A Mixture of Surprises for Unsupervised Reinforcement Learning

Abstract

Unsupervised reinforcement learning aims at learning a generalist policy in a reward-free manner for fast adaptation to downstream tasks. So far, existing methods propose to provide an intrinsic reward based on surprise. Maximizing or minimizing surprise drives the agent to either explore or gain control over its environment. However, both strategies rely on a strong assumption: the entropy of the environment's dynamics is either high or low. This assumption may not always hold in real-world scenarios, where the entropy of the environment's dynamics may be unknown. Hence, choosing between the two objectives is a dilemma. We propose a novel yet simple mixture of policies to address this concern, allowing us to optimize an objective that simultaneously maximizes and minimizes the surprise. Concretely, we train one mixture component whose objective is to maximize the surprise and another whose objective is to minimize the surprise. Hence, our method does not make assumptions about the entropy of the environment's dynamics. We call our method a **M**ixture **O**f **S**urprise**S** (MOSS) for unsupervised reinforcement learning. Experimental results show that, surprisingly, our simple method achieves state-of-the-art performance on the URLB benchmark, outperforming previous pure surprise maximization-based objectives. Our code will be made publicly available.

1 Introduction

Humans can learn meaningful behaviors without external supervision, i.e., in an unsupervised manner, and then adapt those behaviors to new tasks [3]. Inspired by this, unsupervised reinforcement learning decomposes the reinforcement learning (RL) problem into a pretraining phase and a finetune phase [29]. During a pretraining phase, an agent prepares all possible tasks that a user might select. Afterward, the agent tries to figure out the selected task as quickly as possible during finetuning [22]. Doing so allows solving the RL problem in a meaningful order [3], e.g., a cook first has to look at what is in the fridge before deciding what to cook. Unsupervised representation learning has shown great success in Computer Vision [25] and Natural Language Processing [9]; however, one challenge is that RL includes both behavior learning and representation learning [29, 49].

Current unsupervised RL methods provide an intrinsic reward to the agent during a pretraining phase to tackle the behavior learning problem [29]. Intuitively, this intrinsic reward should incentivize the agent to understand its environment [13]. Current methods formulate the intrinsic reward as either maximizing or minimizing surprise [41, 6, 33, 52, 38, 39, 10, 32, 28, 15, 43, 42, 12], where knowledge-based methods quantify surprise as the uncertainty of a prediction model [10, 38, 39] and data-based methods measure surprise as an information-theoretic quantity [41, 6, 52, 33, 5][1]. Surprise

---

[1]Refer to [29] for detailed definitions of data-based, knowledge-based and competence-based methods.

maximization methods [22, 28, 33] formulate the problem as an exploration problem. Intuitively, to prepare all possible downstream tasks, an agent has to explore the state space and figure out what is possible in the environment. For instance, one instantiation is to maximize the agent's state entropy [33]. In contrast to surprise maximization, another line of work takes inspiration from the free-energy principle [20, 19, 18] and proposes to minimize the surprise [6, 41]. In particular, these works argue that external perturbations naturally provide the agent with surprising events. Hence, an agent can learn meaningful behaviors by minimizing its surprise, and minimizing this quantity requires gaining control over these external perturbations [41, 6]. For example, SMiRL [6] proposed to minimize the agent's state entropy.

Figure 1: **Outline of our Mixture Of SurpriseS (MOSS) strategy**. We provide the agent with two paths, each corresponding to maximizing or minimizing surprise. During the pretraining phase, the agent gathers experience from both paths using the skills from the corresponding toolbox. Finally, during the finetuning phase, the agent can choose any skills from any toolbox.

A closer look at these two approaches indicates a strong assumption. Substantial external perturbations already naturally provide an agent with a high state entropy [6]. Therefore, surprise-seeking approaches assume that the environment does not provide significant external perturbations. On the other hand, in an environment without any external perturbations, the agent already achieves minimum entropy by not acting [41]. Therefore, surprise minimization approaches assume that the environment provides external perturbations for the agent to control. However, in real-world scenarios, it is often difficult to quantify the entropy of the environment's dynamics beforehand, or the agent might face both settings. For example, a butler robot performs mundane chores daily in a household. However, the robot might also encounter surprising events (e.g., putting out a fire). Therefore a fixed assumption on the entropy of the environment dynamics is often not possible. In other words, choosing between surprise maximization or minimization for pretraining is a dilemma.

Simultaneously optimizing these two opposite objectives does not make sense. Instead, in this paper, we show that competence-based methods [29] offer a simple yet effective way to combine the benefits of these two objectives. In addition to conditioning the policy on the state, competence-based methods condition the policy on a latent vector [28, 32, 24, 50, 21, 1, 16]. Conditioning the policy offers an appealing way to formulate the unsupervised RL problem. During a pretraining phase, the agent tries to learn a set of possible behaviors in the environment and distills them into skills. Then, during finetuning, the agent tries to figure out the selected task as quickly as possible, using the repertoire of skills gathered during pretraining. For example, as illustrated in Fig. 1, we view skill distributions as a mixture of policies instead of a single policy. In particular, we train one set of skills whose objective is to maximize the surprise and another set of skills whose objective is to minimize the surprise. Surprisingly, this paper shows that this simple approach works well in practice, which simultaneously optimizes two contradicting objectives. Our primary contribution, presented in Section 4, is a simple intrinsic reward called MOSS that does not make assumptions about the entropy of the environment's dynamics. In Section 5, our experimental results on URLB [29] and ViZDoom [27] show that, surprisingly, our MOSS methods achieve state-of-the-art results.

We organize the paper as follows. Section 3 briefly analyzes previous unsupervised RL algorithms under the surprise framework. Then in Section 4, we introduce our MOSS method. Next, experimental results in Section 5 shows that on URLB [29] and ViZDoom [27], our MOSS method improves upon previous pure maximization and minimization methods. Finally, we provide discussions and limitations in Section 6.

2 Preliminaries

Markov Decision Process   Unsupervised RL methods studied in this paper operate under a Markov Decision Process (MDP) [47]. In particular, we specify an MDP as a tuple $\mathcal{M} = (\mathcal{S}, \mathcal{A}, T, r^{\text{ext}}, \rho, \gamma)$ where $\mathcal{S}$ is the state space and $\mathcal{A}$ is the action space of the environment. $T(\mathbf{S}' \mid \mathbf{S}, \mathbf{A})$ represents the state-transition dynamics, $\rho : \mathcal{S} \to [0, 1]$ is the initial state distribution, and $\gamma \in [0, 1)$ is the discount factor. At each discrete time step $t \in \mathbb{Z}^*$, the agent receives a state and performs an action, which we denote as $\mathbf{S}_t \in \mathcal{S}$ and $\mathbf{A}_t \in \mathcal{A}$, respectively. During pretraining, unsupervised RL algorithms compute an intrinsic reward r^{int}; during the finetune phase, the agent receives the extrinsic reward r^{ext} given by the environment at each interaction.

Skill   Intuitively, a *skill* is an abstraction of a specific behavior (e.g., walking), and in practice, a *skill* is a latent conditioned policy [15]. Given a latent vector $\mathbf{z}$, we denote a skill as $\pi_\theta(\mathbf{a}_t \mid \mathbf{s}_t, \mathbf{z})$, where π_θ is the policy parameterized by θ. For instance, during pretraining, the latent vectors are sampled every n steps such that the latent vector $\mathbf{z}$ is associated with the behavior executed during the associated n steps.

Mutual Information   Knowledge-based, data-based, and competence-based methods have different measures of surprise. The study in this paper falls into the category of competence-based methods. In particular, data-based and competence-based methods rely on an information-theoretic definition of surprise, i.e., entropy. Previous competence-based methods acquire skills by maximizing mutual information [14] between $\mathcal{T}$ and skills $\mathbf{Z}$

$$\mathbb{I}(\mathcal{T}; \mathbf{Z}) = \mathbb{H}[\mathcal{T}] - \mathbb{H}[\mathcal{T}|\mathbf{Z}] \tag{1}$$

$$= \mathbb{H}[\mathbf{Z}] - \mathbb{H}[\mathbf{Z}|\mathcal{T}], \tag{2}$$

where $\mathcal{T}$ can be the states $\mathbf{S}$, the joint distribution of state-transitions $(\mathbf{S}', \mathbf{S})$, or the state-transitions $(\mathbf{S}' \mid \mathbf{S})$. In particular, these methods differ in how they decompose the mutual information. Theoretically, these different decompositions are equivalent, i.e., they all maximize the mutual information between states and skills. However, the particular choice greatly influences the performance in practice as optimizing this objective relies on approximations.

To motivate the potential of competence-based methods over data-based or knowledge-based methods, we provide an intuitive understanding of Eq. 1. On the one hand, the entropy term says that we want skills in aggregate that explore the state space; we use it as a proxy to learn skills that cover the set of possible behaviors. On the other hand, It is not enough to learn skills that randomly go to different places. We want to reuse those skills as accurately as possible, meaning we need to be able to discriminate or predict the agent's state transitions from skills. To do so, we minimize conditional entropy. In other words, appropriate skills should cover the set of possible behaviors and should be easily distinguishable.

3 Information-Theoretic Skill Discovery

Competence-based methods employ different intrinsic rewards to maximize mutual information: (1) discriminability-based and (2) exploratory-based intrinsic rewards. For example, the former rewards the agent for discriminable skills. In contrast, the latter rewards the agent for skills that effectively cover the state space using a KNN density estimator [44, 33] to approximate the entropy term. Below we analyze both approaches.

3.1 Discriminability-based Intrinsic Reward

Previous work such as DIAYN [15] uses a discriminability-based intrinsic reward. They use the decomposition in Eq. 2 and given a variational distribution q_ϕ, they optimize the following variational lower bound

$$\begin{aligned}
\mathbb{I}(\mathbf{S}; \mathbf{Z}) &= \mathbb{KL}(p(\mathbf{s}, \mathbf{z}) \mid\mid p(\mathbf{s})p(\mathbf{z})) \\
&= \mathbb{E}_{\mathbf{s}, \mathbf{z} \sim p(\mathbf{s}, \mathbf{z})} \left[\log \frac{q_\phi(\mathbf{z} \mid \mathbf{s})}{p(\mathbf{z})} \right] + \mathbb{E}_{\mathbf{s} \sim p(\mathbf{s})}[\mathbb{KL}(p(\mathbf{z} \mid \mathbf{s}) \mid\mid q_\phi(\mathbf{z} \mid \mathbf{s}))] \\
&\geq \mathbb{E}_{\mathbf{z}, \mathbf{s} \sim p(\mathbf{z}, \mathbf{s})}[\log q_\phi(\mathbf{z} \mid \mathbf{s})] - \mathbb{E}_{\mathbf{z} \sim p(\mathbf{z})}[p(\mathbf{z})],
\end{aligned} \tag{3}$$

where $\mathbf{Z} \sim p(\mathbf{Z})$ is a discrete random variable. In particular, the discriminator rewards the agent if it can guess the skill from the state, i.e., $r^{\text{int}}(\mathbf{s}) \triangleq \log q_\phi(\mathbf{z} \mid \mathbf{s}) - \log p(\mathbf{z})$. These methods may easily run into a chicken and egg problem, where skills learn to be diverse using the discriminator's output. However, the discriminator cannot learn to discriminate skills if the skills are not diverse. Hence, it discourages the agent from exploring. Previous work [45] has tried to solve this problem by decoupling the *aleatoric uncertainty* from the *epistemic uncertainty*.

Furthermore, solving the chicken and egg problem is not enough since a state must map to a single skill in Eq. 2. Accordingly, the methods that use the decomposition in Eq. 2 require the skill space to be smaller than the state space so that the skills are distinguishable. Since previous work showed that a high-dimensional continuous skill space empirically performs better, the intrinsic reward should not rely on the decomposition in Eq. 2. Intuitively, a continuous skill space allows (1) to interpolate between skills and (2) to represent a more significant set of skills in a more compact representation.

