CURSE OF INSTRUCTIONS: LARGE LANGUAGE MODELS CANNOT FOLLOW MULTIPLE INSTRUCTIONS AT ONCE

Anonymous authors
Paper under double-blind review

ABSTRACT

Large language models (LLMs) have demonstrated impressive performance across various natural language processing (NLP) tasks owing to the strong capability of following instructions. To further accelerate the integration of LLMs into our society, it is essential to have LLMs follow many instructions as accurately as humans do. This study reveals that LLMs unexpectedly struggle to follow all instructions simultaneously as the number of instructions increases. First, to validate our claim, we introduce ManyIFEval, a large-scale benchmark dataset comprising task prompts with up to ten objectively verifiable instructions. Second, we conduct experiments based on ManyIFEval with GPT-4o, Claude-3.5, Gemini-1.5, Gemma2, and Llama3.1, demonstrating that as the instruction count rises, the models' ability to follow individual instruction deteriorates gradually but constantly. As a result, the models' ability to follow all the instructions significantly drops: the success rate of all the instructions is precisely explained by the success rate of individual instructions to the power of total number of instructions. We refer to it as the "curse of instructions". Third, to remove the curse without retraining models, we propose an inference-time strategy that enhances performance through iterative self-refinement. We demonstrate that instruction-level chain-of-thought reasoning significantly improves their capability to detect and correct instruction-following errors. Notably, our method has improved the success rate of following ten instructions by GPT-4o from 15% to 31% and Claude 3.5 Sonnet from 44% to 58%. We also show that precision is more important than recall in feedback: just telling LLMs that they are not following all the instructions also improves self-refinement success. Our findings highlight a fundamental limitation of instruction-following ability and suggest a future direction for building trustworthy LLMs that can coexist with human society. [1]

1 INTRODUCTION

Large language models (LLMs) have demonstrated impressive performance across various natural language processing tasks (OpenAI, 2024b; Google, 2023). When utilizing LLMs for solving diverse tasks, prompting (Brown et al., 2020; Vatsal & Dubey, 2024; Sahoo et al., 2024) has become a prevalent approach. Prompting involves providing textual instructions to guide the model's behavior towards desired outcomes. This instruction-following ability mainly comes from instruction tuning process (Wei et al., 2022a; Zhang et al., 2023; Chung et al., 2024).

As LLMs continue to evolve, their ability to follow multiple instructions simultaneously becomes crucial for broader applications. In human society, individuals perform activity under numerous laws and organizational norms. For LLMs to be more reliable and widely applicable in human contexts, they must adhere to the various rules. Moreover, in domain-specific applications, LLMs need to comply with established guidelines and regulations. For instance, legal applications require adherence to thousands of statutes (Guha et al., 2023), while medical applications must follow numerous clinical guidelines (Singhal et al., 2023; Kasai et al., 2023; Hager et al., 2024).

[1] ManyIFEval dataset and inference code are available at `https://anonymous.4open.science/r/ManyIFEval`

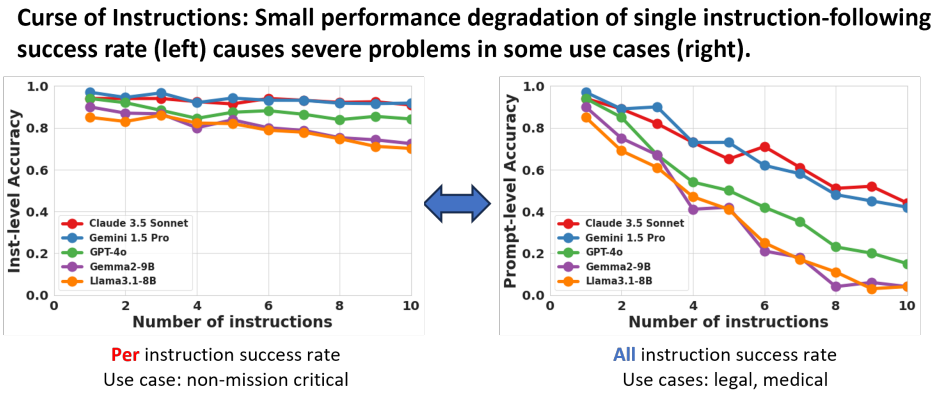

Figure 1: Problem of curse of instructions.

However, the extent to which models can adhere to multiple instructions simultaneously remains unclear. To address this question, we construct ManyIFEval, a large-scale benchmark dataset comprising task prompts with up to ten objectively verifiable sets of instructions. These instructions are designed with a difficulty level such that major models can successfully follow them in most cases. Unlike existing benchmarks that typically provide only a few instructions at a time (Wang et al., 2022b; Wei et al., 2022a; Conover et al., 2023), our benchmark scales up to ten concurrent instructions by extending IFEval (Zhou et al., 2023a) .

Our experiments reveal that as the number of instructions increases, models struggle to adhere to all of them by following a simple rule of instructions. Specifically, we conduct experiments based on ManyIFEval with various type of models, including closed models (GPT-4o (OpenAI, 2024a), Claude 3.5 Sonnet(Anthropic, 2024), and Gemini 1.5 Pro (Gemini Team, 2024)) and open models (Gemma2 (Gemma Team, 2024) and Llama3.1 (Llama Team, 2024)). The experiments demonstrate that as the instruction count rises, the models' ability to follow individual instruction deteriorates gradually but constantly. Consequently, the models' ability to follow all the instructions significantly drops by following a simple rule: the success rate of all the instructions is precisely explained by the success rate of individual instructions to the power of total number of instructions. We refer to it as the "curse of instructions".

To alleviate the curse of significant performance drop without additional training, we explore inference-time strategies (Brown et al., 2024; Welleck et al., 2024) that enhance performance through iterative self-refinement (Madaan et al., 2023). We find that having the model refine its response by feedback from itself leads to improved performance. When creating this feedback, it is beneficial to use Chain-of-Thought reasoning (Wei et al., 2022b; Kojima et al., 2022) for each instruction. This approach enhances performance by increasing inference time without the need for model retraining, making it applicable to models available only through APIs and avoiding the substantial costs associated with retraining model weights. Notably, our method has improved the success rate of the following ten instructions by GPT-4o from 15% to 31% and Claude 3.5 Sonnet from 44% to 58%. We also show that recall is more important than precision in feedback: just telling LLMs that they are not following all the instructions also improves self-refinement success.

In summary, our contributions are as follows.

- We construct and release a new benchmark called ManyIFEval for measuring the performance of multiple instruction adherence by scaling the axis of instruction count.
- Comprehensive analysis based on ManyIFEval with various types of closed models (GPT-4o, Claude-3.5, and Gemini-1.5) and open models (Gemma2 and Llama3.1) demonstrate that even the state-of-the-art models struggle to follow multiple instructions at once when scaling the number of instructions.
- We reveal a secret principle behind the significant drop in performance: as instruction count rises, the models' ability to follow individual instruction deteriorates gradually but constantly. Consequently, the success rate of following all the instructions significantly drops

by following the success rate of individual instructions to the power of total number of instructions.

- We propose a method to mitigate the performance degradation by iterative self-refinement through self-feedback loops in combination with chain-of-thought reasoning for each instruction. We also show that recall is more important than precision for the feedback.
- Our findings highlight a fundamental limitation of instruction-following ability and suggest a future direction for building trustworthy LLMs that can coexist with human society.

2 RELATED WORKS

2.1 BENCHMARKS FOR EVALUATING MULTIPLE INSTRUCTION-FOLLOWING PERFORMANCE

Instruction-following is a critical capability of large language models (LLMs), and various benchmark datasets have been proposed to evaluate this aspect (Wang et al., 2022b; Li et al., 2023; Zheng et al., 2023; Hayati et al., 2024; He et al., 2024b; Jiang et al., 2024; He et al., 2024a). Our study focuses on the relationship between instruction-following performance and the complexity of instructions, specifically measured by the number of instructions within a prompt. While several benchmarks investigate this relationship from different angles, our work uniquely emphasizes the impact of instruction count on model performance.

For instance, FollowBench (Jiang et al., 2024) incrementally adds up to five constraints (e.g. Situation, Format, Style) to a single prompt, organizing data according to the number of added constraints. FollowBench also includes a subset called "Mixed Constraints," which, like our work, adds constraints of different types to simulate real-world use cases. However, their Mixed Constraints primarily involve only tasks that need to edit or transform input sentences. Their findings indicate that instruction-following performance deteriorates as the number of constraints increases. However, the experiment was conducted with a limited number of instruction count and sample size.

ComplexBench (He et al., 2024a) includes not only "And"-type instructions—independent instructions that the model must satisfy simultaneously, similar to our benchmark—but also "Chain" instructions that require sequential execution and "Selection" instructions that involve conditional branching. ComplexBench demonstrates that complex instructions, such as those in the "Selection" and "Chain" categories, pose significant challenges for LLMs in terms of compliance.

IFEval (Zhou et al., 2023a), the basis of our ManyIFEval, consists of a set of 25 categories of verifiable instructions and 541 prompts to which 1 to 3 instructions are assigned. These prompts are first rephrased with few-shot prompting to increase the diversity of wording, and then manually checked to ensure that there are no conflicts between the instructions. Furthermore, the method of judging compliance is programmatic and deterministic, and analysis of the evaluation results leads to insights on instructions that are difficult to comply with and to comparisons among various LLMs.

Regarding the quality of the datasets, it is crutial to have a wide range of complexity and abundant samples for each number of instructions to verify the relationship between the increase in the number of instructions and LLM's ability to follow plural instructions. As shown in Table 1 and Figure 2, because FollowBench and IFEval have the small variation in the number of instructions, it can be difficult to adequately verify the capability of following multiple instructions of LLMs. Furthermore, although samples with 14 instructions are included in ComplexBench, such samples exceedingly rare and the majority of samples are concentrated within the range of 3 to 6, which means that the number of instructions is not balanced across samples. Contrary to them, ManyIFEval includes samples with up to 10 instructions and 100 samples are contained for each instruction count. Therefore, our benchmark is preferable because of the sufficient variation in the number of instructions and the balanced samples.

Regarding evaluation methods, approaches to assess instruction-following can be broadly categorized into human evaluation, model-based automatic evaluation, and program-based automatic evaluation. Human judgment is costly and time-consuming. While Model-based evaluations (Zhang et al., 2020; Liu et al., 2023), which is partially adopted by FollowBench and ComplexBench, can be influenced by the evaluating model's biases and limitations (Zhou et al., 2023b; Shen et al., 2023; Zheng et al., 2023). Program-based methods, which evaluates instruction-following performance by programmable rules, offer a cost-effective and objective alternative, allowing for accurate assess-

Table 1: Feature comparison among multiple instruction benchmarks.

Benchmark	Language	#Samples	#Prompts	#Instructions per sample (max)	Is the number of instructions per sample balanced?	Evaluation Method
FollowBench	English	85	17	✗ 5	✓ Yes	✗ Model & Program
IFEval	English	541	541	✗ 3	✗ No	✓ Program
ComplexBench	Chinese	1150	1150	✓ 14	✗ No	✗ Model & Program
ManyIFEval	English	1000	100	✓ 10	✓ Yes	✓ Program

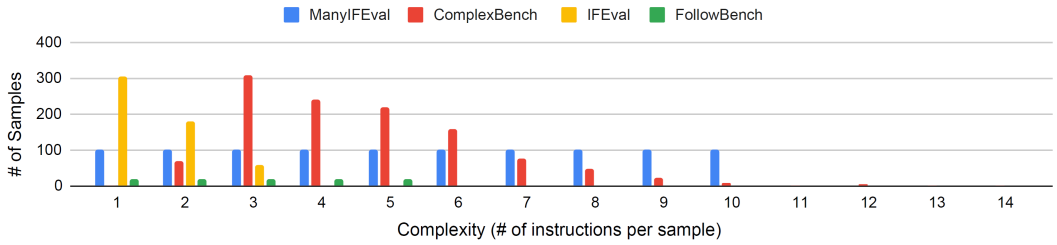

Figure 2: Histogram on the number of instructions per sample for each benchmark.

ments without the constraints of the other approaches. To facilitate reliable and efficient evaluation, we extend an existing dataset called IFEval, which allows for program-based automatic evaluation of instruction-following. By leveraging program-based evaluation, we create a benchmark that not only objectively measures LLMs' ability to follow complex instructions but also provides insights into how instruction count affects performance.

2.2 Methods to Improve Instruction-Following Ability

LLMs are primarily pre-trained on large corpora of web documents to predict subsequent words, without specific training to respond to human textual instructions. To enhance their ability to interpret and follow human instructions, instruction tuning (Wei et al., 2022a; Zhang et al., 2023) is performed as the most representative method for post pre-training. These methods train models on datasets consisting of instructions paired with appropriate responses, such as FLAN (Wei et al., 2022a), Alpaca (Taori et al., 2023), and Dolly (Conover et al., 2023).

More recent studies (Xu et al., 2023; He et al., 2024a) have highlighted that existing datasets often feature only few instructions for each task. The studies have synthesized more complex instruction datasets using LLMs themselves, reporting improvements in instruction-following performance through fine-tuning with these intricate data. While the target instruction count in the studies is limited, this perspective is crucial for enabling models to handle multiple instructions.

However, retraining LLMs is often impractical due to the substantial computational resources required and the risk of catastrophic forgetting, where retraining may degrade the model's performance on previously learned tasks. Additionally, for LLMs accessed via commercial APIs, users are often restricted to access to model parameters and to finetune LLMs.

Therefore, we explore performance enhancement methods that do not require retraining and are applicable to API-accessible models by focusing on inference strategies. Techniques such as generating multiple outputs and selecting the most suitable one through majority voting (Wang et al., 2022a), or self-refinement (Madaan et al., 2023), have demonstrated performance improvements across various tasks. This study focuses on self-refinement for improving the instruction following ability of multiple instructions, where LLMs first produce an initial response and execute a loop of error detection and refinement by themselves.

3 ManyIFEval

To investigate the relationship between the number of instructions and the instruction-following performance of language models, we constructed a dataset called ManyIFEval. This benchmark enables

Figure 3: An example from the ManyIFEval dataset, a benchmark designed to evaluate how well models can follow up to 10 instructions simultaneously. Each example consists of a free-form task prompt, such as *"Write a blog post about a trip to Japan."*, accompanied by a set of objectively verifiable instructions that must be satisfied when performing the task.

an objective evaluation of how the increase in similar-difficulty instructions—up to a maximum of ten—affects a model's ability to follow instructions.

3.1 DATASET

As shown in figure 3, each instance in ManyIFEval consists of a free-form task prompt, such as *"Write a blog post about a trip to Japan."*, accompanied by a set of instructions that must be satisfied when performing the task. To systematically examine the impact of the number of instructions on performance, we created ten instances per task prompt, varying the number of instructions from one to ten.

Considering all possible combinations of which instructions to include and the order in which they appear would result in an enormous number of instances, leading to prohibitive inference costs during evaluation. Therefore, to maintain computational feasibility while ensuring a comprehensive assessment across various models, we limited the dataset to ten instances per task prompt, each with a different number of instructions ranging from one to ten.

The task prompts and instructions were extracted from the existing IFEval benchmark. In the extraction process, we selected task prompts that remain feasible even when additional instructions are provided, and instruction groups that are non-conflicting and can be simultaneously satisfied. Through manual verification, we curated a total of 216 task prompts from an initial set of 541. These were divided into 110 for training, 100 for testing, and 6 for few-shot prompting.

There are a total of 15 instructions categorized into the following six types:

- **Keywords**: Specifying keywords to include or exclude.
- **Length Constraints**: Specifying the length of the answer.
- **Detectable Format**: Requiring bullet point formatting.
- **Change Cases**: Specifying the use of uppercase or lowercase letters.
- **Start with / End with**: Instructions to begin or conclude with quotation mark.
- **Punctuation**: Prohibiting the use of commas.

Details of these instruction types are provided in Appendix B. For instruction types like *Change Cases* and *Length Constraints*, we select one variant each, ensuring that up to ten non-conflicting instructions are chosen from the total of 15.

The compliance with each instruction can be objectively verified programmatically, allowing us to determine success or failure in instruction following. Importantly, the selected 15 instructions are designed such that, when only one instruction is given with the task prompt, GPT-4o(gpt-4o-2024-05-13) achieves high success rate. GPT-4o achieves a success rate of over 90% for nine instructions, over 80% for four instructions, over 60% for two instructions. In other words, these instructions are designed with a difficulty level such that major models can successfully follow them in most cases: we excluded individually challenging instructions from our benchmark to focus on observing changes in performance as the number of instructions increases. By constructing the dataset with in-

structions of similar difficulty, ManyIFEval is well-suited for examining how increasing the number of instructions impacts a model's instruction-following performance.

3.2 Evaluation Metrics

To evaluate instruction-following performance, we adopted metrics based on those used in IFEval and FollowBench. We define:

- **Prompt-level Accuracy**: The success rate of following all given instructions simultaneously for a particular prompt (equation 1). This assesses the model's capability to handle multiple instructions at once. This is Hard Satisfaction Rate (HSR) in FollowBench.
- **Instruction-level Accuracy (Inst-level accuracy)**: The success rate of following individual instructions in its response (equation 2). This metric assesses the model's ability to adhere to each instruction separately. This is Soft Satisfaction Rate (SSR) in FollowBench.

By applying these metrics, we can quantitatively assess how well language models perform as the number of instructions increases, providing valuable insights into their limitations and guiding future improvements in instruction-following capabilities. Concretely, Prompt-level accracy is defined as

$$\text{Prompt-level Accuracy (n)} = \frac{1}{m}\sum_{i=1}^{m}\prod_{j=1}^{n} s_i^j, \tag{1}$$

Where m represents the number of prompts and n represents the number of instructions per prompt, s_i^j represents an binary metric if the target instruction $j \in n$ in a task $i \in m$ is sucessfully followed. $\prod_{j=1}^{n} s_i^j = 1$ if all instructions for prompt i are satisfied, and 0 otherwise. Thus, this metric computes whether every instruction in a prompt is followed or not. Inst-level accracy is defined as

$$\text{Inst-level Accuracy (n)} = \frac{1}{mn}\sum_{i=1}^{m}\sum_{j=1}^{n} s_i^j, \tag{2}$$

where $s_i^j = 1$ if the j-th instruction of the i-th task is satisfied, and $s_i^j = 0$ otherwise.

4 Evaluation

4.1 Models and Settings

To evaluate the impact of scaling the number of instructions on LLMs' ability to follow them, we conducted experiments using both closed-source and open-source models. For closed models which are accessible exclusively via APIs, we evaluated GPT-4o (gpt-4o-2024-05-13), Claude 3.5 Sonnet (claude-3-5-sonnet-20240620), and Gemini 1.5 Pro (gemini-1.5-pro-002). For open-source models, we assessed Gemma2 (gemma-2-9b-it) and Llama 3.1 (Meta-Llama-3.1-8B-Instruct). Inference for the open models was performed using the transformers (Wolf et al., 2020) and vLLM (Kwon et al., 2023) libraries. All models were evaluated using zero-shot prompting.

During decoding, we employed greedy decoding (top-k=1) to ensure deterministic outputs across models. However, for GPT-4o, we were unable to specify greedy decoding directly due to API limitations. As an alternative, we approximated greedy decoding by setting the nucleus sampling parameter to top-p=1e-10, effectively constraining the model to select the highest-probability tokens.

4.2 Effect of increasing the number of instructions

We investigated the effect of increasing the number of instructions on the models' instruction-following performance. In this experiment, we use a standard prompting method, zero-shot prompting: we set a task description and multiple instructions in a prompt and let the models generate an answer. Figure 1 (left) presents the inst-level accuracy and Figure 1 (right) presents the prompt-level accuracy and on the ManyIFEval benchmark. Our observations indicate a consistent trend across all models: even when individual instructions were based on simple rules, the models struggled to follow all instructions as the total number increased. And also, the results revealed that while the

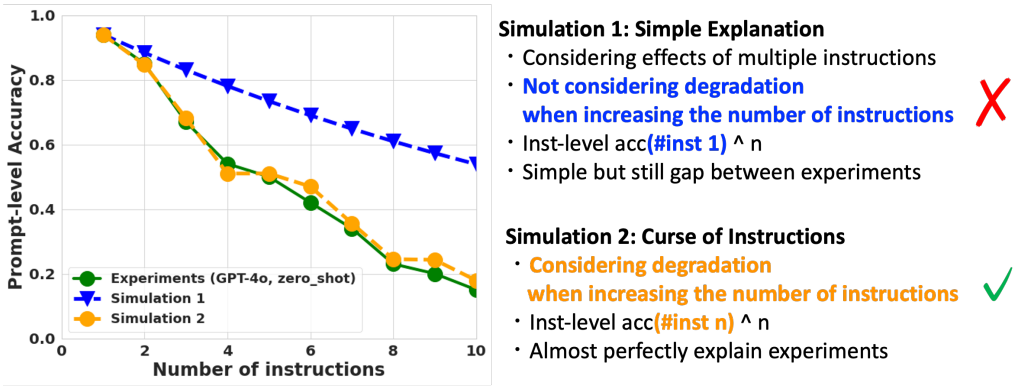

Figure 4: We empirically reveal a secret rule of LLMs when they follow multiple instructions: we refer to it as "curse of instructions". When given a total number of instructions to follow as n, LLMs obey a simple rule: Prompt-level accuracy (n) = (Instruction-level accuracy (n))^n. See Section 4.3 for the detailed explanation. See Appendix F for more results on various models.

models can follow instructions with high accuracy when presented individually, they experienced significant performance degradation of the same instructions as the number of accompanying instructions increased. This indicates that the presence of additional instructions adversely affects the models' ability to attend to and execute each instruction correctly.

4.3 Curse of Instructions

We empirically reveal a secret rule of LLMs when they follow multiple instructions: "curse of instructions". When given a total number of instructions to follow as n, LLMs obey a simple rule.

$$\text{Prompt-level accuracy (n)} = (\text{Instruction-level accuracy (n)})^n. \tag{3}$$

Recall that prompt-level accuracy and instruction-level accuracy are defined in Equation (1) and Equation (2) respectively. **This equation indicates that as the number of instructions increases, the overall instruction-following ability decreases endlessly, unless each instruction-following success rate is 100%.** However, unfortunately, we have confirmed that as the number of instructions increases, the models' ability to follow individual instruction deteriorates gradually but constantly (See Figure 1 (left)). This unacceptable fact further accelerates deterioration of the performance of prompt-level accuracy due to the accumulation of individual errors. As a result, the models' ability to follow all the instructions significantly drops. Figure 4 describes the simulation results of the rule. The result demonstrates that prompt-level accuracy is quite accurately explained by the above equation across models. See Appendix F for more results. In summary, the current LLMs inevitably cannot follow multiple instructions at once. This is an extremely inconvenient fact when we are implementing LLMs in human society, which always have many rules.

5 Inference Time Algorithms to Mitigate the Problem

5.1 Our Method

To alleviate the "curse of instructions", we explore a method to enhance instruction-following performance of LLMs without modifying their parameters. Given the enormous number of parameters in LLMs, fine-tuning or retraining is computationally expensive, and some models are accessible only via APIs, limiting the ability to adjust their internal weights. Therefore, we investigate inference-time strategies that can improve performance without altering the underlying model.

We propose a method of iterative self-refinement in which the model itself evaluates whether the model successfully follow each instruction and then corrects its answers based on this evaluation. An overview of the proposed method is illustrated in Figure 5. Specifically, given a task description and instructions to follow within a prompt, our method lets the model first generate an initial answer

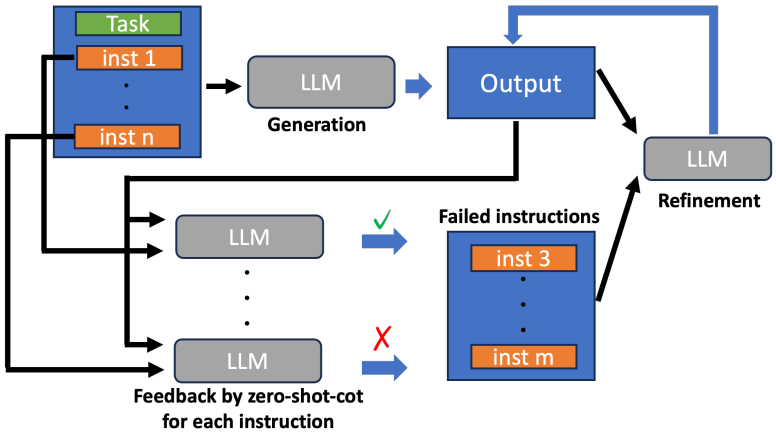

Figure 5: Overview of our method.

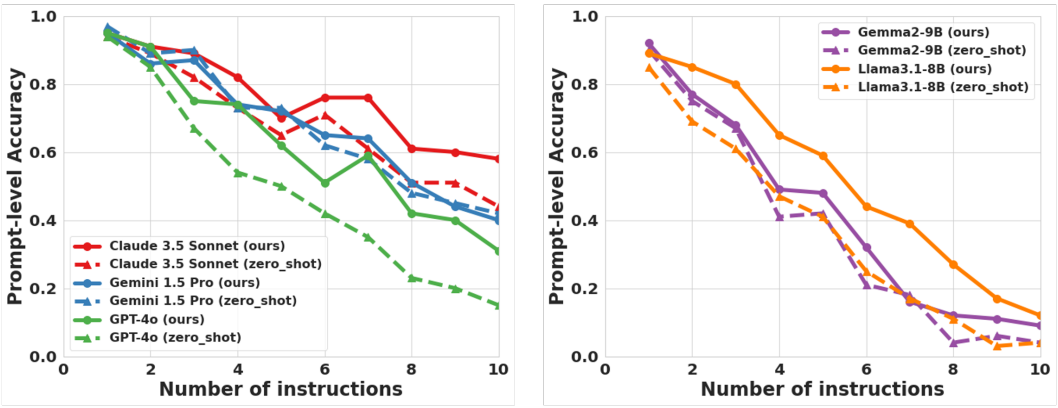

Figure 6: Performance improvement by our method.

(output). As a subsequent process, the model by itself judges the success or failure in following each instruction for the output text. Our method utilizes Zero-shot Chain-of-Thought (Zero-shot-CoT) (Kojima et al., 2022) to improve the judgement ability by enhancing the reasoning. Based on the hypothesis that attentions on multiple instructions may degrade feedback performance of LLMs, our method lets LLMs judges each instruction one by one rather than assessing all instructions at once. After the feedback, we set a subset of instructions that are judged as failure as well as the previous output into the prompt to let the model refine the output texts. Our method iteratively repeat the self-feedback and self-refinement cycle for a fixed number of times T. We set $T = 5$ across all the experiments.

The Experiment results of our method is presented in Figure 6. We observed that the performance of our method drastically improved compared with zero-shot, which is a standard way of just outputting an answer based on the instructions in a prompt (See Section 4.2). Notably, our method has improved the success rate of the following ten instructions by GPT-4o from 15% to 31%, Claude 3.5 Sonnet from 44% to 58%, and Llama3.1-8B from 4% to 12%.

5.2 Comparison With Baseline Methods

To show that our method is appropriately designed so that it achieves the better performance than naive implementation, we conduct a comparison experiment with several baselines which are created by decomposing technical elements in our method. The following is the list of comparison method. Figure 7 also describes the overall procedure of each method.

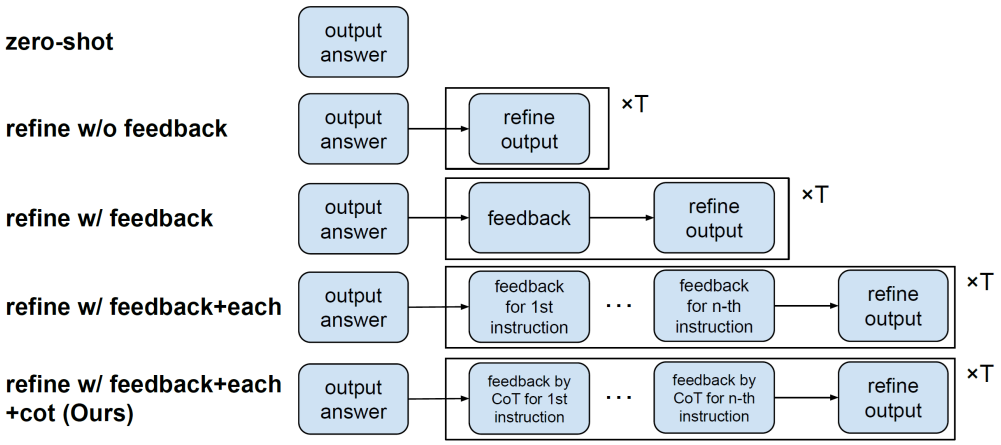

Figure 7: Method Comparison

- **zero-shot**: sets a task description and multiple instructions in a prompt and let the models generate an answer. See Section 4.2.
- **refinement w/o feedback**: self-refines the initial output T times (a predetermined number of iterations) after the initial output.
- **refinement w/ feedback**: self-refines the initial output based on a feedback. In the feedback, the LLM itself evaluates whether the output text complies with each instruction. This feedback and refinement process is repeated T times.
- **refinement w/ feedback+each**: self-refines the initial output based on a feedback similar to "refinement w/o zero-shot", but this method gives feedback by reseting the prompt for each instruction. In other words, this method runs the LLM for the number of times as many as instructions to obtain feedbacks for each instruction.
- **refinement w/ feedback+each+cot (our method)**: See Section 5.1. Our method is regarded as self-refinement by self-feedback for each instructions using Zero-shot-CoT.

The performance comparison results are shown in Table 2 for GPT-4o and Claude 3.5 Sonnet. We confirmed that self-refinement and feedback-each are important contributors for the performance improvement. We also confirmed that the highest performance is achieved when all the components (self-refinement, self-feedback, Chain-of-Thought and feedback per instruction) are combined. Interestingly, just giving self-feedback does not improve the performance (See the performance change from "refinement w/o feedback" to "refinement w/ feedback"). This result indicates that the quality of self-feedback is important for the performance improvement. See Appendix D for the results of the other models.

5.3 Further Analysis

Based on the finding that the quality of self-feedback is important for the performance improvement, we further analyze what characteristics are important for the self-feedback. First, we conduct the following additional baseline experiments:

- **refinement w/ oracle**: uses an external oracle feedback mechanism that can precisely determine whether each instruction was successfully followed. Specifically, this method (1) generates an initial answer; (2) uses the oracle verifier to assess success or failure in following each instruction; (3) lists the instructions that were not followed and prompt the model to correct its answer accordingly. We repeat steps (2) and (3) for T times.
- **refinement w/ all false**: informs the model that it failed to follow all instructions. Specifically, this method (1) generates an initial answer; (2) prompt the model with all the instructions to inform the model that it failed to follow all the instructions and correct its answer accordingly. We repeats steps (2) for T times.

Table 2: Method comparison result on GPT-4o (Top) and Claude 3.5 Sonnet (Bottom). **Bold** means the best and underline means the second best score.

[GPT-4o]	**Prompt-level**	**Inst-level**	**Feedback Performance**		
Method	**Accuracy**	**Accuracy**	**Precision**	**Recall**	**F1 Score**
zero-shot	0.484	0.861	-	-	-
refinement w/o feedback	0.560	0.887	-	-	-
refinement w/ feedback	0.558	0.887	0.79	0.44	0.56
refinement w/ feedback+each	0.615	0.908	**0.84**	0.16	0.27
refinement w/ feedback+each+cot (**Ours**)	**0.621**	**0.909**	0.82	**0.76**	**0.79**
refinement w/ oracle	0.700	0.929	1.0	1.0	1.0
refinement w/ all false	0.613	0.905	1.0	0	0

[Claude 3.5]	**Prompt-level**	**Inst-level**	**Feedback Performance**		
Method	**Accuracy**	**Accuracy**	**Precision**	**Recall**	**F1 Score**
zero-shot	0.683	0.925	-	-	-
refinement w/o feedback	0.709	0.936	-	-	-
refinement w/ feedback	0.703	0.935	0.66	**0.96**	0.78
refinement w/ feedback+each	0.725	0.939	0.70	0.72	0.71
refinement w/ feedback+each+cot (**Ours**)	**0.758**	**0.949**	**0.77**	0.94	**0.85**
refinement w/ oracle	0.853	0.967	1.0	1.0	1.0
refinement w/ all false	0.792	0.955	1.0	0	0

The result is shown at the bottom sides of Table 2. When correct feedback is provided, answer correction leads to substantial improvements in instruction-following performance (refinement w/ oracle). Even when using "all false" feedback—informing the model that it failed to follow all instructions—performance improvement was observed, though not as significant as oracle feedback.

Based on the result, we make the following hypothesis: It is better to pick up all the instructions that are not being followed, even though the prediction includes mistakes, than to overlook the instructions that are not being followed. Here we define the confusion matrix of self-feedback prediction as follows. False-positive: mistakenly judging an instruction that is being followed as not being followed. False-negative: mistakenly judging an instruction that is not being followed as being followed. Based on this definition of the confusion matrix, we calculate precision, recall, and F1 score for each method. The result is shown at the right sides of Table 2. This result demonstrates that instruction-following performance has strong relationship with the precision: As the precision becomes higher, accuracy of the method tends to become high. This observation indicates that our hypothesis is correct. See Appendix E for the detail of the confusion matrix of some models.

6 CONCLUSION AND FUTURE WORK

We hava introduced ManyIFEval, a large-scale benchmark dataset comprising task prompts with up to ten objectively verifiable instructions. We conducted experiments based on ManyIFEval with various models, demonstrating that as the instruction count rises, the models' ability to follow individual instruction deteriorates gradually but constantly. As a result, the models' ability to follow all the instructions significantly drops by the "curse of instructions". To remove the curse without retraining models, we proposed a inference-time method that enhances performance through iterative self-refinement by feedback with instruction-level chain-of-thought reasoning. Our Experiments showed that our method drastically improved the performance of following multiple instructions.

It is important to note that the instructions used in our study were designed to be simple and allowed for objective, binary evaluations of success or failure in instruction following. These instructions did not encompass more abstract or nuanced directives, such as those found in legal texts, where judgments may have gradations and are less clear-cut. Addressing the challenges posed by such complex instructions remains an area for future work. Developing methods for LLMs to handle abstract instructions with subjective success criteria will be crucial for advancing their applicability in real-world scenarios that demand nuanced understanding and interpretation.

REFERENCES

Anthropic. Claude 3.5 sonnet, 2024. URL https://www.anthropic.com/news/claude-3-5-sonnet.

Bradley Brown, Jordan Juravsky, Ryan Ehrlich, Ronald Clark, Quoc V. Le, Christopher Ré, and Azalia Mirhoseini. Large language monkeys: Scaling inference compute with repeated sampling, 2024. URL https://arxiv.org/abs/2407.21787.

Tom Brown, Benjamin Mann, Nick Ryder, Melanie Subbiah, Jared D Kaplan, Prafulla Dhariwal, Arvind Neelakantan, Pranav Shyam, Girish Sastry, Amanda Askell, Sandhini Agarwal, Ariel Herbert-Voss, Gretchen Krueger, Tom Henighan, Rewon Child, Aditya Ramesh, Daniel Ziegler, Jeffrey Wu, Clemens Winter, Chris Hesse, Mark Chen, Eric Sigler, Mateusz Litwin, Scott Gray, Benjamin Chess, Jack Clark, Christopher Berner, Sam McCandlish, Alec Radford, Ilya Sutskever, and Dario Amodei. Language models are few-shot learners. In H. Larochelle, M. Ranzato, R. Hadsell, M.F. Balcan, and H. Lin (eds.), *Advances in Neural Information Processing Systems*, volume 33, pp. 1877–1901. Curran Associates, Inc., 2020. URL https://proceedings.neurips.cc/paper_files/paper/2020/file/1457c0d6bfcb4967418bfb8ac142f64a-Paper.pdf.

Hyung Won Chung, Le Hou, Shayne Longpre, Barret Zoph, Yi Tay, William Fedus, Yunxuan Li, Xuezhi Wang, Mostafa Dehghani, Siddhartha Brahma, Albert Webson, Shixiang Shane Gu, Zhuyun Dai, Mirac Suzgun, Xinyun Chen, Aakanksha Chowdhery, Alex Castro-Ros, Marie Pellat, Kevin Robinson, Dasha Valter, Sharan Narang, Gaurav Mishra, Adams Yu, Vincent Zhao, Yanping Huang, Andrew Dai, Hongkun Yu, Slav Petrov, Ed H. Chi, Jeff Dean, Jacob Devlin, Adam Roberts, Denny Zhou, Quoc V. Le, and Jason Wei. Scaling instruction-finetuned language models. *Journal of Machine Learning Research*, 25(70):1–53, 2024. URL http://jmlr.org/papers/v25/23-0870.html.

Mike Conover, Matt Hayes, Ankit Mathur, Jianwei Xie, Jun Wan, Sam Shah, Ali Ghodsi, Patrick Wendell, Matei Zaharia, and Reynold Xin. Free dolly: Introducing the world's first truly open instruction-tuned llm, 2023. URL https://www.databricks.com/blog/2023/04/12/dolly-first-open-commercially-viable-instruction-tuned-llm.

Gemini Team. Gemini 1.5: Unlocking multimodal understanding across millions of tokens of context, 2024. URL https://arxiv.org/abs/2403.05530.

Gemma Team. Gemma 2: Improving open language models at a practical size, 2024. URL https://arxiv.org/abs/2408.00118.

Google. Palm 2 technical report, 2023. URL https://arxiv.org/abs/2305.10403.

Neel Guha, Julian Nyarko, Daniel E. Ho, Christopher Ré, Adam Chilton, Aditya Narayana, Alex Chohlas-Wood, Austin Peters, Brandon Waldon, Daniel N. Rockmore, Diego Zambrano, Dmitry Talisman, Enam Hoque, Faiz Surani, Frank Fagan, Galit Sarfaty, Gregory M. Dickinson, Haggai Porat, Jason Hegland, Jessica Wu, Joe Nudell, Joel Niklaus, John Nay, Jonathan H. Choi, Kevin Tobia, Margaret Hagan, Megan Ma, Michael Livermore, Nikon Rasumov-Rahe, Nils Holzenberger, Noam Kolt, Peter Henderson, Sean Rehaag, Sharad Goel, Shang Gao, Spencer Williams, Sunny Gandhi, Tom Zur, Varun Iyer, and Zehua Li. Legalbench: A collaboratively built benchmark for measuring legal reasoning in large language models, 2023. URL https://arxiv.org/abs/2308.11462.

Paul Hager, Friederike Jungmann, Robbie Holland, Kunal Bhagat, Inga Hubrecht, Manuel Knauer, Jakob Vielhauer, Marcus Makowski, Rickmer Braren, Georgios Kaissis, and Daniel Rueckert. Evaluation and mitigation of the limitations of large language models in clinical decision-making. *Nature Medicine*, 30(9):2613–2622, Sep 2024. ISSN 1546-170X. doi: 10.1038/s41591-024-03097-1. URL https://doi.org/10.1038/s41591-024-03097-1.

Shirley Anugrah Hayati, Taehee Jung, Tristan Bodding-Long, Sudipta Kar, Abhinav Sethy, Joo-Kyung Kim, and Dongyeop Kang. Chain-of-instructions: Compositional instruction tuning on large language models, 2024. URL https://arxiv.org/abs/2402.11532.

Qianyu He, Jie Zeng, Qianxi He, Jiaqing Liang, and Yanghua Xiao. From complex to simple: Enhancing multi-constraint complex instruction following ability of large language models. *arXiv preprint arXiv:2404.15846*, 2024a.

Qianyu He, Jie Zeng, Wenhao Huang, Lina Chen, Jin Xiao, Qianxi He, Xunzhe Zhou, Jiaqing Liang, and Yanghua Xiao. Can large language models understand real-world complex instructions? In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 38, pp. 18188–18196, 2024b.

Yuxin Jiang, Yufei Wang, Xingshan Zeng, Wanjun Zhong, Liangyou Li, Fei Mi, Lifeng Shang, Xin Jiang, Qun Liu, and Wei Wang. FollowBench: A multi-level fine-grained constraints following benchmark for large language models. In Lun-Wei Ku, Andre Martins, and Vivek Srikumar (eds.), *Proceedings of the 62nd Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers)*, pp. 4667–4688, Bangkok, Thailand, August 2024. Association for Computational Linguistics. URL https://aclanthology.org/2024.acl-long.257.

Jungo Kasai, Yuhei Kasai, Keisuke Sakaguchi, Yutaro Yamada, and Dragomir Radev. Evaluating gpt-4 and chatgpt on japanese medical licensing examinations, 2023. URL https://arxiv.org/abs/2303.18027.

Takeshi Kojima, Shixiang (Shane) Gu, Machel Reid, Yutaka Matsuo, and Yusuke Iwasawa. Large language models are zero-shot reasoners. In S. Koyejo, S. Mohamed, A. Agarwal, D. Belgrave, K. Cho, and A. Oh (eds.), *Advances in Neural Information Processing Systems*, volume 35, pp. 22199–22213. Curran Associates, Inc., 2022. URL https://proceedings.neurips.cc/paper_files/paper/2022/file/8bb0d291acd4acf06ef112099c16f326-Paper-Conference.pdf.

Woosuk Kwon, Zhuohan Li, Siyuan Zhuang, Ying Sheng, Lianmin Zheng, Cody Hao Yu, Joseph E. Gonzalez, Hao Zhang, and Ion Stoica. Efficient memory management for large language model serving with pagedattention. In *Proceedings of the ACM SIGOPS 29th Symposium on Operating Systems Principles*, 2023.

Mosh Levy, Alon Jacoby, and Yoav Goldberg. Same task, more tokens: the impact of input length on the reasoning performance of large language models. In Lun-Wei Ku, Andre Martins, and Vivek Srikumar (eds.), *Proceedings of the 62nd Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers)*, pp. 15339–15353, Bangkok, Thailand, August 2024. Association for Computational Linguistics. URL https://aclanthology.org/2024.acl-long.818.

Xuechen Li, Tianyi Zhang, Yann Dubois, Rohan Taori, Ishaan Gulrajani, Carlos Guestrin, Percy Liang, and Tatsunori B. Hashimoto. Alpacaeval: An automatic evaluator of instruction-following models. https://github.com/tatsu-lab/alpaca_eval, 5 2023.

Nelson F. Liu, Kevin Lin, John Hewitt, Ashwin Paranjape, Michele Bevilacqua, Fabio Petroni, and Percy Liang. Lost in the middle: How language models use long contexts. *Transactions of the Association for Computational Linguistics*, 12:157–173, 2024. doi: 10.1162/tacl_a_00638. URL https://aclanthology.org/2024.tacl-1.9.

Yang Liu, Dan Iter, Yichong Xu, Shuohang Wang, Ruochen Xu, and Chenguang Zhu. G-eval: NLG evaluation using gpt-4 with better human alignment. In Houda Bouamor, Juan Pino, and Kalika Bali (eds.), *Proceedings of the 2023 Conference on Empirical Methods in Natural Language Processing*, pp. 2511–2522, Singapore, December 2023. Association for Computational Linguistics. doi: 10.18653/v1/2023.emnlp-main.153. URL https://aclanthology.org/2023.emnlp-main.153.

Llama Team. The llama 3 herd of models, 2024. URL https://arxiv.org/abs/2407.21783.

Aman Madaan, Niket Tandon, Prakhar Gupta, Skyler Hallinan, Luyu Gao, Sarah Wiegreffe, Uri Alon, Nouha Dziri, Shrimai Prabhumoye, Yiming Yang, Shashank Gupta, Bodhisattwa Prasad Majumder, Katherine Hermann, Sean Welleck, Amir Yazdanbakhsh, and

Peter Clark. Self-refine: Iterative refinement with self-feedback. In A. Oh, T. Naumann, A. Globerson, K. Saenko, M. Hardt, and S. Levine (eds.), *Advances in Neural Information Processing Systems*, volume 36, pp. 46534–46594. Curran Associates, Inc., 2023. URL https://proceedings.neurips.cc/paper_files/paper/2023/file/91edff07232fb1b55a505a9e9f6c0ff3-Paper-Conference.pdf.

OpenAI. Gpt-4o system card, 2024a. URL https://openai.com/index/gpt-4o-system-card/.

OpenAI. Gpt-4 technical report, 2024b. URL https://arxiv.org/abs/2303.08774.

Pranab Sahoo, Ayush Kumar Singh, Sriparna Saha, Vinija Jain, Samrat Mondal, and Aman Chadha. A systematic survey of prompt engineering in large language models: Techniques and applications. *arXiv preprint arXiv:2402.07927*, 2024.

Chenhui Shen, Liying Cheng, Xuan-Phi Nguyen, Yang You, and Lidong Bing. Large language models are not yet human-level evaluators for abstractive summarization. In Houda Bouamor, Juan Pino, and Kalika Bali (eds.), *Findings of the Association for Computational Linguistics: EMNLP 2023*, pp. 4215–4233, Singapore, December 2023. Association for Computational Linguistics. doi: 10.18653/v1/2023.findings-emnlp.278. URL https://aclanthology.org/2023.findings-emnlp.278.

Karan Singhal, Shekoofeh Azizi, Tao Tu, S. Sara Mahdavi, Jason Wei, Hyung Won Chung, Nathan Scales, Ajay Tanwani, Heather Cole-Lewis, Stephen Pfohl, Perry Payne, Martin Seneviratne, Paul Gamble, Chris Kelly, Abubakr Babiker, Nathanael Schärli, Aakanksha Chowdhery, Philip Mansfield, Dina Demner-Fushman, Blaise Agüera y Arcas, Dale Webster, Greg S. Corrado, Yossi Matias, Katherine Chou, Juraj Gottweis, Nenad Tomasev, Yun Liu, Alvin Rajkomar, Joelle Barral, Christopher Semturs, