# Learning by Self-Explaining

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## Abstract

Artificial intelligence (AI) research has a long track record of drawing inspirations from findings from biology, in particular human intelligence. In contrast to current AI research that mainly treats explanations as a means for model inspection, a somewhat neglected finding from human psychology is the benefit of self-explaining in an agents' learning process. Motivated by this, we introduce a novel learning paradigm, termed **Learning by Self-Explaining** (LSX). The underlying idea is that a learning module (learner) performs a base task, e.g. image classification, and provides explanations to its decisions. An internal critic module next evaluates the quality of these explanations given the original task. Finally, the learner is refined with the critic's feedback and the loop is repeated as required. The intuition behind this is that an explanation is considered "good" if the critic can perform the same task given the respective explanation. Despite many implementation possibilities the structure of any LSX instantiation can be taxonomized based on four learning modules which we identify as: Fit, Explain, Reflect and Revise. In our work, we provide distinct instantiations of LSX for two different learner models, each illustrating different choices for the various LSX components. We broadly evaluate these on several datasets and show that Learning by Self-Explaining not only boosts the generalization abilities of AI models, particularly in small-data regimes, but also aids in mitigating the influence of confounding factors, as well as leading to more task-specific and faithful model explanations. Overall, our results provide experimental evidence of the potential of self-explaining within the learning phase of an AI model.

## 1 Introduction

Self-reflection is considered an important building block of human intelligence and a crucial component in the learning process and knowledge development of humans (Gläser-Zikuda, 2012; Ellis et al., 2014). In fact, one aspect of self-reflection—self-explaining—has been identified in several psychological studies as greatly beneficial for the overall learning, problem-solving and comprehension abilities of human subjects (Chi, 2018; Chi et al., 1981; 1994; Chamberland & Mamede, 2015; Belobrovy, 2018; Larsen et al., 2013; Kwon & Jonassen, 2011; Bisra et al., 2018). Accordingly, self-explanations act as a means of making initially implicit knowledge explicit and thereby allow for iterative and critical *self-refinement*.

Indeed, recent works in AI research have picked up on the idea of self-refining, either directly inspired by findings from human studies (Madaan et al., 2023) or otherwise motivated *e.g.*, by the potential of pre-trained large language models (LLMs), *e.g.*, on the topics of self-debiasing (Schick et al., 2021) and self-instructing (Wang et al., 2023). Although these works are quite specific in their form of self-refinement (*cf.* Pan et al. (2023) for a recent survey) and far from the general idea of self-reflection from human psychology, they provide valuable first steps for more *reflective AI*. However, none of these focus on the value and potential of (self-)explanations as the basis and means of such reflective processes. On the other hand, research on interactive machine learning (Teso et al., 2023; Gao et al., 2022) such as explanatory interactive learning (XIL) (Teso & Kersting, 2019; Schramowski et al., 2020) has long identified the value of explanations as a means of communication between human users and AI models and particularly as a means for model refinement. However, hereby explanations are only leveraged for refinement through human guidance.

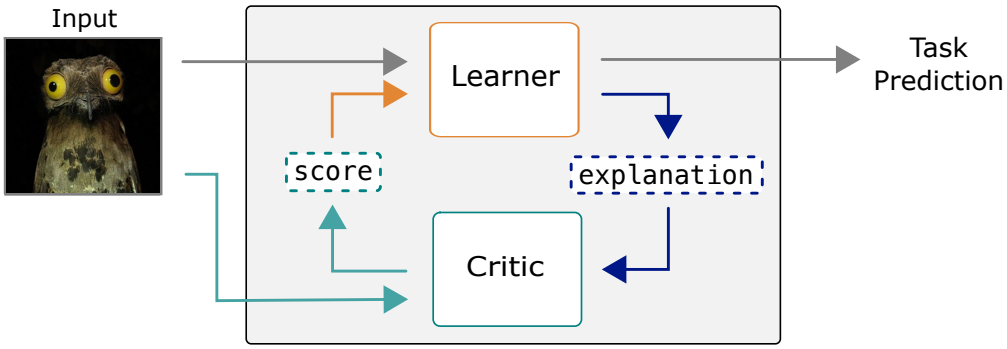


Figure 1: Learning by Self-Explaining (LSX) is a general learning framework that can be integrated into any base learning task, *e.g.*, image classification. It is characterized by two submodels, a *learner* and *critic*, and four distinct training modules: Fit, Explain, Reflect and Revise. Briefly, the learner is optimized for a base task in Fit, after which it provides `explanations` to its decisions in Explain. In the Reflect module these explanations are passed to the critic, which "reflects" on the quality of these explanations. In other words, the critic evaluates how useful the explanations are for performing the base task. The resulting feedback from the critic, `score`, is used to update the learner's representations in Revise. This loop can be repeated as needed.

In this work, we therefore introduce a novel machine learning paradigm called Learning by Self-Explaining (LSX) which leverages explanations in the learning phase of an AI model prior to any form of explanatory human guidance. The main idea is that an AI model consists of two submodels, a *learner* and a *critic*. The learning process in LSX is characterized by four learning modules sketched in Fig. 1. The learner is trained on a base task in Fit, after which it provides explanations for that task in Explain. The critic next performs the same task as the learner, but receives the input *and* corresponding explanations, thereby assessing the quality of these explanations for performing the original task. Intuitively, a "usefull" explanation should thereby provide important information for the task at hand. Finally, the critic's feedback is returned to the learner for revision in the Revise module and the Explain, Reflect and Revise loop is repeated, if needed[1]. In the context of introducing LSX, we further present two instantiations of LSX for training a convolutional neural network (CNN) and the neuro-symbolic concept learner of Stammer et al. (2021) (NeSyCL), thereby illustrating specific configurations of the submodels and learning modules of LSX as well as the flexibility of the paradigm. In the context of our experimental evaluations on multiple datasets, we show that LSX boosts the generalisability of the base learners, particularly in the small data regime. Moreover, we show that LSX helps mitigate the influence of confounding factors and leads to more consolidated, task-specific and faithful model explanations.

In summary, our contributions are the following: (i) We introduce a novel learning paradigm for machine learning, based on a model self-refining itself by evaluating its own explanations. (ii) We introduce two different instantiations of LSX, illustrating different submodel and learning module configuration choices. (iii) We provide extensive experimental evidence on various datasets and evaluation metrics, illustrating the benefits and potential of LSX.

We proceed as follows. In section 2, we formally introduce the LSX paradigm. In section 3, we next introduce two specific instantiations that integrate LSX into their training procedure. In our experimental evaluations in section 4, we provide results on various datasets and metrics illustrated via both LSX instantiations. We finish our work with an extensive discussion on related work and leave the reader with a final conclusion. [2]

## 2 Learning by Self-Explaining (LSX)

LSX is not explicitly bound to any one type of model implementation, data domain or base learning task, but can be considered a general learning approach for any base learner. In this section, we therefore give an

[1] Specifically, within the context of LSX we consider the two submodels to constitute a collective model, whereby both work jointly to perform the same base task. The overall model thus performs learning by explaining to parts of "itself".

[2] Code will be made available soon.

overview of the basic set of modules that characterize LSX before continuing with two specific instantiations in the next section. Let us first provide the background notations.

For simplicity, we introduce LSX here in the context of supervised image classification as base task. More formally, let $x_i \in X$ be an image, with the full dataset $X := [x_1, ..., x_N] \in \mathcal{R}^{N \times L \times M}$, and with corresponding class label to each $x_i$ defined as $y_i \in \{1, ...K\}$. Hereby, $N$ represents the number of data samples, $L$ and $M$ the image dimensions and $K$ the maximal number of image classes. Furthermore, let $X$ be split into a train and test split $X = \{(X_{train}, y_{train}), (X_{test}, y_{test})\}$ with $y_{train}$ representing the set of corresponding image class labels of the training set and $y_{test}$ those of test set. The learner is provided the tuple set $\bar{X}_f = (X_f, y_f) = (X_{train}, y_{train})$ where we denote $y_f = y_{train}$ specifically as the label set provided to the learner. The critic set, $\bar{X}_c$, can represent a subset of $\bar{X}_f$ *e.g.*, $\bar{X}_c \subseteq \bar{X}_f$, but also a previously separated set from the test set (details below). Also for the critic we specifically denote $y_c$ as the label set of the $\bar{X}_c$.

Moreover, let us denote the two submodels: the learner as $f$ and critic as $c$. The learner can represent any desired learning model suited for the base task, e.g. a convolutional neural network (CNN). Also $c$ can in principle be instantiated by any AI model. The general procedure of LSX can be described via four modules Fit, Explain, Reflect and Revise, where the last three modules describe the core of LSX and can be repeated until an iteration budget $T$ is reached. Let us now describe these four modules (presented in pseudo-code in Alg. 1 in the App.) in more detail.

**Base task** (Fit). The Fit module describes the underlying, base learning task in which the learner is optimized to solve a particular problem, *e.g.*, supervised image classification. Overall, this module is independent of LSX as it represents the standard, data-driven machine learning approach. More specifically, in Fit, $f$ is provided with the training dataset, $\bar{X}_f$, makes predictions given the base task, $\hat{y}_f = f(X_f)$, and optimizes its latent representations given the corresponding loss function, $l_{\text{B}}$. This loss function can *e.g.*, correspond to the cross-entropy loss, $l_{\text{B}} = l_{\text{CE}}(\hat{y}_f, y_f)$ when considering supervised classification. However, the underlying task can correspond to any form of learning (*e.g.*, other forms of supervision) and can contain any bells and whistles of modern machine learning setups (*e.g.*, hyperparameter optimization, learning rate schedulers, etc.). Finally, Fit returns a model optimized for the base task, $f = \text{Fit}(f, \bar{X}_f)$.