Instead, in Eq. 1, in contrast to skills that are predictable by states $\mathbb{H}[\mathbf{Z} \mid \mathcal{T}]$, we require that states are predictable by skills $\mathbb{H}[\mathcal{T} \mid \mathbf{Z}]$. Since any state should be predictable from a given skill, the skill space must be larger than the state space (i.e., we do not want a skill mapping to multiple states). Therefore, another work [43] relies on a variational bound on Eq. 1.

$$
\begin{aligned}
\mathbb{I}(\mathbf{S}'; \mathbf{Z} \mid \mathbf{S}) &= \mathbb{E}_{\mathbf{z},\mathbf{s},\mathbf{s}' \sim p(\mathbf{z},\mathbf{s},\mathbf{s}')} \left[\log \frac{q_\phi(\mathbf{s}' \mid \mathbf{s}, \mathbf{z})}{p(\mathbf{s}' \mid \mathbf{s})} \right] + \mathbb{E}_{\mathbf{z},\mathbf{s} \sim p(\mathbf{z},\mathbf{s})} \left[\mathbb{KL}(p(\mathbf{s}' \mid \mathbf{s}, \mathbf{z}) \,\|\, q_\phi(\mathbf{s}' \mid \mathbf{s}, \mathbf{z})) \right] \\
&\geq \mathbb{E}_{\mathbf{z},\mathbf{s},\mathbf{s}' \sim p(\mathbf{z},\mathbf{s},\mathbf{s}')} \left[\log \frac{q_\phi(\mathbf{s}' \mid \mathbf{s}, \mathbf{z})}{p(\mathbf{s}' \mid \mathbf{s})} \right],
\end{aligned}
\tag{4}
$$

which uses a continuous skill space; however, it does not scale to high dimensions as the intrinsic reward $r^{\text{int}}(\mathbf{s}', \mathbf{a}, \mathbf{s}) \triangleq \log \frac{q_\phi(\mathbf{s}' \mid \mathbf{s}, \mathbf{z})}{p(\mathbf{s}' \mid \mathbf{s})}$ relies on an estimation of $p(\mathbf{s}' \mid \mathbf{s})$. In particular, they assume that $p(\mathbf{z} \mid \mathbf{s}) = p(\mathbf{z})$. Intuitively, given $\mathbf{s}$, if we assume each element in the latent vector $(\mathbf{z})_i$ to be independent of each other, the error of this assumption will be scaled by the dimension of $\mathbf{z}$.

3.2 Exploratory-based Intrinsic Reward

As aforementioned, discriminability-based intrinsic reward may easily run into a chicken and egg problem. Hence, other work [28, 32] uses an exploratory-based intrinsic reward to address the chicken and egg problem. In other words, they use the decomposition in Eq. 1, where the intrinsic reward explicitly rewards the agent for exploring through $\mathbb{H}[\mathcal{T}]$.

Previous work [33] maximizes the state entropy, i.e., $\mathcal{T} = \mathbf{S}$. However, the authors in [4] argue that it often results in the discriminator simply memorizing the last state of each skill. Instead, CIC [28] proposes to maximize the entropy of the joint distribution of state-transitions (which from now on we refer as joint entropy), i.e., $\mathbb{H}[\mathbf{S}', \mathbf{S}]$.

Therefore, CIC [28] proposes to estimate the conditional entropy $\mathbb{H}[\mathbf{S}', \mathbf{S} \mid \mathbf{Z}]$ using noise contrastive estimation [28, 23] and the joint entropy $\mathbb{H}[\mathbf{S}', \mathbf{S}]$ using a k-nearest neighbor estimator [44] to handle high dimensional skill space.

KNN-density estimation   Previous works [33, 28] approximate the joint entropy $\mathbb{H}[\mathbf{S}', \mathbf{S}]$ using a k-nearest neighbor estimator [44]. Given a random sample of size N, $\{(\mathbf{S}^{(i)'}, \mathbf{S}^{(i)})\}_{i=1}^N \sim P(\mathbf{S}', \mathbf{S})$, the estimator computes a Monte Carlo estimate [7] of the entropy defined as

$$
\hat{\mathbb{H}}[\mathbf{S}', \mathbf{S}] = -\frac{1}{N} \sum_{i=1}^N \log \hat{p}_k(\mathbf{s}^{(i)'}, \mathbf{s}^{(i)}) + b(k),
\tag{5}
$$

where $\hat{p}_k(\mathbf{s}^{(i)'}, \mathbf{s}^{(i)}) = \frac{k}{N V_k^{(i)}}$ is an estimation of $p(\mathbf{s}^{(i)'}, \mathbf{s}^{(i)})$, $V_k^{(i)}$ is the volume of the hypersphere of radius $R_k^{(i)}$, and $b(k)$ is a constant such that the estimator is unbiased. In particular, R_k is the distance from $\mathbf{s}$ to its k-nearest neighbor $\mathbf{s}'_k$ where we assume a uniform distribution of points within the hypersphere (local uniformity assumption [34]).

In practice, to make the distance R_k meaningful, we do not operate in the state space. For instance, CIC [28] trains an MLP $f_\psi : \mathbb{R}^{|\mathcal{S}|} \to \mathbb{R}^d$ that projects the state into a latent representation such that

158 $R_k = \|f_\psi(s) - f_\psi(s'_k)\|$ where d is the skill dimension. Moreover, in APT [33], it was found that
159 averaging over all k-nearest neighbors leads to better results. Hence, CIC [28] optimizes a quantity
160 proportional to Eq. 5:

$$\hat{\mathbb{H}}[\mathbf{S}', \mathbf{S}] \triangleq \sum_{i=1}^{N} \log \left(c + \frac{1}{k} \sum_k R_k^{(i)} \right), \tag{6}$$

161 where $c = 1$ is constant for numerical stability. We view the joint entropy as an expected reward, and
162 for a transition $(\mathbf{s}^{(i)}, \mathbf{s}^{(i)'})$, the reward function is

$$r^{\text{int}}(\mathbf{s}^{(i)}, \mathbf{s}^{(i)'}) \triangleq \log \left(c + \frac{1}{k} \sum_k R_k^{(i)} \right). \tag{7}$$

163 **Noise Contrastive Estimation**   To train parameters ψ, CIC [28] minimizes the conditional entropy
164 $\mathbb{H}[\mathbf{S}'; \mathbf{S} \mid \mathbf{Z}]$ using a noise contrastive estimation (NCE) [23, 37]. Denote $\mathbf{h} = f_\psi(\mathbf{s})$ and $\mathbf{h}' = f_\psi(\mathbf{s}')$
165 the projected representations of $\mathbf{s}$ and $\mathbf{s}'$, respectively. Furthermore, let $g_{\phi_z} : \mathbb{R}^d \to \mathbb{R}^d$ be an MLP
166 that projects the skill into a latent representation and $g_{\phi_s} : \mathbb{R}^d \times \mathbb{R}^d \to \mathbb{R}^d$ be an MLP that projects $\mathbf{h}$
167 and $\mathbf{h}'$ into a latent representation. We define the NCE loss

$$\mathcal{L}_{\text{nce}}(\mathbf{s}^{(i)}, \mathbf{z}^{(i)}) = -\log \frac{\exp c_i^{(i)}}{\sum_{j=1}^{N} \exp c_j^{(i)}} \tag{8}$$

168 as an approximation to $\mathbb{H}[S'; S \mid Z]$, where we define $\cos(\cdot, \cdot)$ as the cosine similarity operator, ω
169 as a temperature term, and $c_j^{(i)} = \cos(g_{\phi_z}(\mathbf{z}^{(i)}), g_{\phi_s}(\mathbf{h}^{(j)}, \mathbf{h}^{(j)'}))/\omega$. As aforementioned, this term
170 serves as representation learning for parameters ψ. Intuitively, the NCE loss [23] pushes $p(\mathbf{s}' \mid \mathbf{s}, \mathbf{z})$
171 to be a delta-like density function. However, since we define behaviors with n steps, we want a wider
172 distribution, so in practice, ω is set to 0.5 to smooth the distribution.

