C-PLANNING: AN AUTOMATIC CURRICULUM FOR LEARNING GOAL-REACHING TASKS

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ABSTRACT

Goal-conditioned reinforcement learning (RL) can solve tasks in a wide range of domains, including navigation and manipulation, but learning to reach distant goals remains a central challenge to the field. Learning to reach such goals is particularly hard without any offline data, expert demonstrations, and reward shaping. In this paper, we propose an algorithm to solve the distant goal-reaching task by using planning at training time to automatically generate a curriculum of intermediate states. Our algorithm, Classifier-Planning (C-Planning), frames the learning of the goal-conditioned policies as expectation maximization: the E-step corresponds to planning a sequence of waypoints using graph planning, while the M-step aims to learn a goal-conditioned policy to reach those waypoints. Unlike prior methods that combine goal-conditioned RL with graph search, ours performs planning only during training and not testing, significantly decreasing the compute costs of deploying the learned policy. Empirically, we demonstrate that our method is more sample efficient that prior methods. Moreover, it is able to solve very long horizons manipulation and navigation tasks, tasks that prior goal-conditioned methods and methods based on graph search fail to solve.

1 INTRODUCTION

Whereas typical RL methods maximize the accumulated reward, goal-conditioned RL methods learn to reach any goal. Arguably, many tasks are more easily defined as goal-reaching problems than as reward maximizing problems. While many goal-conditioned RL algorithms learn policies that can reach nearby goals, learning to reach distant goals remains a challenging problem. Some prior methods approach this problem by performing search or optimization over subgoals at test time. However, these test-time planning methods either rely on graph search [10, 37], which scales poorly with dimensionality [18], or continuous optimization over subgoals [32], which is expensive and can result in model exploitation.

In this paper, we take a different tack and instead use planning at training time to automatically generate a curriculum. When training the agent to reach one goal, our method first determines some intermediate waypoints enroute to that goal. Then, it commands the agent to reach those waypoints before navigating to the final destination. Collecting data in this manner improves the quality of data, allowing the agent to learn to reach distant goals. Importantly, our method does not perform planning at test time, decreasing the computational demands for deploying the learned agent.

Our curriculum does not require manual engineering or prior knowledge of the tasks. Rather, the curriculum emerges automatically when we use expectation maximization (EM) to maximize a lower bound on the probability of reaching the goal. The M-step corresponds to a prior method for goal-conditioned RL, while the E-step corresponds to graph planning. Thus, EM presents a marriage between previous goal-conditioned RL algorithms and graph-planning methods.

The main contribution of this work is a goal-conditioned RL algorithm, C-Planning, that excels at reaching distant goals. Our method uses an automatic curriculum of subgoals to accelerate training. The automatic waypoint sampling ends up generating a curriculum of waypoints, points that are reachable by the current policy but also lead to the goal. We show that our curriculum emerges from applying variational inference to the goal-reaching problem. Unlike prior work, our method does not require graph search or optimization at test-time. Empirically, C-Planning not only matches but surpasses the performance of these prior search-based methods, suggesting that it is not just amortizing

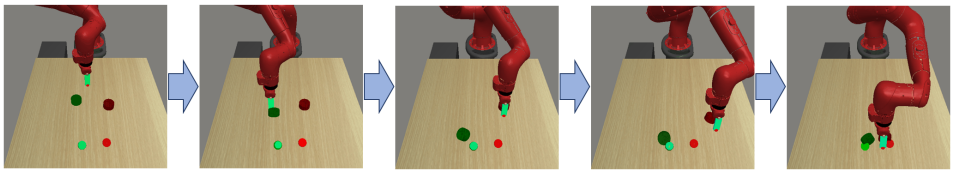

Figure 1: **C-Planning** is an algorithm for goal-conditioned RL that uses an automatic curriculum of waypoints to learn policies that can solve complex tasks. In this manipulation task, the goal requires moving the green puck to the green dot and the red puck to the red dot. Our method learns to solve this task, manipulating multiple objects in sequence, without requiring any reward functions, manual distance functions, or human demonstrations.

the cost of graph search. We empirically evaluate C-Planning on temporally-extended 2D navigation tasks and complex 18D robotic manipulation tasks. C-Planning improves the sample efficiency of prior goal-conditioned RL algorithms and manages to solve more difficult manipulations tasks such as rearranging multiple objects in sequence (see Fig. 1). To the best of our knowledge, no prior method has learned tasks of such difficulty without requiring additional assumptions.

2 Related Work

The problem of learning to achieve goals has a long history, both in the control community Lyapunov [27] and the RL community [20]. Many prior papers approach goal-conditioned RL as a reward-driven, multi-task learning problem, assuming access to a goal-conditioned reward function. One unique feature of goal-conditioned RL, compared to other multi-task RL settings, is that it can also be approached using reward-free methods, such as goal-conditioned behavior cloning [8, 16, 28, 37] and RL methods that employ hindsight relabeling [11, 20, 26, 38]. While goal-conditioned behavior cloning methods are simple to implement and have shown excellent results on a number of real-world settings [29, 39], they are not guaranteed to recover the optimal policy without additional assumptions (e.g., determinism, online data collection). While both methods excel at certain control tasks, both often struggle to solve tasks with longer horizons.

