PRUDEX-Compass: Towards Systematic Evaluation of Reinforcement Learning in Financial Markets

Anonymous authors
Paper under double-blind review

Abstract

The financial markets, which involve more than $90 trillion market capitals, attract the attention of innumerable investors around the world. Recently, reinforcement learning in financial markets (FinRL) has emerged as a promising direction to train agents for making profitable investment decisions. However, the evaluation of most FinRL methods only focuses on profit-related measures and ignores many critical axes, which are far from satisfactory for financial practitioners to deploy these methods into real-world financial markets. Therefore, we introduce **PRUDEX-Compass**, which has 6 axes, i.e., Profitability, Risk-control, Universality, Diversity, rEliability, and eXplainability, with a total of 17 measures for a systematic evaluation. Specifically, i) since most existing FinRL algorithms are only designed to maximize profit with unsatisfactory performance under systematic evaluation, we propose AlphaMix+, which leverages mixture-of-experts and risk-sensitive approaches, to serve as one strong FinRL baseline that outperforms market average[1] on all 6 axes along with PRUDEX-Compass, ii) we evaluate AlphaMix+ and 7 other FinRL methods in 4 long-term real-world datasets of influential financial markets to demonstrate the usage of our PRUDEX-Compass and the superiority of AlphaMix+, iii) PRUDEX-Compass[2] together with 4 real-world datasets, standard implementation of 8 FinRL methods, a portfolio management environment and related visualization toolkits is released as public resources to facilitate the design and comparison of new FinRL methods. We hope that PRUDEX-Compass can not only shed light on future FinRL research to prevent untrustworthy results from stagnating FinRL into successful industry deployment but also provide a new challenging algorithm evaluation scenario for the reinforcement learning (RL) community.

1 Introduction

Quantitative trading is a type of market strategy that relies on mathematical and statistical models to automatically identify investment opportunities (Chan, 2021). With the advent of the AI age, it becomes more popular and accounts for more than 70% and 40% trading volumes, in developed markets (e.g., US) and developing markets (e.g., China), respectively (Karpoff, 1987). How to make profitable investment decisions against the various uncertainties in quantitative trading becomes one of the main challenges for financial practitioners (An et al., 2022). Among the various machine learning methods, such as deep learning (Xu & Cohen, 2018; Sawhney et al., 2021) and boosting decision trees (Ke et al., 2017), deep reinforcement learning (DRL) is attracting increasing attention from both academia and financial industries (Sun et al., 2021a) due to its stellar performance on solving complex sequential problems such as Go (Silver et al., 2017), StarCraft-II (Vinyals et al., 2019), nuclear fusion (Degrave et al., 2022) and matrix mulplication (Fawzi et al., 2022).

Deep RL has achieved significant success in various quantitative trading tasks. Specifically, FDDR (Deng et al., 2016) and iRDPG (Liu et al., 2020b) are designed to learn financial trading signals and micmic behaviors of professional traders for algorithmic trading, respectively. For portfolio management, deep RL

[1] Market average indicates the trading strategy, which invests equal amount of money into all financial assets in the pool, to reflect the average market conditions.

[2] https://anonymous.4open.science/r/PRUDEX-Compass-948C

methods are proposed to account for the impact of market risk (Wang et al., 2021b) and the commission fee (Wang et al., 2021a). A PPO-based framework (Lin & Beling, 2020) is proposed for order execution and a policy distillation mechanism is added to bridge the gap between imperfect market states and optimal execution actions (Fang et al., 2021). For market making, deep RL methods are introduced from both game-theoretic (Spooner et al., 2018) and adversarial learning (Spooner & Savani, 2020) perspectives as an adaptation of traditional mathematical models.

However, the evaluation of existing FinRL methods (Sun et al., 2022; Wang et al., 2021a; Fang et al., 2021) only focuses on profit-related measures, which ignores several critical axes, such as risk-control and reliability. In addition to profitability, financial practitioners care about many other aspects of FinRL methods, i.e., how much risk I need to take for per unit of profit; how FinRL algorithms behave when the market status changes. In preliminary experiments, we find many examples that indicate the weakness of existing profit-seeking FinRL algorithms. For instance, IMIT (Ding et al., 2018) may lead to catastrophic capital loss when black swan events happen (Section 6.7) and SAC (Haarnoja et al., 2018) shows poor risk-control ability, which is not an ideal option for conservative traders (Section 6.3). In practice, due to the low signal-to-noise and distribution shift nature of financial markets (Malkiel, 2003), FinRL methods with only high profit on backtesting are very likely to overfit on historical data and fail in real-world deployment (De Prado, 2018). As David Shaw (founder of a world-class hedge fund) said [3], he will never trade with a method that does not prove itself through a systematic evaluation. Therefore, a benchmark for the systematic evaluation of FinRL methods is urgently needed.

In this paper, we first introduce PRUDEX-Compass, which has 6 axes with a total of 17 measures for systematic evaluation of FinRL methods. we then propose AlphaMix+, a deep RL method composed of diversified mixture-of-experts and risk-aware Bellman backup, as a strong FinRL baseline that significantly outperforms existing FinRL methods under systematic evaluation by mimicking the bottom-up hierarchical trading strategy design workflow in real-world companies (Khorana et al., 2007). In addition, we evaluate 7 widely used FinRL methods together with AlphaMix+ on 4 long-term real-world datasets spanning over 15 years on popular trading tasks to demonstrate the usage of PRUDEX-Compass and the superiority of AlphaMix+. Accompanied with an open-source library[2] of datasets, baseline implementation, RL environment and evaluation toolkits, we call for a change in how we evaluate FinRL methods to facilitate the industry deployment of FinRL methods. Moreover, PRUDEX-Compass also provides the RL community new algorithm evaluation scenarios to test the effectiveness of novel RL algorithms in the ever-changing financial markets.

2 PRUDEX-Compass: Systematic Evaluation of FinRL

To provide a clear exposition of FinRL evaluation, we introduce PRUDEX-Compass to provide an intuitive visual means to give readers a sense of comparability and positioning of FinRL methods. PRUDEX-Compass is composed of two central elements: i) the axis-level (inner), which specifies the different axes considered for FinRL evaluation and ii) measure-level (outer), which specifies the measures used for benchmarking FinRL methods. Figuratively speaking, the axis-level maps out the relative strength of FinRL methods in terms of each axis, whereas the measure-level provides a compact way to visually assess which setup and evaluation measures are practically reported to point out how comprehensive the evaluation are for FinRL algorithms. To provide a practical basis, we have directly filled the exemplary compass visualization in Figure 1. The contributions of PURDEX-Compass are three-fold: i) carefully collecting 17 measures from the literature of multiple disciplines (e.g., finance, AI, statistics and engineering) and properly categorizing them into 6 axes; ii) proposing customized version of the measures suitable for FinRL together with a set of easy-to-use visualization tools (Section 6.2–6.7); iii) introducing PRUDEX-Compass, a unified visual interface composed of two core elements to indicate the relative performance strength of FinRL methods (inner part) and their evaluation completeness (outer part).

[3] https://en.wikipedia.org/wiki/David_E._Shaw

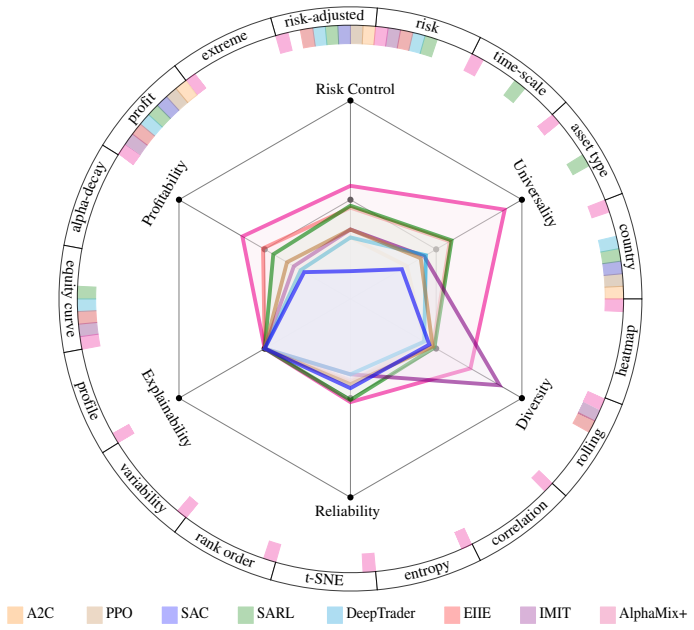


Figure 1: An illustration of our FinRL methods evaluation benchmark PRUDEX-Compass. The inner star plot provides a visual indication of the strength of different FinRL methods in terms of six axes. A mark on the star plot's inner circle suggests the market average. The outer level of the PRUDEX-Compass specifies which particular measures have been evaluated in practice to show the status of evaluation. We fill the compass with AlphaMix+ and 7 widely-used FinRL methods to provide an intuitive example. In general, AlphaMix+ gets the best performance (largest score in 4 out 6 axes) with a comprehensive evaluation (much more markers in the outer level).

2.1 Axes of PRUDEX-Compass

We choose the design of the axis-level compass as a star diagram following (Wang et al., 2022; Mundt et al., 2021). Specifically, the axis-level element contains two hexagons, marks on all vertices of the two hexagons[4], and lines connecting the central point and vertices of hexagons. Since financial practitioners consider relative performance to market average as the golden standard to evaluate their own strategies, we add contours with a mark in the middle of central point and outer circle of the axis-level (e.g., $t = 50$) to indicate the market average for convenient check. To indicate the relative strength of FinRL methods in terms of 6 critical evaluation perspectives, we first calculate the score[5] of each FinRL algorithm in terms of each axis by normalizing the numeric values of original experimental results into an integer score $t \in [0, 100]$. We then decide the position of vertices based the score and connect them to provide a visual impression on the performance of each FinRL method. The advantages of this design are three-fold: i) it provides an ideal visual representation when comparing plot elements (Fuchs et al., 2014), ii) it allows human perceivers to quickly learn more facts by fast visual search (Elder & Zucker, 1993), and iii) the geometric region boundaries in the star plot have high priority in perception (Elder & Zucker, 1998). We introduce the 6 axis-level elements of PRUDEX-Compass as follows:

Profitability. Aligned with the key objective of QT, profitability focuses on the evaluation of FinRL methods' ability to gain market capital. Besides pure return, it also measures how stable (Franco & Leah, 1997) and persistent (Gârleanu & Pedersen, 2013) FinRL methods are to achieve high profit.

Risk-Control. Due to the well-known tradeoff between profit and risk in finance (Brink & McCarl, 1978), financial practitioners take great efforts on the assessment and control of both systematic risk and idiosyncratic risk (Goyal & Santa, 2003), which is also of vital importance in FinRL evaluation.

Universality. The financial market is a complex ecosystem that involves innumerable assets, countries, time-scale and trading styles. Universality tries to evaluate FinRL's ability to achieve satisfied performance (e.g., better than market average) in various quantitative trading scenarios. Designing FinRL methods with better universality (Fang et al., 2021) is in line with popular ML topics such as transfer learning (Pan & Yang, 2009) and meta learning (Hospedales et al., 2021).

[4] The edges and vertices of the inner hexagon become slightly blurry but still distinguishable after filling in the results of 8 FinRL algorithms.

[5] Most users can directly use our setting and compare the score (larger is better). Descriptions of normalization equations and why it makes sense are available in Appendix A.2.

Diversity. In finance, diversification refers to the process of allocating capitals in a way that reduces the exposure to any one particular asset or risk. As Markowitz (Nobel Laureate in Economics) said (Tu & Zhou, 2011), diversity is the only free lunch in investing that plays an indispensable role on enhancing profitability and risk-control. In RL community, diversity is widely used to encourage exploration (Parker et al., 2020). This axis of PRUDEX-Compass tends to address the lack of diversity evaluation of FinRL methods.

Reliability. RL methods tend to be highly variable in performance and considerably sensitive to a range of different factors such as random seeds (Henderson et al., 2018) and market stationarity shift across time (Lee et al., 2010). This variability issue hinders a reliable method and can be costly or even dangerous for high-stake applications such as quantitative trading. This axis introduces techniques on RL reliability evaluation (Chan et al., 2019; Agarwal et al., 2021) with a focus on quantitative trading.

Explainability. Psychologically speaking, *if the users do not trust a model, they will not use it* (Ribeiro et al., 2016). Explainability generally refers to any technique that helps users or developers of models understand why models behave the way they do. In FinRL, it can come in the form that tells traders which model is effective under what market conditions or why one trading action is mistaken and how to fix it. Rigorous regulatory requirements in financial markets further enhance its importance for model debugging (Bhatt et al., 2020), monitoring (Pinto et al., 2019) and audit (Bhatt et al., 2020).

2.2 Measures of PRUDEX-Compass

As the inner star plot contextualizes macroscopic axes of FinRL evaluation, the outer measure-level places emphasis on detailed evaluation setup and metrics. In essence, a mark on the measure-level indicates that a method practically reports corresponding measures in its empirical investigation, where more marks indicate a more comprehensive evaluation. We list the 17 measures on the outer level of the PRUDEX-Compass in Table 1 with brief descriptions. In addition, we leave measures of FinRL explainability as future work due to the lack of FinRL algorithms with solid design of explainability. We conduct literature review on RL explainability and point their potential application in FinRL as follows. DSP (Landajuela et al., 2021) is proposed to discover symbolic policy with expert knowledge. Differentiable decision trees are incorporated into RL for better explainability (Silva et al., 2020). Another line of works tries to discover interpretable features with techniques such as self-supervised learning (Shi et al., 2020) and adversarial learning (Gupta et al., 2020). Open-XAI (Agarwal et al., 2022) offers a comprehensive open-source framework for evaluating and benchmarking post hoc explanation methods. We plan to incorporate suitable evaluation methods, i.e., LIME (Ribeiro et al., 2016) and SHAP (Lundberg & Lee, 2017), from Open-XAI into PRUDEX-Compass with customized adoption on decision-based FinRL methods.

3 FinRL Preliminaries and Problem Formulation

3.1 Portfolio Management

Portfolio management is a fundamental quantitative trading task (Sun et al., 2021a), where investors hold a number of financial assets, i.e., stocks, bonds, as well as cash, and reallocate the proportion of capitals invested in each asset periodically to maximize future profit.

OHLCV is a type of bar chart directly obtained from the financial market. OHLCV vector at time t is denoted as $\mathbf{x}_t = (p_t^o, p_t^h, p_t^l, p_t^c, v_t)$, where p_t^o is the open price, p_t^h is the high price, p_t^l is the low price, p_t^c is the close price and v_t is the volume.

Technical Indicator indicates high-order features calculated by a formulaic combination of the original OHLCV to uncover the underlying pattern of the financial market. We denote the technical indicator vector at time t: $\mathbf{y}_t = \bigcup_k y_t^k$, where $y_t^k = f_k(\mathbf{x}_{t-h}, ..., \mathbf{x}_t, \theta^k)$, f_k and θ^k are the formula function and the parameter of technical indicator k, respectively.

Portfolio is the proportion of capitals allocated to each asset that can be represented as a vector:

$$\mathbf{w_t} = [w_t^0, w_t^1, ..., w_t^M] \in R^{M+1} \quad and \quad \sum_{i=0}^{M} w_t^i = 1 \tag{1}$$

Table 1: Brief summary of evaluation measures in outer level of PRUDEX-Compass: Profitability, Risk-control, Universality, Diversity, rEliability, and eXplainability (see Appendix A.1 for details).

