Adversarially Robust Spiking Neural Networks Through Conversion

Anonymous authors
Paper under double-blind review

Abstract

Spiking neural networks (SNNs) provide an energy-efficient alternative to a variety of artificial neural network (ANN) based AI applications. As the progress in neuromorphic computing with SNNs expands their use in applications, the problem of adversarial robustness of SNNs becomes more pronounced. To the contrary of the widely explored end-to-end adversarial training based solutions, we address the limited progress in scalable robust SNN training methods by proposing an adversarially robust ANN-to-SNN conversion algorithm. Our method provides an efficient approach to embrace various computationally demanding robust learning objectives that have been proposed for ANNs. During a post-conversion robust finetuning phase, our method adversarially optimizes both layer-wise firing thresholds and synaptic connectivity weights of the SNN to maintain transferred robustness gains from the pre-trained ANN. We perform experimental evaluations in a novel setting proposed to rigorously assess the robustness of SNNs, where numerous adaptive adversarial attacks that account for the spike-based operation dynamics are considered. Results show that our approach yields a scalable state-of-the-art solution for adversarially robust deep SNNs with low-latency.

1 Introduction

Spiking neural networks (SNNs) are powerful models of computation based on principles of biological neuronal networks (Maass, 1997). Unlike traditional artificial neural networks (ANNs), the neurons in an SNN communicate using binary signals (i.e., spikes) elicited across a temporal dimension. This characteristic alleviates the need for computationally demanding matrix multiplication operations of ANNs, thus resulting in an advantage of energy-efficiency with event-driven processing capabilities (Roy et al., 2019). Together with the developments in specialized neuromorphic hardware to process information in real-time with low-power requirements, SNNs offer a promising energy-efficient technology to be widely deployed in safety-critical real world AI applications (Davies et al., 2021). There are two main streams of applications for SNNs. First, they are applied directly to spiking input streams, e.g., from dynamic vision sensors (Bellec et al., 2018; Wu et al., 2019; Kim & Panda, 2021a). Second, they are applied to standard machine learning tasks and standard machine learning data sets (Rathi & Roy, 2021; Bu et al., 2022; Jiang et al., 2023). We focus in this article on the latter case. Here, conversion methods that convert a pre-trained ANN to an SNN have been shown to yield SNN models with excellent performance (Diehl et al., 2015; Roy et al., 2019). Post-conversion finetuning can then be used for low-latency and energy-efficient SNNs (Rathi & Roy, 2021; Davies et al., 2021).

Numerous studies have explored the susceptibility of traditional ANNs to adversarial attacks (Szegedy et al., 2013), and this security concern evidently extends to SNNs since effective attacks are gradient-based and architecture agnostic (Sharmin et al., 2019). Recently, there has been growing interest in achieving adversarial robustness with SNNs, which remains an important open problem (Kundu et al., 2021; Ding et al., 2022; Liang et al., 2022). Temporal operation characteristics of SNNs makes it non-trivial to apply existing defenses developed for ANNs (Madry et al., 2018). Nevertheless, current solutions are mainly end-to-end adversarial training based methods that are adapted for SNNs (Ding et al., 2022). These approaches, however, yield limited robustness for SNNs as opposed to ANNs, both due to their computational limitations (e.g., infeasibility of heavily iterative backpropagation across time), as well as the confounding impact of spike-based

end-to-end adversarial training, on the SNN gradients, as we elaborate later in our evaluations. According to the current literature, the widely accepted assumption is that SNNs directly trained with spike-based backpropagation achieve stronger robustness than SNNs obtained by converting a pre-trained ANN (Sharmin et al., 2020). In this work, we challenge this hypothesis by proposing a novel adversarially robust ANN-to-SNN conversion algorithm based solution.

We present an ANN-to-SNN conversion algorithm that improves SNN robustness by exploiting adversarially trained baseline ANN weights at initialization followed by an adversarial finetuning method. Our approach allows to integrate any existing robust learning objective developed for conventional ANNs into an ANN-to-SNN conversion algorithm, thus optimally transferring robustness gains into the SNN. Specifically, we convert a robust ANN into an SNN by adversarially finetuning both the synaptic connectivity weights and the layer-wise firing thresholds, which yields significant robustness benefits. Innovatively, we introduce a highly effective approach to incorporate adversarially pre-trained ANN batch-norm layer parameters – which helps facilitating adversarial training of the deep ANN – within spatio-temporal SNN batch-norm operations, without the need to omit these layers from the models as conventionally done in conversion based methods.

Previous works on improving adversarial robustness of SNNs conduct attack evaluations in a similar way to ANNs (Sharmin et al., 2020; Kundu et al., 2021; Ding et al., 2022), which are insufficient due to not considering the influence of the spike function surrogate gradient used by the adversary. To that end, we also introduce a novel ensemble SNN robustness evaluation approach where we rigorously simulate the attacks by constructing adaptive adversaries based on different differentiable approximation techniques (see Section 4), accounting for the architectural dynamics of SNNs that are different from ANNs. By doing so, we adapt recent observations on evaluating ANNs with non-differentiable operations and/or obfuscated gradients (Athalye et al., 2018a; Carlini et al., 2019) to the domain of SNNs, and improve SNN robustness evaluations with rigor.

In depth experimental analyses show that our approach achieves a scalable state-of-the-art solution for adversarial robustness in deep SNNs with low-latency, outperforming recently introduced end-to-end adversarial training based algorithms with up to 2× larger robustness gains and reduced robustness-accuracy trade-offs.

2 Preliminaries and Related Work

2.1 Spiking Neural Networks

Unlike traditional ANNs with continuous valued activations, SNNs use discrete, pulsed signals to transmit information. Discrete time dynamics of leaky-integrate-and-fire (LIF) neurons in feed-forward SNNs follow:

$$\mathbf{v}^l(t^-) = \tau\, \mathbf{v}^l(t-1) + \mathbf{W}^l\, \mathbf{s}^{l-1}(t), \tag{1}$$

$$\mathbf{s}^l(t) = H(\mathbf{v}^l(t^-) - V^l_{th}), \tag{2}$$

$$\mathbf{v}^l(t) = \mathbf{v}^l(t^-)(1 - \mathbf{s}^l(t)), \tag{3}$$

where the neurons in the l-th layer receive the output spikes $\mathbf{s}^{l-1}(t)$ from the preceding layer weighted by the trainable synaptic connectivity matrix $\mathbf{W}^l$, and τ denotes the membrane potential leak factor. We represent the neuron membrane potential before and after the firing of a spike at time t by $\mathbf{v}^l(t^-)$ and $\mathbf{v}^l(t)$, respectively. $H(.)$ denotes the Heaviside step function. A neuron j in layer l generates a spike when its membrane potential $v^l_j(t^-)$ reaches the firing threshold V^l_{th}. Subsequently, the membrane potential is updated via Eq. (3), which performs a *hard-reset*. Alternatively, a neuron with *soft-reset* updates its membrane potential by subtraction, $\mathbf{v}^l(t) = \mathbf{v}^l(t^-) - \mathbf{s}^l(t)V^l_{th}$, where the residual membrane potential can encode information. Inputs $\mathbf{s}^0(t)$ to the first layer are typically represented either by *rate coding*, where the input signal intensity determines the firing rate of an input Poisson spike train of length T, or by *direct coding*, where the input signal is applied as direct current to $\mathbf{v}^1(t^-)$ for all T timesteps of the simulation.

Direct Training: One category of algorithms to obtain deep SNNs relies on end-to-end training with spike-based backpropagation (Wu et al., 2018; 2019; Lee et al., 2020). Different from conventional ANNs, gradient-based SNN training backpropagates the error through the network temporally (i.e., backpropagation through time (BPTT)), in order to compute a gradient for each forward pass operation. During BPTT, the

discontinuous derivative of $H(\mathbf{z}^l(t))$ for a spiking neuron when $\mathbf{z}^l(t) = \mathbf{v}^l(t^-) - V^l_{th} \geq 0$, is approximated via surrogate gradient functions (Neftci et al., 2019). Such approximate gradient based learning algorithms have reduced the performance gap between deep ANNs and SNNs over the past years (Bellec et al., 2018; Shrestha & Orchard, 2018). Various improvements proposed for ANNs, e.g., residual connections or batch normalization, have also been adapted to SNNs (Fang et al., 2021; Duan et al., 2022). Notably, recent work introduced batch-norm through time (BNTT) (Kim & Panda, 2021b), and threshold-dependent batch-norm (tdBN) (Zheng et al., 2021) mechanisms to better stabilize training of deep SNNs.

ANN-to-SNN Conversion: An alternative approach is to convert a structurally equivalent pre-trained ANN into an SNN (Cao et al., 2015). This is performed by replacing ANN activation functions with LIF neurons (thus keeping weights $\mathbf{W}^l$ intact), and then calibrating layer-wise firing thresholds (Diehl et al., 2015; Sengupta et al., 2019). The main goal is to approximately map the continuous-valued ANN neuron activations to the firing rates of spiking neurons (Rueckauer et al., 2017). While conversion methods leverage prior knowledge from the source ANN, they often need more simulation time steps T than BPTT-based SNNs which can temporally encode information. Recent, *hybrid* approaches tackle this problem via post-conversion finetuning (Rathi et al., 2020). This was later improved by using soft-reset mechanisms (Han et al., 2020), or trainable firing thresholds and membrane leak factors during finetuning (Rathi & Roy, 2021). More recent methods redefine the source ANN activations to achieve minimal loss during conversion (Li et al., 2021; Bu et al., 2022; Jiang et al., 2023).

2.2 Adversarial Attacks and Robustness

Deep neural networks are known to be susceptible to adversarial attacks (Szegedy et al., 2013), and various defenses have been proposed to date. Currently, most effective ANN defense methods primarily rely on exploiting adversarial examples during optimization (Athalye et al., 2018a), which is known as adversarial training (AT) (Madry et al., 2018; Goodfellow et al., 2015).

Given samples $(\mathbf{x}, y)$ from a training dataset $\mathcal{D}$, a neural network $f_{\boldsymbol{\theta}}$ is conventionally trained via the natural cross-entropy loss $\mathcal{L}_{\text{CE}}(f_{\boldsymbol{\theta}}(\mathbf{x}), y)$, which follows a maximum likelihood learning rule. In the context of robust optimization, adversarial training objectives can be formulated by:

$$\min_{\boldsymbol{\theta}} \mathbb{E}_{(\mathbf{x},y)\sim\mathcal{D}} \left[\max_{\tilde{\mathbf{x}}\in\Delta^p_\epsilon(\mathbf{x})} \mathcal{L}_{\text{robust}} \left(f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}}), f_{\boldsymbol{\theta}}(\mathbf{x}), y \right) \right], \tag{4}$$

with $\tilde{\mathbf{x}}$ denoting the adversarial example crafted during the inner maximization step, which is constrained within $\Delta^p_\epsilon(\mathbf{x}) := \{\tilde{\mathbf{x}} : \|\tilde{\mathbf{x}} - \mathbf{x}\|_p \leq \epsilon\}$, defined as the l_p-norm ball around $\mathbf{x}$ with an $\epsilon > 0$ perturbation budget. We will focus on l_∞-norm bounded examples where $\tilde{\mathbf{x}} \in \Delta^\infty_\epsilon(\mathbf{x})$.

Standard AT (Madry et al., 2018) only utilizes iteratively crafted adversarial examples during optimization, i.e., $\mathcal{L}^{\text{AT}}_{\text{robust}} := \mathcal{L}_{\text{CE}}(f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}}), y)$, thus maximizing log-likelihood solely based on $\tilde{\mathbf{x}}$, and does not use benign samples. Conventionally, the inner maximization is approximated by projected gradient descent (PGD) on a choice of an $\mathcal{L}_{\text{PGD}}$ loss (e.g., for standard AT: $\mathcal{L}_{\text{PGD}} = \mathcal{L}_{\text{CE}}(f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}}), y)$), to obtain k-step adversarial examples by: $\tilde{\mathbf{x}}_{k+1} = \Pi_{\Delta^\infty_\epsilon(\mathbf{x})}\left[\tilde{\mathbf{x}}_k + \eta \cdot \text{sign}(\nabla_{\tilde{\mathbf{x}}_k} \mathcal{L}_{\text{PGD}}(f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}}_k), y))\right]$, where $\tilde{\mathbf{x}}_0 = \mathbf{x} + \delta$ with $\delta \sim \mathcal{U}(-\epsilon, \epsilon)$, step size η, and $\Pi_{\Delta^\infty_\epsilon(\mathbf{x})}[.]$ the clipping function onto the ϵ-ball. Due to its iterative computational load, single-step variants of PGD, such as the fast gradient sign method (FGSM) (Goodfellow et al., 2015) or random-step FGSM (RFGSM) (Tramèr et al., 2018), have been explored as alternatives (Wong et al., 2020).

