utilize CPU workers for forward pass evaluations rather than exact gradient computation on GPUs. Such methods are usually unable to train policies involving more than 10K+ parameters due to the sample complexity of zeroth order methods in high dimensional parameter space (Agarwal et al., 2010). However, such methods have proved useful on smaller search spaces for RL, such as hyperparameter optimization (Zhang et al., 2021; Franke et al., 2020b; Parker-Holder et al., 2020; Jaderberg et al., 2017) and algorithm search/"learning to learn" methods (Faust et al., 2019; Co-Reyes et al., 2021).

In terms of differentiable search in RL, methods for tuning hyperparameters and environments include (Zahavy et al., 2020; Xu et al., 2018; Hu et al., 2020). The only previous known application of DARTS is (Akinola et al., 2021), which searches for the optimal way of combining the observation and action tensors together in off-policy QT-OPT (Kalashnikov et al., 2018). However, this approach does not modify the image encoder nor uses the supernet for inference, as off-policy robotic data collected independently from the actual policy is used for training, which leaves the applicability of DARTS to inference-dependent RL as an open question addressed in our work.

3 METHODOLOGY

3.1 VANILLA DARTS AND NAS PRELIMINARIES

We provide a brief review of DARTS which can be pictorially summarized in Figure 2, although more details can be found in the original DARTS paper (Liu et al., 2019). DARTS optimizes substructures called cells, where each cell contains I intermediate nodes organized in a directed acyclic graph, where each node $x^{(i)}$, represents a feature map, and each edge (i, j) consists of an operation (op) $o^{(i,j)}$, with later nodes $x^{(j)}$ merged (e.g. summation) from some previous $o^{(i,j)}(x^{(i)})$. A DARTS supernet is constructed by continuously relaxing selection of ops in $\mathcal{O}$, via softmax weighting, i.e. $\overline{o}^{(i,j)}(x^{(i)}) = \sum_{o \in \mathcal{O}} p_o^{(i,j)} \cdot o(x^{(i)})$, where $p_o^{(i,j)} = \frac{\exp(\alpha_o^{(i,j)})}{\sum_{o' \in \mathcal{O}} \exp(\alpha_{o'}^{(i,j)})}$. The cell's output is by default

the result of a Conv1x1 op on the depthwise concatenation of all intermediate node features, although this may be changed (e.g. simply output last intermediate node's features). We denote the collection of all architecture variables $a_o^{(i,j)}$ as α. Since the total op space $\mathcal{O}$ must contain the Zero and Skip Connection ops, we mainly refer to the main op space as $\mathcal{O}_{base}$ where $\mathcal{O} = \mathcal{O}_{base} \cup \{Zero, Skip\}$. In the standard optimization framework for SL where there is the notion of a validation set, the learning procedure consists of a bilevel optimization problem:

$$\alpha^* = \arg\min_{\alpha} \mathcal{L}_{val}(\theta^*, \alpha) \quad \text{s.t.} \quad \theta^* = \arg\min_{\theta} \mathcal{L}_{train}(\theta, \alpha) \tag{1}$$

where $\mathcal{L}(\theta, \alpha)$ is a loss function defined with respect to the supernet. α^* is then *discretized* into a final cell, by representing each edge (i, j) with the highest softmax weighted op $\arg\max_{o \in \mathcal{O}, o \neq zero} p_o^{(i,j)}$ and then retaining only the top 2 incoming edges for each intermediate node.

Following common NAS practices (Zoph et al., 2018; Pham et al., 2018; Zoph & Le, 2016), we construct our supernet by stacking both normal (N times) and reduction cells (R times) together into *blocks*, which are themselves also stacked together D times (see Figure 2). Normal cells preserve the input shape on output, while reduction cells apply a stride of 2 to reduce height and width immediately on the input. Each block can have its own associated convolutional channel depth which is used throughout all cells in the block. Another common NAS practice we adopt is to train a smaller supernet (e.g. with lower convolutional depths) to reduce computation time, but evaluate final discretized cells on larger models.

Figure 2: Illustration of our supernet via stacking normal and reduction cells. Solid lines correspond to selected ops after discretizing the supernet, which contains all possible ops weighted using α.

