Stage Detection of Mild Cognitive Impairment: Region-dependent Graph Representation Learning on Brain Morphable Meshes

Abstract

Mild cognitive impairment (MCI), as a transitional state between normal cognition and Alzheimer's disease (AD), is crucial for taking preventive interventions in order to slow down AD progression. Given the high relevance of brain atrophy and the neurodegeneration process of AD, we propose a novel mesh-based pooling module, RegionPool, to investigate the morphological changes in brain shape regionally. We then present a geometric deep learning framework with the RegionPool and graph attention convolutions, to perform binary classification on MCI subtypes (EMCI/LMCI). Our model does not require feature engineering and relies only on the relevant geometric information of T1-weighted magnetic resonance imaging (MRI) signals. Our evaluation reveals the state-of-the-art classification capabilities of our network and shows that current empirically derived MCI subtypes cannot identify heterogeneous patterns of cortical atrophy at the MCI stage. The class activation maps (CAMs) generated from the correct predictions provide additional visual evidence for our model's decisions and are consistent with the atrophy patterns reported by the relevant literature.

Keywords: deep learning on meshes, graph neural networks, shape analysis, neuroanatomy

1. Introduction

Alzheimer's disease (AD) is the most common cause of dementia, characterized by an irreversible decline in cognition and loss of behavior skills. To date, there is no effective clinical treatment for AD, which is the advanced stage of the entire disease spectrum. However, the pathological cascade of AD can be slowed down with preventive intervention during the long *preclinical* phase of AD (Sperling et al., 2011). Thus, early detection of AD is highly desirable in order to make more informed decisions for therapeutic intervention and treatment planning. Mild cognitive impairment (MCI) represents the transitional state between normal aging and early dementia and is recognized as an important sign of AD since one-third of MCI develop into AD within five years of follow-up. MCI subjects are subdivided in the dataset of Alzheimer's disease neuroimaging initiative (ADNI) into two subtypes—early MCI (EMCI) and late MCI (LMCI)—based on the WMS-R Logical Memory II Story A score. Compared with LMCI, subjects in the stage of EMCI demonstrate milder degrees of cognitive and functional impairment and slower disease progression (Aisen et al., 2010), which is considered to be the optimal stage for therapeutic interventions. Recently, there has been a surge of interest in identifying the subtle variations between MCI subtypes, but this is challenging because EMCI and LMCI are classified by a single memory score, leading

to low specificity or even misclassification. To address this issue, we seek a more objective method that would allow researchers to make a reliable classification of MCI subtypes.

Brain atrophy assessed on structural magnetic resonance imaging (MRI) has been identified as a valid marker of AD-related neurodegeneration (Whitwell et al., 2012). For example, hippocampus atrophy is long regarded as one of the best established and validated biomarkers of AD (Jack Jr et al., 2011), with its volume progressively decreasing 15-40% across the entire disease spectrum according to post-mortem studies (Bosscher and Scheltens, 2002). Likewise, the amygdala atrophy in AD is also prominent (Scott et al., 1991) and closely correlated to the symptom severity in AD and MCI (Poulin et al., 2011; Yi et al., 2016). Besides, Tondelli *et al.* (Tondelli et al., 2012) indicate that the morphological changes of the brain in shapes even begin ten years prior to the clinical symptoms of AD occurring, which further emphasizes the importance of brain shape analysis in the early detection of AD. In our study, we use 3D morphable triangular mesh manifolds with the same connectivity to approximate the morphology of both cortex and subcortical structures and employ graph neural networks (GNNs) to study their powerful shape-description ability. To that end, a popular choice is using mesh simplification (Ranjan et al., 2018; Yuan et al., 2020) as a readout function to aggregate vertex embeddings to represent the entire mesh. However, this kind of method suffers from two drawbacks: one is the computational complexity of the simplification process, which makes the in-network mesh simplification process always deterministic. Such a static scheme ignores the information encoded by those decimated vertices, limiting the generalization ability and robustness of the model. Another problem arises from the loss of localized information during the mesh simplification process since edges are contracted following a sequence of their global importance.