State-of-the-art robust training methods propose regularization schemes to improve the inherent robustness-accuracy trade-off (Tsipras et al., 2019). A powerful robust training loss, TRADES (Zhang et al., 2019a), redefines the training objective as:

$$\mathcal{L}^{\text{TRADES}}_{\text{robust}} := \mathcal{L}_{\text{CE}}(f_{\boldsymbol{\theta}}(\mathbf{x}), y) + \lambda_{\text{TRADES}} \cdot D_{\text{KL}} \left(f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}}) || f_{\boldsymbol{\theta}}(\mathbf{x}) \right), \tag{5}$$

where D_{KL} denotes the Kullback-Leibler divergence, and λ_{TRADES} is the trade-off hyper-parameter. In a subsequent work (Wang et al., 2020), MART robust training loss proposes to emphasize the error on misclassified examples via:

$$\mathcal{L}^{\text{MART}}_{\text{robust}} := \mathcal{L}_{\text{BCE}}(f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}}), y) \ + \lambda_{\text{MART}} \cdot (1 - f^{(y)}_{\boldsymbol{\theta}}(\mathbf{x})) \cdot D_{\text{KL}} \left(f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}}) || f_{\boldsymbol{\theta}}(\mathbf{x}) \right), \tag{6}$$

where λ_{MART} is the trade-off parameter, $f_{\boldsymbol{\theta}}^{(y)}(\mathbf{x})$ denotes the probability assigned to class y, and the boosted cross-entropy is defined as, $\mathcal{L}_{\text{BCE}}(f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}}), y) := \mathcal{L}_{\text{CE}}(f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}}), y) - \log(1 - \max_{j \neq y} f_{\boldsymbol{\theta}}^{(j)}(\tilde{\mathbf{x}}))$, with the second term improving the decision margin for adversarial samples.

2.3 Adversarial Robustness in Spiking Neural Networks

Earlier explorations of adversarial attacks on SNNs particularly emphasized that direct training exhibits stronger robustness compared to conversion-based SNNs with high latency, and rate input coding SNNs tend to yield higher robustness (Sharmin et al., 2019; 2020). Accordingly, subsequent work mainly focused on end-to-end SNN training methods, yet relying on shallower networks and simpler datasets (Sharmin et al., 2020; Marchisio et al., 2020). Notably, SNNs were also shown to maintain higher resiliency to black-box attacks than their ANN counterparts (Sharmin et al., 2020). Later studies analyzed various components of SNNs and their robustness implications, such as the structural configuration (El-Allami et al., 2021; Kim et al., 2022a), or the surrogate gradient used for training (Xu et al., 2022). Another line of work focuses on designing attacks for event-based neuromorphic data, with stable BPTT gradient estimates (Marchisio et al., 2021; Liang et al., 2021; Büchel et al., 2022). Until recently, there has been limited progress in scalable robust SNN training algorithms.

A recent work (Liang et al., 2022) explores certified adversarial robustness bounds for SNNs on MNIST-variant datasets, based on an interpretation of methods designed for ANNs (Zhang et al., 2019b). Recently, HIRE-SNN (Kundu et al., 2021) proposed adversarial finetuning of SNNs initialized by converting a naturally trained ANN, using a similar approach to (Rathi & Roy, 2021). For finetuning, HIRE-SNN manipulates inputs temporally with single-step adversarial noise, resulting in marginal robustness benefits on relatively small models. The recently proposed SNN-RAT (Ding et al., 2022) algorithm empirically achieved state-of-the-art robustness with SNNs. SNN-RAT interprets the ANN weight orthogonalization methodology to constrain the Lipschitz constant of a feed-forward network (Cisse et al., 2017), in the context of SNNs optimized with single-step adversarial training. Due to its ability to scale to deep SNN architectures, SNN-RAT currently serves as a solid baseline to achieve robustness with SNNs.

3 Adversarially Robust ANN-to-SNN Conversion

3.1 Converting Adversarially Trained Baseline ANNs

Our method converts an adversarially trained ANN into an SNN by initially configuring layer-wise firing thresholds based on the well-known threshold-balancing approach (Sengupta et al., 2019). Then we propose to adversarially finetune these thresholds together with the weights.

Configuration of the SNN: Given an input $\mathbf{x}$, we use a direct input encoding scheme for $\mathbf{s}^0(t)$, where the input signal (e.g., pixel intensity) is applied as a constant current for a simulation length of T timesteps. Subsequently, the network follows the SNN dynamics from Eqs. (1), (2), (3). We mainly consider SNNs with integrate-and-fire (IF) neurons, i.e., $\tau = 1$, similar to Ding et al. (2022) (see *Experiments on TinyImageNet* for simulations with LIF neurons). The output layer of our feed-forward SNN with L layers only accumulates weighted incoming inputs without generating a spike. Integrated output neuron membrane potentials $v_j^L(T)$ for $j = 1, \ldots, N$, with N being the number of classes, are then used to estimate normalized probabilities via:

$$f_{\boldsymbol{\theta}}^{(j)}(\mathbf{x}) = e^{v_j^L(T)} \Big/ \sum_{i=1}^{N} e^{v_i^L(T)}, \quad \text{where} \quad \mathbf{v}^L(t) = \mathbf{v}^L(t-1) + \mathbf{W}^L\, \mathbf{s}^{L-1}(t), \;\; t = 1, \ldots, T, \tag{7}$$

and $f_{\boldsymbol{\theta}}^{(j)}(\mathbf{x})$ denotes the probability assigned to class j. In our case, the neural network parameters $\boldsymbol{\theta}$ to be optimized will include connectivity weights, layer-wise firing thresholds, and batch-norm parameters.

Initializing SNN Weights: We use the weights from a baseline ANN that is adversarially trained via Eq. (4), to initialize the SNN synaptic connectivity matrices. Our approach is in principle agnostic to the ANN adversarial training method. For a feed-forward ANN, neuron output activations $\mathbf{a}^l$ in the l-th layer would be, $\mathbf{a}^l = \sigma(\mathbf{W}^l\, \mathbf{a}^{l-1})$, where $\sigma(.)$ often indicates a ReLU. We essentially maintain $\mathbf{W}^l$ for all layers, and replace $\sigma(.)$ with spiking neuron dynamics.

Conversion of Batch Normalization: Traditional conversion methods either exclude batch-norm from the source ANN (Sengupta et al., 2019), or absorb its parameters into the preceding convolutional layer (Rueckauer et al., 2017). Here, we propose a novel and effective approach to directly integrate robustly pre-trained ANN batch-norm affine transformation parameters into SNN tdBN layers (Zheng et al., 2021), and maintain the weights φ^l and ω^l within:

$$\hat{\mathbf{S}}^l = \varphi^l \cdot \left(\left(\bar{\mathbf{S}}^l - \mathbb{E}[\bar{\mathbf{S}}^l]\right) \Big/ \sqrt{Var[\bar{\mathbf{S}}^l] + \vartheta} \right) + \omega^l, \quad \text{where} \quad \bar{\mathbf{S}}^l = [\bar{\mathbf{s}}^l(1), \bar{\mathbf{s}}^l(2), \ldots, \bar{\mathbf{s}}^l(T)], \tag{8}$$

weighted spiking inputs $\bar{\mathbf{s}}^l(t) = \mathbf{W}^l\, \mathbf{s}^{l-1}(t)$ are gathered temporally in $\bar{\mathbf{S}}^l$, ϑ is a tiny constant, and $\mathbb{E}[.]$ and $Var[.]$ are estimated both across time and mini-batch. This temporal and spatial normalization was found highly effective in stabilizing training. Different from its original formulation (Zheng et al., 2021), we do not perform a threshold-based scaling in the normalization, but instead finetune φ^l and ω^l together with the firing thresholds. Normalized $\hat{\mathbf{s}}^l(t)$ is then integrated into the neuron membrane potential via Eq. (1). We do not re-use the moving average mean and variance estimates from the ANN, which are often tracked to be used at inference time, but estimate them during finetuning.

Initialization of Trainable Firing Thresholds: We generate inputs $\mathbf{s}^0(t)$ by direct coding for T_c calibration time steps, which we choose to be much larger than T, using a number of training set mini-batches. In order to estimate proportionally balanced per-layer firing thresholds as in (Sengupta et al., 2019), starting from the first layer, for all inputs we record the pre-activation values (i.e., summation of the weighted spiking inputs) observed across T_c timesteps, and set the threshold to be the maximum value in the ρ-percentile of the distribution of these pre-activation values (often $\rho > 99\%$). This is performed similarly to (Rathi & Roy, 2021), in order to accommodate for the stochasticity involved due to the use of sampled training set mini-batches (see Suppl. A.2 for more details).

After setting the firing threshold for $l = 1$, we perform a forward pass through the spiking neuron dynamics of this layer, and move on to the next layer with spiking activations. We sequentially set the firing thresholds for all other layers in the same way. During the forward passes, we only use inference-time statistics estimated spatio-temporally on the current batch for normalization via tdBN. After estimating all layer thresholds, we initialize the trainable $\{V_{th}^l\}_{l=1}^{L-1}$ values by scaling the initial estimates with a constant factor $\kappa < 1$, in order to promote a larger number of spikes to flow across layers proportionally to our initial estimates (Lu & Sengupta, 2020) (see Suppl. A.3 for complete algorithm).

3.2 Robust Finetuning of SNN After Conversion

We complement our hybrid conversion approach with spike-based backpropagation based adversarial finetuning. Similar to conventional robust training (Madry et al., 2018; Zhang et al., 2019a), we exploit adversarial examples for weight updates and adjusted firing thresholds. The optimization objective follows:

$$\min_{\boldsymbol{\theta}} \mathbb{E}\left[\mathcal{L}_{\text{CE}}(f_{\boldsymbol{\theta}}(\mathbf{x}), y) + \beta \cdot \max_{\tilde{\mathbf{x}} \in \Delta_\epsilon^p(\mathbf{x})} D_{\text{KL}}(f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}}) || f_{\boldsymbol{\theta}}(\mathbf{x})) \right], \tag{9}$$

where β is a robustness-accuracy trade-off parameter, $\boldsymbol{\theta}$ consists of $\{\mathbf{W}^l, \varphi^l, \omega^l\}_{l=1}^{L}$ and $\{V_{th}^l\}_{l=1}^{L-1}$, and $f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}})$ and $f_{\boldsymbol{\theta}}(\mathbf{x})$ are the probability vectors assigned to a benign and an adversarial example, estimated by the integrated output neuron membrane potentials over T timesteps. Adversarial example $\tilde{\mathbf{x}} \in \Delta_\epsilon^\infty(\mathbf{x})$ is obtained via an RFGSM based single inner maximization step by:

$$\tilde{\mathbf{x}} = \mathbf{x}' + (\epsilon - \alpha) \cdot \text{sign}\left(\nabla_{\mathbf{x}'} \mathcal{L}_{\text{RFGSM}}\right), \quad \text{where} \quad \mathbf{x}' = \mathbf{x} + \alpha \cdot \text{sign}\left(\mathcal{N}(\mathbf{0}, \mathbf{I})\right). \tag{10}$$

Note that only a single gradient computation is used for RFGSM, thus it is a computationally efficient and yet a powerful alternative to PGD (Ding et al., 2022). We use $\mathcal{L}_{\text{RFGSM}} = D_{\text{KL}}(f_{\boldsymbol{\theta}}(\mathbf{x}') || f_{\boldsymbol{\theta}}(\mathbf{x}))$ to obtain an adversarial sample, which maximizes the KL-distance between the vectors of integrated membrane potentials of output class neurons (cf. Suppl B.3 ablations for alternatives). Objective in Eq. (9) is optimized via BPTT, and a piecewise linear surrogate gradient with unit dampening factor is used for the gradients of spikes (Bellec et al., 2018). We present further details in Suppl. A.3, and outline our BPTT-based parameter updates based on Eq. (9), as well as our overall training algorithm.

4 An Ensemble Evaluation Approach for Adversarial Robustness of SNNs

Spike-based backpropagation relies on surrogate gradient functions due to the discontinuous derivative of the spike activation function (Neftci et al., 2019). Thus, differently from ANNs, the success of a backpropagation based SNN adversarial attack also critically depends on the surrogate gradient used by the adversary for the attack. Previous studies on adversarial robustness of SNNs (Sharmin et al., 2020; Kundu et al., 2021; Ding et al., 2022) conduct naive attack evaluations, by only considering the same surrogate gradient function used during training at the time of attack. Here, we propose to adapt recent observations made on ANNs with non-differentiable operations and/or obfuscated gradients (Brendel & Bethge, 2017; Athalye et al., 2018a; Carlini et al., 2019) to the domain of SNNs, in order to improve SNN robustness evaluations by potentially relying on more stable gradient estimates with different surrogate gradient choices at the time of attack.

For evaluations, we therefore implemented an ensemble attack strategy. For each attack algorithm, we anticipate an adaptive SNN adversary, as proposed for ANNs (Carlini et al., 2019), that simulates a number of attacks for a test sample where the BPTT surrogate gradient varies in each case. We consider variants of the three most common surrogate gradient functions: piecewise linear (Bellec et al., 2018), exponential (Shrestha & Orchard, 2018), and rectangular (Wu et al., 2018), with different width, dampening, or steepness parameters (see Suppl. A.4 for parameter details). In the ensemble we also consider straight-through estimation (Bengio et al., 2013), backward pass through rate, and a conversion-based approximation (Ding et al., 2022), where we replace spiking neurons with a ReLU during BPTT. We calculate robust accuracies on the whole test set, and consider an attack successful for a test sample if the model is fooled with any of the attacks from the ensemble. Note that during training we only use the piecewise linear surrogate gradient with a unit dampening factor as in Ding et al. (2022).

5 Experiments

5.1 Datasets and Models

We performed experiments with CIFAR-10, CIFAR-100, SVHN and TinyImageNet datasets. We used VGG11 (Simonyan & Zisserman, 2015), ResNet-20 (He et al., 2016) and WideResNet (Zagoruyko & Komodakis, 2016) architectures with depth 16 and width 4 (i.e., WRN-16-4) in our experiments (see Suppl. A.1 for further details). Unless specified otherwise, SNNs were run for $T = 8$ timesteps as in Ding et al. (2022).

