Invariant Spatiotemporal Representation Learning for Cross-patient Seizure Classification

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Abstract

Automatic seizure type classification from electroencephalogram (EEG) data can help clinicians to better diagnose epilepsy. Although many previous studies have focused on the classification problem of seizure EEG data, most of these methods require that there is no distribution shift between training data and test data, which greatly limits the applicability in real-world scenarios. In this paper, we propose an invariant spatiotemporal representation learning method for cross-patient seizure classification. Specifically, we first split the spatiotemporal EEG data into different environments based on heterogeneous risk minimization to reflect the spurious correlations. We then learn invariant spatiotemporal representations and train the seizure classification model based on the learned representations to achieve accurate seizure type classification across various environments. The experiments are conducted on the largest public EEG dataset, the Temple University Hospital Seizure Corpus (TUSZ) dataset, and the experimental results demonstrate the effectiveness of our method.

1 Introduction

Epilepsy is a pervasive neurological disease that affects individuals all over the world, with considerable cognitive, psychological, and social ramifications [3]. The mainstream approach to epilepsy diagnosis relies on EEG data to classify seizures [6, 7]. However, traditional methods based on human labor are not only costly, but also susceptible to human uncertainty, as these methods require clinicians to meticulously review extensive EEG recordings [15]. As a result, using machine learning techniques to automatically classify seizure type attract increasingly attentions.

Early machine learning methods for accurately classifying EEG data included Support Vector Machines (SVM), k-Nearest Neighbors (k-NN), and Bayesian methods [17, 29]. With the advancement of deep learning, Convolutional Neural Networks (CNNs) [31] and Recurrent Neural Networks (RNNs) [30] have been introduced. CNN-based methods typically aim at learning spatiotemporal feature representations of EEG signals through convolutional operations [4], exemplified by ACPA-ResNet [36]. RNNs, including CNN-BiRNN and CNN-Bi-LSTM [13, 22], capture temporal dependencies and dynamics. To address non-Euclidean geometric properties overlooked by CNNs and RNNs, Graph Neural Networks (GNNs) have been proposed to model the spatial relationships between EEG electrodes using a graph representation [8, 10, 16]. Methods such as REST [1], DCRNN [32], NeuroGNN [9] integrate GNNs with recurrent structures to enhance classification by capturing spatiotemporal dependencies and dynamic interactions.

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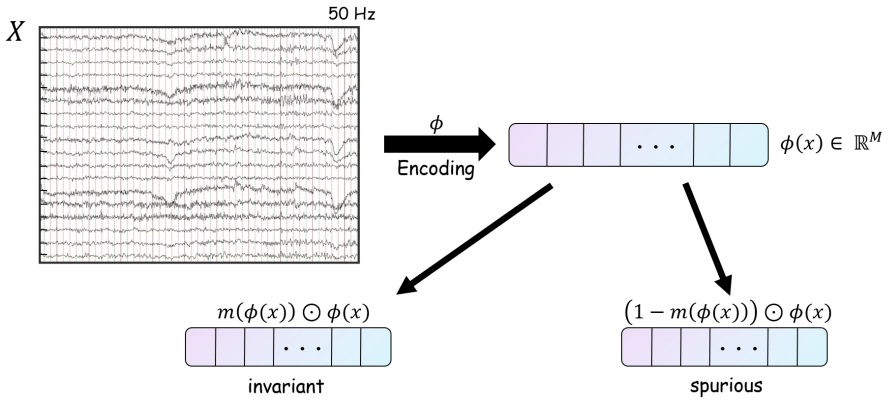

Figure 1: The invariant and spurious part of the EEG feature.

However, these aforementioned methods are predominantly patient-specific and rely on a consistent distribution between training and test sets, which limits their ability to address cross-patient problem [35]. This kind of problems can be partially attributed to the spatial-temporal evolution of EEG data, which is common in real-world scenario where data from different patients exhibit significant variability [20, 38]. Thus, for a group of new patients, it is very likely that this shift will impact the performance of models, leading to less precision and reduced generalizability. These challenges underscore the crucial and urgent need to develop robust cross-patient methods.

