AC-GC: Lossy Activation Compression with Guaranteed Convergence

Abstract

The memory-intensive process needed to train Deep Neural Networks (DNNs) can lead to poor performance on parallel devices (e.g., GPUs) or decreased accuracy due to restricting the batch size. Previous attempts to address this issue, using lossy compression and offloading of activations, rely on expensive hyperparameter search to achieve a suitable trade-off between convergence and compression. There is no guarantee that the tuned compression rates in these approaches will adapt well to other models. Our key insight is to use recent developments on Stochastic Gradient Descent convergence to prove an upper bound on the expected loss increase when training with compressed activation storage. We then express activation compression error in terms of this bound, allowing the compression rate to adapt to training conditions automatically. When combined with error-bounded methods, our approach achieves $15.5\times$ compression on CIFAR10/ResNet50 versus $11.0\times$ for the best manually tuned approach. Our method is suitable for any model, layer, and dataset, with an average accuracy change of 0.10%.

1 Introduction

Stochastic Gradient Descent (SGD) has proven efficient and effective for optimizing DNNs and Convolutional Neural Networks (CNNs). However, due to deeper and automatically generated networks [18, 20, 40, 48], improvement of accuracy has caused a rapid increase in training memory requirements, which are dominated by the temporary storage of activations between the forward and backward pass of the back-propagation algorithm [41, 44]. Reducing memory consumption leads to faster training and, thus, more effective research of DNN models and applications. However, doing this by decreasing the batch size has many drawbacks. On parallel processors, such as GPUs, a small batch size can lead to poor compute saturation, and reduced training throughput [43]. Smaller batch sizes also introduce errors that impact convergence and accuracy [16]. Over 50GB of memory is required to train some networks, e.g., GPIPE [20].

Many works have examined reducing activation storage overheads. Lossy compression of activations in memory can reduce memory footprint without network modifications [5, 12, 23, 25]. Error bounded lossy compression (EBC) [25] has bounded activation error, however, uses an empirical study to select an error target. Activations can also be offloaded to an external memory (e.g. CPU DRAM), using either an uncompressed link [29, 41] or compressed link [12, 42]. Activation compression and offloading have performance overheads from 5% to 60% [12, 23, 25, 41]. Reduced precision training has the side effect of reducing activation size [7, 47, 52]. Finally, restructuring networks to be reversible [15] or efficient scheduling of network layers [6] can reduce memory use.

Prior lossy and reduced precision approaches [5, 7, 12, 23, 47, 52] utilize hyperparameter searches or hand-tuning to determine compression rates, which increases training time and have the potential to select poor compression/accuracy trade-offs. Ideally, an activation compression method has

high compression and minimal decrease in trained accuracy. Tuning to achieve this is prohibitively expensive, for instance, selecting a fixed-point integer (fixpoint) compression rate for ImageNet/ResNet50 using Grid Search uses 16 training runs (Figure 1). Using Successive-Halving [24] can decrease training time, however even with aggressive resource allocations (e.g. 24 GPU-days, Figure 1) total training time is still high. With low resource settings, methods such as SuccessiveHalving [24] and Hyperband [33] allocate little time to some configura-

Figure 1: Activation compression rate search cost for ImageNet/ResNet50 [18]. Each box indicates a different compression from 1- to 16-bit fixpoint.

tions, increasing the likelihood that compression artifacts [5, 23] can be missed, resulting in poor accuracy. Additionally, when tuning hyperparameters, lossy compression makes it difficult to determine the cause of degraded accuracy. Finally, prior compression methods have an unknown impact on convergence behavior.

In this work, we present a framework for lossy Activation Compression with Guaranteed Convergence (AC-GC). To our knowledge, our work is the first to prove convergence bounds on SGD with activation compression. Our method involves allowing an increase in the bound on the expected loss, which we trade-off for increased compression. We formulate this as a constrained optimization problem: maximizing compression subject to a bounded increase in loss. Doing so allows using a single hyperparameter to correlate convergence bounds with the activation error, which creates compression methods that are iteration, network, and dataset agnostic. Our contributions:

- We prove convergence bounds on SGD under error bounded activation compression.