Axes	Measures	Descriptions
P	Profit	A class of metrics to assess FinRL's ability to gain market capital.
	Alpha Decay	Loss in the investment decision making ability of FinRL methods over time due to distribution shift in financial markets (Pénasse, 2022).
	Equity Curve	A graphical representation of the value changes over time.
R	Risk	A class of metrics to assess the risk level of FinRL methods (Shiller, 1992).
	Risk-adjusted Profit	A class of metrics that calculate the normalized profit with regards to different kinds of risks, i.e., volatility and downside risk (Magdon & Atiya, 2004).
	Extreme Market	The relative performance of FinRL methods on extreme market condition during black swan events (Aven, 2013) such as war and covid-19.
U	Country	Financial market across both developed countries (e.g., US and Europe) and developing countries (e.g., China and India).
	Asset Type	Various financial asset types, i.e., stock, future, FX and Crypto
	Time-Scale	Both coarse-grained (e.g., day level) and fine-grained (e.g., second level) financial data to match different trading styles.
D	t-SNE	A statistical visualization tool to map high-dimensional time-series data points into 2-D dimension (Vander & Hinton, 2008) to assess the data-level diversity.
	Entropy	Entropy-based metrics from information theory (Reza, 1994) to show the diversity of FinRL methods' trading behaviors.
	Correlation	Metrics that account the correlation (Kirchner & Zunckel, 2011) between financial assets to assess the diversity of FinRL methods.
	Diversity Heatmap	A visualization tool to demonstrate the diversity of investment decisions among different financial assets with heatmap (Harris et al., 2020)
E	Performance Profile	A visualization of FinRL methods' empirical score distribution (Dolan & Moré, 2002), which is easy to read with qualitative comparisons.
	Variability	The performance standard deviation across different random seeds and hyper-parameters (Henderson et al., 2018).
	Rolling Window	Using rolling time window to retrain or fine-tune FinRL methods and evaluate the performance on multiple test periods (De Prado, 2018).
	Rank Comparison	A visualization toolkit to show the rank of FinRL methods across different metrics, which will not be dominated by extreme values (Agarwal et al., 2021).
X	-	We discuss current status and highlight promising further directions.

where $M+1$ is the number of portfolio's constituents, including cash and M financial assets. w_t^i represents the ratio of the total portfolio value invested at time t on asset i and w_t^0 represents cash.

Asset Price refers to the vector of close price for each financial asset defined as $\mathbf{p_t} = [p_t^0, p_t^1, ..., p_t^M]$, where p_t^i is the close price of asset i at time t. Note that the price of cash p_t^0 is a constant.

Portfolio Value v_{t+1} at time $t+1$ is defined based on the asset price change and portfolio weight as:

$$v_{t+1} = v_t \sum_{i=0}^{M} \frac{w_t^i \; p_{t+1}^i}{p_t^i} \tag{2}$$

The objective of portfolio management is to maximize the final portfolio value given a long time horizon by dynamically tuning the portfolio weight at each time step. As a unified benchmark, evaluation metrics

proposed in PRUDEX-Compass can be easily adopted to all quantitative trading tasks. We focus on portfolio management in this work as an example.

3.2 MDP Formulation

We consider a standard RL scenario in which an agent (investor) interacts with an environment (the financial market) in discrete time. Formally, we introduce MDP, which is defined by the tuple: MDP $= (\mathcal{S}, \mathcal{A}, P, R, \gamma, H)$. Specifically, $\mathcal{S}$ is a finite set of states. $\mathcal{A}$ is a finite set of actions. $P : \mathcal{S} \times \mathcal{A} \times \mathcal{S} \longrightarrow [0, 1]$ is a state transaction function, which consists of a set of conditional transition probabilities between states. $R : \mathcal{S} \times \mathcal{A} \longrightarrow \mathcal{R}$ is the reward function, where $\mathcal{R}$ is a continuous set of possible rewards and R indicates the immediate reward of taking an action in a state. $\gamma \in [0, 1)$ is the discount factor and H is a time horizon indicating the length of the trading period. A (stationary) policy $\pi_\theta : \mathcal{S} \times \mathcal{A} \longrightarrow [0, 1]$, parameterized by θ, assigns each state $s \in \mathcal{S}$ a distribution over actions, where $a \in \mathcal{A}$ has probability $\pi(a|s)$. A Q-value function gives expected accumulated reward when executing action a_t in state s_t and following policy π in the future, which is $Q(s_t, a_t) = \mathbb{E}_{(s_{t+1},...,\pi)} \left[\sum_{i=t}^{T} \gamma^i r(s_i, a_i)\right]$. During training, one episode corresponds to adjusting the portfolio at each time step through the whole trading periods, i.e., time scope of training set, with time horizon H. The objective of the agent is to learn an optimal policy: $\pi_{\theta^*} = argmax_{\pi_\theta} \mathbb{E}_{\pi_\theta} \left[\sum_{i=t}^{T} \gamma^i r_{t+i} \mid s_t = s\right]$.

State $s_t \in \mathcal{S}$ at time t is the concatenation of technical indicator vectors of M financial assets $(\mathbf{y_t^1}, \mathbf{y_t^2}, ..., \mathbf{y_t^i})$, where $\mathbf{y_t^i}$ represent the technical indicator vector of asset i at time t. **Action space** at time t is an $M + 1$ dimension vector $[w_t^0, w_t^1, ..., w_t^M]$ as a portfolio $\mathbf{w}_t$ to represent the proportion of capitals invested at each asset. **Reward** r_t at time t is the change of portfolio value: $r_t = v_{t+1} - v_t$, where positive/negative values indicate earning/losing money, respectively.

3.3 Soft Actor-Critic (SAC) and Other Popular FinRL Methods

We introduce SAC (Haarnoja et al., 2018), which is the base model of many popular FinRL methods (Yuan et al., 2020). SAC is an off-policy actor-critic method based on the maximum entropy RL framework (Ziebart, 2010), which maximizes a weight objective of the reward and the policy entropy, to encourage robustness to noise and exploration. For parameter updating, SAC alternates between a soft policy evaluation and a soft policy improvement. At the soft policy evaluation step, a soft Q-function $Q_\theta(s_t, a_t)$, which is modeled as a neural network with parameters θ, is updated by minimizing the following soft Bellman residual:

$$\mathcal{L}_{critic}^{\text{SAC}}(\phi) = \mathbb{E}_{\tau_t \sim \mathcal{D}}[L_Q(\tau_t, \theta)], \tag{3}$$

$$L_Q(\tau_t, \theta) = (Q_\theta(s_t, a_t) - r_t - \gamma \bar{V}(s_{t+1}))^2, \tag{4}$$

$$where \quad \bar{V}(s_t) = \mathbb{E}_{a_t \sim \pi_\phi}[Q_{\bar{\theta}}(s_t, a_t) - \alpha \log \pi_\phi(a_t \mid s_t)]. \tag{5}$$

where $\tau_t = (s_t, a_t, r_t, s_{t+1})$ is a transition, $\mathcal{D}$ is a replay buffer, $\bar{\theta}$ are the delayed parameters, and α is a temperature parameter. At the soft policy improvement step, the policy π with its parameter θ is updated by minimizing the following objective:

$$\mathcal{L}_{actor}^{\text{SAC}}(\theta) = \mathbb{E}_{s_t \sim \mathcal{D}}[L_\pi(s_t, \phi)], \tag{6}$$

$$L_\pi(s_t, \phi) = \mathbb{E}_{a_t \sim \pi_\phi}[\alpha \log \pi_\phi(a_t \mid s_t) - Q_\theta(s_t, a_t)]. \tag{7}$$

To handle continuous action spaces, the policy is modeled as a Gaussian with mean and covariance given by neural networks. In addition to SAC, A2C (Mnih et al., 2016), a popular actor-critic RL method, shows stellar performance in algorithmic trading (Zhang et al., 2020). The simple and efficient policy gradient method PPO (Schulman et al., 2017) performs well in capturing trading opportunities for order execution (Lin & Beling, 2020). EIIE (Jiang et al., 2017) and Investor-Imitator (IMIT) (Ding et al., 2018) are two pioneering works that apply deep RL for quantitative trading. Furthermore, SARL (Ye et al., 2020) and Deeptrader (Wang et al., 2021b) are proposed with augmented market embedding to take market risk into account for portfolio management.

4 AlphaMix+: A Strong Baseline

Before diving into our systematic evaluation benchmark PRUDEX-Compass[6], AlphaMix+, an FinRL algorithm based on ensemble learning, is proposed to fill the gap due to the poor performance of existing FinRL methods under systematic evaluation. Considering the limitation of existing FinRL methods, the major one is that investment decisions are made by a single agent with high potential risk. The success of real-world trading firms relies on an efficient bottom-up hierarchical workflow with risk management as illustrated in Figure 2). First, multiple experts conduct data analysis and build models independently based on personal trading style and risk tolerance. Later on, a senior portfolio manager summarizes their results, manage risk and makes final investment decisions.

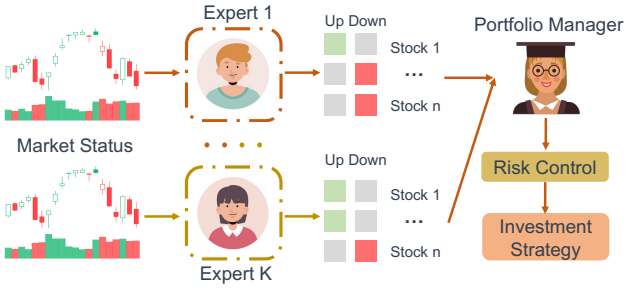


Figure 2: Workflow of real-world trading firms.

Inspired by it, we propose AlphaMix+, a universal deep RL framework with diversified risk-aware mixture-of-experts to mimic this efficient workflow. In principle, AlphaMix+ can be used in conjunction with most modern off-policy RL algorithms for any quantitative trading task. As SAC (Haarnoja et al., 2018) is a sample-efficiency algorithm in quantitative trading (Yuan et al., 2020), we pick it as the base model of AlphaMix+ here for exposition. An overview of AlphaMix+ is shown in Figure 3.

Risk-aware Bellman backup. We consider a trading firm with N trading experts, i.e., $\{Q_{\theta_i}, \pi_{\phi_i}\}_{i=1}^N$, where θ_i and ϕ_i denote the parameters of the i-th soft Q-function and policy. For conventional Q-learning based on the Bellman backup in Eq. (3), one major issue is the negative impact of error propagation that induces the "noise" to the learning "signal" (true Q-value) of the current Q-function (Kumar et al., 2020). This issue is more severe in the financial markets with a low signal-to-noise ratio and can cause unstable convergence (Kumar et al., 2020). To mitigate this issue, for each agent i, we consider a risk-aware Bellman backup (Lee et al., 2021b) as follows:

$$\mathcal{L}_{WQ}(\tau_t, \theta_i) = w(s_{t+1}, a_{t+1})(Q_{\theta_i}(s_t, a_t) - r_t - \gamma \bar{V}(s_{t+1}))^2 \tag{8}$$

where $\tau_t = (s_t, a_t, r_t, s_{t+1})$ is a transition, $a_{t+1} \sim \pi_{\phi_i}(a \mid s_t)$, and $w(s, a)$ is a confidence weight based on the ensemble of target Q-functions:

$$w(s, a) = \sigma(-\bar{Q}_{std}(s, a) * T) + k \tag{9}$$

where $\bar{Q}_{std}(s, a)$ is the empirical standard deviation of all target Q-functions $\{Q_{\bar{\theta}_i}\}_{i=1}^N$ and $T > 0$ is a temperature parameter (Hinton et al., 2015) to adapt the scale of $\bar{Q}_{std}(s, a)$. σ is the sigmoid function and $k > 0$ is used to control the value range of confidence weight. Note that the confidence weight is bounded in $[k, k + 0.5]$ since $\bar{Q}_{std}(s, a)$ is always positive. The objective $\mathcal{L}_{WQ}$ down weights the sample transitions with inconsistent trading suggestions from different experts (high variance across target Q-functions), resulting in a loss function for the Q-updates with better risk management.

Diversified Experts. Bootstrap with random initialization (Osband et al., 2016) is applied to encourage the diversity between trading experts through two ideas: First, we initialize the model parameters of all trading experts with random parameter values for inducing an initial diversity in the models following (Lakshminarayanan et al., 2017; Wenzel et al., 2020). Second, we apply different samples to train each agent based on similar idea in BatchEnsemble (Wen et al., 2019). Specifically, for each SAC agent i in each time step t, we draw the binary masks $m_{t,i}$ from the Bernoulli distribution with parameter $\beta \in (0, 1]$, and store them in the replay buffer.

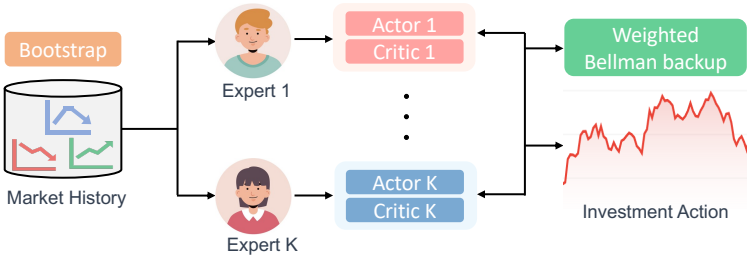


Figure 3: An illustration of AlphaMix+, a universal deep RL framework with diversified risk-aware mixture-of-experts.

[6]Readers whose main interest is the evaluation benchmark may skip this Section and take AlphaMix+ as a strong FinRL baseline.

Then, when updating the model parameters of agents, we multiply the bootstrap mask to each objective function, such as: $m_{t,i}\mathcal{L}_\pi(s_t, \phi_i)$ and $m_{t,i}\mathcal{L}_{WQ}(\tau_t, \theta_i)$ in Eq.(7) and Eq.(8), respectively. This encourages each expert to think individually with diversified strategies. We find it sufficient for AlphaMix+ to have desired diversity (experiments in Section 6.6) with the two simple ideas. Other tricks such as a KL divergence (Yu et al., 2013) loss term is not further incorporated to keep simplicity. For inference, we propose a simple approximation scheme, which first generates N candidate actions from ensemble policies $\{\pi_{\phi_i}{}_{i=1}^{N}\}$, and then chooses the action that maximizes the UCB (Chen et al., 2017) as follows:

$$A_t = a_{t,i} \sim \pi_{\phi_i}(a \mid s_t) \mid i \in 1, ..., N \tag{10}$$

$$a_t = \underset{a \in A_t}{argmax_a}\ Q_{mean}(s_t, a) + \lambda Q_{std}(s_t, a) \tag{11}$$

Where $Q_{mean}(s_t, a)$ and $Q_{std}(s_t, a)$ are the mean and standard deviation of evaluation Q-functions $\{Q_{\theta_i}(s_t, a_{t,i})\}_{i=1}^{N}$. This inference method can encourage exploration by adding a bonus (e.g., Q_{std}) for visiting unseen state-action pairs similar to the UCB algorithm (Auer et al., 2002). We approximate the maximum posterior action by averaging the mean of Gaussian distributions modeled by each ensemble policy. We conduct ablation studies on the effectiveness of each component in AlphaMix+ and parameter analysis to probe sensitivity. We put related experimental results in Appendix D.2 and D.3, respectively.

5 Experimental Setup

5.1 Datasets

We collect real-world financial datasets spanning over 15 years of US stock, China stock, Cryptocurrency (Crypto) and Foreign Exhange (FX) from Yahoo Finance and Kaggle. All raw data and related processing scripts are publicly available. We summarize statistics of the 4 datasets with further elaboration in Table 2. US Stock dataset contains 10-year historical prices of 29 influential stocks with top unit price as a strong assessment of the market's overall health and tendencies. China Stock dataset contains 4-year historical prices of 47 influential stocks with top capitalization from the Shanghai exchange. Both US and China stock data is collected from Yahoo-Finance[7]. Crypto[8] dataset contains 6-year historical prices of 9 influential virtual currency with top unit price and trading volume collected. FX[9] dataset contains 20-year historical prices of 22 most popular currency with top foreign exchange reserves for US dollars. For each dataset, we filter out financial assets with missing values. For data split, we apply the similar split procedure in (Sawhney et al., 2020) with rolling window for all four datasets. As shown in Figure 4, phase 3 uses the last year for test, penultimate year for validation and the remaining of the dataset for training. For phase one and two, their validation/test sets roll back one and two years, respectively.

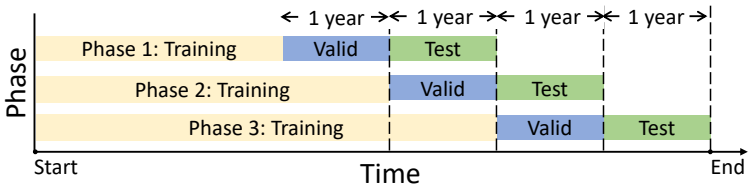


Figure 4: Train/valid/test split procedure with rolling windows.

Table 2: Dataset statistics

Dataset	Market	Freq	Number	Days	From	To	Source
US Stock	US	1d	29	2517	12/01/03	21/12/31	Yahoo
China Stock	China	1h	47	1036	16/06/01	20/09/01	Yahoo
Crypto	-	1d	9	2014	16/01/01	21/07/06	Kaggle
FX	-	1d	22	5015	00/01/03	19/12/31	Kaggle

5.2 Features

[7] https://github.com/yahoo-finance
[8] https://www.kaggle.com/datasets/sudalairajkumar/cryptocurrencypricehistory
[9] https://www.kaggle.com/datasets/brunotly/foreign-exchange-rates-per-dollar-20002019

We generate 11 temporal features as shown in Table 3 to describe the stock markets following (Yoo et al., 2021). z_{open}, z_{high} and z_{low} represent the relative values of the open, high, low prices compared with the close price at current time step, respectively. z_{close} and z_{adj_close} represent the relative values of the closing and adjusted closing prices compared with time step $t-1$. z_{dk} represents a long-term moving average of the adjusted close prices during the last k time steps compared to the current close price. We apply z-score normalization on each feature.