To solve longer-horizon tasks, prior work has combined goal-conditioned RL with graph search, noting that goal-conditioned value functions can be interpreted as dynamical distances [9, 19, 32, 37]. These prior methods typically proceed in two phases: the first phase learns a goal-conditioned policy, and the second phase combines that policy with graph search. While these methods have demonstrated excellent results on a number of challenging control tasks, including real-world robotic navigation [29, 39], the stage-wise approach has a few limitations. First, the post-hoc use of graph search means that graph search cannot improve the underlying goal-conditioned policy. It is well known that the performance of RL algorithms is highly dependent on the quality of the collected data [21, 22, 24]. By integrating planning into the learning of the underlying goal-conditioned policy, our method will improve the quality of the data used to train that policy. A second limitation of these prior methods is the cost of deployment: choosing actions using graph search requires at least $\mathcal{O}(|\mathcal{V}|)$ queries to a neural network.[1] In contrast, our method performs planning at training time rather than test time, so the cost of deployment is $\mathcal{O}(1)$. While this design decision does increase the computational complexity of training, it significantly decreases the latency at deployment. Our method is similar to RIS [5], which also performs planning during training instead of deployment. Our method differs from RIS in how planning is used: whereas RIS modify the *objective*, our method uses planning to modify the *data*. This difference not only unifies the objectives for RL and graph planning, but also significantly improves the performance of the algorithm. , a subtle distinction that avoids favoring the learned policy and unifies the objectives for RL and graph planning. We demonstrate the importance of this difference in our experiments.

Effectively solving goal-conditioned RL problems requires performing good exploration. In the goal-conditioned setting, the quality of exploration depends on how goals are sampled, a problem studied in many prior methods [9, 13, 14, 33, 34, 36, 45, 46]. These methods craft objectives that try to optimize for learning progress, and the resulting algorithms achieve good results across a range of environments. Our method differs from these methods in that the method for optimizing

[1] While computing all pairwise distances requires $\mathcal{O}(|\mathcal{V}|^2)$ time, only $|\mathcal{V}|$ edges change at each time step. The cost of computing the remaining edges can be amortized across time.

the goal-conditioned policy and the method for sampling waypoints are jointly optimized using the same objective. We demonstrate the importance of this difference in our experiments.

Our approaches can also be viewed as one Hierarchical RL [7, 25, 43] method with the distance function specified by the classifier. However, one important difference between C-Planning and many other HRL methods is that our approach doesn't require training a high-level policy for generating subgoals for the lower-level policy to reach [16, 25, 30]. Comparing with approaches try to build a graph/tree for planning [10, 19, 32], our approach doesn't require any planning at deployment, saves a lot of computation time.

Our method builds on the idea that reinforcement learning can be cast as inference problems [4, 23, 35, 41, 42, 47]. The observation that variational inference for certain problems corresponds to graph planning is closely related to Attias [4]. Our work extends this inferential perspective to hierarchical models.

3 Preliminaries

We introduce the goal-conditioned RL problem and a recent goal-conditioned RL algorithm, C-learning, upon which our method builds.

Goal-Conditioned RL. We focus on controlled Markov processes defined by states $\boldsymbol{s}_t \in \mathcal{S}$ and actions $\boldsymbol{a}_t$. The initial state is sampled $\boldsymbol{s}_0 \sim p_0(\boldsymbol{s}_0)$ and subsequent states are sampled $\boldsymbol{s}_{t+1} \sim p(\boldsymbol{s}_{t+1} \mid \boldsymbol{s}_t, \boldsymbol{a}_t)$. Our aim is to navigate to the goal states, $\boldsymbol{s}_g \in \mathcal{S}$, which are sampled from $\boldsymbol{s}_g \sim p_g(\boldsymbol{s}_g)$. We define a policy $\pi(\boldsymbol{a}_t \mid \boldsymbol{s}_t, \boldsymbol{s}_g)$ conditioned on both the current state and the goal. The objective is to maximize the probability (density) of reaching the goal in the future.

To derive our method, or any other goal-conditioned RL algorithm, we must make a modeling assumption about *when* we would like the agent to reach the goal. This modeling assumption is only used to derive the algorithm, not for evaluation. Formally, let $\Delta \in \mathbb{N}^+$ be a random integer indicating when we reach the goal. The user specifies a prior $p(\Delta)$. Most prior work (implicitly) uses the geometric distribution, $p(\Delta) = \textsc{Geom}(1-\gamma)$. The geometric distribution is ubiquitous because it is easy to incorporate into temporal difference learning. Despite its wide usage, it may not reflect the prior belief on when the agent will solve the task or when the episode will terminate. Thus, while it is natural to use geometric distribution, other choices of distributions can also be consdiered. Prior work has also considered non-geometric distributions [12]. In this paper, we use the negative binomial distribution, $p(\Delta) = \textsc{NegBinom}(p = 1-\gamma, n = 2)$. Given a prior $p(\Delta)$, we define the distribution over future states as

$$p^{\pi(\cdot|\cdot,\boldsymbol{s}_g)}_{p(\Delta)}(\boldsymbol{s}_{t+} = \boldsymbol{s}_{t+} \mid \boldsymbol{s}_t, \boldsymbol{a}_t) = \mathbb{E}_{p(\Delta)}\left[p^{\pi(\cdot|\cdot,\boldsymbol{s}_g)}_{\Delta}(\boldsymbol{s}_{t+\Delta} = \boldsymbol{s}_{t+} \mid \boldsymbol{s}_t, \boldsymbol{a}_t)\right], \tag{1}$$

where $p^{\pi}_{\Delta}(\boldsymbol{s}_{t+\Delta} \mid \boldsymbol{s}_t, \boldsymbol{a}_t)$ is the probability density of reaching state $\boldsymbol{s}_{t+\Delta}$ exactly Δ steps in the future when sampling actions from $\pi(\boldsymbol{a}_t \mid \boldsymbol{s}_t, \boldsymbol{s}_g)$. For example, the γ-discounted state occupancy measure [17, 31] can be written as $p^{\pi(\cdot|\cdot,\boldsymbol{s}_g)}_{\textsc{Geom}(1-\gamma)}$. Our objective for goal-reaching is to maximize the probability of reaching the desired goal:

$$\max_{\pi} \mathbb{E}_{p_g(\boldsymbol{s}_g)}\left[p^{\pi(\cdot|\cdot,\boldsymbol{s}_g)}_{\textsc{NegBinom}(p=1-\gamma,n=2)}(\boldsymbol{s}_{t+} = \boldsymbol{s}_g)\right]. \tag{2}$$

