CONVOLVING DNA USING TWO-DIMENSIONAL HILBERT CURVE REPRESENTATIONS

ABSTRACT

The folding structure of the DNA molecule combined with helper molecules, also referred to as the chromatin, is highly relevant for the functional properties of DNA. The chromatin structure is largely determined by the underlying primary DNA sequence, though the interaction is not yet fully understood. In this paper we develop a convolutional neural network that predicts key determinants of chromatin structure from primary DNA sequence. Our experiments show that the method outperforms several existing methods both in terms of prediction accuracy and training time.

1 INTRODUCTION

DNA is perceived as a sequence over the letters $\{A,C,G,T\}$, the alphabet of nucleotides. This sequence constitutes the code that acts as a blueprint for all processes taking place in a cell. But beyond merely reflecting primary sequence, DNA is a molecule, which implies that DNA assumes spatial structure and shape. The spatial organization of DNA is achieved by integrating ("recruiting") other molecules, the histone proteins, that help to assume the correct spatial configuration. The combination of DNA and helper molecules is called chromatin; the spatial configuration of the chromatin, finally, defines the functional properties of local areas of the DNA (de Graaf & van Steensel, 2013).

Chromatin can assume several function-defining *epigenetic states*, where states vary along the genome (Ernst et al., 2011). The key determinant for spatial configuration is the underlying primary DNA sequence: sequential patterns are responsible for recruiting histone proteins and their chemical modifications, which in turn give rise to or even define the chromatin states. The exact configuration of the chromatin and its interplay with the underlying raw DNA sequence are under active research. Despite many enlightening recent findings (e.g. Brueckner et al., 2016; The EN-CODE Project Consortium, 2012; Ernst & Kellis, 2013), comprehensive understanding has not yet been reached. Methods that predict chromatin related states from primary DNA sequence are thus of utmost interest.

In machine learning, many prediction methods are available, of which deep neural networks have recently been shown to be promising in many applications (LeCun et al., 2015). Also in biology deep neural networks have been shown to be valuable (see Angermueller et al. (2016) for a review), though there is still room for improvement. We hypothesize that changing the input representation from sequential to a 2D image-like representation enhances the predictive power of neural networks, based on the following three arguments. First, existing convolutional neural network (CNN) based approaches for genome sequence data directly operate on the sequence (e.g. Nguyen et al., 2016); however, CNNs have been optimized for multi-dimensional input, such as in image classification (Simonyan & Zisserman, 2014). Second, treating genome sequence data as just a sequence neglects its inherent and biologically relevant spatial configuration. Third, due to the lack of comprehensive understanding with respect to the structure of the chromatin, sensible suggestions for higher-dimensional representations of DNA do not exist. In summary, despite being highly desirable, higher-dimensional representations of DNA that cater to the particular power of CNN-based applications and better resemble the molecular structure of the DNA molecule have not yet been presented.

To better take the spatial features of DNA sequences into account, this paper presents a novel kind of DNA representation by mapping DNA sequences to higher-dimensional images using space-filling curves. Space-filling curves map a 1-dimensional line to a 2-dimensional space by mapping each element of the sequence to a pixel in the 2D image. By doing so, proximal elements of the sequence will stay in close proximity to one another, while the distance between distal elements is reduced. In this work, we show that representing DNA-sequences with 2D images using space-filling curves improves on the currently available methods from (Pahm et al., 2005; Higashihara et al., 2008; Nguyen et al., 2016) in terms of both prediction accuracy of epistatic state and efficiency.

The space-filling curve that will be used in this work is the Hilbert-curve which has several advantages. **(i)**: [Continuity] Hilbert curves optimally ensure that the pixels representing two sequence elements that are close within the sequence are also close within the image Bader (2016); Aftosmis et al. (2004). **(ii)**: [Clustering property] Cutting out rectangular subsets of pixels yields a minimum amount of disconnected subsequences Moon et al. (2001). **(iii)**: If a rectangular subimage cuts out two subsequences that are disconnected in the original sequence, chances are maximal that the two different subsequences are relatively far apart (see our analysis in Appendix A).

The combination of these points arguably renders Hilbert curves an interesting choice for representing DNA sequence as two-dimensional images. **(i)** is a basic requirement for mapping short-term sequential relationships, which are ubiquitous in DNA (such as codons, motifs or intron-exon structure). **(ii)** relates to the structure of the chromatin, which - without all details being fully understood - is tightly packaged and organized in general. Results from Elgin (2012) indicate that when arranging DNA sequence based on Hilbert curves, contiguous areas belonging to identical chromatin states cover rectangular areas. In particular, the combination of **(i)** and **(ii)** motivate the application of convolutional layers on Hilbert curves derived from DNA sequence: rectangular subspaces, in other words, submatrices encoding the convolution operations, contain a minimum amount of disconnected pieces of DNA. **(iii)** finally is beneficial insofar as long-term interactions affecting DNA can also be mapped. This in particular applies to so-called enhancers and silencers, which exert positive (enhancer) or negative (silencer) effects on the activity of regions harboring genes, even though they may be far apart from those regions in terms of sequential distance.

