Improving Generative Adversarial Networks via Adversarial Learning in Latent Space

Abstract

For Generative Adversarial Networks which map a latent distribution to the target distribution, in this paper, we study how the sampling in latent space can affect the generation performance, especially for images. We observe that, as the neural generator is a continuous function, two close samples in latent space would be mapped into two nearby images, while their quality can differ much as the quality is generally not a continuous function in pixel space. From such a continuous mapping function perspective, it is also possible that two distant latent samples can be mapped into two close images (if not exactly the same). In particular, if the latent samples are mapped in aggregation into a single mode, mode collapse occurs. Accordingly, we propose adding an implicit latent transform before the mapping function to improve latent z from its initial distribution, e.g., Gaussian. This is achieved using well-developed adversarial sample mining techniques, e.g. iterative fast gradient sign method (I-FGSM). We further propose new GAN training pipelines to obtain better generative mappings w.r.t quality and diversity by introducing targeted latent transforms into the bi-level optimization of GAN. Experimental results on visual data show that our method can effectively achieve improvement in both quality and diversity.

1 Introduction

Generative Adversarial Networks (GANs) [1] have shown effectiveness for generating high-fidelity data, especially for images under various settings [2; 3; 4; 5; 6]. Based on the zero-sum game, the model is trained by the adversarial process between the generator and the discriminator. Many efforts have been made to achieve a more realistic generation from different perspectives. For instance, WGAN [7], SNGAN [8], LSGAN [9] aim to design better objective functions. ImprovedGAN [10], AC-GAN [11] propose practical training techniques. While more complex network structures are studied in BigGAN [12], StyleGAN [13], SAGAN [14].

Despite the above progress, a relatively less studied question is how the latent space affects the generation quality and diversity, which can be orthogonal to the above frequently studied factors like model architectures and training techniques. In this paper, we argue that the latent samples from a standard continuous distribution (e.g. Gaussian) can often be mapped to varying-quality samples for the generation. One reason is that the generator is a continuous function (as neural nets) while the generation quality (e.g. natural images in pixel space) is not. Moreover, it has been shown in GAN literature [15] that many image objects lie upon multiple disjoint manifolds. A continuous mapping from a continuous latent distribution, e.g., Gaussian, may generate invalid samples in the between of the manifolds when the generator seeks to cover all the meaningful modes. See Fig. 1 (a) for illustration. This fact also implies a dilemma: for complex real-world data, there is a trade-off between quality and diversity when the latent vectors are sampled from a continuous uni-mode distribution, e.g., Gaussian, based on that the generator as a network is a continuous mapping.

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(a) Quality Discontinuity   (b) Our Sampling Transform

Figure 1: Red dashed lines: real data manifolds and their preimages; yellow circles/squares: samples for sound generation; black circles/squares: samples for bad generation; orange dashed lines: the generator mapping; blue dashed lines: z transform; blue shades and solid blue lines: latent distribution and generated distribution. Due to the continuity of the network-based generator, close samples in latent space will be mapped to close images in pixel space, while the quality can vary. Cat (a) and Cat (b) are close in pixel space, but Cat (a) loses its right ear. Our method transforms bad latent $\mathbf{z}$ towards the preimage of the nearest real manifold, thus avoiding terrible generation.

Figure 2: The generated distributions mapped from a fixed latent distribution reflect the mapping quality (same legends as in Fig. 1). Left: bad generation quality as the generated distribution does not match the real distribution well. Right: bad generation diversity as the mapping misses modes.

The above contradiction between the discontinuity in generation data quality and the continuity of latent distribution as well as mapping function, can be one of the significant factors to the well-known difficulty in GANs training, especially for generators, as one unreasonably hopes to enforce a discontinuous mapping via continuous neural nets. On the other hand, the mapping is also critical to the performance of functions with continuous nature, as badly trained mapping can lead to poorly fitted generated distribution. Meanwhile, by realizing that the mapping function allows for many-to-one mapping, mode collapse [16] can naturally happen when different latent samples are mapped into few or even a single mode in the target space.

To tackle these issues, we impose an extra (implicit) transform function $z^*(\cdot)$ on the raw sampling $\mathbf{z}$, and the generation can be written by $G(z^*(\mathbf{z}))$, which requires twofold efforts on both $G(\cdot)$ and $z^*(\cdot)$. From this perspective, most existing works employ $z^*(\cdot)$ as an identity function, while we try to find a more effective one. We model the $\mathbf{z}$ transform process as making perturbations to the original sampling since $z^*(\mathbf{z})$ shall not depart much from $\mathbf{z}$ otherwise the generative expression will differ. This leads to the adversarial learning methods. Specifically, the implicit function based transform $z^*(\cdot)$ can be achieved by updating the latent $\mathbf{z} \sim p(\mathbf{z})$ to minimize $loss_G$ i.e. $\log(1 - D(G(\mathbf{z})))$ using adversarial sample mining techniques e.g. iterative fast gradient sign method (I-FGSM) [17] with the parameters of G and D fixed, and we name the method as AdvLatGAN-z. See Fig. 1 (b) for the schematic diagram. We will show that our $\mathbf{z}$ transform (perturbations) can deliver a latent distribution better fitting the real distribution with the fixed G.