4   Mixture Of Suprises (MOSS)

174 Our goal is to provide an algorithm that does not build on any assumption about the entropy of the
175 environment's dynamics. A straightforward way to achieve this is to maximize and minimize surprise
176 simultaneously. A benefit of such an objective is that it promotes exploration to find a more effective
177 policy for minimizing the surprise [6]. In particular, in [6], they maximize surprise according to all
178 prior experiences while minimizing surprise according to the current episode. However, they find
179 that it only helps in some cases. The challenge is to find an effective way to optimize these two
180 opposite objectives since if we add the two objectives, it would simply yield a linear interpolation of
181 the two objectives, which still corresponds to either maximizing *or* minimizing. A previous work
182 [17], dubbed Adversarial Surprise (AS), resolves this challenge using an adversarial game where
183 two policies compete against each other: one maximizes surprise while the other minimizes surprise.
184 AS [17] requires training two policies that do not share parameters or data. Instead, we propose a
185 novel yet simple mixture of policies to maximize and minimize surprise simultaneously. Our mixture
186 of policies does not rely on an adversarial game [17] in which training is known to be challenging
187 [35] and uses a single network for both objectives resulting in higher sample efficiency. Mainly, our
188 method only requires a minor change to CIC [28] that does not involves any computational cost
189 during training. In particular, our mixture of policies builds on a competence-based approach [28],
190 meaning we use two disjoint skill sets. We separate the two opposite objectives using a different skill
191 set for each objective: one skill set for surprise maximization and another for surprise minimization.

192 Specifically, we define the mixture of policies using a binary random variable M, where we associate
193 each mixture component with a continuous uniform distribution $\mathcal{U}^d(a, b)$ on an interval $[a, b]$. Each
194 uniform distribution constitutes a skill distribution. Maintaining two different skill distributions
195 allows us to define a different objective for each distribution. In particular, we define two distributions
196 $\mathbf{Z}_{\max} \sim P(\mathbf{Z} \mid M = 0)$ and $\mathbf{Z}_{\min} \sim P(\mathbf{Z} \mid M = 1)$. Since we do not assume any priors on the
197 entropy of the environment's dynamics, we deterministically set $M = 0$ for the first half of the steps
198 and $M = 1$ for the other half of the steps in the episode. Compared to more sophisticated methods
199 (e.g., appendix B) for setting M (i.e., switching the objective), such a heuristic adds no computational
200 cost during training, requires no hyper-parameter tuning, and performs well.

Algorithm 1 MOSS: Unsupervised pretraining

Input: Environment, number of pretraining steps N_T.
Initialize DDPG, and ϕ_s, ϕ_z, ψ
for $t = 1$ **to** N_T **do**
  if $(t\%\text{update skill every}) == 0$ **then**
    Sample $m_t \sim p(m)$ $\triangleright$ setting to $m = 0$ is equivalent to CIC[28]
    Sample $\mathbf{z}_t \sim p(\mathbf{z} \mid m_t)$
  end if
  Take some action $\mathbf{a}_t$ and observe $\mathbf{s}_{t+1}$
  Store $(\mathbf{s}_t, \mathbf{s}_{t+1}, m_t, \mathbf{z}_t)$ into buffer $\mathcal{B}$
  if $t \geq 4000$ **then**
    Sample a batch $\{(\mathbf{a}^{(i)}, \mathbf{s}^{(i)}, \mathbf{s}^{(i)'}, m^{(i)}, \mathbf{z}^{(i)})\}_{i=1}^N$ and compute intrinsic reward r^{int} using equation 9.
    Update DDPG using intrinsic reward.
    Update ϕ_s, ϕ_z, ψ using noise contrastive loss in equation 8.
  end if
end for

Moreover, motivated by the discussions in Section 3.2, we build our method on top of the CIC [2] [28] framework. This framework is appealing as it bypasses the chicken and egg problem and supports high-dimensional skills. In addition, it significantly outperforms previous competence-based methods on the URLB benchmark [29]. Hence, following CIC [28], we use the decomposition in Eq. 1

$$\mathbb{I}(\mathbf{S}', \mathbf{S}; \mathbf{Z}) = \mathbb{H}[\mathbf{S}', \mathbf{S}] - \mathbb{H}[\mathbf{S}', \mathbf{S} \mid \mathbf{Z}].$$

In particular, we define *surprise* as the joint entropy, which corresponds to maximizing and minimizing $\mathbb{H}[\mathbf{S}', \mathbf{S}]$, and as in CIC [28] we use Eq. 6 to approximate the joint entropy. We approximate the conditional entropy $\mathbb{H}[\mathbf{S}', \mathbf{S} \mid \mathbf{Z}]$ using a noise contrastive estimation following Eq. 8. By minimizing the conditional entropy, we distill behaviors into skills. Doing so also serves as representation learning for computing the joint entropy [28].

Implementation To ensure fairness, all hyper-parameters are kept as in CIC [28] and we use the same RL algorithm (i.e., DDPG [31] as implemented in DrQ-V2 [51]).