3.2 RL-DARTS

For notation, we use standard conventions in the RL literature: for a given MDP $\mathcal{M}$, we denote s_t, a_t, r_t as the state, action, reward respectively at time t. π_θ is the policy with neural network weights θ, γ is the discount factor, and $\mathcal{D}$ is the replay buffer which contains collected trajectories $\tau = (s_0, a_0, r_0, s_1, ...)$. The goal of the RL algorithm is to maximize $J(\pi_\theta) = \mathbb{E}_{\tau \sim \pi_\theta}\left[\sum_{t \geq 0} r_t\right]$, the expected cumulative reward when using policy π_θ. In most RL algorithms, there is the notion of a neural network torso, or *encoder* which maps a state s (or sequence τ) to a feature vector, which may be projected to correct action dimensions, behind the scenes in forming π_θ. In the DARTS case, we use a supernet for this encoder instead, which leads to $\pi_{\theta,\alpha}$.

The original bilevel optimization framework (Eq. 1) is notoriously difficult and unstable, sometimes requiring special techniques (Liu et al., 2018; Dong & Yang, 2019; Hundt et al., 2019; Li et al., 2020; Chu et al., 2020b;a;c; Liang et al., 2019; Wang et al., 2021b) specific to SL optimization. To avoid such confounding factors, especially when DARTS has not yet been fully

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Algorithm 1: RL-DARTS Procedure.

1. Supernet training: Compute α^* from $\arg\max_{\theta,\alpha} J(\pi_{\theta,\alpha})$.

2. Discretization: Discretize α^* to construct evaluation policy $\pi_{\theta,\delta(\alpha^*)}$.

3. Evaluation: Report $\max_\theta J(\pi_{\theta,\delta(\alpha^*)})$.

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validated in RL, we may simply optimize sample complexity and raw training performance which are common metrics in RL. We thus joint optimize both θ and α:

$$\arg\max_{\theta,\alpha} J(\pi_{\theta,\alpha}) \quad \text{via} \quad \arg\min_{\theta,\alpha} \mathcal{L}(\theta, \alpha) \tag{2}$$

which leads to an optimal α^*. For convenience, (with slight abuse of notation), we denote $\pi_{\theta,\delta(\alpha^*)}$ to be the policy when using the discrete cell under discretization $\delta(\alpha^*)$ and $\mathcal{L}_{\delta(\alpha^*)}(\theta)$ to be the corresponding (now regular) loss function. Note that under standard NAS procedure, we must then *evaluate* the discretized cell via training from scratch again to obtain the final reward:

$$\max_\theta J(\pi_{\theta,\delta(\alpha^*)}) \quad \text{via} \quad \arg\min_{\theta} \mathcal{L}_{\delta(\alpha^*)}(\theta) \tag{3}$$

This can be concisely summarized in Algorithm 1, although we remind the reader that $\mathcal{L}(\cdot)$ is defined with respect to replay buffer $\mathcal{D}$ and is not necessarily equivalent to optimizing $J(\cdot)$. Unless specified, we by default use consistent hyperparameters (found in Appendix D) for all comparisons found inside a figure, although learning rate and minibatch size may be altered when training models of different sizes due to GPU memory limits. Thus, even though RL is commonly sensitive to hyperparameters (Zhang et al., 2021), we find that **once a pre-existing RL baseline has already been setup, incorporating DARTS requires no extra cost in tuning, as evidence of its ease-of-use.**

4 EXPERIMENTS

4.1 EXPERIMENT SETUP

We perform key experiments to understand the behavior of RL-DARTS, and answer the following main questions in our analysis:

1. Does the supernet train end-to-end at all or will it fail to even initially collect good online data? Does α converge towards a sparse solution over time, and what is the computational cost?
2. Even if the supernet trains, do the corresponding discrete cells also improve in evaluation performance throughout α's training, despite common integrality gap issues? What kinds of failure modes occur?
3. How do the final discrete cells perform at evaluation, and how does RL-DARTS compare against random search? Can a large-scale joint optimization over multiple diverse environments lead to a single transferrable cell?