Table 3: Features to describe the financial markets

Features	**Calculation Formula**
$z_{open}, z_{high}, z_{low}$	$z_{open} = open_t/close_t - 1$
z_{close}	$z_{close} = close_t/close_{t-1} - 1$
$z_{d_5}, z_{d_10}, z_{d_15}$ $z_{d_20}, z_{d_25}, z_{d_30}$	$z_{d_5} = \frac{\sum_{i=0}^{4} close_{t-i}/5}{close_t} - 1$

5.3 Baselines

We conduct experiments with 7 representative FinRL methods including 3 classic RL methods: A2C (Mnih et al., 2016), PPO (Schulman et al., 2017), SAC (Haarnoja et al., 2018), 4 RL-based trading methods: EIIE (Jiang et al., 2017), Investor-Imitator (IMIT) (Ding et al., 2018), SARL (Ye et al., 2020) and DeepTrader (DT) (Wang et al., 2021b) and our AlphaMix+. Descriptions of baselines are as follows:

- A2C (Mnih et al., 2016) is a classic actor-critic RL algorithms that introduce an advantage function to enhance policy gradient update by reducing variance.
- PPO (Schulman et al., 2017) is a proximal policy optimization that constrain the difference between current policy and updated policy with simplified clipping term in the objective function.
- SAC (Haarnoja et al., 2018) is an off-policy actor-critic method based on the maximum entropy RL framework, which encourages the robustness to noise and exploration by maximizing a weight objective of the reward and the policy entropy.
- SARL (Ye et al., 2020) proposes a state-augmented RL framework, which leverages the price movement prediction as additional states, based on deterministic policy gradient (Silver et al., 2014) methods.
- DeepTrader (DT) (Wang et al., 2021b) is a policy gradient based method. To tackle the risk-return balancing issue, it simultaneously uses negative maximum drawdown and price rising rate as reward functions to balance between profit and risk with an asset scoring unit.
- EIIE (Jiang et al., 2017) is a deterministic policy gradient based RL framework, which contains: 1) an ensemble of identical independent evaluators topology; 2) a portfolio vector memory; 3) an online stochastic batch learning scheme.
- Investor-Imitator (IMIT) (Ding et al., 2018) imitates behaviors of different investors (e.g., oracle/collaborate/public investor) using investor-specific reward functions with a set of logic descriptors.

Non-RL methods are not included as baselines for two reasons: i) In general, RL methods outperform different types of non-RL methods (Moskowitz et al., 2012; Ke et al., 2017; Xu & Cohen, 2018) in different trading tasks. ii) PRUDEX-Compass focuses on the evaluation of RL methods in financial markets. We leave comparison with non-RL methods as future directions and discuss our plan in Section 7.

5.4 Training Setup

We perform all experiments on an RTX 3090 GPU with 5 fixed random seeds. We apply grid search for AlphaMix+ on Crypto and FX datasets and apply the same hyperparameters on China and US stock datasets. We try scale parameter k in list $[0.3, 0.5, 0.7, 0.9]$, binomial sample parameter β in list $[0.3, 0.4, 0.5, 0.6, 0.7]$ and temperature T in list $[18, 19, 20, 21, 22]$.We explore batch size in list $[256, 512, 1024]$ and hidden size in range $[64, 128]$, We apply learning rate $7e^{-4}$ for both actor and critic. Adam is used as the optimizer. One full list of hyperparameters is available in Appendix C.1. We train AlphaMix+ for 10 epochs on all datasets. It takes about 1-1.5 hours to train and test on China stock, US stock, FX and Crypto datasets, respectively.

For other FinRL methods, there are two conditions: i) if there are authors' official or open-source FinRL library (Liu et al., 2020a) implementations, we apply the same hyperparameters for a fair comparison. This condition applies for A2C, PPO, SAC, SARL and DeepTrader. ii) if there are no publicly available implementations, we reimplement the algorithms and try our best to maintain consistency based on the original papers. This applies for EIIE and IMIT.

5.5 RL Environment Implementation

In this work, we apply the popular portfolio management environment (Liu et al., 2020a) implemented based on OpenAI Gym (Brockman et al., 2016), which simulates live financial markets with realistic historical market data according to the principle of time-driven simulations. During training, we feed observations of technical indicators as input of RL agents. RL agents generate a portfolio (action) and the environment returns the net value change at each time step as reward. By interacting with the environment, the trading agents will try to derive a trading strategy with high profits. Specifically, the environment assumes the trading volume of agents is not very large and has little impact on the market. Then, it is reasonable to use the price fluctuation of offline historical financial data to build a model for reward calculation during online simulation.

6 Demonstrative Usages of PRUDEX-Compass and Related Evaluation Toolkits

In this section, we conduct experiments on portfolio management with real-world datasets of 4 influential financial markets to demonstrate the usage of PRUDEX-Compass and related evaluation toolkits. In Section 6.1, we show how different investors can get a general impression on FinRL algorithms' performance with PRUDEX-Compass. Moreover, we provide example usage of other evaluation toolkits with a focus on one particular perspective including: (1) t-SNE plot to show data-level diversity, (2) PRIDE-Star to report the performance of 8 point-wise financial metrics for evaluating profitability, risk-control and diversity, (3) performance profile and rank distribution plot as unbiased and robust measures towards reliable FinRL methods, (4) portfolio diversity heatmap to evaluate the decision-level diversity, (5) extreme market scenarios with black swan events to evaluate the risk-control and generalization ability of FinRL algorithms. In particular, investors can either use these evaluation toolkits together with PRUDEX-Compass to pursue a systematic evaluation or as an independent measure with a focus on the perspective they care about.

6.1 A General Impression with PRUDEX-Compass

As shown in Figure 1, we fill the PRUDEX-Compass based on the experimental results of the 8 FinRL methods. For axis-level, it directly illustrates the relative performance of each method in terms of 6 axes to provide a general impression. We normalized the score into 0 to 100 with 50 as the market average (details in Appendix A.2). For explainability, all methods are scored 50 as we leave it as future direction. AlphaMix+ performs best in all 5 remaining axes. Specifically, it outperforms other FinRL methods 53% and 43% in universality and diversity, respectively, which demonstrates the effectiveness of the weighted Bellman backup and diversified bootstrap initialization.

For measure-level, we give a mark if one measure is used in the evaluation of the FinRL methods, the goal here is to show how comprehensive the methods are evaluated. Together with all measures we proposed, AlphaMix+ clearly has a more rigorous evaluation, which makes the results more trustworthy. Arguably, PRUDEX-Compass provides a compact visualization to evaluate FinRL methods that is much better than only looking at a result table of different metrics especially when lots of FinRL methods are involved. In other words, the compass highlights the required subtleties, that may otherwise be challenging to extract from text descriptions, potentially be under-specified and prevent readers to misinterpret results based on result table display. With PRUDEX-Compass, users can flexibly pick suitable methods with regards to their personal interests. Conservative traders may prefer methods with a relative stable profit rate and low risk. Aggressive traders may pay more attention on profitability, as they are willing to take high risk to pursue extremely high profit. For international trading firms, they may have high expectation on universality and diversity.

6.2 Visualizing Financial Markets with t-SNE

Even though it is a wide consensus that different financial markets share different trading patterns (Campbell et al., 1998), there is a lack of visualization tool to demonstrate how different are these markets. To show data-level diversity of evaluation, we use t-SNE here to map all 4 datasets into a 2-D dimension plot with the 11 features described in Table 3 as the input. To avoid overlapping in financial data, we pick a data point every 30 time step for each asset across 4 financial markets. Each data point corresponds to the value vector of 11 features at each time step, where necessary temporal information is maintained[10] In Figure 5, the US stock and FX datasets lie in the lower left and upper right corner, respectively, as a whole cluster, which is consistent with their status as relative mature and stable markets (Emenyonu & Gray, 1996). For China stock and the Crypto, data points are scattered with more outliers that demonstrate their essence as emerging and violate markets (De Santis et al., 1997). The t-SNE plot is useful to provide an intuitive expression on the data-level diversity of different markets while evaluating FinRL methods.

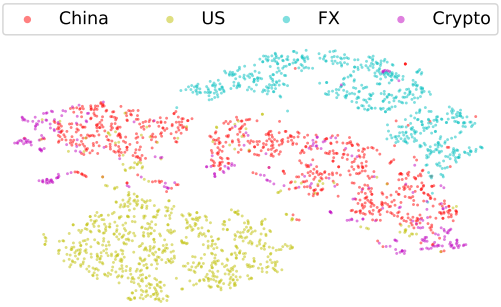


Figure 5: t-SNE market visualization.

6.3 PRIDE-Star for Evaluating Profitability, Risk-Control and Diversity

As the evaluation measures for Profitability, RIsk and DivErsity (PRIDE) are point-wise metrics with real number values, we use the PRIDE-star, which is a star plot to show the relative strength of 8 metrics including 1 profit metrics: total return (TR), 2 risk metrics: volatility (Vol) (Shiller, 1992) and maximum drawdown (MDD) (Magdon & Atiya, 2004), 3 risk-adjusted profit metrics: Sharpe ratio (SR) (Sharpe, 1998), Calmar ratio (SR) and Sortino ratio (SoR), and 2 diversity metrics: entropy (ENT) (Jost, 2006) and effect number of bets (ENB) (Kirchner & Zunckel, 2011). The mathematical definitions of these metrics are in Appendix A.1. We report the overall performance across the 4 financial markets of the 6 FinRL methods in Figure 6, where the inner circle represents market average. In general, AlphaMix+ performs best in the PRIDE-Star plot. In addition, AlphaMix+ outperforms the second best by 25% in terms of ENT that shows the effectiveness of the boostrap with random initialization component in AlphaMix+.

6.4 Performance Profile: An Unbiased Approach to Report Performance

The performance profile reports the score distribution of all runs across the 4 financial markets that are statistically unbiased, more robust to outliers and require fewer runs for lower uncertainty compared to conventional point estimates such as mean. Performance profiles proposed herein visualize the empirical tail distribution function of a random score (higher curve is better), with point-wise confidence bands based on stratified bootstrap (Efron, 1979). A score distribution shows the fraction of runs above a certain normalized score that is an unbiased estimator of the underlying performance distribution. As shown in Figure 7a, AlphaMix+ is generally a robust but conservative FinRL methods that shows the least bad runs, which makes it an attractive option for conservative investors that care more about risk. However, radical investors may pick SAC as it has the largest probability of achieving score 100, which indicates a return rate higher than twice the market average.

6.5 Rank Distribution to Demonstrate the Rank of FinRL methods

In Figure 7b, we plot the rank distribution of 8 FinRL methods in terms of TR, SR, VOL and Entropy across 4 financial markets with results of 5 random seeds in each market. The i-th column in the rank distribution plot shows the probability that a given method is assigned rank i in the corresponding metrics. For x-axis, rank 1 and 8 indicate the best and worst performance.[11] For y-axis, the bar length of a given method on a

[10] It is common to incorporate temporal information into features in Fintech. For instance, z_{d_5} uses the close price at time step $t-4$ to t..

[11] For TR, SR and entropy, higher values indicate better performance. For VOL, lower values indicate better performance

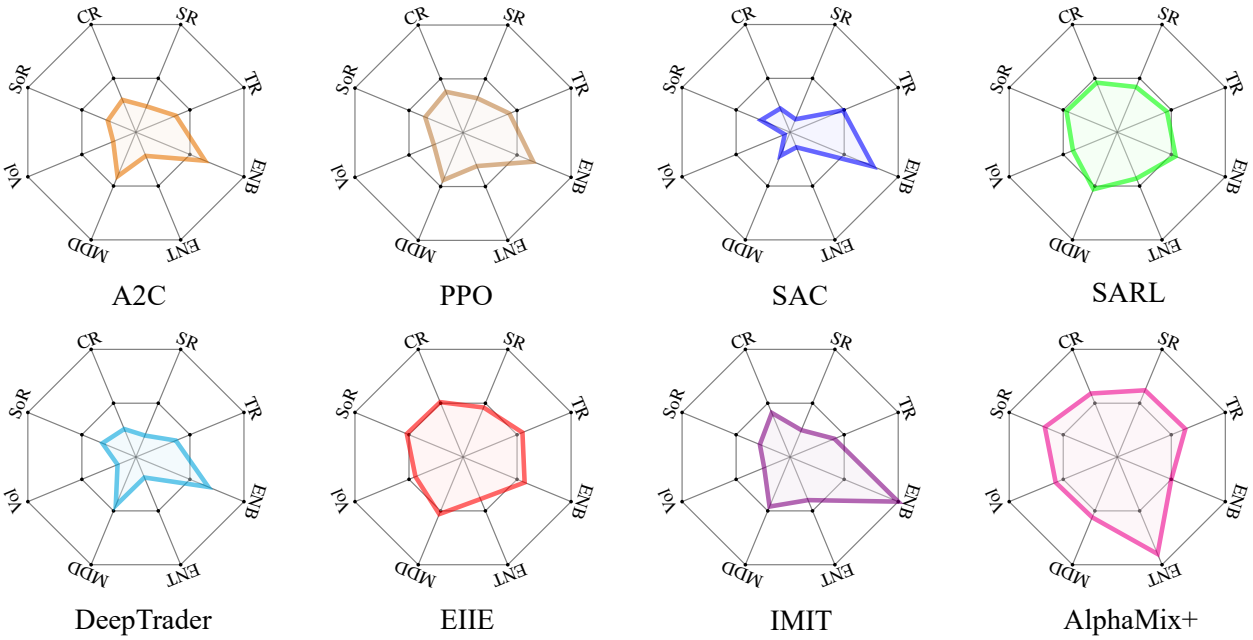
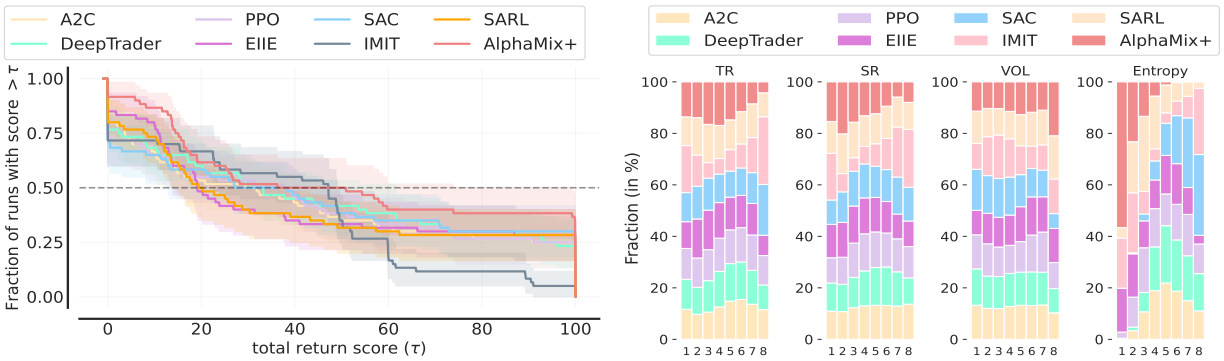


Figure 6: Overall performance across 4 financial markets on PRIDE-Star to evaluate profitability, risk-control and diversity, where AlphaMix+ achieves the best performance in 7 out of 8 metrics.



(a) (b)

Figure 7: (a) Performance profile of total return score distributions across 4 financial markets. Shaded regions show pointwise 95% confidence bands based on percentile bootstrap with stratified sampling. (b) Rank distribution in terms of TR, SR, Vol and ENT across 4 financial markets.

given metric with rank i corresponds to the % fraction of rank i it achieves across the 4 financial markets, 3 test periods and 5 random seeds ($4 \times 3 \times 5 = 60$ in total), i.e., if the rank 1 column of TR is purely red, it indicates AlphaMix+ achieves the highest TR in all random seeds across 4 financial markets.

For TR and SR, AlphaMix+ slightly outperforms other methods with 27% and 35% probability to achieve top 2 performance. For Vol, SAC gets the overall best performance while AlphaMix+ goes through higher volatility. For ENT, AlphaMix+ significantly outperforms other FinRL methods with over 56% probability for rank 1, which demonstrates its ability to train mixture of diversified trading experts.