On top of our first effort, we propose a training strategy to further improve the generative mapping respectively for quality and diversity. See Fig. 2 for the schematic diagram. This is achieved by introducing $\mathbf{z}$ optimization (i.e., targeted implicit transforms on $\mathbf{z}$) into GAN training, specifically, updating $\mathbf{z} \sim p(\mathbf{z})$ using I-FGSM to find more effective latents in the bi-level optimization of vanilla GAN. Respectively for quality and diversity, we use two iterative updating strategies for $\mathbf{z}$ under different objectives, and we name the two training algorithms as AdvLatGAN-qua and AdvLatGAN-div. **The highlights of this paper include:**

1) We rethink the role of the generator as a continuous function, which may incur quality discontinuity in target space when the latent samples are directly sampled from a continuous distribution, together with poorly fitted generated distribution and mode aggregation (collapse) when the function suffers from bad properties w.r.t. quality or diversity. Then, we propose a composite generation perspective by formulating the mapping from $G(\mathbf{z})$ to $G(z^*(\mathbf{z}))$. It provides new methodological design guidance to GAN which requires twofold efforts on both $G(\cdot)$ and $z^*(\cdot)$.

2) We propose a pipeline for $G(\cdot)$ and $z^*(\cdot)$, by first training generative mappings for better generation quality and diversity respectively. Then the transform $z^*(\cdot)$ namely AdvLatGAN-z is enforced and computed implicitly to obtain an improved distribution for the effective generation. The training involves latent vector transform under different objective functions for quality and diversity, leading to new GAN models: AdvLatGAN-qua/div and their variants.

Figure 3: Generation examples of StyleGAN2-ada [18]. Sampling equidistantly from $p(\mathbf{z})$ in latent space, the samples from the generated distribution in pixel space are shown here. The beginning and ending images of each row locate in different manifolds. The intermediate results are sampled in the between of disjoint manifolds. The discontinuity causes weird generation (see yellow boxes – (**top**: missed ear and crooked head; **middle**: white spots on the nose; **bottom**: two bodies share one head).

3) Experimental results on synthetic data and natural images including large-scale datasets e.g. ImageNet show the notable improvement of our approach on both generation quality and diversity, whereby the performance gain is basically orthogonal to those from existing GAN techniques.

2 Related Work

Our latent vector transform pipeline mines effective latent samples and the resulting perturbations relate to adversarial methods. The proposed GAN training pipelines include the aforementioned transform in network training, which can be viewed as mining adversarial samples in training, namely adversarial training. Hence we briefly review existing works on latent space mining for GANs and adversarial learning. Also, techniques for avoiding mode collapse are studied.

Latent space mining in GANs. Techniques have been devised for latent space mining for GANs. By utilizing the steerability of GANs in latent space, StyleGAN [13] introduces a latent variable shift to better decouple the various styles by using a linear network (which is still continuous). [19], [20] and [21] introduce the latent space mining into training to achieve clustering objectives or improve the dynamic of training. In addition, some recent works focus on improving latent sampling quality to obtain high-quality images. For example, interactive evolutionary computation is used to make the generation process more controllable in [22], which meanwhile also brings additional manual efforts. To reduce manual intervention, [23; 24] use Koncept512 [25] as a criterion to improve the generation quality. However, as discussed in [23], this strategy is somehow biased and can not work well for each dataset (e.g., Pokemons). The reason is that the quality estimator is not even designated to access the real-data distribution information. Instead, the generation is guided by a predefined score function. Exploring the real distribution's guidance from the discriminator, DOT [26] utilizes optimal transport in latent space to improve the initial sampled distribution, and DDLS [27] develops discriminator driven Langevin dynamics to obtain high-quality samples.

Mitigating mode collapse for GANs. Efforts are made to mitigate mode collapse, which are based on the thinking that real-world samples lie in disjoint manifolds [15]. One way is to introduce a collection of generators such that each generator may cover a specific mode since a single generator can hardly fulfill a discontinuous function [15]. However, more works focus on improving mapping properties, explicitly obtaining a mapping covering more modes [28; 29; 30]. Note that the generated distribution obtained by this method will contain invalid parts due to the continuity of the latent distribution and the mapping. This calls for the selective sampling of the continuous latent distribution or directly amending the latent distribution, which is rarely noticed in these works.

Adversarial samples and adversarial training. Adversarial samples are manipulated samples crafted by adding indistinguishable perturbations to fool deep nets. Since [31], various adversarial attack methods have been devised [32; 17; 33]. For defense, adversarial training is meanwhile developed [32; 34; 35]. In particular, recent studies have shown that adversarial training can bring many benefits to GANs, not just improving robustness. RGAN [36] shows that adversarial training can enhance the generalization of the generator and discriminator. Based on theoretical analysis and empirical results, [37; 38; 39] show that updating the discriminator's parameters with the loss calculated by adversarial disturbed image samples can stabilize training and accelerate convergence.

In this paper, we use an off-the-shelf adversarial sample mining method iterative fast gradient sign method (I-FGSM) [17], to perform latent transform and mine effective $\mathbf{z}$ samples that benefit GAN training in its bi-level optimization process, which respectively relate to the procedure of adversarial sample mining and adversarial training. More adversarial methods e.g. PGD [33] and MI-FGSM [40] are also tried and discussed in Appendix E. The pre-existing works mentioned above that interplay between GANs and adversarial learning make perturbations on raw pixel space (real samples or generated samples), while we instead work on mining the latent space and introducing perturbations on latent samples, which we show is a novel and effective way to improve the generation.