C-Learning. Our method builds upon a prior method for goal-conditioned RL, C-Learning [11]. C-Learning learns a classifier for predicting whether a state $\boldsymbol{s}_t$ comes from a future state density $p^{\pi(\cdot|\cdot,\boldsymbol{s}_g)}_{p(\Delta)}(\boldsymbol{s}_{t+} = \boldsymbol{s}_{t+} \mid \boldsymbol{s}_t, \boldsymbol{a}_t)$ or a marginal state density:

$$p^{\pi(\cdot|\cdot,\boldsymbol{s}_g)}_{p(\Delta)}(\boldsymbol{s}_{t+} = \boldsymbol{s}_{t+}) = \int p^{\pi(\cdot|\cdot,\boldsymbol{s}_g)}_{p(\Delta)}(\boldsymbol{s}_{t+} = \boldsymbol{s}_{t+} \mid \boldsymbol{s}_t, \boldsymbol{a}_t)\, p(\boldsymbol{s}_t, a_t)\, d\boldsymbol{s}_t\, d\boldsymbol{a}_t.$$

The Bayes-optimal classifier can be written in terms of these two distributions:

$$C_\theta(\boldsymbol{s}, \boldsymbol{s}_g) = \frac{p^{\pi(\cdot|\cdot,\boldsymbol{s}_g)}_{\textsc{Geom}}(\boldsymbol{s}_g \mid \boldsymbol{s})}{p^{\pi(\cdot|\cdot,\boldsymbol{s}_g)}_{\textsc{Geom}}(\boldsymbol{s}_g \mid \boldsymbol{s}) + p^{\pi(\cdot|\cdot,\boldsymbol{s}_g)}_{\textsc{Geom}}(\boldsymbol{s}_g)}. \tag{3}$$

In C-Learning, this classifier acts as a value function for training the policy. Our method will use this classifier not only to update the policy, but also to sample waypoints.

4 C-PLANNING: GOAL-CONDITIONED RL WITH PLANNING

We now present our method, C-Planning. The main idea behind our method is to decompose the objective of Eq. 2 into a sequence of easier goal-reaching problems. Intuitively, if we want a sub-optimal agent to navigate from some initial state $\boldsymbol{s}_0$ to a distant goal state $\boldsymbol{s}_g$, having the agent try to reach that state again and again will likely prove futile.

Instead, we can command a sequence of goals, like a trail of bread-crumbs leading to the goal $\boldsymbol{s}_g$. To select these waypoints, we will command the policy to reach those states it would visit *if* it were successful at reaching $\boldsymbol{s}_g$. Sampling subgoals in this way can ease the difficulty of training the agent (see Fig. 2.).

At a high-level algorithm summary, our method consists of two steps: using waypoing sampling to collect experience and performing standard goal-conditioned RL using the collected experience. The main challenge is the first step, as modeling the distribution over waypoints is difficult. In Sec. 4.1, we solve analytically for waypoint distribution, and then propose a simple practical method to sample from this distribution in Sec. 4.2.

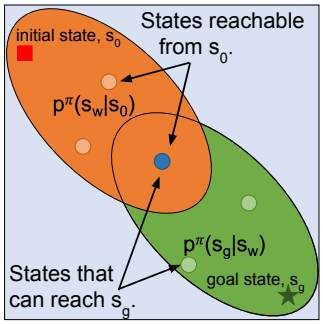

Figure 2: **Waypoint Sampling**: Our method samples waypoints that are reachable from the initial state, and from which the agent can reach the goal.

4.1 PLANNING AND VARIATIONAL INFERENCE

To formally derive our method for waypoint sampling, we cast the problem of goal-reaching as a latent variable problem. We assume that the agent starts at state $\boldsymbol{s}_0$ and ends at state $\boldsymbol{s}_g$, but the intermediate states that the agent will visit are unknown latent variables. This problem resembles standard latent variable modeling problems (e.g., VAE), where the intermediate state serves the role of the inferred representation. We can thus derive an evidence lower bound on the likelihood of reaching the desired goal:

Lemma 1. *The objective $\mathcal{L}$, defined below, is a lower bound on the goal-reaching objective (Eq. 2):*

$$\log p^{\pi(\cdot|\cdot,\boldsymbol{s}_g)}_{\text{NEGBINOM}}(\boldsymbol{s}_{t+} = \boldsymbol{s}_g \mid \boldsymbol{s}_0) \geq \mathbb{E}_{q(\boldsymbol{s}_w|\boldsymbol{s}_g,\boldsymbol{s}_0)}\Big[\log p^{\pi(\cdot|\cdot,\boldsymbol{s}_g)}_{\text{GEOM}}(\boldsymbol{s}_{t+} = \boldsymbol{s}_g \mid \boldsymbol{s}_w) + \log p^{\pi(\cdot|\cdot,\boldsymbol{s}_g)}_{\text{GEOM}}(\boldsymbol{s}_w \mid \boldsymbol{s}_0) - \log q(\boldsymbol{s}_w \mid \boldsymbol{s}_g, \boldsymbol{s}_0)\Big] \triangleq \mathcal{L}(\pi, q(\boldsymbol{s}_w \mid \boldsymbol{s}_g, \boldsymbol{s}_0)).$$