5.2 Robust Training Configurations

Baseline ANNs: We performed adversarially robust ANN-to-SNN conversion with baseline ANNs optimized via state-of-the-art robust training objectives: standard AT (Madry et al., 2018), TRADES (Zhang et al., 2019a), and MART (Wang et al., 2020), as well as ANNs optimized with natural training. We mainly focus on adversarial training with a perturbation bound of $\epsilon_1 = 2/255$. In addition, for CIFAR-10 we also performed conversion of ANNs with standard AT under $\epsilon_2 = 4/255$ and $\epsilon_3 = 8/255$. This resulted in baseline ANNs with: AT-ϵ_1, TRADES-ϵ_1, MART-ϵ_1, AT-ϵ_2, AT-ϵ_3.

Converted SNNs: Robust finetuning was performed for 60 epochs (only for CIFAR-100 we used 80 epochs). Regardless of the baseline ANN training scheme, SNN finetuning was always performed with ϵ_1 bounded perturbations. At test time, we evaluated robustness also at higher perturbation levels ϵ_2 and ϵ_3, similar to Ding et al. (2022). We used $\beta = 2$ for CIFAR-10, and $\beta = 4$ in all other experiments. Further hyper-parameter configurations are detailed in Suppl. A.2.

5.3 Adversarial Robustness Evaluations

White-box Adversarial Attacks: In accordance with the ensemble setting presented in Section 4, we evaluate SNNs against FGSM (Goodfellow et al., 2015), RFGSM (Tramèr et al., 2018), PGD (Madry et al., 2018), and Auto-PGD attacks based on cross-entropy loss (APGD_{CE}) and difference of logits ratio loss (APGD_{DLR}) (Croce & Hein, 2020). We also consider a targeted version of this attack ($\text{T-APGD}_{\text{CE}}$), where each sample was adversarially perturbed towards 9 target classes from CIFAR-10 or CIFAR-100, until

Table 1: Robustness evaluations (%) of baseline ANNs and our converted SNNs across different datasets and architectures. Robust accuracies of converted SNNs are evaluated separately under $\epsilon_1 = 2/255$, $\epsilon_2 = 4/255$, $\epsilon_3 = 8/255$ perturbation budgets, with white-box ensemble attacks. Robustness of baseline ANNs are evaluated with AutoAttack (Croce et al., 2020) at an ϵ_3 perturbation budget.

Dataset & Architecture	ANN Training Objective	Baseline ANN	Adversarially Robust ANN-to-SNN Conversion						
		Clean / ϵ_3-Robust Acc.	Clean Acc.	ϵ_1-Robust Acc.		ϵ_2-Robust Acc.		ϵ_3-Robust Acc.	
				FGSM	PGD^{20}	FGSM	PGD^{20}	FGSM	PGD^{20}
CIFAR-10 with VGG11	Natural	95.10 / 0.00	93.53	66.62	59.22	42.81	22.44	15.71	0.74
	AT-ϵ_1	93.55 / 16.64	92.14	74.10	70.02	59.11	46.59	33.94	13.18
	TRADES-ϵ_1	92.10 / 27.62	91.39	75.01	72.00	62.64	51.47	41.42	19.65
	MART-ϵ_1	92.68 / 21.98	91.47	74.83	70.35	62.87	49.51	44.39	17.79
CIFAR-100 with WRN-16-4	Natural	78.93 / 0.00	70.87	41.16	35.49	26.08	13.87	11.25	1.40
	AT-ϵ_1	74.90 / 7.05	70.02	47.91	44.73	34.74	27.41	18.60	7.64
	TRADES-ϵ_1	73.87 / 8.43	67.84	45.48	42.73	33.62	26.78	18.13	7.79
	MART-ϵ_1	72.61 / 11.04	67.10	45.99	43.46	34.03	27.40	18.93	8.90
SVHN with ResNet-20	Natural	97.08 / 0.08	94.18	77.38	74.30	59.93	48.09	31.50	10.35
	AT-ϵ_1	96.50 / 23.58	91.90	74.15	71.80	60.66	52.68	36.60	21.51
	TRADES-ϵ_1	96.29 / 27.16	92.78	76.38	74.27	62.45	55.59	37.76	23.96
	MART-ϵ_1	96.16 / 27.65	92.71	76.76	74.82	62.60	55.52	37.90	24.11

successful. PGD attack step size η is determined via $2.5 \times \epsilon/\#\text{steps}$ (Madry et al., 2018). For baseline ANNs, we performed evaluations via AutoAttack (Croce et al., 2020) at ϵ_3 (see Table A1 for extended evaluations).

Black-box Adversarial Attacks: We performed query-based Square Attack (Andriushchenko et al., 2020) evaluations with various numbers of limited queries (presented in Section 6.4). We also evaluated transfer-based attacks (Papernot et al., 2017) to verify that such black-box attacks succeed less often than our white-box evaluations (presented in Suppl. B.1).

6 Experimental Results

6.1 Evaluating Robustness of Adversarially Trained ANN-to-SNN Conversion

We present our results in Table 1 using FGSM and PGD^{20} ensemble attacks – which are significantly stronger than the attacks used during robust finetuning – for models obtained by converting baseline ANNs optimized with natural and different adversarial training objectives. These results show that our approach is compatible with any baseline ANN adversarial training algorithm, and an initialization from a relatively more robust ANN proportionally transfers its robustness to the SNN. Although we use an identical robust finetuning procedure, converted SNNs that used weaker (natural training) ANNs show minimal robustness under ensemble attacks (e.g., ϵ_3-PGD^{20} for CIFAR-10, Natural: 0.74, AT-ϵ_1: 13.18, TRADES-ϵ_1: 19.65, MART-ϵ_1: 17.79, similar results can be observed with CIFAR-100 and SVHN). Here, conversion of a natural ANN with robust finetuning is analogous to the HIRE-SNN approach by Kundu et al. (2021), where the finetuning objective and optimized parameters are still slightly different, nevertheless the final robustness remains significantly weak.

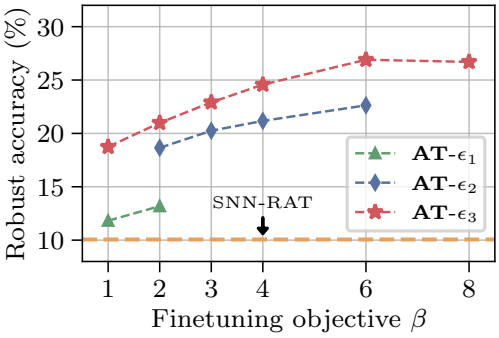


Figure 1: ϵ_3-Robust accuracies under PGD^{20} vs. β, with different baseline ANN standard AT perturbation levels.

Our finetuning objective and the use of trainable V_{th}^l also appear critical to maintain robustness. We elaborate this later in our ablation studies in Suppl. B.3. In brief, we observed that natural $\mathcal{L}_{\text{CE}}$ finetuning (Rathi & Roy, 2021), or using fixed V_{th}^l during

Table 2: Comparisons with the state-of-the-art robust SNN training method SNN-RAT, based on the model checkpoints from Ding et al. (2022). All attacks are l_∞-norm bounded with $\epsilon_3 = 8/255$, and evaluated through an ensemble. Note that FGSM, RFGSM and PGD^7 (with $\eta = 0.01$) are the only attacks evaluated in Ding et al. (2022), which we also include in ensemble setting.

		CIFAR-10 with VGG11				CIFAR-100 with WRN-16-4			
		SNN-RAT	**Conversion (Ours)**			SNN-RAT	**Conversion (Ours)**		
			AT-ϵ_1	**TRADES-ϵ_1**	**MART-ϵ_1**		**AT-ϵ_1**	**TRADES-ϵ_1**	**MART-ϵ_1**
Clean Acc.		90.74	**92.14**	91.39	91.47	69.32	**70.02**	67.84	67.10
ϵ_3-Robust Acc.	FGSM	32.80	33.94	41.42	**44.39**	**19.79**	18.60	18.13	18.93
	RFGSM	55.29	57.52	61.42	**61.59**	32.39	**32.55**	31.77	32.00
	PGD^7	13.47	15.98	**23.63**	23.04	7.76	9.53	9.29	**10.70**
	PGD^{20}	10.06	13.18	**19.65**	17.79	6.04	7.64	7.79	**8.90**
	PGD^{40}	9.45	12.67	**19.20**	16.99	5.84	7.43	7.67	**8.48**
	APGD$_{\text{DLR}}$	11.71	14.07	**23.28**	20.12	8.81	8.88	8.92	**9.68**
	APGD$_{\text{CE}}$	9.07	10.05	**17.63**	15.54	5.22	6.62	6.94	**7.67**
	T-APGD$_{\text{CE}}$	7.69	9.19	**16.11**	13.09	4.72	5.41	5.50	**6.43**

robust finetuning, yields worse robustness (e.g., from Table B4, PGD^{20} ϵ_3-robustness when converting using natural $\mathcal{L}_{\text{CE}}$: 10.03, using Eq. (9) but with fixed V_{th}^l: 11.51, Ours (with trainable V_{th}^l): 13.18).

Fig. 1 shows the impact of baseline ANN training ϵ, on the converted SNN, as well as the robustness-accuracy trade-off parameter in Eq. (9) for CIFAR-10. Note that we still perform finetuning with ϵ_1 similar to Ding et al. (2022), since larger perturbations via BPTT yields an unstable finetuning process. We observe that baseline ANN robustness transfers also in this case, and one can obtain even higher SNN robustness (e.g., ϵ_3-robustness with AT-ϵ_3, $\beta = 6$: 26.90%) by using our method via heavier adversarial training of the ANN where optimization stability is not a problem.

6.2 Comparisons to State-of-the-Art Robust SNNs with Direct Adversarial Training

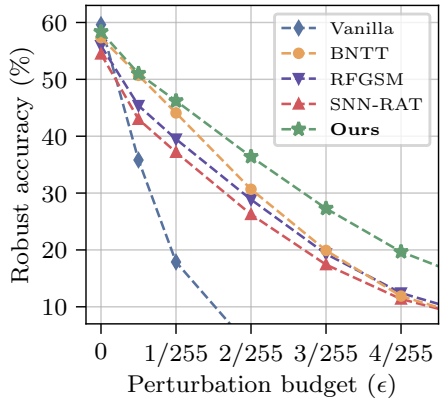
In Table 2, we compare our approach with the current state-of-the-art method SNN-RAT, using the models and specifications from Ding et al. (2022), under extensive white-box ensemble attacks[1]. Our models yield both higher clean accuracy and adversarial robustness across various attacks, with some models being almost twice as robust against strong adversaries, e.g., clean/PGD^{40} for CIFAR-10, SNN-RAT: 90.74/9.45, Ours (TRADES-ϵ_1): 91.39/19.20. Note that in Table 2 we only compare our models trained through baseline ANNs with ϵ_1-perturbations, since SNN-RAT also only uses ϵ_1-adversaries (see Fig. 1 as to where SNN-RAT stands with respect to our models which can also exploit larger perturbation budgets via conversion). Overall, we observe that SNNs gradually get weaker against stronger adversaries, however our models maintain relatively higher robustness, also against powerful APGD$_{\text{CE}}$ and T-APGD$_{\text{CE}}$ attacks.

We further compare our approach with other direct AT methods (e.g., TRADES), within our ablation studies in Suppl. B.3, which again revealed worse performance than our conversion-based approach (e.g., from Table B4, clean/PGD^{20} for CIFAR-10, direct TRADES training: 91.75/6.70, Ours (AT-ϵ_1): 92.14/13.18).

Experiments on TinyImageNet: Results are summarized in Fig. 2. Here, we utilize the same VGG11 architecture used for BNTT (Kim & Panda, 2021b), which has claimed robustness benefits through its batch-norm mechanism combined with Poisson input encoding (see Suppl. A.4 for attack details on this model). For comparisons, besides our usual IF ($T = 8$) setting, we also converted (AT-ϵ_1) ANNs by using LIF neurons ($\tau = 0.99$) and soft-reset with direct coding.

Results in Fig. 2b show that our model achieves a scalable, state-of-the-art solution for adversarially robust SNNs. Our model remains superior to RFGSM and SNN-RAT based end-to-end AT methods in the usual IF

[1]The original work in Ding et al. (2022) reports a BPTT-based PGD^7 with 21.16% on CIFAR-10, and 11.31% on CIFAR-100 ϵ_3-robustness. While we could confirm these results in their naive BPTT setting, this particular attack yielded lower SNN-RAT robust accuracies with our ensemble attack: 13.47% on CIFAR-10, and 7.76% on CIFAR-100.



(a) Robustness under PGD^{20} attacks.

	Input Enc.	SNN Config.	Adv. Train	Clean Acc.	ϵ_2-Robust Acc.	
					FGSM	PGD^{20}
Vanilla	Direct	IF ($T = 8$)	✗	57.29	1.93	0.13
RFGSM	Direct	IF ($T = 8$)	✓	54.29	19.21	14.55
SNN-RAT	Direct	IF ($T = 8$)	✓	52.76	22.39	16.63
Ours (AT-ϵ_1)	Direct	IF ($T = 8$)	✓	55.98	**22.91**	**17.82**
Vanilla	Direct	LIF ($T = 30$)	✗	59.62	1.76	0.05
BNTT	Poisson	LIF ($T = 30$)	✗	57.33	17.64	11.88
RFGSM	Direct	LIF ($T = 8$)	✓	55.92	17.51	12.42
SNN-RAT	Direct	LIF ($T = 8$)	✓	54.47	19.66	11.37
Ours (AT-ϵ_1)	Direct	LIF ($T = 8$)	✓	57.21	22.52	16.25
Ours (AT-ϵ_1)	Direct	LIF ($T = 30$)	✓	58.36	**24.02**	**19.67**

(b) Comparisons with $\epsilon_2 = 4/255$ attacks.

Figure 2: Evaluations on TinyImageNet, with comparisons to SNN-RAT (Ding et al., 2022), an RFGSM based mixed AT baseline from Ding et al. (2022), BNTT (Kim & Panda, 2021b), and a vanilla SNN with natural training. SNNs with LIF neurons ($\tau = 0.99$) use soft-reset as in Kim & Panda (2021b). In (a) we compare LIF-neuron models from the bottom half of the table in (b), using Ours with $T = 30$.

($T = 8$) setting with 17.82% robust accuracy. Results with LIF neurons show that our models can improve clean accuracy and robustness with higher T ($T = 30$)[2], whereas RFGSM and SNN-RAT perform generally worse with LIF neurons. Results in Fig. 2a also reveal stronger robustness of our LIF-based ($T = 30$) model starting from smaller perturbations, where it consistently outperforms existing methods. Our evaluations of BNTT show that AT is particularly useful for robustness (Ours ($T = 30$): 19.67%, BNTT: 11.88%). Although direct coding does not approximate inputs and attacks become simpler (Kim et al., 2022a), we show that direct coding SNNs can still yield higher resilience when adversarially calibrated.

6.3 Coding Efficiency of Adversarially Robust SNNs

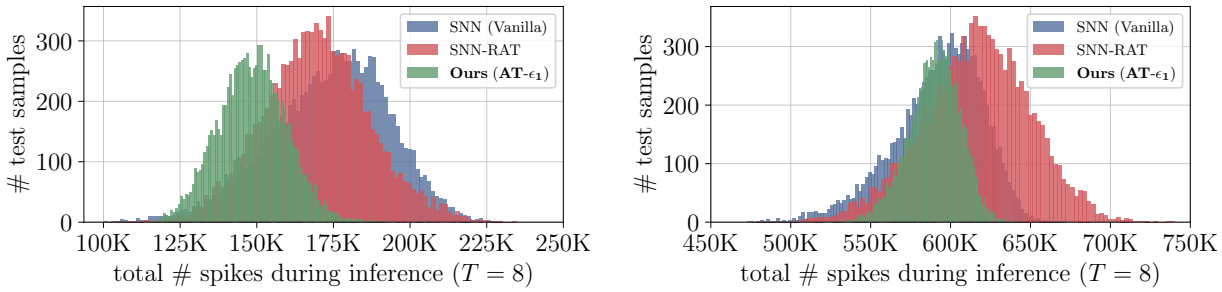
In Fig. 3, we demonstrate higher coding efficiency of our approach. Specifically, VGG11 models consisted of 286,720 IF neurons operating for $T = 8$ timesteps, which could induce a total of approx. 2.3M possible spikes for inference on a single sample. For CIFAR-10, on average for a test sample (i.e., mean of histograms in Fig. 3a), the total #spikes elicited across a VGG11 was 148,490 with Ours, 169,566 for SNN-RAT, and 173,887 for a vanilla SNN. This indicates an average of only 6.47% active spiking neurons with our method, whereas SNN-RAT: 7.39%, and vanilla SNN: 7.58%. For CIFAR-100 in Fig. 3b, total #spikes elicited on average was 589,774 with Ours, 616,439 for SNN-RAT, and 592,297 for vanilla SNN, across approx. 3.8M possible spikes from the 475,136 neurons in WRN-16-4. Here, our model was 15.52% actively spiking, whereas 16.22% with SNN-RAT. We did not observe an efficiency change with our more robust SNNs, and spike activity was similar to the models converted from a baseline ANN with AT-ϵ_1.

6.4 Further Experiments

Query-based Black-box Robustness: We evaluated SNNs with adversaries who have no knowledge of the defended model parameters, but can send a limited number of queries to it. Results are shown in Fig. 4, where our models consistently yield higher robustness (CIFAR-10 at 5000 queries: Ours: 50.2 vs. SNN-RAT: 46.3, CIFAR-100: 18.8 vs. 17.5). We also see that after 1000 queries, the baseline ANN shows weaker resilience than our SNNs. This reveals improved black-box robustness upon conversion to a spiking architecture, which is consistent with previous findings (Sharmin et al., 2020).

Transfer-based Black-box Robustness: Previous work (Athalye et al., 2018a) suggests that transfer-based attacks should be considered as a baseline to verify no potential influence of gradient masking or obfuscation.

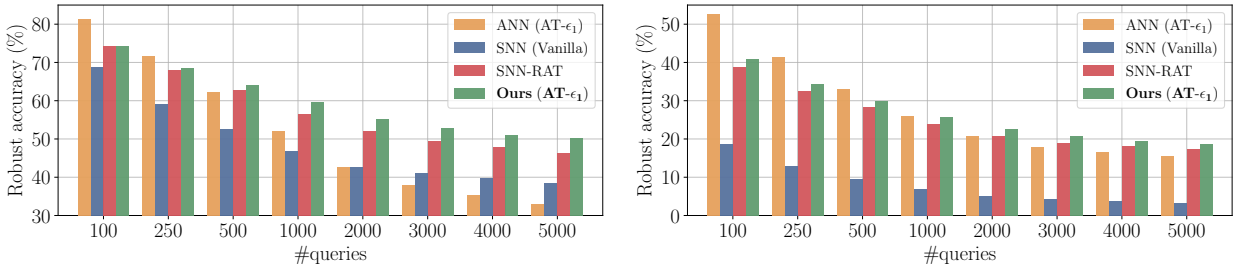
[2]End-to-end adversarial SNN training, e.g., with SNN-RAT, for $T = 30$ was computationally infeasible using BPTT.



(a) CIFAR-10 with VGG11

(b) CIFAR-100 with WRN-16-4

Figure 3: Coding efficiency comparisons of vanilla and adversarially robust SNNs.



(a) CIFAR-10 evaluations with VGG11

(b) CIFAR-100 evaluations with WRN-16-4

Figure 4: Square Attack (Andriushchenko et al., 2020) evaluations with limited number of queries for the baseline ANN (AT-ϵ_1), end-to-end trained vanilla SNN, adversarially trained SNN-RAT, and ours (AT-ϵ_1).

Accordingly, we present our evaluations in Suppl. B.1, where we verify (in Table B1) that fully black-box transfer attacks succeed less often than our ensemble white-box evaluations.

Performance of Ensemble Attacks: We elaborate the effectiveness of our ensemble attack approach in Suppl. B.2. In brief, we reveal that changing the shape or dampening magnitude of the surrogate gradient during BPTT can result in much stronger adversaries. Specifically, these attacks revealed stronger and more accurate robustness evaluations for SNNs directly optimized with AT (Ding et al., 2022). We argue that our attacks reveal a more reliable robustness quantification for SNNs.

Out-of-distribution Generalization: We evaluated robust SNNs on CIFAR-10/100-C benchmarks (Hendrycks & Dietterich, 2019) in Suppl. B.4. Our analyses yielded mean CIFAR-10-C accuracies of 83.85% with our model, whereas SNN-RAT: 81.72%, Vanilla SNN: 81.22% (CIFAR-100-C, Ours: 54.06%, SNN-RAT: 51.95%, Vanilla SNN: 46.14%). We observed that this result was consistent for all corruptions beyond noise (Patel et al., 2019) (see Tables B5 and B6).

7 Discussion

We propose an adversarially robust ANN-to-SNN conversion algorithm that exploits robustly trained baseline ANN weights at initialization, to improve SNN resiliency. Our method shows state-of-the-art robustness in feed-forward SNNs with low latency, outperforming recent end-to-end AT based methods in robustness, generalization, and coding efficiency. Our approach embraces any robust ANN training method to be incorporated in the domain of SNNs, and can also adopt further improvements to robustness, such as leveraging additional data (Rebuffi et al., 2021). Importantly, we empirically show that SNN evaluations against non-adaptive adversaries can be misleading (Carlini et al., 2019; Pintor et al., 2022), which has been the common practice in the field of SNNs.

We argue that direct AT methods developed for ANNs yield limited SNN robustness both because of their computational limitations with BPTT (e.g., use of single-step inner maximization), and also our findings

with BPTT-based AT leading to SNNs with bias to the used surrogate gradient and vulnerability against adversaries that can leverage this. Therefore we propose to harness stronger and stable AT possibility through ANNs, and exploit better robustness gains.

There were no observed white-box robustness benefits of SNNs with respect to ANNs. However, under black-box scenarios, our converted SNNs were more resilient. Overall, we achieved to significantly improve robustness of deep SNNs, considering their progress in safety-critical settings (Davies et al., 2021). Since SNNs offer a promising energy-efficient technology, we argue that their robustness should be an important concern to be studied for reliable AI applications.

7.1 Limitations

There are two main application scenarios for SNNs: (1) on event-based data, (2) standard non-event-based data sets where one can still achieve significant energy savings via SNNs (Davies et al., 2021). In our study we only focus on the latter, that is on direct coding SNNs with low latency where conventional attacks remain powerful as an important open problem. In this case, we can simply use a conventional ANN that is robustly pre-trained on the same task, which our method requires. On the other hand, DVS adversaries constitute a different problem setting tailored to the event-based domain where a pre-trained ANN is not available. This problem also requires consideration of specialized attacks where adversarial noise should be binary, hence the conventional l_∞-norm attacks are not directly applicable (Marchisio et al., 2021; Büchel et al., 2022).

References

Maksym Andriushchenko, Francesco Croce, Nicolas Flammarion, and Matthias Hein. Square attack: a query-efficient black-box adversarial attack via random search. In *European Conference on Computer Vision*, pp. 484–501, 2020.

Anish Athalye, Nicholas Carlini, and David Wagner. Obfuscated gradients give a false sense of security: Circumventing defenses to adversarial examples. In *International Conference on Machine Learning*, pp. 274–283, 2018a.

Anish Athalye, Logan Engstrom, Andrew Ilyas, and Kevin Kwok. Synthesizing robust adversarial examples. In *International Conference on Machine Learning*, pp. 284–293, 2018b.

Guillaume Bellec, Darjan Salaj, Anand Subramoney, Robert Legenstein, and Wolfgang Maass. Long short-term memory and learning-to-learn in networks of spiking neurons. *Advances in Neural Information Processing Systems*, 31, 2018.

Yoshua Bengio, Nicholas Léonard, and Aaron Courville. Estimating or propagating gradients through stochastic neurons for conditional computation. *arXiv preprint arXiv:1308.3432*, 2013.

Wieland Brendel and Matthias Bethge. Comment on "biologically inspired protection of deep networks from adversarial attacks"'. *arXiv preprint arXiv:1704.01547*, 2017.

Tong Bu, Wei Fang, Jianhao Ding, PengLin Dai, Zhaofei Yu, and Tiejun Huang. Optimal ANN-SNN conversion for high-accuracy and ultra-low-latency spiking neural networks. In *International Conference on Learning Representations*, 2022.

Julian Büchel, Gregor Lenz, Yalun Hu, Sadique Sheik, and Martino Sorbaro. Adversarial attacks on spiking convolutional neural networks for event-based vision. *Frontiers in Neuroscience*, 16, 2022.

Yongqiang Cao, Yang Chen, and Deepak Khosla. Spiking deep convolutional neural networks for energy-efficient object recognition. *International Journal of Computer Vision*, 113:54–66, 2015.

Nicholas Carlini, Anish Athalye, Nicolas Papernot, Wieland Brendel, Jonas Rauber, Dimitris Tsipras, Ian Goodfellow, Aleksander Madry, and Alexey Kurakin. On evaluating adversarial robustness. *arXiv preprint arXiv:1902.06705*, 2019.

Moustapha Cisse, Piotr Bojanowski, Edouard Grave, Yann Dauphin, and Nicolas Usunier. Parseval networks: improving robustness to adversarial examples. In *International Conference on Machine Learning*, pp. 854–863, 2017.

Francesco Croce and Matthias Hein. Reliable evaluation of adversarial robustness with an ensemble of diverse parameter-free attacks. In *International Conference on Machine Learning*, pp. 2206–2216, 2020.

Francesco Croce, Maksym Andriushchenko, Vikash Sehwag, Edoardo Debenedetti, Nicolas Flammarion, Mung Chiang, Prateek Mittal, and Matthias Hein. Robustbench: a standardized adversarial robustness benchmark. *arXiv preprint arXiv:2010.09670*, 2020.

Mike Davies, Andreas Wild, Garrick Orchard, Yulia Sandamirskaya, Gabriel A Fonseca Guerra, Prasad Joshi, Philipp Plank, and Sumedh R Risbud. Advancing neuromorphic computing with Loihi: A survey of results and outlook. *Proceedings of the IEEE*, 109(5):911–934, 2021.

Shikuang Deng, Yuhang Li, Shanghang Zhang, and Shi Gu. Temporal efficient training of spiking neural network via gradient re-weighting. In *International Conference on Learning Representations*, 2022.

Peter U Diehl, Daniel Neil, Jonathan Binas, Matthew Cook, Shih-Chii Liu, and Michael Pfeiffer. Fast-classifying, high-accuracy spiking deep networks through weight and threshold balancing. In *International Joint Conference on Neural Networks (IJCNN)*, pp. 1–8. IEEE, 2015.

Jianhao Ding, Tong Bu, Zhaofei Yu, Tiejun Huang, and Jian Liu. SNN-RAT: Robustness-enhanced spiking neural network through regularized adversarial training. *Advances in Neural Information Processing Systems*, 35:24780–24793, 2022.

Chaoteng Duan, Jianhao Ding, Shiyan Chen, Zhaofei Yu, and Tiejun Huang. Temporal effective batch normalization in spiking neural networks. *Advances in Neural Information Processing Systems*, 35:34377–34390, 2022.

Rida El-Allami, Alberto Marchisio, Muhammad Shafique, and Ihsen Alouani. Securing deep spiking neural networks against adversarial attacks through inherent structural parameters. In *Design, Automation & Test in Europe Conference & Exhibition (DATE)*, pp. 774–779. IEEE, 2021.

Wei Fang, Zhaofei Yu, Yanqi Chen, Tiejun Huang, Timothée Masquelier, and Yonghong Tian. Deep residual learning in spiking neural networks. *Advances in Neural Information Processing Systems*, 34:21056–21069, 2021.

Ian J Goodfellow, Jonathon Shlens, and Christian Szegedy. Explaining and harnessing adversarial examples. In *International Conference on Learning Representations*, 2015.

Bing Han, Gopalakrishnan Srinivasan, and Kaushik Roy. RMP-SNN: Residual membrane potential neuron for enabling deeper high-accuracy and low-latency spiking neural network. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pp. 13558–13567, 2020.

Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pp. 770–778, 2016.

Dan Hendrycks and Thomas Dietterich. Benchmarking neural network robustness to common corruptions and perturbations. In *International Conference on Learning Representations*, 2019.

Sergey Ioffe and Christian Szegedy. Batch normalization: Accelerating deep network training by reducing internal covariate shift. In *International Conference on Machine Learning*, pp. 448–456, 2015.

Haiyan Jiang, Srinivas Anumasa, Giulia De Masi, Huan Xiong, and Bin Gu. A unified optimization framework of ANN-SNN conversion: towards optimal mapping from activation values to firing rates. In *International Conference on Machine Learning*, pp. 14945–14974, 2023.

Hoki Kim. Torchattacks: A Pytorch repository for adversarial attacks. *arXiv preprint arXiv:2010.01950*, 2020.

Youngeun Kim and Priyadarshini Panda. Optimizing deeper spiking neural networks for dynamic vision sensing. *Neural Networks*, 144:686–698, 2021a.

Youngeun Kim and Priyadarshini Panda. Revisiting batch normalization for training low-latency deep spiking neural networks from scratch. *Frontiers in Neuroscience*, pp. 1638, 2021b.

Youngeun Kim and Priyadarshini Panda. Visual explanations from spiking neural networks using inter-spike intervals. *Scientific Reports*, 11(1):19037, 2021c.

Youngeun Kim, Hyoungseob Park, Abhishek Moitra, Abhiroop Bhattacharjee, Yeshwanth Venkatesha, and Priyadarshini Panda. Rate coding or direct coding: Which one is better for accurate, robust, and energy-efficient spiking neural networks? In *IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)*, pp. 71–75, 2022a.

Youngeun Kim, Yeshwanth Venkatesha, and Priyadarshini Panda. PrivateSNN: privacy-preserving spiking neural networks. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 36, pp. 1192–1200, 2022b.

Klim Kireev, Maksym Andriushchenko, and Nicolas Flammarion. On the effectiveness of adversarial training against common corruptions. In *Uncertainty in Artificial Intelligence*, pp. 1012–1021, 2022.

Alex Krizhevsky. Learning multiple layers of features from tiny images. *Technical Report, University of Toronto*, 2009.

Souvik Kundu, Massoud Pedram, and Peter A Beerel. HIRE-SNN: Harnessing the inherent robustness of energy-efficient deep spiking neural networks by training with crafted input noise. In *Proceedings of the IEEE/CVF International Conference on Computer Vision (ICCV)*, pp. 5209–5218, 2021.

Ya Le and Xuan Yang. Tiny ImageNet visual recognition challenge, 2015.

Chankyu Lee, Syed Shakib Sarwar, Priyadarshini Panda, Gopalakrishnan Srinivasan, and Kaushik Roy. Enabling spike-based backpropagation for training deep neural network architectures. *Frontiers in Neuroscience*, pp. 119, 2020.

Yuhang Li, Shikuang Deng, Xin Dong, Ruihao Gong, and Shi Gu. A free lunch from ANN: Towards efficient, accurate spiking neural networks calibration. In *International Conference on Machine Learning*, pp. 6316–6325. PMLR, 2021.

Yuhang Li, Youngeun Kim, Hyoungseob Park, and Priyadarshini Panda. Uncovering the representation of spiking neural networks trained with surrogate gradient. *Transactions on Machine Learning Research*, 2023.

Ling Liang, Xing Hu, Lei Deng, Yujie Wu, Guoqi Li, Yufei Ding, Peng Li, and Yuan Xie. Exploring adversarial attack in spiking neural networks with spike-compatible gradient. *IEEE Transactions on Neural Networks and Learning Systems*, 2021.

Ling Liang, Kaidi Xu, Xing Hu, Lei Deng, and Yuan Xie. Toward robust spiking neural network against adversarial perturbation. *Advances in Neural Information Processing Systems*, 35:10244–10256, 2022.

Sen Lu and Abhronil Sengupta. Exploring the connection between binary and spiking neural networks. *Frontiers in Neuroscience*, 14:535, 2020.

Wolfgang Maass. Networks of spiking neurons: the third generation of neural network models. *Neural Networks*, 10(9):1659–1671, 1997.

Aleksander Madry, Aleksandar Makelov, Ludwig Schmidt, Dimitris Tsipras, and Adrian Vladu. Towards deep learning models resistant to adversarial attacks. In *International Conference on Learning Representations*, 2018.

Alberto Marchisio, Giorgio Nanfa, Faiq Khalid, Muhammad Abdullah Hanif, Maurizio Martina, and Muhammad Shafique. Is spiking secure? a comparative study on the security vulnerabilities of spiking and deep neural networks. In *International Joint Conference on Neural Networks (IJCNN)*, pp. 1–8. IEEE, 2020.

Alberto Marchisio, Giacomo Pira, Maurizio Martina, Guido Masera, and Muhammad Shafique. Dvs-attacks: Adversarial attacks on dynamic vision sensors for spiking neural networks. In *International Joint Conference on Neural Networks (IJCNN)*, pp. 1–9. IEEE, 2021.

Emre O Neftci, Hesham Mostafa, and Friedemann Zenke. Surrogate gradient learning in spiking neural networks: Bringing the power of gradient-based optimization to spiking neural networks. *IEEE Signal Processing Magazine*, 36(6):51–63, 2019.

Yuval Netzer, Tao Wang, Adam Coates, Alessandro Bissacco, Bo Wu, and Andrew Y Ng. Reading digits in natural images with unsupervised feature learning, 2011.

Nicolas Papernot, Patrick McDaniel, Ian Goodfellow, Somesh Jha, Z Berkay Celik, and Ananthram Swami. Practical black-box attacks against machine learning. In *Proceedings of the 2017 ACM on Asia Conference on Computer and Communications Security*, pp. 506–519, 2017.

Adam Paszke et al. Pytorch: An imperative style, high-performance deep learning library. *Advances in Neural Information Processing Systems*, 32:8026–8037, 2019.

Devdhar Patel, Hananel Hazan, Daniel J Saunders, Hava T Siegelmann, and Robert Kozma. Improved robustness of reinforcement learning policies upon conversion to spiking neuronal network platforms applied to atari breakout game. *Neural Networks*, 120:108–115, 2019.

Maura Pintor, Luca Demetrio, Angelo Sotgiu, Ambra Demontis, Nicholas Carlini, Battista Biggio, and Fabio Roli. Indicators of attack failure: Debugging and improving optimization of adversarial examples. *Advances in Neural Information Processing Systems*, 35:23063–23076, 2022.

Nitin Rathi and Kaushik Roy. DIET-SNN: A low-latency spiking neural network with direct input encoding and leakage and threshold optimization. *IEEE Transactions on Neural Networks and Learning Systems*, pp. 1–9, 2021.

Nitin Rathi, Gopalakrishnan Srinivasan, Priyadarshini Panda, and Kaushik Roy. Enabling deep spiking neural networks with hybrid conversion and spike timing dependent backpropagation. In *International Conference on Learning Representations*, 2020.

Sylvestre-Alvise Rebuffi, Sven Gowal, Dan Andrei Calian, Florian Stimberg, Olivia Wiles, and Timothy A Mann. Data augmentation can improve robustness. *Advances in Neural Information Processing Systems*, 34:29935–29948, 2021.

Kaushik Roy, Akhilesh Jaiswal, and Priyadarshini Panda. Towards spike-based machine intelligence with neuromorphic computing. *Nature*, 575(7784):607–617, 2019.

Bodo Rueckauer, Iulia-Alexandra Lungu, Yuhuang Hu, and Michael Pfeiffer. Theory and tools for the conversion of analog to spiking convolutional neural networks. *arXiv preprint arXiv:1612.04052*, 2016.

Bodo Rueckauer, Iulia-Alexandra Lungu, Yuhuang Hu, Michael Pfeiffer, and Shih-Chii Liu. Conversion of continuous-valued deep networks to efficient event-driven networks for image classification. *Frontiers in Neuroscience*, 11:682, 2017.

Abhronil Sengupta, Yuting Ye, Robert Wang, Chiao Liu, and Kaushik Roy. Going deeper in spiking neural networks: VGG and residual architectures. *Frontiers in Neuroscience*, 13:95, 2019.

Saima Sharmin, Priyadarshini Panda, Syed Shakib Sarwar, Chankyu Lee, Wachirawit Ponghiran, and Kaushik Roy. A comprehensive analysis on adversarial robustness of spiking neural networks. In *International Joint Conference on Neural Networks (IJCNN)*, pp. 1–8. IEEE, 2019.

Saima Sharmin, Nitin Rathi, Priyadarshini Panda, and Kaushik Roy. Inherent adversarial robustness of deep spiking neural networks: Effects of discrete input encoding and non-linear activations. In *European Conference on Computer Vision*, pp. 399–414, 2020.

Sumit B Shrestha and Garrick Orchard. Slayer: Spike layer error reassignment in time. *Advances in Neural Information Processing Systems*, 31, 2018.

Karen Simonyan and Andrew Zisserman. Very deep convolutional networks for large-scale image recognition. In *International Conference on Learning Representations*, 2015.

Christian Szegedy, Wojciech Zaremba, Ilya Sutskever, Joan Bruna, Dumitru Erhan, Ian Goodfellow, and Rob Fergus. Intriguing properties of neural networks. *arXiv preprint arXiv:1312.6199*, 2013.

Jihoon Tack, Sihyun Yu, Jongheon Jeong, Minseon Kim, Sung Ju Hwang, and Jinwoo Shin. Consistency regularization for adversarial robustness. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 36, pp. 8414–8422, 2022.

Florian Tramèr, Alexey Kurakin, Nicolas Papernot, Ian Goodfellow, Dan Boneh, and Patrick McDaniel. Ensemble adversarial training: Attacks and defenses. In *International Conference on Learning Representations*, 2018.

Dimitris Tsipras, Shibani Santurkar, Logan Engstrom, Alexander Turner, and Aleksander Madry. Robustness may be at odds with accuracy. In *International Conference on Learning Representations*, 2019.

Yisen Wang, Difan Zou, Jinfeng Yi, James Bailey, Xingjun Ma, and Quanquan Gu. Improving adversarial robustness requires revisiting misclassified examples. In *International Conference on Learning Representations*, 2020.

Eric Wong, Leslie Rice, and J Zico Kolter. Fast is better than free: Revisiting adversarial training. In *International Conference on Learning Representations*, 2020.

Yujie Wu, Lei Deng, Guoqi Li, Jun Zhu, and Luping Shi. Spatio-temporal backpropagation for training high-performance spiking neural networks. *Frontiers in Neuroscience*, 12:331, 2018.

Yujie Wu, Lei Deng, Guoqi Li, Jun Zhu, Yuan Xie, and Luping Shi. Direct training for spiking neural networks: Faster, larger, better. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 33, pp. 1311–1318, 2019.

Nuo Xu, Kaleel Mahmood, Haowen Fang, Ethan Rathbun, Caiwen Ding, and Wujie Wen. Securing the spike: On the transferabilty and security of spiking neural networks to adversarial examples. *arXiv preprint arXiv:2209.03358*, 2022.

Sergey Zagoruyko and Nikos Komodakis. Wide residual networks. In *British Machine Vision Conference*, 2016.

Hongyang Zhang, Yaodong Yu, Jiantao Jiao, Eric Xing, Laurent El Ghaoui, and Michael Jordan. Theoretically principled trade-off between robustness and accuracy. In *International Conference on Machine Learning*, pp. 7472–7482, 2019a.

Huan Zhang, Hongge Chen, Chaowei Xiao, Sven Gowal, Robert Stanforth, Bo Li, Duane Boning, and Cho-Jui Hsieh. Towards stable and efficient training of verifiably robust neural networks. *arXiv preprint arXiv:1906.06316*, 2019b.

Hanle Zheng, Yujie Wu, Lei Deng, Yifan Hu, and Guoqi Li. Going deeper with directly-trained larger spiking neural networks. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 35, pp. 11062–11070, 2021.

A Details on the Experimental Setup

A.1 Datasets and Models

We experimented with CIFAR-10, CIFAR-100, SVHN and TinyImageNet datasets. CIFAR-10 and CIFAR-100 datasets both consist of 50,000 training and 10,000 test images of resolution 32×32, from 10 and 100 classes respectively (Krizhevsky, 2009). SVHN dataset consists of 73,257 training and 26,032 test samples of resolution 32×32 from 10 classes (Netzer et al., 2011). TinyImageNet dataset consists of 100,000 training and 10,000 test images of resolution 64×64 from 200 classes (Le & Yang, 2015). We use VGG11 (Simonyan & Zisserman, 2015), ResNet-20 (He et al., 2016) and WideResNet (Zagoruyko & Komodakis, 2016) models with depth 16 and width 4 (i.e., WRN-16-4).

For baseline ANN optimization, we adopted the conventional data augmentation approaches that were found beneficial in robust adversarial training (Rebuffi et al., 2021; Tack et al., 2022). During SNN finetuning after conversion, we follow the simple traditional data augmentation scheme that was also adopted in previous work (Ding et al., 2022). This procedure involves randomly cropping images into 32×32 dimensions by padding zeros for at most 4 pixels around it, and randomly performing a horizontal flip. For TinyImageNet we instead perform a random resized crop to 64×64, also followed by a random horizontal flip. All image pixel values are normalized using the conventional metrics estimated on the training set of each dataset.

A.2 Robust Training Configurations

Baseline ANNs: During robust optimization with standard AT, TRADES, and MART, adversarial examples are iteratively crafted for each mini-batch (inner maximization step of Eq. (4)), by using 10 PGD steps with random starts under l_∞-bounded perturbations, and $\eta = 2.5 \times \epsilon/\#\text{steps}$. For standard AT and MART we perform the inner maximization PGD using $\mathcal{L}_{\text{PGD}} = \mathcal{L}_{\text{CE}}(f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}}), y)$, whereas for TRADES we use $\mathcal{L}_{\text{PGD}} = D_{\text{KL}}(f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}})||f_{\boldsymbol{\theta}}(\mathbf{x}))$ as the inner maximization loss, following the original works (Madry et al., 2018; Zhang et al., 2019a; Wang et al., 2020). We set the trade-off parameter $\lambda_{\text{MART}} = 4$ in all experiments, and $\lambda_{\text{TRADES}} = 6$ in CIFAR-10 and $\lambda_{\text{TRADES}} = 3$ in CIFAR-100 and SVHN experiments. We present extended robustness evaluations of the baseline ANNs used in our experiments in Table A1.

Converted SNNs: During initialization of layer-wise firing thresholds, we use 10 training mini-batches of size 64 with a calibration sequence length of $T_c = 100$ timesteps, and observe the pre-activation values. We choose the maximum value in the $\rho = 99.7\%$ percentile of the distribution of observed values. This process is performed similarly to (Rathi & Roy, 2021; Lu & Sengupta, 2020), and is a better alternative to simply using the largest observed pre-activation value for threshold balancing (Sengupta et al., 2019), since the procedure involves the use of randomly sampled training batches which might lead to large valued outliers compared to the rest of the distribution. We use $\kappa = 0.3$ in CIFAR-10 and SVHN, and $\kappa = 0.1$ in CIFAR-100 and TinyImageNet experiments. During BPTT-based finetuning, we used the piecewise linear surrogate gradient in Eq (16) with $\gamma_w = 1$, as in Ding et al. (2022). For the initial random step of RFGSM, we set $\alpha = \epsilon_1/2$ in CIFAR-10 and SVHN, and $\alpha = \epsilon_1/5$ in CIFAR-100 and TinyImageNet experiments. For CIFAR-10 experiments with AT-ϵ_2 and AT-ϵ_3, we used $\alpha = \epsilon/4$.

End-to-end trained SNNs used for comparisons were initialized statically at $V_{th}^l = 1$ for all layers, as in Ding et al. (2022). During robust finetuning, we impose a lower bound for the trainable firing thresholds such that they remain $V_{th}^l \geq 0.03$. At inference-time with our models, for tdBN layers, we use the mean and variance moving averages estimated during the robust finetuning process from scratch. Since we performed conversion with baseline ANNs without bias terms (Sengupta et al., 2019; Rueckauer et al., 2016), only in CIFAR-10/100 experiments we introduce bias terms during finetuning in the output dense layers to be also optimized, in order to have identical networks to SNN-RAT. Although it slightly increased model performance, we did not find the use of bias terms strictly necessary in our method.

Optimization: We used momentum SGD with a cosine annealing based learning rate scheduler, and a batch size of 64 in all model training settings. All end-to-end trained models (i.e., baseline ANNs and vanilla SNNs) were optimized for 200 epochs with an initial learning rate of 0.1, following the conventional settings (Madry et al., 2018; Zhang et al., 2019a; Wang et al., 2020). After ANN-to-SNN conversion and

Table A1: Robustness evaluations (%) of used baseline ANN architectures in our experiments. All attacks are evaluated under an l_∞-norm bounded $\epsilon_3 = 8/255$ perturbation budget. AA_∞ indicates AutoAttack evaluations. PGD attack step sizes were determined by $2.5 \times \epsilon/\#\text{steps}$. Maximum number of queries for SquareAttack were set to 5000.

		Clean Acc.	ϵ_3-Robust Accuracies					
			FGSM	PGD^{10}	PGD^{50}	APGD_{CE}	Square	AA_∞
CIFAR-10 with VGG11	Natural	95.10	20.35	0.13	0.06	1.07	0.45	0.00
	AT-ϵ_1	93.55	42.71	21.86	20.76	18.98	32.99	16.64
	TRADES-ϵ_1	92.10	51.26	33.59	32.56	29.75	41.90	27.62
	MART-ϵ_1	92.68	47.21	28.43	27.43	24.58	37.56	21.98
	AT-ϵ_2	91.05	51.55	37.00	36.32	34.62	45.87	32.61
	AT-ϵ_3	85.07	58.30	53.57	53.24	51.65	52.98	45.05
CIFAR-100 with WRN-16-4	Natural	78.93	6.79	0.00	0.00	0.00	0.00	0.00
	AT-ϵ_1	74.90	20.23	9.85	9.34	8.49	15.53	7.05
	TRADES-ϵ_1	73.87	20.40	11.07	10.53	9.64	15.61	8.43
	MART-ϵ_1	72.61	23.93	15.08	14.47	13.26	19.51	11.04
SVHN with ResNet-20	Natural	97.08	63.83	0.71	0.08	1.87	1.38	0.08
	AT-ϵ_1	96.50	52.53	30.36	29.25	25.86	29.30	23.58
	TRADES-ϵ_1	96.29	54.11	33.43	32.18	29.13	32.10	27.16
	MART-ϵ_1	96.16	56.66	36.02	34.82	31.04	31.70	27.65

setting initial thresholds, SNNs were finetuned for 60 epochs on CIFAR-10, SVHN and TinyImageNet, and 80 epochs on CIFAR-100, with an initial learning rate of 0.001. During robust finetuning, we used a weight decay parameter of 0.001 in CIFAR-10, SVHN and TinyImageNet experiments, whereas we used 0.0001 for CIFAR-100. We also used lower weight decay parameters of 0.0005 and 0.0001 during post-conversion finetuning of AT-ϵ_2 and AT-ϵ_3 models respectively in our CIFAR-10 experiments.

Computational Overhead: Although our method uses a larger amount of total training epochs (baseline ANN training and robust SNN finetuning), the overhead does not differ much from end-to-end AT methods (e.g., SNN-RAT) due to the heavier computational load of AT with SNNs which involves the temporal dimension. To illustrate quantitatively (CIFAR-10 with VGG11), Ours: baseline ANN training for 200 epochs takes $\sim$11 hours and robust SNN finetuning for 60 epochs takes $\sim$10.5 hours, SNN-RAT: robust end-to-end training for 200 epochs takes $\sim$23 hours wall-clock time.

Implementations: All models were implemented with the PyTorch 1.13.0 (Paszke et al., 2019) library, and experiments were performed using GPU hardware of types NVIDIA A40, NVIDIA Quadro RTX 8000 and NVIDIA Quadro P6000. Adversarial attacks were implemented using the TorchAttacks (Kim, 2020) library, with the default attack hyper-parameters. Our code and implementations will later be publicly available.

A.3 Robust SNN Finetuning Parameter Updates with Surrogate Gradients

Our robust optimization objective after the initial ANN-to-SNN conversion step follows:

$$\min_{\boldsymbol{\theta}} \mathbb{E}\left[\mathcal{L}_{\text{CE}}(f_{\boldsymbol{\theta}}(\mathbf{x}), y) + \beta \cdot \max_{\tilde{\mathbf{x}} \in \Delta_\epsilon^p(\mathbf{x})} D_{\text{KL}}(f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}}) || f_{\boldsymbol{\theta}}(\mathbf{x}))\right], \tag{11}$$

where $\boldsymbol{\theta}$ consist of $\{\mathbf{W}^l, \varphi^l, \omega^l\}_{l=1}^L$ and $\{V_{th}^l\}_{l=1}^{L-1}$, the adversarial example $\tilde{\mathbf{x}} \in \Delta_\epsilon^\infty(\mathbf{x})$ is obtained at the inner maximization via RFGSM using $\mathcal{L}_{\text{RFGSM}} = D_{\text{KL}}(f_{\boldsymbol{\theta}}(\mathbf{x}')||f_{\boldsymbol{\theta}}(\mathbf{x}))$,

$$\mathcal{L}_{\text{CE}} = -\sum_j y^{(j)} \log(f_{\boldsymbol{\theta}}^{(j)}(\mathbf{x})) \quad \text{and} \quad D_{\text{KL}} = \sum_j f_{\boldsymbol{\theta}}^{(j)}(\tilde{\mathbf{x}}) \log \frac{f_{\boldsymbol{\theta}}^{(j)}(\tilde{\mathbf{x}})}{f_{\boldsymbol{\theta}}^{(j)}(\mathbf{x})}. \tag{12}$$

Following the robust optimization objective that minimizes an overall loss function expressed in the brackets of Eq. (11), say $\mathcal{L}_{\text{robust}}$, the gradient-based synaptic connectivity weight and firing threshold updates in the hidden layers of the SNN $l = \{1, \ldots, L-1\}$ are determined via BPTT as:

$$\Delta \mathbf{W}^l = \sum_t \frac{\partial \mathcal{L}_{\text{robust}}}{\partial \mathbf{W}^l} = \sum_t \frac{\partial \mathcal{L}_{\text{robust}}}{\partial \mathbf{s}^l(t)} \frac{\partial \mathbf{s}^l(t)}{\partial \mathbf{z}^l(t)} \frac{\partial \mathbf{z}^l(t)}{\partial \mathbf{v}^l(t^-)} \frac{\partial \mathbf{v}^l(t^-)}{\partial \mathbf{W}^l}, \tag{13}$$

$$\Delta V_{th}^l = \sum_t \frac{\partial \mathcal{L}_{\text{robust}}}{\partial V_{th}^l} = \sum_t \frac{\partial \mathcal{L}_{\text{robust}}}{\partial \mathbf{s}^l(t)} \frac{\partial \mathbf{s}^l(t)}{\partial \mathbf{z}^l(t)} \frac{\partial \mathbf{z}^l(t)}{\partial V_{th}^l}, \tag{14}$$

where $\mathbf{z}^l(t) = \mathbf{v}^l(t^-) - V_{th}^l$ is the input to the Heaviside step function: $\mathbf{s}^l(t) = H(\mathbf{z}^l(t))$. For BPTT we use the piecewise linear surrogate gradient with a unit dampening factor:

$$\frac{\partial \mathbf{s}^l(t)}{\partial \mathbf{z}^l(t)} := \max\{0, 1 - |\,\mathbf{z}^l(t)|\}. \tag{15}$$

Remaining gradient terms can be computed via LIF neuron dynamics. For the layers containing tdBN operations, the parameters φ^l and ω^l are also updated similarly through normalized $\hat{\mathbf{s}}^l(t)$, following the original gradient computations from Ioffe & Szegedy (2015), which are however gathered temporally (Zheng et al., 2021). Since there is no spiking activity in the output layer, weight updates can be computed via BPTT without surrogate gradients, similar to the definitions from (Kundu et al., 2021; Rathi & Roy, 2021). Our complete robust ANN-to-SNN conversion procedure is outlined in Algorithm 1.

A.4 Ensemble Adversarial Attacks

The success of an SNN attack depends critically on the surrogate gradient used for by the adversary. Therefore we consider adaptive adversaries that perform a number of attacks for any test sample, where the surrogate gradient used to approximate the discontinuity of the spike function during BPTT varies in each case. Specifically, as part of the attack ensemble we perform backpropagation by using the piecewise linear (triangular) function (Bellec et al., 2018; Neftci et al., 2019) defined as in Eq. (16) with $\gamma_w \in \{0.25, 0.5, 1.0, 2.0, 3.0\}$,

$$\frac{\partial \mathbf{s}^l(t)}{\partial \mathbf{z}^l(t)} := \frac{1}{\gamma_w^2} \cdot \max\{0, \gamma_w - |\,\mathbf{z}^l(t)|\}, \tag{16}$$

the exponential surrogate gradient function (Shrestha & Orchard, 2018) defined as in Eq. (17) with hyper-parameters $(\gamma_d, \gamma_s) \in \{(0.3, 0.5), (0.3, 1.0), (0.3, 2.0), (1.0, 0.5), (1.0, 1.0), (1.0, 2.0)\}$,

$$\frac{\partial \mathbf{s}^l(t)}{\partial \mathbf{z}^l(t)} := \gamma_d \cdot \exp\left(-\gamma_s \cdot |\,\mathbf{z}^l(t)|\right), \tag{17}$$

and the rectangular function (Wu et al., 2018) defined as in Eq. (18) with $\gamma_w \in \{0.25, 0.5, 1.0, 2.0, 4.0\}$,

$$\frac{\partial \mathbf{s}^l(t)}{\partial \mathbf{z}^l(t)} := \frac{1}{\gamma_w} \cdot \text{sign}\left(|\,\mathbf{z}^l(t)| < \frac{\gamma_w}{2}\right). \tag{18}$$

For the rectangular and piecewise linear (triangular) functions, γ_w indicates the width that determines the input range to activate the gradient. The dampening factor of these surrogate gradients is then inversely proportional to γ_w (Ding et al., 2022; Deng et al., 2022; Wu et al., 2018; 2019). For the exponential function, γ_d controls the dampening and γ_s controls the steepness. A conventional choice for the exponential is $(\gamma_d, \gamma_s) = (0.3, 1.0)$ (Shrestha & Orchard, 2018), while we also experimented by varying these parameters. Interestingly, we could verify that varying the shape and parameters of this surrogate gradient function occasionally had an impact on the success of the adversary for various test samples. This scenario, for instance, indicates having approximate gradient information long before the membrane potential reaches the firing threshold (i.e., larger γ_w), which can be useful to attack SNNs from the perspective of an adaptive adversary. In Section B.2 we present the effectiveness of the individual components of the ensemble.

Algorithm 1 Adversarially robust ANN-to-SNN conversion

Input: Training dataset $\mathcal{D}$, adversarially pre-trained baseline ANN parameters $\{\mathbf{W}^l, \varphi^l, \omega^l\}_{l=1}^{L}$, number of calibration samples, calibration sequence length T_c, percentile ρ, threshold scaling factor κ, number of finetuning iterations, perturbation strength ϵ and random step α for RFGSM, simulation timesteps T, membrane leak factor τ, trade-off parameter β.
Output: Robust SNN f with parameters $\boldsymbol{\theta}$ consisting of $\{\mathbf{W}^l, \varphi^l, \omega^l\}_{l=1}^{L}$ and $\{V_{th}^l\}_{l=1}^{L-1}$.

▷ Converting the adversarially trained baseline ANN
Initialize: Set weights of the SNN f directly from the pre-trained ANN parameters $\{\mathbf{W}^l, \varphi^l, \omega^l\}_{l=1}^{L}$.
for $l = 1$ **to** $L-1$ **do**
  for $c = 1$ **to** $\#calibration_samples$ **do**
    for $t = 1$ **to** T_c **do**
      $\mathbf{r}^l \leftarrow$ Store pre-activation values at layer l during forward pass with direct input coding.
    end for
    if $\max[\rho\text{-percentile of the dist. in } \mathbf{r}^l] > V_{th}^l$ **then**
      $V_{th}^l = \max[\rho\text{-percentile of the distribution in } \mathbf{r}^l]$
    end if
  end for
end for

▷ Initializing trainable firing thresholds
for $l = 1$ **to** $L-1$ **do**
  $V_{th}^l \leftarrow \kappa \cdot V_{th}^l$
end for

▷ Robust finetuning of SNN after conversion
for $i = 1$ **to** $\#finetuning_iterations$ **do**
  Sample a mini-batch of $(\mathbf{x}, y) \sim \mathcal{D}$
  ▷ Inner maximization for single-step adversarial examples
  $\mathbf{x}' \leftarrow \mathbf{x} + \alpha \cdot \text{sign}\left(\mathcal{N}(\mathbf{0}, \mathbf{I})\right)$
  $f_{\boldsymbol{\theta}}(\mathbf{x}'), f_{\boldsymbol{\theta}}(\mathbf{x}) \leftarrow$ Forward pass direct coded $\mathbf{x}'$ and $\mathbf{x}$ via Eqs. (1), (2), (3), (7), with τ.
  $\tilde{\mathbf{x}} \leftarrow \mathbf{x}' + (\epsilon - \alpha) \cdot \text{sign}\left(\nabla_{\mathbf{x}'} \mathcal{L}_{\text{RFGSM}}\right)$ with $\mathcal{L}_{\text{RFGSM}} = D_{\text{KL}}(f_{\boldsymbol{\theta}}(\mathbf{x}') || f_{\boldsymbol{\theta}}(\mathbf{x}))$.
  ▷ Outer optimization with the robust finetuning objective
  $f_{\boldsymbol{\theta}}(\mathbf{x}), f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}}) \leftarrow$ Forward pass direct coded $\mathbf{x}$ and $\tilde{\mathbf{x}}$ via Eqs. (1), (2), (3), (7), with τ.
  $\mathcal{L}_{\text{robust}} \leftarrow \mathbb{E}\left[\mathcal{L}_{\text{CE}}(f_{\boldsymbol{\theta}}(\mathbf{x}), y) + \beta \cdot D_{\text{KL}}\left(f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}}) || f_{\boldsymbol{\theta}}(\mathbf{x})\right)\right]$
  $\Delta\, \mathbf{W}^l \leftarrow \sum_t \frac{\partial\, \mathcal{L}_{\text{robust}}}{\partial\, \mathbf{W}^l}$
  $\Delta \varphi^l \leftarrow \sum_t \frac{\partial\, \mathcal{L}_{\text{robust}}}{\partial \varphi^l}$
  $\Delta \omega^l \leftarrow \sum_t \frac{\partial\, \mathcal{L}_{\text{robust}}}{\partial \omega^l}$
  $\Delta V_{th}^l \leftarrow \sum_t \frac{\partial\, \mathcal{L}_{\text{robust}}}{\partial V_{th}^l}$
end for

In the ensemble, we also considered the straight-through estimator (STE) (Bengio et al., 2013), backward pass through rate (BPTR) (Ding et al., 2022), and a conversion-based approximation, where spiking neurons are replaced with ReLU functions during BPTT (Ding et al., 2022). STE uses an identity function as the surrogate gradient for all SNN neurons during backpropagation. BPTR performs a differentiable approximation by taking the derivative of the spike functions directly from the average firing rate of the neurons between layers (Ding et al., 2022). In this case the gradient does not accumulate through time, and the complete neuronal dynamic is approximated during backpropagation by a single STE that maintains gradients for neurons that have a non-zero spike rate in the forward pass. We use the same BPTR implementation based on the evaluations from Ding et al. (2022). Conversion-based approximation was an earlier attempt to design adversarial attacks on SNNs which we also include, although we found it to be only minimally effective (Sharmin et al., 2019).

Table B1: Evaluating $\epsilon_1 = 2/255$ and $\epsilon_3 = 8/255$ robust accuracies under black-box (BB) transfer attacks (Papernot et al., 2017), obtained via adversarial examples crafted with ensemble PGD^{20} attacks on a source model. In white-box (WB) setting, the source and target models are identical. BB_{SNN} indicates attacks via a source model that undergoes the same ANN-to-SNN conversion procedure as the target model, with a different random seed during finetuning. BB_{ANN} indicates transfer attacks where the source model is the baseline ANN used for conversion (hence no ensemble needed).

			Adversarially Robust ANN-to-SNN Conversion					
		Clean Acc.	ϵ_1-Robust Accuracies			ϵ_3-Robust Accuracies		
			WB	BB_{SNN}	BB_{ANN}	WB	BB_{SNN}	BB_{ANN}
CIFAR-10 with VGG11	Natural	93.53	59.22	76.93	82.21	0.74	6.87	21.99
	AT-ϵ_1	92.14	70.02	85.40	82.04	13.18	42.27	29.81
	TRADES-ϵ_1	91.39	72.00	86.21	82.29	19.65	52.34	38.18
	MART-ϵ_1	91.47	70.35	84.19	81.43	17.79	41.82	32.26
CIFAR-100 with WRN-16-4	Natural	70.87	35.49	45.95	64.44	1.40	3.15	48.12
	AT-ϵ_1	70.02	44.73	54.88	59.36	7.64	11.88	25.52
	TRADES-ϵ_1	67.84	42.73	53.14	58.20	7.79	11.86	27.23
	MART-ϵ_1	67.10	43.46	53.21	57.83	8.90	13.39	28.03
SVHN with ResNet-20	Natural	94.18	74.30	82.21	91.71	10.35	14.96	89.18
	AT-ϵ_1	91.90	71.80	81.47	84.18	21.51	29.94	44.51
	TRADES-ϵ_1	92.78	74.27	83.30	85.00	23.96	31.62	43.37
	MART-ϵ_1	92.71	74.82	82.94	85.67	24.11	33.01	44.27

Attacks on the Poisson encoding BNTT model: In our TinyImageNet experiments, for FGSM and PGD^{20} on the BNTT model (Kim & Panda, 2021b), we used the SNN-crafted BPTT-based adversarial input generation methodology by Sharmin et al. (2020). These attacks approximate the non-differentiable Poisson input encoding layer by using the gradients obtained for the first convolution layer activations during the attack, and was found to be a powerful substitute. We also used two expectation-over-transformation (EOT) iterations (Athalye et al., 2018b) while crafting adversarial examples on this model, due to the involved randomness in input encoding (Athalye et al., 2018a). Overall, we use the same surrogate gradient ensemble approach, however with an obligatory approximation of the input encoding and EOT iterations for stable gradient estimates.

B Additional Experiments

B.1 Black-box Transfer Attacks

In Table B1 we present our transfer-based black-box robustness evaluations (Papernot et al., 2017), using both the baseline ANN, and a similar SNN model obtained with the same conversion procedure using a different random seed. We craft adversarial examples on the source models with PGD^{20} also in an ensemble setting. In all models, we observe that white-box robust accuracies are significantly lower than black-box cases. This result holds both for the ϵ_1 perturbation budget where the models were trained and finetuned on, as well as ϵ_3 where we investigate robust generalization to higher perturbation bounds. Only in CIFAR-10, we observed that adversarially trained baseline ANNs used for conversion were able to craft stronger adversarial examples than the SNNs converted and finetuned in an identical setting (e.g., ϵ_3-robustness for AT-ϵ_1: BB_{ANN}: 29.81%, BB_{SNN}: 42.27%). We believe that this is related to our weaker choice of $\beta = 2$ for finetuning in CIFAR-10 experiments, whereas we used $\beta = 4$ in all other models. On another note, we observed that BB_{SNN} attacks are highly powerful on converted SNNs based on natural baseline ANN training (e.g., CIFAR-10 ϵ_3-robustness WB: 0.74%, BB_{SNN}: 6.87%), demonstrating their weakness even in the black-box setting.

Table B2: Evaluating $\epsilon_3 = 8/255$ FGSM attack robust accuracies from our CIFAR-10 experiments with VGG11, under individual components of the white-box ensemble. Triangular (piecewise linear), exponential and rectangular surrogate gradients were used as part of BPTT. Underlined values indicate the strongest individual attack within the ensemble.

		SNN-RAT	**ANN-to-SNN Conversion (Ours)**			
			Natural	**AT-ϵ_1**	**TRADES-ϵ_1**	**MART-ϵ_1**
	Clean Accuracy	90.74	93.53	92.14	91.39	91.47
	Ensemble FGSM	**32.80**	**15.71**	**33.94**	**41.42**	**44.39**
Triangular	$\gamma_w = 1.0$	45.01	28.16	53.61	71.50	62.16
	$\gamma_w = 2.0$	39.27	63.06	74.36	82.94	79.27
	$\gamma_w = 3.0$	43.23	77.79	83.59	87.72	86.30
	$\gamma_w = 0.5$	82.20	<u>19.62</u>	<u>39.25</u>	52.09	51.56
	$\gamma_w = 0.25$	90.15	54.15	57.48	51.03	<u>50.16</u>
Exponential	$(\gamma_d, \gamma_s) = (0.3, 0.5)$	48.94	80.75	83.89	87.68	86.70
	$(\gamma_d, \gamma_s) = (0.3, 1.0)$	<u>36.91</u>	54.96	69.65	79.66	74.97
	$(\gamma_d, \gamma_s) = (0.3, 2.0)$	37.65	27.15	51.66	67.60	60.02
	$(\gamma_d, \gamma_s) = (1.0, 0.5)$	62.73	89.41	89.01	90.36	89.41
	$(\gamma_d, \gamma_s) = (1.0, 1.0)$	41.63	64.45	75.37	83.30	79.34
	$(\gamma_d, \gamma_s) = (1.0, 2.0)$	38.65	32.07	55.96	70.99	62.55
Rectangular	$\gamma_w = 0.25$	90.01	88.14	85.22	71.08	66.57
	$\gamma_w = 0.5$	89.15	26.58	42.51	51.18	53.44
	$\gamma_w = 1.0$	65.28	25.10	49.85	68.98	61.68
	$\gamma_w = 2.0$	45.21	63.45	73.59	83.49	80.22
	$\gamma_w = 4.0$	52.62	88.84	89.42	90.93	89.43
Backward Pass Through Rate		51.46	23.90	41.33	<u>46.68</u>	58.26
Conversion-based Approx.		84.25	39.73	55.35	89.43	87.79
Straight-Through Estimation		90.14	92.84	90.74	90.68	91.03

On the Analysis of Gradient Obfuscation: Previous SNN robustness studies (Kundu et al., 2021; Ding et al., 2022) analyzes gradient obfuscation (Athalye et al., 2018a) solely based on the five principles: (1) iterative attacks should perform better than single-step attacks, (2) white-box attacks should perform better than transfer-based attacks, (3) increasing attack perturbation bound should result in lower robust accuracies, (4) unbounded attacks can nearly reach 100% success[3], (5) adversarial examples can not be found through random sampling[4]. In the main paper and our results presented here, we could confirm all of these observations in our evaluations. However, we argue that more reliable SNN assessments should ideally go beyond these, as we clarify in further depth via our ensemble evaluations (Carlini et al., 2019).