6.6 Visualizing Strategy Diversity with Heatmap

To demonstrate the overall investment diversity of FinRL methods, we show the average portfolio across the test period as a heatmap in Figure 8. Formally, we define the average portfolio as $\bar{w}$:

$$\bar{\mathbf{w}} = [\frac{\sum_{j=t}^{t+h} w_i^0}{h+1}, \frac{\sum_{j=t}^{t+h} w_i^1}{h+1}, ..., \frac{\sum_{j=t}^{t+h} w_i^M}{h+1}] \tag{12}$$

where $M+1$ is the number of portfolio's constituents, including cash and M financial assets. w_t^i represents the ratio of the total portfolio value invested at time t on asset i, h represents the length of the evaluation period and w_t^0 represents cash.

For IMIT, it puts all capital in one or two assets. The portfolio of SARL and EIIE is not that diversified with near 0 weight on many assets more (red). For A2C, DT, PPO and SAC, the portfolio is closed to uniform, which is not desirable due to poor profitability. Our AlphaMix+ achieves an ideal investment portfolio, which is generally diversified and allocate more weights on a few bullish stocks.

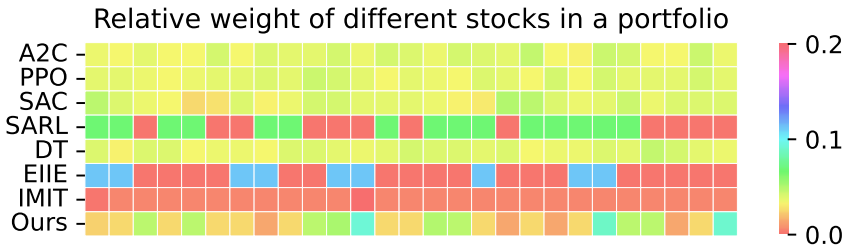


Figure 8: Heatmap of average portfolio on China stock market.

6.7 The Impact of Extreme Market Conditions

To further evaluate the risk-control and reliability, we pick three extreme market periods with black swan events. For China stock market, the period is from February 1st to March 31st 2021 when strict segregation policy is implemented in China to fight against the COVID-19 pandemic (Lee et al., 2021a). For US stock market, the period is from March 1st to April 30th 2020, when the global financial markets are violate due the global pandemic of COVID-19 (Mazur et al., 2021). For Crypto, the period is from April 1st to May 31st 2021 when many countries posed regulation against Crypto oligarch. To report the results of different metrics with different numerical value scale, we normalize them into a score m_{score} as follows:

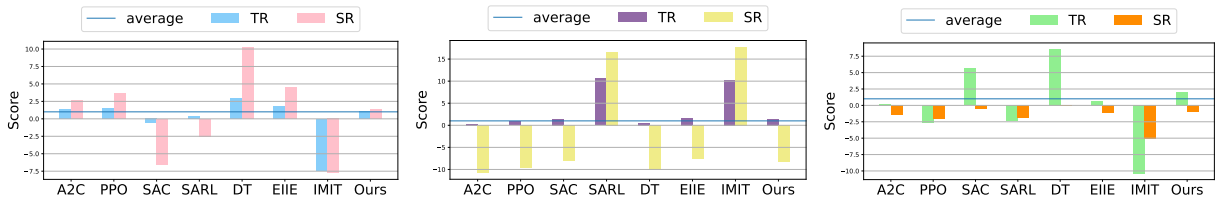
$$m_{score} = (m_{ave}/|m_{ave}|)(m_{rl}/m_{ave} - 1) * k + 1 \tag{13}$$

We define the metrics value for FinRL methods and market average as m_{rl} and m_{ave}, respectively. k is a scale parameter.

In Figure 9, we plot the bar chart of TR and SR during the period of extreme market conditions. As a conservative method, AlphaMix+'s performance is unsatisfactory in extreme market conditions, which proves the general consensus that radical methods such as DeepTrader (DT) and SARL are more suitable for extreme markets (Marimoutou et al., 2009). Analyzing the performance on extreme market conditions can shed light on the design of FinRL methods, which is in line with economists' efforts on understanding the financial markets. For instance, incorporating volatility-aware auxiliary task (Sun et al., 2021b) and multi-objective RL (Hayes et al., 2022) in AlphaMix+ may further make it be aware of extreme market conditions in advance and behave as a profit-seeking agents to achieve better performance during extreme market conditions.

7 Discussion

Complementary Related Efforts. Apart from the above aspects described in PRUDEX-Compass, there also exist several orthogonal perspectives for FinRL evaluation, which encompass a *check-list* (Pineau et al., 2021) for quantitative experiments, the construction of elaborate *dataset sheets* (Gebru et al., 2021), and the creation of *model cards* (Mitchell et al., 2019). We stress that these perspectives remain indispensable, as novel datasets and their variants are regularly suggested in FinRL and the PRUDEX-Compass does not disclose intended use with respect to human-centered application domains, ethical considerations, or their



(a) US (b) China (c) Crypto

Figure 9: Performance of FinRL methods during extreme market conditions.

caveats. We believe that it is best to report both the prior works and PRUDEX-Compass together to further improve the evaluation quality.

Potential Impact. We hope that PRUDEX-Compass could encourage both researchers and financial practitioners to avoid fooling themselves by evaluating FinRL methods in a systematic way and facilitate the design of stronger FinRL methods. While accounting for all elements in PRUDEX-Compass is not a panacea, it provides a strong foundation for trustworthy results on which the community can build on and further increase the confidence for real-world industry deployment. For RL community, PRUDEX-Compass introduces a new challenging scenario with different evaluation axes for the test of novel RL algorithms in financial market. In addition, the usage of PRUDEX-Compass is not limited in RL settings, most elements of PRUDEX-Compass can be easily generalized to supervised learning settings with broader impact.

Future Plans. We plan to improve PRUDEX-Compass from the following perspectives: i) For axis-level, we plan to explore the evaluation of FinRL explainability with measures and plots; ii) For measure-level, we plan to include metrics to evaluate alpha decay and more metrics, e.g., optimality gaps, for profits and risks; iii) For a comprehensive evaluation under different market stationarity assumptions, we plan to add one toolkit to automatically categorize market into different styles (e.g., bull/bear) and evaluate the performance of FinRL methods under different styles. Furthermore, there can be a data-driven simulator to generate unseen stylized data for further evaluation; iv) For visualization, we plan to further develop a GUI software version accompanied with a website to further lower the barrier for dissemination and use; v) As most axes and measures in PRUDEX-Compass are also key points for non-RL trading scenarios, we plan to bring PRUDEX-Compass into more general machine learning settings with implementations and results of non-RL methods for broader impact.

Auxiliary Experiments. Due to space limitations, we have included some auxiliary yet important experiments in Appendix D. Specifically, the result tables with mean and standard deviation of the 8 metrics in PRIDE-Star are reported in Appendix D.1. The equity curves with standard deviation shades on the 4 financial markets are included in Appendix D.4. We plot the PRIDE-Star, performance profile and rank comparison of each financial market individually in Appendix D.5, D.6, D.7, respectively. Furthermore, we include ablation studies on the effectiveness of each component in AlphaMix+ in Appendix D.2 and hyperparameter sensitivity experiments in Appendix D.3.

Hosting, Maintenance, Licensing. The PRUDEX-Compass datasets are hosted on Google Drive. The source code are publicly available at https://anonymous.4open.science/r/PRUDEX-Compass-948C. The authors will provide important bug fixes to the community as commits to the GitHub repository. There will be summary of changes to the code and the datasets in the README web page of the GitHub repository. In the unlikely case that the Google Drive link stops operating, we will migrate the dataset to another hosting and announce the new links in the GitHub repository. The provided source code and dataset are copyrighted by us and under the MIT license[12]. Users have the permission to reuse the codes for any purpose.

[12] https://opensource.org/licenses/MIT

References

Chirag Agarwal, Eshika Saxena, Satyapriya Krishna, Martin Pawelczyk, Nari Johnson, Isha Puri, Marinka Zitnik, and Himabindu Lakkaraju. Openxai: Towards a transparent evaluation of model explanations. *arXiv preprint arXiv:2206.11104*, 2022.

Rishabh Agarwal, Max Schwarzer, Pablo Samuel Castro, Aaron C Courville, and Marc Bellemare. Deep reinforcement learning at the edge of the statistical precipice. In *Advances in Neural Information Processing Systems*, 2021.

Bo An, Shuo Sun, and Rundong Wang. Deep reinforcement learning for quantitative trading: Challenges and opportunities. *IEEE Intelligent Systems*, 37(2):23–26, 2022.

Peter Auer, Nicolo Cesa-Bianchi, and Paul Fischer. Finite-time analysis of the multiarmed bandit problem. *Machine learning*, 47(2):235–256, 2002.

Terje Aven. On the meaning of a black swan in a risk context. *Safety Science*, 57, 2013.

Umang Bhatt, Alice Xiang, Shubham Sharma, Adrian Weller, Ankur Taly, Yunhan Jia, Joydeep Ghosh, Ruchir Puri, José MF Moura, and Peter Eckersley. Explainable machine learning in deployment. In *ACM Conference on Fairness, Accountability, and Transparency*, 2020.

Lars Brink and Bruce McCarl. The tradeoff between expected return and risk among cornbelt farmers. *American Journal of Agricultural Economics*, 60(2), 1978.

Greg Brockman, Vicki Cheung, Ludwig Pettersson, Jonas Schneider, John Schulman, Jie Tang, and Wojciech Zaremba. Openai gym. *arXiv preprint arXiv:1606.01540*, 2016.

John Y Campbell, Andrew W Lo, A Craig MacKinlay, and Robert F Whitelaw. The econometrics of financial markets. *Macroeconomic Dynamics*, 2(4), 1998.

Ernest P Chan. *Quantitative trading: how to build your own algorithmic trading business.* Wiley, 2021.

Stephanie CY Chan, Samuel Fishman, Anoop Korattikara, John Canny, and Sergio Guadarrama. Measuring the reliability of reinforcement learning algorithms. In *International Conference on Learning Representations*, 2019.

Richard Y Chen, Szymon Sidor, Pieter Abbeel, and John Schulman. Ucb exploration via q-ensembles. *arXiv preprint arXiv:1706.01502*, 2017.

Cédric Colas, Olivier Sigaud, and Pierre-Yves Oudeyer. How many random seeds? statistical power analysis in deep reinforcement learning experiments. *arXiv preprint arXiv:1806.08295*, 2018.

Marcos Lopez De Prado. *Advances in financial machine learning.* John Wiley & Sons, 2018.

Giorgio De Santis et al. Stock returns and volatility in emerging financial markets. *Journal of International Money and Finance*, 16(4), 1997.

Jonas Degrave, Federico Felici, Jonas Buchli, Michael Neunert, Brendan Tracey, Francesco Carpanese, Timo Ewalds, Roland Hafner, Abbas Abdolmaleki, Diego de Las Casas, et al. Magnetic control of tokamak plasmas through deep reinforcement learning. *Nature*, 602(7897), 2022.

Yue Deng, Feng Bao, Youyong Kong, Zhiquan Ren, and Qionghai Dai. Deep direct reinforcement learning for financial signal representation and trading. *IEEE Transactions on Neural Networks and Learning Systems*, 28(3), 2016.

Yi Ding, Weiqing Liu, Jiang Bian, Daoqiang Zhang, and Tie-Yan Liu. Investor-imitator: A framework for trading knowledge extraction. In *ACM SIGKDD International Conference on Knowledge Discovery & Data Mining*, 2018.

Elizabeth D Dolan and Jorge J Moré. Benchmarking optimization software with performance profiles. *Mathematical Programming*, 91(2), 2002.

B Efron. Bootstrap methods: Another look at the jackknife. *The Annals of Statistics*, 7(1), 1979.

James Elder and Steven Zucker. The effect of contour closure on the rapid discrimination of two-dimensional shapes. *Vision Research*, 33(7), 1993.

James H Elder and Steven W Zucker. Evidence for boundary-specific grouping. *Vision Research*, 38(1), 1998.

Emmanuel N Emenyonu and Sidney J Gray. International accounting harmonization and the major developed stock market countries: an empirical study. *The International Journal of Accounting*, 31(3), 1996.

Yuchen Fang, Kan Ren, Weiqing Liu, Dong Zhou, Weinan Zhang, Jiang Bian, Yong Yu, and Tie-Yan Liu. Universal trading for order execution with oracle policy distillation. In *AAAI Conference on Artificial Intelligence*, 2021.

Alhussein Fawzi, Matej Balog, Aja Huang, Thomas Hubert, Bernardino Romera-Paredes, Mohammadamin Barekatain, Alexander Novikov, Francisco J R Ruiz, Julian Schrittwieser, Grzegorz Swirszcz, et al. Discovering faster matrix multiplication algorithms with reinforcement learning. *Nature*, 610(7930):47–53, 2022.

Franco and Leah. Risk-adjusted performance. *Journal of Portfolio Management*, 23(2), 1997.

Johannes Fuchs, Petra Isenberg, Anastasia Bezerianos, Fabian Fischer, and Enrico Bertini. The influence of contour on similarity perception of star glyphs. *IEEE Transactions on Visualization and Computer Graphics*, 20(12), 2014.

Nicolae Gârleanu and Lasse Heje Pedersen. Dynamic trading with predictable returns and transaction costs. *The Journal of Finance*, 68(6), 2013.

Timnit Gebru, Jamie Morgenstern, Briana Vecchione, Jennifer Wortman Vaughan, Hanna Wallach, Hal Daumé Iii, and Kate Crawford. Datasheets for datasets. *Communications of the ACM*, 64(12), 2021.

Amit Goyal and Pedro Santa, Clara. Idiosyncratic risk matters! *The Journal of Finance*, 58(3), 2003.

Piyush Gupta, Nikaash Puri, Sukriti Verma, Dhruv Kayastha, Shripad Deshmukh, Balaji Krishnamurthy, and Sameer Singh. Explain your move: understanding agent actions using specific and relevant feature attribution. In *International Conference on Learning Representations*, 2020.

Tuomas Haarnoja, Aurick Zhou, Pieter Abbeel, and Sergey Levine. Soft actor-critic: Off-policy maximum entropy deep reinforcement learning with a stochastic actor. In *International Conference on Machine Learning*, 2018.

Charles R Harris, K Jarrod Millman, Stéfan J Van Der Walt, Ralf Gommers, Pauli Virtanen, David Cournapeau, Eric Wieser, Julian Taylor, Sebastian Berg, Nathaniel J Smith, et al. Array programming with numpy. *Nature*, 585(7825), 2020.

Conor F Hayes, Roxana Rădulescu, Eugenio Bargiacchi, Johan Källström, Matthew Macfarlane, Mathieu Reymond, Timothy Verstraeten, Luisa M Zintgraf, Richard Dazeley, Fredrik Heintz, et al. A practical guide to multi-objective reinforcement learning and planning. *Autonomous Agents and Multi-Agent Systems*, 36 (1), 2022.

Peter Henderson, Riashat Islam, Philip Bachman, Joelle Pineau, Doina Precup, and David Meger. Deep reinforcement learning that matters. In *AAAI conference on artificial intelligence*, 2018.

Geoffrey Hinton, Oriol Vinyals, Jeff Dean, et al. Distilling the knowledge in a neural network. *arXiv preprint arXiv:1503.02531*, 2015.

Timothy Hospedales, Antreas Antoniou, Paul Micaelli, and Amos Storkey. Meta-learning in neural networks: A survey. *IEEE transactions on pattern analysis and machine intelligence*, 44(9):5149–5169, 2021.

Zhengyao Jiang, Dixing Xu, and Jinjun Liang. A deep reinforcement learning framework for the financial portfolio management problem. *arXiv preprint arXiv:1706.10059*, 2017.

Scott Jordan, Yash Chandak, Daniel Cohen, Mengxue Zhang, and Philip Thomas. Evaluating the performance of reinforcement learning algorithms. In *International Conference on Machine Learning*, 2020.

Lou Jost. Entropy and diversity. *Oikos*, 113(2), 2006.

Jonathan M Karpoff. The relation between price changes and trading volume: A survey. *Journal of Financial and Quantitative Analysis*, 22(1):109–126, 1987.

Guolin Ke, Qi Meng, Thomas Finley, Taifeng Wang, Wei Chen, Weidong Ma, Qiwei Ye, and Tie-Yan Liu. Lightgbm: A highly efficient gradient boosting decision tree. In *Advances in Neural Information Processing Systems*, 2017.

