ITERATED LEARNING FOR EMERGENT SYSTEMATICITY IN VQA

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ABSTRACT

Although neural module networks have an architectural bias towards compositionality, they require gold standard layouts to generalize systematically in practice. When learning layouts and modules jointly, compositionality does not arise automatically. An explicit pressure for systematic generalization is necessary for the emergence of layouts exhibiting the right structure. Iterated learning is a theory of the emergence of compositional languages, which has primarily been applied to toy problems in the machine learning literature. Considering the layouts of module networks as samples from an emergent language, we use iterated learning to encourage structure within this language. We show that the resulting layouts support systematic generalization in neural agents solving the more complex task of visual question-answering. Our regularized iterated learning method can outperform baselines without iterated learning on SHAPES-SyGeT (**SHAPES Sy**stematic **Ge**neralization **T**est), a new split of the SHAPES dataset we introduce to evaluate systematic generalization, and on CLOSURE, an extension of CLEVR also designed to test systematic generalization. We demonstrate superior performance in recovering ground-truth compositional program structure through limited supervision on both SHAPES-SyGeT and CLEVR.

1 INTRODUCTION

Although great progress has been made in visual question answering (VQA), recent methods still struggle to generalize systematically to inputs coming from a distribution different from that seen during training (Bahdanau et al., 2018; 2019). Neural module networks (NMNs) present a natural solution to improve generalization in VQA, using a symbolic *layout* or *program* to arrange neural computational modules into computation graphs. If these modules are learned to be specialized, they can be composed in arbitrary legal layouts to produce different processing flows. However, for modules to learn specialized roles, programs must support this type of compositionality; if programs reuse modules in non-compositional ways, modules are unlikely to become layout-invariant.

This poses a substantial challenge for the training of NMNs. Although Bahdanau et al. (2018) and Bahdanau et al. (2019) both observe that NMNs can systematically generalize if given human-designed ground-truth programs, creating these programs imposes substantial practical costs. It becomes natural to jointly learn a *program generator* alongside the modules (Johnson et al., 2017b; Hu et al., 2017; Vedantam et al., 2019), but the generated programs often fail to generalize systematically and lead to worse performance (Bahdanau et al., 2018).

Iterated learning (IL) offers one way to address this problem. Originating in cognitive science, IL claims that the language evolves to become more compositional and easy-to-acqure, in a repeated transmission process, where each new-born child need to acquire the parents' language with a limited dataset (Kirby et al., 2014). Early works on human experiments (Kirby et al., 2008) as well as agent-based simulations (Zuidema, 2003) support this hypothesis. Recently machine learning community also show increasing interest in applying IL into emergent communication (Guo et al., 2019; Li & Bowling, 2019; Cogswell et al., 2019; Dagan et al., 2020; Ren et al., 2020). Different from previous works, we believe that IL is an algorithmic principle that is equally applicable to recovering compositional structure in more general tasks. We thus propose treating NMN programs as a "layout language" and applying IL to the challenging problem of VQA. Our effort highlights the potential of applying IL to a broader aspect of machine learning beyond toy languages.

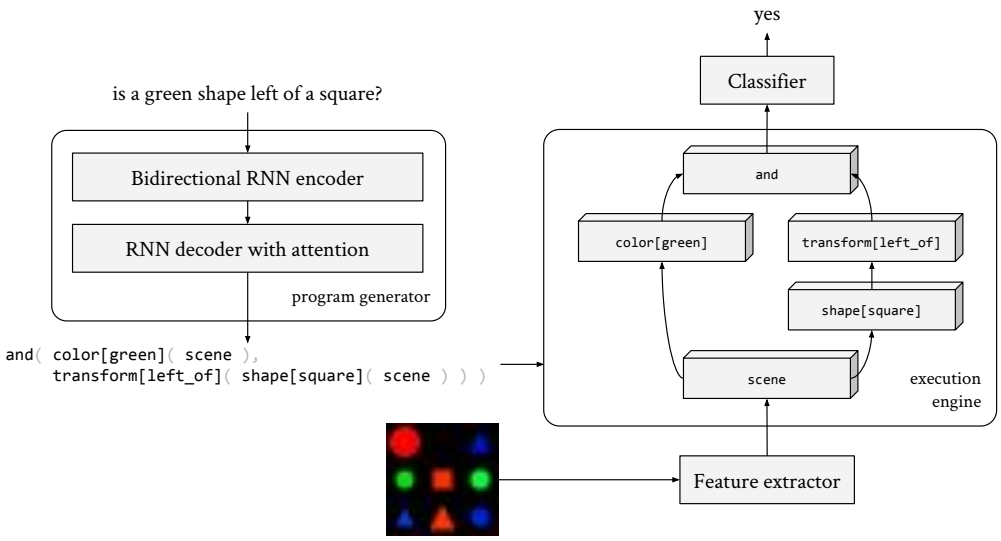


Figure 1: An overview of neural module networks (NMNs). A question $\boldsymbol{q}$ is read by the *program generator* to produce a program $\hat{\boldsymbol{z}}$. The *execution engine* assembles neural modules according to the layout $\hat{\boldsymbol{z}}$ and feeds the input image $\boldsymbol{x}$ into the assembled module network. A classifier takes the output of the top-level module to produce an answer $\hat{y}$ for the given $(\boldsymbol{q}, \boldsymbol{x})$ pair.

To demonstrate our method, we introduce a lightweight benchmark for systematic generalization research based on the popular SHAPES dataset (Andreas et al., 2016) called SHAPES-SyGeT (**SHAPES Sy**stematic **Ge**neralization **T**est). Our experiments on SHAPES-SyGeT, CLEVR (Johnson et al., 2017a), and CLOSURE (Bahdanau et al., 2019) show that the IL algorithm accelerates the learning of compositional program structure, leading to better generalization to both unseen questions from the training question templates and unseen question templates.

2 Related work

Systematic generalization. Systematicity was first proposed as a topic of research in neural networks by Fodor et al. (1988), who argue that cognitive capabilities exhibit certain symmetries, and that representations of mental states have combinatorial syntactic and semantic structure. Whether or not neural networks can exhibit systematic compositionality has been a subject of much debate in the research community (Fodor et al., 1988; Christiansen et al., 1994; Marcus, 1998; Phillips, 1998; Chang, 2002; Marcus, 2018; van der Velde et al., 2004; Botvinick & Plaut, 2009; Bowers et al., 2009; Brakel & Frank, 2009; Fodor & Lepore, 2002; Marcus, 2018; Calvo & Symons, 2014).

Bahdanau et al. (2018) investigate various VQA architectures such as neural module networks (NMNs) (Andreas et al., 2016), MAC (Hudson & Manning, 2018), FiLM (Perez et al., 2018), and relation networks (Santoro et al., 2017) on their ability to systematically generalize on a new synthetic dataset called SQOOP. They show that only NMNs are able to robustly solve test problems, but succeed only when a fixed tree-structured layout is provided. When learning to infer the module network layout, robust tree-structured layouts only emerged if given a strong prior to do so. The authors conclude that explicit regularization and stronger priors are required.