See Appendix A.1 for the proof. The lower bound, $\mathcal{L}$, depends on two quantities: the goal-conditioned policy and an *inferred* distribution over waypoints, $q(\boldsymbol{s}_w \mid \boldsymbol{s}_0, \boldsymbol{s}_g)$. This bound holds for any choice of $q(\boldsymbol{s}_w \mid \boldsymbol{s}_0, \boldsymbol{s}_g)$, and we can optimize this lower bound with respect to this waypoint distribution. We can see more intuition behind the negative binomial distribution here. With the negative binomial distribution, we can decompose a hard problem into a sequence of easier RL problems. Each of these easier (goal-conditioned) RL problems uses geometric distributions, and the sum of geometric random variables is a negative binomial distribution.

We will perform expectation maximization [6] to optimize the lower bound, alternating between estimating waypoint distribution and optimizing the goal-conditioned policy using this waypoint distribution. We now describe these two steps in detail.

E-Step. The E-step estimates the waypoint distribution, $q(\boldsymbol{s}_w \mid \boldsymbol{s}_0, \boldsymbol{s}_g)$. The three terms in the lower bound indicate that the sampled waypoint should be reachable from the initial state, the goal state should be reachable from the sampled waypoint, and that the waypoint distribution should have high entropy. These first two terms resemble shortest-path planning, where distances are measured using log probabilities. Importantly, reachability is defined in terms of the capabilities of the current policy. We can analytically solve for the waypoint distribution:

Lemma 2. *The waypoint distribution that optimizes our lower bound (Lemma 1) satisfies:*

$$q^*(\boldsymbol{s}_w \mid \boldsymbol{s}_g, \boldsymbol{s}_0) = \frac{p^{\pi(\cdot|\cdot,\boldsymbol{s}_g)}_{\text{GEOM}}(s_g \mid \boldsymbol{s}_w) p^{\pi(\cdot|\cdot,\boldsymbol{s}_w)}_{\text{GEOM}}(s_w \mid \boldsymbol{s}_0)}{\int p^{\pi(\cdot|\cdot,\boldsymbol{s}_g)}_{\text{GEOM}}(\boldsymbol{s}_g \mid \boldsymbol{s}'_w) p^{\pi(\cdot|\cdot,\boldsymbol{s}_w)}_{\text{GEOM}}(\boldsymbol{s}'_w \mid \boldsymbol{s}_0) d\boldsymbol{s}'_w}.$$

See Appendix A.1 for a full derivation. We illustrate this waypoint distribution in Fig. 2. In general, accurately estimating the distribution, q^*, is challenging. However, in the next section, we develop a simple algorithm that only requires learning a classifier instead of a generative model.

M-step. The M-step optimizes the lower bound with respect to the goal-conditioned policy. We can ignore the $-\log q(\boldsymbol{s}_w \mid \boldsymbol{s}_0, \boldsymbol{s}_g)$ term, which does not depend on the policy. The remaining two terms look like goal-conditioned RL objectives, with a subtle but important difference in how the trajectories are sampled. When collecting data, a standard goal-conditioned RL algorithm initially samples a goal and then collects a trajectory where the policy attempts to reach that goal. Our method collects data in a different manner. The agent samples a goal, *then samples an intermediate waypoint that should lead to that goal.* The agent attempts to reach the waypoint *before* attempting to reach the goal. After the trajectory has been collected, the policy updates are the same as a standard goal-conditioned RL algorithm.

Two mental models. The algorithm sketch we have presented, which will be fleshed out in the subsequent section, can be interpreted in two ways. One interpretation is that the method performs a soft version of graph planning during exploration, using a distance function of $d(\boldsymbol{s}_1, \boldsymbol{s}_2) = \log p_{\text{GEOM}}^{\pi(\cdot \mid \cdot, \boldsymbol{s}_2)}(\boldsymbol{s}_{t+} = \boldsymbol{s}_2 \mid \boldsymbol{s}_1)$. From this perspective, the method is similar to prior work that performs graph search during test-time [10, 37]. However, our method will perform planning at training time. Extensive ablations in Sec. 5 show that our method outperforms alternative approaches that only perform search during test-time.

The second interpretation focuses on the task of reaching the goal from different initial states. The choice of waypoint distribution, and the policy's success at reaching those waypoints, determines the initial state distribution for this task. Intuitively, the best initial state distribution is one that sometimes starts the agent at the true initial state $\boldsymbol{s}_0$, sometimes starts the agent at the final state $\boldsymbol{s}_g$, and sometimes starts the agent in between. In fact, prior work has formally shown that the optimal initial state distribution is the marginal state distribution of the optimal policy [21]. Under somewhat strong assumptions,[2] this is precisely what our waypoint sampling achieves. We refer the reader for the discussion and experiments in Appendix. A.

4.2 A Practical Implementation

We now describe how we implement the policy updates (M-step) and waypoint sampling (E-step). For the policy updates, we simply apply C-learning [11]. The main challenge is waypoint sampling, which requires sampling a potentially high-dimensional waypoint distribution. While prior work [14] has approached such problems by fitting high-capacity generative models, our approach will avoid such generative models and instead use importance sampling.