Previous methods addressing the cross-patient problem can be broadly categorized into three types. The first type involves unsupervised representation learning, particularly domain generalization, to initialize more robust representations for downstream tasks [34, 37]. The second category focuses on supervised model learning for OOD generalization, employing invariant risk minimization, causal learning, etc., to enhance end-to-end model performance in OOD scenarios [23–25]. The third category targets optimization techniques, particularly distributionally robust optimization (DRO), which aims to ensure worst-case performance under distributional shifts, offering theoretical guarantees and applicability across various existing methods [19, 27]. However, most of these methods ignore the spatiotemporal information, which leads to sub-optimal performance.

In this paper, we proposed a novel spatiotemporal invariant risk minimization loss to solve this problem. Specifically, we first use the invariant mask function to separate the raw EEG feature into the invariant representation and variant representation, and use the self-supervised learning (SSL) to guarantee the preserved invariant information is able to predict the invariant feature at next timestamp. In addition, we use the label information to generate the supervised signal to ensure the preserved invariant information can predict the seizure type. Finally, we use the variance of the gradient toward the mask function to control the time-varying variation of our methods in different patient groups.

We highlight our contributions as follows:

- We use the mask function to capture the invariant spatio temporal information in the raw EEG data and use such information for self-supervise learning.
- To further control the variation of the loss of the classification model, we use the variance of the gradient as the penalty to achieve invariant learning.
- The experiments on the largest public dataset verify the effectiveness of our method.

2 Preliminary

2.1 Problem Setup

The primary objective of the seizure classification task is to predict the seizure type from a given EEG signal clip. These clips were sliced from seizure EEGs using non-overlapping sliding windows with fixed temporal size T. For each sample, we denote $X \in \mathbb{R}^{T \times N \times M}$ as the EEG clip feature after preprocessing, where T is the temporal length of the EEG clip, N is the number of EEG

channels/electrodes, and M is the number of features obtained through Fast Fourier Transform (FFT). Meanwhile, we denote y as the seizure class label. For the independent identical distributed scenario, different clips from the same patient may appear in both the training and test sets. However, in real healthcare scenarios, patients in the test sets (a group of new patients) may completely unseen in the training set, leading to the cross-patient problem [39], which can be further formulated as follows: The patient set P is divided into two disjoint subsets, P_T and P_D, such that $P_T + P_D = P$ and $P_T \cap P_D = \emptyset$. Here, P_D is used for training, and P_T is used for testing.

2.2 Previous Graph-Based methods for EEGs

Graph Representing. Let $\mathcal{G} = \{\mathcal{V}, \mathcal{E}, \boldsymbol{W}\}$ denote the graph structure, where $\mathcal{V}$ is the set of nodes, $\mathcal{E}$ refers to the set of edge, and $\boldsymbol{W}$ is the adjacency matrix of the graph. In consideration of the distribution of nodes and the physiological properties of the brain, two distinct approaches to graph construction on EEG clips are evident. One undirected distance graph-based approach is to utilize the Euclidean distance between different nodes on standard 10-20 EEG electrode placement as the basis, followed by the threshold Gaussian kernel to determine the weights between v_i and v_j :

$$W_{ij} = \begin{cases} \exp\left(-\frac{\text{dist}(v_i, v_j)^2}{\sigma^2}\right) & \text{if dist}(v_i, v_j) \leq \kappa \\ 0 & \text{otherwise} \end{cases}$$

Where dist(v_i, v_j) represents the Euclidean distance between two nodes v_i and v_j, σ is the standard deviation of the distances, while κ is the threshold for sparsity.