CLEVR (Johnson et al., 2017a) is a popular VQA dataset, and various benchmarks achieve almost-perfect validation scores (Hu et al., 2017; Hudson & Manning, 2018; Perez et al., 2018; Santoro et al., 2017). Bahdanau et al. (2019) proposed an extension of CLEVR with a new evaluation dataset called CLOSURE, containing novel combinations of linguistic concepts found in CLEVR. The authors found that many of the existing models in the literature fail to systematically generalize to CLOSURE. Moreover, there is a significant gap between the performance achieved with ground-truth layouts and learned layouts on CLOSURE.

Language emergence and compositionality. Agents interacting in a cooperative environment can learn a language to communicate to solve a particular task. The emergence of such a communication

protocol has been studied extensively in multi-agent referential games. In these games, one agent must describe what it saw to another agent, which is tasked with figuring out what the first agent saw (Lewis, 2008; Skyrms, 2010; Steels & Loetzsch, 2012). To encourage a dialogue between agents, several multi-stage variants of such a game have also been proposed (Kottur et al., 2017; Evtimova et al., 2017). Most approaches to learning a discrete communication protocol between agents use reinforcement learning (Foerster et al., 2016; Lazaridou et al., 2016; Kottur et al., 2017; Jorge et al., 2016; Havrylov & Titov, 2017). Although, the Gumbel straight-through estimator (Jang et al., 2016) can also be used (Havrylov & Titov, 2017), as can backpropagation when the language in question is continuous (Foerster et al., 2016; Sukhbaatar et al., 2016; Singh et al., 2018).

Several works in the literature have found that compositionality only arises in emergent languages if appropriate environmental pressures are present (Kottur et al., 2017; Choi et al., 2018; Lazaridou et al., 2018; Chaabouni et al., 2020). While generalization pressure is not sufficient to guarantee compositionality, compositional languages tend to exhibit better systematic generalization (Bahdanau et al., 2018; Chaabouni et al., 2020). The community still lacks strong research indicating what general conditions are necessary or sufficient for compositional language emergence.

Iterated learning. The origins of the compositionality of human language, which leads to an astounding open-ended expressive power, have attracted much interest over the years. Kirby (2001) suggests that this phenomenon is a result of a *learning bottleneck* arising from the need to learn a highly expressive language with only a limited set of supervised learning data. The iterated application of this bottleneck, as instantiated by IL, has been demonstrated to cause artificial languages to develop structure in experiments with human participants (Kirby et al., 2008; Silvey et al., 2015).

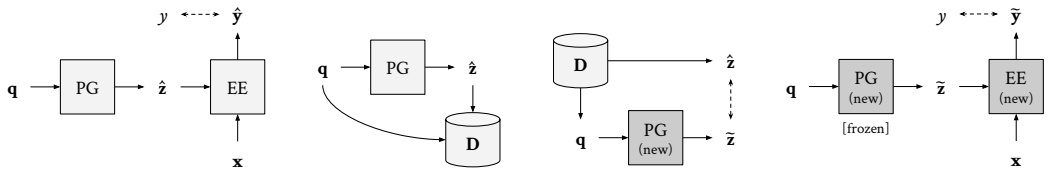
Ren et al. (2020) present *neural IL* following the principles of Kirby (2001), where neural agents play a referential game and evolve a communication protocol through IL. They use topographic similarity (Brighton & Kirby, 2006) to quantify compositionality, and find that high topographic similarity improves the learning speed of neural agents, allows the listener to recognize more objects using less data, and increases validation performance. However, these experiments are limited to toy domains with very simple object and message structure.

Several ablation studies (Li & Bowling, 2019; Ren et al., 2020) have found that re-initializing the speaker and the listener between generations is necessary to reap the benefits of compositionality from IL. However, *seeded IL* (Lu et al., 2020) proposes to seed a new agent with the previous generation's parameters at the end of the learning phase. Since an interacting phase has not yet fine-tuned this initialization, it has not had the opportunity to develop a non-compositional language to fit the training data. The authors find that seeded IL helps counter language drift in a translation game. They suggest that this might be because IL maintains the compositionality of the natural language.

3 METHOD

We are interested in solving the task of visual question-answering (VQA). Let $\mathcal{X}$ be the space of images about which our model will be required to answer questions. Next, let $\mathcal{Q}$ be the space of natural-language questions and $\mathcal{Y}$ the space of all possible answers to the questions. Additionally, we consider a space $\mathcal{Z}$ of programs, which represent computation graphs of operations that can be performed on an image in $\mathcal{X}$ to produce an output in $\mathcal{Y}$. We consider a question template $\boldsymbol{T}$ to be a set of tuples $(\boldsymbol{q}, \boldsymbol{z})$, where $\boldsymbol{q} \in \mathcal{Q}$ and $\boldsymbol{z} \in \mathcal{Z}$. Each question template contains questions with the same structure but varying primitive values. For example, the questions "Is a triangle blue" and "Is a square red" belong to a template "Is a `SHAPE COLOR`." The program $\boldsymbol{z}$ corresponding to the question $\boldsymbol{q}$ in a template defines a computation graph of operations that would produce the correct answer in $\mathcal{Y}$ to $\boldsymbol{q}$ for any input image $\boldsymbol{x} \in \mathcal{X}$. Finally, let $\mathcal{T}$ be a finite set of question templates.

The dataset for training our model and evaluating VQA performance constitutes tuples of the form $(\boldsymbol{q}, \boldsymbol{z}, \boldsymbol{x}, y)$. First, a template $\boldsymbol{T} \in \mathcal{T}$ is sampled and a tuple $(\boldsymbol{q}, \boldsymbol{z})$ is sampled from $\boldsymbol{T}$. Then, an image $\boldsymbol{x} \in \mathcal{X}$ is sampled and the answer y is produced by passing $\boldsymbol{x}$ through the program $\boldsymbol{z}$. These collected variables $(\boldsymbol{q}, \boldsymbol{z}, \boldsymbol{x}, y)$ form a single example in the task dataset. To evaluate our model's performance on unseen question templates, we define $\mathcal{T}_{train} \subset \mathcal{T}$ to be a subset of training templates and $\mathcal{T}_{test} = \mathcal{T} - \mathcal{T}_{train}$ to be the subset of test templates. The training dataset $\mathcal{D}$ is prepared from templates in $\mathcal{T}_{train}$ and the out-of-distribution test dataset $\mathcal{D}_{test}$ from templates in $\mathcal{T}_{test}$. We allow a program $\boldsymbol{z}$ to be *absent* in $\mathcal{D}$, in which case it is not used for auxiliary supervision during training.



(a) Interacting phase. (b) Transmitting phase. (c) Program generator learning phase. (d) Execution engine learning phase.

Figure 2: Phases of IL for emergent module layouts. Solid arrows indicate forward pass through the model, and dashed lines indicate the cross-entropy loss between predictions and targets. After proceeding through phases (a)-(d), the new program generator and execution engine begin an interacting phase (a) of a new generation.