- We express activation compression and convergence as a constrained optimization problem and analyze the activation error tolerance of common DNN layers within this framework.

- We combine these error bounds with fixpoint, image, and error bounded compression, to create methods with guaranteed convergence and zero hyperparameter tuning.

2 Preliminaries

DNNs are commonly used on problems involving a sum, for instance, minimize the total error on a set of training images. The loss $\mathcal{L}$ for such a problem takes the form

$$\mathcal{L}(\phi) = \sum_n f(\phi, X_n) \tag{1}$$

where f represents the loss of one example input X_n with weights ϕ.

Stochastic Gradient Descent (SGD) is typically used to optimize these finite sums, using the iteration

$$\phi^{(t+1)} = \phi^{(t)} - \alpha \nabla_\phi f(\phi^{(t)}, X_{n_t}) \tag{2}$$

where α is the learning rate, t is the iteration, and $\nabla_\phi f$ represents the gradient of f with respect to ϕ. n_t is a randomly chosen training example index from the distribution over n such that $\mathbb{E}[\nabla_\phi f(\phi^{(t)}, X_{n_t})] = \nabla_\phi \mathcal{L}(\phi^{(t)})$.

Figure 2a shows the computation graph for the back-propagation [44] algorithm for a single DNN layer without compression. Back-propagation is often used as it allows efficient calculation of parameter gradients at the expense of storing activations [44]. A DNN layer is any linear or non-linear function, e.g., a convolution or ReLU activation. The functions `fwd`, `bwd_param`, `bwd_act` are algorithmic implementations of the layer function and the gradients w.r.t. ϕ and X. In the forward pass, each layer calculates an output activation $Y = \texttt{fwd}(X)$ which is fed to subsequent layers. These activations are temporarily stored after use to avoid recalculating them in the backward pass. In the backward pass, parameter gradients and activation gradients are calculated using `bwd_param` and `bwd_act`. Parameter gradients are used to update the parameters (Eqn. (2)), and activation gradients are sent downward to the next layer. Depending on the layer type and its derivatives, the `bwd_param` and `bwd_act` functions may require activations to be stored. For example, it is computationally

Figure 2: Computation graph for training of a DNN layer. Activations are a) stored between the forward (left) and backward pass (right) or b) compressed (C) in the forward pass, and decompressed (D) in the backward pass. Red indicates paths potentially affected by compression errors.

efficient to store the input X for convolution layers [38, 49]. The many layer types place a diverse set of constraints on activation storage.

Activation compression addresses one of the most significant contributors to memory consumption in DNNs. In the forward pass, an activation can be lazily compressed after its last usage (C, Figure 2b). Eagerly compressing activations would require storing both a compressed and uncompressed copy until its last use. In the backward pass, activations are decompressed before their first use (D, Figure 2b). The backward pass begins only after the forward pass is completed for all layers, resulting in a large reuse distance for stored activations. Compression can thus be performed off the critical path, resulting in memory savings with low performance overheads.

We denote the uncompressed activation as $X = (x_{nchw}) \in \mathbb{R}^{N \times C \times H \times W}$, where N, C, H, and W represent the batch size, channel, height and width, respectively. In the uncompressed backward pass, gradients are calculated from the saved activations, parameters, and gradients from the upward layer (Figure 2 with a); we write this as $\nabla_\phi f(\phi, X) = \texttt{bwd\_param}(X, \phi, \nabla_Y f(\phi, X))$. We model lossy compression between the forward and backward pass as an independent perturbation on each value in the activation, $\Delta X \in \mathbb{R}^{N \times C \times H \times W}$. Thus, in the compressed backward pass, the perturbed activation is $X + \Delta X$. We denote the approximate gradient resulting from lossy error as $\hat{\nabla}_\phi f(\phi, X) := \texttt{bwd\_param}(X + \Delta X, \phi, \nabla_Y f(\phi, X))$, and the corresponding gradient error as $\Delta \nabla_\phi f(\phi, X) := \hat{\nabla}_\phi f(\phi, X) - \nabla_\phi f(\phi, X)$.