Let $b(\cdot)$ be the background distribution, which we take to be the replay buffer. Our algorithm corresponds to the following two-step procedure. First, we sample a batch of waypoints from the buffer. Then, we sample one waypoint from within that batch using the normalized importance weights, $\frac{q(\boldsymbol{s}_w \mid \boldsymbol{s}_g, \boldsymbol{s}_0)}{b(\boldsymbol{s}_w)}$. We can estimate these importance weights using the classifier learned by C-learning (Eq. 3):

Lemma 3. *We can write the importance weights in terms of this value function*

$$\frac{q(\boldsymbol{s}_w \mid \boldsymbol{s}_g, \boldsymbol{s}_0)}{b(\boldsymbol{s}_w)} = \frac{C_\theta(\boldsymbol{s}_w, \boldsymbol{s}_g)}{1 - C_\theta(\boldsymbol{s}_w, s_g)} \frac{C_\theta(\boldsymbol{s}_0, \boldsymbol{s}_w)}{1 - C_\theta(\boldsymbol{s}_0, \boldsymbol{s}_w)} Z(\boldsymbol{s}_0, \boldsymbol{s}_g), \tag{4}$$

where $Z(\boldsymbol{s}_0, \boldsymbol{s}_g)$ is a normalizing constant.

See Appendix A.3 for a full derivation. Since we will eventually normalize these importance weights (over $\boldsymbol{s}_w$), we do not need to estimate $Z(\boldsymbol{s}_0, \boldsymbol{s}_g)$. We call our complete algorithm *C-Planning*, and summarize it in Alg. 1. Note that our algorithm requires changing only a single line of pseudocode: during data collection, we command the agent to the intermediate waypoint $\boldsymbol{s}_w$ instead of the final goal $\boldsymbol{s}_g$. The sampling procedure in Alg. 2 is scalable and easy to implement.

The core idea of our method is to sample waypoints enroute to the goal. Of course, at some point we must command the agent to directly reach the goal. We introduce a hyperparameter n_g to indicate how many times we resample the intermediate waypoint before commanding the agent to reach the goal. This parameter is not the planning horizon, which is always set to 2.

[2] The assumptions are that *(1)* the policy always reaches the commanded waypoint, and that *(2)* that the goal-reaching probabilities $p_{\text{GEOM}}^{\pi(\cdot \mid \cdot, \cdot)}$ reflect the probability that the *optimal* policy reach some state.

Algorithm 1 **C-Planning** performs planning in data collection, modifies C-learning by $L5 \rightarrow L6-7$. The update for the policy and classifier ($L9$) is the same.

1: $\mathcal{D} \leftarrow \emptyset, N_g, \epsilon_d$
2: **for** $0 \le i \le N$ **do**
3: Set $n_g \leftarrow 0$ if new episode
4: $\boldsymbol{s}_0 \sim p_0(\boldsymbol{s}_0), \boldsymbol{s}_g \sim p_g(\boldsymbol{s}_g)$
5: $\cancel{\tau \sim p^\pi(\tau \mid \boldsymbol{s}_0, \boldsymbol{s}_g)}$
6: $\boldsymbol{s}_w, n_g \leftarrow$ CPLANNING(n_g, C, s_g)
7: $\tau \leftarrow (\tau_1 \sim p^\pi(\tau \mid \boldsymbol{s}_0, \boldsymbol{s}_w), \tau_2 \sim p^\pi(\tau \mid \boldsymbol{s}_0, \boldsymbol{s}_w))$
8: $\mathcal{D} \leftarrow \mathcal{D} \cup \{\tau\}$
9: $\pi, C \leftarrow$ CLEARNING$(\mathcal{D}, \pi, C)$

Algorithm 2 **C-Planning** samples the intermediate waypoints, then command the agent to reach them.

1: n_g: number of waypoints agent has reached in an episode
2: **function** CPLANNING(n_g, C, s_g)
3: **if** ($t = 0$ or $d(\boldsymbol{s}_t, \boldsymbol{s}_w) \le \epsilon_d$) and $n_g \le N_g$ **then**
4: $n_g \leftarrow n_g + 1$
5: Sample M waypoints $\boldsymbol{s}_w^{(i)} \sim$ Buffer$(\boldsymbol{s}_w)$
6: Compute distances for each candidate waypoint: $d^{(i)} \leftarrow \log \frac{C(F=1|\boldsymbol{s}_w, \boldsymbol{s}_g)}{C(F=0|\boldsymbol{s}_w, \boldsymbol{s}_g)} + \log \frac{C(F=1|\boldsymbol{s}_0, \boldsymbol{s}_w)}{C(F=0|\boldsymbol{s}_0, \boldsymbol{s}_w)})$
7: $\boldsymbol{s}_w \propto$ SOFTMAX$(d^{(i)})$
8: **else**
9: Set $\boldsymbol{s}_w \leftarrow \boldsymbol{s}_g$
10: **return** $\boldsymbol{s}_w, n_g$

5 EXPERIMENTS

Our experiments study whether C-Planning can compete with prior goal-conditioned RL methods both on benchmark tasks and on tasks designed to pose a significant planning and exploration challenge. Our first experiments use these tasks to compare C-Planning to prior methods for goal-conditioned RL. We then study the importance of a few design decisions through ablation experiments.The benefits of C-Planning, compared with prior methods, are especially pronounced on these challenging tasks. To provide more intuition for why C-Planning outperforms prior goal-conditioned RL methods, we plot the gradient norm for the actor and critic functions, finding that C-Planning enjoys larger norm gradients for the critic and smaller variance of the gradient for the actor. Ablation experiments study the number of waypoints used in training. We finally measure the inference time of choosing actions, finding that C-Planning is up to $4.7\times$ faster than prior methods that perform search at test time.

