Stimulative Training of Residual Networks: A Social Psychology Perspective of Loafing

Abstract

Residual networks have shown great success and become indispensable in today's deep models. In this work, we aim to re-investigate the training process of residual networks from a novel social psychology perspective of loafing, and further propose a new training strategy to strengthen the performance of residual networks. As residual networks can be viewed as ensembles of relatively shallow networks (i.e., *unraveled view*) in prior works, we also start from such view and consider that the final performance of a residual network is co-determined by a group of sub-networks. Inspired by the social loafing problem of social psychology, we find that residual networks invariably suffer from similar problem, where sub-networks in a residual network are prone to exert less effort when working as part of the group compared to working alone. We define this previously overlooked problem as *network loafing*. As social loafing will ultimately cause the low individual productivity and the reduced overall performance, network loafing will also hinder the performance of a given residual network and its sub-networks. Referring to the solutions of social psychology, we propose *stimulative training*, which randomly samples a residual sub-network and calculates the KL-divergence loss between the sampled sub-network and the given residual network, to act as extra supervision for sub-networks and make the overall goal consistent. Comprehensive empirical results and theoretical analyses verify that stimulative training can well handle the loafing problem, and improve the performance of a residual network by improving the performance of its sub-networks.

1 Introduction

Since ResNet [1] wins the first place at the ILSVRC-2015 competition, simple-but-effective residual connections are applied in various deep networks, such as CNN, MLP, and transformer. To explore the secrets behind the success of residual networks, numerous studies have been proposed. He et. al [1] exploit the residual structure to avoid the performance degradation of deep networks. Further, He et. al [2] consider that such a structure can transfer any low level features to high level layers in forward propagation and directly transmit the gradients from deep to shallow layers in backward propagation. Balduzzi et. al [3] find that residual networks can alleviate the shattered gradients problem that gradients resemble white noise. In addition, Veit et. al [4] experimentally verify that residual networks can be seen as a collection of numerous networks of different lengths, namely *unraveled view*. Following this view, Sun et. al [5] further attribute the success of residual networks to shallow sub-networks, which may correspond to the low-degree term when regarding the neural network as a polynomial function. Since unraveled view is supported both experimentally and theoretically, we further investigate some interesting mechanism behind residual networks based on this inspiring work. Specifically, we treat a residual network as the ensemble of relatively shallow sub-networks and consider its final performance to be co-determined by a group of sub-networks.

Submitted to 36th Conference on Neural Information Processing Systems (NeurIPS 2022). Do not distribute.

Figure 1: Different residual networks invariably suffer from the problem of network loafing, and deeper residual network tends to have more serious loafing problem. All these networks are trained on CIFAR10 dataset. The horizontal axis means the sampled different sub-networks from ResNetx.

In social psychology, working in a group is always a tricky thing. Compared with performing tasks alone, group members tend to make less efforts when working as part of a group, which is defined as the social loafing problem [6, 7]. Moreover, social psychology researches find that increasing the group size may aggravate social loafing for the decrease of individual visibility [8, 9]. Inspired by these, we find that the ensemble-like networks formed by residual connections also have a similar problem and behavior. As shown in Fig. 1, we can see that, different residual networks invariably suffer from the loafing problem, that is, the sub-networks working in a given residual network are prone to exert degraded performances than these sub-networks working individually. For example, a sub-network ResNet32 in the ResNet56 only has a 46.80% Top1 accuracy, much lower than ResNet32 trained individually with accuracy of 92.63%. Moreover, the loafing problem of deeper residual networks inclines to be more severe than that of shallower ones, that is, the same sub-network in deeper residual networks constantly presents inferior performance than that in shallower residual networks. For example, ResNet20 within ResNet32 has a 55.28% Top1 accuracy, while ResNet20 within ResNet56 (deeper than ResNet 32) only has a 23.17% Top1 accuracy. Such problems have not been addressed in the literature so far as we know. Hereafter, we define this previously overlooked problem as *network loafing*. As social psychology researches show that social loafing will ultimately cause low productivity of each individual and the collective [10, 11], we consider that network loafing may also hinder the performance of given residual network and all of its sub-networks.