1.1 Related Work

Since Watson and Crick first discovered the double-helix model of DNA structure in 1953 (Watson & Crick, 1953), researchers have attempted to interpret biological characteristics from DNA. DNA sequence classification is the task of determining whether a sequence S belongs to an existing class C, and this is one of the fundamental tasks in bio-informatics research for biometric data analysis (Z. Xing, 2010). Many methods have been used, ranging from statistical learning (Vapnik, 1998) to machine learning methods (Michalski et al., 2013). Deep neural networks (LeCun et al., 2015) form the most recent class of methods used for DNA sequence classification (R.R. Bhat, 2016; Salimans et al., 2016; Zhou & Troyanskaya, 2015; Angermueller et al., 2016).

To the best of our knowledge, only few other works aim to predict chromatin state from sequence. Both Pahm et al. (2005) and Higashihara et al. (2008) use support vector machines (SVM) to predict chromatin state from DNA sequence features. While Pahm et al. (2005) use the entire set of features as input to the SVM, Higashihara et al. (2008) use random forests to pre-select a subset of features that are expected to be highly relevant for prediction of chromatin state to use as input to the SVM. Only Nguyen et al. (2016) use a CCN as we do. There are two major differences between their approach and ours. First and foremost, while we use a space-filling curve to transform the sequence data into an image-like tensor, Nguyen et al. (2016) keep the sequential form of the input data. Second, the model architecture is different: the network in Nguyen et al. (2016) consists of two convolution layers followed by pooling layers, a fully connected layer and a sigmoid layer, while our model architecture is more complicated (see Methods). Residual connections are applied in our network to encourage the reuse of learned features, and the network is far deeper. The main difference is the format of the input: we use images as input for the network while their model uses sequences. Apart from Elgin (2012), the only example we are aware of where Hilbert curves were used to map DNA sequence into two-dimensional space is from Anders (2009), who demonstrated the power of Hilbert curves for visualizing DNA. Beyond our theoretical considerations, these last two studies suggest there are practical benefits of mapping DNA using Hilbert curves.

1.2 CONTRIBUTION

Our contributions are twofold. First, we predict chromatin state using a CNN that, in terms of architecture, resembles conventional CNNs for image classification. Second, we propose a method to transform DNA sequence patches into two-dimensional image-like arrays to enhance the strengths of CNNs using space-filling curves, in particular the Hilbert curve. Our experiments demonstrate the benefits of our approach: the developed CNN outperforms all existing approaches for predicting the chromatin state in terms of both prediction accuracy and runtime, an improvement which is further enhanced by the convolution of DNA sequence to a 2D image. In summary, we present a novel, powerful way to harness the power of CNNs in image classification for predicting biologically relevant features from primary DNA sequence.

2 METHODS

2.1 DNA SEQUENCE REPRESENTATION

We transform DNA sequences into images through three steps. First, we represent a sequence as a list of k-mers. Next, we transform each k-mer into a one-hot vector, which results in the sequence being represented as a list of one-hot vectors. Finally, we create an image-like tensor by assigning each element of the list of k-mers to a pixel in the image using Hilbert curves. Each of the steps is explained in further detail below.

From a molecular biology point of view, the nucleotides that constitute a DNA sequence do not mean much individually. Instead, nucleotide motifs play a key role in protein synthesis. In bioinformatics it is common to consider a sequence's k-mers, defined as the k-letter words from the alphabet {A,C,G,T} that together make up the sequence. In computer science the term q-gram is more frequently used, and is often applied in text mining (Tomovic et al., 2006). As an example, the sequence TGACGAC can be transformed into the list of 3-mers {TGA, GAC, ACG, CGA, GAC} (note that these are overlapping). The first step in our approach is thus to transform the DNA sequence into a list of k-mers. Previous work has shown that 3-mers and 4-mers are useful for predicting epigenetic state (Pahm et al., 2005; Higashihara et al., 2008). Through preliminary experiments, we found that $k = 4$ yields the best performance: lower values for k result in reduced accuracy, while higher values yield a high risk of overfitting. Only for the Splice dataset (see experiments) we used $k = 1$ to prevent overfitting, as this is a small dataset.

In natural language processing, it is common to use word embeddings as GloVe or word2vec or one-hot vectors (Goldberg, 2017). The latter approach is most suitable for our method. Each element of such a vector corresponds to a word, and a vector of length N can thus be used to represent N different words. A one-hot vector has a one in the position that corresponds to the word the position is representing, and a zero in all other positions. In order to represent all k-mers in a DNA sequence, we need a vector of length 4^k, as this is the number of words of length k that can be constructed from the alphabet {A,C,G,T}. For example, if we wish to represent all 1-mers, we can do so using a one-hot vector of length 4, where A corresponds to [1 0 0 0], C to [0 1 0 0], G to [0 0 1 0] and T to [0 0 0 1]. In our case, the DNA sequence is represented as a list of 4-mers, which can be converted to a list of one-hot vectors each of length $4^4 = 256$.