Ajay Khorana, Henri Servaes, and Lei Wedge. Portfolio manager ownership and fund performance. *Journal of financial economics*, 85(1):179–204, 2007.

Ulrich Kirchner and Caroline Zunckel. Measuring portfolio diversification. *arXiv preprint arXiv:1102.4722*, 2011.

Aviral Kumar, Abhishek Gupta, and Sergey Levine. Discor: Corrective feedback in reinforcement learning via distribution correction. *Advances in Neural Information Processing Systems*, 2020.

Balaji Lakshminarayanan, Alexander Pritzel, and Charles Blundell. Simple and scalable predictive uncertainty estimation using deep ensembles. *Advances in Neural Information Processing Systems*, 2017.

Mikel Landajuela, Brenden K Petersen, Sookyung Kim, Claudio P Santiago, Ruben Glatt, Nathan Mundhenk, Jacob F Pettit, and Daniel Faissol. Discovering symbolic policies with deep reinforcement learning. In *International Conference on Machine Learning*, 2021.

Chi-Chuan Lee, Chien-Chiang Lee, and Yizhong Wu. The impact of covid-19 pandemic on hospitality stock returns in china. *International Journal of Finance & Economics*, 2021a.

Chien-Chiang Lee, Jun-De Lee, and Chi-Chuan Lee. Stock prices and the efficient market hypothesis: Evidence from a panel stationary test with structural breaks. *Japan and the world economy*, 22(1):49–58, 2010.

Kimin Lee, Michael Laskin, Aravind Srinivas, and Pieter Abbeel. Sunrise: A simple unified framework for ensemble learning in deep reinforcement learning. In *International Conference on Machine Learning*, 2021b.

Siyu Lin and Peter A Beling. An end-to-end optimal trade execution framework based on proximal policy optimization. In *International Joint Conference on Artificial Intelligence*, 2020.

Xiao-Yang Liu, Hongyang Yang, Qian Chen, Runjia Zhang, Liuqing Yang, Bowen Xiao, and Christina Dan Wang. Finrl: A deep reinforcement learning library for automated stock trading in quantitative finance. *arXiv preprint arXiv:2011.09607*, 2020a.

Yang Liu, Qi Liu, Hongke Zhao, Zhen Pan, and Chuanren Liu. Adaptive quantitative trading: An imitative deep reinforcement learning approach. In *AAAI Conference on Artificial Intelligence*, 2020b.

Scott M Lundberg and Su-In Lee. A unified approach to interpreting model predictions. *Advances in neural information processing systems*, 30, 2017.

Malik Magdon and Amir F Atiya. Maximum drawdown. *Risk Magazine*, 17(10), 2004.

Burton G Malkiel. The efficient market hypothesis and its critics. *Journal of Economic Perspectives*, 17(1): 59–82, 2003.

Velayoudoum Marimoutou, Bechir Raggad, and Abdelwahed Trabelsi. Extreme value theory and value at risk: application to oil market. *Energy Economics*, 31(4), 2009.

Mieszko Mazur, Man Dang, and Miguel Vega. Covid-19 and the march 2020 stock market crash. evidence from s&p1500. *Finance research letters*, 38:101690, 2021.

Margaret Mitchell, Simone Wu, Andrew Zaldivar, Parker Barnes, Lucy Vasserman, Ben Hutchinson, Elena Spitzer, Inioluwa Deborah Raji, and Timnit Gebru. Model cards for model reporting. In *ACM Conference on Fairness, Accountability, and Transparency*, 2019.

Volodymyr Mnih, Adria Puigdomenech Badia, Mehdi Mirza, Alex Graves, Timothy Lillicrap, Tim Harley, David Silver, and Koray Kavukcuoglu. Asynchronous methods for deep reinforcement learning. In *International Conference on Machine Learning*, 2016.

John Moody and Matthew Saffell. Reinforcement learning for trading. In *Advances in Neural Information Processing Systems*, 1998.

Tobias J Moskowitz, Yao Hua Ooi, and Lasse Heje Pedersen. Time series momentum. *Journal of Financial Economics*, 104(2), 2012.

Martin Mundt, Steven Lang, Quentin Delfosse, and Kristian Kersting. Cleva-compass: A continual learning evaluation assessment compass to promote research transparency and comparability. In *International Conference on Learning Representations*, 2021.

Ralph Neuneier. Optimal asset allocation using adaptive dynamic programming. In *Advances in Neural Information Processing Systems*, 1996.

Ian Osband, Charles Blundell, Alexander Pritzel, and Benjamin Van Roy. Deep exploration via bootstrapped dqn. *Advances in Neural Information Processing Systems*, 2016.

Sinno Jialin Pan and Qiang Yang. A survey on transfer learning. *IEEE Transactions on Knowledge and Data Engineering*, 22(10), 2009.

Jack Parker, Aldo Pacchiano, Krzysztof M Choromanski, and Stephen J Roberts. Effective diversity in population based reinforcement learning. *Advances in Neural Information Processing Systems*, 2020.

Julien Pénasse. Understanding alpha decay. *Management Science*, 2022.

Joelle Pineau, Philippe Vincent-Lamarre, Koustuv Sinha, Vincent Larivière, Alina Beygelzimer, Florence d'Alché Buc, Emily Fox, and Hugo Larochelle. Improving reproducibility in machine learning research: A report from the neurips 2019 reproducibility program. *Journal of Machine Learning Research*, 22, 2021.

Fábio Pinto, Marco OP Sampaio, and Pedro Bizarro. Automatic model monitoring for data streams. *arXiv preprint arXiv:1908.04240*, 2019.

Fazlollah M Reza. *An introduction to information theory*. Courier Corporation, 1994.

Marco Tulio Ribeiro, Sameer Singh, and Carlos Guestrin. "why should i trust you?" explaining the predictions of any classifier. In *ACM SIGKDD International Conference on Knowledge Discovery and Data Mining*, 2016.

Ramit Sawhney, Shivam Agarwal, Arnav Wadhwa, and Rajiv Ratn Shah. Spatiotemporal hypergraph convolution network for stock movement forecasting. In *2020 IEEE International Conference on Data Mining (ICDM)*, pp. 482–491, 2020.

Ramit Sawhney, Shivam Agarwal, Arnav Wadhwa, and Rajiv Shah. Exploring the scale-free nature of stock markets: Hyperbolic graph learning for algorithmic trading. In *Acm Web Conference*, 2021.

John Schulman, Filip Wolski, Prafulla Dhariwal, Alec Radford, and Oleg Klimov. Proximal policy optimization algorithms. *arXiv preprint arXiv:1707.06347*, 2017.

Claude Elwood Shannon. A mathematical theory of communication. *The Bell system technical journal*, 27 (3):379–423, 1948.

William F Sharpe. The sharpe ratio. *Journal of Portfolio Management*, 1998.

Wenjie Shi, Gao Huang, Shiji Song, Zhuoyuan Wang, Tingyu Lin, and Cheng Wu. Self-supervised discovering of interpretable features for reinforcement learning. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 2020.

Robert J Shiller. *Market volatility*. MIT press, 1992.

Andrew Silva, Matthew Gombolay, Taylor Killian, Ivan Jimenez, and Sung-Hyun Son. Optimization methods for interpretable differentiable decision trees applied to reinforcement learning. In *International Conference on Artificial Intelligence and Statistics*, 2020.

David Silver, Guy Lever, Nicolas Heess, Thomas Degris, Daan Wierstra, and Martin Riedmiller. Deterministic policy gradient algorithms. In *International Conference on Machine Learning*, pp. 387–395, 2014.

David Silver, Julian Schrittwieser, Karen Simonyan, Ioannis Antonoglou, Aja Huang, Arthur Guez, Thomas Hubert, Lucas Baker, Matthew Lai, Adrian Bolton, et al. Mastering the game of go without human knowledge. *Nature*, 550(7676), 2017.

Thomas Spooner and Rahul Savani. Robust market making via adversarial reinforcement learning. In *International Joint Conference on Artificial Intelligence*, 2020.

Thomas Spooner, John Fearnley, Rahul Savani, and Andreas Koukorinis. Market making via reinforcement learning. In *International Conference on Autonomous Agents and MultiAgent Systems*, 2018.

Shuo Sun, Rundong Wang, and Bo An. Reinforcement learning for quantitative trading. *arXiv preprint arXiv:2109.13851*, 2021a.

Shuo Sun, Rundong Wang, Xu He, Junlei Zhu, Jian Li, and Bo An. Deepscalper: A risk-aware deep reinforcement learning framework for intraday trading with micro-level market embedding. *arXiv preprint arXiv:2201.09058*, 2021b.

Shuo Sun, Wanqi Xue, Rundong Wang, Xu He, Junlei Zhu, Jian Li, and Bo An. Deepscalper: A risk-aware reinforcement learning framework to capture fleeting intraday trading opportunities. In *ACM International Conference on Information & Knowledge Management*, 2022.

Jun Tu and Guofu Zhou. Markowitz meets talmud: A combination of sophisticated and naive diversification strategies. *Journal of Financial Economics*, 99(1):204–215, 2011.

Laurens Vander and Geoffrey Hinton. Visualizing data using t-sne. *Journal of Machine Learning Research*, 9 (11), 2008.

Oriol Vinyals, Igor Babuschkin, Wojciech M Czarnecki, Michaël Mathieu, Andrew Dudzik, Junyoung Chung, David H Choi, Richard Powell, Timo Ewalds, Petko Georgiev, et al. Grandmaster level in starcraft ii using multi-agent reinforcement learning. *Nature*, 575(7782), 2019.

Rundong Wang, Hongxin Wei, Bo An, Zhouyan Feng, and Jun Yao. Commission fee is not enough: A hierarchical reinforced framework for portfolio management. In *AAAI Conference on Artificial Intelligence*, 2021a.

Wenhui Wang, Hangbo Bao, Li Dong, Johan Bjorck, Zhiliang Peng, Qiang Liu, Kriti Aggarwal, Owais Khan Mohammed, Saksham Singhal, Subhojit Som, et al. Image as a foreign language: Beit pretraining for all vision and vision-language tasks. *arXiv preprint arXiv:2208.10442*, 2022.

Zhicheng Wang, Biwei Huang, Shikui Tu, Kun Zhang, and Lei Xu. Deeptrader: A deep reinforcement learning approach to risk-return balanced portfolio management with market conditions embedding. In *AAAI Conference on Artificial Intelligence*, 2021b.

Yeming Wen, Dustin Tran, and Jimmy Ba. Batchensemble: an alternative approach to efficient ensemble and lifelong learning. In *International Conference on Learning Representations*, 2019.

Florian Wenzel, Jasper Snoek, Dustin Tran, and Rodolphe Jenatton. Hyperparameter ensembles for robustness and uncertainty quantification. *Advances in Neural Information Processing Systems*, 2020.

Yumo Xu and Shay B Cohen. Stock movement prediction from tweets and historical prices. In *Annual Meeting of the Association for Computational Linguistics*, 2018.

Yunan Ye, Hengzhi Pei, Boxin Wang, Pin-Yu Chen, Yada Zhu, Ju Xiao, and Bo Li. Reinforcement-learning based portfolio management with augmented asset movement prediction states. In *AAAI Conference on Artificial Intelligence*, 2020.

Jaemin Yoo, Yejun Soun, Yong-chan Park, and U Kang. Accurate multivariate stock movement prediction via data-axis transformer with multi-level contexts. In *ACM SIGKDD Conference on Knowledge Discovery & Data Mining*, 2021.

Dong Yu, Kaisheng Yao, Hang Su, Gang Li, and Frank Seide. Kl-divergence regularized deep neural network adaptation for improved large vocabulary speech recognition. In *IEEE International Conference on Acoustics, Speech and Signal Processing*, 2013.

Pengqian Yu, Joon Sern Lee, Ilya Kulyatin, Zekun Shi, and Sakyasingha Dasgupta. Model-based deep reinforcement learning for dynamic portfolio optimization. *arXiv preprint arXiv:1901.08740*, 2019.

Yuyu Yuan, Wen Wen, and Jincui Yang. Using data augmentation based reinforcement learning for daily stock trading. *Electronics*, 9(9), 2020.

Zihao Zhang, Stefan Zohren, and Stephen Roberts. Deep reinforcement learning for trading. *The Journal of Financial Data Science*, 2(2), 2020.

Brian D Ziebart. *Modeling purposeful adaptive behavior with the principle of maximum causal entropy.* Carnegie Mellon University, 2010.

Appendix

A PRUDEX-Compass

A.1 PRUDEX-Compass Measure

We elaborate 16 measures in Table 1 with mathematical definitions and detailed descriptions.

Profit measure contains metrics to evaluate FinRL methods' ability to gain market capital. Total return (TR) is the percent change of net value over time horizon h. The formal definition is $TR = (n_{t+h} - n_t)/n_t$, where n_t is the corresponding value at time t.

Alpha Decay indicates the loss in the investment decision making ability of FinRL methods over time due to distribution shift in financial markets. In finance, information coefficient (IC) across time is widely-used to measure alpha decay (Pénasse, 2022).

Equity Curve is a graphical representation of the value changes of trading strategies over time. An equity curve with a consistently positive slope typically indicates that the trading strategies of the account are profitable. In RL settings, we usually plot equity curves with mean and standard deviation of multiple random seeds.

Risk includes a class of metrics to assess the risk level of FinRL methods.

- **Volatility (Vol)** is the variance of the return vector $\mathbf{r}$. It is widely used to measure the uncertainty of return rate and reflects the risk level of strategies. The definition is $Vol = \sigma[\mathbf{r}]$
- **Maximum drawdown (MDD)** measures the largest decline from the peak in the whole trading period to show the worst case. The formal definition is $MDD = \max_{\tau \in (0,t)}[\max_{t \in (0,\tau)} \frac{n_t - n_\tau}{n_t}]$
- **Downside deviation (DD)** refers to the standard deviation of trade returns that are negative.

Risk-adjusted Profit calculates the potential normalized profit by taking one share of the risk. We define three metrics with different types of risk:

- **Sharpe ratio (SR)** is a risk-adjusted profit measure, which refers to the return per unit of deviation: $SR = \frac{\mathbb{E}[\mathbf{r}]}{\sigma[\mathbf{r}]}$
- **Sortino ratio (SoR)** is a variant of risk-adjusted profit measure, which applies DD as risk measure: $SoR = \frac{\mathbb{E}[\mathbf{r}]}{DD}$
- **Calmar ratio (CR)** is another variant of risk-adjusted profit measure, which applies MDD as risk measure: $CR = \frac{\mathbb{E}[\mathbf{r}]}{MDD}$

Extreme Market. It is necessary to evaluate on extreme market conditions with black swan events to show the reliability of FinRL methods .By analyzing the trading behaviors during extreme markets, we can understand their cons and pros and further design better FinRL methods. There are a few potential testbed such as COVID-19 pandemic, financial crisis, government regulation and war.

Countries. Financial markets in different countries have different trading patterns, where markets in developed countries is more "effcient" with high proportion of institutional investors and markets in developing countries is more noisy with high personal investors. It is necessary to evaluate FinRL methods on multiple mainstream financial markets in different countries, such as US, Europe and China, to evaluate universality.

Asset Type. A financial asset is a liquid asset that derives its value from any contractual claim. Different asset types have different liquidity, trading rules and value models. It is necessary to evaluate FinRL methods on various financial asset types to evaluate universality.

Time Scale. We can evaluate FinRL methods on multiple trading scenarios with financial data on different time-scale (both coarse-grained and fine-grained). For instance, second-level data can be used for high

frequency trading; minute-level data is suitable for intraday trading; day-level data can be applied for long-term trend trading.

Rolling Window. Due to the remarkable distribution shift in financial markets, researchers need to train and evaluate FinRL methods in a rolling time window, which means retrain or fine-tune RL models periodically to fit on current market status. Backtest with rolling window can evaluate the reliability of FinRL.

t-SNE is a statistical method for visualizing high-dimensional data by giving each datapoint a location in a two-dimensional map. First, t-SNE constructs a probability distribution over pairs of high-dimensional objects where similar objects are assigned a higher probability. Second, t-SNE defines a similar probability distribution over the points in the low-dimensional map, and it minimizes the KL divergence between the two distributions with respect to the locations of the points in the map. In FinRL, we use t-SNE to visualize financial datasets to show the relative position of them.

Entropy. (Shannon, 1948) is applied in finance to measure the amount of information give by observing the financial market. In a portfolio, it is defined as $H(\omega) = -exp\,(\sum_{i=1}^{n} \omega_i \, log\, \omega_i)$, where $\omega = (\omega_1, \omega_2, ..., \omega_n)$ is a portfolio among N financial assets. This measure reach a minimum value 1 if a portfolio is fully concentrated in one single asset and a maximum equal to N that representation the equally weighted portfolio.