Environments. We investigate environments of various difficulty, some of which we visualize in in Fig. 3. The first set of environments is taken directly from the Metaworld benchmark suite [44], a common benchmark for goal-conditioned RL. These tasks are challenging because of the manipulation skills required to push and reorient objects. While prior goal-conditioned RL methods do solve some of these tasks (e.g., `Push` and `Reach`), they stand at the edge of the capabilities of current methods. The second set of environments, 2D navigation mazes, are designed to stress-test the planning capabilities of different methods. Successfully solving these tasks requires reasoning over long horizons of up to 50 steps. These are challenging because, unlike many benchmarks, they require non-greedy exploration: greedy strategies get stuck in local optima. Our final set of environments combine the challenges of these environments. We extend the tasks in Metaworld to involve *sequential* manipulation of *multiple* objects, similar to the tasks in prior work [40]. For example, the `Obstacle-Drawer-Close` task require the robotic arm to manipulate multiple objects in sequence, first pushing an object and then opening a drawer. Solving these tasks are difficult because the agent is given no demonstrations, no reward shaping, and no manually specified distance metrics.

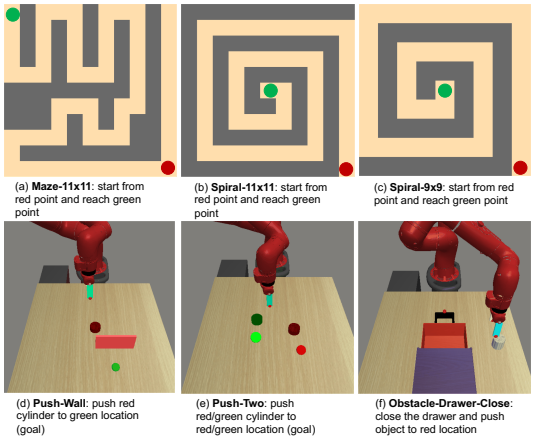
(a) **Maze-11x11**: start from red point and reach green point
(b) **Spiral-11x11**: start from red point and reach green point
(c) **Spiral-9x9**: start from red point and reach green point
(d) **Push-Wall**: push red cylinder to green location (goal)
(e) **Push-Two**: push red/green cylinder to red/green location (goal)
(f) **Obstacle-Drawer-Close**: close the drawer and push object to red location

Figure 3: **Environments**: Visualization of the 2D navigation maze environments *(top row)* and robotics manipulation tasks *(bottom row)*.

Baselines. We will compare C-Planning to a number of baselines. C-Learning is a recent goal-conditioned RL method that does not perform planning. C-Learning performs the same gradient

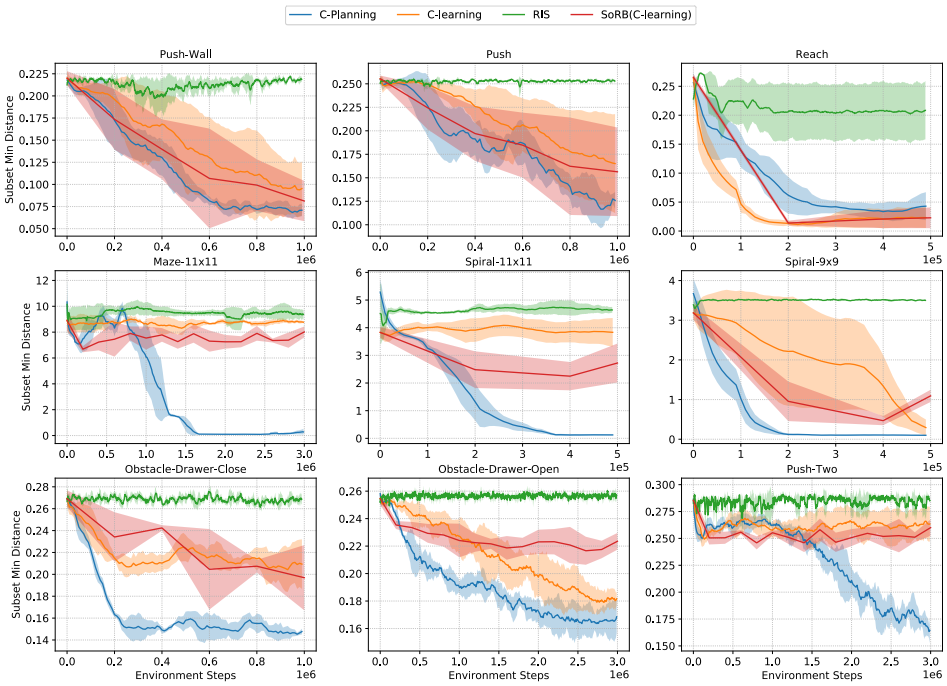

Figure 4: **Comparison of goal-conditioned RL methods**: We compare C-Planning to prior goal-conditioned RL algorithms on various tasks: *(top)* benchmark manipulation tasks from Metaworld, *(middle)* 2D maze navigation, and *(bottom)* robot manipulation tasks that require long horizon planning. For each task, we record the Euclidean distance to the goal, taking the minimum distance within an episode. All but the easiest task (`Reach`), C-Planning outperforms all prior methods, including those that perform planning. Only C-Planning is able to solve the most challenging navigation and manipulation tasks.