In social psychology, there are two commonly used solutions for preventing social loafing within groups: 1) establishing individual accountability by increasing the *individual supervision* and 2) making tasks cooperative by setting up the overall goal [8, 9]. Inspired by this, we propose a novel training strategy for improving residual networks, namely *stimulative training*. In details, for each mini-batch during stimulative training, besides the main loss of the given residual network in conventional training, we will randomly sample a residual sub-network (individual supervision) and calculate the KL-divergence loss between the sampled sub-network and the given residual network (consistent overall goal). This simple yet effective training strategy can relieve the loafing problem of residual networks, by strengthening the individual supervision of sub-networks and making the goals of residual sub-networks and the given residual network more consistent.

Comprehensive empirical analyses verify that stimulative training can solve the loafing problem of residual networks effectively and efficiently, thus improve both the performance of a given residual network and all of its residual sub-networks by a large margin. Furthermore, we theoretically show the connection of the proposed stimulative training strategy and the improved performance of a given residual network and all of its residual sub-networks. Besides, experiments on various benchmark datasets using various residual networks demonstrate the effectiveness of the proposed training strategy. The contributions of our work can be summarized as the following:

- We understand residual networks from a social psychology perspective, and find that different residual networks invariably suffer from the problem of network loafing.

- We improve residual networks from a social psychology perspective, and propose a simple-but-effective stimulative training strategy to improve the performance of the given residual network and all of its sub-networks.

- Comprehensive empirical and theoretical analysis verify that stimulative training can well solve the loafing problem of residual networks.

2 Related Works

2.1 Unraveled View

As one pioneer work to investigate residual networks, [4] experimentally shows that residual networks can be seen as a collection of numerous networks of different length, namely unraveled view. Subsequently, [5] follows this view and further attributes the success of residual networks to shallow sub-networks first. Besides, [5] considers the neural network as a polynomial function and corresponds shallow sub-network to low-degree term to explain the working mechanism of residual networks. Similar to [4] and [5], this paper also investigates residual networks from the unraveled view. Differently, inspired by social psychology, we further reveal the loafing problem of residual networks under the unraveled view. Besides, we propose a novel stimulative training method to relieve this problem and further unleash the potential of residual networks.

2.2 Knowledge Distillation

As a classical method, knowledge distillation [12] transfers the knowledge from a teacher network to a student network via approximating the logits [12, 13, 14] or features [15, 16, 17] output. To avoid the huge cost of training a high performance teacher, some works abandon the naive teacher-student framework, like mutual distillation [18] making group of students learn from each other online, and self distillation [19] transferring knowledge from deep layers to shallow layers. Generally, all these distillation methods need to introduce additional networks or structures, and employ fixed teacher-student pairs. As a comparison, our method does not require any additional network or structure, and the student network is a randomly sampled sub-network of a network. Besides, our method is essentially designed to address the loafing problem of residual networks, which is different from knowledge distillation that aims to obtain a compact network with acceptable accuracy.

2.3 One-shot NAS

One-shot NAS is an important branch of neural architecture search (NAS). Along this direction, [20] trains an once-for-all (OFA) network with progressive shrinking and knowledge distillation to support kinds of architectural settings. Following this work, BigNAS [21] introduces several technologies to train a high-quality single-stage model, whose child models can be directly deployed without extra retraining or post-processing steps. Both OFA and BigNAS aim at simultaneously training and searching various networks with different resolutions, depths, widths and operations. Differently, the proposed method aims at improving a given residual network, thus can be seamlessly applied to the searched model of NAS. As OFA and BigNAS are not designed to solve the loafing problem, their sampling space and supervision signal are also different with the proposed method. More importantly, the social-psychology-inspired problem of network loafing may explain why OFA and BigNAS work.

2.4 Stochastic Depth

As a regularization technique, Stochastic Depth [22] randomly disables the convolution layers of residual blocks, to reduce training time and test error substantially. In Stochastic Depth, the reduction in test error is attributed to strengthening gradients of earlier layers and the implicit ensemble of numerous sub-networks of different depths. In fact, its improved performance can be also interpreted as relieving the network loafing problem defined in this work. The theoretical analysis in this work can be also applied to Stochastic Depth. Besides, for better solving the loafing problem, our method samples sub-networks with ordered depth, and uses an additional KL-divergence loss to provide a more achievable target and make the output of a given network and its sub-networks more consistent.