Correlation. As entropy ignore the correlation between different financial assets, effective number of bets (ENB) is proposed to remove the correlation while calculating entropy. We first define diversification distribution as $p_i(\omega) = \omega_{F_i}^2 \lambda_i^2 / \sum_{i=1}^{n} \omega_{F_i}^2 \lambda_i^2$. We formulate the covariance matrix of N assets Σ as $E'\Sigma E = \lambda$ where λ is a diagonal matrix,λ_i is the element of the diagonal matrix and $\omega_f = E^{-1}\omega$ where ω is the our original portfolios' weights. The effective number of bets is defined as: $ENB(\omega) = -exp\,(\sum_{i=1}^{n} p_i(\omega)\, log\, p_i(\omega))$, where $p_i(\omega)$ is the ith diversification distribution for the portfolios' weights ω.

Diversity Heatmap is a visualization tool to demonstrate the diversity of investment decisions among different financial assets with heatmap (Harris et al., 2020). The x-axis refers to the relative weight of each asset in the portfolio. The y-axis includes the results of different FinRL algorithms.

Performance Profile reports the score distribution of all runs across the 4 financial markets that are statistically unbiased, more robust to outliers and require fewer runs for lower uncertainty compared to point estimates such as mean. Performance profiles proposed herein visualize the empirical tail distribution function of a random score (higher curve is better), with point-wise confidence bands based on stratified bootstrap (Efron, 1979). A score distribution shows the fraction of runs above a certain normalized score that is an unbiased estimator of the underlying performance distribution.

Variability refers the variance of performance across different random seeds in RL. As a high stake domain, it is important to test the variability, which is closely relevant to reliability.

Rank Comparison

In the rank distribution plot, the ith column shows the probability that a given method is assigned rank i in the corresponding metrics, which provides a indication on the overall rank of FinRL methods.

A.2 Creating a PRUDEX-Compass

To make the PRUDEX-Compass as accessible as possible and disseminate in a convenient way, we provide two options for practical use.

- We provide a **LaTeX template** for PRUDEX-Compass, making use of the TikZ library to draw the compass with LaTeX. We envision that such a template makes it easy for other authors to include a compass into their future research, where they can adapt the naming and values of the entries respectively.

- We further provide a **Python script** to generate the PRUDEX-Compass. In fact, because the use of drawing in LaTeX with TikZ may be unintuitive for some, we have written a Python script that automatically fills above LaTeX template, so that it can later simply be included into a LaTeX

document. The Python script takes a path to a JSON file that needs to be filled by the user. There is a default JSON file that is easy to adopt.

A.3 Computing Scores for PRUDEX-Compass Axes

We introduce how the value of each axe for each FinRL method is computed in this subsection. The basic principle is to propose a distinguishable and robust way to show the performance difference of FinRL methods across multiple evaluation measures in terms of each axe. Generally speaking, we normalize the performance of different measures on the 6 axes to a score from 0 to 100. We mark market average strategy (evenly invest on all assets) as 50. All scores are calculated with the average of 4 financial markets. We define the metrics value for FinRL methods and market average as m_{rl} and m_{ave}, respectively. For the 4 profit-related metrics (TR, SR, CR, SoR), we normalized them into a score S_{pro} with range $[0, 100]$: $S_{pro} = (m_{rl}/m_{ave} - 0.8) * 250$, where 20% higher profit than market average is scored 100. We clip values lower than 0 and higher than 100 as 0 and 100, respectively. For the 2 risk metrics (Vol, MDD), we normalized them into a score S_{risk} with range $[0, 100]$: $S_{risk} = (1.2 - m_{rl}/m_{ave}) * 250$, where 20% lower risk than market average is scored 100. We clip values lower than 0 and higher than 100 as 0 and 100, respectively.

For universality, we directly use the raw return rate and calcualte the 4 indicators of profitability, we then plot a rank graph and for each measures of profitability, we multiply the probability obtained from the rank matrix and the rankscore(if it's 1st, the score is 100 and if 6th, the score is 0) to get a score for that measure. Then we average the 4 measures together to get the university score for that algorithm. For the 2 diversity metrics (ENT, ENB), we normalized them into a score S_{div}:

$$S_{div} = \begin{cases} m_{rl}/m_{ave} \times 100, & \text{for ENT} \\ m_{rl}/m_{ave} \times 50, & \text{for ENB} \end{cases}$$

where the diversity of uniform policy is scored 100 for ENT and 50 for ENB. For explainability, we set the explainability score 50 for all FinRL methods. For reliability, we use the total return rate score we just normalized using average policy as a indicator and draw a performance profile graph, then we use the area under the curve for each algorithm to calculate the reliability. The constants in the equations (e.g., 20%) are applied to make the plot distinguishable and easy to follow, which does not influence the robustness of axes in PRUDEX-Compass.

B Related Works

FinRL Methods. Recent years have witnessed the successful marriage of reinforcement learning and quantitative trading. Neuneier (1996) made the first attempt to learn trading strategies using Q-learning. Moody & Saffell (1998) proposed a policy-based method, namely recurrent reinforcement learning (RRL), for quantitative trading. However, traditional RL approaches have difficulties in selecting market features and learning good policy in large scale scenarios. To tackle these issues, many deep RL approaches have been proposed to learn market embedding through high dimensional data. Jiang et al. (2017) used DDPG to dynamically optimize cryptocurrency portfolios. Deng et al. (2016) applied fuzzy learning and deep learning to improve financial signal representation. Yu et al. (2019) proposed a model-based RL framework for daily frequency portfolio trading. Liu et al. (2020b) proposed an adaptive DDPG-based framework with imitation learning. A comprehensive survey of FinRL is at (Sun et al., 2021a).

Rigorous Evaluation in RL. There are many prior works focusing on rigorous evaluation in RL. Henderson et al. (2018) highlights various reproducibility issues in RL. Colas et al. (2018) studies the minimum number of random seeds required to report results with statistical significance. Agarwal et al. (2021) recommend for reporting interval estimates of aggregate performance and propose performance profiles for reliable RL evaluation with a handful of runs. Chan et al. (2019) propose metrics to measure the reliability of RL algorithms in terms of their stability during training and their variability and risk in returns across multiple episodes. Jordan et al. (2020) propose a game-theoretic evaluation procedure for "complete" algorithms that do not require any hyperparameter tuning and recemmend evaluating between 1000 to 10000 runs per task to detect statstically significant results.

C Experiment Setup

C.1 Training Setup

Table 4: Hyperparameters of AlphaMix+

Hyperparameter	**Value**	**Hyperparameter**	**Value**
Replay buffer size	10000	Initial step	10000
Layer(MLP)	(128,128)	Stacked frame	3
Evaluation episodes	10	Optimizer	Adam
Temperature	20	Uncertainty	0.5
Actor learning rate	0.0007	Critic learning rate	0.0007
Batch size	256	Action numbers	29(US) 47(China) 22(FX) 9(Crypto)
Discount γ	0.99	Ber_mean	0.5
Non-linear	Sigmoid	Observation	Number of assets $\times$ 11

D Experimental Results

D.1 Result Table

In this subsection, we report detailed results of 8 metrics in the four financial markets. Since we apply 1 year rolling window during training, each financial market has 3 tables for 3 consecutive years.

Table 5: US Stock 2021

Metrics	A2C	PPO	SAC	SARL	DeepTrader	EIIE	IMIT	AlphaMix+
TR(%)	12.4±6.3	13.1±4.4	20.0±10.3	17.3±2.0	17.2±7.4	16.9±1.2	4.0±10.1	20.7±1.8
SR	1.03±0.50	0.94±0.26	1.30±0.57	1.37±0.12	1.22±0.50	1.39±0.08	0.35±0.64	1.64±0.11
CR	0.81±0.34	0.83±0.13	0.91±0.19	1.06±0.03	0.84±0.23	1.06±0.02	0.47±0.61	1.09±0.02
SoR	1.52±0.70	1.38±0.44	1.89±0.87	2.02±0.21	1.81±0.75	2.03±0.12	0.52±0.91	2.36±0.17
MDD(%)	15.0±1.9	15.3±2.5	19.7±4.6	15.6±1.2	19.1±3.9	15.2±0.6	14.6±3.7	17.9±1.4
VOL(%)	0.78±0.06	0.87±0.03	0.91±0.02	0.76±0.02	0.86±0.03	0.73±0.03	1.0±0.12	0.74±0.02
ENT	2.26±0.26	1.82±0.02	1.67±0.02	2.79±0.11	1.82±0.01	2.90±0.26	1.89±0.1	3.25±0.12
ENB	1.34±0.10	1.49±0.01	1.61±0.02	1.14±0.06	1.51±0.02	1.19±0.10	1.73±0.10	1.11±0.03

Table 6: US Stock 2020

Metrics	A2C	PPO	SAC	SARL	DeepTrader	EIIE	IMIT	AlphaMix+
TR(%)	7.46±4.86	18.3±8.4	7.77±21.1	9.23±8.79	10.2±10.5	15.8±16.1	-20.6±9.5	12.7±1.7
SR	0.36±0.12	0.62±0.19	0.37±0.52	0.41±0.21	0.42±0.25	0.55±0.30	-0.28±0.21	0.52±0.04
CR	0.36±0.12	0.54±0.15	0.30±0.48	0.38±0.19	0.42±0.22	0.49±0.22	-0.28±0.22	0.47±0.03
SoR	0.44±0.14	0.76±0.23	0.50±0.63	0.50±0.26	0.56±0.33	0.68±0.38	-0.36±0.27	0.62±0.05
MDD(%)	36.6±2.4	42.2±2.4	42.8±5.3	37.8±3.19	34.9±3.91	38.9±6.69	43.5±6.42	38.2±0.96
VOL(%)	2.25±0.09	2.32±0.03	2.45±0.16	2.26±0.17	2.31±0.09	2.21±0.23	2.9± 0.39	2.16±0.04
ENT	1.96±0.20	1.82±0.02	1.61±0.03	2.07±0.67	1.82±0.02	2.41±0.67	1.85 ±0.21	3.22±0.03
ENB	1.05±0.01	1.05±0.004	1.1±0.003	1.05±0.03	1.05±0.002	1.05±0.05	1.13± 0.04	1.0± 0.006

Table 7: US Stock 2019

Metrics	A2C	PPO	SAC	SARL	DeepTrader	EIIE	IMIT	AlphaMix+
TR(%)	20.5±9.27	21.5±10.1	27.3±9.79	27.7±1.63	22.9±3.51	30.2±8.42	20.6±9.52	25.1±1.42
SR	1.47±0.58	1.53±0.62	1.72±0.54	2.00±0.15	1.60±0.24	2.12±0.27	1.28±0.21	1.98±0.06
CR	1.00±0.06	1.01±0.06	1.05±0.09	1.02±0.05	1.01±0.05	1.06 ±0.05	0.28±0.22	1.03±0.007
SoR	1.96±0.78	2.04±0.83	2.17±0.78	2.52±0.24	2.16±0.43	2.82±0.42	0.36±0.27	2.47±0.09
MDD(%)	18.8±5.95	19.4±6.26	23.4±4.70	24.7±2.63	21.2±2.41	25.2±4.83	43.6±6.42	22.3±0.99
VOL(%)	0.82±0.01	0.83±0.02	0.91±0.05	0.79±0.10	0.84±0.03	0.79±0.11	1.9±0.39	0.73±0.02
ENT	1.83±0.01	1.82±0.01	1.63±0.02	2.08±0.67	1.81±0.01	2.32±0.48	1.89±0.16	3.27±0.03
ENB	1.28±0.01	1.27±0.01	1.38±0.01	1.29±0.21	1.26±0.005	1.15±0.06	1.73±0.10	1.05± 0.01

Table 8: China Stock 2020

Metrics	A2C	PPO	SAC	SARL	DeepTrader	EIIE	IMIT	AlphaMix+
TR(%)	5.52±4.82	6.20±7.57	13.4±20.1	11.4±8.84	12.3±14.2	13.0±3.8	52.6±20.8	14.8±3.30
SR	0.35±0.21	0.40±0.37	0.59±0.68	0.63±0.41	0.62±0.60	0.73± 0.17	2.68±0.83	0.79±0.12
CR	0.25±0.15	0.29±0.27	0.41±0.48	0.42±0.27	0.36±0.39	0.51±0.08	1.18±0.24	0.53±0.06
SoR	0.40±0.24	0.45±0.42	0.71±0.81	0.71±0.46	0.71±0.69	0.80±0.18	4.04±1.2	0.89±0.15
MDD(%)	28.1±3.68	25.3±1.59	29.9±7.38	26.5±5.09	31.5±6.02	27.0±2.41	34.2±9.16	29.1±1.85
VOL(%)	0.74±0.04	0.68±0.004	0.81±0.06	0.68±0.02	0.76±0.01	0.67±0.02	0.66±0.09	0.69±0.01
ENT	1.85±0.42	2.82±0.01	1.10±0.02	2.60±0.17	1.53±0.001	2.39±0.10	1.30 ±0.85	3.12±0.02
ENB	1.12±0.05	1.04±0.01	1.27±0.01	1.04±0.01	1.16±0.004	1.06± 0.01	2.82± 0.85	1.02±0.01

Table 9: China Stock 2019

Metrics	A2C	PPO	SAC	SARL	DeepTrader	EIIE	IMIT	AlphaMix+
TR(%)	31.9±10.6	29.7±8.42	25.4±10.4	32.6±5.78	22.1±13.6	36.2± 7.09	-7.14±0.82	32.2±2.20
SR	1.59±0.46	1.65±0.39	1.13±0.38	1.80±0.24	1.19±0.59	1.77± 0.05	-0.34±0.1	1.79±0.10
CR	0.90±0.16	0.94±0.13	0.79±0.23	1.01±0.07	0.74±0.21	1.04± 0.05	-0.29±0.07	1.01±0.02
SoR	2.32±0.75	2.41±0.63	1.70±0.64	2.63±0.34	1.72±0.91	2.57± 0.15	-0.37± 0.08	2.62±0.14
MDD(%)	31.7±2.85	28.6±2.82	29.8±2.38	28.9±2.38	27.5±4.92	30.5±3.74	20.4± 0.63	28.9±0.90
VOL(%)	0.65±0.02	0.58±0.004	0.74±0.02	0.57±0.01	0.63±0.02	0.64±0.11	0.77± 0.06	0.57±0.01
ENT	1.54±0.01	2.85±0.005	1.02±0.02	2.47±0.17	1.53±0.009	1.97±0.90	1.30±0.85	3.15±0.07
ENB	1.18±0.009	1.05±0.002	1.32±0.009	1.05±0.01	1.18±0.004	1.21 ±0.18	1.19±0.85	1.04±0.01

Table 10: China Stock 2018

Metrics	A2C	PPO	SAC	SARL	DeepTrader	EIIE	IMIT	AlphaMix+
TR(%)	-6.86±11.30	-6.56±3.66	-4.05±10.77	-5.77±4.04	5.67±5.95	-2.27±1.99	-7.14± 0.82	-0.70±1.38
SR	-0.28±0.61	-0.31±0.22	-0.12±0.50	-0.25±0.21	0.37±0.30	-0.05± 0.12	-0.34±0.1	0.03±0.08
CR	-0.14±0.50	-0.25±0.16	-0.06±0.42	-0.20±0.15	0.40±0.32	-0.04±0.11	-0.29±0.07	0.04±0.10
SoR	-0.33±0.78	-0.41±0.26	-0.15±0.75	-0.35±0.29	0.54±0.45	-0.07± 0.17	-0.37±0.08	0.04±0.11
MDD(%)	22.3±5.52	20.5±1.55	25.9±4.95	20.2±3.49	19.1±3.39	17.5±1.52	20.4±0.63	16.1±1.45
VOL(%)	0.67±0.03	0.59±0.01	0.75±0.03	0.61±0.03	0.66±0.02	0.59± 0.03	0.77±0.06	0.57±0.02
ENT	1.54±0.01	2.85±0.007	1.01±0.03	2.41±0.40	1.53±0.007	2.55±0.15	1.30± 0.85	3.12±0.02
ENB	1.31±0.01	1.08±0.005	1.57±0.009	1.11±0.10	1.30±0.009	1.05± 0.01	1.19 ±0.08	1.03±0.003