An alternative approach, based on directed correlation graph, particularly focuses on the dynamic connectivity between different nodes. To evaluate the connectivity, only the weights that fall within the most k similar neighbors (including self-edges) are preserved to ensure the sparsity of the graph. The weight can be formulated as follows:

$$W_{ij} = \begin{cases} Corr(\mathbf{X}_{:,i,:}, \mathbf{X}_{:j,:}) & \text{if } v_j \in \mathcal{C}(v_i) \\ 0 & \text{otherwise} \end{cases}$$

Here, $X_{:,i,:}$ and $X_{:,j,:}$ denotes the preprocessed signals in v_i and v_j, $Corr(\cdot, \cdot)$ represents the pearson correlation coefficient, and $\mathcal{C}(v_i)$ referring to the most k similar neighbors of v_i.

Diffusion Convolutional Recurrent Neural Network. Previous works utilize the diffusion convolutional recurrent neural network (DCRNN) to effectively capture the temporal and spatial dependencies in EEG signals. To capture the temporal dependencies in EEG data, modified gated recurrent units (GRUs) are employed.

For spatial dependency, diffusion convolution provides significant insights into the influence exerted by each node on all others, and the extent of this kind of influence can be quantified by applying bidirectional random walk on the directed graph and calculating a K-step diffusion convolution. The diffusion convolution is defined by:

$$X_{:,m \star \mathcal{G}} f_\theta = \sum_{k=0}^{K-1} \left(\theta_{k,1}(D_O^{-1}W)^k + \theta_{k,2}(D_I^{-1}W^\intercal)^k\right) X_{:,m}, \quad m \in \{1, \ldots, M\},$$

where X is the preprocessed segment with N nodes and M features at time step $t \in \{1, \cdots, T\}$, $\theta \in \mathbb{R}^{K \times 2}$ are the parameters of the filter, and D_O and D_I are the out-degree and in-degree diagonal matrices of the graph. The transition matrices for the diffusion processes are $D_O^{-1}W$ and $D_I^{-1}W^\intercal$.

For undirected graphs, the process converts to ChebNet spectral graph convolution [5], using Chebyshev polynomial bases:

$$X_{:,m \star \mathcal{G}} f_\theta = \boldsymbol{\Phi}\left(\sum_{k=0}^{K-1} \theta_k \boldsymbol{\Lambda}^k\right)\boldsymbol{\Phi}^\intercal X_{:,m} = \sum_{k=0}^{K-1} \theta_k \mathbf{L}^k X_{:,m} = \sum_{k=0}^{K-1} \tilde{\theta}_k T_k(\tilde{L}) X_{:,m}, \quad m \in \{1, ..., M\},$$

where L denotes the scaled graph Laplacian, ensuring stability through Chebyshev polynomial bases.

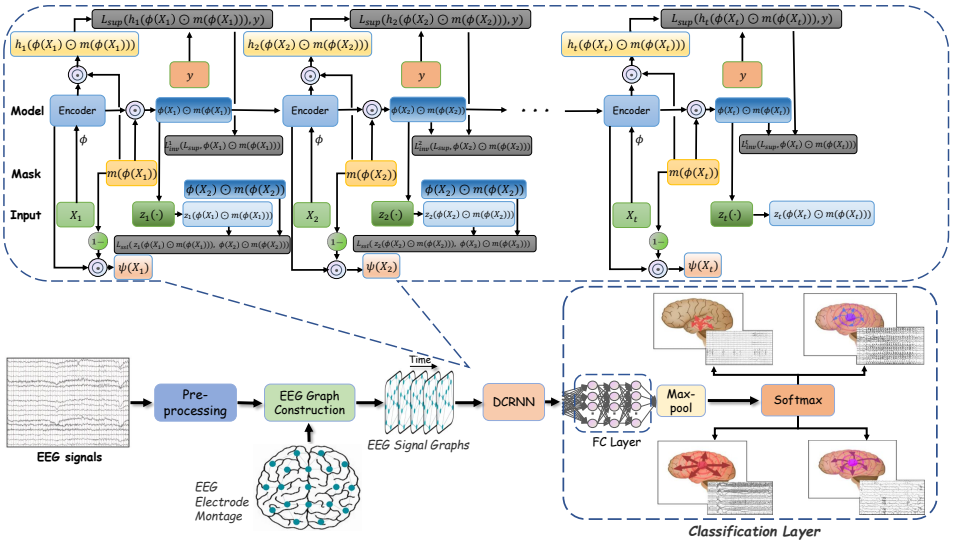

Figure 2: Overview of the proposed spatiotemporal invariant learning method.