3 Stimulative Training

3.1 Motivation

Social loafing is a social psychology phenomenon that individuals lower their productivity when working in a group. Based on the novel perspective that a residual network behaves like an ensemble network [4], we find various residual networks invariably exhibit loafing-like behaviors as shown in Fig. 1 and Fig. 4, which we define as network loafing. As social loafing is "a kind of social disease" that will harm the individual and collective productivity [10], we consider network loafing

(a) **Common training** scheme suffers from severe **network loafing** problem

(b) **Stimulative training** scheme can relieve **network loafing** and improve the performance

Figure 2: Illustration of common and stimulative training schemes. Stimulative training can relieve the network loafing problem, and improve the performance of a given residual network (from 77.3% to 81.07%) and all of its sub-networks (e.g., from 60% to 79%). 65% and 75% denote the individual performance of each sub-network.

may also hinder the performance of a residual network and its sub-networks. To alleviate network loafing, it is intuitive to learn from social psychology. There are two common methods for solving social-loafing problem in sociology, namely, establishing individual accountability (i.e., increasing the individual supervision) and making tasks cooperative (i.e., setting up the overall goal) [8, 9]. In order to increase individual supervision, we sample sub-networks in the whole network and provide extra supervision to train each sub-network sufficiently. For the overall goal, we adopt KL divergence loss to constrain the output of sub-networks not far from that of the whole network, which aims at reducing the performance gap and driving the sampled sub-networks to develop cooperatively.

3.2 Training Algorithm

In this subsection, we briefly illustrate the working scheme of the proposed stimulative training strategy, and show its difference from the common training method. As shown in Fig. 2, common training only focuses on optimization of main network, thus suffers from severe network loafing, that is, sub-networks lower their performance when working in an ensemble. For example, as shown in Fig. 2(a) sub-networks within the residual network only has an accuracy of 60% and 70%, much lower than their individual accuracy of 65% and 75%. As a comparison, stimulative training optimizes the main network and meanwhile uses it to provide extra supervision for a sampled sub-network at each training iteration, thus well handles the loafing problem. In the test procedure, our method can adopt the main network or any sub-network as the inference model, thus requiring the same or lower memory and inference cost compared with a given residual network.

Formally, for a given residual network to be optimized, we define the main network as D_m and the sub-network as D_s. All the sub-networks share weights with the main network, and make up the sampling space $\Theta = \{D_s | D_s = \pi(D_m)\}$, where π is sampling operator, usually random sampling. In the training process, we randomly sample a sub-network at each iteration to ensure the whole sampling space can be fully explored. To make the training more efficient and effective, we define a new sampling space obeying ordered residual sampling rule to be discussed in Section 3.3. Denoting θ_{Dm} and θ_{Ds} as weights of the main network and the sampled network respectively, x as the mini-batch training sample and y as its label, $\mathcal{Z}$ as the output of network, the total loss of stimulative training is computed as

$$\mathcal{L}_{mt} = \underbrace{CE(\mathcal{Z}(\theta_{D_m}, x), y)}_{\text{main supervision}} + \underbrace{\lambda KL(\mathcal{Z}(\theta_{D_m}, x), \mathcal{Z}(\theta_{D_s}, x))}_{\text{extra common direction supervision}}, D_s \in \Theta \qquad (1)$$

where the CE and KL are the standard cross entropy loss and KL divergence loss. λ is the balanced coefficient, and CE loss denotes the main supervision for the main network. KL loss provides an extra supervision for the sampled sub-network, and guarantees all sub-networks to be optimized in the same direction with the main network, which can be considered as setting a common goal for the "ensemble network". We use the standard stochastic gradient descent for updating the model, denoted as $\theta_{D_m}^{t+1} = \theta_{D_m}^t - \eta \frac{\partial \mathcal{L}_{ut}}{\partial \theta_{D_m}}$, where η is the learning rate. Thanks to the weight-sharing between

Figure 3: Illustration of ordered residual unraveling rule. Compared with two other sampling strategies, ordered residual sampling can facilitate training and reduce the sampling space to get better main network performance.

sub-networks and the main network, we only need to update θ_{D_m} once for each iteration to optimize both the θ_{D_m} and θ_{D_s}. The pseudo code is shown in Appendix C.1.

3.3 Ordered Residual Sampling

Network loafing is based on the novel view that residual networks can be seen as the ensemble of numerous different sub-networks[4]. It is intuitive to adopt raw unraveled view to design sampling space, namely raw sampling. However, there exist two problems in raw sampling. First, it introduces a mass of single branch sub-networks which are hard to optimize, as shown in the left sub-figure of Fig. 3. Second, with the growth of network depth, the size of sampling space increases exponentially. For a residual stage of n blocks, there are 2^n sub-networks, which constitutes a too large space to explore. Under limited computation resources, it is difficult to provide sufficient supervision to each sub-network, causing insufficient stimulative training.