In order to study the behavior of RL-DARTS, we use the Procgen benchmark (Cobbe et al., 2019; 2020), which readily provides pre-existing baselines for both PPO (Schulman et al., 2017) and Rainbow DQN (Hessel et al., 2018) algorithms, over a diverse selection of 16 games, each with infinite levels to benchmark RL-DARTS in large data regimes where episodes may drastically change, relevant for generalization. We use the standard "easy" difficulty commonly benchmarked by a variety of other works (Raileanu et al., 2020; Raileanu & Fergus, 2021; Parker-Holder et al., 2021).

We also use the default IMPALA-CNN architecture (Espeholt et al., 2018) as a strong hand-designed baseline when comparing both supernet and discrete cell performances. IMPALA-CNN can be seen as specific instance of the stacked cell design in Subsection 3.1 and Figure 2, where its "Reduction Cell" consists of a [Conv3x3, MaxPool3x3 w/ Stride 2] with $R = 1$ and its "Normal Cell" consists of a residual layer with Conv3x3's and ReLU's, with $N = 2$. More details can be found in the original paper (Espeholt et al., 2018).

As for RL-DARTS's search space, we consider the following base ops $\mathcal{O}_{base}$, corresponding algorithms, and (N, R, I):

- **Classic + PPO:** $\mathcal{O}_{base,N}$ = {Conv3x3+ReLU, Conv5x5+ReLU, Dilated3x3+ReLU, Dilated5x5+ReLU} for normal ops and $\mathcal{O}_{base,R}$ = {Conv3x3, MaxPool3x3, AveragePool3x3} for reduction ops, which is standard in supervised learning (Liu et al., 2019; Zoph et al., 2018; Pham et al., 2018). We use $(N, R, I) = (1, 1, 4)$ to be comparable to the baseline.

- **Micro + Rainbow:** $\mathcal{O}_{base,N}$ = {Conv3x3, ReLU, Tanh}, a more fine-grained and novel search space which has not been used previously in SL. The inclusion of Tanh is motivated by its use previously for continuous control architectures (Salimans et al., 2017; Song et al., 2020). In order to avoid hidden confounding effects from the reduction cell when displaying the normal cell in figures, we use $(N, R, I) = (2, 0, 4)$, where reduction ops default to IMPALA-CNN's.

4.2 TRAINING THE SUPERNET

In SL, it is expected to see the supernet's asymptotic validation accuracy eventually reach a sufficient threshold, comparable (although slightly worse) to a discrete cell's validation accuracy (Liu et al., 2019; Li et al., 2020). The question is, can a RL supernet achieve the same result for training

reward? As mentioned earlier in the introduction, this is unclear as a negative feedback loop can occur where initially, a suboptimal supernet collects poor data for training, which leads to an even worse supernet, as α may potentially upweight suboptimal ops. However, we find that **training the supernet end-to-end works effectively, even with minimal hyperparameter tuning** for both PPO (Figure 3) and Rainbow (Figure 4), although PPO may take longer (50M steps) to reach comparable scores to IMPALA-CNN while Rainbow only needs 25M steps. However, this is a non-issue during discretization, as the α has already converged to a sparse solution (via softmax weight magnitudes) by 25M steps on PPO.

Figure 3: Left: Softmax op weights over all edges in the cell when training the supernet with PPO + "Classic" search space on Dodgeball. Zero op weight is not shown to improve clarity. Note that by 25M steps, the op choices have already converged towards a sparser solution. **Right:** Comparison between the supernet and vanilla IMPALA-CNN using [16,16,16] depths on various environments when using infinite levels.

Figure 4: Analogous settings with Figure 3 using Rainbow + "Micro" search space. **Left:** Softmax weights when training Rainbow with infinite levels on Bigfish, also converging towards a sparser solution. **Right:** Supernet vs IMPALA-CNN comparison with Rainbow.