Our next step is to transform the list of one-hot vectors into an image. For this purpose, we aim to assign each one-hot vector to a pixel. This gives us a 3-dimensional tensor, which is similar in shape to the tensor that serves as an input to image classification networks: the color of a pixel in an RGB-colored image is represented by a vector of length 3, while in our approach each pixel is represented by a one-hot vector of length 256.

What remains now is to assign each of the one-hot vectors in the list to a pixel in the image. For this purpose, we can make use of space-filling curves, as they can map 1-dimensional sequences to a 2-dimensional surface preserving continuity of the sequence (Bader, 2016; Aftosmis et al., 2004). Various types of space-filling curves are available. We have compared the performance of several such curves, and concluded that Hilbert curves yield the best performance (Appendix A). This corresponds with our intuition: the Hilbert curve has several properties that are advantageous in the case of DNA sequences, as discussed in the introduction section.

The Hilbert curve is a well-known space-filling curve that is constructed in a recursive manner: in the first iteration, the curve is divided into four parts, which are mapped to the four quadrants of a square (Fig. 1a). In the next iteration, each quadrant is divided into four sub-quadrants, which, in a similar way, each hold 1/16th of the curve (Fig. 1b). The quadrants of these sub-quadrants each hold 1/64th of the curve, etc (Figs. 1c and d).

By construction, the Hilbert curve yields a square image of size $2^n \times 2^n$, where n is the order of the curve (see Fig. 1). However, a DNA sequence does not necessarily have $2^n * 2^n$ k-mers. In order to fit all k-mers into the image, we need to choose n such that $2^n * 2^n$ is at least the number of k-mers in the sequence, and since we do not wish to make the image too large, we pick the smallest such n. In many cases, a large fraction of the pixels then remains unused, as there are fewer k-mers than pixels in the image. By construction, the used pixels are located in upper half of the image. Cropping the picture by removing the unused part of the image yields rectangular images, and increases the fraction of the image that is used (Figure 1e).

In most of our experiments we used sequences with a length of 500 base pairs, which we convert to a sequence of 500 - 4 + 1 = 497 4-mers. We thus need a Hilbert curve of order 5, resulting in an image of dimensions $2^5 \times 2^5 \times 256 = 32 \times 32 \times 256$ (recall that each pixel is assigned a one-hot vector of length 256). Almost half of the resulting 1024 pixels are filled, leaving the other half of the image empty which requires memory. We therefore remove the empty half of the image and end up with an image of size $16 \times 32 \times 256$.

The data now has the appropriate form to input in our model.

(a) Order=1   (b) Order=2

(c) Order=3   (d) Order=4   (e) Cropped image

Figure 1: Hilbert Curve and cropped image

2.2 NETWORK ARCHITECTURE

Modern CNNs or other image classification systems mainly focus on gray-scale images and standard RGB images, resulting in channels of length 1 or 3, respectively, for each pixel. In our approach, each pixel in the generated image is assigned a one-hot vector representing a k-mer. For increasing k, the length of the vector and thus the image dimension increases. Here, we use $k = 4$ resulting in 256 channels, which implies that each channel contains very sparse information. Due to the curse of dimensionality standard network architectures applied to such images are prone to severe overfitting.

Here, we design a specific CNN for the kind of high dimensional image that is generated from a DNA sequence. The architecture is inspired by the ResNet (He et al., 2015) and Inception (Szegedy et al., 2015). The network has L layers and each layer implements a non-linear function $\mathcal{F}_l(x_l)$ where l is

Figure 2: A simplified version of HCNN with two computational blocks

the index of the hidden layer with output x_{l+1}. The function $\mathcal{F}_l(x_l)$ consists of various layers such as convolution (denoted by c), batch normalization (bn), pooling (p) and non-linear activation function (af).

The first part of the network has the objective to reduce the sparseness of the input image (Figure 2, and consists of the consecutive layers $[c, bn, c, bn, af, p]$. The main body of the network enhances the ability of the CNN to extract the relevant features from DNA space-filling curves. For this purpose, we designed a specific Computational Block inspired by the ResNet residual blocks (He et al., 2015). The last part of the network consists of 3 fully-connected layers, and softmax is used to obtain the output classification label. The complete model is presented in Table 1, and code will be provided on Github upon publication of the paper. A simplified version of our network with two Computational Blocks is illustrated in Figure 2.

Computation Block. In the Computation Block first the outputs of two Residual Blocks and one identity mapping are summed, followed by a bn and an af layer (Figure 2). In total, the computational block has 4 convolutional layers, two in each Residual Block (see Figure 3). The Residual Block first computes the composite function of five consecutive layers, namely $[c, bn, af, c, bn]$, followed by the concatenation of the output with the input tensor. The residual block concludes with an af.