Given the high relevance of brain shape in the neurodegeneration process of AD, we propose a geometric deep learning framework built upon the graph attentional convolutions (Veličković et al., 2017) and REGIONPOOL defined in Sec. 2.3, to investigate the morphological changes in brain shape. Similar to the spatial pooling operation in CNNs, our approach REGIONPOOL defines hierarchical "patches" with varying topologies and sizes on the mesh surface and generates region-level representations by global average-pooling the embeddings of a set of sampled geometrical-important vertices within each region. As we will show later, our proposed model can not only achieve superior performance in EMCI/LMCI classification but can also identify the subtle morphological changes in brain shape and provide high-resolution 3D visual interpretations of *classifier reasoning*, which is a highly desired property of deep learning model in medical image analysis.

2. Methods

2.1. Graph Construction

All data used in our study are transformed into triangular mesh manifolds and registered to a standard template (same number of vertices/edges per sample) following the procedures in Appendix B. A single mesh instance will contain 47,616 vertices, including 32,768 (69%) from the cortical structure and 14,848 (31%) from the subcortical structure. The feature vector of the cortical vertices has six dimensions corresponding to the Cartesian coordinates of both white matter and gray matter vertices in their subjects' native space. Since all corresponding edges of white and gray matter share the same edge weight $\mathbf{e}_{i,j}$,

they can be considered to form the same "faces" with different coordinates (Azcona et al., 2020). Similarly, subcortical vertices are assigned three features, which is also the Cartesian coordinate of the subcortical vertices in their subjects' native space. As shown in Fig. 1, according to the anatomy structure, the mesh vertices are categorized into four types, $\mathcal{A} = [A_{lc}, A_{rc}, A_{ls}, A_{rs}]$, associated by two relations in $\mathcal{R} = [R_c, R_s]$.

Figure 1: Graphical illustration of our constructed heterogeneous mesh, which contains four types of vertices: Rh-Cortex (A_{rc}), Lh-Cortex (A_{lc}), Rh-Subcortical (A_{rs}), Lh-Subcortical (A_{ls}) and two types of relations: Cortex connection (R_c) and Subcortical connection (R_s).

2.2. Graph Attention Convolution

Based on the message passing scheme defined in Sec. A, we introduce a shared attention mechanism $\mathbf{a}$ on every pair of vertices (v_i, v_j) to compute the attention weight $\alpha_{i,j}$, which indicates the relative/normalized importance of j's features to i. Following the convention of (Veličković et al., 2017), the graph attentional convolution (GATconv) can be typically defined as: $\mathbf{h}_i^{(k)} = \alpha_{i,i} \Theta \mathbf{h}_i^{(k-1)} + \sum_{j \in \mathcal{N}_i} \alpha_{i,j} \Theta \mathbf{h}_j^{(k-1)}$. Here, consider the multi-dimensional edge features $\mathbf{e}_{i,j}$ of graphs, the attention weight $\alpha_{i,j}$ are specially computed as:

$$\alpha_{i,j} = \frac{\exp\left(\text{LeakyReLU}\left(\mathbf{a}^\top \left[\Theta^{(k)} \mathbf{h}_i^{(k-1)} \middle\| \Theta^{(k)} \mathbf{h}_j^{(k-1)} \middle\| \Theta_e^{(k)} \mathbf{e}_{i,j}^{(k-1)}\right]\right)\right)}{\sum_{k \in \mathcal{N}_i \cup \{i\}} \exp\left(\text{LeakyReLU}\left(\mathbf{a}^\top \left[\Theta^{(k)} \mathbf{h}_i^{(k-1)} \middle\| \Theta^{(k)} \mathbf{h}_k^{(k-1)} \middle\| \Theta_e^{(k)} \mathbf{e}_{i,k}^{(k-1)}\right]\right)\right)} \quad (1)$$

where $\mathbf{a}$ is a single-layer feedforward neural network. The weight matrices $\Theta_e \in \mathbb{R}^{d^{(k)} \times d^{(k-1)}}$ and $\Theta \in \mathbb{R}^{c^{(k)} \times c^{(k-1)}}$ denote the corresponding linear transformations that map the input features of edges and vertices to a higher-level space.