Interestingly, on Dodgeball with PPO, we find that the process strongly downweights all base ops except for the standard Conv3x3+ReLU, with 5x5 ops possessing the lowest softmax weights. Conveniently, this provides an opportunity to understand whether α **downweights suboptimal ops throughout training.** We confirm this result in Table 1 by performing evaluations over standard IMPALA-CNN cells using either

Scenario	Conv 3x3	Conv 5x5
Train (Inf. levels)	**15.1 $\pm$ 2.5**	13.2 $\pm$ 2.3
Train (200 levels)	**12.1 $\pm$ 1.7**	9.8 $\pm$ 2.1
Test (from Train)	**10.2 $\pm$ 2.3**	5.9 $\pm$ 1.7

Table 1: PPO IMPALA-CNN evaluations (mean return at 50M steps) on Dodgeball. Learning curves can be found in Appendix B.1, Figure 12.

purely 3x3 or 5x5 convolutions for the whole network, and demonstrating that the 3x3 setting outperforms the 5x5 setting (especially in limited data (200 level) train/test regime), suggesting the signaling ability of α on op choice.

Scenario	Rainbow (25M Steps)		PPO (50M Steps)	
	Trainable α	Uniform α	With ReLU	No ReLU
Training (Inf. levels) Reward	**3.1 $\pm$ 0.5**	0.9 $\pm$ 0.2	**7 $\pm$ 0.9**	1.9 $\pm$ 0.3

Table 2: Supernet training rewards on Dodgeball. Learning curves can be found in Appendix A.

Although the training abilities of supernets in RL have been established, an important contrasting question now surfaces: *Can any supernet train?* The supernet possesses an incredibly dense set of weights, and thus one might wonder whether trainability occurs with any search space or settings. We answer in the negative, where a **poorly designed supernet can fail.** To show this clearly, we remove all ReLU nonlinearities from the "Classic" search space used for PPO (although ReLUs still exist in final MLP projections), as well as simply freeze α to be uniform for Rainbow, and find both cases

produce poor training in Table 2. **Thus, the supernet in RL provides important search signals in terms of reward and α during training, especially on the quality of a search space.**

We further provide computational efficiency metrics in Table 3, where we find that the practical wall-clock time required for training the supernet (i.e. the search cost) is very comparable with DARTS in SL (Liu et al., 2019), requiring only a few GPU days. We do note that unlike SL where the vast majority of the cost is due to the network, RL time cost is partially is based on non-network factors such as environment simulation, and thus wall-clock times may change depending on specific implementation.

Network	Search Cost in GPU Days (w/ specific algorithm)
IMPALA-CNN	1 (PPO), 0.5 (Rainbow)
"Classic" Supernet	2.5 (PPO)
"Micro" Supernet	1.5 (Rainbow)
CIFAR-10 Supernet (Liu et al., 2019)	4 (SL/Original DARTS)

Table 3: Computational Efficiency in terms of wall-clock time, achieved on a V100 GPU. For the RL cases (PPO + Rainbow), all networks use depths of $[16, 16, 16]$. Search cost in RL is defined as the wallclock time taken to reach 25M steps, rounded to the nearest 0.5 GPU day. We have also included reported time for DARTS in SL (Liu et al., 2019) as comparison.

4.3 DISCRETE CELL IMPROVEMENT

Due to the existence of *integrality gaps* in SL between a continuously relaxed supernet and its discrete cell (Wang et al., 2021b;a), this also raises the same question in RL. We answer this in the affirmative, demonstrating that even using the default δ discretization from (Liu et al., 2019) leads to both qualitative and quantitative improvements, although we leave potential improvements to future works.

In terms of **qualitative improvement**, we display discretized cells when training a supernet with Rainbow on the Starpilot environment in Figure 5. As we can see, the earlier cell is clearly a poor design in comparison to the later cell, with specific qualities mentioned in the caption. We provide more extensive cell evolution ablations for PPO in Figures 13, 14 in Appendix B.2, displaying more sophisticated yet still interpretable changes in cell topology.

Figure 5: Evolution of discovered cells over a DARTS optimization process. **Left**: A cell discovered in the early stage which is dominated by skip connections and only linear ops. **Right**: A cell discovered in the end which possesses several reasonable local structures similar to Conv + ReLU residual connections.

For **quantitative improvement**, as α changes during supernet training, so do the outputs of the discretization procedure on α. We collect all distinct discrete cells $\{\delta(\alpha_1), \delta(\alpha_2), ...\}$ into a sequence, and evaluate each cell's performance $\max_\theta J(\pi_{\theta, \delta(a_i)})\ \forall i$ via training from scratch for 25M steps, displayed in Figure 6. As we can see, the performance generally improves over time, indicating that supernet optimization selects better cells. However, we find that such behavior can be environment-dependent, as some environments possess less monotonic evaluation curves (see Figure 15 in Appendix B).