The Residual Block can be viewed as a new kind of non-linear layer denoted by $Residual_l[k_j, k_{j+1}, d_{link}, d_{out}]$, where k_j and k_{j+1} are the respective filter sizes of the two convolutional layers. d_{link} and d_{out} are the dimensions of the outputs of the first convolutional layer and the Residual Block, respectively, where $d_{link} < d_{out}$; this condition simplifies the network architecture and reduces the computational cost. The Computational Block can be denoted as $\mathcal{C}[k1, k2, k3, k4]$ with the two residual blocks defined as $Residual_1[k_1, k_2, d_{link}, d_{out}]$ and $Residual_2[k_3, k_4, d_{link}, d_{out}]$. Note that here we chose the same d_{link} and d_{out} for both Residual Blocks in a Computational Block.

Figure 3: Residual Block

Implementation details. Most convolutional layers use small squared filters of size 2, 3 and 4, except for the layers in the first part of the network, where large filters are applied to capture long range features. We use Exponential Linear Units (ELU, Clevert et al. (2015)) as our activation function af to reduce the effect of gradient vanishing: preliminary experiments showed that ELU preformed significantly better than other activation functions (data not shown).

For the pooling layers p we used Average pooling. Average pooling outperformed Max pooling in terms of prediction accuracy by more than 2% in general, as it reduces the high variance of the sparse generated images. Cross entropy was used as the loss function.

Table 1: Network Architecture. The output size is given as height, width, channels.

Layers	Description	Output size
Input		16,32,256
Conv1	7×7 conv, BN	16,32,64
Conv2	5×5 conv, BN	16,32,64
Activation		
Average-Pool	2×2 filter, stride 2	8,16,64
ComputationBlock	[8,4,4,3], $d_{link} = 4$	8,16,32
ComputationBlock	[3,3,3,3], $d_{link} = 4$	8,16,32
Average-Pool	2×2 filter, stride 2	4,8,32
ComputationBlock	[2,4,4,3], $d_{link} = 4$	4,8,32
ComputationBlock	[2,2,2,2], $d_{link} = 4$	4,8,32
ComputationBlock	[3,2,2,3], $d_{link} = 4$	4,8,32
Average-Pooling	2×2 filter, stride 2	2,4,32
BN,Activation		
Average-Pool	2×2 filter, stride 2	1,2,32
Classification layer1	64D FC layer	
	activation	
	dropout with 0.5	
Classification layer2	100D FC layer	
	activation	
	dropout with 0.5	
Classification layer3	50D FC layer, softmax	

Table 2: DNA Datasets

Name	♯Samples	Description
H3	14965	H3 occupancy
H4	14601	H4 occupancy
H3K9ac	27782	H3K9 acetylation relative to H3
H3K14ac	33048	H3K14 acetylation relative to H3
H4ac	34095	H4 acetylation relative to H3
H3K4me1	31677	H3K4 monomethy-lation relative to H3
H3K4me2	30683	H3K4 dimethylation relative to H3
H3K4me3	36799	H3K4 trimethylation relative to H3
H3K36me3	34880	H3K36 trimethylation relative to H3
H3K79me3	28837	H3K79 trimethylation relative to H3
Splice	3190	Splice-junction Gene Sequences

3 EXPERIMENTS

We test the performance of our approach using ten public available datasets from Pokholok et al. (2005). The datasets contain DNA subsequences with a length of 500 base pairs. Each sequence is labeled either as "positive" or "negative", indicating whether or not the subsequence contains regions that are wrapped around a histone protein. The ten datasets each consider a different type of histone protein, indicated by the name of the dataset. Details can be found in Table 5.

A randomly chosen 90% of the dataset is used for training the network, 5% is used for validation and early stopping, and the remaining (5%) is used for evaluation. We train the network using the AdamOptimizer (Kingma & Ba, 2017)[1]. The learning rate is set to 0.003, the batch-size was set to 300 samples and the maximum number of epochs is 10. After each epoch the level of generalization is measured as the accuracy obtained on the validation set. We use early stopping to prevent over-fitting. To ensure the model stops at the correct time, we combine the GL_α measurement (Prechelt, 1998) of generalization capability and the No-Improvement-In-N-Steps(Nii-N) method (Prechelt, 1998). For instance, Nii-2 means the train process is terminated when generalization capability is not improved in two consecutive epochs.

We compare the performance of our approach, referred to as HCNN, to existing models. One of these is the support vector machine (SVM) model by Higashihara et al. (2008), for which results

---

[1]The LSTM model was implemented in Keras (Chollet et al., 2015), all other models were implemented in Tensorflow (Abadi et al., 2015).

are available in their paper. Second, in tight communication with the authors, we reconstructed the Seq-CNN model presented in (Nguyen et al., 2016) (the original software was no longer available), see Appendix C for detailed settings. Third, we constructed the commonly used LSTM, where the so-called 4-mer profile of the sequence is used as input[2]. A 4-mer profile is a list containing the number of occurrences of all 256 4-mers of the alphabet {A,C,G,T} in a sequence. Preliminary tests showed that using all 256 4-mers resulted in overfitting, and including only the 100 most frequent 4-mers is sufficient. Details of the LSTM architecture can be found in Table 8 in Appendix C.