Therefore, in order to facilitate stimulative training, we re-design two different sampling ways: stochastic residual sampling and ordered residual sampling. Fig. 3 shows a three-block residual network as a simple illustration for three sampling ways. For raw sampling, we obey the raw definition of [4], that means each sub-network is composed of stacked convolution layers. For stochastic residual sampling, we keep the basic structure of residual blocks and skip some blocks randomly. For ordered residual sampling, we also keep the residual structure but skip blocks orderly, (i.e., always skip the last several blocks). We implement these sampling methods for MobileNetV3 [23] on CIFAR-100. Experimental results show that ordered residual sampling performs better than other two methods (by 5.77% and 0.58% respectively). To explain the superiority of ordered residual sampling, we should pay attention to keeping residual structure and ordered sampling. For keeping residual structure, it can drive the network training process easier and improve the final performance [1]. For ordered sampling, it can noticeably reduce the size of sampling space (from $O(2^n)$ to $O(n)$), making it possible to train each sub-network sufficiently. Besides, all deep networks with residual connections can be approximated by neural differential equations [24], which treat discrete network layers as continuous and regard the layer output as the result of adding an integral to the layer input. From this perspective, ordered sampling will maintain the continuity of residual networks. Because of these outstanding features, we will adopt ordered residual sampling in the following experiments.

4 Empirical Analysis

In this section, we conduct extensive experiments to analyze and compare the proposed stimulative training and the common training strategy in detail. We first illustrate the loafing problem of residual networks with different training strategies. We further demonstrate statistical characteristics of the performance of the trained residual network and all of its sub-networks. Then, we show

| (a) 6 sub-networks | (b) 48 sub-networks | (c) 144 sub-networks |

Figure 4: Stimulative training using 6, 48, and 144 sub-networks. With more sub-networks involved, the network loafing problem could be relieved better, and the performance of the residual network and all of its sub-networks could be improved more significantly. We train MobileNetV3 with different schemes on CIFAR100 dataset.

| (a) Maximum Value | (b) Mean Value | (c) Standard Deviation |

Figure 5: (a) Maximum, (b) mean value and (c) standard deviation when training MobileNetV3 with different strategies on CIFAR100 dataset. Sampling 0 sub-networks denotes the common training strategy. Stimulative training with more sub-networks can provide higher maximum, mean and lower standard deviation.

the performance drop when destructing trained residual networks at test time, including deleting individual layers, deleting more layers and permuting layers. Besides, we also record the KL distance between a given residual network and all of its sub-networks in the whole training process. For the convenience of analysis, we always use a NAS-searched model MobileNetV3 [23] as the residual network and train it on CIFAR100, unless otherwise specified. The detailed experimental settings can be found in Appendix C.2.

4.1 Experiment 1: Checking the loafing problem of residual networks with different training strategies

First, we find that the NAS-searched residual network MobileNetV3 still suffers from the loafing problem. As shown in Fig. 4, when applying the common training strategy to MobileNetV3, the sub-networks from MobileNetV3 (blue solid circle) have much lower accuracies than the same sub-networks individually trained (green five-pointed star), and the performance gap increases when the size of the sub-network decreases. Second, we show that the proposed stimulative training strategy can well handle the loafing problem. As shown in Fig. 4(c), when applying the stimulative training strategy to MobileNetV3, the sub-networks from MobileNetV3 (red five-pointed star) have even better performance than the same sub-networks individually trained (green five-pointed star). More interestingly, as shown in Fig. 4(a), even when we apply stimulative training with 6 sub-networks (red five-pointed star) to MobileNetV3, the performance of all the sub-networks (red solid circle) can be also greatly improved compared to that of common training (blue solid circle). Besides, As shown in Fig. 4, with more sub-networks involved in stimulative training, the network loafing problem could be relieved better, and the performance of a given residual network and all of its sub-networks could be improved more significantly. More similar results of different datasets and residual networks can be found in Appendix A.