2.3. Region-dependent Pooling on Mesh Surface

2.3.1. VERTICES SELECTION VIA SHAPE-PRESERVING MESH SIMPLIFICATION

Our mesh simplification process is based on the work of (Garland and Heckbert, 1997), which simplifies the mesh by repeatedly contracting the edge with the least *collapse cost*. To that end, as an initial step, the original work associates each vertex $v_i = [x_i\ y_i\ z_i\ 1]^\top$ with a set of planes $\mathcal{P}$ by defining an error s.t. $\Delta(v) = v^\top Q v$, where Q is the sum of the corresponding fundamental error quadrics of the planes in $\mathcal{P}$, which is defined in Sec. A. For a given edge contraction $(v_1, v_2) \to \bar{v}$, they use $\bar{Q} = Q_i + Q_j$ as a new error quadric

Figure 2: The process of mesh simplification and building the mesh hierarchies. (a) provides the overall pooling pipeline. (b)-(d) illustrate the process of edge contraction via vertex decimation. (d)-(e) illustrate the process of defining hierarchical regions on the original mesh surface based on the simplification process.

to approximate the error at the target contraction position $\bar{v}$. Note that in our study, we choose a simple scheme to decide the position of $\bar{v}$, i.e., to select either v_1 or v_2 depending on which one of them produces a smaller *decimation error* $\Delta(\bar{v})$. To better illustrate, given the condition $\Delta(v_1) < \Delta(v_2)$, we will have: $\omega_2 = \Delta(v_1) = \min(\Delta(v_1), \Delta(v_2))$. Here, we use ω_2 to denotes the corresponding collapse cost of contracting the edge (v_1, v_2) to v_1 by decimating v_2. A graphical example of this process can be found in Fig. 2b to 2c, while Fig. 2d provides an example of the simplified mesh surface, with the grey arrows indicating the trajectories of edge contraction.

2.3.2. COST-ORIENTED SAMPLING

Our REGIONPOOL further exploits this simplification process by adopting a cost-oriented sampling strategy. The key intuition here is that we want our model to learn the mesh representation not only from the vertices of the simplified mesh, $\mathcal{V}_s$, but also from those decimated vertices, $\mathcal{V}_d$.

For this purpose, we first define hierarchical "patches" with varying *topologies* and *sizes* on the mesh surface (Fig. 2d to 2e). As mentioned in the previous section, at each step of the mesh simplification, we contract a valid edge (v_i, v_j) by selecting the target position $\bar{v}$ from either v_i or v_j depending on their corresponding decimation error Δ. Thus, by simplifying meshes in such a one-to-one manner, the vertices of the simplified mesh, $\mathcal{V}^s = \{v_1^s, v_2^s, ..., v_n^s\} \in \mathbb{R}^n$, and decimated vertices, $\mathcal{V}^d = \mathcal{V} \setminus \mathcal{V}^s$, will eventually form n independent *pooling regions*, denoted as $R = \{r_1, r_2..., r_n\} \in \mathbb{R}^n$. As shown in Fig. 2a, any region r_i consists of one vertex from the simplified mesh, $v_i^s \in \mathcal{V}^s$, and a set of decimated vertices, $\mathcal{V}_i^d \subset \mathcal{V}^d$, that were iteratively contracted to v_i^s during the mesh simplification process.

Next, we propose a cost-oriented sampling strategy for all $r_i \in R$, providing a self-adaptive approach to extract the most representative features from different mesh hierar-

chies, i.e., for a given region r_i, we defined the corresponding sampling strategy $S_i(\cdot)$ to be a random sample (without replacement) of m decimated vertices from a specific categorical distribution, $Cat(\pi_1, \pi_1, ..., \pi_k)$. Here, the class probability π_k indicates the probability of v_k^d being sampled, which is defined as: $\pi_k = \frac{\omega_k}{\sum_{k=1}^{|\mathcal{V}_i^d|} \omega_k}$, $\forall k \in \{1, 2, ..., |\mathcal{V}_i^d|\}$ where ω_k is the corresponding collapse cost of the decimated vertex v_k^d, defined in equations 2.3.1, considering the geometric significance of ω_k (i.e., the geometric error caused by contracting a certain vertex to a new position), we normalize it and interpret it as the relative importance of v_k^d. Note that if the number of samples exceeds the number of decimated vertices in that region, i.e., $m > |\mathcal{V}_i^d|$, we will directly take all decimated vertices to be the sampling result, i.e., $S_i(\mathcal{V}_i^d) = \mathcal{V}_i^d$. This process addresses the different geometrical importance of decimated vertices, enabling our model to learn a descriptive mesh representation.