Our goal of systematic generalization is to learn a model $p(\boldsymbol{Y} \mid \boldsymbol{X}, \boldsymbol{Q})$ that performs well on the dataset $\mathcal{D}_{test}$ created using unseen question templates, where $\boldsymbol{Y}$, $\boldsymbol{X}$, and $\boldsymbol{Q}$ are random variables taking values in $\mathcal{Y}$, $\mathcal{X}$, and $\mathcal{Q}$. We define our model to be a composition of a program generator $PG_\theta(\boldsymbol{Z} \mid \boldsymbol{Q})$ and execution engine $EE_\phi(\boldsymbol{Y} \mid \boldsymbol{X}, \boldsymbol{Z})$, parameterized by θ and ϕ respectively.

3.1 Model architecture

Our overall model architecture is illustrated in Figure 1. An attention-based sequence-to-sequence model acts as the program generator, which translates an input question $\boldsymbol{q}$ into a sampled program $\hat{\boldsymbol{z}}$. The execution engine assembles modules into a layout dictated by $\hat{\boldsymbol{z}}$ to instantiate an NMN that takes the input image $\boldsymbol{x}$ to predict an answer $\hat{y}$. In this work, we explore three execution engine architecture choices, including *Tensor-NMN*, based on the module architecture from Johnson et al. (2017b), and *Vector-NMN* from Bahdanau et al. (2019). We also experiment with a novel hybrid of these architectures that performs better on SHAPES-SyGeT, which we dub *Tensor-FiLM-NMN*.

The goal of the Tensor-FiLM-NMN architecture is to combine the minimalist, FiLM-based definition of modules in Vector-NMN with the spatial representational power of Tensor-NMN. As such, the modules in Tensor-FiLM-NMN use FiLM to condition global operations on module-specific embeddings, as in Vector-NMN, but module inputs and outputs are tensor-valued feature maps like in Tensor-NMN. The following equations illustrate the working of a Tensor-FiLM-NMN module:

$$\tilde{\boldsymbol{h}}_1 = \boldsymbol{\gamma}_h \odot \boldsymbol{h}_1 \oplus \boldsymbol{\beta}_h, \quad \tilde{\boldsymbol{h}}_2 = \boldsymbol{\gamma}_h \odot \boldsymbol{h}_2 \oplus \boldsymbol{\beta}_h \tag{1}$$

$$\boldsymbol{g} = \boldsymbol{W}_1 * [(\boldsymbol{\gamma}_x \odot \boldsymbol{x} \oplus \boldsymbol{\beta}_x); \max(\tilde{\boldsymbol{h}}_1, \tilde{\boldsymbol{h}}_2); (\tilde{\boldsymbol{h}}_1 - \tilde{\boldsymbol{h}}_2)] \oplus \boldsymbol{b}_1 \tag{2}$$

$$\boldsymbol{y} = \mathrm{ReLU}(\boldsymbol{W}_2 * (\boldsymbol{\gamma}_g \odot \mathrm{ReLU}([\boldsymbol{g}; \mathrm{cumsum_left}(\boldsymbol{g}); \mathrm{cumsum_down}(\boldsymbol{g})]) \oplus \boldsymbol{\beta}_g) \oplus \boldsymbol{b}_2 + \boldsymbol{e}). \tag{3}$$

Here, $\boldsymbol{x}$ is the input image, $\boldsymbol{h}_1$ and $\boldsymbol{h}_2$ are the module inputs, and $\boldsymbol{y}$ is the module output. $\boldsymbol{\gamma}_\cdot$ and $\boldsymbol{\beta}_\cdot$ are FiLM parameters computed using 2-layer MLPs per layer on module-specific embeddings $\boldsymbol{m}_\cdot$. All weights and biases are shared across all modules. Note that we further strengthen our model's ability for spatial relational reasoning by using cumulative sums of an intermediate representation across locations in left-to-right and top-to-bottom directions. This allows our model, for example, to select regions to the 'left of' objects through appropriate scaling and thresholding.

3.2 Iterated learning for NMNs

We can view the program generator and the execution engine as communicating agents in a cooperative VQA game where the programs passed between agents are messages drawn from an emergent language. Introducing more compositional structure to this language, such as reusing low-level concepts using the same tokens and high-level concepts using the same sequence of tokens, helps address the combinatorial complexity of the question space, allowing agents to perform better on new question templates containing previously-unseen combinations of known concepts. Figure 2 illustrates the phases of our algorithm for training module networks with compositional emergent layouts. We follow Ren et al. (2020) in dividing our method into three stages, an *interacting* phase, a *transmitting* phase, and a *learning* phase, which are cycled through until the end of training.

Interacting phase. The program generator and the execution engine must work together. Without programs that consistently use the same tokens to mean the same operations, the execution engine cannot assign the correct semantics to modules. Simultaneously, the program generated depends on the language grounding provided by the execution engine to provide reinforcement signal for beneficial layouts. To make the problem more tractable, it is common to provide the model with a small set of ground-truth programs Johnson et al. (2017b); Vedantam et al. (2019). We find that providing program supervision with a small number of ground-truth programs throughout the interacting phase helps in generalization. This can be seen as a form of supervised self-play (Lowe et al., 2020), and has the effect of *simulating* an inductive bias towards the desired program language.

The agents are jointly trained for T_i steps to minimize answer prediction error on data sampled from the training dataset $\mathcal{D}$, with predictions given by $\hat{\boldsymbol{z}} \sim PG_\theta(\boldsymbol{q})$; $\hat{\boldsymbol{y}} = EE_\phi(\boldsymbol{x}, \hat{\boldsymbol{z}})$. We train EE_ϕ by minimzing the cross-entropy loss L between the true answer label y and the predicted distribution $\hat{\boldsymbol{y}}$. Additionally, we estimate the gradients for the parameters θ using REINFORCE:

$$\nabla_\theta L_{PG}(\theta) = \mathbb{E}_{\hat{\boldsymbol{z}} \sim p_\theta(\cdot|\boldsymbol{q})} \left[\text{clip}(-L, -5, 5) \nabla_\theta \log p_\theta(\hat{\boldsymbol{z}} \mid \boldsymbol{q}) \right]. \tag{4}$$

Here, p_θ is the distribution over programs returned by $PG_\theta(\boldsymbol{q})$. We use the negative cross-entropy loss $-L$ clipped between -5 and 5 as the reward for the program generator. When a ground-truth program $\boldsymbol{z}$ is available, we additionally minimize a weighted cross-entropy loss between $\boldsymbol{z}$ and the generated program $\hat{\boldsymbol{z}}$ using teacher forcing. In practice, the model operates on minibatches of data, and a subset of every minibatch is subsampled from data examples with ground-truth programs.

Transmitting phase. During the transmitting phase, a new dataset $\boldsymbol{D}$ with T_t samples is prepared for use during the learning phase. Questions $\boldsymbol{q}$, as well as ground-truth programs $\boldsymbol{z}$ if available, are sampled from $\mathcal{D}$. For data examples without ground-truth programs, a program $\hat{\boldsymbol{z}}$ is sampled from the execution engine using $\boldsymbol{q}$. Finally, question-program pairs $(\boldsymbol{q}, \boldsymbol{z})$, if $\boldsymbol{z}$ is available, or $(\boldsymbol{q}, \hat{\boldsymbol{z}})$ are added to $\boldsymbol{D}$. By transmitting the ground-truth programs when available, we continue simulating the inductive bias towards desirable programs during the learning phase.