3 Guaranteed Convergence

This section details how gradient error $\Delta \nabla_\phi f(\phi, X)$ impacts convergence of SGD. Following this, the lossy compression error ΔX can be expressed in terms of the gradient error, and the compression rate for many methods can be determined. For example, the bitwidth b of fixpoint compression of an activation with range $(-1, 1)$ is

$$b \geq -\log_2 |\Delta x_{nchw}| + ... \tag{3}$$

where the remaining terms are constants determined by the rounding mode, sign, etc. Any compression method with bounded activation error for a given rate can be combined with the error bounds from this work to guarantee convergence (Sections 3.2 and 4).

3.1 SGD Convergence

We will briefly summarize the convergence of SGD under uncompressed conditions from [26]. Consider training using t iterations of SGD with loss $\mathcal{L}(\phi^{(t)})$, with a constant learning rate α and initial point $\phi^{(0)}$. We assume that $\mathcal{L}$ has an optimal point $\phi^{(*)}$ and satisfies $\mathbb{E}[\|\nabla_\phi f(\phi, X_{n_t})\|^2] \leq V^2$ for all ϕ and some V^2. We refer to V^2 as the variance. With the additional assumptions and problem-defined constants C_1 and C_2, Karimi et al. [26] demonstrate that the expected error at iteration t is

$$\mathbb{E}[\mathcal{L}(\phi^{(t)}) - \mathcal{L}(\phi^{(*)})] \leq (1 - C_1\alpha)^t (\mathcal{L}(\phi^{(0)}) - \mathcal{L}(\phi^{(*)})) + C_2\alpha V^2 \tag{4}$$

Initially when training, fast convergence occurs as $(1 - C_1\alpha)^t$ approaches zero (Figure 3a). Later in training, $C_2\alpha V^2$ dominates, resulting in an approximately constant expected error (Figure 3b).

Figure 3: SGD convergence behavior. a) and b) without compression, c) this work, and d) ResNet50 training with $\alpha = 0.25$ and fixpoint activation compression (average over five runs, shaded indicates the minimum and maximum training loss).

Figure 4: 1D Example for the relationship between the error bound, bounding function, and gradient error for an activation error Δx. Shaded region satisfies $D(\Delta x) \leq \frac{e^2 V^2}{2}$.

Many DNN classes fall under this progress bound as it uses relatively weak assumptions and does not require a convex f. DNNs using ReLU activations are Lipschitz continuous [50], and those with an L2 loss are piecewise strongly convex, which implies that the required Polyak-Łojasiewic condition is satisfied locally [36]. Networks this does not apply to could use another progress bound [3, 26, 37].

3.2 Compressed Convergence

Lossy compression trades accuracy for compression and can be empirically observed with fixpoint compression on CIFAR10/ResNet50 (Figure 3d, Section 6). Our method functions by *allowing* the loss to increase by some multiplicative error $(2 + e^2)$, and determining how much compression can be extracted from the change (Figure 3c). Using the result from Karimi et al. [26], this translates into a bound on the compressed gradient, and thus gradient error. Finally, for each network layer we derive an activation error $\Delta X^{(*)}$ which satisfies this bound. e^2 becomes the sole hyperparameter in our method, and selection determines the maximum increase in loss, and the compression rate.

Figure 4 illustrates the relationship between activation error and gradient error. The maximum gradient error $e^2 V^2/2$ corresponds to the $(2 + e^2)$ loss bound (Theorem 1). There may be multiple regions where the gradient error is below $e^2 V^2/2$, which would require iterative solvers to determine suitable activation errors. To apply our technique in practice we introduce a convex function $D(\Delta X) \geq \|\Delta \nabla_\phi f(\phi, X)\|$, which provides a flexible proxy for the gradient error. We can use $D(\Delta X)$ to obtain an activation error, $\Delta X^{(*)}$, which satisfies the bound on compressed training loss. This is formally defined in Theorem 1.