Following that, we compute the region-level embedding, $\mathbf{y}_i^r \in \mathbb{R}^{c^{(K)}}$, by element-wise pooling the embeddings of both sampled vertices v_i^s and $S_i(\mathcal{V}_i^d) \subset \mathcal{V}_i^d$. Finally, those region-level embeddings are concatenated as the representation of the entire mesh s.t.

$$\mathbf{y}^g = \sigma \left(\mathop{\Big\|}_{i=1}^{n} \text{POOL} \left(\mathbf{h}_{v_i^s}^{(K)}, \left\{ \mathbf{h}_{v_i^d}^{(K)}, \ \forall v_i^d \in S_i(\mathcal{V}_i^d) \right\} \right) \right) \tag{2}$$

where σ is any possible non-linear activation function (e.g., ReLU, ELU), and POOL can be any regular pooling method (e.g., global max/mean/sum/attention-pooling). By default, we choice global mean-pooling to support the grad-cam (Selvaraju et al., 2017) visualization in Sec. 3.4 and take ELU as the activation function.

2.4. Heterogeneous Brain Mesh Attention Network (Het-BMAT)

As illustrated in Fig. 3, our proposed network, Het-BMAT, is built upon the GATconv in Sec. 2.2, REGIONPOOL in Sec. 2.3, and a combination of hetero and normal linear layers. As an initial step, a standard GATconv is used as the "pre-conv" block to map the input

Figure 3: Our network architecture. Given a 3D mesh input, G_i, the Het-BMAT network will predict its corresponding label, y_i, using the learned representation, y^g, of the entire mesh.

features to a high dimensional space to obtain sufficient expressive power. Then, given the

different sizes of substructures of the brain meshes, we propose a simple mesh attention (MAT) block, to provide various receptive fields, addressing the "over smoothing" problem by introducing skip connection (Veit et al., 2016) to every stacked GATconv layer. In the following experiment, all GATconvs will share the same channel size of 16. Besides, to get fully used of the*inherent coarse-grained hierarchies* of the brain meshes, we adopt two hetero linear layers to further aggregate the output of REGIONPOOL (i.e., a concatenation of region-level embedding) to a higher-level embedding space—the embeddings of the *left and right hemispheres*. Finally, an ELU (exponential linear unit (Clevert et al., 2015)) activation function is introduced after every convolution and linear layer to add nonlinearity to the network training. We use a softmax function to compute the corresponding predicted possibility and employ a standard binary cross entropy (BCE) loss function to do the model training.

3. Experiment

3.1. Dataset and experiment Setting

In this paper, we use 4,072 T1-weighted MRI volumes from the Alzheimer's Disease Neuroimaging Initiative (ADNI) dataset, corresponding to 492 individual subjects. Basic demographic information includes the number of samples with different labels, as well as the age and gender distribution of the subjects are shown in Table 4. Our network was trained with 16 samples per batch over 200 epochs and adopted an Adam (Kingma and Ba, 2014) optimizer with a learning rate of 1×10^{-3} and a decay rate of 0.95 per 5 epochs to minimize a BCE loss function. Besides, the weights of our network were initialized using Xavier uniform initializer (Glorot and Bengio, 2010) and L_2-regularized (weight decay) with a weight decay of 1×10^{-3} to avoid over-fitting.