3 Proposed Method

This section presents our twofold effort to lift the final generative performance: AdvLatGAN-z to achieve the targeted transform $z^*(\cdot)$; AdvLatGAN-qua and AdvLatGAN-div to obtain generation mapping G with better generation quality (i.e., -qua) and diversity (i.e., -div). Both methods are derived from the iterative updating in latent space.

3.1 Preliminaries

We introduce adversarial samples and adversarial training which is used to facilitate: i) generate $z^*(\mathbf{z})$; ii) develop training algorithms, including a new training pipeline based on vanilla adversarial process and regularization technique devised in MSGAN [29] for mode seeking.

Adversarial samples and adversarial training. Adversarial training aims to defend against adversarial attacks. It uses adversarial samples to calculate the loss. In classification, for each image-label pair $(\mathbf{x}_i, y_i)$ from the labeled training set, the adversarial samples $\mathbf{x}'$ is defined as:

$$\mathbf{x}'_i = \operatorname*{arg\,max}_{||\mathbf{x}-\mathbf{x_i}||_p \leq \epsilon} l(f_\theta(\mathbf{x}), y_i) \tag{1}$$

Here ϵ is the radius of the closed ball to constrain perturbation. While f_θ and l denote the attack target (a neural net) and the corresponding loss (e.g. cross-entropy loss). p denotes the norm dimension. Given in total n adversarial samples, adversarial training is fulfilled by the optimization:

$$\theta = \min_\theta \frac{1}{n} \sum_{i=1}^{n} l(f_\theta(\mathbf{x}'_i), y_i) \tag{2}$$

Mode coverage by regularizing distance of generated samples. MSGAN [29] mitigates mode collapse for conditional generation by adding a regularizer over randomly sampled $\mathbf{z}_1$ and $\mathbf{z}_2$:

$$\mathcal{L}_{ms} = \frac{d_I\left(G(c, \mathbf{z}_1), G(c, \mathbf{z}_2)\right)}{d_z\left(\mathbf{z}_1, \mathbf{z}_2\right)} \tag{3}$$

where c is the condition vector for generation, and d_I and d_z are the distance metrics in the target (image) space and latent space, respectively. It encourages the distance to be maintained or even enlarged in the target space to avoid the generated samples being trapped into an aggregation.

By integrating the regularization term with the original objective of cGANs [41], the final minimization objective in MSGAN for training G and D is:

$$\begin{aligned} \mathcal{L} &= \mathcal{L}_{ori} + \lambda_{ms}\mathcal{L}_{ms} \\ \mathcal{L}_{ori} &= \mathbb{E}_{c,\mathbf{x}}[\log D(c, \mathbf{x})] + \mathbb{E}_{c,\mathbf{z}}[\log(1 - D(c, G(c, \mathbf{z})))] \end{aligned} \tag{4}$$

where $\mathcal{L}_{ori}$ denotes the original objective, $\mathbf{x}$ denotes real data, and λ_{ms} is the weight hyper-parameter. Since Eq. 3 is to be maximized hence one can interpret λ_{ms} as a negative coefficient.

3.2 Latent Adversarial Mining for Generation Quality

3.2.1 Latent Space Transform

Note that as the targeted real-data space is a union of disconnected manifolds [15], via a continuous generative mapping G, the optimal subset in the latent space w.r.t the fixed G is in no way connected. We denote the targeted real-data subset in the high-dimensional pixel space X as $X_r \subset X$, and each disjoint submanifold as M_i. Then we obtain $X_r = \bigcup_{i=1}^{n_r} M_i$ where M_1 to M_{n_r} are disconnected to each other. Here we require the splitting of X_r to the extent that each submanifold keeps connected.

Figure 4: Visualization results of AdvLatGAN-z on STL-10. The left column shows the generations of raw Gaussian samples, while samples from left to right present the process of AdvLatGAN-z.

Definition 3.1. Suppose $G[\cdot] : \mathcal{P}(Z) \to \mathcal{P}(X)$ is the image-of-set function corresponding to the generative mapping function $G(\cdot) : Z \to X$, where Z and X denote subsets in latent space and pixel space, and $\mathcal{P}(\cdot)$ denotes the power set. Then $Z^{op}(G)$ is the optimal subset corresponding to G in latent space if $G[Z^{op}(G)] = X_r$.

Proposition 3.2. *For any continuous $G[\cdot]$ whose codomain includes multiple disconnected manifolds, $Z^{op}(G)$ is a union of disconnected subsets in the latent space.*

The proof is given in Appendix B. Proposition 3.2 implies that with the fixed continuous G, fitting the real-data manifolds requires a disconnected latent space support. Below we show how to implicitly transform the latent raw samples from Gaussian (or other forms e.g. uniform) to a new distribution closer to $Z^{op}(G)$ via the idea of mining adversarial samples as introduced above.

We design the following constrained optimization that requires the new $\mathbf{z}^*$ to be close enough[1] to $\mathbf{z}$. Its prediction score by the discriminator D should be as high as possible to improve the generation quality. Recall otherwise the given $\mathbf{z}_0$ may correspond to a poor generation as discussed in Sec. 1. Here both G and D are fixed.

$$\mathbf{z}^*(\mathbf{z}_0) = \underset{\mathbf{z} \in \{\mathbf{z}|d(\mathbf{z}_0,\mathbf{z}) \leq \epsilon\}}{\arg\min} \log(1 - D(G(\mathbf{z}))) \tag{5}$$

where $\mathbf{z}_0$ denotes the original latent vector, $\mathbf{z}^*(\mathbf{z}_0)$ denotes the newly computed $\mathbf{z}$, $d(\cdot, \cdot)$ denotes the distance which is ℓ_∞ in this paper, in line with the popular protocol in literature [32].