Figure 6: Evaluation of 9 distinct discrete cells in order from the trajectory of α on the Starpilot environment when using Rainbow.

One reason for why a **discretized cell may underperform is if its corresponding supernet fails to learn**. One simple reason is due to the inherent variance in RL training. For example, in Figure 7, we see that when using Rainbow and only varying the random seed while keeping all other settings fixed, an unlucky run occurs where "Supernet 2" does not learn and thus neither does its corresponding

discrete cell, while the inverse occurs with "Supernet 1" and its own discrete cell. The discrete cells' rewards can also be qualitatively explained (ex: see Figure 7's caption). We perform further studies in Appendix B.3, Figure 16, showing that supernet and discrete cell rewards are indeed correlated, but also have environment-dependent integrality gaps, suggesting that search quality can be improved via both better supernet training (Raileanu et al., 2020; Zhang et al., 2021), as well as better discretization procedures (Liang et al., 2019; Wang et al., 2021b).

(a) Two seeds for supernet runs, with corresponding discretized cell training curves.

(b) Discretized Cell 1

(c) Discretized Cell 2

Figure 7: (a) Two supernets trained on the Dodgeball environment using Rainbow, with corresponding discretized cells evaluated using 3 random seeds. **(b)** Discretized cell from Supernet 1. Note the similarity to regular Conv3x3 + ReLU designs. **(c)** Discretized cell from Supernet 2, which uses too many Tanh nonlinearities, known to cause vanishing gradient effects.

4.4 SINGLE GAME EVALUATIONS

As we have established above the search improvement capability of DARTS, we now focus our attention to comparisons between discrete architectures and baselines. We first present results in the standard scenario, where RL-DARTS is applied to each game independently, discretized at 25M steps.

Figure 8: Left 2x2 Plot: Examples of discrete cell evaluations using the "Classic" search space with PPO, with depths [64,64,64]. **Right:** Normal (Top) and Reduction (Bottom) cells found for "Plunder" which achieves faster training than IMPALA-CNN. Note the interesting use of 5x5 convolutional kernel sizes later in the cell.

We use random search as an important baseline to gauge the search space's difficulty (4×10^{11} total configurations possible). Since defining cost in terms of environment steps is only applicable to multi-trial blackbox optimization (Franke et al., 2020a) while RL-DARTS only trains one agent and thus one "trial", a fair comparison instead is to ensure total wall-clock time (with same hardware) stays equal, as common in (Liu et al., 2019). We thus use Table 3's data where a PPO supernet takes

2.5x longer to reach 25M steps, and round this to a random search budget of 3 cells and train them with depths [16, 16, 16] for 25M steps. The best of the 3 cells is used for full evaluation.

As we can see in Figure 8, random search underperforms quite significantly in many cases, which also shows IMPALA-CNN is a strong hand-designed baseline. **However, RL-DARTS with PPO is capable of finding architectures from scratch which outperform IMPALA-CNN on few environments such as Plunder and Heist, while maintaining competitive performance on others.** In terms of average performance over all 16 games using normalized scoring from (Cobbe et al., 2020), in Table 4 we see that RL-DARTS is competitive against IMPALA-CNN, and strongly outperforms random search.

	IMPALA-CNN	RL-DARTS (Discrete Cell)	Random Search
Avg. Normalized Reward	0.708	0.709	0.489

Table 4: Average normalized scores across all 16 environments w/ PPO. Full details and results (including Rainbow) are presented in Appendix C.

4.5   TRANSFER EVALUATION

Instead of performing the RL-DARTS by joint training a supernet across infinite levels within only *one game*, one may ask if it is possible to **joint train a supernet across *all games* over all infinite levels to find a single transferrable cell**, which may be of interest to practitioners seeking to find a common architecture general to a broad class of RL problems. We confirm this approach using Rainbow, where a learner performs gradient updates over actor replay data from all 16 games.

Figure 9: Left 2x2 Plot: Evaluation of the discrete cell joint-trained over all environments using depths [64,64,64,64,64] to emphasize comparison differences. **Right (Top):** Discrete cell found. **Right (Bottom):** Average Normalized rewards over all 16 games during supernet + baseline training.