updates as C-Planning, and only differs in how experience is collected. Comparing to C-Learning will allow us to identify the marginal contribution of our curriculum of waypoints. The second baseline is SoRB [10], a goal-conditioned RL method that performs search at test-time, rather than training time. We didn't manage to run the comparison with [19] since it requires a reward function and a termination function from the environment. While SoRB was originally implemented using Q-learning, we find that a version based on C-learning worked substantially better, so we use this stronger baseline in our experiments. Comparing against SoRB will allow us to study the tradeoffs between performing planning during training versus testing. Because SoRB performs search at testing, it is considerably more expensive to deploy in terms of computing. Thus, even matching the performance of SoRB, without incurring the computational costs of deployment would be a useful result. The third baseline is an ablation of our method designed to resemble RIS [5]. Like C-Planning, RIS performs planning during training and not testing, but the planning is used differently from C-Planning. Whereas C-Planning uses planning to collect data, leaving the gradient updates unchanged, RIS modifies the RL objective to include an additional term that resembles behavior cloning. Our comparison with RIS thus allows us to study how our method for using the sampled waypoints compares to alternative methods to learn from those same sampled waypoints.

5.1 Comparison with Prior Goal-Conditioned RL Methods

To compare C-Planning to prior goal-conditioned RL algorithms, we start with three tasks from the MetaWorld suite: `Reach`, `Push`, `Push-Wall`. While C-Planning learns slightly slower than prior methods on the easiest task (`Reach`), we see a noticeable improvement over prior methods on the more challenging `Push` and `Push-Wall` tasks, tasks that require reasoning over longer horizons to solve. This observation suggests that that the waypoint sampling performed by C-Planning might be especially beneficial for solving tasks that require planning over long horizons.

To test the planning capabilities of C-Planning, we design a series of 2D navigation mazes. While the underlying locomotion motions are simple, these tasks post challenges for planning and are designed so that a greedy planning algorithm would fail. On all three mazes, C-Planning learns faster than all baselines and achieves a lower asymptotic distance to the goal, as compared to the baselines. On

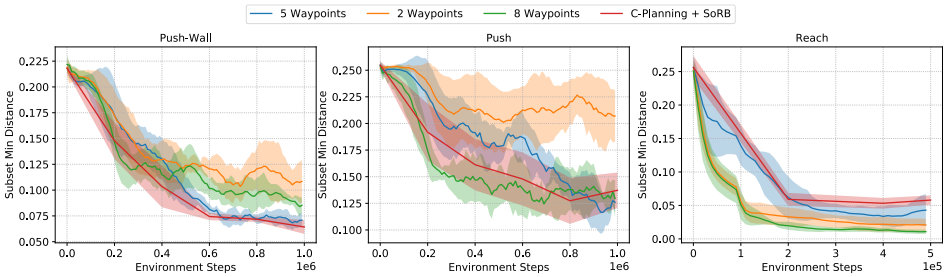

Figure 5: **Planning at Training Versus Testing:** We ablate the number of intermediate waypoints used to reach the goal, and compare against a variant of our method that performs planning during both training and testing ("C-Planning + SoRB"). This variant does not improve performance, indicating that the feedforward policy learned by C-Planning has already "internalized" these planning capabilities.

the most challenging maze, `Maze-11x11`, only our method is able to make any learning progress. Of particular note is the comparison with SoRB, which uses the same underlying goal-conditioned RL algorithm as C-Planning, but differs in that it performs search at testing, rather than training. While SoRB performs better than C-learning, which does not perform planning, SoRB consistently performs worse than C-Planning. This observation suggests that C-Planning is not just amortizing the cost of performing search. Rather, these results suggest that incorporating planning into training can produce significantly larger gains than incorporating planning into the deployed policy.

As the last set of experiments, study higher dimensional tasks that require long-range planning. We design three environments: `Obstacle-Drawer-Close`, `Obstacle-Drawer-Open` and `Push-Two`. These tasks have a fairly large dimension (15 to 18) and require sequential manipulation of multiple objects. C-Planning outperforms all baselines on all three tasks. While C-learning makes some learning progress, SoRB (which modifies C-learning with search at test time) does not improve the results. RIS, which also samples waypoints during training but uses those waypoints differently, does not make any learning progress on these tasks. Taken together, these results suggest that waypoint sampling (as performed by C-Planning) can significantly aid in the solving of complex manipulation tasks, but only if that waypoint sampling is performed during training. Moreover, the comparison with RIS suggests that those waypoints should be used to collect new data, rather than to augment the policy learning objective. To the best of our knowledge, C-Planning is the first method to learn manipulation behavior of this complexity without additional assumptions (such as dense rewards or demonstrations).

5.2 Why Does C-Planning Work?

We ran many additional experiments to understand *why* C-Planning works so well. To start, we run ablation experiments to answer two questions: *(1)* Although C-Planning only applies planning at training time, does *additionally* performing planning at test time further improve performance? *(2)* How many times should we resample the waypoint before directing the agent to the goal?

Fig 5 shows the results of ablation experiments. C-Planning performs the same at test-time with and without SoRB-based planning, suggesting that our training-time planning procedure already makes the policy sufficiently capable of reaching distant goals, such that it does not benefit from additional test-time planning. Fig. 5 also shows that C-Planning is relatively robust to n_g, the number of waypoints used before directing the agent to the goal. For all choices of this hyperparameter, C-Planning still manages to solve all the tasks.