In order to assess the effect of using a 2D representation of the DNA sequence in isolation, we compare HCNN to a neural network using a sequential representation as input. We refer to this model as seq-HCNN. As in HCNN, the DNA sequence is converted into a list of kmer representing one-hot vectors, though the mapping of the sequence into a 2D image is omitted. The network architecture is a "flattened" version of the one used in HCNN: for example, a $7{\times}7$ convolution filter in HCNN is transformed to a $49{\times}1$ convolution filter in the 1D-sequence model. We refer to this approach as seq-HCNN.

In order to test whether our method is also applicable to other DNA sequence classification tasks than chromatin state prediction only, we performed additional tests on the splice-junction gene sequences dataset from Lichman (2013). Most of the DNA sequence is unused, and splice-junctions refer to positions in the genetic sequence where the transition from an unused subsequence (intron) to a used subsequence (exon) or vice versa takes place. The dataset consists of DNA subsequences of length 61 base pairs, and each of the sequences is known to be a intron-to-exon splice-junction, an exon-to-intron splice junction or neither. As the dataset is relatively small, we used 1-mers instead of 4-mers. Note that the sequences are much shorter than for the other datasets, resulting in smaller images (dimensions $8 \times 8 \times 4$).

4 RESULTS

Table 3 shows the mean prediction accuracy over ten folds as well as the corresponding standard deviation, and training times are reported in Table 4. An additional comparison based on precision, recall, AP and AUC for HCNN and seq-HCNN is presented in Table 5. All reported results except training times concern the test set. Test accuracy and runtimes obtained with the SVM-based approach by Higashihara et al. (2008), the Seq-CNN model from Nguyen et al. (2016), the seq-HCNN, the LSTM method and HCNN are listed in Table 3. The results for the SVM method are taken from Higashihara et al. (2008), all other results are obtained using our own implementations.

The results show that SVM and Seq-CNN were both outperformed by HCNN and seq-HCNN; LSTM shows poor performance. HCNN and seq-HCNN show similar performance in terms of prediction accuracy, though HCNN shows more consistent results over the ten folds. HCNN outperforms all methods in terms of training time (Table 4). Furthermore, HCNN yields better performance than seq-HCNN in terms of precision, recall, AP and AUC (Table 5).

The good performance of HCNN observed above may either be attributable to the conversion from DNA sequence to image, or to the use of the Hilbert curve. In order to address this question, we adapted our approach by replacing the Hilbert curve with other space-filling curves and compared their prediction accuracy. Besides the Hilbert curve, other space-filling curves exist (Moon et al., 2001) (see Appendix A). In Figure 4, we compare the performance of our model with different mapping strategies in various datasets as displayed. We find that the images generated by the space-filling Hilbert curve provide the best accuracy on most datasets and the 1-d sequence performs worst.

5 DISCUSSION

In this paper we developed a CNN that outperforms the state-of-the-art for prediction of the epistatic state. Indeed, our methods show improved prediction accuracy and training time compared to the currently available chromatin state prediction methods from Pahm et al. (2005); Higashihara et al. (2008) and Nguyen et al. (2016) as well as an LSTM model. Additionally, we showed that repre-

---

[2]In terms of model size, the Seq-CNN model contains 1.1M parameters, the both HCNN and seq-HCNN 961K parameters, and the LSTM 455K parameters.

Table 3: Prediction accuracy and runtime obtained with an SVM-based method, Seq-CNN from Nguyen et al. (2016), LSTM, seq-HCNN and HCNN. The results for SVM are taken from Table 12 in Higashihara et al. (2008). Runtimes are presented as min:sec. In splice dataset, Seq-CNN performed best when using 4-mers, while for HCNN 1-mers yielded the best performance.

Dataset	SVM	LSTM	Seq-CNN	seq-HCNN	HCNN
H3	86.47%	64.13%	79.25%	$86.86 \pm 1.563\%$	**87.34 $\pm$0.263**%
H4	87.82%	63.82%	81.86%	$87.31 \pm 0.952\%$	**87.33$\pm$0.264**%
H3K9ac	75.08%	63.07%	68.76%	$78.47 \pm 0.699\%$	**79.19$\pm$0.239**%
H3K14ac	73.28%	68.31%	68.31%	**75.06** $\pm$0.987%	74.79$\pm$**0.226**%
H4ac	72.06%	60.63%	64.80%	$77.04 \pm 1.256\%$	**77.06$\pm$0.233**%
H3K4me1	69.71%	60.43%	62.60%	**73.47** $\pm$0.789%	73.21$\pm$**0.221**%
H3K4me2	68.97%	61.45%	62.38%	$73.91 \pm 0.631\%$	**74.27$\pm$0.224**%
H3K4me3	68.57%	58.03%	62.33%	**74.54** $\pm$0.865%	74.45$\pm$**0.225**%
H3K36me1	75.19%	60.78%	72.20%	**77.18** $\pm$0.973%	77.03$\pm$**0.232**%
H3K79me1	80.58%	63.84%	75.07%	**81.66** $\pm$1.264%	81.63$\pm$**0.246**%
Splice	94.70%	96.23%	91.82%	$93.21 \pm 1.645\%$	**94.11$\pm$0.284**%