In practice, $\mathbf{Z}_{\max} \sim P(\mathbf{Z} \mid M = 0) \triangleq \mathcal{U}^d(0, 1)$ and $\mathbf{Z}_{\min} \sim P(\mathbf{Z} \mid M = 1) \triangleq \mathcal{U}^d(-1, 0)$ (we refer readers to appendix for other variants that we tried), where we set $M = 0$ for the first half of steps and $M = 1$ for the remaining half of steps in the episode. Hence, the RL agent maximizes

$$\mathcal{F}(\theta) \triangleq -\mathbb{E}_{\mathbf{z}_{\max} \sim \mathcal{U}^d(0,1)} \mathbb{E}_{p_{\mathbf{z}_{\max}}(\mathbf{s}', \mathbf{s})}[\log p_{\mathbf{z}_{\max}}(\mathbf{s}', \mathbf{s})] + \mathbb{E}_{\mathbf{z}_{\min} \sim \mathcal{U}^d(-1,0)} \mathbb{E}_{p_{\mathbf{z}_{\min}}(\mathbf{s}', \mathbf{s})}[\log p_{\mathbf{z}_{\min}}(\mathbf{s}', \mathbf{s})].$$

And the intrinsic reward is a function of the state-transition and the binary random variable M

$$r^{\text{int}}(\mathbf{s}^{(i)}, \mathbf{s}^{(i)'}, M) = \begin{cases} \log\left(c + \frac{1}{k}\sum_k R_k^{(i)}\right) & M = 0, \\ -\log\left(c + \frac{1}{k}\sum_k R_k^{(i)}\right) & M = 1. \end{cases} \tag{9}$$

As in CIC [28], we approximate the joint entropy using Eq. 6.

MOSS's implementation is straightforward; i.e., at each time step, instead of sampling $\mathbf{Z} \sim P(\mathbf{Z})$, we sample $\mathbf{Z} \sim P(\mathbf{Z} \mid M)$ and replace the intrinsic reward with Eq. 9. Pseudocode for MOSS is provided in Alg. 1. In fact, fixing $M = 0$ yields CIC [28].

5 Experiments

Environments We present the main results of method by evaluating on the Unsupervised Reinforcement Learning Benchmark (URLB) [29], which is a standard unsupervised RL benchmark for continuous control. URLB [29] has three different domains listed in order of increasing difficulty:

---

[2] The implementation provided by CIC (https://github.com/rll-research/cic) is based on the arxiv version (https://arxiv.org/abs/2202.00161v2) which is an updated version of the ICLR version (https://openreview.net/forum?id=kOtkgUGAVTX). In particular, in the arxiv version, the intrinsic reward only relies on the KNN estimates and the NCE term is only used to train ϕ_s, ϕ_z, ψ. While, the ICLR version includes the NCE term in the intrinsic reward.

- Walker is a biped robot domain constrained to a 2D vertical plane. The challenge for this domain is to learn how to balance and maneuver simultaneously.
- Quadruped is a four-legged robot in 3D space. This domain has a higher dimensional state and action space than the Walker domain.
- Jaco is a 6-DOF robotic arm domain with a three-finger gripper in 3D space that has to learn action constraints and manipulation.

Furthermore, each of the three domains has four different downstream tasks with varying difficulties. We refer readers to Tab 1 for the complete list of 12 tasks. Finally, in OpenAI gym environments [8], since an episode terminates as soon as a robot falls, the agent will naturally avoid falling to the ground as it will get a 0 reward. Hence, during pretraining, the OpenAI gym environment [8] may leak some task information (e.g., standing) to the unsupervised learning agent [28]. Therefore, URLB [29] builds on top of the Deepmind Control Suite [48] to avoid leaking some task information.

The domains in URLB [29] use low-dimensional state information, deterministic transitions, and non-evolving environments. In contrast, ViZDoom [27] uses raw pixel observations, stochastic transition, and evolving environments. Furthermore, since the environment randomly spawns enemies that shoot fireballs, the agent faces external perturbations that surprise the agent. We evaluate our method on the *DefendTheLine* and *TakeCover* maps.

Evaluation We follow the benchmark's standard training procedure by pretraining the agent for 2 million steps in each of the three domains and then finetuning the pre-trained agent for $100k$ steps with downstream task rewards. Since AS trains two network-independent policies, we ensure both policies each perform 2 million environment steps during pretraining. To ensure fairness, we pretrain and finetune each method with the same 12 seeds (0-11) using the code provided in URLB[3] [29]. We present the results in Fig. 2 for a total of 1584 ($=$ 11 algorithms $\times 12$ tasks $\times 12$ seeds) runs. Our main evaluation metrics are interquartile mean (IQM) and Optimality Gap (OG) of normalized scores, where we used the score of a DDPG [51] agent trained from scratch for 2 million steps as the expert scores [29]. On the one hand, IQM is more robust to outliers than the mean, and IQM is significantly less biased than the median [2]. On the other hand, the Optimality Gap measures how far scores are from the expert scores [2].

Baselines Baselines include methods presented in the URLB benchmark [29] as well as CIC [28]. The baseline methods fall into knowledge-based methods, i.e., ICM [38], Disagreement [39], RND [10], data-based methods, i.e., APT [33], Proto-RL [52], AS [17], and competence-based methods, i.e., SMM [30], DIAYN [15], APS [32], CIC [28]. We refer readers to the Appendix of URLB [29] for details on the different baselines. Lastly, since the two policies (Alice and Bob) in AS are parameter-independent, we pretrain for 4 million steps, each policy trained using 2 million steps.

We evaluate our agent in ViZDoom [27] against CIC [28], and a modified version of CIC [28], dubbed NegativeCIC, where the intrinsic reward is the negative joint entropy. Since the ViZDoom environment has high natural environment dynamics entropy, NegativeCIC should act as a strong baseline. We adopt the same pretraining and finetuning procedure as in URBL for ViZDoom.

MOSS We keep all hyperparameters as those in CIC [28]. Specifically, unless specified otherwise, we set $M = 0$ for the first half of steps and $M = 1$ for the other half of steps in the episode. We refer readers to the Appendix for more details.

5.1 Results

To ensure the reliability of our main results, we report results as described in [2] to account for the uncertainty. We present results in Fig. 2, where, surprisingly, our method obtains state-of-the-art performance on the URLB benchmark [29] on our main evaluation metrics [2]. In particular, the performance profile in Fig. 2b reveals that MOSS stochastically dominates all other methods. We also present numerical results in Tab. 1 for a detailed breakdown over individual tasks.

For the IQM metric, we report an increase of 6% compared to CIC, which is the second leading method. Furthermore, as for the Optimality Gap metric, we decreased 20% compared to CIC.

---

[3]our experiments are based on the code of URLB `https://github.com/rll-research/url_benchmark`, and CIC `https://github.com/rll-research/cic`

(a) **Aggregate Statistics**. MOSS obtains the highest IQM and the lowest Optimality Gap.