Gradient analysis. We provide an empirical observation why C-Planning is better than vanilla goal-conditioned RL methods. We hypothesize that, by introducing waypoints, C-Planning provides a better learning signal, increasing the gradient norm for training the critic and decreasing the variance of the gradient for the policy. Prior work has theoretically analyzed the importance of gradient norms for RL [1] and we will provide some empirical evidence for the importance of controlling gradient norms. In addition, variance reduction has also long been a core problem in RL [3, 15] and smaller variance will help stabilize the RL algorithm. In Fig. 7, we plot the norm of the gradient (mean and variance) of both C-Planning and C-Learning using the Maze-11x11 environment, finding that our method increases the norm of the critic norm and decreases the variance of the actor gradient norm.

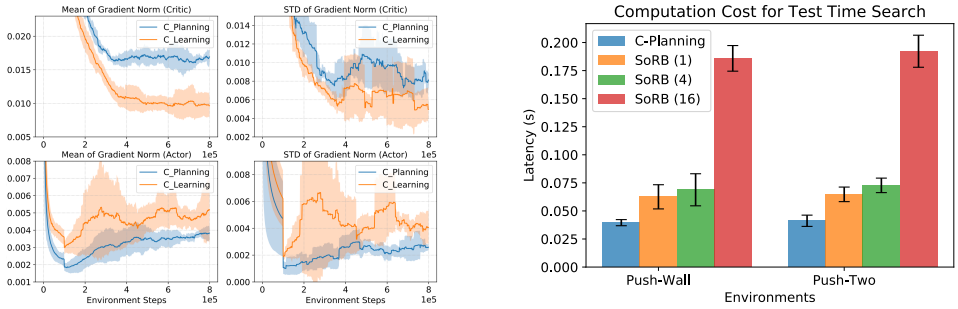

Figure 7: **Gradient Analysis and Computation Cost:** *(Left)* Mean and standard deviation of the gradient norm for the actor and critic networks. C-Planning has a larger critic gradient norm than C-Learning. C-Planning shows a smaller variance comparing to C-Learning. *(Right)* Computation cost in latency of C-Planning and SoRB with various number of waypoints.

Test-time latency. One important advantage of C-Planning is that it enables direct execution at test time, does not require any online planning. At test time, we directly set the agent's goal to the final goal state without commanding any intermediate states. This makes C-Planning considerably different from previous planning methods, such as SoRB [10]. Not only does our method achieve a higher return, but it does so with significantly less computing at deployment. We measure the execution time at evaluation time for C-Planning and SoRB with a various number of waypoints in Fig. 7. C-Planning is 1.74× faster than planning over four waypoints and 4.71× faster than planning over 16 waypoints in `Push-Wall` environment.

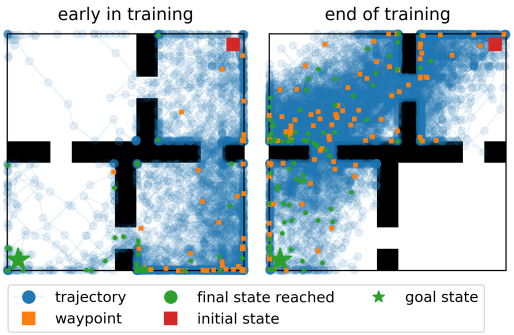

Figure 6: **Waypoint sampling:** *(Left)* Early in training, the agent samples waypoints closer to the initial state. *(Right)* At convergence, waypoints are evenly distributed along states visited by the optimal policy, as predicted by our theory.

Visualizing the training dynamics. To further gain intuition into the mechanics of our method, we visualize how the distribution over waypoints changes during training of the 2D navigation of the four rooms environment. Fig. 6 shows the sampled waypoints. The value functions (i.e., future state classifiers) are randomly initialized at the start of training, so the waypoints sampled are roughly uniform over the state space. As training progresses, the distribution over waypoints converges to the states that an optimal policy would visit enroute to the goal. While we have only shown one goal here, our method trains the policy for reaching all goals. This set of experiments provides intuition of how C-Planning works as the distribution of waypoints shrinks from a uniform distribution to the single path connecting start state and goal state. This visualization is aligned with our theory (Eq. 2), which says that the distribution of waypoints should resemble the states visited by the optimal policy.

6 Conclusion

In this paper, we introduced C-Planning, a method for incorporating planning into the training of goal-conditioned agents. The method enables the automatic generation of a curriculum over intermediate waypoints. Unlike prior methods, our approach avoids the computational complexity of performing search at test time. C-Planning is simple to implement on top of existing goal-conditioned RL algorithms and achieves state-of-the-art results on a range of navigation and manipulation tasks.

Our work suggests a few directions for future work. First, C-Planning samples waypoint that correspond to the optimal state distribution, which is proovably optimal in some settings [21]. How might similar ideas be applied to reward-driven tasks? Second, while this paper studied sought to learn agents for reaching distant goals, we assumed that those distant goals were provided as part of the task definition. Goal-conditioned algorithms that can propose their own distant goals, while already studied in some prior work [14, 34], remains an important direction for future work.

Ethics Statement. Our paper focus on one of the core questions in RL, i.e. can we design an search/planning algorithm to help goal-conditioned RL agent learn complex long-range behavior. As a general algorithm for goal-conditioned RL, currently we cannot foresee any positive/negative social impact of our work. As we conduct our experiments on standard environments like 2D navigation maze and robotic manipulation benchmarks (MetaWorld), our experiments should not suffer from any discrimination/bias/fairness concerns.

Reproducibility Statement. Our code is directly adapted from the open-sourced code base from [11] and we have introduced our implementation details in Appendix C.2 and Appendix C. We believe our results can be easily reproduced, and our code is available at `https://sites.google.com/view/cplanning`.

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