5   CONCLUSION

Our research has demonstrated that in a minimally invasive way, it is entirely possible to apply DARTS to RL, a completely different optimization paradigm than SL, which DARTS was originally proposed for. We believe this work can open new doors to both NAS and RL communities alike. Especially for theorists and analysts of DARTS, RL is a completely new frontier for which to understand softmax routing and continuous relaxation techniques. Previous DARTS techniques (Wang et al., 2021b; Chu et al., 2020a; Liang et al., 2019) may be tested in the RL setting, and new RL-specific ways of discretization and training may also be proposed, which may increase the utility of RL-DARTS even more. For RL practitioners, RL-DARTS could be important to finding better architectures for large-scale robotics (James et al., 2019; Akinola et al., 2021), as well as transferable architectures in offline RL (Levine et al., 2020). Better RNNs for memory (Pritzel et al., 2017; Fortunato et al., 2019; Kapturowski et al., 2019) and adaptation (Duan et al., 2016; Wang et al., 2017) may also be searched end-to-end with DARTS.

6 STATEMENTS

Ethics Statement: The only relevant potential concerns in our work occur normally with general NAS methods, which can sacrifice model interpretability in order to achieve higher objectives. For the field of RL specifically, this may warrant more attention in AI safety when used for real world robotic pipelines. Furthermore, as with any NAS research, the initial phase of discovery and experimentation may contribute to carbon emissions due to the computational costs of extensive tuning. However, this is usually a means to an end, such as an efficient search algorithm, which this paper proposes with no extra hardware costs.

Reproducibility Statement: In Appendix D, we have discussed the explicit hyperparameters, as well as search space details in Subsection 4.1. The original DARTS implementation is readily available across the Github (e.g. `https://github.com/quark0/darts`) as it is a highly popular algorithm. Similarly, Procgen is publicly available (`https://github.com/openai/procgen`) along with its training code and details (Cobbe et al., 2020). For our case, we used TF-Agents, available at `https://www.tensorflow.org/agents`. Since our algorithm is relatively simple to assemble given preexisting pipelines, we believe that our approach should require minimal effort to reproduce.

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APPENDIX

A   WHAT AFFECTS SUPERNET TRAINING?

Given the positive training results we demonstrated in the main body of the paper, one may wonder, *can any supernet, no matter how poorly designed or setup, still train well in the RL setting?* If so, this would imply that the search method would not be producing meaningful, but instead, random signals.

We refute this hypothesis by performing ablations over our supernet training in order to have a better understanding of what components affect its performance. We ultimately show that the search space and architecture variables play a very significant role in its optimization, thus validating our method.

A.1   ROLE OF SEARCH SPACE

We remove the ReLU nonlinearities from the "Classic" search space, so that $\mathcal{O}_{base} = \{$Conv3x3, Conv5x5, Dilated3x3, Dilated5x5$\}$ and thus the DARTS cell consists of only linear operations. As shown in Fig. 10, this leads to a dramatic decrease in supernet performance, providing evidence that the search space matters greatly.

Figure 10: Supernet training using PPO on Dodgeball with infinite levels, when using the "Classic" search space with/without ReLU nonlinearities, under the same hyperparameters.

A.2   UNIFORM ARCHITECTURE VARIABLES

We further demonstrate the importance of the architecture variables α on training. We see that in Fig. 11, freezing α to be uniform throughout training makes the Rainbow agent unable to train at all. This suggests that it is crucial for α to properly route useful operations throughout the network.

Figure 11: Supernet training using Rainbow on Dodgeball with infinite levels, when using the "Micro" search space with/without trainable architecture variables α, under the same hyperparameters.

B   WHAT AFFECTS DISCRETE CELL PERFORMANCE?

B.1   SOFTMAX WEIGHTS VS DISCRETIZATION

As seen from Figure 3 in the main body of the paper, the DARTS supernet strongly downweights Conv5x5+ReLU operations when using the "Classic" search space with PPO. In order to verify the predictive power of the softmax weights, as a proxy, we thus also performed evaluations when using purely 3x3 or 5x5 convolutions on a large IMPALA-CNN with [64,64,64,64,64] depths. We see that the Conv3x3 setting indeed outperforms Conv5x5, corroborating the results in which during training, α strongly upweights the Conv3x3+ReLU operation and downweights Conv5x5+ReLU.