The above target can be readily solved by the well-developed tools in adversarial sample mining, e.g. the classic iterative fast gradient sign method (I-FGSM) [17] as formulated below in Eq. 6. In Appendix E, we also present comparison of more adversarial techniques e.g. PGD [33], MI-FGSM [40], that can be seamlessly incorporated by our framework, and we show the simple I-FGSM outperforms. We conjecture the reason may be due to the simplicity of the latent space in our case.

$$\mathbf{z}_{i+1} \leftarrow \mathbf{z}_i - \epsilon \cdot sgn\left(\nabla_{\mathbf{z}_i}\log(1 - D(G(\mathbf{z}_i)))\right) \tag{6}$$

From the distribution perspective, the transform is given by:

$$p_z^* = \underset{D(p_z,p_z^0) \leq \epsilon}{\arg\min} E_{\mathbf{z} \sim p_z}\left[\log(1 - D(G(\mathbf{z})))\right] \tag{7}$$

where p_z^0 denotes the original latent distribution, p_z^* denotes the newly searched one. $D(p_z, p_z^0) \leq \epsilon$ means that there is a limit to the distribution variation. A newly mined $\mathbf{z}$ can be considered as a sample from p_z^* if the sampling is within the perturbation circle. Fig. 4 shows the results by the pre-trained SNGAN [8] (i.e. the given G and D) on STL-10 [42].

We then show that Eq. 7 guarantees the correct optimization direction that optimizes the source distribution p_z towards the optimal probability distribution in latent space according to the current fixed G, i.e. $p_z^{op}(G)$ defined in Definition. 3.3. The proof for Proposition 3.4 is given in Appendix B.

Definition 3.3. Given G, $p_z^{op}(G)$ is the optimal probability distribution in latent space corresponding to $Z^{op}(G)$ when $p_z^{op}(G)$ satisfies that if $z \sim p_z^{op}(G)$ then $G(z) \sim p_r$. Here p_r denotes the real-data probability distribution in pixel space.

Proposition 3.4. *Optimizing GAN's training criterion i.e.* $\min_G \max_D \{E_{\mathbf{z} \sim p_z^0}[\log(1 - D(G(\mathbf{z})))] + E_{\mathbf{x} \sim p_r}[\log(D(\mathbf{x}))]\}$ *is to minimize* $JSD(p_z^{op}(G), p_z^0)$.

Prop. 3.4 implies that the GAN's optimization is to minimize the difference between $p_z^{op}(G)$ and p_z^0. Note that for optimizing p_z, the criterion merely involves $E_{\mathbf{z} \sim p_z^0}[\log(1 - D(G(\mathbf{z})))]$ i.e. the objective in Eq. 7. Given optimized fixed G and D (and p_z^{op} is thereby fixed), leaving p_z the only trainable parameter, optimizing the training criterion with p_z in the neighborhood of p_z^0 is driving p_z closer to p_z^{op}. Note that p_z in the neighborhood of p_z^0 is necessary otherwise the optimized criterion will depart much from JSD, and we achieve this condition by enforcing $D(p_z, p_z^0) \leq \epsilon$ in Eq. 7.

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[1]To maintain generative expression and satisfy the theoretical guarantee (see last paragraph of this section).

3.2.2 Quality Targeted Training Pipeline

Considering the pairwise approach for adversarial sample mining, i.e. adversarial training, we hope to mine samples that benefit the optimization in GAN training, which is achieved by utilizing the aforementioned latent space transform. Conducting the transform in training to obtain the new (probably disconnected) latent distribution for each iteration can compensate for the difficulty for generators to align the pace of generators and discriminators, as it is widely recognized that it is much more challenging to train the generator than the discriminator, for its inherent defect that it cannot map a continuous distribution to a disconnected one with multiple modes.

Specifically, the transform is conducted to the raw Gaussian sampling in D updating iterations while the rest of the training algorithm remains consistent with vanilla GAN [1] and other variants with the orthogonal efforts to latent space mining. We present the algorithm in Alg. 1 in the appendix which we call Adversarial Latent GAN with a post meaning quality (AdvLatGAN-qua). The latent transform is first computed by I-FGSM to mine the adversarial samples in latent space, then D and G are updated. The iteration continues until enough steps or the convergence of G.

The above latent transform model does not consider how to avoid mode collapse, as each time only one latent sample is considered for optimization in isolation. A similar constrained optimization formulation can be devised to improve generation diversity, as shown in the following subsection.

3.3 Latent Adversarial Mining for Diversity

We take a hard sample mining perspective to improve mode coverage. Given a sample $\mathbf{z}_0$ from the raw latent distribution, we aim to search its paired sample $\mathbf{z}^*$ to form a hard sample pair, in the sense that their generations are close in the target space given G. We consider two aspects. First, as hard samples, the paired samples shall still belong to the same category $\mathbf{c}$ which can be modeled with conditional GAN. Second, their distance in the latent space shall also be not too close, otherwise they may be aggregated in the target space due to continuous mapping. In other words, hard samples causing mode collapse shall be those close in target space while apart in latent space, when G is given. Hence, we adopt the form of Eq. 8 to design our search procedure:

$$\mathbf{z}^*(\mathbf{z}_0) = \underset{\mathbf{z} \in \{\mathbf{z}|d(\mathbf{z}_0, \mathbf{z}) \leq \epsilon\}}{\arg\min} \frac{d_I(G(\mathbf{c}, \mathbf{z}_0), G(\mathbf{c}, \mathbf{z}))}{d_z(\mathbf{z}_0, \mathbf{z})} \tag{8}$$

The symbols and terms are similar to Eq. 3. Akin to AdvLatGAN-qua, we use I-FGSM to obtain $\mathbf{z}^*$ and again use ℓ_∞ to control deviation magnitude. For each update step, we randomly select the first latent vector $\mathbf{z}_0$, and the second vector $\mathbf{z}^*$ is searched by n iterations of the I-FGSM method under the ℓ_∞ restriction starting from the Gaussian neighborhood of $\mathbf{z}_0$ with a small standard deviation.

Table 1: Ratio between image and latent distance by Eq. 8 to derive new $\mathbf{z}^*$. -*inv*: using inverse form.

Dataset	Eq. 8	Eq. 8-inv
Cifar-10	0.241	4.023
FACADES	0.3785	1.3385

Table 1 shows the effectiveness of the above paired hard sample seeking method, with experiments on Cifar-10 [43] and Facades [44] with DCGAN [45] as backbone. The visual results on Facades as shown in Fig. 6 suggest that the pair obtained by solving Eq. 8 tend to collapse (as they are hard samples), while the opposite leads to better diversity by using the inverse form of Eq. 8.

The above experiments verify the efficacy of our mining technique. We further introduce it into the initial training process of MSGAN [29]. In MSGAN, the regularization term by Eq. 3 regularizes the optimization process, where the selection of the pair is entirely random, without using any heuristic information. We instead use the $\mathbf{z}$ pair that is more inclined to collapse by randomly taking one $\mathbf{z}$ and iterating by the aforementioned method to get another $\mathbf{z}$. The other settings remain unchanged.

By using Eq. 8 to generate adversarial sample pairs to address mode collapse, we finally develop our new diversity enhancing GAN training approach AdvLatGAN-div as shown in Alg. 2 in the appendix, which can be further enhanced by post-training as discussed in experiments.

4 Experiments

Experiments on ImageNet and CelebA are performed on GPUs of Tesla V100. Other public benchmark results are performed on a single GPU of GeForce RTX 3090. Code will be publicly available.

Figure 5: Latent distribution transform with WGAN-GP/DCGAN as backbones on MNIST. As the I-FGSM iteration continues, the latent distribution deviates from the standard Gaussian, and contains more valleys and peaks which can be mapped into generated images as shown at the bottom. Note that the generations by the valley points are of low quality, and our scheme can effectively avoid them as the sampling probability is low (valley) in our transformed distribution.

Figure 6: Each of the six columns shows two compared pairs of generated examples (first pair: 1st + 2nd row; second pair: 3rd row + 2nd row) by our diversity driven iterative transform scheme in latent space with the same number of iterations to obtain z^* from initial z. **Middle:** generation by vanilla latent sampling z; **Top:** by latent samples mined by Eq. 8; **Bottom:** by latent samples mined by Eq. 8's inverse form. It shows that using Eq. 8 generates more similar image pairs serving as hard training samples.

Figure 7: The logic of our 5 variant methods in Sec. 4.1. Blue and red is for quality and diversity.

Table 2: Five variants in Sec. 4.1.

Variant	Latent Transform z^*	Improved mapping G
i)	✓	✗
ii)	✗	✓
iii)	✗	✓
iv)	✓	✓
v	✓	✓

4.1 Experimental Setup

We validate the effectiveness of the proposed methods for two parts, i.e., effective latent sampling improvement z^* and improved generation mapping G. In particular, five variant methods can be derived for different targets, among which AdvLatGAN-qua+ and AdvLatGAN-div+ are the final full version of our contributions. We present the methods below:

i) AdvLatGAN-z: post-training latent sampling improvement fighting against quality discontinuity; **ii) AdvLatGAN-qua:** GAN training for better quality using in-training latent sampling transform; **iii) AdvLatGAN-div:** GAN training for a more diverse generation by using in-training latent sampling transform; **iv) AdvLatGAN-qua+:** integration of in and post-training latent sampling improvement for generation quality; **v) AdvLatGAN-div+:** integration of in- and post-training latent sampling improvement for diversity. We compare these methods in Fig. 7 and Table 2.

We adopt the popular Inception Score [46], Fréchet Inception Distance [47] and density/coverage [48] for evaluation. IS utilizes the classification results of the generated images by the Inception Network to evaluate the generation quality. FID additionally considers the target distribution and evaluates the quality by fitting the distribution distance. Density and coverage are more recently proposed evaluation metrics that analyze the target and generated manifolds and estimate the similarity. Experimental results on hyper-parameter study and overhead discussion are presented in Appendix C and D.

4.2 AdvLatGAN-z: Performance Boosting by Post-training Latent Sampling

We evaluate the boosting effect by post-training latent sampling improvement termed as AdvLatGAN-z (previously denoted as z^*, an implicit transform on the original latent sampling from Gaussian). It aims to mitigate quality discontinuity. The results are given as follows.

Results on Synthetic Data. We test AdvLatGAN-z on Grid and Ring datasets consisting of a mixture of 25 and 8 2-D Gaussians as done in [49]. The result is given in Fig. 8. By updating the latent variables, our method achieves high-quality generation (samples closer to target Gaussian centers).

Table 3: Post-training latent sampling improvement with two architectures on STL-10.

Method	DCGAN IS(↑)	DCGAN FID(↓)	WGAN-GP IS(↑)	WGAN-GP FID(↓)	SNGAN IS(↑)	SNGAN FID(↓)
bare w/o sampling transform	7.199±0.027	58.675±0.023	8.749±0.093	35.706±0.395	8.482±0.138	37.059±0.768
EvolGAN [23]	7.174±0.086	58.761±0.030	8.773±0.068	35.851±0.003	8.517±0.069	36.343±0.512
DOT [51]	7.195±0.022	58.670±0.076	9.708±0.013	30.745±0.113	8.798±0.024	36.769±0.133
DDLS [27]	7.300±0.131	62.256±1.042	9.370±0.125	32.738±0.436	8.595±0.071	35.301±0.161
AdvLatGAN-z	**7.933±0.041**	**54.913±0.451**	**10.549±0.048**	**27.053±0.245**	**9.426±0.058**	**31.891±0.027**

Table 4: The results of AdvLatGAN-qua and AdvLatGAN-qua+ for Cifar-10 and STL-10.

Dataset	Method	bare IS(↑)	bare FID(↓)	AdvLatGAN-qua IS(↑)	AdvLatGAN-qua FID(↓)	AdvLatGAN-qua+ IS(↑)	AdvLatGAN-qua+ FID(↓)
Cifar-10	DCGAN [45]	5.92 ± 0.05	46.4 ± 0.7	6.21 ± 0.07	41.7 ± 1.0	**6.62 ± 0.26**	**40.2 ± 1.9**
	WGAN [7]	6.63 ± 0.05	32.8 ± 0.5	7.21 ± 0.04	27.3 ± 0.7	**7.93 ± 0.02**	**26.9 ± 0.6**
	WGAN-GP [52]	7.47 ± 0.09	24.7 ± 0.2	7.60 ± 0.06	22.6 ± 0.4	**8.84 ± 0.08**	**16.6 ± 0.4**
	SNGAN [8]	7.29 ± 0.09	25.5 ± 0.3	7.58 ± 0.03	22.3 ± 0.5	**8.33 ± 0.03**	**18.1 ± 0.1**
	LSGAN [9]	5.87 ± 0.14	49.3 ± 2.2	6.13 ± 0.27	42.8 ± 1.3	**6.55 ± 0.10**	**42.3 ± 1.3**
	WGAN-div [53]	7.43 ± 0.02	23.8 ± 0.3	7.81 ± 0.03	20.6 ± 0.4	**8.87 ± 0.11**	**15.2 ± 0.6**
	ACGAN [54]	6.02 ± 0.28	59.5 ± 1.5	6.06 ± 0.21	53.7 ± 1.6	**6.24 ± 0.16**	53.9 ± 0.5
STL-10	DCGAN [45]	7.18 ± 0.09	61.2 ± 1.2	7.33 ± 0.07	56.3 ± 1.0	**7.98 ± 0.02**	**52.8 ± 0.4**
	WGAN [7]	6.51 ± 0.07	73.0 ± 0.2	7.62 ± 0.04	**51.0 ± 0.6**	**8.57 ± 0.04**	52.1 ± 2.9
	WGAN-GP [52]	8.86 ± 0.05	37.4 ± 0.4	8.90 ± 0.05	34.2 ± 0.9	**10.78 ± 0.02**	**25.0 ± 0.0**
	SNGAN [8]	8.49 ± 0.09	36.8 ± 0.4	8.63 ± 0.08	34.5 ± 0.21	**9.64 ± 0.05**	**29.9 ± 0.1**
	LSGAN [9]	7.08 ± 0.12	62.9 ± 2.2	7.16 ± 0.15	58.5 ± 1.3	**7.85 ± 0.08**	55.3 ± 1.4
	WGAN-div [53]	8.82 ± 0.02	37.7 ± 0.2	9.00 ± 0.01	32.0 ± 0.6	**10.98 ± 0.28**	**23.0 ± 1.3**

Results on MNIST. Low complexity of MNIST [50] makes it possible to generate recognizable results by two-dimensional latent variables which can be better visualized. The iterative latent distribution change is illustrated in Fig. 5. We respectively conduct AdvLatGAN-z for the trained DCGAN and WGAN-GP models, with single-step iteration constraint using ℓ_∞ and iterated step size ϵ is set as 0.03. We present the first 30 iterations that can reflect the most significant changes.

Results on STL-10. STL-10 [42] maintains a higher resolution and richer image representation. We utilize AdvLatGAN-z for pre-trained DCGAN, WGAN-GP and SNGAN, with ℓ_∞ single-step constraint and the iteration step size ϵ is set as 0.05. We conduct 20 steps each time. IS and FID are adopted for evaluation, which are calculated over 10,000 generated images. We compare other efforts enhancing GAN performance by latent space mining including DOT, DDLS and EvolGAN. Table 3 present the results. AdvLatGAN-z outperforms the baselines and delivers at most 24.3% advantage for FID on vanilla in the WGAN-GP setting.

Results on AFHQ and FFHQ. To address the issues in Fig. 3, we evaluate on AFHQ [55] and FFHQ [56] based on StyleGAN2-ada [18]. In the setting of Fig. 3, when the sampling encounters invalid examples, AdvLatGAN-z is able to transform the bad z to generation-friendly $z^*(z)$ to avoid bad generation. Here we verify whether invalid samples can be improved with AdvLatGAN-z. We select six bad generations with the first three corresponding to those in Fig. 3' and conduct AdvLatGAN-z to their latent vectors. Fig. 9 shows that AdvLatGAN-z can effectively fix or avoid image defects.

Figure 8: Post-training latent sampling improvement on Grid and Ring by AdvLatGAN-qua.

Figure 9: Results of AdvlatGAN-z on AFHQ and FFHQ. The top row are bad generations (the first three correspond to those in Fig. 3) with the defects as follows: **1st column**: the cat misses an ear; **2nd column**: white spots on the nose; **3rd column**: two bodies share one head; **4th column**: green face; **5th and 6th columns**: semi-existing glasses. The bottom row are results under AdvLatGAN-z. AdvLatGAN-z can effectively mitigate defects.

4.3 AdvLatGAN-qua/div: Improving Generation Map

This section shows the effectiveness of the proposed GAN training pipelines, which aim to improve the generation mapping G respectively for quality and diversity.

AdvLatGAN-qua for Quality Improvement. Table 4 show the results on Cifar-10 and STL-10, using the mainstream architectures including DCGAN, WGAN, WGAN-GP, SNGAN, LSGAN, WGAN-div and ACGAN. We do not include ACGAN in the STL-10 setting because it requires labels [54] and does not work on unlabeled STL-10. IS and FID are adopted. We adversarially train GAN using AdvLatGAN-qua. The number of latent iterations during training is set as one per

Table 5: The results of AdvLatGAN-div and AdvLatGAN-div+ for Cifar-10 and STL-10.

Dataset	Metrics	Models	overall	airplane	automobile	bird	cat	deer	dog	frog	horse	ship	truck
Cifar-10	FID(↓)	MSGAN	30.225	73.083	69.518	78.258	74.525	57.778	86.831	63.287	69.705	69.994	66.434
		AdvLatGAN-div	27.054	70.933	71.627	75.650	67.670	**54.457**	**84.274**	55.836	65.083	69.662	**63.127**
		AdvLatGAN-div+	**26.169**	**67.100**	**67.499**	**73.449**	**67.070**	55.817	85.815	**55.227**	**64.159**	**67.265**	63.223
	density(↑)	MSGAN	0.517	0.351	0.226	**0.289**	0.6046	**0.536**	0.264	**0.685**	0.307	0.353	0.221
		AdvLatGAN-div	**0.524**	0.345	0.260	0.254	**0.657**	0.524	**0.306**	0.666	**0.351**	0.365	0.225
		AdvLatGAN-div+	0.492	**0.348**	**0.311**	0.227	0.595	0.430	0.296	0.590	0.332	**0.366**	**0.247**
	coverage(↑)	MSGAN	0.828	0.789	0.848	0.596	0.765	0.833	0.610	0.880	**0.916**	0.957	0.775
		AdvLatGAN-div	0.844	0.850	0.908	0.600	0.793	0.864	**0.607**	0.919	0.915	**0.962**	**0.788**
		AdvLatGAN-div+	**0.849**	**0.874**	**0.922**	**0.604**	**0.800**	**0.891**	0.599	**0.934**	0.877	0.959	0.780
STL-10	FID(↓)	MSGAN	67.849	92.021	125.723	108.434	118.938	111.784	133.680	140.486	121.907	101.232	101.059
		AdvLatGAN-div	65.088	92.007	125.237	109.672	118.645	104.859	132.424	140.266	113.745	93.833	99.739
		AdvLatGAN-div+	**60.205**	**88.871**	**118.886**	**104.206**	**111.238**	**99.255**	**125.287**	**131.170**	**106.568**	**91.895**	**95.715**
	density(↑)	MSGAN	0.353	0.198	0.241	0.083	0.558	0.378	0.364	0.146	0.232	0.120	0.118
		AdvLatGAN-div	0.429	0.220	0.292	0.114	0.686	0.404	0.384	0.193	0.336	0.164	0.123
		AdvLatGAN-div+	**0.431**	**0.248**	**0.295**	**0.125**	**0.733**	**0.401**	**0.381**	**0.209**	**0.330**	**0.190**	**0.149**
	coverage(↑)	MSGAN	0.455	0.538	0.535	0.261	0.539	0.380	0.391	0.370	0.410	0.456	0.324
		AdvLatGAN-div	0.514	0.526	0.455	0.350	0.624	0.483	0.409	0.513	0.439	0.513	0.363
		AdvLatGAN-div+	**0.540**	**0.554**	**0.519**	**0.364**	**0.699**	**0.514**	**0.433**	**0.550**	**0.484**	**0.564**	**0.383**

discriminator step, and other details will be given in Appendix K.1. As they are orthogonal to each other, we integrate AdvLatGAN-z with AdvLatGAN-qua (i.e. AdvLatGAN-qua+) and include it in comparison. The iteration step size ϵ of AdvLatGAN-z is set to 0.05 and we conduct 20 steps each time. Our method achieves a notable improvement compared to that without the latent space transform strategy. AdvLatGAN-qua+ achieves the best gain on IS in WGAN STL-10 setting from 6.51 to 8.57 and FID in WGAN-div setting from 37.7 to 23.0.

Table. 6 presents experimental results on larger scale datasets including LSUN Church [57], CelebA [58] and ImageNet [59], using WGAN-GP and SNGAN as backbones. We adopt FID, density and coverage as the evaluation metrics. We include AdvLatGAN-qua and AdvLatGAN-qua+ in the comparison. The number of latent iterations during training is set as 1 per discriminator step, and other details will be given in Appendix K.1. The iteration step size ϵ of AdvLatGAN-z is set to 0.01 for SNGAN and 0.002 for WGANGP and we conduct 100 steps each time. AdvLatGAN-qua+ has achieved the best performance gain on FID in SNGAN LSUN-64 setting from 11.961 to 7.285.

AdvLatGAN-div for Diversity Improvement. We test on Cifar-10 and STL-10 for conditional generation and we adopt FID, density and coverage as the metrics, respectively for the entire set of generated images and for those in each label. We test AdvLatGAN-div and AdvLatGAN-div+

Table 6: Evaluation on larger-scale data.

Data	Methods	FID ↓	Density ↑	Coverage ↑
LSUN-64	WGANGP	14.079 ± 0.192	0.747 ± 0.013	0.897 ± 0.005
	WGANGP-qua	12.415 ± 0.028	0.755 ± 0.001	0.909 ± 0.003
	WGANGP-qua+	**10.353 ± 0.257**	**0.765 ± 0.011**	**0.926 ± 0.021**
	SNGAN	11.961 ± 0.331	1.059 ± 0.014	0.925 ± 0.003
	SNGAN-qua	9.917 ± 0.104	**1.078 ± 0.033**	0.939 ± 0.002
	SNGAN-qua+	**7.285 ± 0.029**	1.063 ± 0.003	**0.963 ± 0.002**
LSUN-128	WGANGP	14.180 ± 0.583	0.754 ± 0.047	0.835 ± 0.007
	WGANGP-qua	12.581 ± 0.145	0.851 ± 0.014	0.878 ± 0.013
	WGANGP-qua+	**11.093 ± 0.210**	**0.869 ± 0.004**	**0.914 ± 0.004**
	SNGAN	16.078 ± 0.193	0.946 ± 0.035	0.863 ± 0.003
	SNGAN-qua	14.277 ± 0.035	1.097 ± 0.052	0.869 ± 0.004
	SNGAN-qua+	**11.244 ± 0.396**	**1.133 ± 0.068**	**0.908 ± 0.004**
CelebA-64	WGANGP	19.834±0.398	0.247±0.017	0.596±0.017
	WGANGP-qua	18.972±0.174	0.246±0.005	0.602±0.005
	WGANGP-qua+	**17.748±0.285**	**0.262±0.012**	**0.631±0.003**
	SNGAN	19.490±0.473	0.295±0.002	0.612±0.750
	SNGAN-qua	18.255±0.209	**0.301±0.006**	0.632±0.002
	SNGAN-qua+	**17.213±0.104**	0.279±0.007	**0.639±0.008**
CelebA-128	WGANGP	25.208±0.409	0.204±0.005	0.505±0.015
	WGANGP-qua	22.376±0.181	0.247±0.007	0.579±0.012
	WGANGP-qua+	**21.374±0.361**	**0.256±0.012**	**0.597±0.008**
	SNGAN	22.940±0.092	**0.467±0.004**	0.649±0.004
	SNGAN-qua	22.476±0.023	0.462±0.006	0.651±0.005
	SNGAN-qua+	**20.235±0.402**	0.414±0.008	**0.668±0.005**
ImageNet	WGANGP	78.150±0.298	0.200±0.002	0.289±0.005
	WGANGP-qua	73.677±0.576	0.242±0.005	0.322±0.010
	WGANGP-qua+	**71.227±0.444**	**0.251±0.002**	**0.333±0.004**
	SNGAN	98.344±0.758	0.188±0.003	0.213±0.007
	SNGAN-qua	79.087±0.546	0.207±0.003	0.266±0.007
	SNGAN-qua+	**74.643±0.844**	**0.209±0.009**	**0.288±0.009**

compared to the baseline MSGAN. The results are shown in Table 5. The proposed method outperforms MSGAN reflected by all three metrics. Note that the models are trained on the overall set and for each label the optimization may not guarantee targeted enough guidance (there may exist trade-offs between optimization for different data), thus the improvement for each label may not be so significant but still shows superiority. AdvLatGAN-div+ achieves the best overall performance gain on FID from 30.225 to 26.169, density from 0.353 to 0.431 and coverage from 0.455 to 0.54.

5 Conclusion and Broader Impact

This work analyzes GANs from the continuous mapping perspective and notes that lifting the overall generative performance requires a twofold effort including latent distribution transform and mapping improvement. Adversarial sample mining techniques are introduced to explore latent space and novel training pipelines are derived to improve the generative mapping. The proposed AdvLatGAN has shown promising power in both quality and diversity. Our technique is basically orthogonal to existing mainstream methods. For its limitation, it remains open for how to effectively combine the proposed two techniques for diversity and quality. For potential negative social impact, fake content by the generation models including ours shall always be carefully treated to avoid abuse.

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