**Obtain explanations** (Explain). Explain represents the first of three core modules of LSX. In this module $f$ provides explanations to its decisions given a set of data samples, $X_c$. This is achieved via a predefined explanation method which returns an `explanation` for each sample, $E_c = \text{Explain}(f, X_c)$, where $E_c := \{e_1, ..., e_{|X_c|}\}$. If $\bar{X}_c$ contains ground-truth annotations, explanations can be queried given the ground-truth labels ($E_c = \text{Explain}(f, X_c|y_c)$), otherwise the learner provides `explanations` given its predictions. Hereby $\bar{X}_c$ can be a subset of $\bar{X}_f$ (*i.e.*, $\bar{X}_c \subseteq \bar{X}_f$), but can also represent a separate set that is with-held during the initial optimization of $f$ (*i.e.*, $\bar{X}_c \cap \bar{X}_f = \emptyset$). Overall, this explanation module can be realized with any explanation method from the vast literature of XAI (*cf.* Guidotti et al. (2018); Ras et al. (2022b); Liao & Varshney (2021); Carvalho et al. (2019)). Given the architectural constraints of the learner, it can, *e.g.*, be an explanation in form of an importance map that indicates the degree by which a part of the input was important for a model's decision, an inherent concept-based explanation representing the activation of specific concepts that are present in an input, but also a generated natural language explanation, to name a few. Notably, this module is commonly also found in XIL (Friedrich et al., 2023) approaches. In summary, this module returns explanations, $E_c$, from the learner.

**Reflect on explanations** (Reflect). In the second core module, and arguably most distinctive module of LSX, the high-level role of the critic is to "reflect" on the quality of the explanations. This is an abstract measure and in LSX is quantified by the ability of the critic to perform the base task, given the learner's explanations. This explanation evaluation is performed in the Reflect module whereby the critic returns a `score` of the learner's `explanations`, given $E_c$ and the corresponding original data that was used for generating these explanations, $\bar{X}_c$. In other words, `score` represents an indication of how well the critic performs the base task on the data $\bar{X}_c$ given the additional knowledge of the provided explanations, $E_c$ (an idea that is related to (Pruthi et al., 2022)). What `score` exactly represents depends very much on the model type of the critic. For example, it can represent the signal from a classification loss function over $\bar{X}_c$ and $E_c$ or a scoring of how probable an explanation is given the evidence of $\bar{X}_c$. By evaluating the quality of explanations based on their benefit in solving a task, the Reflect module represents one of the core aspects

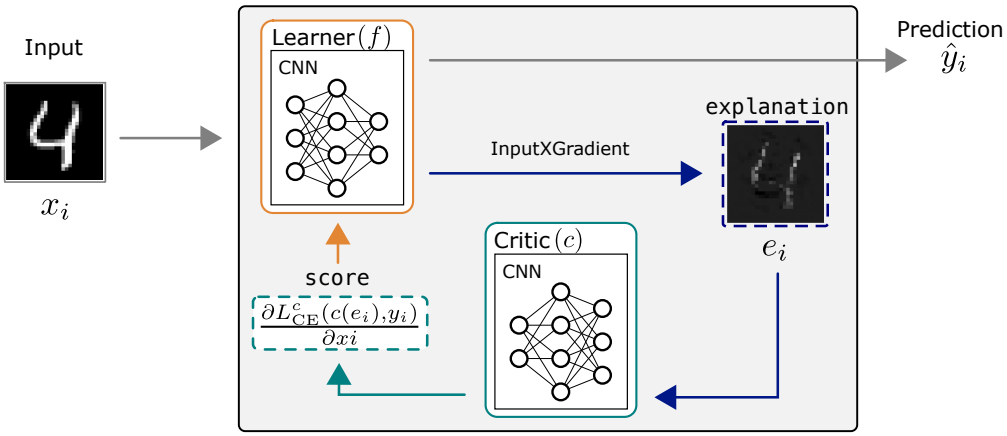


Figure 2: CNN-LSX: Learning by Self-Explaining instantiation for training CNNs for supervised image classification. Here CNNs represent both the *learner* and *critic*. Explanations are generated via InputXGradient. The `score` represents the classification loss signal of the critic on these explanations.

of LSX. Overall, explanations are thus treated not just as a one-way approach for indicating the importance of features when making a prediction (as often done in XAI). Rather, LSX specifically contributes to the view of explanations as verifiable rationales as in Fok & Weld (2023).

**Integrate feedback on explanations** (Revise). In the last module of an LSX loop, the feedback signal, `score`, obtained from the critic in the Reflect module, is used to refine the learner within Revise. This revision module can be realized in one of the many ways provided in interactive learning settings (Teso & Kersting, 2019; Friedrich et al., 2023). Standard revision tools entail loss-based methods (Ross et al., 2017; Selvaraju et al., 2019) as well as more parameter-efficient finetuning alternatives (Houlsby et al., 2019; Hu et al., 2022). But also non-differentiable revision approaches can be considered, *e.g.*, data augmentation approaches (Teso & Kersting, 2019) or retrieval-based setups that store the revisory feedback in an explicit revision engine (Friedrich et al., 2022; Tandon et al., 2022). In our LSX instantiations, we implement the revision step by adding an additional explanation loss, $l_{\text{expl}}$ (*e.g.*, a HINT-like loss (Selvaraju et al., 2019) and a cross-entropy loss of the critic's classification) to the optimization process. The learner is thus jointly optimized in Revise via $L = l_{\text{B}} + \lambda l_{\text{expl}}$, where $\lambda \in \mathbb{R}$ represents a scaling factor.

## 3 Instantiating LSX

Many implementation details in the above overview depend strongly on the exact choice of the LSX components. Importantly, these are interdependent, *e.g.*, the choice of explanation method influences how the critic can evaluate the explanations, the choice of critic module influences the way the feedback score is computed, but also how this is integrated into the learner, etc. To give a better understanding of these abstract modules, in this section, we introduce two instantiations of how to integrate different base setups into LSX, where we refer to App. B.1 and B.2 for further details. These instantiations will also be the point of investigation in our experimental evaluations. Both differ in several LSX components. Importantly, these two instantiations are by no means conclusive in how to integrate a base task into LSX, but serve as illustrations of how to integrate LSX into different models. We conclude this section with a more general perspective of Learning by Self-Explaining.

### 3.1 Neural and Neurosymbolic Instantiations

**CNN-LSX via differentiable feedback score.** We begin with a CNN-based setup shown in Fig. 2 (*cf.* App. B.1 for formulas and further details). This instantiation which we denote as CNN-LSX consists of a standard CNN as learner, $f$, and a duplicate of the learner as critic, $c$. Specifically, in this instantiation the learner is trained on raw images to predict the corresponding class labels and is optimized via a cross-entropy loss as $l_{\text{B}} := l^f_{\text{CE}}(f(X_f), y_f)$, thus representing the Fit module. The explain module is realized

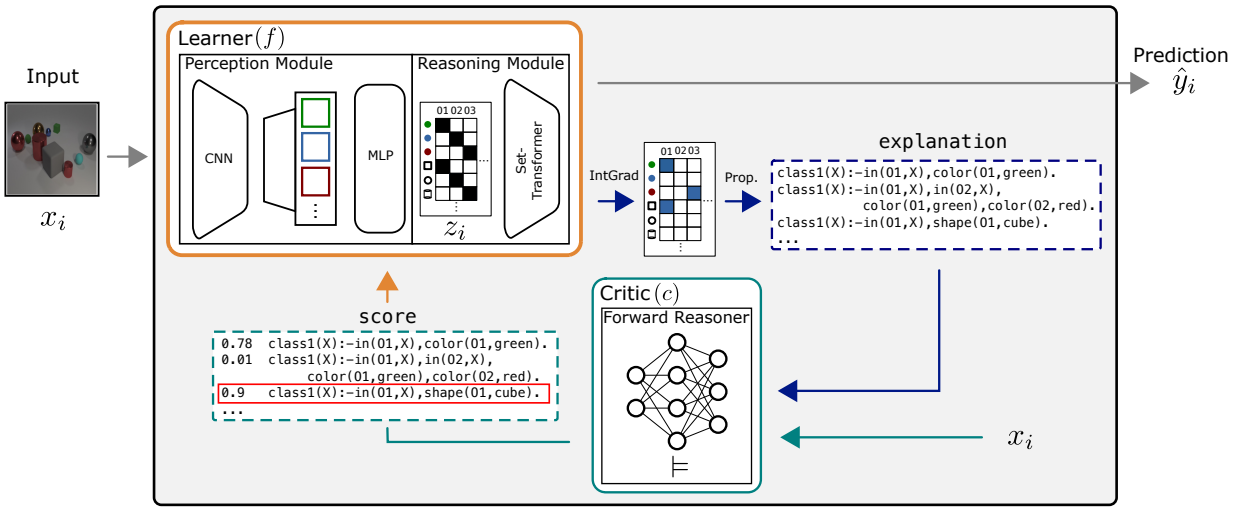


Figure 3: NeSyCL-LSX: Learning by Self-Explaining instantiation for supervised image classification via neuro-symbolic concept learner. The critic represents a neuro-symbolic forward reasoner, which computes all possible consequences in a differentiable manner given visual and logical input. An `explanation` represents a logical statement that is derived from concept-level saliency maps. The feedback `score` represents a probabilistic ranking of these logical explanations with which we identify the most likely explanation per image class and revise the learner to only produce this explanation.

with the post-hoc, differentiable InputXGradient method (Shrikumar et al., 2017; Hechtlinger, 2016) and we compute $E_c = \textsc{Explain}(X_c|y_c)$ with $\bar{X}_c \subseteq \bar{X}_f$. Specifically, an explanation via InputXGradient represents importance values per input pixel for the model's decision. It is based on taking the partial derivatives of the output with respect to the input and multiplying this with the input. Thus, as an InputXGradient `explanation` also contains the input, it is not required to separately pass $X_c$ to the critic. In the Reflect module, the critic therefore only receives these explanations as input and predicts the corresponding class labels from these $\hat{y}_c = c(E_c)$. The quality of the predictions is quantified via a second cross-entropy loss averaged over all samples in $E_c$, denoted as $l^c_{\text{CE}}(c(E_c), y_c)$. Next, in Revise, $f$ is optimized via the joint loss $L = l^f_{\text{CE}}(f(X_f), y_f) + \lambda l^c_{\text{CE}}(c(E_c), y_c)$. In other words, the learner's parameters are updated based on both classification losses: the one from the learner given the training images $X_f$ *and* that from the critic given the explanations of $X_c$. Lastly, we perform the final Revise step (*i.e.*, when iteration budget $T$ has been reached) with both loss functions evaluated on $X_f$: $L = l^f_{\text{CE}}(f(X_f), y_f) + \lambda l^c_{\text{CE}}(c(E_f), y_f)$.