3 Methodology

In a cross-patient scenario, we propose the spatiotemporal invariant risk minimization (ST-IRM) loss, making the prediction model ahieve both (a) accurately predicting patient's seizure type in each patient group; (b) The variation of prediction between the different groups are small. Specifically, for a timestamp t, we derive an invariant mask function $m(\cdot)$ to separate the raw EEG feature X_t into invariant representation $\phi(X_t) = m(X_t) \odot X_t$ and variant representation $\psi(X_t) = (1 - m(X_t)) \odot X_t$, where $m(X_t) \in [0,1]^{N \times M}$. Next, we introduce our method in detail step by step.

In time-series data, especially in the EEG data, there should be some correlation of the previous feature X_{t-1} with the current feature X_t [32]. Unlike the previous SSL approach that aims to learn a model $z_t(\cdot)$ to ensure $z_t(X_{t-1}) \approx X_t$, we claim that preserve the relation between $\psi(X_{t-1})$ and $\psi(X_t)$ may not be helpful due to the spurious correlation. Thus, the proposed SSL loss is as below:

$$\mathcal{L}_{ssl} = \frac{1}{|nT|} \sum_{i=1}^{n} \sum_{t=1}^{T} \mathcal{L}(z_{t-1}(\phi(X_{t-1}^i) \odot m(\phi(X_{t-1}^i))), \phi(X_{t-1}^i) \odot m(\phi(X_t^i))),$$

where $\mathcal{L}(\cdot,\cdot)$ is the loss function such as mean-square-error loss and $X_t^i \in \mathbb{R}^{N \times M}$ is the preprocessed signal for sample i at timestamp t. In addition, we want the information preserved by the mask function can not only predict the next invariant feature but also can predict the final seizure type, thus we use the following loss to provide the supervised signal for training the mask function:

$$\mathcal{L}_{sup} = \frac{1}{|n|} \sum_{i=1}^{n} \mathcal{L}(h_T(\phi(X_T^i) \odot m(\phi(X_T^i))), y_i),$$

where $h_T(\cdot)$ is the classification model and y_i is the ground truth label.

In addition, an ideal mask function ϕ should be able to capture the invariant feature from raw EEG data. Thus, for a specific timestamp t, the object function is composed of two major terms:

$$\mathcal{L}_{inv}^t = \mathbb{E}_{g \in \mathcal{G}} \mathcal{L}_{sup}^{g,t} + \lambda \left\| \mathrm{Var}_{g \in \mathcal{G}} \left(\nabla_{\Theta^{\mathrm{m}}} \mathcal{L}_{sup}^{g,t} \cdot (\phi(X_t) \odot m(\phi(X_t))) \right) \right\|^2,$$

where $\mathcal{L}_{sup}^{g,t}$ is the loss in group g at time t, Θ^{m} is the parameter of the mask function, and λ is the hyper parameter. For further incorporating the spatiotemporal information, because the more information being observed, the more accurate classification should be, we propose the weight decay loss below to illustrate these things:

$$\mathcal{L}_{inv} = \sum_{t=1}^{T} w^{T-t} \mathcal{L}_{inv}^t,$$

	12-s			60-s		
Method	F1	Recall	Precision	F1	Recall	Precision
CNN-LSTM	0.596 ± 0.035	0.654 ± 0.030	0.647 ± 0.036	0.623 ± 0.028	0.661 ± 0.030	0.647 ± 0.036
LSTM	0.690 ± 0.043	0.724 ± 0.033	0.725 ± 0.041	0.692 ± 0.011	0.718 ± 0.007	0.717 ± 0.017
Dense-CNN	0.657 ± 0.069	0.690 ± 0.053	0.694 ± 0.049	0.653 ± 0.085	0.704 ± 0.057	0.659 ± 0.118
MSTGCN	0.670 ± 0.031	0.719 ± 0.023	0.734 ± 0.029	0.647 ± 0.046	0.696 ± 0.027	0.694 ± 0.030
NeuroGNN	0.647 ± 0.040	0.710 ± 0.024	0.744 ± 0.030	0.698 ± 0.044	0.733 ± 0.042	0.714 ± 0.056
Corr-DCRNN	0.729 ± 0.058	0.756 ± 0.041	0.752 ± 0.047	0.672 ± 0.038	0.712 ± 0.021	0.705 ± 0.029
Dist-DCRNN	0.713 ± 0.044	0.735 ± 0.043	0.734 ± 0.045	0.695 ± 0.028	0.735 ± 0.013	0.738 ± 0.021
PANN-DCRNN	0.728 ± 0.052	0.753 ± 0.042	0.755 ± 0.041	0.684 ± 0.023	0.717 ± 0.016	0.720 ± 0.024
ST-InvDCRNN(ours)	$\mathbf{0.748 \pm 0.038}$	$\mathbf{0.772 \pm 0.028}$	$\mathbf{0.764 \pm 0.043}$	$\mathbf{0.713 \pm 0.043}$	$\mathbf{0.741 \pm 0.024}$	$\mathbf{0.742 \pm 0.037}$

Table 1: Performance comparison of different methods under 12-second and 60-second scenario.

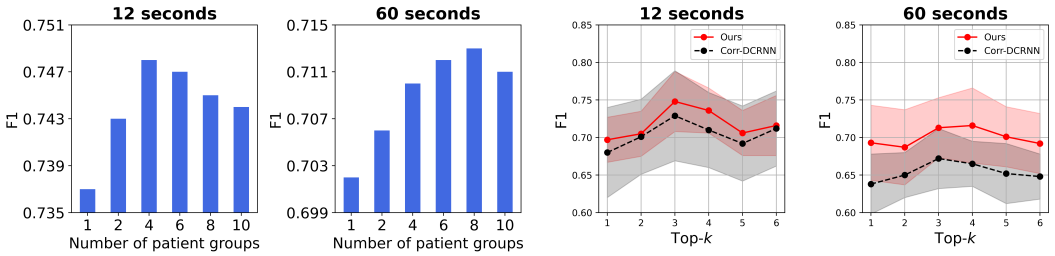

Figure 3: F1 under different numbers of patient groups (the two subfigures on the left) and different values of hyper-parameter top-k to control the graph sparsity (the two subfigures on the right).

where $w \in (0, 1)$ is the weight decay rate. The final proposed ST-IRM loss is:

$$\mathcal{L}_{ST-IRM} = \mathcal{L}_{ssl} + \alpha \mathcal{L}_{sup} + \beta \mathcal{L}_{inv},$$

where α and β are the hyper-parameters.

4 Experiments

4.1 Experimental Settings

Datasets. Following previous works [18, 28, 33], we utilized the Temple University Hospital EEG Seizure Corpus (TUSZ) dataset, which is the largest public dataset for our experiments. Specifically, we use the version v1.5.2 of the TUSZ dataset. The TUSZ dataset contains 5,612 EEG signals, and 3,050 annotated seizure events from over 300 patients, covering eight seizure types. The EEG signal was recorded using 19 electrodes from the standard 10-20 system [12].

Data preprocessing and Experiment Details. We follow Tang et al. [32] to preprocess the data. Following prior methodologies [2], EEG recordings were resampled to 200Hz and segmented into non-overlapped 60-second windows (clips). For seizure classification, only clips that contain a single type of seizure are considered. If a seizure event ends and another begins within the same clip, it is truncated and zero-padded to preserve a 60-second duration. Each 60-second clip is then segmented into 1-second intervals. The Fast Fourier Transform (FFT) algorithm is applied to each segment to obtain the logarithmic amplitudes of non-negative frequency components, as is outlined in Tang et al. [32]. Consequently, each 60-second clip is transformed into a sequence of 60 log-amplitude vectors. In addition, following recent studies on seizure type classification [2, 32], we use weighted F1-score as the main evaluation metric with precision and recall as well to measure the classification performance. See Appendix A for more experiment protocols and details.

Baselines. We compare our proposed method with CNN-based method: **DenseCNN** [26], RNN-based method: **LSTM** [11], and hybrid approach that combine CNN and RNN: **CNN-LSTM** [2]. We also compared our method with GNN-based methods: **MSTGCN** [14], **Dist-DCRNN** [32], **Corr-DCRNN** [32], **NeuroGNN** [9], and **PANN** [39].

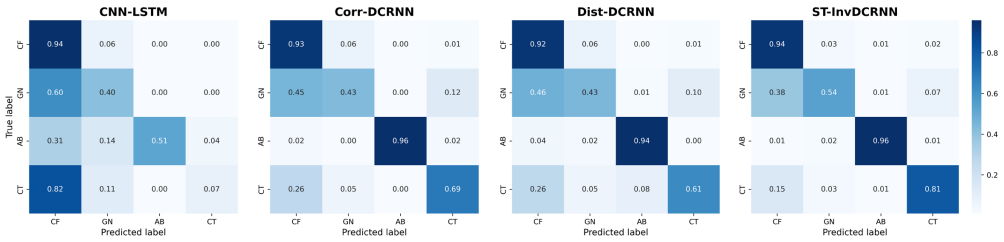

Figure 4: Confusion matrices for four classes of seizures.

4.2 Performance Analysis

Table 1 shows the performance of our method compared with various baseline methods, evaluating with three metrics, i.e., weighted F1, Recall, and Precision scores. First, the DCRNN-based model achieves competitive performance among all baselines. Second, our method significantly outperforms the baselines under both scenarios with 12-second and 60-second clip windows. Note that we adopt DCRNN as a backbone in the experiment, which is shown in Figure 2, and the superior against DCRNN-based methods demonstrates the effectiveness of our invariant learning framework.

4.3 In-Depth Analysis

To comprehensively evaluate the proposed invariant learning method, we conduct three in-depth analyses of the number of patient groups, the value of hyper-parameter top-k, and the classification confusion matrix, respectively. Note that the patients are clustered into groups according to their EEG recordings, and the two subfigures on the left of Figure 3 show that different numbers of groups result in varying performance. In the scenario of 12-second clip windows, the best choice for group number is 4, while in the 60-second case, the best value is 8. Our method outperforms Corr-DCRNN with top-k ranging from 1 to 6, and the highest F1 is achieved when top-k is around 3 for both scenarios. In addition, we provide the results of the recall metric in Appendix B.

Figure 4 presents the confusion matrices for four seizure classification models. The comparison highlights the improved performance of our method across multiple seizure classes. In particular, the ST-InvDCRNN demonstrates superior accuracy in distinguishing between different seizure types, providing more distinct class separations, with fewer misclassifications compared to other models. A notable example is its performance in identifying the CT class, where it achieves an impressive 0.81 accuracy. This significantly surpasses the results of other methods, which tend to exhibit higher levels of confusion, especially when differentiating between CF and CT. Besides, our method achieves an accuracy of 0.54 in classifying GN seizures, significantly outperforming the baseline models, which only reach 0.40 (CNN-LSTM), 0.43 (Corr-DCRNN), and 0.43 (Dist-DCRNN). Our method shows a marked reduction in confusion between these classes, thereby providing a more reliable and accurate classification. These results demonstrate the effectiveness of the ST-InvDCRNN in handling complex seizure types where other methods struggle.

5 Conclusion

Epilepsy remains a significant global health challenge, with traditional EEG-based diagnostic methods posing limitations due to their reliance on clinicians' review. With the recent advancement of deep learning, techniques such as CNNs, RNNs, and GNNs are proposed to automatically classify the seizure type. However, existing methods often lack cross-patient robustness and guarantee, which is very common in practice. In addition, most of the methods addressing the cross-patient problem ignore the spatiotemporal information. To bridge this gap, we propose a spatiotemporal invariant risk minimization approach that addresses these challenges by adopting self-supervised learning and capturing time-varying invariant features. Experimental results on the largest public dataset verify the effectiveness of our approach, demonstrating its potential to advance epilepsy diagnosis in the cross-patient scenario. One of the possible limitations is to investigate a more efficient way to learn the model parameter and reduce the complexity while maintaining the classification performance.

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Appendix

A Experimental Details

We tune the following hyper-parameters on the validation set.

- $lr_init \in [1e-5, 5e-3]$, the initial learning rate;
- top-$k \in \{1, 2, 3, 4, 5, 6\}$, the number of neighbors included in the correlation graphs for each node;
- $K \in \{2, 3, 4\}$, the maximum diffusion step;
- $d \in [0, 0.7]$, the dropout probability in the prediction networks.
- $e \in [20, 40, 60, 80, 100]$, the number of training epochs.

Each batch has 40 EEG clips and the cosine annealing learning rate scheduler [21] is adopted.

B Additional Evaluation Results

Figure 5 shows the weighted F1 and the Recall scores to evaluate the performance of our method under different number of patient groups, for both 12-second and 60-second clip windows. The results show that the F1 score increases with the number of patient groups, reaching its peak at 4 groups for the 12-second window and 8 groups for the 60-second window, before declining. A similar trend is observed for the Recall-score, which also attains its highest value at 4 groups for the 12-second case and 8 groups for the 60-second case.

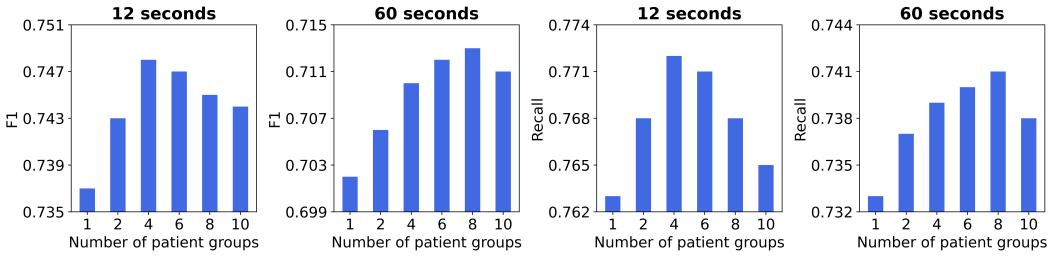

Figure 5: Performance under different numbers of patient groups.

Figure 6 presents a comparison of the performance of our method and Corr-DCRNN, based on the F1 score and Recall score, under varying top-k values, for both 12-second and 60-second clip windows. As the top-k value increases from 1 to 3, both the F1 score and Recall score of our method exhibit an overall upward trend, reaching their respective peaks at top-$k = 3$, while Corr-DCRNN exhibits a less pronounced improvement and does not reach the same peak performance as our method, ST-InvDCRNN. These results indicate that ST-InvDCRNN outperforms Corr-DCRNN across all top-k values, with the optimal performance occurring at top-$k = 3$ for both cases. This trend highlights the effectiveness of ST-InvDCRNN.

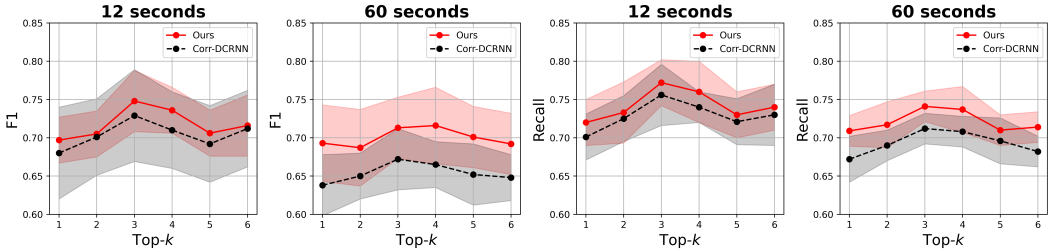

Figure 6: Performance under different values of top-k.