3.2. MCI subtypes classification

In our first experiment, we perform 5-fold cross-validation to analyze the effectiveness of incorporating different brain structures, i.e., the cortex/subcortical/both structures, for MCI subtypes classification and report the averaged result. Note that to avoid samples from the same subjects appearing in both training and testing sets, the data samples are shuffled with respect to their subject identifiers. Following the convention defined in Sec. 2.3, we respectively divide the subcortical and cortex structure into $n = 128$ pooling regions, and for every single region r_i, we will sample $|\mathcal{V}_i^d| = 40$ decimated vertices to do the REGIONPOOL. Table 1 summarizes the results of our ablation study with different brain structural inputs. Our Het-BMAT network performs best by incorporating the subcortical structures as input. Although ordered atrophy patterns in MCI patients have been proven to be associated with their profiles of increasing cognitive dysfunction, the classifier's performance does not improve with the inclusion of cortex structures. It becomes even worse when only cortex structures are used as input, suggesting that the morphological changes occurring in the subcortical structures are more critical for the EMCI/LMCI classification. Moreover, it also indicates that current empirically derived MCI subtypes (based on the subject's neuropsychological profile) may not be able to capture the heterogeneity of cortical atrophy at the MCI stage (Edmonds et al., 2016).

Table 1: 5-fold cross-validation of EMCI vs. LMCI classification using different brain structures

Structure	Threshold=0.5			AUC	
	Precision	Recall	F1	ROC-AUC	PR-AUC
all structures	$\mathbf{0.822 \pm 0.026}$	0.810 ± 0.047	0.812 ± 0.044	0.877 ± 0.040	0.859 ± 0.053
subcortical structures	0.822 ± 0.044	$\mathbf{0.824 \pm 0.040}$	$\mathbf{0.821 \pm 0.044}$	$\mathbf{0.888 \pm 0.036}$	$\mathbf{0.865 \pm 0.061}$
cortical structures	0.667 ± 0.043	0.651 ± 0.044	0.661 ± 0.054	0.689 ± 0.053	0.650 ± 0.095

[1] Precision, Recall, and F1-score in this paper are macro averaged

[2] *ROC/PR-AUC* Area Under the Receiver Operating Characteristic/Precision-Recall Curve

Table 2: Baseline comparison of several graph-based pooling modules and prior studies on EMCI vs. LMCI classification

(*a*) REGIONPOOL vs. Graph pooling approaches

Module	Threshold=0.5			AUC	
	Precision	Recall	F1	ROC-AUC	PR-AUC
RegionPool	**0.861**	**0.860**	**0.860**	**0.922**	**0.897**
MESHSIM	0.841	0.837	0.834	0.904	0.868
GAP	0.790	0.785	0.785	0.845	0.817
SET2SET	0.762	0.757	0.758	0.822	0.800
SORTPOOL	0.721	0.721	0.720	0.790	0.808

[1] MESHSIM adopts the mesh simplification process in Sec. 2.3.1 to extract hierarchical features from the mesh surface. SORTPOOL sorts the node embedding in ascending order and selects the features of top-k nodes. SET2SET adopts iterative content-based attention to generate an order invariant representation.

(*b*) Het-BMAT vs. Related studies

Study	Target (EMCI/LMCI)	Method	Classifier	Acc
Ours (2022)	**259/233**	Learn shape descriptors of neuroanatomical structures	GNN	0.822
Goryawala et al. (2015)	114/91	Use both cortical volume & neuropsychological scores	LDA	0.736
Jie et al. (2018)	56/43	Combine temporal & spatial properties of DCNs	SVM	0.787
Nozadi et al. (2018)	164/189	Extract regional features from FDG/AV45-PET	RF	0.725
Shi et al. (2020)	77/64	Extract features from rs-fMRI signals using HHT	SVM	**0.879**

[1] *LDA* linear discriminant analysis. *DCNs* dynamic connectivity networks. *SVM* support vector machine. *RF* random forest. *HHT* Hilbert-Huang transform.

3.3. Baseline comparison

Based on the fundamental architecture of the Het-BMAT network, we evaluate our proposed REGIONPOOL against four baseline pooling modules on the same classification task in Sec. 3.2: including three commonly used global pooling approaches for graph classification (GAP, SET2SET (VINYALS ET AL., 2015), SORTPOOL (ZHANG ET AL., 2018)), and a hierarchical pooling approach (MESHSIM (Ranjan et al., 2018)). For all global pooling approaches, we applied it to each subcortical structure and used their concatenation for classification, otherwise, the model will perform poorly due to "information loss". All experiments will be conducted on the base implementation, the same training fold with the highest accuracy in the previous 5-folds cross-validation and use only subcortical structures as input. Each experiment was repeated five times, and the average results were reported. Table 2(*a*) demonstrates that our REGIONPOOL outperforms all the baseline pooling modules in precision, recall, F1 score, and both Area Under the Curve (AUC) statistics.