Learning phase. Program generators and execution engines are initialized in the learning phase, forming a new generation of agents to play the VQA game. The new program generator then acquires the previous agents' language from the transmitted data $\boldsymbol{D}$. However, it does so imperfectly due to a learning bottleneck that exerts pressure towards compositionality (Ren et al., 2020).

We implement the learning bottleneck by limiting the number of training iterations T_p and T_e used in this training phase, effectively performing *early stopping*. Optionally, we further regularize the model by applying *spectral normalization* (Miyato et al., 2018) on the program generator's decoder LSTM parameters.

We train the new program generator $PG_{\tilde{\theta}}$ by minimizing the cross-entropy loss between model samples $\tilde{\boldsymbol{z}} \sim PG_{\tilde{\theta}}(\boldsymbol{q})$ and transmitted programs $\hat{\boldsymbol{z}}$ corresponding to $\boldsymbol{q}$ in $\boldsymbol{D}$ for T_p gradient steps. Then, the new execution engine $EE_{\tilde{\phi}}$ is trained with programs from the new program generator $PG_{\tilde{\theta}}$, using the entire dataset $\mathcal{D}$ for T_e steps. The forward pass in the execution engine learning phase is similar to that in the interacting phase, but only affects the execution engine parameters $\tilde{\phi}$.

4 SYSTEMATIC GENERALIZATION TEST FOR SHAPES

The SHAPES dataset (Andreas et al., 2016) is a popular yet simple VQA dataset. The lower image and question complexity of SHAPES relative to CLEVR make it an attractive choice for experimentation since the training time can be significantly lower and it requires fewer resources. Each of the 15616 data points in SHAPES contains a unique image. However, there are only 244 unique questions. Although the validation and test splits of SHAPES contain unique questions not present in any of the other splits, the questions are of the same form as the ones in the training split.

To the best of our knowledge, there is no published systematic generalization evaluation setup for SHAPES. Thus, we present *SHAPES-SyGeT*, a **SHAPES Sy**stematic **Ge**neralization **T**est. To understand the distribution of question types in SHAPES, we categorized questions into 12 standard templates, out of which 7 are used for training, and 5 to test systematic generalization.

Table 1: SHAPES-SyGeT accuracies. NMNs are trained with 20 or 135 ground-truth programs; FiLM (Perez et al., 2018) and MAC (Hudson & Manning, 2018) do not use program supervision.

Model	**Val-IID**		**Val-OOD**	
FiLM	0.720 ± 0.01		$\mathbf{0.609 \pm 0.01}$	
MAC	$\mathbf{0.730 \pm 0.01}$		0.605 ± 0.01	
	#GT 20	**#GT 135**	**#GT 20**	**#GT 135**
`Tensor-NMN`	0.645 ± 0.01	0.700 ± 0.01	0.616 ± 0.01	0.641 ± 0.003
`Tensor-NMN`+IL	0.756 ± 0.07	0.763 ± 0.04	0.648 ± 0.02	0.661 ± 0.02
`Tensor-FiLM-NMN`	0.649 ± 0.02	0.851 ± 0.01	0.605 ± 0.01	0.692 ± 0.06
`Tensor-FiLM-NMN`+IL	$\mathbf{0.954 \pm 0.07}$	$\mathbf{1.000 \pm 0.00}$	$\mathbf{0.858 \pm 0.15}$	$\mathbf{0.971 \pm 0.02}$

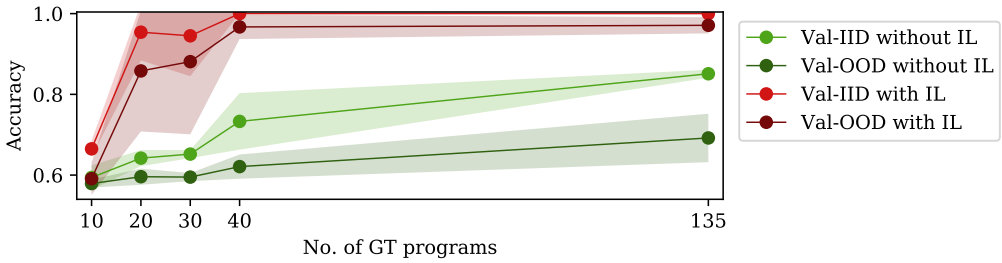


Figure 3: SHAPES-SyGeT answer accuracies of models with varying number of ground-truth programs, with and without IL. All models use a Tensor-FiLM-NMN execution engine.

To evaluate the in-distribution and out-of-distribution generalization performance of our models, we prepare the SHAPES-SyGeT training set with only a subset of the questions under each train template and use the rest as an in-distribution validation set (*Val-IID*). Questions belonging to the evaluation templates are used as an out-of-distribution validation set (*Val-OOD*). Please see Appendix C for further details about the question templates and the dataset splits.

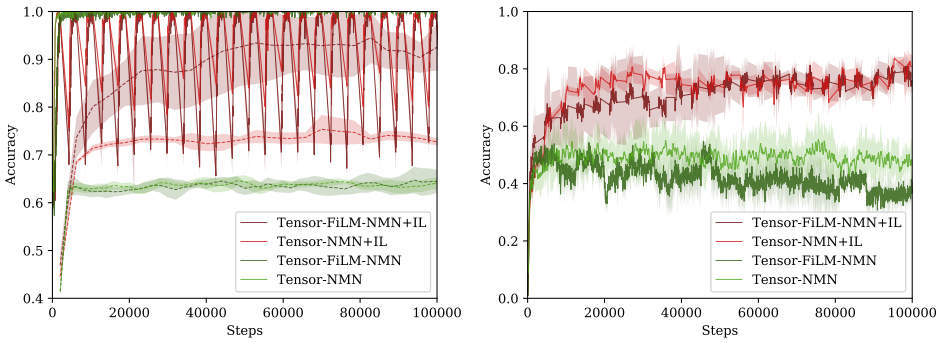
5 Experiments

In this section, we present results on SHAPES-SyGeT, CLEVR, and CLOSURE. Every experiment is run with 3 different seeds and we report the mean and standard deviation of metrics over these trials. CLEVR experiments use representations of images from a pre-trained ResNet-101 (He et al., 2016) as input, whereas the SHAPES-SyGeT runs use standardized raw images. Please see Appendix A for the hyperparameters we use.

5.1 SHAPES-SyGeT

The lightweight nature of SHAPES-SyGeT makes it an attractive choice for probing to understand the essential components of our method. For all SHAPES-SyGeT experiments, we record the in-distribution Val-IID and the out-of-distribution Val-OOD accuracies. However, model selection and early stopping are done based on Val-IID. For our IL experiments, we use spectral normalization of the program generator during the learning phase, and we study its utility in Appendix D. We do not report results on Vector-NMN, which performs very poorly. We believe that this is because SHAPES-SyGeT requires intermediate module outputs to contain detailed spatial information, which Vector-NMN has an inductive bias against thanks to its module outputs being vectors.

We note that the reported results on SHAPES in the literature make use of NMN architectures with specially designed modules for each operation (Andreas et al., 2016; Hu et al., 2017; Vedantam et al., 2019). In contrast, we use generic modules in order to study compositional layout emergence with minimal semantic priors, making our results hard to compare directly to prior work using SHAPES.