(b) **Performance Profiles.** MOSS stochastically dominates all other methods.

Figure 2: **Main results.** We report aggregate statistics (a) and performance profiles (b) following [2] for 12 downstream tasks on URLB with 12 seeds, providing a total of 144 seeds.

Table 1: **Numerical results.** Following URLB [29] we show the mean and standard error over 12 seeds (0-11). We denote competence-based methods, knowledge-based, and data-based methods in blue, black, and red, respectively.

| Domain | | Walker | | | | Quadruped | | | | Jaco | | |
Task	Flip	Run	Stand	Walk	Jump	Run	Stand	Walk	Bottom Left	Bottom Right	Top Left	Top Right
ICM[38]	381±10	180±15	868±30	568±38	337±18	221±14	452±15	234±18	112±7	94±5	90±6	93±11
Disagreement [39]	313±8	166±9	658±33	453±37	512±14	395±12	686±30	358±25	120±7	132±5	111±10	113±10
RND [10]	412±18	267±18	842±19	694±26	**681±11**	455±7	875±25	581±42	106±6	111±6	83±7	107±5
ICM APT[33]	596±24	491±18	949±3	850±22	508±44	390±24	676±44	464±52	114±5	120±3	116±4	114±8
Proto [52]	378±4	225±16	828±24	610±40	426±32	310±22	702±59	348±55	130±12	131±11	134±12	146±10
AS-Bob	475±16	247±23	917±36	675±21	449±24	285±23	594±37	353±39	116±21	**166±12**	143±12	139±13
AS-Alice	491±20	211±9	868±47	655±36	415±20	296±18	590±41	337±17	109±20	141±19	140±17	129±15
SMM[30]	428±8	345±31	924±9	731±43	271±35	222±23	388±51	167±20	52±5	55±2	53±2	57±5
DIAYN [15]	306±12	146±7	631±46	394±22	491±38	325±21	662±38	273±19	35±5	35±6	23±3	31±5
APS [32]	355±18	166±15	667±56	500±40	283±22	206±16	379±31	192±17	61±6	79±12	51±5	56±7
CIC [28]	715±40	**535±25**	**968±2**	914±12	541±31	376±19	717±46	460±36	147±8	150±6	145±9	139±9
MOSS (Ours)	**729±40**	531±20	962±3	**942±5**	674±11	**485±6**	**911±11**	**635±36**	**151±5**	150±5	**150±5**	**150±6**

269 Furthermore, in Fig. 2.b previous methods intersect at multiple points (making it hard to conclude
270 whether a method is better than the other), while MOSS is always above all previous methods. In
271 addition, in Fig. 2.b, MOSS maintains all runs greater than a normalized score as high as 0.5.

Table 2: **ViZDoom Results**. We report on two maps from ViZDoom to illustrate the robustness of our method in different environments.

	Defend the Line	Take Cover
NegativeCIC	462±11	51793±2936
MOSS	**510±22**	**63497±2384**

272 We also evaluated our method on ViZDoom [27]. Since the *TakeCover* and *DefendTheLine* maps
273 in ViZDoom provides natural perturbations, we use NegativeCIC as the baseline. We present the
274 numerical results in Tab. 2. Since the environments in ViZDoom are highly stochastic, we remove
275 the top and bottom 10% of scores and report the mean and standard error to account for any outliers.
276 Like in the main results presented earlier, MOSS consistently outperforms the baseline method under
277 this completely new setting.

5.2 Ablation

279 In MOSS, we maintain two different skill distributions, i.e., $\mathbf{Z}_{\max} \sim \mathcal{U}^d(0,1)$ and $\mathbf{Z}_{\min} \sim \mathcal{U}^d(-1,0)$.
280 In particular, setting $\mathbf{Z}_{\min}$ to the same distribution as $\mathbf{Z}_{\max} \sim \mathcal{U}^d(0,1)$ is equivalent to directly op-
281 timizing CIC [28] with the two objectives simultaneously. We dub MOSS with the same skill
282 distribution, MOSS_SAME. In Fig. 3b, we observe that naively doing so can result in poor perfor-
283 mance, showing the effectiveness of our method in mitigating the simultaneous optimization of two
284 contradicting objectives.

285 Moreover, as shown in Fig. 3b, NegativeCIC performs poorly on the URLB benchmark [29] since
286 most tasks required structured exploration in a low entropy environment.

(a) **Ablation on environment.** Adding stochasticity in the URLB environment hurts CIC. We notice that MOSS is significantly more robust to the stochasticity than CIC.

(b) **Ablation on policy.** Removing the mixture significantly hurts the performance.

Figure 3: **MOSS ablation experiments** on the Walker domain [29]. In (a), we inject stochasticity by adding a Gaussian noise on the agent's action according to a Bernoulli with $p = 0.3$ and report performance loss. In (b), we report performance for CIC, MOSS_SAME, and NegativeCIC. Specifically, MOSS_SAME represents MOSS without the mixture of policies, and NegativeCIC represents CIC with the intrinsic reward as the negative joint entropy.

Since MOSS does not make assumptions about the entropy of the environment's dynamics, we are interested in knowing whether adding stochasticity affects performance. For this stochastic setup, during each interaction with the environment, we sample $Y \sim \text{Bernoulli}(0.3)$ and if $Y = 1$, we add a Gaussian Noise $\mathcal{N}(0, 0.2)$ to the agent's intended action. In Fig. 3a, we observe that CIC's [28] performance drops while MOSS' performance is almost unaffected. This finding empirically supports previous works which claim that solely maximizing surprise for unsupervised RL agents is sometimes not enough, especially in stochastic environments [6, 41].

6 Discussions & Limitations

We presented MOSS, an unsupervised RL method that does not make assumptions about the environment dynamics' entropy by simultaneously maximizing and minimizing surprises. Our method falls into competence-based methods. Leveraging a mixture of policies for more than surprise maximization and minimization is an interesting future research.

Limitations One limitation is that our method has a simple and effective deterministic rule for switching between the two objectives *independent* of state or history. We did explore a more sophisticated method in Appendix B that had a better performance but required tuning and extra computation. Therefore, a promising direction is to explore methods that take advantage of state information (e.g., using a meta-controller [26]) to output a more optimal switching mechanism that incentivizes deep structured exploration [40]. Moreover, we only considered competence-based methods. Extending our method to other unsupervised RL methods would be interesting to investigate in future work. Additionally, when finetuning, we transferred network weights which could lead to unlearning of already learned behaviors [11]. Works like [11] utilized frozen pretrained policies to improve downstream finetuning further. Lastly, we only considered two objectives, and including more meaningful objectives like empowerment or anxiety [36, 46] during pretraining could be an exciting direction.