**NeSyCL-LSX via non-differentiable feedback score.** Next, we will introduce an instantiation around the neuro-symbolic concept learner (NeSyCL) of Stammer et al. (2021) as base model (learner). We denote this instantiation as NeSyCL-LSX (*cf.* Fig. 3 and App. B.2 for formulas and further details). The NeSyCL consists of a slot attention-based perception module (Locatello et al., 2020) and set-transformer-based reasoning module (Lee et al., 2019). An image, $x_i$, is first processed by a pretrained perception module into a symbolic representation, $z_i \in [0,1]^{O \times A}$, indicating the presence of objects and their attributes in the corresponding image. Here, $O$ indicates the number of objects (or slots) and $A$ the number of predicted attributes. The reasoning module next makes a final class prediction given $z_i$. As in the CNN-LSX instantiation, NeSyCL-LSX performs supervised image classification. This is the base task in the Fit module with $l_{\text{B}}$ representing a cross-entropy loss. Obtaining `explanations` (Explain) is based on the approach of (Stammer et al., 2021) where saliency maps of $z_i$ are created via Integrated Gradients (Sundararajan et al., 2017). These thus indicate which objects and which of their attributes are relevant for a prediction, denoted here as $e'_i \in [0,1]^{O \times A}$. By thresholding via an additional hyperparameter, $\delta \in [0,1]$, these saliency maps are binarized to $e''_i \in \{0,1\}^{O \times A}$. We next propositionalize $e''_i$ by representing the explanation as a set of logical rules that are present in $e''_i$. These rules consist of conjunctive combinations of the important attributes and objects. We denote this set of candidate explanatory rules as $e_i$. Finally, by iterating over all samples in $X_c$ and grouping the resulting candidate rules by image class we receive a set of candidate rules per

class as $E_c = \{e^1, ..., e^K\}$. Moving on to the next modules, the critic in NeSyCL-LSX is represented by the neuro-symbolic forward reasoner of (Shindo et al., 2021; 2023), which computes all possible consequences in a differentiable manner given visual and logical input. In the Reflect module the forward reasoner evaluates the `explanations`, $E_c$, by estimating the validity of each candidate explanation rule given the data in $\bar{X}_c$. Finally, based on the resulting estimated probabilities (`score`), the most probable rule per class $j$ is chosen, denoted as $e^j_{\text{max}}$, and $E_{\text{max}} = \{e^1_{\text{max}}, ..., e^K_{\text{max}}\}$ is passed back to the learner (Revise). Here, these logical explanations are next transformed back into binary vector form in the dimensions of the learner's original symbolic representation, $\bar{E}_{\text{max}} = \{\bar{e}^1_{\text{max}}, ..., \bar{e}^K_{\text{max}}\}$ with $\bar{e}^j_{\text{max}} \in \{0, 1\}^{O \times A}$. Finally, $f$ is updated via an additional mean-squared-error loss between the learner's explanations and these transformed explanations leading to $L = l^f_{\text{CE}}(f(X_f), y_f) + \lambda l_{\text{MSE}}(\bar{E}_{\text{max}}, E_f)$.

**Configuration choices.** As mentioned, many instantiations of LSX are possible, each with their own specific module and configuration choices. The instantiations introduced in this work, however, already sketch some interesting aspects and differences which we wish to highlight here. The most fundamental difference between CNN-LSX and NeSyCL-LSX lies within their Reflect modules, specifically how a `score` of the learner's `explanations` are computed. In CNN-LSX the `score` represents a differentiable signal, where in NeSyCL-LSX this represents a probabilistic ranking of logical explanations. This second form of critiquing allows to weigh explanations and *e.g.*, identify the most "useful" explanation. The first form of critiquing, on the other hand, allows to fine-tune explanations. Related to this and concerning the Explain modules, where in CNN-LSX *continuous* input-level `explanations` are being processed, the logical `explanations` in NeSyCL-LSX are *discrete*. As an effect of this, the form of revision in the Revise module differs. In CNN-LSX we can simply pass the backpropagated signal from the critic to the learner via a classification loss. In NeSyCL-LSX we identify the most-likely explanation. Additionally, in CNN-LSX the critic represents a duplicate CNN of its learner. In NeSyCL-LSX, on the other hand, the critic represents a different model type altogether compared to its learner.

### 3.2 General Perspective

In the following, we wish to provide a general perspective for LSX on important current challenges of AI.

**Human-machine interactions.** Accurate and trustworthy human-machine interactions have been identified as important criteria for the future deployability of AI systems (Friedrich et al., 2023; Teso et al., 2023; Holzinger, 2021; Angerschmid et al., 2022). Whereas much of ML research is not developed with this in mind the LSX framework automatically facilitates the development and integration of mechanisms that allow for fruitful human-machine interactions. *E.g.*, via the Explain module a human user can query the learner's reasons for a prediction and via the Revise module integrate feedback on these explanations into the model. As explanations in LSX explicitly act as the means for revision and bidirectional communication between the two submodels, LSX fits well into the line of research that has identified the importance of leveraging explanations for bi-directional communication between human user and AI model (Teso et al., 2023). Finally, LSX does not ultimately remove the need for human-machine interactions for a sustainable model deployment, rather it can be used for an AI model to reflect on its learned reasons before receiving important human feedback. Deploying LSX in this way potentially reduces the amount and costs of human resources required (Friedrich et al., 2023).

**System 1 and 2 processing.** A prominent and well-studied hypothesis from cognitive psychology is that human cognition is mainly composed of two systems: an approximate, fast processing system (system 1) that handles the majority of familiar, daily situations and an embedded, slower, yet more exact system (system 2) that handles processing in more unfamiliar settings (Kahneman, 2011). This idea has recently gained much interest in the AI community (Goyal & Bengio, 2022; Kautz, 2022; Ganapini et al., 2022; Booch et al., 2021) and we here highlight several connections that can be made between the system 1 and 2 processing framework and Learning by Self-Explaining. Similar to the system 1 and 2 framework, within LSX there are two processing systems where one is embedded in the other. This differentiation is not necessarily based on the two submodels (*learner* and *critic*, *cf.* Fig. 1), but rather on the learning modules (*cf.* Alg. 1). Hereby, Fit takes over the fast, initial processing phase, and the triad consisting of Explain, Reflect and Revise results in a slower, embedded processing phase.

A major open question, particularly in AI research on system 1 and 2 processing, is what form of communication the two systems should be using (Goyal & Bengio, 2022; Kautz, 2022). In our work, we consider explanations to represent a valuable means of communication between the different systems. Specifically, the learner provides initial, associative explanations to its decisions which, in turn, are either directly interpreted as (*cf.* CNN-LSX) or transformed (*cf.* NeSyCL-LSX) into verifiable and refinable rationales. In line with Goyal & Bengio (2022), the process of explaining and reflecting on the learner's explanations can thus be seen as making the implicit knowledge of the learner explicit. At the same time, system 2 can also influence the processing of system 1. Evidence for this can be seen in our findings on explanation consolidation (*cf.* Tab. 3), where the critic's feedback leads to the learner adapting its explanations to represent more task-specific rationales. Lastly, relating to Henry Kautz's proposed Neuro[Symbolic] approach (Kautz, 2022) for AI system 1 and 2 processing, our NeSyCL-LSX has many parallels concerning the integration of neural and symbolic components. LSX in general, however, does not necessarily require a specific model type, but rather aims for an integration of any type of model via explanations.

## 4 Experimental Evidence

In the following experiments, we investigate the benefits of Learning by Self-Explaining with the help of two instantiations, CNN-LSX and NeSyCL-LSX. Specifically, we compare the performances of LSX to the standard training setup (*i.e.*, supervised learning). Over the course of our evaluations, we will investigate the potential benefits of LSX concerning test-set generalization, explanation consolidation, explanation faithfulness and shortcut learning mitigation.