4.2 Experiment 2: Collecting statistical characteristics of the performance of all residual sub-networks

To demonstrate that stimulative training can improve the performance of a given residual network and all of its sub-networks, we collect various statistical characteristics of the performance of all residual

Figure 6: Top1 accuracy drop when (a) deleting one layer, (b) deleting more layers and (c) permuting layers from MobileNetV3 with stimulative/common training on CIFAR100 dataset. Stimulative training can provide stronger robustness in resisting various network destruction operations than common training.

sub-networks after the stimulative training and common training. As shown in Fig. 5, MobileNetV3 with common training (i.e., sample 0 sub-networks) has the lowest maximum value, mean value, and the highest standard deviation, which is mainly caused by the network loafing problem. As a contrast, MobileNetV3 with stimulative training (i.e., sample 144 sub-networks) has the highest maximum value, mean value, and the lowest standard deviation. Moreover, we can see that, MobileNetV3 using stimulative training with more sub-networks can usually provide higher maximum value, mean value and lower standard deviation. All these results indicate that stimulative training can improve the performance of all residual sub-networks effectively and efficiently.

4.3 Experiment 3: Destructing residual networks at test time

In this experiment, we verify that stimulative training can provide stronger robustness in resisting various network destruction operations including deleting individual layers, deleting more layers and permuting layers than common training.

Deleting individual layers. We first show the performance drop when deleting individual layers from trained MobileNetV3 at test time. As shown in Fig. 6(a), when applying common training to MobileNetV3, the performance drop is non-negligible when some layers are deleted (especially for the last several layers of each stage), and the trained MobileNetV3 is sensitive to the index of deleted layer. As a comparison, when applying stimulative training to MobileNetV3, no matter which layer is deleted, the performance drop of stimulative trained model is always lower than that of the common trained model, and the performance drop is always smaller than or equal to 1%. Such results verify that stimulative training can reduce the dependence between sub-networks significantly.

Deleting more layers. We then show the performance drop when deleting more layers from trained MobileNetV3 at test time. Note that, deleting more layers may come in a variety of combinations, thus we show the statistical box plot of performance drops for all combinations. As shown in Fig. 6(b), when applying common training to MobileNetV3, the medium value, minimum value and maximum value of performance drop for all combinations keeps continuously rising as the number of deleted layers increases. And the difference in performance drop for different combinations when removing the same number of layers can be very large. For example, when deleting 4 layers of common trained MobileNetV3, the Top1 accuracy drop for different combinations can vary from less than 5% to higher than 35%. Differently, when applying stimulative training, no matter how many layers are deleted, the values of performance drop for all combinations always keep very low (i.e., no more than 3%), indicating that stimulative training can bring strong robustness in resisting network destruction.

Permuting layers. We further show the performance drop when permuting layers in trained MobileNetV3 at test time. Note that, only the layers in the same stage can be permuted since the resolution and width of different stages are varying, and we show the detailed experimental settings in Appendix C.3. As shown in Fig. 6(c), when applying common training to MobileNetV3, the medium value, minimum value and maximum value of performance drop for all combinations increases with the rising number of permuted layers, and the variance of performance drop for different combinations when permuting the same number of layers may be also very large. As a comparison, the values of performance drop for all permuting combinations always keep very low (i.e., less than 1%), when stimulative training is applied. This further verifies the superiority of stimulative training.

4.4 Experiment 4: Recording the KL divergence between a residual network and all of its sub-networks when training

To study the consistency between the output of a given residual network and all of its sub-networks, we record their KL distance in the whole training process. As shown in Fig. 7, when applying common training to MobileNetV3, the variance, maximum and medium value of KL distance between a given residual network and all of its sub-networks continuously increases with rising training epoch. For comparison, when stimulative training is applied to MobileNetV3, all values of KL distance between MobileNetV3 and all of its sub-networks keep very small (i.e., no more than 0.25) in the whole training process. Such results imply that the proposed stimulative training can maintain the consistency between the output of a given residual network and all of its sub-networks.

Figure 7: The distribution of KL distance between MobileNetV3 and all of its sub-networks in the whole training process. We train MobileNetV3 on CIFAR100 with stimulative and common schemes.

5 Theoretical Analysis

Analysis 1: Why the performance of sub-networks can be improved. Based on Eq. 1, our method can be treated as optimizing $CE(\mathcal{Z}(\theta_{D_m}, x), y)$ and $KL(\mathcal{Z}(\theta_{D_m}, x), \mathcal{Z}(\theta_{D_s}, x))$ at the same time. According to the convergence of stochastic gradient descent, after enough number of iterations, both losses can be bounded by a constant, which is formulated as

$$CE(\mathcal{Z}(\theta_{D_m}, x), y) = -\sum_{i=1}^{N} y_i \log p_i^m < \epsilon_1 \tag{2}$$