Potential Negative Impact Since we operate under the unsupervised reinforcement learning domain, the agent receives rewards that incentives exploration. Therefore, agents under this domain can be more unpredictable than agents that receive task rewards for intended behaviors. Furthermore, there is no current safeguard for the agent to not act maliciously in its environment; the agent may potentially cause harm to properties situated in the environment, including the agent itself. Therefore, unsupervised learning with safety constraints would be an exciting area of future research to mitigate this potential negative impact.

References

[1] Joshua Achiam, Harrison Edwards, Dario Amodei, and Pieter Abbeel. Variational option discovery algorithms. *arXiv preprint arXiv:1807.10299*, 2018.

[2] Rishabh Agarwal, Max Schwarzer, Pablo Samuel Castro, Aaron C Courville, and Marc Bellemare. Deep reinforcement learning at the edge of the statistical precipice. *Advances in Neural Information Processing Systems*, 34, 2021.

[3] Arthur Aubret, Laetitia Matignon, and Salima Hassas. A survey on intrinsic motivation in reinforcement learning. *arXiv preprint arXiv:1908.06976*, 2019.

[4] Kate Baumli, David Warde-Farley, Steven Hansen, and Volodymyr Mnih. Relative variational intrinsic control. *arXiv preprint arXiv:2012.07827*, 2020.

[5] Marc Bellemare, Sriram Srinivasan, Georg Ostrovski, Tom Schaul, David Saxton, and Remi Munos. Unifying count-based exploration and intrinsic motivation. *Advances in neural information processing systems*, 29, 2016.

[6] Glen Berseth, Daniel Geng, Coline Devin, Nicholas Rhinehart, Chelsea Finn, Dinesh Jayaraman, and Sergey Levine. Smirl: Surprise minimizing reinforcement learning in unstable environments. *arXiv preprint arXiv:1912.05510*, 2019.

[7] Christopher M Bishop and Nasser M Nasrabadi. *Pattern recognition and machine learning*, volume 4. Springer, 2006.

[8] Greg Brockman, Vicki Cheung, Ludwig Pettersson, Jonas Schneider, John Schulman, Jie Tang, and Wojciech Zaremba. Openai gym. *arXiv preprint arXiv:1606.01540*, 2016.

[9] Tom Brown, Benjamin Mann, Nick Ryder, Melanie Subbiah, Jared D Kaplan, Prafulla Dhariwal, Arvind Neelakantan, Pranav Shyam, Girish Sastry, Amanda Askell, et al. Language models are few-shot learners. *Advances in neural information processing systems*, 33:1877–1901, 2020.

[10] Yuri Burda, Harrison Edwards, Amos Storkey, and Oleg Klimov. Exploration by random network distillation. *arXiv preprint arXiv:1810.12894*, 2018.

[11] Víctor Campos, Pablo Sprechmann, Steven Hansen, André Barreto, Steven Kapturowski, Alex Vitvitskyi, Adrià Puigdomènech Badia, and Charles Blundell. Coverage as a principle for discovering transferable behavior in reinforcement learning. *CoRR*, abs/2102.13515, 2021.

[12] Víctor Campos, Alexander Trott, Caiming Xiong, Richard Socher, Xavier Giró-i Nieto, and Jordi Torres. Explore, discover and learn: Unsupervised discovery of state-covering skills. In *International Conference on Machine Learning*, pages 1317–1327. PMLR, 2020.

[13] Nuttapong Chentanez, Andrew Barto, and Satinder Singh. Intrinsically motivated reinforcement learning. *Advances in neural information processing systems*, 17, 2004.

[14] Thomas M Cover. *Elements of information theory*. John Wiley & Sons, 1999.

[15] Benjamin Eysenbach, Abhishek Gupta, Julian Ibarz, and Sergey Levine. Diversity is all you need: Learning skills without a reward function. In *International Conference on Learning Representations*, 2019.

[16] Benjamin Eysenbach, Ruslan Salakhutdinov, and Sergey Levine. The information geometry of unsupervised reinforcement learning. *arXiv preprint arXiv:2110.02719*, 2021.

[17] Arnaud Fickinger, Natasha Jaques, Samyak Parajuli, Michael Chang, Nicholas Rhinehart, Glen Berseth, Stuart Russell, and Sergey Levine. Explore and control with adversarial surprise. *arXiv preprint arXiv:2107.07394*, 2021.

[18] Karl Friston. The free-energy principle: a unified brain theory? *Nature reviews neuroscience*, 11(2):127–138, 2010.

[19] Karl Friston, Thomas FitzGerald, Francesco Rigoli, Philipp Schwartenbeck, Giovanni Pezzulo, et al. Active inference and learning. *Neuroscience & Biobehavioral Reviews*, 68:862–879, 2016.

[20] Karl Friston, James Kilner, and Lee Harrison. A free energy principle for the brain. *Journal of physiology-Paris*, 100(1-3):70–87, 2006.

[21] Karol Gregor, Danilo Jimenez Rezende, and Daan Wierstra. Variational intrinsic control. *ArXiv*, abs/1611.07507, 2017.

[22] Abhishek Gupta, Benjamin Eysenbach, Chelsea Finn, and Sergey Levine. Unsupervised meta-learning for reinforcement learning. *arXiv preprint arXiv:1806.04640*, 2018.

[23] Michael Gutmann and Aapo Hyvärinen. Noise-contrastive estimation: A new estimation principle for unnormalized statistical models. In *Proceedings of the thirteenth international conference on artificial intelligence and statistics*, pages 297–304. JMLR Workshop and Conference Proceedings, 2010.

[24] Steven Hansen, Will Dabney, Andre Barreto, Tom Van de Wiele, David Warde-Farley, and Volodymyr Mnih. Fast task inference with variational intrinsic successor features. *arXiv preprint arXiv:1906.05030*, 2019.

[25] Kaiming He, Xinlei Chen, Saining Xie, Yanghao Li, Piotr Dollár, and Ross Girshick. Masked autoencoders are scalable vision learners. *arXiv preprint arXiv:2111.06377*, 2021.

[26] Maximilian Igl, Andrew Gambardella, Jinke He, Nantas Nardelli, N Siddharth, Wendelin Boehmer, and Shimon Whiteson. Multitask soft option learning. In Jonas Peters and David Sontag, editors, *Proceedings of the 36th Conference on Uncertainty in Artificial Intelligence (UAI)*, volume 124 of *Proceedings of Machine Learning Research*, pages 969–978. PMLR, 03–06 Aug 2020.

[27] Michał Kempka, Marek Wydmuch, Grzegorz Runc, Jakub Toczek, and Wojciech Jaśkowski. Vizdoom: A doom-based ai research platform for visual reinforcement learning. In *2016 IEEE conference on computational intelligence and games (CIG)*, pages 1–8. IEEE, 2016.

[28] Michael Laskin, Hao Liu, Xue Bin Peng, Denis Yarats, Aravind Rajeswaran, and Pieter Abbeel. CIC: Contrastive intrinsic control for unsupervised skill discovery, 2022.

[29] Michael Laskin, Denis Yarats, Hao Liu, Kimin Lee, Albert Zhan, Kevin Lu, Catherine Cang, Lerrel Pinto, and Pieter Abbeel. URLB: Unsupervised reinforcement learning benchmark. In *Thirty-fifth Conference on Neural Information Processing Systems Datasets and Benchmarks Track (Round 2)*, 2021.

[30] Lisa Lee, Benjamin Eysenbach, Emilio Parisotto, Eric Xing, Sergey Levine, and Ruslan Salakhutdinov. Efficient exploration via state marginal matching. *arXiv preprint arXiv:1906.05274*, 2019.

[31] Timothy P Lillicrap, Jonathan J Hunt, Alexander Pritzel, Nicolas Heess, Tom Erez, Yuval Tassa, David Silver, and Daan Wierstra. Continuous control with deep reinforcement learning. *arXiv preprint arXiv:1509.02971*, 2015.

[32] Hao Liu and Pieter Abbeel. Aps: Active pretraining with successor features. In *International Conference on Machine Learning*, pages 6736–6747. PMLR, 2021.

[33] Hao Liu and Pieter Abbeel. Behavior from the void: Unsupervised active pre-training. *Advances in Neural Information Processing Systems*, 34, 2021.

[34] Damiano Lombardi and Sanjay Pant. Nonparametric k-nearest-neighbor entropy estimator. *Physical Review E*, 93(1):013310, 2016.

[35] Takeru Miyato, Toshiki Kataoka, Masanori Koyama, and Yuichi Yoshida. Spectral normalization for generative adversarial networks. *arXiv preprint arXiv:1802.05957*, 2018.

[36] Shakir Mohamed and Danilo Jimenez Rezende. Variational information maximisation for intrinsically motivated reinforcement learning. *Advances in neural information processing systems*, 28, 2015.

[37] Aaron van den Oord, Yazhe Li, and Oriol Vinyals. Representation learning with contrastive predictive coding. *arXiv preprint arXiv:1807.03748*, 2018.

[38] Deepak Pathak, Pulkit Agrawal, Alexei A Efros, and Trevor Darrell. Curiosity-driven exploration by self-supervised prediction. In *International conference on machine learning*, pages 2778–2787. PMLR, 2017.

[39] Deepak Pathak, Dhiraj Gandhi, and Abhinav Gupta. Self-supervised exploration via disagreement. In *International conference on machine learning*, pages 5062–5071. PMLR, 2019.

[40] Miruna Pîslar, David Szepesvari, Georg Ostrovski, Diana Borsa, and Tom Schaul. When should agents explore? *arXiv preprint arXiv:2108.11811*, 2021.

[41] Nicholas Rhinehart, Jenny Wang, Glen Berseth, John Co-Reyes, Danijar Hafner, Chelsea Finn, and Sergey Levine. Information is power: Intrinsic control via information capture. *Advances in Neural Information Processing Systems*, 34, 2021.

[42] Archit Sharma, Michael Ahn, Sergey Levine, Vikash Kumar, Karol Hausman, and Shixiang Gu. Emergent real-world robotic skills via unsupervised off-policy reinforcement learning. *arXiv preprint arXiv:2004.12974*, 2020.

[43] Archit Sharma, Shixiang Gu, Sergey Levine, Vikash Kumar, and Karol Hausman. Dynamics-aware unsupervised discovery of skills. *arXiv preprint arXiv:1907.01657*, 2019.

[44] Harshinder Singh, Neeraj Misra, Vladimir Hnizdo, Adam Fedorowicz, and Eugene Demchuk. Nearest neighbor estimates of entropy. *American journal of mathematical and management sciences*, 23(3-4):301–321, 2003.

[45] DJ Strouse, Kate Baumli, David Warde-Farley, Vlad Mnih, and Steven Hansen. Learning more skills through optimistic exploration. *arXiv preprint arXiv:2107.14226*, 2021.

[46] Chenyu Sun, Hangwei Qian, and Chunyan Miao. From psychological curiosity to artificial curiosity: Curiosity-driven learning in artificial intelligence tasks. *arXiv preprint arXiv:2201.08300*, 2022.

[47] Richard S Sutton and Andrew G Barto. *Reinforcement learning: An introduction.* 2018.

[48] Yuval Tassa, Yotam Doron, Alistair Muldal, Tom Erez, Yazhe Li, Diego de Las Casas, David Budden, Abbas Abdolmaleki, Josh Merel, Andrew Lefrancq, et al. Deepmind control suite. *arXiv preprint arXiv:1801.00690*, 2018.

[49] Manan Tomar, Utkarsh A Mishra, Amy Zhang, and Matthew E Taylor. Learning representations for pixel-based control: What matters and why? *arXiv preprint arXiv:2111.07775*, 2021.

[50] Kelvin Xu, Siddharth Verma, Chelsea Finn, and Sergey Levine. Continual learning of control primitives: Skill discovery via reset-games. *Advances in Neural Information Processing Systems*, 33:4999–5010, 2020.

[51] Denis Yarats, Rob Fergus, Alessandro Lazaric, and Lerrel Pinto. Mastering visual continuous control: Improved data-augmented reinforcement learning. *arXiv preprint arXiv:2107.09645*, 2021.

[52] Denis Yarats, Rob Fergus, Alessandro Lazaric, and Lerrel Pinto. Reinforcement learning with prototypical representations. In *International Conference on Machine Learning*, pages 11920–11931. PMLR, 2021.