### 4.1 Experimental Setup

**Data.** We provide experimental results on four different datasets. Particularly, we evaluate CNN-LSX on the MNIST (LeCun et al., 1989) and ChestMNIST (Yang et al., 2023; Wang et al., 2017) datasets and NeSyCL-LSX on the concept-based datasets CLEVR-Hans3 (Stammer et al., 2021) and a variant of Caltech-UCSD Birds-200-2011 dataset (Wah et al., 2011), CUB-10 (*cf.* App. C). Overall, the number of training images in MNIST corresponds to 60k, in ChestMNIST to 78k, in CLEVR-Hans3 to 9k and in CUB-10 to 300 images. Finally, for investigating the effect of confounding factors as a form of shortcut learning (Geirhos et al., 2020), we evaluate accuracies on CLEVR-Hans3 and DecoyMNIST (Ross et al., 2017), a confounded variant of the MNIST dataset. In the confounded settings of CLEVR-Hans3 specific object attribute combinations are fully correlated at training time, but uncorrelated at test time. *E.g.*, all large cubes are gray in the train set, but have any color in the test set. In Decoy-MNIST, on the other hand, confounders represent grayscale boxes in the corners of the images. Though the position in any of the four corners is random for an MNIST digit class, specific grayscale values are tied to specific classes at train time, but are random at test time. We particularly refer to App. C for details on this.

**Metrics.** We provide evaluations of LSX based on five metrics where we briefly describe these here and refer to App. D for details. **(1)** The first metric is the standard *balanced classification accuracy* on a held-out test set. **(2)** For investigating the revised explanations via LSX we provide the classification accuracy of a linear, ridge regression model. This model is optimized to classify a set of the learner's explanations, given their corresponding ground-truth class labels and evaluated on a held-out set of explanations. **(3)** We further provide a cluster analysis based metric over all explanations, similar to the Dunn index (Dunn, 1973; 1974). This metric, which we denote as *Inter- vs. Intraclass Explanation Similarity* (IIES), quantifies how similar explanations are within one class, but dissimilar between classes (lower values indicate better separability). For investigating whether the learner in fact makes a decision based on the reported explanations, we analyse the faithfulness (Hooker et al., 2019; Chan et al., 2022) of the learner's explanations via two metrics as introduced by (DeYoung et al., 2020), namely **(4)** *sufficiency* and **(5)** *comprehensiveness*. Both metrics measure the impact on the model's performances of removing specific parts of the input based on the explanations. For comprehensiveness, parts of the input are removed which correspond to important features as identified by the explanation. For sufficiency, parts of the input are removed which correspond to unimportant features as identified by the explanation. For continuous input settings (MNIST and ChestMNIST) we modify the computation of these two metrics slightly by subtracting the impact when randomly chosen features are

Table 1: Improved (few-shot) generalization via LSX on various datasets and models. We here present the accuracy in % on a held-out test set across varying training set sizes.

| | MNIST | | |
|---|---|---|---|
| | 1.2k | 3k | full (60k) |
| CNN | 89.83±0.2 | 93.83±0.08 | **98.70**±0.1 |
| CNN-LSX | **91.59**±0.91 | **94.31**±0.43 | 98.03±0.2 |
| | ChestMNIST | | |
| | 1.6k | 4k | full (78k) |
| CNN | 58.68±0.15 | 58.49±0.31 | 60.86±0.08 |
| CNN-LSX | **61.16**±0.54 | **61.77**±0.75 | **63.41**±1.3 |
| | CLEVR-Hans3 | | |
| | 180 | 450 | full (9k) |
| NeSyCL | 91.40±1.80 | 96.81±0.94 | 99.00±0.28 |
| NeSyCL-LSX | **94.51**±1.94 | **97.34**±0.44 | **99.08**±0.17 |
| | CUB-10 | | |
| | 100 | 150 | full (300) |
| NeSyCL | 83.57±1.67 | 87.14±0.4 | 93.13±0.4 |
| NeSyCL-LSX | **84.49**±1.18 | **93.05**±1.72 | **96.33**±0.31 |
| avg. improvement | **2.07** | **2.55** | **1.29** |

Table 2: Mitigating confounders via LSX: Test set performances on confounded datasets, both with deconfounded samples during training (*w/ deconf.*) and without (*w/ conf.*).

| | DecoyMNIST | |
|---|---|---|
| | w/ conf. | w/ deconf. |
| CNN | 63.52±1.39 | 86.88±0.68 |
| CNN-LSX | **78.99**±2.71 | **88.43**±2.34 |
| | CLEVR-Hans3 | |
| | w/ conf. | w/ deconf. |
| NeSyCL | 85.96±4.20 | 91.23±1.2 |
| NeSyCL-LSX | **90.90**±4.38 | **95.64**±2.21 |

removed. This way we compensate for the potential influence of such out-of-distribution input. Notably, this can lead to negative values. In both formulations, however, higher comprehensiveness and lower sufficiency scores are better. Both metrics are not normalized and provide a relative comparison.

**Setup.** In all evaluations, we compare the performances of the LSX instantiations with the performances of the base learners that were trained for the same overall number of epochs, but only in the standard supervised manner. These are denoted as CNN and NeSyCL. We evaluate CNN-LSX on the MNIST and ChestMNIST datasets and NeSyCL-LSX on the CLEVR-Hans3 and CUB-10 datasets. The baselines were trained on the same data as the LSX versions, *i.e.*, $\bar{X}_f^{\text{baseline}} = \bar{X}_f^{\text{LSX}} \cup \bar{X}_c^{\text{LSX}}$. Note that for NeSyCL-LSX on CUB-10, we replaced the pretrained slot-attention module with a pretrained Inception-v3 network as perception module (Szegedy et al., 2016) and the reasoning module with a single linear layer as in (Koh et al., 2020). Hereby, the perception modules where pretrained to predict the symbolic representations, $z$, *i.e.*, relevant object attributes. These modules were used in the NeSyCL configurations both for the baseline as well as LSX configurations. Unless specifically noted, $\bar{X}_c$ represents a random subset of $\bar{X}_f$. We provide all results as mean values with standard deviations over five runs with different random seeds. Lastly, for investigating shortcut behavior we provide balanced accuracy scores on the unconfounded held-out test sets of Decoy-MNIST and CLEVR-Hans3 while being trained on the confounded train set. In the CLEVR-Hans3 evaluations that do not target evaluating the effect of confounding factors, the original confounded evaluation set of CLEVR-Hans3 was used as held-out test set.

### 4.2 Experimental Results

**Improved (few-shot) generalisation.** An intuitive aspect of psychological findings on learning via self-explaining is that reflecting on one's learned explanations leads to improved generalizable knowledge (Chi et al., 1994). We investigate LSX in our first evaluation by measuring the held-out test set accuracy of CNN-LSX on the MNIST and ChestMNIST datasets and of NeSyCL-LSX on the CLEVR-Hans3 and CUB-10 datasets. In the rightmost column of Tab. 1, we present the respective test set accuracies for all learning configurations when trained on the full training size of each dataset. We can observe that on average, *i.e.*, over all datasets and over both LSX instantiations, there is a substantial boost in test set accuracy (last row). In the remaining columns of Tab. 1, we present the test-set accuracy in the smaller-data regime, *i.e.*, when the models were trained on different-sized subsets of the original training set [3]. We can observe large performance gains with LSX for all configurations and datasets. Particularly, these improvements are on average greater than those observed on the full training set sizes. Altogether these results suggest that

[3] Hereby, the size of these subsets varies over the different datasets due to different specifics of each dataset, e.g. the original training set sizes.

Table 3: Explanation consolidation via LSX. The metrics here are Inter- vs. Intraclass Explanation Similarity (IIES) of a learner's explanations (left) and the classification accuracy of a ridge regression model (RR. Acc., in %) on the learner's explanations (right). Both metrics are proxies for the explanation similarity within a class, yet separability between classes.

| | IIES (↓) | RR Acc. (↑) |
|---|---|---|
| | MNIST | |
| CNN | 2.7±0.07 | 12.32±0.35 |
| CNN-LSX | **0.7**±0.01 | **99.91**±0.06 |
| | ChestMNIST | |
| CNN | 3.89±0.13 | 74.87±0.24 |
| CNN-LSX | **0.75**±0.05 | **99.92**±0.03 |
| | CLEVR-Hans3 | |
| NeSyCL | 0.65±0.07 | 93.48±2.41 |
| NeSyCL-LSX | **0.2**±0.06 | **100**±0.0 |
| | CUB-10 | |
| NeSyCL | 0.0266±0.0005 | **100**±0.0 |
| NeSyCL-LSX | **0.0024**±0.0001 | **100**±0.0 |

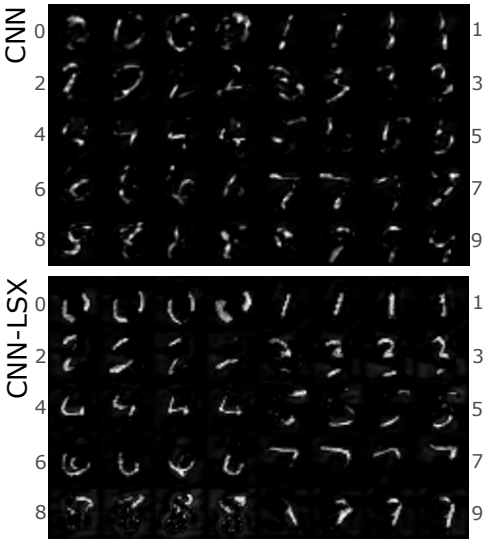


Figure 4: Exemplary explanations on MNIST of CNN baseline vs. CNN-LSX. Four random explanations are shown per image class (class ids on sides).

learning via self-explaining leads to improved test-set generalization performances with larger improvements, particularly in small-data regimes.