(a) Task accuracy. Solid lines are training and dashed lines are Val-IID.

(b) Program accuracy.

Figure 4: Learning curves of models with and without IL on SHAPES-SyGeT, using 20 ground-truth programs. The dips in the IL curves indicate the beginning of new generations.

In-distribution and out-of-distribution accuracies. Table 1 illustrates the difference in the performance of various configurations of our models. All the reported models achieve perfect accuracy on the training data but generalize differently to Val-IID and Val-OOD. We find that Tensor-FiLM-NMN generalizes better than Tensor-NMN trained with supervision of both 20 and 135 ground-truth programs. Moreover, we find that IL improves generalization across all configurations. We further evaluate the relationship between program supervision and performance in Figure 3 and find that IL improves performance at all levels of supervision, effectively improving data efficiency.

Learning bottleneck. Although all models achieve perfect training accuracy in under 5000 steps, we notice that IL leads to gradually increasing systematic generalization as training progresses. Figure 4 shows the effect of the learning bottleneck of IL, comparing our two architectures with and without IL. Here, we find that program accuracy[1] increases steadily as training progresses, indicating increasing structure in the language of the programs. Although generated programs that do not match the ground-truth programs exactly could conceivably be compositional, it is unlikely that the 20 ground-truth supervision programs can successfully be incorporated in a compositional structure other than the ground-truth. Importantly, this process is due entirely to the influence of the IL learning bottleneck, as program accuracy without IL actually declines later in training.

Ablation tests. We use SHAPES-SyGeT to perform a series of ablations tests. We report full results for these experiments in Appendix D. Instead of re-initializing agent parameters from scratch at each generation, we consider seeded IL (Lu et al., 2020), in which agents are re-initialized with parameters from the end of the learning phase of the previous generation, as well as simply not re-initializing agents. We explore these strategies for the execution engine, observing large declines in generalization compared to the standard setting. We also study the effect of spectral normalization, finding it highly beneficial when applied to the program generator decoder during the learning phase of IL, but of only marginal benefit otherwise. Finally, we examine a setting where the program generator is reinitialized but not trained to acquire the previous generation's language, which we also find to greatly harm performance, indicating that the learning phase is key.

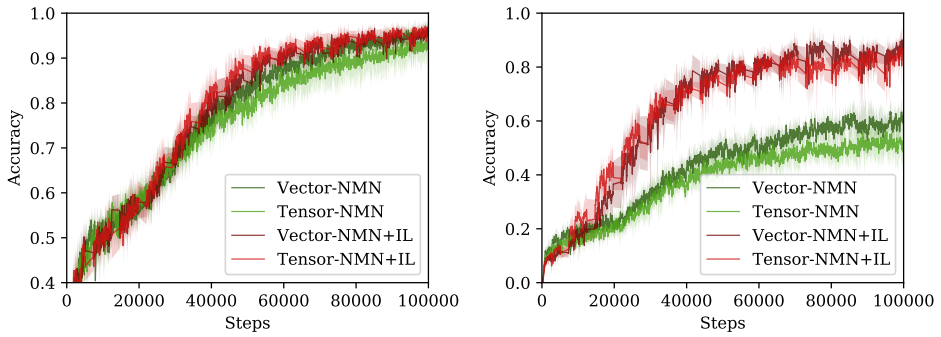
5.2 CLEVR AND CLOSURE

CLEVR is significantly larger and more complex than SHAPES-SyGeT. It takes an execution engine over a day to reach 95% task accuracy on the CLEVR validation set on a Nvidia RTX-8000 GPU, even when trained with ground-truth programs without a program generator. Re-training the execution engine from scratch for every generation of IL is thus computationally infeasible. Between using seeded IL and not resetting the execution engine at all, we find not resetting the execution engine generalizes better. CLEVR contains 699989 training questions, and we provide 100 ground-truth programs for program supervision, one-tenth of that used by Vedantam et al. (2019). For

[1] We consider a program correct if it matches the ground-truth program exactly and incorrect otherwise.

Table 2: Task accuracy on the CLEVR validation set and each CLOSURE category for models trained with and without IL, using 100 ground-truth programs.

Evaluation set	**Tensor-NMN**		**Vector-NMN**	
	Without IL	**With IL**	**Without IL**	**With IL**
CLEVR-Val	0.897 ± 0.05	$\mathbf{0.953 \pm 0.01}$	0.938 ± 0.01	$\mathbf{0.946 \pm 0.00}$
`and_mat_spa`	$\mathbf{0.392 \pm 0.08}$	0.375 ± 0.08	$\mathbf{0.380 \pm 0.11}$	0.240 ± 0.19
`or_mat`	0.379 ± 0.03	$\mathbf{0.516 \pm 0.17}$	0.409 ± 0.08	$\mathbf{0.439 \pm 0.16}$
`or_mat_spa`	0.359 ± 0.05	$\mathbf{0.429 \pm 0.14}$	$\mathbf{0.408 \pm 0.13}$	0.368 ± 0.24
`compare_mat`	0.672 ± 0.16	$\mathbf{0.816 \pm 0.11}$	0.713 ± 0.09	$\mathbf{0.811 \pm 0.13}$
`compare_mat_spa`	0.632 ± 0.08	$\mathbf{0.799 \pm 0.10}$	0.703 ± 0.08	$\mathbf{0.780 \pm 0.12}$
`embed_spa_mat`	0.737 ± 0.07	$\mathbf{0.849 \pm 0.07}$	$\mathbf{0.844 \pm 0.06}$	0.806 ± 0.05
`embed_mat_spa`	0.743 ± 0.11	$\mathbf{0.910 \pm 0.03}$	0.853 ± 0.06	$\mathbf{0.913 \pm 0.02}$



(a) Task training accuracy.

(b) Program accuracy.

Figure 5: Learning curves of models trained with and without IL on CLEVR using 100 ground-truth programs. The dips in the IL curves indicate the beginning of new generations.

CLEVR, we found that Tensor-FiLM-NMN did not improve over Vector-NMN, so for conciseness we report results only on the two standard architectures.

Figure 5 illustrates training dynamics with and without IL on CLEVR, and Table 2 reports model performance on the CLEVR validation set and CLOSURE categories. The CLEVR validation curves through training are presented in Appendix E. Similar to Bahdanau et al. (2019), we find that Vector-NMN generalizes better than Tensor-NMN. However, Tensor-NMN systematically generalizes substantially better with IL. Across both models, using IL improves generalization on CLOSURE, greatly increases program accuracy, and achieves validation performance on CLEVR close to ProbNMN (Vedantam et al., 2019) despite using far fewer ground-truth programs.

6 Conclusion

We establish IL as a practical tool for the emergence of structure in machine learning by demonstrating its utility in challenging VQA tasks using NMNs. Our work shows that IL leads to improved performance with less supervision, and even facilitates systematic generalization. As the study of IL in neural agents is relatively young and has largely dealt with toy problems, our setting presents several important new challenges for IL methods. Unlike in simple games (Ren et al., 2020), the emergence of compositional language entirely from scratch is thus far infeasible in VQA. However, by exploring learning phase regularization, suitable model architectures, and the learning dynamics of IL, we are able to dramatically reduce the amount of ground-truth supervision necessary; the surprising success of spectral normalization in particular should motivate further research into the role of regularization during the learning phase. We hope that this progress will spur future work both to improve IL methods and extend them to other challenging tasks in machine learning.