Apart from that, we also compare our Het-BMAT network against a number of prior studies (Goryawala et al., 2015; Jie et al., 2018; Nozadi et al., 2018; Shi and Liu, 2020) on the same classification task. We only select studies with a subject number close to 100. As shown in Table 2(*b*), our proposed model not only achieves superior results among all baseline methods but also possesses the following merits. *Simple process:* Our approach does not require any feature engineering. *More reliable:* Our model is trained on a larger dataset. *More objective:* The classification is completely based on the geometric information of brain neuroanatomical structures from the MRI signals.

Figure 4: Grad-Cam visualization for all correct predictions by the Het-BMAT network. (a) and (b) are, respectively the lateral and medial views of the CAM projected on the mesh template.

3.4. Gradient-weighted class activation mapping (Grad-cam) visualization

Following the convention defined in (Selvaraju et al., 2017), we employ a Het-BMAT model pre-trained on subcortical structures to generate class activate maps (CAMs) for each correctly classified sample (TP & TN predictions) in the test set. Those CAMs are then averaged and projected onto the subcortical template surface, which is shown in Fig. 4, where we can observe a significant involvement of the amygdala, left putamen and left thalamus shape in the EMCI/LMCI classification, which matches the findings in (de Jong et al., 2008; Yi et al., 2016). Besides, we also observe a remarkable asymmetry in CAMs, i.e., compared with the RH, the morphological change in LH is more pronounced and indicative. Such left lateralization of brain atrophy in AD progression has been reported by (Long et al., 2013; Thompson et al., 2007) and is thought to be related to the linguistic nature of neuropsychological tests in AD diagnosis (Keilp et al., 1996).

4. Conclusion

Our study investigates the corresponding cortical and subcortical atrophy patterns in MCI subtypes (EMCI/LMCI) by learning representations of the brain meshes regionally. The ablation study reveals the limitation of using a single neuropsychological score to capture the heterogeneous patterns of cortical atrophy at the MCI stage in the diagnosis of AD, suggesting the need to incorporate diverse profiles into current cognition-based diagnostic criteria for more meaningful staging of MCI subtypes. Notably, our Het-BMAT network together with REGIONPOOL demonstrates a superior MCI subtype classification capability using only the geometric information of subcortical structures and outperforms the state-of-the-art methods in the baseline comparison. In addition, the generated class activation maps (CAMs) provide qualitatively visual interpretations of classifier decisions and are consistent with the morphological changes reported in the related literature, providing solid evidence for the feasibility of employing geometrical deep learning in disease diagnosis.

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Appendix A. Supplementary Definition

In this section, we define some important terminologies related to the heterogeneous graphs used in our study. A detailed description of all mentioned notations in this paper is summarized in Table 3 for quick reference.