**Self-unconfounding.** In the second set of evaluations, we are interested in how far LSX can help mitigate shortcut behaviour (Geirhos et al., 2020). We particularly focus on confounded behaviour as a form of shortcut learning in which a learner picks up on spurious correlations within the training dataset that are not present in the test set (Schramowski et al., 2020). We investigate two settings. (i) With the first (denoted as *w/ conf.*), we investigate the performance of LSX in mitigating confounding behaviour without additional knowledge on the confounding factors. To this end, we train the two LSX instantiations (and baselines) as in the previous setups with $\bar{X}_c \subseteq \bar{X}_f$, and $\bar{X}_f$ representing a confounded dataset. (ii) In the second setting, $\bar{X}_c$ represents a dataset that is with-held from training the learner (*i.e.*, $\bar{X}_c \cap \bar{X}_f = \emptyset$) and represents a dataset that is explicitly deconfounded (*cf.* App. D.3 for details on the sizes of $\bar{X}_c$). In other words, the spurious correlation found in $X_f$ is not present in $\bar{X}_c$. We denote this case as *w/ deconf.* For the standard training scheme the models have access to $\bar{X}_c$ within their training phase. We evaluate the CNN-LSX configuration on the Decoy-MNIST dataset and the NeSyCL-LSX configuration on the CLEVR-Hans dataset.

In Tab. 2, we present the held-out test set accuracies of all configurations. We observe a strong improvement in performances when training LSX on the deconfounded critic sets (*w/ deconf.*), indicating that reflecting on the explanations of an explicitly deconfounded critic set can lead to much improved shortcut mitigation behaviour compared to the baseline learning setup.

Even more interesting is the result of the *w/ conf.* setting. We observe that the LSX trained models, though never having seen deconfounded data, lead to strong mitigation improvements. This result suggests great practical implications, as it does not require prior knowledge on the confounding factors. We hypothesize that the inductive biases of the specific explanation method and critic instantiation play a critical role for this effect. For example, the InputXGradient method (Explain) of CNN-LSX produces input-region-based explanations. The confounders in DecoyMNIST, on the other hand, represent gray-scale patches randomly placed in one of four corners where the digits themselves are rather consistently placed in the center of an image. Together with the results in Tab. 3 on more consistent, task-specific explanations this suggests that explanations based on more variable input-regions are more likely to be ignored via the reflection loop in LSX than explanations on the actual digits.

Table 4: Explanation faithfulness via LSX: Comprehensiveness and sufficiency results of explanations for models trained on all training samples.

| | Comp. (↑) | Suff. (↓) |
|---|---|---|
| | MNIST | |
| CNN | −1.34±0.39 | 23.11±1.18 |
| CNN-LSX | **16.49**±2.79 | **-0.21**±4.18 |
| | ChestMNIST | |
| CNN | 13.98±0.43 | −4.2±1.84 |
| CNN-LSX | **18.84**±0.38 | **-8.55**±1.92 |

| | Comp. (↑) | Suff. (↓) |
|---|---|---|
| | CLEVR-Hans3 | |
| NeSyCL | 59.3±3.6 | 21.67±4.55 |
| NeSyCL-LSX | **63.26**±2.57 | **7.73**±1.28 |
| | CUB-10 | |
| NeSyCL | 64.54±0.2 | 10.44±0.45 |
| NeSyCL-LSX | **64.59**±0.23 | **6.3**±0.34 |

Overall, our results suggest a beneficial effect of Learning by Self-Explaining in mitigating the issue of shortcut learning, specifically confounded behaviour.

**Explanation consolidation.** In the next evaluation, we wish to analyze how the critic's feedback signal influences the learner's representations, specifically its explanations. Based on the intuition behind the Reflect module concerning "good" explanations, we hypothesize that the explanations of a LSX trained model represent more task-specific rationales. We present our results based on the Inter- vs. Intraclass Explanation Similarity (IIES) and the accuracy of a ridge regression model that was trained to classify a set of explanations and evaluated on a second, held-out set. Both of these metrics measure the class-based separability of a model's explanations. In Tab. 3, one can observe that over both metrics training via LSX leads to much more separable and distinct explanations. This effect appears less pronounced for the NeSy datasets, which is likely due to the sparseness and low dimensionality of their concept-level data and therefore also of the explanations. In Fig. 4, we also provide qualitative results of the explanation consolidation for MNIST, where explanations from four randomly sampled input samples are presented for each digit class. These visualizations undermine the quantitative results of Tab. 3 and particularly indicate the distinctness of the explanations from a LSX trained model within one data class from those of other classes. Overall, we observe that LSX leads to more consistent explanations across samples of one class, yet distinctly separate explanations to samples of other classes. We refer to such an effect as *explanation consolidation*.

**Explanation faithfulness.** Although the performance improvements of the first evaluation suggest that LSX learners do make use of the critic's *explanatory feedback*, and the evaluations regarding explanation consolidation indicate that models learn more distinct explanations via LSX, an open question remains whether the learner's in fact make use of these *explanations* for making their decisions. In other words: are a learner's explanations faithful to its decision process? This is a relevant question on its own, particularly in the field of XAI (Hooker et al., 2019; DeYoung et al., 2020) and XIL (Schramowski et al., 2020) as models that produce unfaithful explanations are detrimental for building trust between human users and machines and at the same time make potential revisions via these explanations difficult (Schramowski et al., 2020; Teso et al., 2023). To investigate the faithfulness of LSX-learned explanations we turn to established faithfulness metrics of AI literature. Specifically, we use the *sufficiency* and *comprehensiveness* metrics of DeYoung et al. (2020). In Tab. 4, we present the results of these metrics over all four datasets and both LSX implementations[4]. One can observe a strong improvement via LSX in both metrics across all models and datasets. Specifically, the comprehensiveness results indicate that the information, considered as relevant by the explanations learned via LSX, are indeed important for the model to make its prediction. At the same time, the sufficiency results indicate that less important information based on the explanations has a decreased impact on the learner's decisions. Overall, these results suggest that training via LSX leads to more faithful explanations.

Overall, our evaluations provide strong evidence for the benefits of training via LSX on a variety of important tasks and metrics that go beyond standard evaluations of ML research.

[4]For CNN-LSX, we adapt these for handling continuous data (*cf.* App. D).

## 5 Related Works

LSX is related to work in explainable AI (XAI), leveraging explanations in ML and, importantly, model refinement via self-refinement or feedback from a second model. Let us highlight these works in the following.

### 5.1 (Leveraging) Explanations in ML

Receiving explanations to an AI model's decision has become a heavily advocated and researched topic in recent years, culminating in the field of *explainable AI* (XAI) (*cf.* (Guidotti et al., 2019; Ras et al., 2022a; Roy et al., 2022; Saeed & Omlin, 2023) for valuable overviews) and *interpretable AI*, which focuses on developing models that are *explicitly* interpretable by design (Räuker et al., 2023; Li et al., 2018; Rudin et al., 2022; Rudin, 2019). XAI methods, in general, are used to evaluate the reasons for a (black-box) model's decision by presenting the model's explanation in a hopefully human-understandable way. Current methods can be divided into various categories based on characteristics (Ras et al., 2022a), *e.g.*, their level of intrinsicality or if they are based on back-propagation computations. Across the spectrum of XAI approaches, from backpropagation-based (Sundararajan et al., 2017; Ancona et al., 2018), to model distillation (Ribeiro et al., 2016), or prototype-based (Li et al., 2018) methods, very often an explanation is created by highlighting or otherwise relating direct input elements to the model's prediction, thus visualizing an explanation at the level of the input space. Several studies have investigated methods that produce explanations other than these visual explanations, such as multi-modal explanations (Rajani et al., 2020), including visual and logic rule explanations (Aditya et al., 2018; Rabold et al., 2019). More recent work has also focused on creating concept-based explanations (Stammer et al., 2021; Zhou et al., 2018; Ghorbani et al., 2019).

An additional branch of research can be placed between explainable AI and interpretable AI, namely that of *self-explaining models* (Alvarez-Melis & Jaakkola, 2018; Lee et al., 2022; Roy et al., 2022; Camburu et al., 2018; Bastings et al., 2019; Majumder et al., 2022). In all of these works above and in contrast to LSX, explanations are only provided in a one-way communication as a means of model inspection for humans and not considered as a means of model refinement.

The idea of leveraging explanations in the training process has only recently been picked up by parts of the ML community. In the field of explanatory interactive learning (XIL) (Teso & Kersting, 2019; Schramowski et al., 2020; Stammer et al., 2021; Friedrich et al., 2023) human users provide revisory feedback on the explanations of an ML model. Similar ideas can also be identified in other works of human-machine interactive learning (Teso et al., 2023; Gao et al., 2022), *e.g.*, in preference selection based interactions for learning vision language models (Brack et al., 2023). Compared to these, we argue for the importance of leveraging explanations in the training loop even before the necessity of human-machine interactions and advocate for the potential of explanations in a form of self-refinement in a model's initial learning process.

In contrast, several works have identified the value of leveraging explanations outside of human-interactive learning (*e.g.*, (Giunchiglia et al., 2022; Lampinen et al., 2021; 2022; Norelli et al., 2022)). In the works of Lei et al. (2016) and Bastings et al. (2019) (later categorized under the term *explain-then-predict models* by Zhang et al. (2021)), the goal is for one model to learn to extract the rationale[5] from an input and a second model to learn to predict the final class from these rationales. Similar ideas were picked up by (Zhang et al., 2021; Krishna et al., 2023). None of these works evaluate the correctness of explanations and particularly none use explanations as a means to *revise* a model.