Figure 12: Large IMPALA-CNNs evaluated on Dodgeball using either Infinite or 200 levels with PPO. For the 200 level setting, lighter colors correspond to test performance.

B.2   DISCRETE CELL EVOLUTIONS

Along with Figure 5 in the main body of the paper, we also compare extra examples of discretizations before and after supernet training, to display reasonable behaviors induced by the trajectory of α.

In Figure 13, we use PPO with the "Classic" search space, but instead use $(N, R, I) = (1, 0, 6)$ along with outputting the last node (instead of concatenation with a Conv1x1 for the output) to allow a larger normal cell search space and graph topology. In Figure 14, the discretized cell initially uses a large number of skip connections as well as dead-end nodes. However, at convergence, it eventually utilizes all nodes to compute the final output. Curiously, we find that the skip connection between the input and output appears commonly throughout many searches.

Figure 13: Comparison of discretized cells before and after supernet training, on Starpilot using PPO with $I = 6$ nodes.

Figure 14: Comparison of discretized cells before and after supernet training, on Plunder using PPO with $I = 6$ nodes.

For the Rainbow setting, in Figure 6 in the main body of the paper, we saw that when the search process is successful, the supernet's training trajectory induces discretized cells which improve

evaluation performance as well. The cells discovered later generally perform better than cells discovered earlier in the supernet training process. In Figure 15, we show more examples of such evaluation curves.

Figure 15: Evaluated discretized cells discovered throughout training the supernet with Rainbow. To save computation, we evaluate every 2nd cell that was discovered.

B.3 CORRELATION BETWEEN SUPERNET AND DISCRETIZED CELLS

Given that the discretized cell only explicitly depends on architecture variables α and not necessarily model weights θ, one may wonder: *Is there a relationship between the rewards of the supernet and of its corresponding discretized cell?* For instance, the degenerate/underperformance setting mentioned in Section 4.4 and Appendix B can be thought of as an extreme scenario. At the same time, there could be an integrality gap, where there the discretization process $\delta(\alpha)$ produces cells which give different rewards than the supernet.

In order to make such an analysis comparing rewards, we first must prevent confounding factors arising from Rainbow's natural performance on an environment regardless of architecture. We thus first divide the supernet and discrete cell scores by the score obtained by the IMPALA-CNN baseline, where all networks use depths of $[16, 16, 16]$.

In Figure 16, when using Rainbow and observing across environments, we find both high correlation and also integrality gaps: for some environments such as Ninja and Coinrun, there is a significant correlation between supernet and discrete cell rewards, while for other environments such as Dodgeball, there is a significant gap. This suggests that search quality can be improved via both better supernet training such as using hyperparameter tuning or data augmentation (Raileanu et al., 2020), as well as better discretization procedures such as early stopping and stronger pruning (Chu et al., 2020a; Liang et al., 2019; Wang et al., 2021b).

Figure 16: Supernet and their corresponding discrete cell rewards across all environments in Procgen using Rainbow, after normalizing using IMPALA-CNN's performances. Thus, the black dashed line at 1.0 corresponds to IMPALA-CNN.

C NUMERICAL SCORES

In Tables 8 and 5b, we display the average normalized reward after 25M steps, as standard in Procgen (Cobbe et al., 2020), for a subset of environments in which RL-DARTS performs competitively. The normalized reward for each environment is computed as $R_{norm} = (R - R_{min})/(R_{max} - R_{min})$ where R_{max} and R_{min} are calculated using a combination of theoretical maximums and PPO-trained agents, and can be found in (Cobbe et al., 2020).