Table 4: Training time table

Dataset	LSTM	seq-CNN	seqHCNN	HCNN
H3	35:43	95:23	6:47	3:40
H4	45:32	95:53	5:12	3:12
H3K9ac	76:06	173:18	17:24	7:40
H3K14ac	81:21	180:56	17:42	13:24
H4ac	93:32	181:33	24:48	17:32
H3K4me1	93:44	192:20	18:30	10:38
H3K4me2	94:22	188:13	18:23	14:38
H3K4me3	96:03	162:32	20:40	11:33
H3K36me3	93:48	161:12	21:52	16:37
H3K79me3	64:28	158:34	14:25	10:13
Splice	6:42	35:12	3:42	1:30

senting DNA-sequences with 2D images using Hilbert curves further improves precision and recall as well as training time as compared to a 1D-sequence representation.

We showed that seq-HCNN and HCNN are not only capable of predicting chromatin state, but can also predict the presence or absence of splice-junctions in DNA subsequences. This suggests that our approach could be useful for DNA sequence classification problems in general.

Hilbert curves have several properties that are desirable for DNA sequence classification. The intuitive motivation for the use of Hilbert curves is supported by good results when comparing Hilbert

Table 5: Mean of measurements-Recall,Precision,AP and AUC

Dataset	Recall		Precision		AP		AUC	
	seqHCNN	HCNN	seqHCNN	HCNN	seqHCNN	HCNN	seqHCNN	HCNN
H3	85.67%	**87.33**%	85.67%	**87.33**%	90.33%	**93.33**%	91.00%	**93.67**%
H4	87.00%	**87.33**%	87.00%	**87.00**%	92.67%	**94.67**%	93.67%	**94.67**%
H3K9ac	78.33%	**79.00**%	78.67%	**79.00**%	78.33%	**85.00**%	79.67%	**85.33**%
H3K14ac	**74.00**%	73.67%	74.67%	**75.00**%	73.67%	**79.67**%	76.33%	**81.33**%
H4ac	76.67%	**77.67**%	77.33%	**78.33**%	78.67%	**82.67**%	80.33%	**83.33**%
H3K4me1	72.33%	**73.00**%	72.67%	**73.67**%	70.67%	**76.33**%	71.67%	**78.33**%
H3K4me2	70.67%	**72.33**%	73.00%	**74.00**%	69.33%	**77.33**%	70.00%	**78.67**%
H3K4me3	74.33%	**74.67**%	**75.00**%	74.67%	71.00%	**78.67**%	72.00%	**80.00**%
H3K36me3	76.00%	**76.67**%	77.00%	**77.67**%	76.33%	**82.00**%	79.33%	**83.00**%
H3K79me3	81.00%	**82.33**%	81.00%	**82.67**%	79.67%	**88.00**%	81.00%	**88.67**%
Splice	91.00%	**95.00**%	90.67%	**94.33**%	95.00%	**97.67**%	97.33%	**98.67**%

Figure 4: HCNN with different mapping strategies

curves to other space-filling curves. Additionally, Hilbert curves have previously been shown to be useful for visualization of DNA sequences (Anders, 2009).

The main limitation of Hilbert curves is their fixed length, which implies that the generated image contains some empty spaces. These spaces consume some computation resources; nevertheless, the 2D representation still yields reduced training times compared to the 1D-sequence representation, presumably due to the high degree of optimization for 2D inputs present in standard CNN frameworks.

REFERENCES

M. Abadi, A. Agarwal, P. Barham, E. Brevdo, Z. Chen, C. Citro, G.S.Corrado, A. Davis, J. Dean, M. Devin, S. Ghemawat, I. Goodfellow, A. Harp, G. Irving, M. Isard, Y. Jia, R. Jozefowicz, L. Kaiser, M. Kudlur, J. Levenberg, D. Mané, R. Monga, S. Moore, D. Murray, C. Olah, M. Schuster, J. Shlens, B. Steiner, I. Sutskever, K. Talwar, P. Tucker, V. Vanhoucke, V. Vasudevan, F. Viégas, O. Vinyals, P. Warden, M. Wattenberg, M. Wicke, Y. Yu, and X. Zheng. TensorFlow: Large-scale machine learning on heterogeneous systems, 2015. URL `https://www.tensorflow.org/`. Software available from tensorflow.org.