### 5.2 (Self-)Refinement in ML

A recent, but quickly growing field of research related to our work is that which we categorize under the term of *self-refining AI*. This roughly encompasses research that investigates forms of self-supervised refinement of an AI model, *e.g.*, Wang et al. (2023) propose an approach for instruction-tuning. In the self-alignment approach of Sun et al. (2023), a LLM is aligned with few human provided principles. Schick et al. (2021), on the other hand, identify that LLMs can, to a certain degree, identify biases in their own generations and the authors leverage this characteristic in a finetuning process to mitigate biased generation in future prompts.

[5]Here we mean the term "rationale" as adopted in research on explainability in NLP.

In the work of Madaan et al. (2023) a model is used to provide feedback to its initial generations, where the feedback generation is guided via targeted, few-shot prompting. Zelikman et al. (2022), on the other hand, investigate finetuning a model by based on generated "chain-of-thought" rationales that lead to correct task predictions. Lastly, Paul et al. (2023) propose an approach in which a model learns to provide explicit intermediate reasoning steps for an answer via feedback from a critic model. Importantly in this work, the critic is specifically trained to identify false reasoning steps. In contrast to LSX only few of these mentioned approaches focus on refinement via explanations. Those that do require specifically trained modules for providing feedback on the explanations. In contrast in LSX explanations are quantified in how far they can help perform a task. Thus the evaluation and refinement of a model is performed without specific pretraining or prompt specification.

In contrast to self-refining AI a different branch of research focuses on revising a model based on forms of feedback from a second model. Such et al. (2020) which represents a meta-learning training data generation process in which a data generator and learner model are optimized for the same goal of improving the learner's performance on a given task. Nair et al. (2023) propose a general chat framework that leverages two agents, *researcher* and *decider*, to iteratively work through a task. The researcher plays the role of making task-specific suggestions to the decider, where the decider responds to the information provided by the researcher. In the student-teacher framework (Wang & Yoon, 2022) the goal is knowledge distillation, *i.e.*, learned knowledge from a trained model should be conveyed to a second model, the student model. Somewhat related to this is the concept of self-paced learning within the field of curriculum learning (Kumar et al., 2010; Wang et al., 2022) in which a model provides a signal on how "fast" to learn. Interestingly, Pruthi et al. (2022) frame the utility of an explanation in a student-teacher setup in which the goal is for a student model to simulate a teacher's behaviour best possible. Also Schneider & Vlachos (2023) argue for the importance of explanations in reflective processes. However, the authors only propose an approach where a model makes a final prediction based on the input and explanation that is estimated by a second model, similar to (Lei et al., 2016; Bastings et al., 2019; Zhang et al., 2021; Krishna et al., 2023). Overall, these approaches have a different target and motivation than our work. Particularly, in LSX the role of the critic submodel is to represent an internal optimization loop based on whether the explanations provided from the learner are beneficial in performing the original task.

## 6 Conclusion

In this work, we have introduced a novel learning framework, Learning by Self-Explaining (LSX), with which we argue for a novel perspective on the role of self-explaining in the process of learning in AI models. Thus, we claim that explanations are important not just for human users to understand or to revise an AI model, but that they can play an even more important role in a form of self-reflection in which an agent assesses its own learned knowledge via its explanations. Our experimental evaluations highlight several benefits of training via LSX in the context of generalization, knowledge consolidation, explanation faithfulness and shortcut mitigation. Conclusively, with this work, we argue and provide evidence for the potential of explanations within a models learning process and, ultimately, for developing *reflective* AI.

**Limitations.** Despite the promising results of our instantiations there is still great potential for other design choices. Investigating such instantiations and their benefits is essential for consolidating the findings of this work and thereby for supporting LSX as an advantageous learning paradigm. Surely, the "no one fits all solution" issue of AI also holds for LSX as for any other learning approach. *E.g.*, in the context of our results on self-deconfounding, our results suggest that LSX can be considered as *one* tool in a toolbox of several mitigation strategies against the complex issue of shortcut behaviour (Geirhos et al., 2020).

**Future Research.** There are many avenues for future research related to LSX. *E.g.*, applying LSX to settings with other modalities, such as natural language, but also with several modalities, *i.e.*, based on current multimodal models (Radford et al., 2021; Li et al., 2022; Rombach et al., 2021; Alayrac et al., 2022). A more conceptual direction is the integration of a memory buffer of past LSX optimized explanations, allowing for models to re-iterate over previous generations of explanations (Chi et al., 1994). Another interesting point lies in adding apriori constraints onto the learner's explanations, *e.g.*, by integrating background knowledge into the explanation reflection process. Related to this and to the discussion on the system 1 and 2 processing

framework, future research should investigate the potential of LSX *e.g.*, via a memory of explanations for detecting and handling out-of-distribution situations (Goyal & Bengio, 2022). Another important viewpoint to consider is the connection between self- and causal explanations (Carloni et al., 2023; Zečević et al., 2021; Heskes et al., 2020; Schwab & Karlen, 2019; Galhotra et al., 2021). Specifically, can an AI agent utilize its self-explanations to perform interventional and counterfactual experiments, thereby relating to the formalization of "successfull" explanations by Woodward (2005) and Beckers (2022)? Lastly, in the formulation of LSX and in our specific instantiations we have focused on supervised learning as base task. Another crucial avenue going forward is to apply LSX to other forms of supervision, such as self-supervised learning or reinforcement learning approaches *e.g.*, integrating into actor-critic approaches or for guiding curiosity driven replay (Kauvar et al., 2023).

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# Appendix

In the following, you can find details on our LSX instantiations, experimental data and evaluation metrics.

## A LSX in Pseudo-code

**Algorithm 1** Learning by Self-Explaining: Given two submodels, a learner model ($f$) and internal critic model ($c$), input sample sets $\bar{X}_f = (X_f, y_f)$ and $\bar{X}_c = (X_c, y_c)$ (tuple sets which include raw input samples *e.g.*, $X_f$, and corresponding label sets *e.g.*, $y_f$), original task (e.g. image classification) and iteration budget $T$.

1: $f \leftarrow \textsc{Fit}(f, \bar{X}_f)$ {Learner optimized for base task}
2: **repeat**
3: $\quad E_c \leftarrow \textsc{Explain}(f, \bar{X}_c)$ {Obtain explanations from learner for examples $X_c$}
4: $\quad$ `score` $\leftarrow \textsc{Reflect}(c, E_c, \bar{X}_c)$ {Critic provides feedback on the quality of the explanations}
5: $\quad f \leftarrow \textsc{Revise}(f, \bar{X}_f, \bar{X}_c,$ `score`$)$ {Learner is updated given feedback from critic}
6: **until** budget $T$ is exhausted or $f$ converged
7: **return** $f$

## B Model and Training Details

Exact implementation details can be found in the corresponding code.

### B.1 CNN-LSX

The CNN-LSX configurations are identical for the MNIST and ChestMNIST dataset.

**Learner.**

The learner corresponds to a convolutional neural network with two convolutional layers, ReLU activation layers, one average pooling layer and two linear layers.

**Critic.**

The critic for CNN-LSX is identical to the architecture of the corresponding learner for both MNIST and ChestMNIST.

Fit.

Within the Fit module the learner is optimized via a cross-entropy loss as $l_{\mathrm{B}} := l^{f}_{\mathrm{CE}}(f(X_f), y_f)$.

Explain.

The explanation method of CNN-LSX corresponds to the InputXGradient method described in Shrikumar et al. (2017) and implemented via the captum[6] pytorch package. Following Ancona et al. (2018), for an input sample $x_i$ and the output of model $f$ given the corresponding ground truth label, $y_i$, it is defined as:

$$\mathrm{InpXGrad}_i = x_i \cdot \frac{\partial f_{y_i}(x_i)}{\partial x_i}.$$

Reflect.

In the Reflect module for CNN-LSX the critic trains for one epoch on the explanations obtained from the learner given the input data of $\bar{X}_c$, *i.e.*, $E_c$. Specifically, the critic here is trained via a cross-entropy loss to predict the corresponding class of the learner's explanations. We allow the critic to update its parameters while iterating over all batches in $(E_c, y_c)$ whereby the loss values are accumulated over all batches and

[6] captum.ai/

averaged. In practice we found that it was beneficial to reinitialize the critic with each LSX iteration. The final accumulated and averaged loss value is passed back to the learner and represents the feedback `score` in CNN-LSX.

Revise.

In a standard Revise step the learner again performs the original base task via $l_{\text{B}}$ while jointly optimizing for the feedback via the critic in the previous Reflect step. Specifically, the learner optimizes a joint loss: $L = l_{\text{B}} + \lambda l^{c}_{\text{CE}}(c(E_c), y_c)$. Hereby, $\lambda$ represents a scaling hyperparameter which we set quite high (*e.g.*, $\lambda \geq 100$) in our evaluations to prevent the learner from mainly optimizing for good prediction. Also here we refer to the corresponding code for the exact parameter values.

We perform the triad of LSX modules (Explain, Reflect, Revise) for several iterations until iteration budget $T$ is reached.

As a final Revise step, *i.e.*, when the iteration budget has been reached, we perform a fine-tuning step in which we let the learner produce explanations for all samples in $X_f$, $E_f = \text{Explain}(f, X_f | y_f)$, and let $f$ be optimized for the base task making sure that it does not diverge its explanations from $E_f$ in the process. This is done via the combined loss $L = l_B + \lambda_{ft} l_{ft}(E'_f, E_f)$, where $l_{ft}$ represents a simple mean-squared error loss between $E_f$ and the explanations $E'_f$ of each optimisation iteration.

**Dataset ratios.**

For the results in Tab. 1 via CNN-LSX $\bar{X}_c$ presented about $\frac{1}{2}$, $\frac{2}{3}$ and $\frac{1}{2}$ of $\bar{X}_f$, from left column to right column, respectively.