Theorem 1. *Given f which obeys (4), and a convex function $D(\Delta X)$ which bounds the gradient error from above for all X, ϕ, and ΔX:*

$$\|\Delta \nabla_\phi f(\phi, X)\|^2 \leq D(\Delta X) \tag{5}$$

then any solution $\Delta X^{(*)}$ to $D(\Delta X^{(*)}) \leq \frac{e^2 V^2}{2}$ satisfies

$$\mathbb{E}[\|\hat{\nabla}_\phi f(\phi, X_{n_t})\|^2] \leq (2 + e^2)V^2 \tag{6}$$

assuming that $\mathbb{E}[\|\Delta \nabla_\phi f(\phi, X_{n_t})\|] = 0$ for all ϕ, with positive value e^2, and variance V^2 satisfying $\mathbb{E}[\|\nabla_\phi f(\phi, X_{n_t})\|^2] \leq V^2$. All expectations are taken over the training examples n_t.

Proof: See Appendix A.

Figure 3c shows the impact of this theorem on training. The variance of the compressed gradients is below $(2 + e)V^2$ when compression is used with activation errors satisfying $D(\Delta X^{(*)}) \leq e^2V^2/2$. If $\mathcal{L}$ follows (4) before compression, the variance in (4) increases with compression, and thus the expected error as $t \to \infty$ increases to $(2 + e^2)C_2\alpha V^2$.

4 Framework for Activation Compression

For our evaluation of AC-GC, we develop activation error bounds for various commonly used DNN layers and apply them to several recent networks. This section summarizes bounds for common layers, and derivations and additional layer bounds are provided in Appendix B. Calculating compression error from the gradient error bound $e^2V^2/2$ requires expressing and solving for the compression/convergence trade-off. We tackle this by formulating the trade-off as a constrained optimization problem: maximizing the compression subject to bounded gradient error. The problem must be solved once per layer type.

Using the method of Lagrange multipliers, we can solve for activation error using the system

$$\nabla B(\Delta X) = \lambda \nabla D(\Delta X) \quad \text{subject to} \quad D(\Delta X) \leq \frac{e^2V^2}{2} \tag{7}$$

where $B(\Delta X)$ is a convex function that measures compression rate, and λ is the Lagrange multiplier. Given the convexity of $D(\Delta X)$, the constraint $D(\Delta X) \leq e^2V^2/2$ defines a region of permissible ΔX values (shaded, Figure 4). Because $B(\Delta X)$ is also convex, the maximum value over this region must occur along the boundary. Hence, maximizing $B(\Delta X)$ subject to $D(\Delta X) = e^2V^2/2$ also yields the maximum over the entire region. This implies that any $\Delta X \in [0, \Delta X^{(*)}]$ also satisfies (6).

Many compression methods use a variation of fixpoint. Hence, we select B to measure the number of bits removed from the activation when compressed with reduced precision fixpoint (8). We ignore clipping, however, rounding mode and sign are constant factors that do not affect the result. The target compression method loosely influences the objective, hence, non-fixpoint methods may fare better with another error objective.

$$B(\Delta X) := \sum_{n,c,h,w}^{N,C,H,W} \log |\Delta x_{nchw}| \tag{8}$$

To derive AC-GC error bounds for DNN layers not presented in this work, one can:

1. Derive $\|\Delta \nabla_\phi f(\phi, X)\|^2$ for the layer type

2. Choose a suitable convex bounding function, $D(\Delta X) \geq \|\Delta \nabla_\phi f(\phi, X)\|^2$

3. Obtain the maximum error $\Delta X^{(*)}$ by solving (7) using the method of Lagrange multipliers

For the sake of brevity, we will summarize the notation, assumptions, and AC-GC error bounds for fully connected, convolution, and batch normalization layers (Table 1). We aim to locate closed-form solutions with low computation overheads, although tighter bounding functions likely exist. Henceforth we omit arguments of f and use the following definitions: Batch size N, input channels C, output channels K, input and output activations X and Y, and compression error ΔX.

A) Fully Connected: Table 1A relates the error for guaranteed convergence with compression error for a fully connected layer, with weights $\phi = (\phi_{kc}) \in \mathbb{R}^{K \times C}$, input activation $X = (x_{nc}) \in \mathbb{R}^{N \times C}$, and output activation gradient $\nabla_Y f = (\partial f/\partial y_{nk}) \in \mathbb{R}^{N \times K}$. As the error bound $(e^2V^2/2)$ decreases, the compression must decrease to compensate. All activations for a fully connected layer have the same error tolerance.

B) Convolution: Convolution with no padding follows a similar trend to linear layers, with the addition of stride T, a filter size of $R \times S$, and increased dimensions $X = (x_{nchw}) \in \mathbb{R}^{N \times C \times H \times W}$ and $\nabla_Y f = (\partial f/\partial y_{nkhw}) \in \mathbb{R}^{N \times K \times H \times W}$. We assume an average usage of activations due to stride, as uneven usage leads to uneven compression, which would require tracking per-element compression rates. Comparing linear and convolution reveals that convolutions have a lower error tolerance due to the increased number of activations (HW) and weights (RS).

Table 1: Guaranteed convergence equations for common network layers. See Appendices for full derivations and assumptions. Empty sums are over all indicies, i.e. $\sum := \sum_{n,c,h,w}^{N,C,H,W}$.

QUANTITY	A) FULLY CONNECTED	B) CONVOLUTION	C) BATCH NORMALIZATION
$D(\Delta X) :=$	$\|\nabla_Y f\|^2 \|\Delta X\|^2$	$\dfrac{RS}{T^2} \|\nabla_Y f\|^2 \|\Delta X\|^2$	$\sum \dfrac{2\gamma_c^2 g_c^2}{N^2 H^2 W^2 \sigma_c^4} \Delta x_{nchw}^2$
$\Delta x_{nchw}^{(*)2} =$	$\dfrac{e^2 V^2}{2NC\|\nabla_Y f\|^2}$	$\dfrac{e^2 V^2 T^2}{2RSNCHW\|\nabla_Y f\|^2}$	$\dfrac{e^2 V^2 NHW \sigma_c^4}{C\gamma_c^2 g_c^2}$

To fully cover cases encountered in CNNs, we also derive error bounds for cases where activation errors affect multiple convolution layers (e.g., in ResNets [18]).

C) Batch Normalization: Batch normalization [22] re-normalizes the activation from per-channel standard deviation $\sigma \in \mathbb{R}^C$ to a learned $\gamma \in \mathbb{R}^C$. There is a different dependence on activation error from convolution and linear layers. Instead of causing errors in the parameter gradient $\nabla_\gamma f$ exclusively, activation error propagates to the activation gradient $\nabla_X f$ and then to all subsequent layers in the network. To avoid bounding all weights in the network, we isolate the layer and bound the convergence of the batch normalization activations using

$$\|\Delta \nabla_X f\|^2 \leq \frac{e^2 V^2}{2} \tag{9}$$

Arriving at a closed-form solution further requires a bound on the parameter gradient error within the layer using positive values $(g_c^2) \geq (\hat{\nabla}_\gamma f)^2$ (Appendix B). Although not observed for the networks in this work, as network parameter gradients are not directly bounded, the convergence bounds on networks with batch normalization may be violated.

ReLU, Dropout, Max Pooling, and Summation: Summation does not require storage of any activation, and the remaining layers only require a bitmask to calculate their respective gradients. For instance, ReLU requires storage of the bitmask $X \geq 0$ [12, 23]. As these layers have an efficient lossless high compression method available, we do not analyze them.

5 Practical Automatic Lossy Compression

Using the AC-GC error bounds, we create convergence bounded compression methods with automatic compression rates, collectively referred to as AutoX. The first two methods (AutoQuant and AutoCuSZ) adapt scaled fixpoint [12] and error-bounded compression [25], which have bounded errors for a given compression rate. The errors for these methods are unbiased provided that unbiased rounding to fixpoint is used [4, 25]. The third method (AutoJPEG) uses lossy JPEG compression [12]. We bound JPEG error by means of an empirical error-compression relationship using flat Discrete Quantization Tables and sampled training data from CIFAR10/ResNet50 [18]. We follow these methods with lossless Zero Value Compression [42] to better compress sparse activations, creating AutoQuantZ and AutoJPEGZ.

As all AutoX we explore use some form of fixpoint, we can express activation error in terms of bits. For any layer type, (3) can describe the relationship between bitwidth b and the convergence bound as

$$b \geq -\log_2 |\Delta x_{nchw}| + ... = -\log_2 |e| - \log_2 \|\nabla_\phi f\| + ... \tag{10}$$

Two issues with using AC-GC in a compression method are: 1) the various norms required are computationally expensive, and 2) the formulation assumes exact gradient information is available during the forward pass. We address both issues by statistically estimating activation error bounds. Instead of evaluating at every iteration, statistics are calculated at the end of every *recalculation interval*, specified in iterations. In the forward pass, a *summary* (mean or maximum) of the last ten recalculations is used when calculating the errors. This also allows approximating $V^2 \approx \|\nabla_\phi f\|^2$. Although some quantities are available in the forward pass, we estimate all of the activations, parameters, and gradients to avoid performing norm calculations at every iteration. Despite norms being estimated, we do not observe that the convergence bound (6) is violated for any network examined. A few training iterations can be used to verify correctness of the norm estimates (Figure 5c).

Figure 5: a-b) MNIST/LeNet average loss at epoch 10. Shaded regions indicate the minimum and maximum loss over five runs. c) Gradient measurements for the first convolution for ImageNet/ResNet18 using dual training. Clusters indicate the first 50 iterations of every ten epochs.

6 Evaluation

We examine activation compression by modifying the Chainer framework [49] to compress and decompress activations during training. We measure compression rates every 100 iterations, and otherwise perform paired compression/decompression to maintain the highest performance for our experiments. We focus our analysis on CNNs with image and text datasets, as they have large activation memory requirements, but avoid the largest networks [20, 48] due to limited resources.

For ImageNet [9], CIFAR10 [2] and Div2K [1], we use SGD and 0.9 momentum for VGG16 [46], ResNets (RN18 and RN50) [18], Wide ResNet (WRN) [54], and VDSR [27]. IMDB [35] is trained using ADAM on a CNN extractor [49]. All image datasets are augmented with random sizing, flip, and crop, as well as whitening and PCA for ImageNet [28], and 8×8 cutout for CIFAR10 [10]. Learning rates, batch sizes, and epochs are 0.05, 128, 300 (CIFAR10, [45]), 0.1, 64, 105 (ImageNet, [53]), 0.1, 32, 110 (Div2K, grid search), and 0.001, 64, 20 (IMDB, [49]).

All forward and backward pass calculations use floating-point, using activations that have been compressed and decompressed between the two passes. Baseline refers to uncompressed training, i.e., 32-bit floating-point activations. GridQuantZ uses the same implementation of AutoQuantZ, however, uses grid search over bit widths of $2, 4, 6, ...16$ bits, and selecting the lowest with an accuracy within 0.1% of the baseline. SuccessiveHalving [24] and Hyperband [33] produce similar accuracy/compression to grid search but take less time. Unless otherwise stated, all experiments use $e^2 = 1$, parameter estimates from the mean of a ten entry window, and a recalculation interval of 100 iterations. Appendices C and D contain additional detail on hyperparameters and implementations.

6.1 Parameter Sensitivity

We isolate the impacts of parameter estimation and e selection by training LeNet [31] on MNIST [30], and RN18 [18] on ImageNet [9]. We train MNIST to convergence by using SGD with no momentum, a learning rate of 0.001, a batch size of 64, and 10 epochs.

The effect of e, recalculation interval, and summary method are evaluated by training MNIST/Lenet with different configurations of AutoQuant (AQ) (Figures 5a and b). Decreasing e (which increases bitwidth) causes the loss to increase, however, the average loss does not violate the bound in Theorem 1 (Figure 5a). All networks examined have loss changes below 2% and validation score changes below 0.5%, which demonstrates that AC-GC error bounds are not violated. Both interval and summary method have a minimal impact on the training loss for MNIST (Figure 5b). As there is an insignificant change in loss, we use the mean for AC-GC as it has higher compression.

We evaluate ImageNet/ResNet18 using a dual training approach to ensure the correctness of parameter estimation (Figure 5c). This involves training using AutoQuant, while evaluating the *true* weight gradients $\nabla_\phi f$ offline and comparing against their compressed counterpart $\hat{\nabla}_\phi f$. The ratio is ≈ 1 for the duration of training, which does not violate the bound for $e^2 = 1$ (i.e., ≤ 3). The mean ratio is less than one, likely due to decreased activation variance from compression to a discrete set of values. We observe similar behavior for the other layers in the network (not shown).

Table 2: Accuracy/Power Signal Noise Ratio (PSNR) and compression rate (bracketed) for fixpoint with grid search (GridQuantZ), AutoX methods, and JPEG-ACT (optL5H from [12]), averaged over 5 runs. The highest accuracy and compression are bolded. Trained using 450 GPU-days (RTX 2080 Ti).

MODEL	BASE	AUTO QUANTZ	AUTO CUSZ	AUTO JPEGZ	JPEG-ACT[12]	GRID QUANTZ
CIFAR10 % TOP-1 TEST ACCURACY						
VGG	93.6	**93.5** (7.4×)	**93.5** (9.4×)	92.9 (**12.5**×)	92.4 (11.9×)	**93.5** (6.3×)
RN50	94.9	**95.0** (4.2×)	94.7 (**15.5**×)	94.3 (9.2×)	94.4 (7.5×)	**95.0** (5.7×)
WRN	95.8	95.9 (6.5×)	95.8 (**14.6**×)	95.3 (11.7×)	94.2 (10.9×)	**96.0** (7.6×)
DIV2K BEST VAL. PSNR						
VDSR	36.1	**36.1** (5.1×)	35.8 (**25.2**×)	**36.1** (7.9×)	35.4 (9.1×)	36.0 (6.7×)
IMDB % BEST VAL. ACCURACY						
CNN	61.44	61.6 (12.2×)	**61.8** (**19.3**×)	61.4 (11.2×)	–	61.7 (16.5×)
AVERAGE CHANGE AND COMPRESSION RATIO						
ALL	0	+0.1 (7.1×)	−0.1 (16.8×)	−0.4 (10.5×)	−1.0 (9.9×)	+0.1 (8.6×)

Table 3: ImageNet top-1 center crop val. accuracy and compression rate (bracketed) for a single run. The highest accuracy and compression are bolded. Trained using 150 GPU-days (RTX 2080 Ti).

MODEL	BASE	AUTO QUANTZ	JPEG-ACT[12]	GRID QUANTZ
RN18	68.7	68.4 (5.4×)	67.3 (7.2×)	**68.7** (**9.1**×)
RN50	72.3	72.1 (4.9×)	71.6 (**5.9**×)	**73.0** (4.8×)
AVERAGE	0	−0.2 (5.2×)	−1.1 (6.6×)	+0.3 (6.9×)

6.2 CIFAR10, Div2K and IMDB

We compare the AutoX methods with fixpoint grid search (GridQuantZ), and with prior works on lossy JPEG compression [12] (Table 2). Grid search requires oracle knowledge of the baseline, and 8× the training iterations of any other method in Table 2. Compared to GridQuantZ, AutoQuantZ uses a single run of training, and provides a similar compression rate of 7.1×. AutoCuSZ has a compression 1.70× higher than JPEG-ACT, while maintaining accuracy to within 0.1 of the baseline on average. With a suitable error bound, CuSZ can extract significant compression from zeros and spatial information. AutoJPEGZ vs. JPEG-ACT demonstrates that using AC-GC error bounds gives higher accuracy and compression than using heuristics to select JPEG hyperparameters. In general, we find that using $e^2 > 1$ decreases accuracy, leaving little reason to modify it.

6.3 ImageNet

Table 3 examines training on ImageNet with ResNets. GridQuantZ achieves a significantly higher compression on ResNet18 than AutoQuant. Note that selecting 4-bit for ResNet18 achieves baseline accuracy, however, *increasing* the bitwidth to 6-bit *decreases* the accuracy by 0.5%, and accuracy does not increase to baseline-levels until 10-bit compression. This could be due to a local optimum or good training seed, highlighting the issues with selecting compression rates using hyperparameter search techniques. Using AutoQuantZ provides a bound on how loss can increase when changing compression, despite lower compression. When compared to JPEG-ACT, AutoQuantZ provides 0.79× compression while increasing accuracy by 0.9%. The average accuracy/PSNR change over all datasets is -0.10 (AutoQuantZ for ImageNet and AutoCuSZ otherwise).

6.4 Overheads

The AutoX methods require error bound calculation (common to all methods) and compression. We calculate the average computation overhead for AC-GC error bound calculation as 0.2% floating-point operations (FLOPs) over uncompressed training. This is negligible when compared to compression

Table 4: Comparison with prior works on CIFAR10 (C10) and ImageNet (IN). $\pm$ indicates standard deviation, if available. Accuracy is presented relative to the baseline accuracy of each work.

	AUTO CUSZ	WAGE [52]	GIST [23]	BAA [5]	JPEG-ACT[12]	ULP [47]	EBC [25]
DATASET	C10	C10	IN	C10	C10	C10	IN
MODEL	RN50	VGG16	VGG16	RN152	RN50	RN50	RN50
METHOD	AUTO -CUSZ	8-BIT	16-BIT +CSR	4-BIT +RECALC.	JPEG +ZVC	4-BIT	CUSZ
ACC. (%)	-0.2 ± 0.2	-0.3	$\approx0^1$	-0.1 ± 0.2	-0.1	-0.3	-0.3
COMPR.	$15.5\times$	$4\times$	$2.2\times$	$8\times^2$	$7.5\times$	$8\times$	$11.0\times$

overhead, e.g., 4% for fixpoint [12, 23], 17% for CuSZ [25], or 13% for hardware accelerated JPEG [12]. Compression can be performed in parallel with training which can further decrease overheads.

7 Related Works

We compare AutoCuSZ with the most recent works in activation compression [5, 12, 23, 25] and reduced precision training [47, 52] (Table 4). AutoCuSZ obtains similar accuracy and higher compression than any other work, with the added benefit of not requiring a search over compression rates. BAA [5] also presents a technique of recalculating activations similar to [6], halving memory footprint[2]. Recalculation is an orthogonal method to compression, and can be combined with any technique in Table 4 including the AutoX methods. AutoCuSZ obtains higher compression and accuracy than EBC [25], demonstrating that AC-GC error bounds are better than hand tuning in this case. WAGE [52] and ULP [47] provide lower compression rates and accuracy in exchange for reducing training compute through reduced precision. AutoX methods can potentially be combined with low precision training and other compression techniques to further reduce memory requirements.

Other works that directly address memory can be grouped into scheduling, offloading, and restructuring. Scheduling can be used to recalculate or avoid saving some activations [6, 23]. Offloading methods [29, 41] provide expanded memory at the expense of moderate performance overheads. Restructuring involves reducing the size of the network [19] or making the network reversible [15].

Many works examine techniques to address inference, such as precision reduction [8, 13, 21, 32], compression [11, 17, 51], and sparsification [14, 39]. These methods often increase training memory requirements as variables are added to track added state such as sparsity. Gradient compression during training also increases memory footprint, albeit with decreased synchronization bandwidth for multi-device systems [34].

8 Conclusions

The AC-GC automatic compression methods described in this work provide high compression rates with no hyperparameter tuning. Avoiding hyperparameter search comes at a computational overhead of only 0.2%, many times less than tuning techniques. AC-GC can be further combined with any lossy compression method, layer, or network to guarantee convergence with high activation compression. By lowering training costs, this framework allows for training larger models and faster exploration of the machine learning field's landscape. Detailed derivations, implementations, and algorithms can be found in the supplemental material. Code is available https://anonymous.4open.science/r/1a20254bbe.

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[1] Accuracy change in this work appears to be zero from the accuracy plots presented.
[2] Does not include $2\times$ memory reduction from recalculating activations, which is orthogonal to this work.

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