M. Aftosmis, M. Berger, and S. Murman. Applications of space-filling-curves to cartesian methods for cfd. *42nd AIAA Aerospace Sciences Meeting and Exhibit*, May 2004. doi: 10.2514/6. 2004-1232.

S. Anders. Visualization of genomic data with the Hilbert curve. *Bioinformatics*, 25(10):1231–1235, 2009.

C. Angermueller, T. Pärnamaa, L. Parts, and O. Stegle. Deep learning for computational biology. *Molecular Systems Biology*, 12(7):878, 2016.

M. Bader. *Space-filling curves: an introduction with applications in scientific computing*. Springer, 2016.

L. Brueckner, J. van Arensbergen, W. Akhtar, L. Pagie, and B. van Steensel. High-throughput assessment of context-dependent effects of chromatin proteins. *Epigenetics and Chromatin*, 9(1): 43, 2016.

F. Chollet et al. Keras. `https://github.com/fchollet/keras`, 2015.

D.-A. Clevert, T. Unterthiner, and S. Hochreiter. Fast and accurate deep network learning by exponential linear units (elus). *arXiv preprint arXiv:1511.07289*, 2015.

C.A. de Graaf and B. van Steensel. Chromatin organization: form to function. *Current Opinion in Genetics and Development*, 23(2):185–190, 2013.

S.C.R. Elgin. http://slideplayer.com/slide/7605009/, 2012. Slides 55-57.

J. Ernst and M. Kellis. Interplay between chromatin state, regulator binding, and regulatory motifs in six human cell types. *Genome Research*, 23(7):1142–1154, 2013.

J. Ernst, P. Kheradpour, T.S. Mikkelsen, N. Shoresh, Ward L.D., et al. Mapping and analysis of chromatin state dynamics in nine human cell types. *Nature*, 473(7345):43–49, 2011.

Y. Goldberg. *Neural network methods for natural language processing*. Morgan & Claypool, 2017.

K. He, X. Zhang, S. Ren, and J. Sun. Deep residual learning for image recognition, Dec 2015. URL `https://arxiv.org/abs/1512.03385`.

M. Higashihara, J.D. Rebolledo-Mendez, Y. Yamada, and K. Satou. Application of a feature selection method to nucleosome data: Accuracy improvement and comparison with other methods. *WSEAS Transactions on Biology and Biomedicine*, 2008.

D. P. Kingma and J. Ba. Adam: A method for stochastic optimization, Jan 2017. URL `https://arxiv.org/abs/1412.6980`.

Y. LeCun, Y. Bengio, and G. Hinton. Deep learning. *Nature*, 521(7553):436–444, 2015.

M. Lichman. UCI machine learning repository, 2013. URL `http://archive.ics.uci.edu/ml`.

R. S. Michalski, J. G. Carbonell, and T.M. Mitchell. *Machine Learning: An Artificial Intelligence Approach*. Springer Berlin, 2013.

B. Moon, H.V. Jagadish, C. Faloutsos, and J.H. Saltz. Analysis of the clustering properties of the Hilbert space-filling curve. *IEEE Transactions on Knowledge and Data Engineering*, 13(1): 124–141, 2001. doi: 10.1109/69.908985.

N.G. Nguyen, V.A. Tran, D.L. Ngo, D. Phan, F.R. Lumbanraja, et al. DNA sequence classification by convolutional neural network. *Journal of Biomedical Science and Engineering*, 9(5):280–286, 2016.

T.H. Pahm, D.H. Tran, T.B. Ho, K. Satou, and G. Valiente. Qualitatively predicting acetylation and methylation areas in dna sequences. *Genome Informatics*, 16(2):3–11, 2005.

D.K. Pokholok, C.T. Harbison, S. Levine, M. Cole, N.M. Hannett, T.I. Lee, G.W. Bell, K. Walker, P. A. Rolfe, and E. Herbolsheimer. Genome-wide map of nucleosome acetylation and methylation in yeast. *Cell*, 122(4):517–527, 2005. doi: 10.1016/j.cell.2005.06.026.

L. Prechelt. Automatic early stopping using cross validation: quantifying the criteria. *Neural Networks*, 11(4):761–767, 1998.

X. Li R.R. Bhat, V. Viswanath. Deepcancer: Detecting cancer through gene expressions via deep generative learning. *arXiv*, 2016.

Tim Salimans, Ian Goodfellow, Wojciech Zaremba, Vicki Cheung, Alec Radford, and Xi Chen. Improved techniques for training gans, Jun 2016. URL `https://arxiv.org/abs/1606.03498`.

K. Simonyan and A. Zisserman. *Very deep convolutional networks for large-scale image recognition.* arxiv. org/abs/1409.1556, 2014. URL `CoRRabs/1409.1556(2014).`

C. Szegedy, W. Liu, Y. Jia, P. Sermanet, S. Reed, D. Anguelov, D. Erhan, V. Vanhoucke, and A. Rabinovich. Going deeper with convolutions. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pp. 1–9, 2015.