For the results in Tab. 2 via CNN-LSX on Decoy-MNIST we present the critic with 512 samples from approximately 60000 training samples for *w/ conf.* and 1024 test set samples for *w/ deconf.*.

### B.2 NeSyCL-LSX

**Learner.**

The learner submodel for the NeSyCL-LSX instantiation differs for the CLEVR-Hans3 and CUB-10 datasets. For CLEVR-Hans3 the learner corresponds to the concept learner of Stammer et al. (2021) which incorporates a slot attention encoder for predicting the object's attributes and a set transformer for the final class prediction. As in Stammer et al. (2021), in our experimental evaluations, we make use of a pretrained perception (slot attention) module and perform updates only to the reasoning (set transformer) module, *i.e.*, the module making the final predictions. For the CUB-10 configuration the learner corresponds to the setup of Koh et al. (2020) representing an Inception-v3 model Szegedy et al. (2016) for predicting the bird concepts and a simple linear layer to make the final class prediction.

**Critic.**

The critic, $c$, of the NeSyCL-LSX instantiation, both for CLEVR-Hans3 and CUB-10, corresponds to the neural-symbolic forward reasoner of Shindo et al. (2021). Where the predicate specifications etc. required for the forward reasoner for CLEVR-Hans3 correspond to the original ones of Shindo et al. (2021) for CUB-10 we had to redefine each of the 28 bird concepts as neural predicates *e.g.*, `haswingcolor` can take six different values which in the notation of Shindo et al. (2021; 2023) is defined as: `haswingcolor:brown,grey,yellow,black,white,buff`. We refer here to our repository and the original work of Shindo et al. for details.

Fit.

Similar to the CNN-LSX instantiation the Fit module in NeSyCL-LSX corresponds to optimizing for class prediction via a cross-entropy loss $l_{\text{B}} = l_{\text{CE}(f(X_f), y_f)}$. As previously mentioned, in our evaluations we hereby freeze the parameters of the perception module of $f$, thus optimizing only the parameters of the reasoning (aka predictor) module of the learner.

Explain.

The Explain module of NeSyCL-LSX builds on the explanation approach of the concept learner of Stammer et al. (2021). Specifically, it first computes the integrated gradients Sundararajan et al. (2017) of the concept representation, $z_i$. Again following the notation of Ancona et al. (2018) this is defined as:

$$\text{IntGrad}_i = (x_i - \bar{x}_i) \cdot \int_{\alpha=0}^{1} \frac{\partial f_{y_i}(\tilde{x}_i)}{\partial \tilde{x}_i}|_{\tilde{x}_i = \bar{x}_i + \alpha(x_i - \bar{x})} d\alpha.$$

Hereby, $\bar{x}_i$ represents a "baseline" value, which in our evaluations corresponds to a zero vector. Next, the resulting importance map on the latent concept representations is binarized via a hyperparameter $\delta \in [0, 1]$ to $e_i'' \in \{0, 1\}^{O \times A}$. We next propositionalize [7] $e_i''$ by representing the explanation as a set of logical rules that are present in $e_i''$. These rules consist of conjunctive combinations of the important attributes and objects. We denote this set of candidate explanatory rules as $e_i$. For example, let us assume that for a specific CLEVR-Hans3 sample $i$ of class 1 in the explanation form $e_i''$ we identify two objects to be important for the final class prediction. Hereby, the attributes green color and spherical shape are important for the first object and cubical shape for the second object. Following the notation of Shindo et al. (2023) The set of possible conjunctive rules within this explanation, $e_i''$ are now:

```
class1(X):- in(O1,X),color(O1,green).
class1(X):- in(O1,X),shape(O1,sphere).
class1(X):- in(O1,X),shape(O1,cube).
class1(X):- in(O1,X),color(O1,green),shape(O1,sphere).
class1(X):- in(O1,X),in(O2,X),color(O1,green),shape(O2,cube).
class1(X):- in(O1,X),in(O2,X),shape(O1,sphere),shape(O2,cube).
class1(X):- in(O1,X),in(O2,X),color(O1,green),shape(O1,sphere),shape(O2,cube).
```

We refer to this step of constructing all potential candidate rules as propositionalizing.

Notably, each input sample thereby produces a set of such candidate rules which may potentially contain many duplicates over samples of the same underlying class. Finally, by iterating over all samples in $X_c$, grouping the resulting candidate rules by image class and removing duplicates we receive a set of candidate rules per class as $E_c = \{e^1, ..., e^K\}$.

For improved running times it is beneficial to limit the number of candidate rules per input sample by a maximum number of objects and attributes per object within an explanation rule *e.g.*, maximally four objects per rule. In our evaluations we set these two hyperparameters to still greatly overestimate the ground-truth rule and refer to the code for details (as well as for the values of $\delta$). It is important to note that the propositionalizing step breaks the differentiality of the explanations.

Reflect.

Having obtained the set of candidate `explanation` rules per image class, we pass these candidate rules to the critic *i.e.*, forward reasoner of Shindo et al. (2021). For each underlying class and based on the data within $X_c$ the critic next estimates the validity of each candidate rule, where we refer to Shindo et al. (2021) and Shindo et al. (2023) for details on this.

This evaluation is done for all positive examples of a class and for all negative examples of a class (*i.e.*, all remaining classes), resulting in two probabilities for the ith explanation rule $e_i^j$ of class $j$. We denote these probabilities as $\sigma_i^{j+}$ and $\sigma_i^{j-}$, respectively. The first probability represents the validity of the rule in samples of the relevant class (class $j$) and the second the validity in samples of all other (irrelevant) classes ($k \in \{1, ..., K\} \backslash j$).

[7] Changing the representation of relational data.

As we consider an explanation to be good if it distinguishes an input sample from samples of opposite classes, but indicates similarities to samples of the same class, we next compute the probability for each candidate explanation rule as $\sigma_i^j = \sigma_i^{j+} - \sigma_i^{j-}$. These probabilities, $\sigma$, correspond to the `score` of NeSyCL-LSX and represent the numerical values in the `score` representation in Fig. 3. Finally, per image class, $j$, we select the explanation rule with the maximal probability from $\sigma^j$ corresponding to the red enclosed rule in Fig. 3. We denote this as $e_{\max}^j$ for class $j$ with $E_{\max} = \{e_{\max}^1, ..., e_{\max}^K\}$ for the set over all classes. We thus pass $E_{\max}$ to the learner in the Revise module, rather than the raw `score` value.

Revise.

The selected explanations of the previous Reflect step, $E_{\max}$, are next mapped back into binary vector form in the dimensions of the learner's symbolic representation latent concept representation $\bar{E}_{\max} = \{\bar{e}_{\max}^1, ..., \bar{e}_{\max}^K\}$ with $\bar{e}_{\max}^j \in \{0,1\}^{O \times A}$. This is required so we can compare the learner's explanations to the valid explanations as identified by the critic in a differentiable manner. Specifically, in the Revise step of NeSyCL-LSX we optimize a joint loss function corresponding to $L = l^{\mathrm{B}} + \lambda l_{\mathrm{MSE}}(\bar{E}_{\max}, E_f)$. For explanation $e_i$ of input sample $x_i \in X_f$ with corresponding class label $y_i$ $l_{\mathrm{MSE}}$ is defined as:

$$l_{\mathrm{MSE}}(\bar{e}_{\max}^j, e_i) = \frac{1}{O \times A} \sum_{q=1}^{O \times A} (e_{i_q} - \bar{e}_{\max_q}^{y_i})^2.$$

In comparison to CNN-LSX in this instantiation $T = 1$. Meaning the critic only scores the proposed underlying logical explanations once and passes this back as feedback. Although it is in principle possible to perform multiple steps of this, *e.g.*, by first removing explanations which are most unprobable from the learner's representations and only after several of such iterations choose the most likely explanation, we leave this for future investigations.

**Dataset ratios.**

In the setting of NeSyCL-LSX on CLEVR-Hans3 for the results in Tab. 1 $\bar{X}_c \cap \bar{X}_f = \emptyset$. Specifically, from left column to right column the ratio between $\bar{X}_c$ and $\bar{X}_f$ was 30 to 150, 75 to 375 and 1500 to 7500, respectively. via NeSyCL-LSX on CLEVR-Hans3 the critic was provided 1500 samples from the original training set of 9000 samples.

The setting of NeSyCL-LSX on CUB-10 for the results in Tab. 1 represented a small variation from the previous settings in that $\bar{X}_f \subseteq \bar{X}_c$ due to the very small number of samples per class in CUB-10 in combination with the neuro-symbolic forward reasoner (*i.e.*, the critic). In this way for the results in Tab. 1 for CUB-10 from left column to right column the ration between $\bar{X}_c$ and $\bar{X}_f$ was 29 to 24, 149 to 124 and 300 to 249, respectively.

For the results in Tab. 2 via NeSyCL-LSX on CLEVR-Hans3 we present the critic with 50 samples and the learner 7500 separate training samples for *w/ conf.* and 150 test set samples for *w/ deconf.*.

## C Data

**CUB-10.** CUB-10 represents a subset of the original Caltech-UCSD Birds-200-2011 dataset (CUB-200-2011) (Wah et al., 2011) that comprises images of the first 10 classes of the full dataset. Koh et al. (2020) originally perform a preprocessing step for CUB-200-2011 where concept vectors are replaced with the max voting vector over all samples of a class. In other words, the resulting concept activations are identical across all samples of a class which leads to a one-to-one mapping between concept activations and the class affiliation.