REFERENCES

Jacob Andreas, Marcus Rohrbach, Trevor Darrell, and Dan Klein. Neural module networks. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pp. 39–48, 2016.

Dzmitry Bahdanau, Kyunghyun Cho, and Yoshua Bengio. Neural machine translation by jointly learning to align and translate. *arXiv preprint arXiv:1409.0473*, 2014.

Dzmitry Bahdanau, Shikhar Murty, Michael Noukhovitch, Thien Huu Nguyen, Harm de Vries, and Aaron Courville. Systematic generalization: what is required and can it be learned? *arXiv preprint arXiv:1811.12889*, 2018.

Dzmitry Bahdanau, Harm de Vries, Timothy J O'Donnell, Shikhar Murty, Philippe Beaudoin, Yoshua Bengio, and Aaron Courville. Closure: Assessing systematic generalization of clevr models. *arXiv preprint arXiv:1912.05783*, 2019.

Matthew M Botvinick and David C Plaut. Empirical and computational support for context-dependent representations of serial order: Reply to bowers, damian, and davis (2009). 2009.

Jeffrey S Bowers, Markus F Damian, and Colin J Davis. A fundamental limitation of the conjunctive codes learned in pdp models of cognition: Comment on botvinick and plaut (2006). 2009.

Philémon Brakel and Stefan Frank. Strong systematicity in sentence processing by simple recurrent networks. In *Proceedings of the Annual Meeting of the Cognitive Science Society*, volume 31, 2009.

Henry Brighton and Simon Kirby. Understanding linguistic evolution by visualizing the emergence of topographic mappings. *Artificial life*, 12(2):229–242, 2006.

Paco Calvo and John Symons. *The architecture of cognition: Rethinking Fodor and Pylyshyn's systematicity challenge*. MIT Press, 2014.

Rahma Chaabouni, Eugene Kharitonov, Diane Bouchacourt, Emmanuel Dupoux, and Marco Baroni. Compositionality and generalization in emergent languages. *arXiv preprint arXiv:2004.09124*, 2020.

Franklin Chang. Symbolically speaking: A connectionist model of sentence production. *Cognitive science*, 26(5):609–651, 2002.

Edward Choi, Angeliki Lazaridou, and Nando de Freitas. Compositional obverter communication learning from raw visual input. *arXiv preprint arXiv:1804.02341*, 2018.

M Christiansen, Nick Chater, et al. Generalization and connectionist language learning. *Mind and Language*, 9(3), 1994.

Michael Cogswell, Jiasen Lu, Stefan Lee, Devi Parikh, and Dhruv Batra. Emergence of compositional language with deep generational transmission. *arXiv preprint arXiv:1904.09067*, 2019.

Gautier Dagan, Dieuwke Hupkes, and Elia Bruni. Co-evolution of language and agents in referential games. *arXiv preprint arXiv:2001.03361*, 2020.

Katrina Evtimova, Andrew Drozdov, Douwe Kiela, and Kyunghyun Cho. Emergent communication in a multi-modal, multi-step referential game. *arXiv preprint arXiv:1705.10369*, 2017.

Jerry A Fodor and Ernest Lepore. *The compositionality papers*. Oxford University Press, 2002.

Jerry A Fodor, Zenon W Pylyshyn, et al. Connectionism and cognitive architecture: A critical analysis. *Cognition*, 28(1-2):3–71, 1988.

Jakob Foerster, Ioannis Alexandros Assael, Nando De Freitas, and Shimon Whiteson. Learning to communicate with deep multi-agent reinforcement learning. In *Advances in neural information processing systems*, pp. 2137–2145, 2016.

Shangmin Guo, Yi Ren, Serhii Havrylov, Stella Frank, Ivan Titov, and Kenny Smith. The emergence of compositional languages for numeric concepts through iterated learning in neural agents. *arXiv preprint arXiv:1910.05291*, 2019.

Serhii Havrylov and Ivan Titov. Emergence of language with multi-agent games: Learning to communicate with sequences of symbols. In *Advances in neural information processing systems*, pp. 2149–2159, 2017.

Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pp. 770–778, 2016.

Sepp Hochreiter and Jürgen Schmidhuber. Long short-term memory. *Neural computation*, 9(8): 1735–1780, 1997.

Ronghang Hu, Jacob Andreas, Marcus Rohrbach, Trevor Darrell, and Kate Saenko. Learning to reason: End-to-end module networks for visual question answering. In *Proceedings of the IEEE International Conference on Computer Vision*, pp. 804–813, 2017.

Drew A Hudson and Christopher D Manning. Compositional attention networks for machine reasoning. *arXiv preprint arXiv:1803.03067*, 2018.

Eric Jang, Shixiang Gu, and Ben Poole. Categorical reparameterization with gumbel-softmax. *arXiv preprint arXiv:1611.01144*, 2016.

Justin Johnson, Bharath Hariharan, Laurens van der Maaten, Li Fei-Fei, C Lawrence Zitnick, and Ross Girshick. Clevr: A diagnostic dataset for compositional language and elementary visual reasoning. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pp. 2901–2910, 2017a.

Justin Johnson, Bharath Hariharan, Laurens Van Der Maaten, Judy Hoffman, Li Fei-Fei, C Lawrence Zitnick, and Ross Girshick. Inferring and executing programs for visual reasoning. In *Proceedings of the IEEE International Conference on Computer Vision*, pp. 2989–2998, 2017b.

Emilio Jorge, Mikael Kågebäck, Fredrik D Johansson, and Emil Gustavsson. Learning to play guess who? and inventing a grounded language as a consequence. *arXiv preprint arXiv:1611.03218*, 2016.

Diederik P Kingma and Jimmy Ba. Adam: A method for stochastic optimization. *arXiv preprint arXiv:1412.6980*, 2014.

Simon Kirby. Spontaneous evolution of linguistic structure-an iterated learning model of the emergence of regularity and irregularity. *IEEE Transactions on Evolutionary Computation*, 5(2):102–110, 2001.

Simon Kirby, Hannah Cornish, and Kenny Smith. Cumulative cultural evolution in the laboratory: An experimental approach to the origins of structure in human language. *Proceedings of the National Academy of Sciences*, 105(31):10681–10686, 2008.

Simon Kirby, Tom Griffiths, and Kenny Smith. Iterated learning and the evolution of language. *Current opinion in neurobiology*, 28:108–114, 2014.

Satwik Kottur, José MF Moura, Stefan Lee, and Dhruv Batra. Natural language does not emerge'naturally'in multi-agent dialog. *arXiv preprint arXiv:1706.08502*, 2017.

Angeliki Lazaridou, Alexander Peysakhovich, and Marco Baroni. Multi-agent cooperation and the emergence of (natural) language. *arXiv preprint arXiv:1612.07182*, 2016.

Angeliki Lazaridou, Karl Moritz Hermann, Karl Tuyls, and Stephen Clark. Emergence of linguistic communication from referential games with symbolic and pixel input. *arXiv preprint arXiv:1804.03984*, 2018.