$$KL(\mathcal{Z}(\theta_{D_m}, x), \mathcal{Z}(\theta_{D_s}, x)) = \mathbb{E}_\Theta \left[\sum_{i=1}^{N} p_i^m \log \frac{p_i^m}{p_i^s} \right] < \epsilon_2 \tag{3}$$

where N is the number of categories. The ϵ_1 and ϵ_2 are the tiny constants for corresponding losses. Θ is the set of all sub-networks. The p^m and p^s are the classification probability of main network and sub-network, respectively. Further, we can prove that *the absolute difference of cross entropy of sub-networks and main network can be bounded by a constant* (detailed proof can be found in Appendix B), which can be formulated as

$$|CE(\mathcal{Z}(\theta_{D_m}, x), y) - \mathbb{E}_\Theta \left[CE(\mathcal{Z}(\theta_{D_s}, x), y) \right]| < \frac{\epsilon_2 + \log N}{e^{-\epsilon_1}} + \epsilon_1 \tag{4}$$

where $\frac{\epsilon_2 + \log N}{e^{-\epsilon_1}} + \epsilon_1$ is a small constant after optimization. Eq. 4 demonstrates that the performance gap between sub-networks and the main network is constrained. Thus, *as the rising of the main network performance, sub-networks performance will be improved step by step.*

Analysis 2: Why the performance of given residual networks can be improved. Neural network training is in fact a form of polynomial regression, and any neural network with activation functions can roughly correspond to a fitted polynomial [25]. For simplifying notations, suppose that both input x and output y in a neural network have only one element. Then, we can consider the training of a neural network as the fitting of a polynomial function.

$$y = F(x) = c_0 + c_1 x + c_2 x^2 + \cdots + c_n x^n + \ldots \tag{5}$$

where c_1, c_2, ..., c_n, ... represent the polynomial coefficients. Based on training samples, we can establish the polynomial (neural network), which denotes the mapping relationship between inputs and outputs. For a test sample x, there always exists a point x_0 (e.g., a training sample) close enough to x, which can obtain an accurate output via the trained model. According to Taylor expansion, $F(x)$ at x_0 can be computed as :

$$\begin{aligned} y = F(x) = \frac{F(x_0)}{0!} + \frac{F'(x_0)}{1!}(x - x_0) + \\ \frac{F''(x_0)}{2!}(x - x_0)^2 + \cdots + \frac{F^{(n)}(x_0)}{n!}(x - x_0)^n + R_n(x) \end{aligned} \tag{6}$$

Table 1: The main network and all sub-networks performance (%) of stimulative training (ST) compared with common training (CT), on various residual networks and datasets.

method	MBV3_C10	MBV3_C100	Res50_C100	Res50_Img	Res101_Img
CT(main)	95.72	77.39	76.53	76.1	77.37
ST(main)	**96.88(+1.16)**	**81.07(+3.68)**	**81.06(+4.43)**	**77.22(+1.12)**	**78.58(+1.21)**
CT(all)	78.13±14.29	55.26±13.37	34.03±18.92	39.46±16.82	35.78±18.84
ST(all)	**96.21±0.43**	**80.01±0.59**	**79.66±1.77**	**73.3±2.89**	**75.52±3.6**

289 where $R_n(x)$ denotes the higher degree infinitesimal of $(x - x_0)^n$. According to Eq. 5 and Eq. 6, it is
290 obvious that different terms of the fitted polynomial have different effects, and the low-degree terms
291 tend to have greater effects on the predicted performance. Based on this point, [5] further figures
292 out that shallow sub-networks in residual networks roughly correspond to low-degree polynomials
293 consisting of low-degree terms, while deep sub-networks are opposite. Following this theory, the
294 proposed stimulative training can not only *strengthen the learning of different items* of the polynomial
295 (neural network), but also *pay more attention to the learning of low-degree items*. As a result, the
296 final performance of given residual networks can be improved by stimulative training.

6 Verification on Various Datasets and Networks

298 **CIFAR implementation details.**   CIFAR[26] is a classical image classification dataset consisting
299 of 50,000 training images and 10,000 testing images. It includes CIFAR-100 in 100 categories and
300 CIFAR-10 in 10 categories. For MobileNetV3 and ResNet50, the data augmentations follow [27], we
301 use SGD optimizer and train the model for 500 epochs with a batch size of 64. The initial learning
302 rate is 0.05 with cosine decay schedule. The weight decay is 3×10^{-5} and momentum is 0.9.