B.2 Evaluations with Alternative Surrogate Gradient Functions

Our detailed results for one particular ensemble attack is demonstrated in Table B2, where we focus on single-step FGSM without an initial randomized start. The third row indicates a naive BPTT-based FGSM attack where the adversary uses the same surrogate gradient function utilized during model training (e.g., SNN-RAT: 45.01%, Ours (AT-ϵ_1): 53.61%). Importantly, we observe that there are stronger attacks that can be crafted by a versatile adversary, by varying the shape or parameters of the used surrogate gradient. Moreover, in this particular case with FGSM attacks, we observe 4-6% difference in attack performance between the strongest individual attack configuration within the ensemble (e.g., underlined SNN-RAT: 36.91%, Ours (AT-ϵ_1): 39.25%), versus using an ensemble of alternative possibilities (e.g., SNN-RAT: 32.80%,

[3]After a perturbation bound of 16/255, ensemble attacks on all models reached $< 1\%$ robust accuracy.
[4]Gaussian noise with ϵ_3 standard deviation only led to a 0.4-3.0% decrease from the clean acc. of the models.

Ours (AT-ϵ_1): 33.94%). This further emphasizes the relative strength of our evaluations, in comparison to traditional naive evaluation settings.

Table B3: Impact of ensemble SNN attacks on CIFAR-10/100, with comparisons to ANNs under the analogous ϵ_3-attack. $\text{PGD}^{20}_{\text{vanilla}}$ uses BPTT with training-time surrogate gradient.

CIFAR-10 with VGG11	ANN		SNN		
	Clean	PGD^{20}	Clean	$\text{PGD}^{20}_{\text{vanilla}}$	$\text{PGD}^{20}_{\text{ensemble}}$
AT-ϵ_1	93.55	21.15	92.14	37.42	13.18
TRADES-ϵ_1	92.10	32.94	91.39	62.03	19.65
MART-ϵ_1	92.68	27.54	91.47	49.90	17.79
CIFAR-100 with WRN-16-4	ANN		SNN		
	Clean	PGD^{20}	Clean	$\text{PGD}^{20}_{\text{vanilla}}$	$\text{PGD}^{20}_{\text{ensemble}}$
AT-ϵ_1	74.90	9.46	70.02	12.56	7.64
TRADES-ϵ_1	73.87	10.74	67.84	12.97	7.79
MART-ϵ_1	72.61	14.72	67.10	14.27	8.90

Table B3 shows a comparison of ANNs and SNNs under *analogous* PGD^{20} attack settings. Here, SNN evaluations under $\text{PGD}^{20}_{\text{vanilla}}$ indicate naive BPTT-based attacks, where the adversary only uses the same surrogate gradient utilized during training. Simply running these evaluations would generally be considered analogous to those for the PGD^{20} ANN attacks (Ding et al., 2022), although they are essentially not identical. Considering $\text{PGD}^{20}_{\text{vanilla}}$ accuracies, results might even be (wrongly) perceived as SNNs being more robust than ANNs, as claimed in previous work based on shallow models and naive evaluation settings (Kim & Panda, 2021c; Li et al., 2023). However, since the SNN attack depends on the surrogate gradient, we also consider the ensemble PGD^{20}, as we did throughout our work. Note that this stronger attack is not necessarily equivalent to the ANN attack either, but we believe it is a better basis for comparison.

B.3 Ablations on the Robust SNN Finetuning Objective

Our ablation studies are presented in Table B4. The first three rows respectively denote comparisons to end-to-end trained SNNs using a natural cross-entropy loss, and using our robust finetuning objective without and with trainable thresholds, for 200 epochs. Note that in the third row, we are essentially comparing our ANN-to-SNN conversion approach, to simply end-to-end adversarially training the SNN using the TRADES objective. Our method yields approximately twice as more robust models than the model in the third row (i.e., ensemble APGD_{CE}: 4.72 versus 10.05), indicating that the weight initialization from an adversarially trained ANN brings significant gains. The fourth model indicates weight initialization from a naturally trained ANN within our conversion approach (previously included in Table 1 as well), which yields nearly no robustness since these weights are inclined to a non-robust configuration during natural ANN training.

Remaining models compare different choices for $\mathcal{L}_{\text{RFGSM}}$ (e.g., adversarial cross-entropy loss (Tramèr et al., 2018)), and the outer optimization scheme (e.g., standard AT (Madry et al., 2018)), which we have eventually chosen to follow a similar one to TRADES (Zhang et al., 2019a). We also observed significant robustness benefits of using trainable V^l_{th} during post-conversion finetuning as proposed in Rathi & Roy (2021) (e.g., clean/PGD^{20}: 91.09/9.39 vs. 92.14/10.05). Overall, these results show that our design choices were important to achieve better robustness. Nevertheless, several alternatives in Table B4 (e.g., standard AT based outer optimization or $\mathcal{L}_{\text{CE}}(f_{\boldsymbol{\theta}}(\mathbf{x}'), y)$ based RFGSM) still remained effective to outperform existing defenses.

Robust ANN Conversion Without Finetuning: In another ablation study, we evaluate our method without the robust finetuning phase altogether. It is important to note that in hybrid conversion, finetuning is a critical component to shorten the simulation length such that one can achieve low-latency. Since we also reset the moving average batch statistics of tdBN layers during conversion, these parameters can only be estimated reliably during the robust finetuning phase. Thus, right after conversion and setting the thresholds, our SNNs only achieve chance-level accuracies with direct input coding for a simulation length of $T = 8$.

However, we evaluated our models (CIFAR-10 with VGG-11) that were only finetuned for a single epoch, or only two epochs to exemplify. After one epoch of robust finetuning the SNN could only achieve a clean/PGD^{20} robust acc. of 87.25%/11.42%, and with only two epochs of robust finetuning it achieves 89.15%/12.97%, whereas our model obtains 92.14%/13.18% in the same setting after 60 epochs of finetuning. These results reveal the benefit of a reasonable robust finetuning stage, both in terms of obtaining more reliable tdBN batch statistics following conversion, as well as adversarial finetuning of layer-wise firing thresholds.

Table B4: Ablations for the robust SNN finetuning objective with our CIFAR-10 experiments. Robust accuracies are evaluated via ensemble white-box attacks. Bottom row indicates our method.

Baseline ANN	Inner Max. $\mathcal{L}_{\text{RFGSM}}$	Outer Optimization	Trainable V_{th}^{l}	Clean Acc.	ϵ_3-Robust Accuracies		
					FGSM	PGD^{20}	APGD_{CE}
✗	–	$\mathcal{L}_{\text{CE}}(f_{\boldsymbol{\theta}}(\mathbf{x}), y)$	✗	93.73	6.43	0.00	0.00
✗	$D_{\text{KL}}(f_{\boldsymbol{\theta}}(\mathbf{x}')\|\|f_{\boldsymbol{\theta}}(\mathbf{x}))$	Eq. (11)	✗	91.90	24.94	7.23	5.32
✗	$D_{\text{KL}}(f_{\boldsymbol{\theta}}(\mathbf{x}')\|\|f_{\boldsymbol{\theta}}(\mathbf{x}))$	Eq. (11)	✓	91.75	23.83	6.70	4.72
Natural	$D_{\text{KL}}(f_{\boldsymbol{\theta}}(\mathbf{x}')\|\|f_{\boldsymbol{\theta}}(\mathbf{x}))$	Eq. (11)	✓	93.53	15.71	0.74	0.44
AT-ϵ_1	–	$\mathcal{L}_{\text{CE}}(f_{\boldsymbol{\theta}}(\mathbf{x}), y)$	✓	92.18	32.31	10.03	8.40
AT-ϵ_1	$\mathcal{L}_{\text{CE}}(f_{\boldsymbol{\theta}}(\mathbf{x}'), y)$	$\mathcal{L}_{\text{CE}}(f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}}), y)$	✓	92.02	34.17	12.19	9.40
AT-ϵ_1	$D_{\text{KL}}(f_{\boldsymbol{\theta}}(\mathbf{x}')\|\|f_{\boldsymbol{\theta}}(\mathbf{x}))$	$\mathcal{L}_{\text{CE}}(f_{\boldsymbol{\theta}}(\tilde{\mathbf{x}}), y)$	✓	91.59	32.83	11.78	9.26
AT-ϵ_1	$\mathcal{L}_{\text{CE}}(f_{\boldsymbol{\theta}}(\mathbf{x}'), y)$	Eq. (11)	✓	92.13	33.15	11.96	9.32
AT-ϵ_1	$D_{\text{KL}}(f_{\boldsymbol{\theta}}(\mathbf{x}')\|\|f_{\boldsymbol{\theta}}(\mathbf{x}))$	Eq. (11)	✗	91.09	34.03	11.51	9.39
AT-ϵ_1 (Ours)	$D_{\text{KL}}(f_{\boldsymbol{\theta}}(\mathbf{x}')\|\|f_{\boldsymbol{\theta}}(\mathbf{x}))$	Eq. (11)	✓	**92.14**	**33.94**	**13.18**	**10.05**

Table B5: Evaluations of vanilla and adversarially robust SNNs on out-of-distribution generalization to common image corruptions and perturbations using the CIFAR-10-C test set (Hendrycks & Dietterich, 2019). Values indicate averaged accuracies across the complete test set for all five severities.

	Clean Acc.	C10-C (all)	C10-C (w/o noise)	Noise			Blur				Weather				Digital			
				Gauss	Shot	Impulse	Defocus	Glass	Motion	Zoom	Snow	Frost	Fog	Bright	Contrast	Elastic	Pixel	JPEG
Vanilla SNN	93.73	81.22	83.04	72.3	79.0	70.5	85.1	73.3	80.0	83.4	85.3	85.8	80.9	91.8	67.5	86.6	88.4	88.4
SNN-RAT	90.74	81.72	81.60	83.4	85.9	77.3	85.2	83.3	80.8	83.8	83.5	83.2	72.3	87.7	56.1	85.3	89.2	88.7
Ours (AT-ϵ_1)	92.14	83.85	83.66	86.3	88.0	79.5	86.2	82.0	81.9	84.9	85.8	87.3	74.9	90.7	65.3	85.3	90.0	89.6

Table B6: Evaluations of vanilla and adversarially robust SNNs on out-of-distribution generalization to common image corruptions and perturbations using the CIFAR-100-C test set (Hendrycks & Dietterich, 2019). Values indicate averaged accuracies across the complete test set for all five severities.

	Clean Acc.	C100-C (all)	C100-C (w/o noise)	Noise			Blur				Weather				Digital			
				Gauss	Shot	Impulse	Defocus	Glass	Motion	Zoom	Snow	Frost	Fog	Bright	Contrast	Elastic	Pixel	JPEG
Vanilla SNN	74.10	46.14	50.60	20.7	29.0	35.2	56.8	19.9	50.9	51.9	51.5	46.0	59.2	69.1	48.2	57.2	46.63	49.9
SNN-RAT	69.32	51.95	54.26	39.4	45.4	43.5	58.5	40.6	52.8	56.2	57.0	54.6	47.9	64.6	35.3	59.0	61.8	62.9
Ours (AT-ϵ_1)	70.02	54.06	55.54	42.5	49.3	52.5	59.6	41.2	53.6	57.5	58.6	57.5	49.2	66.0	38.4	58.9	62.0	64.1

B.4 Out-of-Distribution Generalization to Common Image Corruptions

It has been argued that adversarial training can have the potential to improve out-of-distribution generalization (Kireev et al., 2022). Tables B5 and B6 presents our evaluations on CIFAR-10-C and CIFAR-100-C respectively (Hendrycks & Dietterich, 2019). Results show that averaged accuracies across all corruptions (noise, blur, weather and digital) improved with our AT-ϵ_1 model (i.e., CIFAR-10-C: 83.85% and CIFAR-100-C: 54.06%), in comparison to SNN-RAT and vanilla SNNs. Importantly, this improvement persists across all individual corruptions, and CIFAR-10/100-C performance without the noise corruptions maintains a similar behavior (see w/o noise averages in Tables B5 and B6). Notably for CIFAR-10-C we observe that SNN-RAT provides noise robustness, but mostly not improving performance in other corruptions (i.e., CIFAR-10-C (all): 81.72%, CIFAR-10-C (w/o noise): 81.60%).

Overall, our conversion-based approach achieved to significantly improve SNNs in terms of their adversarial robustness and generalization. Nevertheless, there are also various other security aspects that were not in the scope of our current work (e.g., preserving privacy in conversion-based SNNs (Kim et al., 2022b)), which requires attention in future studies towards developing trustworthy SNN-based AI applications.