The ENCODE Project Consortium. An integrated encyclopedia of DNA elements in the human genome. *Nature*, 489(7414):57–74, 2012.

A. Tomovic, P. Janicic, and V. Keselj. n-gram-based classification and unsupervised hierarchical clustering of genome sequences. *Computer Methods and Programs in Biomedicine*, 81(2): 137–153, 2006. doi: 10.1016/j.cmpb.2005.11.007.

V. N. Vapnik. *Statistical learning theory.*, volume 1. Wiley, 1998.

J.D. Watson and F.H. Crick. Molecular structure of nucleic acids. *Nature*, 171(4356):737–738, 1953.

E. Keogh Z. Xing, J. Pei. A brief survey on sequence classification. *ACM*, 2010.

J. Zhou and O.G. Troyanskaya. Predicting effects of noncoding variants with deep learning–based sequence model. *Nature methods*, 12:931–934, 2015.

A   COMPARISON OF SPACE-FILLING CURVES WITH REGARD TO LONG-TERM INTERACTIONS

As noted before, long-term interactions are highly relevant in DNA sequences. In this section we consider these long-term interactions in four space-filling curves: the reshape curve, the snake curve, the Hilbert curve and the diag-snake curve. See Fig. 5 for an illustration.

(a) Reshape curve   (b) snake curve   (c) Diag-Snake curve   (d) Hilbert curve

Figure 5: Space-filling curves

As can be seen in Fig. 5, mapping a sequence to an image reduces the distance between two elements that are far from one another in the sequence, while the distance between nearby elements does not increase. Each of the curves does have a different effect on the distance between far-away elements. In order to assess these differences, we use a measure that is based on the distance between two sequence elements as can be observed in the image. We denote this distance by $\mathcal{L}_C(x,y)$ where $x, y \in \mathcal{S}$, with $\mathcal{S}$ the sequence and C the curve under consideration. Then for the sequence $\mathcal{S} = \{A,B,C,D,E,\cdots,P\}$ we obtain

- $\mathcal{L}_{seq}(A,P) = 15$ for the sequence;
- $\mathcal{L}_{reshape}(A,P) = 3\sqrt{2}$ for the reshape curve;
- $\mathcal{L}_{snakesnake}(A,P) = 3$ for the snake curve;
- $\mathcal{L}_{diag-snake}(A,P) = 3\sqrt{2}$ for the diagonal snake curve.
- $\mathcal{L}_{hilbert}(A,P) = 3$ for the Hilbert curve;

We now introduce the following measure:

$$\Gamma(\mathbf{C}) = \frac{\text{mean}(\Delta(\mathbf{C}))}{\text{max}(\Delta(\mathbf{C}))},$$

where the $\Delta(\mathbf{C})$ is the set of the weighted distances between all pairs of the elements in the sequence. Here, $\Delta(C)$ is a set containing the distance between any two sequence elements, weighted by their distance in the sequence:

$$\Delta(\mathbf{C}) = \{\mathcal{L}_{seq}(x,y) \cdot \mathcal{L}_{\mathbf{C}}(x,y) \mid x, y \in \mathbf{C}, x \neq y\}.$$

Note that a low $\text{max}(\Delta(\mathbf{C}))$ relative to $\text{mean}(\Delta(\mathbf{C}))$ implies that long-term interactions are strongly accounted for, so a high $\Gamma(C)$ is desirable.

$\Gamma(C)$ is evaluated for the four space-filling curves as well as the sequence representation for sequences of varying lengths. The results show that the Hilbert curve yields the highest values for $\Gamma(C)$ 6 and thus performs best in terms of retaining long-distance interactions.

Curve	Sequence Length : bits				
	16	64	256	1024	4096
Reshape	0.22	0.18	0.16	0.16	0.15
Snake	0.28	0.20	0.17	0.16	0.16
Diag-snake	0.22	0.17	0.16	0.15	0.15
Hilbert	**0.30**	**0.24**	**0.22**	**0.21**	**0.21**

Table 6: $\Gamma(C)$ for four space-filling curves,
evaluated in sequences of varying lengths.

B FROM SEQUENCE TO IMAGE

Figure 6 shows the conversion from DNA sequence to image.

Figure 6: Sequence to Image

C   DETAILS OF ALTERNATIVE NEURAL NETWORKS

Table 7: Sequence Convolutional Model

Layer	filter size	stride	output dim
Convolution 1	7	2	60
Activation			
Max pooling	3	3	60
Convolution 2	5	2	30
Activation			
Max pooling	3	2	30
Dropout, 0.5			
FC layer			100
Activation			
Dropout, 0.5			
Classifier			2

Table 8: Bir-Direction LSTM

Layer	Description
Embedding	
Conv 1	1-by-3 convolution layer with 32 filter size activation function is RELU
Max pooling	1×2 max pooling layer
Bir-LSTM 1	100 units
Bir-LSTM 2	128 units
Dropout	0.3 dropout rate
Classifier	sigmoid