Env	IMPALA-CNN Baseline	RL-DARTS (Discrete)	Random Search
Bigfish	**0.60**	**0.60**	0.42
Bossfight	0.75	0.73	**0.81**
Caveflyer	0.75	0.47	**0.85**
Chaser	**0.71**	0.55	0.15
Climber	0.69	**0.90**	0.61
Coinrun	**0.91**	0.53	0.8
Dodgeball	0.53	**0.59**	0.29
Fruitbot	**0.92**	**0.93**	0.83
Heist	0.72	**0.89**	0.38
Jumper	0.62	0.76	**1.0**
Leaper	0.2	**0.28**	-0.28
Maze	**1.0**	**1.0**	0.0
Miner	0.74	**0.85**	0.70
Ninja	**0.87**	0.69	0.38
Plunder	0.57	**0.76**	0.43
Starpilot	0.71	**0.73**	0.40

(a) PPO + Classic

Env	IMPALA-CNN Baseline	RL-DARTS (Discrete)	Random Search
Bigfish	**0.71**	0.65	0.60
Bossfight	**0.54**	**0.48**	0.45
Caveflyer	-0.05	**-0.03**	**-0.01**
Chaser	**0.30**	**0.26**	0.22
Climber	**-0.04**	**-0.02**	**-0.05**
Coinrun	0.06	**0.21**	0.15
Dodgeball	**0.57**	**0.59**	-0.05
Fruitbot	**0.68**	**0.68**	**0.70**
Heist	**-0.48**	**-0.49**	**-0.47**
Jumper	**0.21**	**0.18**	0.17
Leaper	-0.07	-0.07	**-0.03**
Maze	**0.76**	**0.74**	0.51
Miner	**0.35**	-0.03	0.11
Ninja	0.03	0.13	**0.28**
Plunder	**0.14**	0.02	0.03
Starpilot	**0.91**	0.80	0.76

(b) Rainbow + Micro

Table 5: Normalized Rewards in ProcGen across different search methods, evaluated at 25M steps with depths [64,64,64]. Largest scores on the specific environment (as well as values within 0.03 of the largest) are **bolded**.

D HYPERPARAMETERS

In our code, we entirely use Tensorflow 2 for auto-differentation, as well as the April 2020 version of Procgen. For compute, we either used P100 or V100 GPUs based on convenience and availability. Below are the hyperparameter settings for specific methods. For all training curves, we use the common standard for reporting in RL (i.e. plotting mean and standard deviation across 3 seeds).

D.1 DARTS

Initially, we sweeped the softmax temperature in order to find a stable default value that could be used for all environments. For PPO, the sweep was across the set $\{5.0, 10.0, 15.0\}$. For Rainbow, the sweep was across $\{10.0, 20.0, 50.0\}$.

For tabular reported scores in Figures 8 and 5b, we used a consistent softmax temperature of 5.0 for PPO, and 10.0 for Rainbow.

D.2 RAINBOW-DQN

We use Acme (Hoffman et al., 2020) for our code infrastructure. We use a learning rate 5×10^{-5}, batch size 256, n-step size 7, discount factor 0.99. For the priority replay buffer (Schaul et al., 2016), we use priority exponent 0.8, importance sampling exponent 0.2, replay buffer capacity 500K. For particular environments (Bigfish, Bossfight, Chaser, Dodgeball, Miner, Plunder, Starpilot), we use n-step size 2 and replay buffer capacity 10K. For C51 (Bellemare et al., 2017), we use 51 atoms, with $v_{min} = 0, v_{max} = 1.0$. As a preprocessing step, we normalize the environment rewards by dividing the raw rewards by the max possible rewards reported in (Cobbe et al., 2020).

D.3 PPO

We use TF-Agents (Guadarrama et al., 2018) for our code infrastructure, along with equivalent PPO hyperparameters found from (Cobbe et al., 2020). Due to necessary changes in minibatch size when applying DARTS modules or networks with higher GPU memory usage, we thus swept learning rate across $\{1 \times 10^{-4}, 2.5 \times 10^{-4}, 5 \times 10^{-4}\}$ and number of epochs across $\{1, 2, 3\}$.

The default minibatchsize with a $[16, 32, 32]$ IMPALA-CNN is 2048. For other models, we use a maximum power of 2 minibatch size before encountering GPU out-of-memory issues on a standard 16 GB GPU. Thus, for a $[16, 16, 16]$ DARTS supernet, we set the minibatch size to be 256, which is also used for evaluation with a $[64, 64, 64]$ discretized CNN. Our hyperparameter gridsearch for the evaluation led to an optimal setting of learning rate $= 1 \times 10^{-4}$ and number of epochs $= 1$.