David Lewis. *Convention: A philosophical study*. John Wiley & Sons, 2008.

Fushan Li and Michael Bowling. Ease-of-teaching and language structure from emergent communication. In *Advances in Neural Information Processing Systems*, pp. 15851–15861, 2019.

Ryan Lowe, Abhinav Gupta, Jakob Foerster, Douwe Kiela, and Joelle Pineau. On the interaction between supervision and self-play in emergent communication. *arXiv preprint arXiv:2002.01093*, 2020.

Yuchen Lu, Soumye Singhal, Florian Strub, Olivier Pietquin, and Aaron Courville. Countering language drift with seeded iterated learning. *arXiv preprint arXiv:2003.12694*, 2020.

Gary F Marcus. Rethinking eliminative connectionism. *Cognitive psychology*, 37(3):243–282, 1998.

Gary F Marcus. *The algebraic mind: Integrating connectionism and cognitive science*. MIT press, 2018.

Takeru Miyato, Toshiki Kataoka, Masanori Koyama, and Yuichi Yoshida. Spectral normalization for generative adversarial networks. *arXiv preprint arXiv:1802.05957*, 2018.

Ethan Perez, Florian Strub, Harm De Vries, Vincent Dumoulin, and Aaron Courville. Film: Visual reasoning with a general conditioning layer. In *Thirty-Second AAAI Conference on Artificial Intelligence*, 2018.

Steven Phillips. Are feedforward and recurrent networks systematic? analysis and implications for a connectionist cognitive architecture. *Connection Science*, 10(2):137–160, 1998.

Yi Ren, Shangmin Guo, Matthieu Labeau, Shay B Cohen, and Simon Kirby. Compositional languages emerge in a neural iterated learning model. *arXiv preprint arXiv:2002.01365*, 2020.

Adam Santoro, David Raposo, David G Barrett, Mateusz Malinowski, Razvan Pascanu, Peter Battaglia, and Timothy Lillicrap. A simple neural network module for relational reasoning. In *Advances in neural information processing systems*, pp. 4967–4976, 2017.

Catriona Silvey, Simon Kirby, and Kenny Smith. Word meanings evolve to selectively preserve distinctions on salient dimensions. *Cognitive science*, 39(1):212–226, 2015.

Amanpreet Singh, Tushar Jain, and Sainbayar Sukhbaatar. Learning when to communicate at scale in multiagent cooperative and competitive tasks. *arXiv preprint arXiv:1812.09755*, 2018.

Brian Skyrms. *Signals: Evolution, learning, and information*. Oxford University Press, 2010.

Luc Steels and Martin Loetzsch. The grounded naming game. *Experiments in cultural language evolution*, 3:41–59, 2012.

Sainbayar Sukhbaatar, Rob Fergus, et al. Learning multiagent communication with backpropagation. In *Advances in neural information processing systems*, pp. 2244–2252, 2016.

Frank van der Velde, Gwendid T van der Voort van der Kleij, and Marc de Kamps. Lack of combinatorial productivity in language processing with simple recurrent networks. *Connection Science*, 16(1):21–46, 2004.

Ramakrishna Vedantam, Karan Desai, Stefan Lee, Marcus Rohrbach, Dhruv Batra, and Devi Parikh. Probabilistic neural-symbolic models for interpretable visual question answering. *arXiv preprint arXiv:1902.07864*, 2019.

Willem H Zuidema. How the poverty of the stimulus solves the poverty of the stimulus. In *Advances in neural information processing systems*, pp. 51–58, 2003.

Table 3: IL hyperparameters used in our experiments.

Hyperparameter	**Value**
Optimizer	Adam (Kingma & Ba, 2014)
PG learning rate	0.0001
EE learning rate	0.0001 for CLEVR, 0.0005 for SHAPES-SyGeT Tensor-NMN, 0.001 for Tensor-FiLM-NMN
Batch size	128
GT programs in batch	4
PG spectral normalization	On for SHAPES-SyGeT, off for CLEVR
Interacting phase length T_i	2000 for SHAPES-SyGeT, 5000 for CLEVR
Transmitting phase length T_t	2000
PG learning phase length T_p	2000
EE learning phase length T_e	For SHAPES-SyGeT, 250 when re-initializating EE from scratch, 200 for seeded IL; 50 when not resetting EE (both SHAPES-SyGeT and CLEVR)

A HYPERPARAMETERS

Table 3 details the hyperparameters used in our experiments in Section 5 for both SHAPES-SyGeT and CLEVR.

B NMN DETAILS

B.1 PROGRAM GENERATOR

The program generator is a seq2seq model that translates input questions to programs. We use the Seq2SeqAtt model of Bahdanau et al. (2019), where unlike Johnson et al. (2017b), the decoder uses an attention mechanism (Bahdanau et al., 2014) over the encoder hidden states. We found this model to generalize better on held-out in-distribution questions in preliminary experiments. Ideally, the program generator's target must be tree-structured since the output program represents a computation graph. Since a seq2seq model cannot directly model graphs, we instead model a serialized representation of the programs. Like Johnson et al. (2017b), we chose to use the Polish (or prefix) notation to serialize the syntax tree.

Considering the program generator parameterized by θ, the probability distribution over layouts $\hat{\boldsymbol{z}}$ is given by

$$p_\theta(\hat{\boldsymbol{z}} \mid \boldsymbol{q}) = \prod_{i=1}^{t} p_\theta(\hat{z}_i \mid \hat{z}_{1:i-1}, \boldsymbol{q}). \tag{5}$$

During training, we sample programs from this distribution but take the $\arg\max$ at each timestep when evaluating our model. We use an LSTM (Hochreiter & Schmidhuber, 1997) trained using teacher forcing to represent the distribution $p_\theta(\hat{z}_i \mid \hat{z}_{1:i-1}, \boldsymbol{q})$ at every timestep i. To condition on $\boldsymbol{q}$ for each decoder step, we perform attention on the hidden states of a bidirectional LSTM encoder over the question $\boldsymbol{q}$.

B.2 EXECUTION ENGINE

To run the program $\hat{\boldsymbol{z}}$ produced by the program generator, the execution engine assembles neural modules according to $\hat{\boldsymbol{z}}$ into a neural network that takes $\boldsymbol{x}$ as input to produce an answer $\hat{y}$. We consider this execution engine $EE_\phi(\boldsymbol{x}, \hat{\boldsymbol{z}})$ to be parameterized by ϕ. To illustrate a forward pass through the module network, consider the program '`and color[green] scene transform[left_of] shape[square] scene`' from Figure 1. '`scene`' is a special module which represents the input image features from a CNN feature extractor. According to the annotators, the '`color[green]`' module should filter green shapes from the scene, and the

Split	Total questions	Unique questions
Train	13568	212
Val	1024	16
Test	1024	16

(a) SHAPES dataset.

Split	Total questions	Unique questions
Train	7560	135
Val-IID	1080	135
Val-OOD	6976	109

(b) SHAPES-SyGeT dataset.

Table 4: Split of questions in the SHAPES and SHAPES-SyGeT datasets.