303 **ImageNet implementation details.**   We implement our method on large-scale ImageNet[28] dataset
304 containing 1.2 million training images and 50,000 validation images from 1,000 categories. For
305 ResNet families, we use standard data augmentations for ImageNet, as done in [29, 30, 31]. We
306 utilize SGD optimizer to train the model for 100 epochs with a batch size of 512, and the learning
307 rate is 0.2 with cosine decay schedule. The weight decay is 1×10^{-4} and momentum is 0.9.

308 **Main network and sub-networks performance.**   We further verify the effectiveness of stimulative
309 training (ST) on various networks and datasets. Table.1 shows its comparison with common training
310 (CT). Besides the Top1 accuracy of main network, we also report the the mean value and standard
311 deviation of Top1 accuracy for all sub-networks. It is obvious that stimulative training can noticeably
312 improve the performance of various networks on various datasets compared to common training (e.g.,
313 by 4.43% for ResNet50 on CIFAR-100 and 1.21% for ResNet101 on ImageNet). Moreover, the mean
314 performance of all sub-networks is dramatically improved and standard deviation greatly drops. For
315 example, stimulative training for MobileNetV3 on CIFAR100 has a mean performance of 80.01%
316 (much higher than common training of 55.26%) and a standard deviation of 0.59% (much lower
317 than 13.37%). Such results validate that stimulative training can well alleviate the network loafing
318 problem, and improve the performance of the given residual network and all of its sub-networks.
319 Experimental results on various models and datasets verify the generalization of stimulative training,
320 we advocate utilizing it as a general technology to train residual networks.

7 Conclusions

322 The paper understands and improves residual networks from a social psychology perspective of
323 loafing. Based on the novel view that a residual network behaves like an ensemble network, we
324 find that various residual networks invariably exhibit loafing-like behaviors that are consistent with
325 the social loafing problem of social psychology. We define this previously overlooked problem as
326 network loafing. As the loafing problem hinders the productivity of each individual and the whole
327 collective, we learn from social psychology and propose a stimulative training strategy to solve
328 the network loafing problem. Comprehensive empirical analyses show that stimulative training can
329 improve the performance of a given residual network and all of its sub-networks, and provide strong
330 robustness in resisting various network destruction operations. Furthermore, we theoretically show
331 why the performance of a given residual network and its sub-networks can be improved. Experiments
332 on various datasets and residual networks demonstrate the effectiveness of the proposed method.

References

[1] Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 770–778, 2016.

[2] Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Identity mappings in deep residual networks. In *European conference on computer vision*, pages 630–645. Springer, 2016.

[3] David Balduzzi, Marcus Frean, Lennox Leary, JP Lewis, Kurt Wan-Duo Ma, and Brian McWilliams. The shattered gradients problem: If resnets are the answer, then what is the question? In *International Conference on Machine Learning*, pages 342–350. PMLR, 2017.

[4] Andreas Veit, Michael J Wilber, and Serge Belongie. Residual networks behave like ensembles of relatively shallow networks. *Advances in neural information processing systems*, 29, 2016.

[5] Tongfeng Sun, Shifei Ding, and Lili Guo. Low-degree term first in resnet, its variants and the whole neural network family. *Neural Networks*, 2022.

[6] Alan G Ingham, George Levinger, James Graves, and Vaughn Peckham. The ringelmann effect: Studies of group size and group performance. *Journal of experimental social psychology*, 10(4):371–384, 1974.

[7] Richard E Petty, Stephen G Harkins, Kipling D Williams, and Bibb Latane. The effects of group size on cognitive effort and evaluation. *Personality and Social Psychology Bulletin*, 3(4):579–582, 1977.

[8] Kipling D Williams and Steven J Karau. Social loafing and social compensation: The effects of expectations of co-worker performance. *Journal of personality and social psychology*, 61(4):570, 1991.

[9] Jennifer M George. Asymmetrical effects of rewards and punishments: The case of social loafing. *Journal of Occupational and Organizational Psychology*, 68(4):327–338, 1995.

[10] Bibb Latané, Kipling Williams, and Stephen Harkins. Many hands make light the work: The causes and consequences of social loafing. *Journal of personality and social psychology*, 37(6):822, 1979.

[11] Ashley Simms and Tommy Nichols. Social loafing: a review of the literature. *Journal of Management Policy and Practice*, 15(1):58, 2014.

[12] Geoffrey Hinton, Oriol Vinyals, Jeff Dean, et al. Distilling the knowledge in a neural network. *arXiv preprint arXiv:1503.02531*, 2(7), 2015.

[13] Jangho Kim, SeongUk Park, and Nojun Kwak. Paraphrasing complex network: Network compression via factor transfer. *Advances in neural information processing systems*, 31, 2018.

[14] Seyed Iman Mirzadeh, Mehrdad Farajtabar, Ang Li, Nir Levine, Akihiro Matsukawa, and Hassan Ghasemzadeh. Improved knowledge distillation via teacher assistant. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 34, pages 5191–5198, 2020.

[15] Adriana Romero, Nicolas Ballas, Samira Ebrahimi Kahou, Antoine Chassang, Carlo Gatta, and Yoshua Bengio. Fitnets: Hints for thin deep nets. *arXiv preprint arXiv:1412.6550*, 2014.

[16] Zehao Huang and Naiyan Wang. Like what you like: Knowledge distill via neuron selectivity transfer. *arXiv preprint arXiv:1707.01219*, 2017.

[17] Byeongho Heo, Minsik Lee, Sangdoo Yun, and Jin Young Choi. Knowledge transfer via distillation of activation boundaries formed by hidden neurons. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 33, pages 3779–3787, 2019.

[18] Ying Zhang, Tao Xiang, Timothy M Hospedales, and Huchuan Lu. Deep mutual learning. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 4320–4328, 2018.

[19] Linfeng Zhang, Jiebo Song, Anni Gao, Jingwei Chen, Chenglong Bao, and Kaisheng Ma. Be your own teacher: Improve the performance of convolutional neural networks via self distillation. In *Proceedings of the IEEE/CVF International Conference on Computer Vision*, pages 3713–3722, 2019.

[20] Han Cai, Chuang Gan, Tianzhe Wang, Zhekai Zhang, and Song Han. Once-for-all: Train one network and specialize it for efficient deployment. *arXiv preprint arXiv:1908.09791*, 2019.

[21] Jiahui Yu, Pengchong Jin, Hanxiao Liu, Gabriel Bender, Pieter-Jan Kindermans, Mingxing Tan, Thomas Huang, Xiaodan Song, Ruoming Pang, and Quoc Le. Bignas: Scaling up neural architecture search with big single-stage models. In *European Conference on Computer Vision*, pages 702–717. Springer, 2020.

[22] Gao Huang, Yu Sun, Zhuang Liu, Daniel Sedra, and Kilian Q Weinberger. Deep networks with stochastic depth. In *European conference on computer vision*, pages 646–661. Springer, 2016.

[23] Andrew Howard, Mark Sandler, Grace Chu, Liang-Chieh Chen, Bo Chen, Mingxing Tan, Weijun Wang, Yukun Zhu, Ruoming Pang, Vijay Vasudevan, et al. Searching for mobilenetv3. In *Proceedings of the IEEE/CVF International Conference on Computer Vision*, pages 1314–1324, 2019.

[24] Ricky TQ Chen, Yulia Rubanova, Jesse Bettencourt, and David K Duvenaud. Neural ordinary differential equations. *Advances in neural information processing systems*, 31, 2018.

[25] Xi Cheng, Bohdan Khomtchouk, Norman Matloff, and Pete Mohanty. Polynomial regression as an alternative to neural nets. *arXiv preprint arXiv:1806.06850*, 2018.

[26] Alex Krizhevsky, Geoffrey Hinton, et al. Learning multiple layers of features from tiny images. 2009.

[27] Manas Sahni, Shreya Varshini, Alind Khare, and Alexey Tumanov. Compofa: Compound once-for-all networks for faster multi-platform deployment. *arXiv preprint arXiv:2104.12642*, 2021.

[28] Jia Deng, Wei Dong, Richard Socher, Li-Jia Li, Kai Li, and Li Fei-Fei. Imagenet: A large-scale hierarchical image database. In *2009 IEEE conference on computer vision and pattern recognition*, pages 248–255. Ieee, 2009.

[29] Christian Szegedy, Wei Liu, Yangqing Jia, Pierre Sermanet, Scott Reed, Dragomir Anguelov, Dumitru Erhan, Vincent Vanhoucke, and Andrew Rabinovich. Going deeper with convolutions. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 1–9, 2015.

[30] Gao Huang, Zhuang Liu, Laurens Van Der Maaten, and Kilian Q Weinberger. Densely connected convolutional networks. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 4700–4708, 2017.

[31] Golnaz Ghiasi, Tsung-Yi Lin, and Quoc V Le. Dropblock: A regularization method for convolutional networks. *Advances in neural information processing systems*, 31, 2018.