Table 3: Description of notations in this paper

Notations	Descriptions
$\mathbb{R}^N$	N-dimensional Euclidean space
p, q	The number of nodes and edges in a graph
c, d	The dimension of the node and edge feature vector
n	The number of vertices in the simplified mesh
$R \in \mathbb{R}^n$	A set of all pooling regions, defined in Sec. 2.3.1
r_i	A single pooling region, where $r_i \in R$
$\mathcal{N}_i$	The neighborhood nodes set of v_i
$\mathbf{x}_i \in \mathbb{R}^c$	The vertex feature vector of v_i
$\mathbf{X} \in \mathbb{R}^{p \times c}$	The vertex feature matrix
$\mathbf{e}_{i,j} \in \mathbb{R}^d$	The edge feature vector of (v_i, v_j)
$\mathbf{E} \in \mathbb{R}^{q \times d}$	The edge feature matrix
$\mathbf{h}_i^{(k)}$	Hidden state of node i at k-th GNN layer
$\mathbf{y}^g$	The embedding of the entire graph G
$\mathbf{y}_i^r$	The embedding of the pooling region r_i
$(v_i, v_j) \rightarrow \bar{v}$	Contracting edge (v_i, v_j) into $\bar{v}$ via vertex decimation
$\mathcal{V}^s \in \mathbb{R}^n$	A set of vertices in the simplified mesh
$\mathcal{V}^d \in \mathbb{R}^{p-n}$	A set of all decimated vertices, where $\mathcal{V} = \mathcal{V}^s \cup \mathcal{V}^d$
$\mathcal{V}_i^d \in \mathbb{R}^{m_i}$	A set of decimated vertices that being contracted to v_i^s
$\mathcal{A}, \mathcal{R}$	Vertex types and relations in the heterogeneous graphs
$\sigma(\cdot)$	Non-linearity activation function
Θ, γ, ψ	Function with learnable parameters
$S_i(\cdot)$	The cost-oriented sampling defined for pooling region r_i
m	The sample size of the cost-oriented sampling
$\parallel$	Vector concatenation

Definition 2.1. Triangular Mesh Manifolds. In graph signal processing (Wu et al., 2020), meshes can be treated as a special variation of the undirected graph and defined as

$\mathcal{M} = (\mathcal{V}, \mathcal{E}, \mathcal{F})$, where $\mathcal{V}$ is a finite set of $|\mathcal{V}| = p$ vertices, and $\mathcal{E}$, $\mathcal{F}$ are respectively a set of edges and faces. Each vertex in the mesh is assigned with a c-dimensional feature vector $\mathbf{x}_i \in \mathbb{R}^c$, and a vertex feature matrix $\mathbf{X} \in \mathbb{R}^{p \times c}$ is used to encapsulate all those feature vectors. Similarly, a d-dimensional feature vector $\mathbf{e}_{i,j} \in \mathbb{R}^d$ is also defined for the vertex connection (v_i, v_j) between v_i and v_j and will be stored in the edge feature matrix $\mathbf{E} \in \mathbb{R}^{q \times d}$.

Definition 2.2. Graph-level classification with GNN. For a set of labeled graphs, $\{(G_1, y_1), (G_2, y_2), ..., (G_i, y_i)\}$, where $y_i \in \mathcal{Y}$ is the corresponding label of $G_i \in \mathcal{G}$. The ultimate goal of graph-level classification is to learn the mapping f from $\mathcal{G}$ to $\mathcal{Y}$ (i.e., $f : \mathcal{G} \to \mathcal{Y}$). A major challenge of applying GNNs to graph-level classification is to derive a general representation of a given graph G from node embeddings of the K-th layer via a readout function.

$$\mathbf{y}^g = \text{Readout}\left(\left\{\mathbf{h}_v^{(K)}, \forall v \in G\right\}\right) \tag{3}$$

A Common choice of readout function is to perform global max/mean/sum pooling to all node embeddings, which works well on "small" graphs, but considering the information loss during the dimension compression, it cannot support graphs of "large" scale.

Definition 2.3. Message Passing Scheme (Gilmer et al., 2017). Message Passing Neural Network (MPNN) defines convolution directly on the graph and operates on a set of spatially closed neighborhood vertices. Generally, message passing consists of two steps, i.e., *message computation* and *aggregation*. Consider the message passing at vertex v_i, the message computation operation takes the embedding of the neighborhood vertices of v_i (including v_i) and the corresponding edge feature $\mathbf{e}_{i,j} \in \mathbf{R}^d$ (optional) at the previous layer, creating a new message $\mathbf{m}_j^{(k)}$ by applying a certain transformation $\psi^{(k)}$, such that:

$$\mathbf{m}_j^{(k)} = \psi^{(k)}\left(\mathbf{h}_i^{(k-1)}, \mathbf{h}_j^{(k-1)}, \mathbf{e}_{i,j}^{(k-1)}\right), \ \forall j \in \mathcal{N}_i \tag{4}$$