'`shape[square]`' module should filter squares. '`transform[left_of]`' should select regions to the left of the filtered squares. In Figure 1, the final '`and`' module should then compute the intersection of green shapes and the region to the left of squares. A classifier takes this output from the top-level module to produce a distribution $\hat{\boldsymbol{y}}$ over answers. We consider the final answer $\hat{y}$ to be the $\arg\max$ of $\hat{\boldsymbol{y}}$.

Each module corresponds to one token of the program and can be reused in different configurations. Like Johnson et al. (2017b), our modules are not hand-designed to represent certain functions but have a similar architecture for all operators. Other than the '`scene`' module which has arity 0, all other modules are implemented as a CNN on the module inputs to produce a module output. In this work, we explore three module architecture choices to make up the execution engine: *Tensor-NMN*, *Vector-NMN*, and *Tensor-FiLM-NMN*. Here, the Tensor-NMN module architecture is the module network proposed by Johnson et al. (2017b), and Vector-NMN is the architecture from Bahdanau et al. (2019).

C SHAPES-SyGeT TEMPLATES AND SPLITS

The images in SHAPES are arranged in a 3×3 grid, where each grid cell can contain a triangle, square, or circle that is either red, green, or blue, or the cell can be empty. Table 4a shows the standard splits for training and evaluating SHAPES used in the literature (Andreas et al., 2016; Hu et al., 2017; Vedantam et al., 2019). We categorize SHAPES questions into 12 standard templates, listed in Table 5. We then derive new splits for the SHAPES data, such that each split has the same primitives, but different ways in which the primitives are combined. The final split of the SHAPES-SyGeT dataset is presented in Table 4b.

D ABLATION EXPERIMENTS

We do ablation experiments on SHAPES-SyGeT rather than CLEVR or CLOSURE, as the computational requirements of experiments on this dataset are nearly an order of magnitude lighter. Results are presented in Table 6. We focus primarily on the Tensor-FiLM-NMN, which we find benefits far more from IL than the default Tensor-NMN. In all cases we use 20 ground-truth supervision programs, a setting which we find to most clearly reflect differences between methods.

To confirm that our results are not solely due to our use of spectral normalization, we examine the use of SN throughout training in non-IL runs ("FullSN"); we find that it has at best marginal impacts on performance, indicating that it is not responsible for the success of our method.

We also consider various schemes for the reinitialization of the execution engine parameters $\tilde{\phi}$, including the standard method (reinitialization from the same random distribution initially used), *Seeded* reinitialization, where parameters from the end of the previous generation's learning phase (but before its interaction phase) are used, and not resetting the network at all ('NoReset'). We find a clear benefit to reinitializing the execution engine from scratch, although seeded IL outperforms not resetting the execution engine at all.

Finally, we also consider the effects of simply not retraining the program generator at all during the learning phase, entirely ablating the aspect of generational transmission. We find that this setting performs roughly comparably to the no-IL setting; this is expected, as in this case little generational

Template		Total questions	Unique questions
Train templates		8640	135
1.	is a COLOR shape RELATIVE(1) a COLOR shape	2304	36
2.	is a SHAPE RELATIVE(1) a COLOR shape	2304	36
3.	is a SHAPE RELATIVE(2) a COLOR shape	960	15
4.	is a SHAPE RELATIVE(2) a SHAPE	1344	21
5.	is a COLOR shape a SHAPE	576	9
6.	is a SHAPE COLOR	576	9
7.	is a SHAPE a SHAPE	576	9
Evaluation templates		6976	109
8.	is a COLOR shape RELATIVE(2) a COLOR shape	960	15
9.	is a COLOR shape RELATIVE(1) a SHAPE	2304	36
10.	is a COLOR shape RELATIVE(2) a SHAPE	832	13
11.	is a SHAPE RELATIVE(1) a SHAPE	2304	36
12.	is a COLOR shape COLOR	576	9

Table 5: Overview and splits of the SHAPES-SyGeT templates. The placeholder COLOR can take values in 'red,' 'green,' and 'blue,' and SHAPE can be either 'circle,' 'triangle,' or 'square.' RELATIVE(1) is a placeholder for one of the positional prepositions 'above,' 'below,' 'left of,' or 'right of,' whereas RELATIVE(2) is a combination of two RELATIVE(1)s, such as 'above left of.'

PG: Seq2SeqAtt	**EE: Tensor-NMN**	**Val-IID**	**Val-OOD**
+FullSN	-	0.646 ± 0.03	0.614 ± 0.01
+NoSN	-	0.645 ± 0.01	0.616 ± 0.01
	EE: Tensor-FiLM-NMN		
+FullSN	-	0.642 ± 0.02	0.596 ± 0.02
+NoSN	-	0.649 ± 0.02	0.605 ± 0.01
+IL	+IL	0.954 ± 0.07	0.858 ± 0.15
+IL+NoSN	+IL	0.803 ± 0.13	0.630 ± 0.07
+IL+NoRetrain	+IL	0.834 ± 0.13	0.664 ± 0.06
+IL	+IL+Seeded	0.792 ± 0.05	0.626 ± 0.01
+IL+NoSN	+IL+Seeded	0.744 ± 0.13	0.647 ± 0.12
+IL+NoRetrain	+IL+Seeded	0.794 ± 0.12	0.662 ± 0.11
+IL	+IL+NoReset	0.624 ± 0.02	0.586 ± 0.01
+IL+NoSN	+IL+NoReset	0.629 ± 0.01	0.588 ± 0.01
+IL+NoRetrain	+IL+NoReset	0.682 ± 0.05	0.600 ± 0.01

Table 6: Ablation experiments for models on SHAPES-SyGeT trained with 20 ground-truth programs. 'FullSN': spectral normalization applied throughout training;"NoSN': no spectral normalization in any phase; 'NoRetrain': new program generator is taken from the previous generation without any re-training; 'Seeded': new execution engine is initialized to the state after previous learning phase; 'NoReset': execution engine is not re-initialized at the start of a generation.

transmission occurs, meaning that the IL bottleneck that encourages gradual drift towards compositionality cannot take effect.

In summary, these results indicate that the generational transmission aspect of our algorithm is a key component of its success, and bolster our contention that regularization during the student's acquisition of its predecessors' language has a uniquely positive effect, far outweighing its impact during regular training.

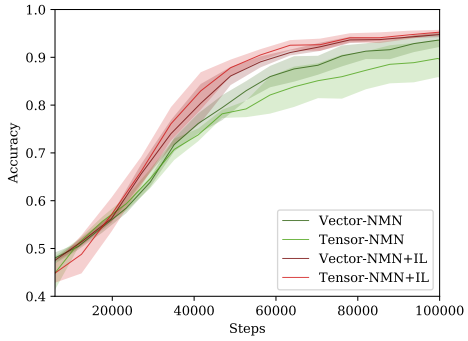


Figure 6: Learning curves of models trained with and without IL on CLEVR using 100 ground-truth programs. The dips in the IL curves indicate the beginning of new generations.

E CLEVR VALIDATION CURVES

The validation curves for CLEVR, illustrated in Figure 6, are similar to the training curves in Figure 5. Although CLEVR training exhibits a lower amount of overfitting compared to SHAPES-SyGeT, we observe higher systematic generalization performance on CLOSURE with models trained using IL.