Table 11: Crypto 2021

Metrics	A2C	PPO	SAC	SARL	DeepTrader	EIIE	IMIT	AlphaMix+
TR(%)	223±346	146±129	377±982	199±195	398±344	146±137	140± 155	291±71
SR	1.38±0.74	1.22±0.56	1.13±0.67	1.41±0.45	1.71±0.45	1.46± 0.42	1.24±0.34	1.87±0.09
CR	1.77±1.02	1.48±0.53	2.18±2.05	1.75±0.74	2.18±0.84	1.44±0.49	1.39±0.58	2.02±0.26
SoR	2.15±1.23	2.13±1.11	3.16±3.31	2.42±1.24	2.97±1.35	2.42± 1.22	2.03± 0.80	3.14±0.56
MDD(%)	77.1±15.7	74.9±10.4	80.1±15.6	79.4±10.0	85.1±8.42	72.5±10.2	71.0± 11.2	85.7±4.14
VOL(%)	7.30±1.91	6.97±0.94	10.94±8.13	7.26±2.31	7.85±2.05	5.22±1.06	5.56± 1.61	6.80±0.84
ENT	1.02±0.31	0.72±0.05	0.47±0.07	1.42±0.25	0.56±0.04	1.53±0.23	0.58±0.23	2.09±0.02
ENB	1.79±0.15	1.94±0.04	1.99±0.05	1.67±0.40	1.97±0.03	1.12±0.05	1.66±0.38	1.47±0.15

Table 12: Crypto 2020

Metrics	A2C	PPO	SAC	SARL	DeepTrader	EIIE	IMIT	AlphaMix+
TR(%)	61.4±58.1	59.1±58.4	16.0±38.4	31.4±12.8	37.9±27.1	30.7± 11.7	55.3± 17.6	33.8±6.16
SR	1.12±0.66	1.12±0.67	0.51±0.50	0.81±0.24	0.85±0.38	0.79±0.17	1.03± 0.08	0.86±0.08
CR	1.06±0.47	1.02±0.45	0.59±0.58	0.86±0.23	0.97±0.42	0.82±0.19	0.73± 0.07	0.87±0.09
SoR	1.58±1.20	1.62±1.22	0.59±0.63	0.89±0.29	1.04±0.54	0.92±0.18	1.49± 0.32	0.94±0.10
MDD(%)	52.9±7.58	52.2±8.03	55.7±2.12	46.6±8.08	50.3±8.04	44.6±3.22	56.6± 4.43	46.5±2.43
VOL(%)	3.86±0.22	3.75±0.17	4.46±0.35	3.66±0.76	4.05±0.32	3.37± 0.36	2.86± 0.53	3.46±0.22
ENT	0.59±0.04	0.59±0.04	0.45±0.02	1.32±0.45	0.60±0.01	1.24±0.52	0.58±0.52	2.17±0.07
ENB	1.05±0.01	1.06±0.03	1.07±0.03	1.01±0.005	1.05±0.01	1.01±0.01	1.01±0.01	1.00±0.001

Table 13: Crypto 2019

Metrics	A2C	PPO	SAC	SARL	DeepTrader	EIIE	IMIT	AlphaMix+
TR(%)	82.8±51.5	85.8±57.1	73.9±33.9	61.0±19.3	39.1±54.5	50.8±13.2	110.6± 17.6	68.3±17.8
SR	1.37±0.50	1.39±0.55	1.27±0.35	1.26±0.26	0.83±0.59	1.15±0.20	2.06± 0.08	1.43±0.22
CR	1.14±0.30	1.14±0.33	1.06±0.24	1.06±0.11	0.73±0.39	0.98±0.10	1.45± 0.07	1.08±0.11
SoR	2.19±0.98	2.22±1.02	2.10±0.65	1.89±0.39	1.30±1.12	1.77±0.28	2.99± 0.32	2.16±0.35
MDD(%)	59.5±9.64	59.9±10.5	59.1±7.74	52.4±6.49	51.3±11.3	49.9±5.80	56.6± 4.43	55.5±3.58
VOL(%)	3.69±0.36	3.69±0.35	3.63±0.27	3.29±0.35	3.46±0.24	3.15±0.30	2.86± 0.53	3.09±0.18
ENT	0.60±0.02	0.62±0.03	0.43±0.03	1.21±0.40	0.59±0.02	1.24±0.52	0.58±0.52	2.15±0.10
ENB	1.15±0.006	1.14±0.01	1.15±0.008	1.06±0.02	1.14±0.01	1.01±0.01	1.01±0.01	1.01±0.01

Table 14: Foreign Exchange 2019

Metrics	A2C	PPO	SAC	SARL	DeepTrader	EIIE	IMIT	AlphaMix+
TR(%)	-0.94±3.14	-1.49±2.68	-1.02±3.11	0.96±0.36	-0.19±2.88	1.42±0.24	-5.53± 0.05	1.22±0.46
SR	-0.22±0.73	-0.34±0.64	-0.21±0.64	0.29±0.09	-0.03±0.66	0.39±0.05	-0.97± 0.01	0.41±0.16
CR	-0.07±0.42	-0.16±0.35	-0.02±0.43	0.22±0.08	0.04±0.46	0.32±0.07	-0.49± 0.01	0.36±0.17
SoR	-0.32±1.05	-0.51±1.00	-0.26±0.86	0.50±0.17	0.06±1.11	0.65±0.07	-1.5± 0.02	0.74±0.31
MDD(%)	7.90±1.85	6.28±1.37	6.94±2.07	4.60±0.47	6.84±1.38	4.65± 0.43	11.17± 0.05	3.77±0.56
VOL(%)	0.27±0.01	0.28±0.01	0.31±0.01	0.22±0.01	0.26±0.01	0.23±0.01	0.25 ±0.01	0.19±0.01
ENT	1.44±0.08	1.37±0.01	0.93±0.04	2.55± 0.10	1.35±0.02	2.23±0.08	3.08±0.01	2.97±0.04
ENB	1.65±0.06	1.73±0.01	2.02±0.04	1.18±0.10	1.71±0.03	1.16±0.06	1.08±0.01	1.18±0.06

Table 15: Foreign Exchange 2018

Metrics	A2C	PPO	SAC	SARL	DeepTrader	EIIE	IMIT	AlphaMix+
TR(%)	-5.43±2.29	-5.25±2.45	-5.61±3.02	-4.52±1.91	-4.99±2.82	-6.15±0.28	-5.53± 0.05	-4.92±0.32
SR	-1.01±0.45	-0.97±0.49	-0.91±0.43	-0.93±0.41	-0.91±0.55	-1.15±0.14	-0.97± 0.01	-1.15±0.10
CR	-0.50±0.14	-0.48±0.16	-0.50±0.18	-0.48±0.19	-0.49±0.21	-0.59±0.04	-0.49± 0.01	-0.57±0.03
SoR	-1.43±0.64	-1.36±0.68	-1.23±0.44	-1.42±0.62	-1.29±0.74	-1.66±0.26	-1.5± 0.02	-1.77±0.16
MDD(%)	10.4±1.67	10.4±1.85	10.7±1.80	9.08±0.96	9.41±2.20	10.6±0.91	11.2± 0.05	8.66±0.14
VOL(%)	0.34±0.02	0.34±0.02	0.37±0.03	0.31±0.02	0.34±0.01	0.34±0.03	0.25± 0.0	0.27±0.01
ENT	1.38±0.03	1.34±0.03	0.94±0.03	2.23±0.37	1.37±0.01	1.55±0.72	3.08± 0.01	2.98±0.03
ENB	1.45±0.01	1.46±0.03	1.65±0.05	1.16±0.09	1.45±0.02	1.39±0.27	1.08±0.01	1.11±0.01

Table 16: Foreign Exchange 2017

Metrics	A2C	PPO	SAC	SARL	DeepTrader	EIIE	IMIT	AlphaMix+
TR(%)	6.93±1.71	6.85±1.44	8.25±3.62	5.81±2.26	5.94±2.50	6.71±2.72	6.42± 0.16	7.16±0.36
SR	1.34±0.29	1.32±0.24	1.41±0.48	1.34±0.57	1.13±0.51	1.26±0.47	0.81± 0.02	1.72±0.13
CR	0.82±0.12	0.81±0.12	0.88±0.17	0.79±0.27	0.77±0.19	0.88±0.11	0.73± 0.01	0.93±0.02
SoR	2.15±0.45	2.14±0.42	2.17±1.01	2.28±0.97	1.74±0.89	1.89±0.80	1.21± 0.03	3.04±0.27
MDD(%)	8.21±1.28	8.20±1.12	9.01±2.45	7.12±1.27	7.46±1.87	7.33±2.08	8.98± 0.12	7.51±0.43
VOL(%)	0.32±0.01	0.32±0.01	0.35±0.03	0.28±0.04	0.33±0.02	0.34±0.08	0.36± 0.01	0.25±0.01
ENT	1.34±0.02	1.35±0.02	0.90±0.03	2.17±0.45	1.37±0.01	1.41±0.57	3.08±0.01	2.98±0.10
ENB	1.58±0.01	1.59±0.04	1.82±0.02	1.29±0.15	1.57±0.02	1.55±0.18	1.05±0.04	1.10±0.04

D.2 Ablation Studies

Models	Ensemble	Weight BB	Diveristy	TR(%)↑	SR↑	CR↑	SoR↑	MDD(%)↓	VOL(%)↓	ENT↑	ENB↑
SAC				7.77	0.37	0.30	0.50	42.8	2.45	1.61	1.10
AlphaMix+	√			10.2	0.46	0.50	0.55	31.6	2.15	3.25	1.01
	√	√		10.1	0.45	0.48	0.54	32.3	2.15	3.28	1.01
	√		√	10.9	0.47	0.52	0.57	32.0	2.19	3.26	1.02
	√	√	√	12.7	0.52	0.47	0.62	38.2	2.16	3.22	1.00

Table 17: US Stock 2020 Ablation

Models	Ensemble	Weight BB	Diveristy	TR(%)↑	SR↑	CR↑	SoR↑	MDD(%)↓	VOL(%)↓	ENT↑	ENB↑
SAC				13.4	0.59	0.41	0.71	29.9	0.81	1.10	1.27
AlphaMix+	√			13.6	0.75	0.77	0.83	19.0	0.69	3.15	1.01
	√	√		11.6	0.66	0.68	0.73	18.7	0.68	3.09	1.02
	√		√	12.0	0.68	0.70	0.76	18.7	0.68	3.20	1.02
	√	√	√	14.8	0.79	0.53	0.89	29.1	0.69	3.12	1.02

Table 18: China Stock 2020 Ablation

Models	Ensemble	Weight BB	Diveristy	TR(%)↑	SR↑	CR↑	SoR↑	MDD(%)↓	VOL(%)↓	ENT↑	ENB↑
SAC				16.0	0.51	0.59	0.59	55.7	4.46	0.45	1.07
AlphaMix+	√			24.4	0.73	0.72	0.76	44.8	3.26	2.08	1.00
	√	√		27.7	0.77	0.78	0.82	46.5	3.42	2.14	1.00
	√		√	32.2	0.83	0.86	0.89	48.0	3.62	2.19	1.00
	√	√	√	33.8	0.86	0.87	0.94	46.5	3.46	2.17	1.00

Table 19: Crypto 2020 Ablation

Models	Ensemble	Weight BB	Diveristy	TR(%)↑	SR↑	CR↑	SoR↑	MDD(%)↓	VOL(%)↓	ENT↑	ENB↑
SAC				-1.02	-0.21	-0.02	-0.26	6.94	0.31	0.93	2.02
AlphaMix+	√			1.06	0.33	0.26	0.58	4.24	0.21	2.98	1.22
	√	√		1.11	0.34	0.27	0.60	4.47	0.22	2.91	1.19
	√		√	1.04	0.33	0.25	0.57	4.34	0.21	3.01	1.19
	√	√	√	1.22	0.41	0.36	0.74	3.77	0.19	2.97	1.18