The message aggregation operation aggregates the transformed messages from the neighborhood vertices of v_i and passes it through a function $\gamma^{(k)}$ with learnable parameters (e.g., Multi-Layer Perceptrons (MLPs) (Fey and Lenssen, 2019)). Therefore, a single message passing operator is defined as:

$$\mathbf{h}_i^{(k)} = \gamma^{(k)}\left(\mathbf{h}_i^{(k-1)}, \underset{j \in \mathcal{N}_i}{\square} \psi^{(k)}\left(\mathbf{h}_i^{(k-1)}, \mathbf{h}_j^{(k-1)}, \mathbf{e}_{i,j}^{(k-1)}\right)\right) \tag{5}$$

where $\square$ represents differentiable permutation-invariant operation (e.g., Σ, Max, Mean).

Definition 2.4. Error Quadrics (Garland and Heckbert, 1997). Given a plane $\mathbf{p} = [a\ b\ c\ d]^\top$ defined by the equation $ax + by + cz + d = 0$ where $a^2 + b^2 + c^2 = 1$. We can define the *fundamental error quadric* matrix as:

$$\mathbf{K_p} = \mathbf{pp}^\top, \tag{6}$$

which can be thought of as the quadratic representation of plane $\mathbf{p}$. In practice, we can represent an entire set of planes $\mathcal{P} = \{\mathbf{p}_1\ \mathbf{p}_2\ ...\ \mathbf{p}_n\}$ as a single matrix $Q_\mathcal{P}$ by summing up

their corresponding fundamental error quadrics:

$$Q_{\mathcal{P}} = \sum_{\mathbf{p} \in \mathcal{P}} \mathbf{K_p} \tag{7}$$

Appendix B. Description of Dataset

Data used in the preparation of this study were obtained from the Alzheimer's Disease Neuroimaging Initiative (ADNI) database (adni.loni.usc.edu). Beginning in 2004, ADNI is a longitudinal multi-center study, led by Dr. Michael W. Weiner that aimed at the early detection and progression tracking of Alzheimer's disease (AD) using clinical, imaging (e.g., MRI, PET image data), genetic, and biochemical markers.

B.1. Mesh Extraction

Starting from the T1-weighted MRIs, each scanned image was processed by a set of preprocessing procedures, including image denoising using FreeSurfer v6.0 (Bruce, 2012), B1 field homogeneity correction, and intensity/spatial normalization to extract the wanted surfaces. For the cortex structure, the inner cortical surfaces (modeling the interface between grey and white matter) and outer cortical surfaces (modeling the cerebrospinal fluid/grey matter interface) were extracted. Besides, seven subcortical structures (amygdala, nucleus accumbens, caudate, hippocampus, pallidum, putamen, thalamus) per hemisphere were segmented and modeled into the surface using SPHARM-PDM (https://www.nitrc.org/projects/spharm-pdm)

To preserve the anatomy of both cortex and subcortical structures, their surfaces were inflated, parameterized to a sphere, and registered to a spherical surface template using a rigid body registration (Besson et al., 2014; Azcona et al., 2020). Then, the surface templates were converted to triangular meshes following a triangulation scheme. Here, each edge was assigned a weight $\mathbf{e}_{i,j}$ which corresponds to its geodesic distance $\psi_{i,j}$ along the surface, such that:

$$\mathbf{e}_{i,j} = \frac{1}{\sigma\sqrt{2\pi}} \exp\left\{ -\frac{1}{2}\left(\frac{\psi_{i,j}}{\sigma}\right)^2 \right\} \tag{8}$$

B.2. Data Statistics

4072 T1-weighted MRI volumes are used in this paper, which corresponds to 492 subjects. Basic demographic information includes the number of samples with different labels, as well as the age and gender distribution of the subjects are shown in the Table below:

Table 4: Demographic information of the ADNI dataset, including sample numbers across different labels and the age and gender distribution of the subjects.

	Samples	Gender (M/F)	Age (mean± SD)	MMSE (mean± SD)
EMCI (n=259)	1880	143/116	71.0 ± 7.6	27.4 ± 1.4
LMCI (n=233)	2156	127/105	74.1 ± 7.1	25.3 ± 2.4

[1] *MMSE* Mini-mental State Examination