In CUB-10 we simulate a more realistic setting in which the class concept activations of (Koh et al., 2020) are overlaid with additional random noise, thereby maintaining the underlying class-based concept activation, but producing random variations per class sample. Specifically, we add uniformly distributed noise between 0 and 1 onto the class-based concept activations and binarize the resulting activations with a threshold of 0.75.

Figure 5: Example images from Decoy-MNIST.

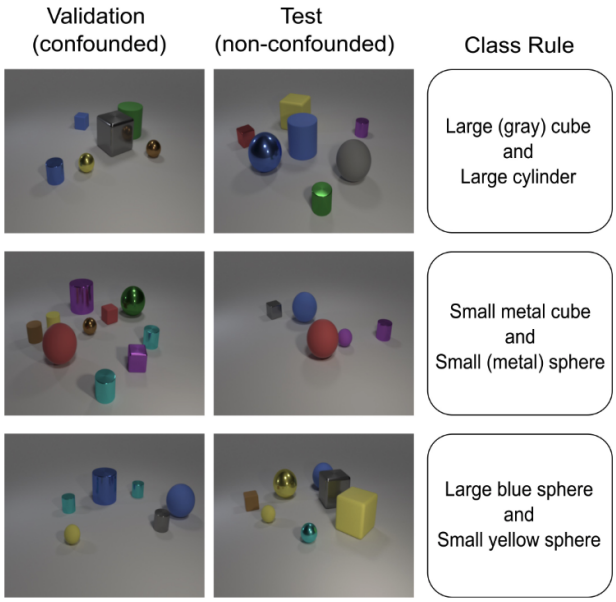


Figure 6: Figure from (Stammer et al., 2021).

**DecoyMNIST**

DecoyMNIST (Ross et al., 2017) represents a version of MNIST (LeCun et al., 1989) in which small boxes are placed randomly in one of the four corners for each sample (*cf.* Fig. 5). Importantly, the dataset contains confounders. Within the training set the gray boxes possess a specific grayscale value for each digit class, where this grayscale value is randomized at test time.

**CLEVR-Hans3**

Fig. 6 presents the data distribution in CLEVR-Hans3 (Stammer et al., 2021). Specifically, CLEVR-Hans3 is based on the graphical environment of the original CLEVR dataset (Johnson et al., 2017), however reframed for image classification rather than visual question answering. Each class is represented by an underlying logical rule consisting of the presence of specific object combinations. Within the original training and validation set specific combinations of object properties are highly correlated, where they are not within the test set. *E.g.*, for the first class all large cubes are gray within the training set, but any color in the test set. This gray color thus represents a confounding factor within CLEVR-Hans3.

## D Metrics

### D.1 Explanation Consolidation.

**Ridge Regression Classification.** For evaluating the separability of learned explanations, we provide the accuracy of a ridge regression (RR) model that is fitted on a set of tuples consisting of explanations from a trained learner and the corresponding ground-truth (GT) class labels of the underlying image. The RR

model is fitted on a training set and tested on an additional, held-out set of explanations (and corresponding class labels).

This evaluation acts as a proxy of the separability of learned explanations. The higher the RR accuracy on the test set the better the separability between explanations. For each learning configuration in our evaluations we train a RR model separately on the explanations from the five differently seeded models.

**Encoding Analysis.** The Inter- vs Intraclass Explanation Similarity (IIES) is defined as:

$$\text{IICS} = \frac{1}{K}\sum_{k}^{K} \frac{\frac{1}{M}\sum_{i}^{M} d(z_i^k, \mu^k)}{\frac{1}{K}\sum_{j,j\neq k}^{K} d(\mu^j, \mu^k)}$$

Essentially, this metric estimates in how far the explanations stemming from samples of one class are close to another compared to the explanations of samples from other classes. The encoding of a pretrained model, $h$, provides the encoding space in which this similarity is assessed. The lower the values of IICS the better separable are the data for $h$.

Here $z_i^k$ corresponds to the encoding of the explanation of a sample $i$ from class $k$. This encoding is provided by an additional model, $h$, via $h(e_i) = z_i^k$, where $e_i$ is a provided explanation of sample $i$ from a learner $f$. $h$ is identical in architecture to the learner of which the explanations are being evaluated, however $h$ was separately pretrained only on the original task. Specifically, for evaluating explanations from the CNN configurations, $h$ corresponds to an identical CNN that was trained for image classification as in the vanilla configurations. For evaluating the NeSyCL configurations a NeSyCL was pretrained for classification as in the NeSyCL vanilla setting. In both cases $h$ was provided with a random seed different from those used in the original training setups.

Furthermore, $\mu^k$ corresponds to the average encoding over all samples of class $k$ (where for notations sake we assume $M$ samples in each class, although this can vary in practice). $d(x, y)$ represents a distance metric between $x$ and $y$, where we have used the euclidean distance in our evaluations. We divide the distance within one class by the average distance between the encoding mean of class $k$ and those of all other classes, corresponding to an estimate of the distance to all other class encodings. Finally this is averaged over all classes.

### D.2 Faithfulness

For comprehensiveness, parts of the input are removed that correspond to important features as identified by the explanation. As a result, the model should be less accurate in its predictions. In the case of sufficiency, one removes those input features which were deemed unimportant according to the explanation. Hereby, the model should not lose much accuracy. Notably, the original sufficiency and comprehensiveness metrics of (DeYoung et al., 2020) were introduced in the context of NLP in which input sequences are considered as discrete inputs. However, removing input features from continuous inputs such as images presents an issue (Hooker et al., 2019) as measured differences due to pixel removal may reflect the influence of the modified, out-of-distribution input rather than faithfulness of the explanation. For this case, we modified the metrics for the CNN configurations (*i.e.*, for explanations that are in a continuous form) to approximately compensate for this effect. For evaluating explanation faithfulness we thus provide results for CNN-LSX (and vanilla CNN) via the continuous adaptation of both metrics (denoted as $\text{COMP}_{cont.}$ and $\text{SUFF}_{cont.}$) and for NeSyCL-LSX (and NeSyCL vanilla) via the original comprehensiveness and sufficiency definitions (denoted as $\text{COMP}_{discr.}$ and $\text{SUFF}_{discr.}$). We formalize these in the following.

We follow the notation for $\text{COMP}_{discr.}$ and $\text{SUFF}_{discr.}$ of Chan et al. (2022). For this, $x$ denotes an input sample. We denote the predicted class of $x$ as $c(x)$, and the predicted probability corresponding to class $j$ as $p_j(x)$. Assuming an explanation is given, we denote denote the input containing only the $q\%$ important elements as $x_{:q\%}$. We denote the modified input sequence from which a token sub-sequence $x'$ are removed as $x \setminus x'$. Comprehensiveness and sufficiency for discrete explanations are finally defined as:

$$\text{COMP}_{\text{discr.}} = \frac{1}{|B|}\sum_{q\in B}\frac{1}{N}\sum_{j=1}^{N}(p_{c(x_j)}(x_j) - p_{c(x_j)}(x_j \backslash x_{j:q\%}))$$

$$\text{SUFF}_{\text{disc.}} = \frac{1}{|B|}\sum_{q\in B}\frac{1}{N}\sum_{j=1}^{N}(p_{c(x_j)}(x_j) - p_{c(x_j)}(x_{j:q\%})).$$

Where $N$ here represents the number of data samples in the evaluation set. In our evaluations we set $B = \{1, 5, 10, 20, 50\}$ as in the original work of DeYoung et al. (2020).

For computing comprehensiveness and sufficiency scores based on continuous explanations we first compute the comprehensiveness and sufficiency when a percentage $q$ of the top input elements (*e.g.*, pixels) are set to the median value of all input elements of the evaluation set. In comparison to the definition of $\text{COMP}_{discr.}$ and $\text{SUFF}_{discr.}$ of DeYoung et al. (2020) for the adaptation to continuous explanations we base the metrics on class accuracy rather than class probabilities. We denote these alternative computations as:

$$\hat{\text{COMP}}_{\text{cont.}} = \frac{1}{B}\sum_{q\in B}\text{acc}(f(X\backslash X^{\text{median}}_{:q\%}), y)$$

$$\hat{\text{SUFF}}_{\text{cont.}} = \frac{1}{B}\sum_{q\in B}\text{acc}(X^{\text{median}}_{:q\%}, y).$$

Here, $\text{acc}(f(X), y)$ corresponds to the accuracy score of a models prediction given input data, $f(X)$, compared to the ground truth labels, $y$. $X_{:q\%}$ corresponds to the full dataset in which everything but the top $q\%$ of each samples input elements were set to the median value of the dataset and $X\backslash X^{\text{median}}_{:q\%}$ where the top $q\%$ of each samples input elements were set to the median value of the dataset.

Next we compute the same metrics, but when removing randomly chosen $q\%$ of the input elements by setting them to the median value. We denote these computations as $\hat{\text{COMP}}^{rand}_{cont.}$ and $\hat{\text{SUFF}}^{rand}_{cont.}$. Finally, we subtract these from the original values, leading to:

$$\text{COMP}_{\text{cont.}} = \hat{\text{COMP}}^{rand}_{cont.} - \hat{\text{COMP}}_{cont.}$$

and

$$\text{SUFF}_{\text{cont.}} = \hat{\text{COMP}}^{rand}_{cont.} - \hat{\text{COMP}}_{cont.}$$

### D.3 Self-unconfounding

For the *w/ deconf.* case we provide the critic in each case with samples from the original test sets, whereby we remove these samples from the final test set evaluations. In the baseline configurations we add these samples to the learner's training dataset for a fair comparison. Specifically, for evaluations on CLEVR-Hans3 *w/ deconf.* we provide the critic with 150 randomly selected sampled from the original test set. For DecoyMNIST we provide the critic with 1024 test set samples.