Table 20: Foreign Exchange 2019 Ablation

D.3 Parameter Analysis: Probing Sensitivity

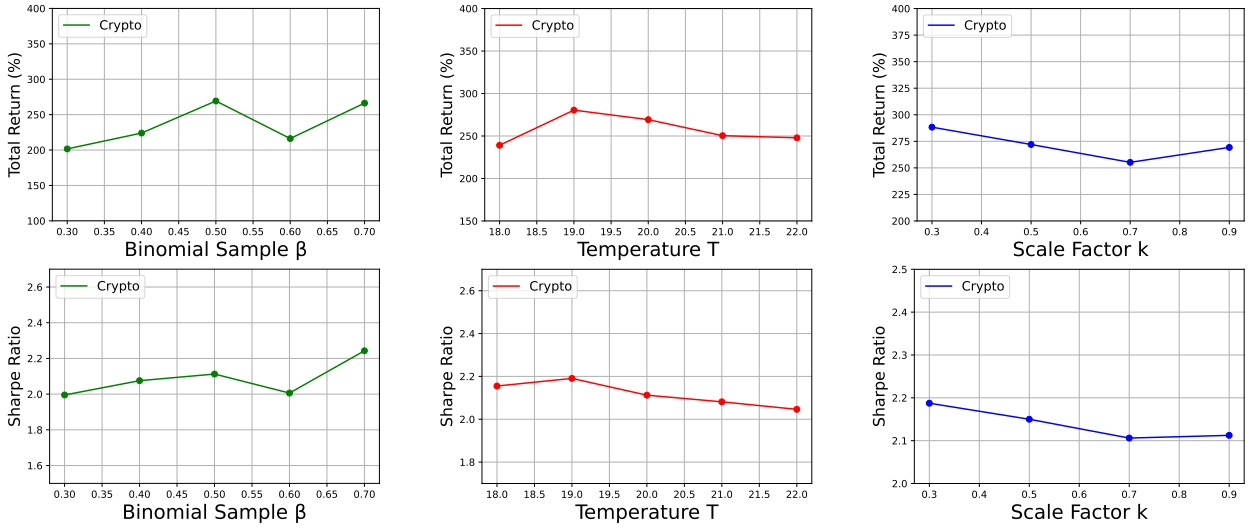


Figure 10: Hyperparameter Sensitivity Experiment Results on Crypto

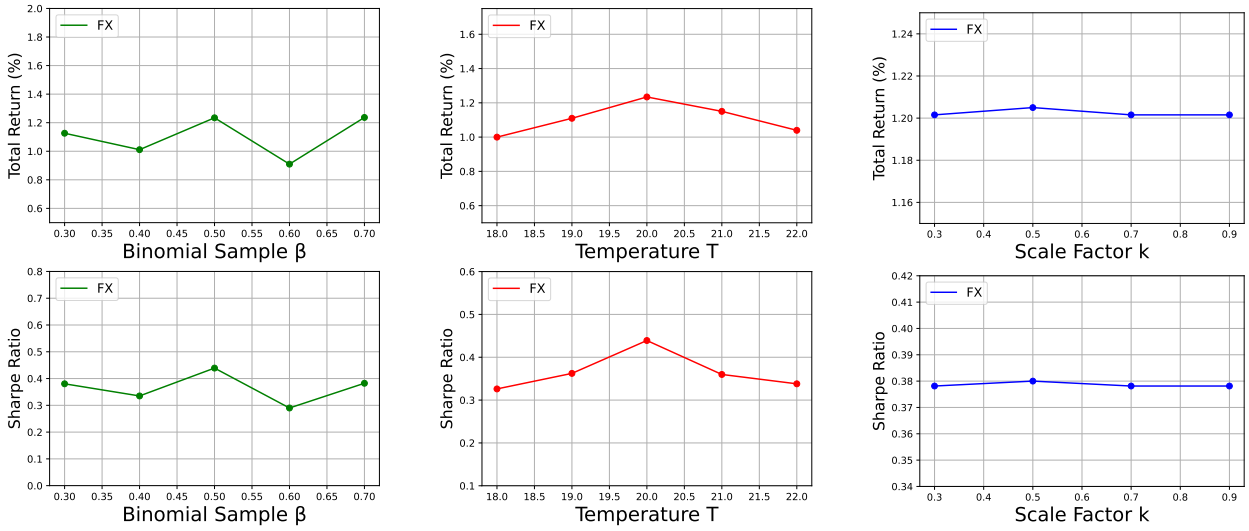
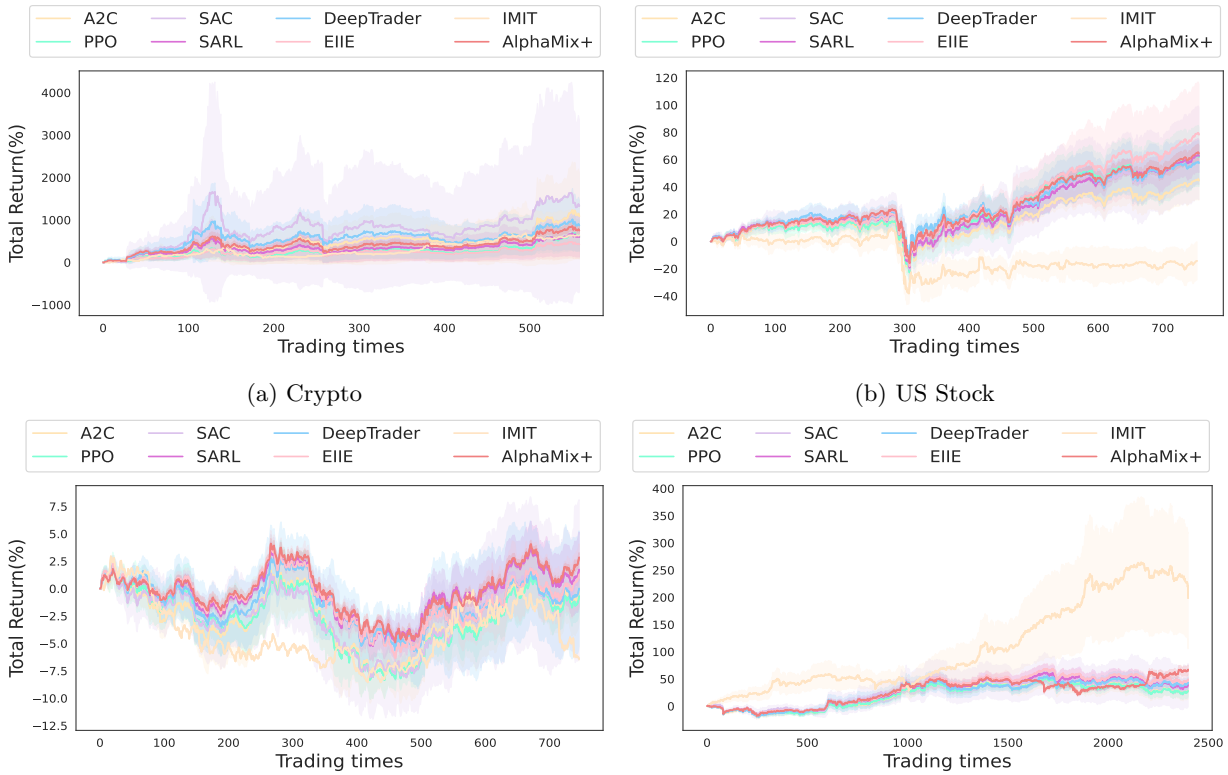


Figure 11: Hyperparameter Sensitivity Experiment Results on FX

D.4 Equity Curve

In subsection, we plot the equity curve of the 4 financial markets. Each line is the mean of 5 individual runs with the shaded area as the standard deviation.

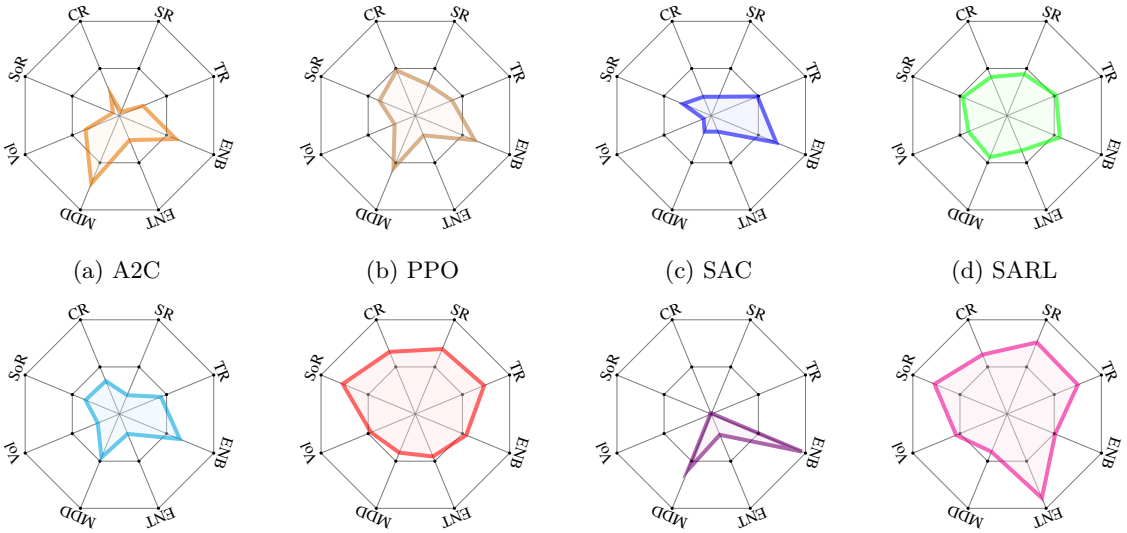


(a) Crypto (b) US Stock

(c) FX (d) China Stock

Figure 12: Equity curve on 4 influential financial markets

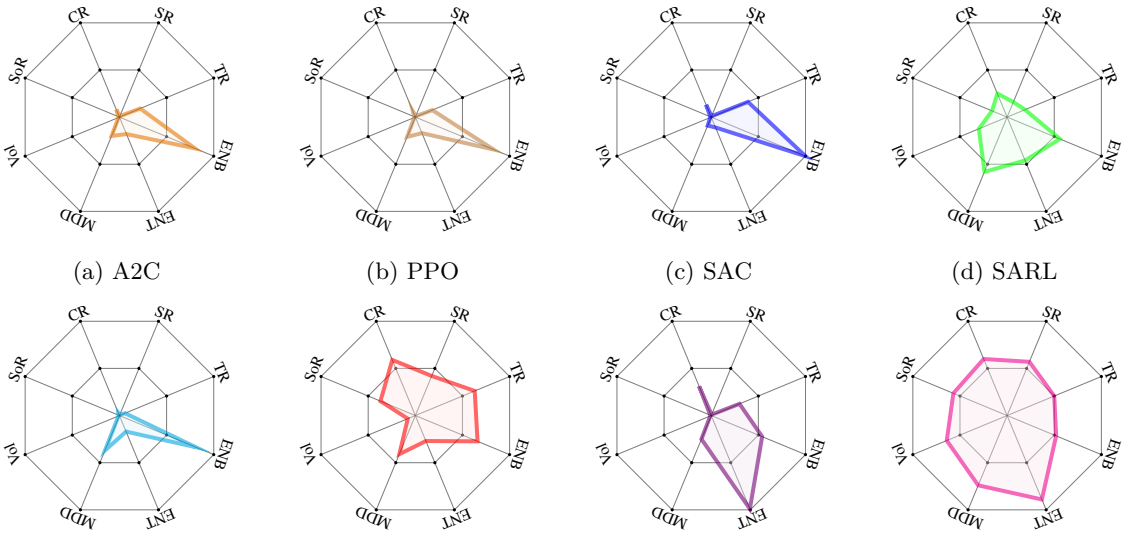
D.5 PRIDE-Star



(a) A2C (b) PPO (c) SAC (d) SARL

(e) DeepTrader (f) EIIE (g) IMIT (h) AlphaMix+

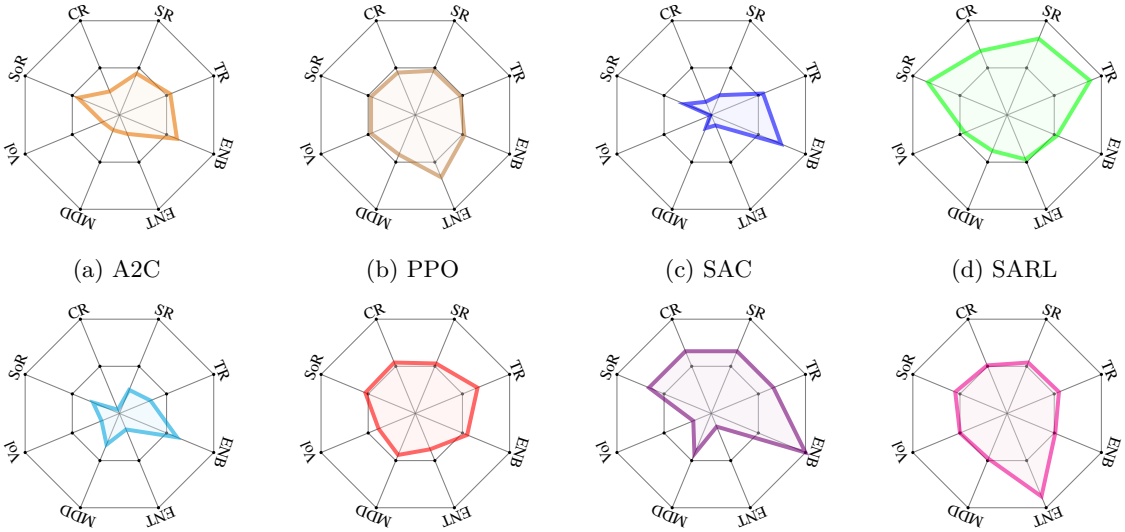
Figure 13: PRIDE-Star on US Stock



(a) A2C (b) PPO (c) SAC (d) SARL

(e) DeepTrader (f) EIIE (g) IMIT (h) AlphaMix+

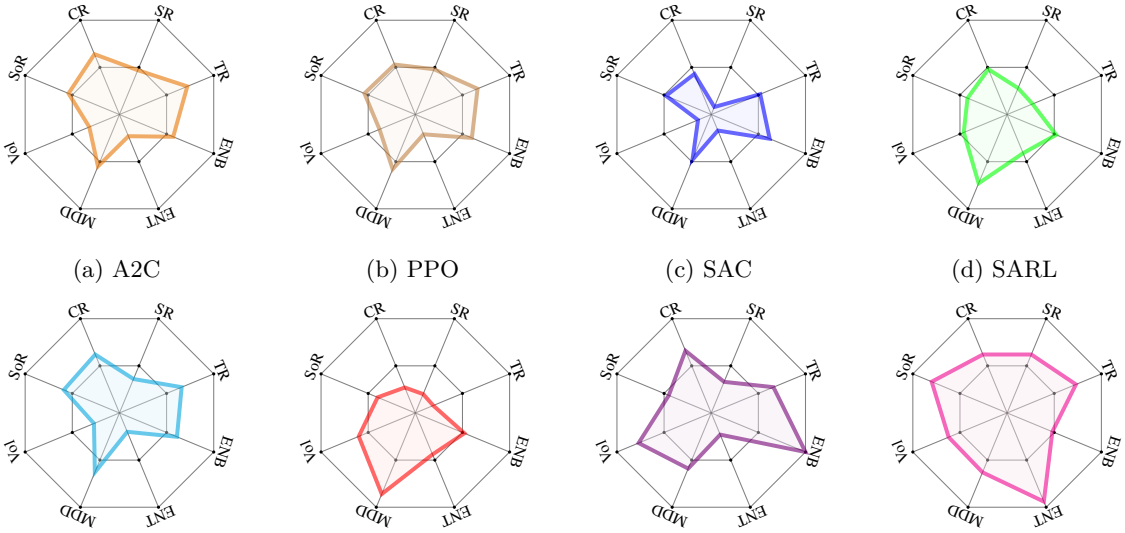
Figure 14: PRIDE-Star on FX



(a) A2C (b) PPO (c) SAC (d) SARL

(e) DeepTrader (f) EIIE (g) IMIT (h) AlphaMix+

Figure 15: PRIDE-Star on China Stock

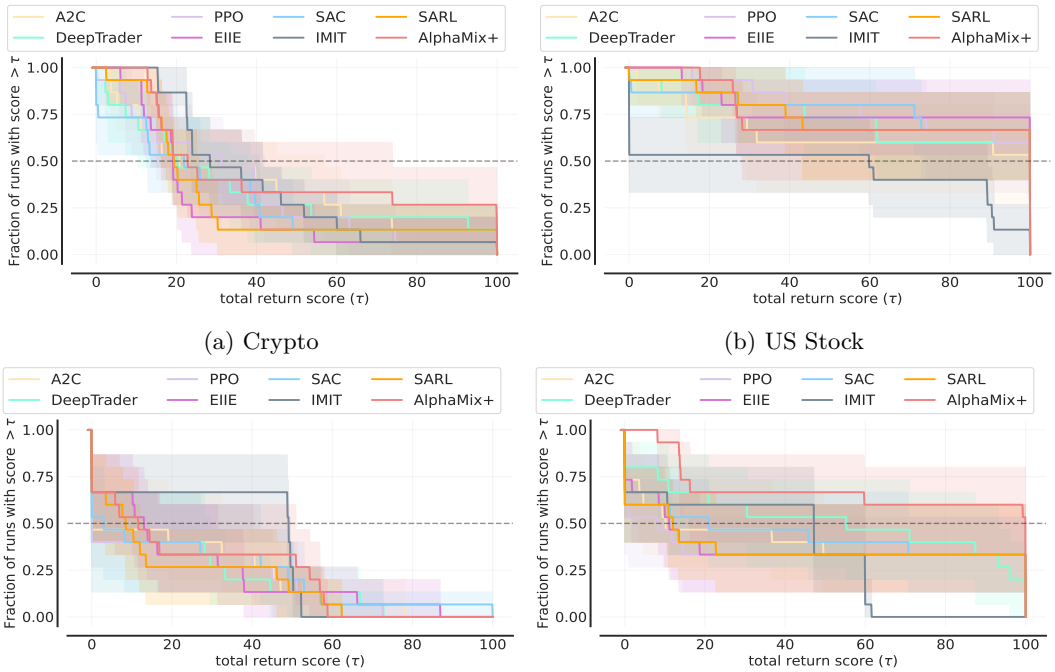


(a) A2C (b) PPO (c) SAC (d) SARL

(e) DeepTrader (f) EIIE (g) IMIT (h) AlphaMix+

Figure 16: PRIDE-Star on Crypto

D.6 Performance Profile

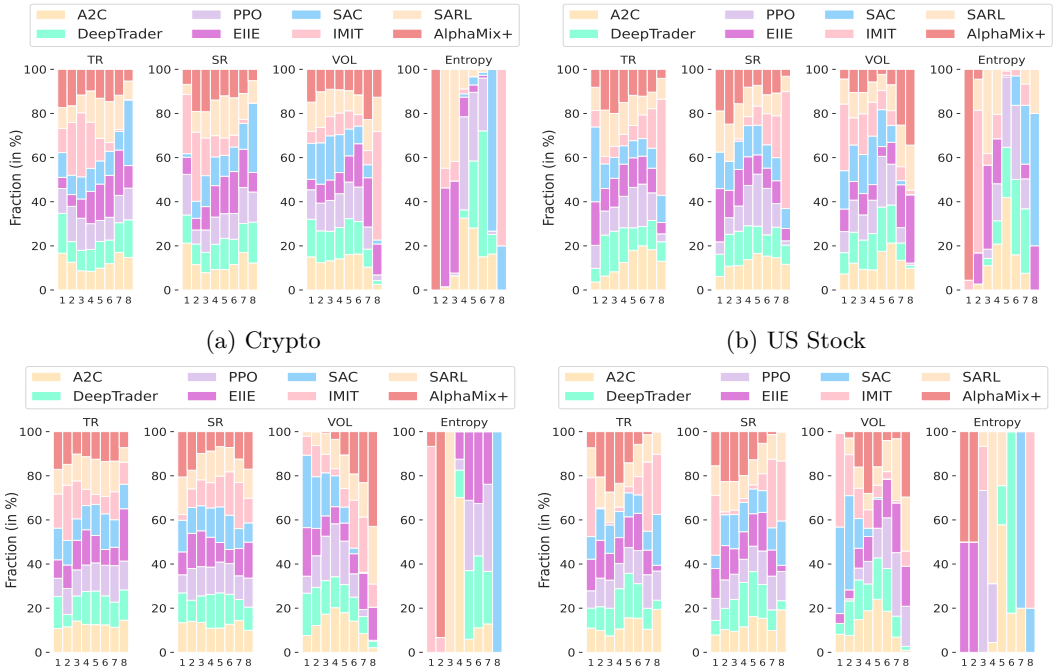


(a) Crypto (b) US Stock

(c) FX (d) China Stock

Figure 17: Performance profile on 4 influential financial markets

D.7 Rank Distribution



(a) Crypto (b) US Stock

(c) FX (d) China Stock

Figure 18: Rank distribution on 4 influential financial markets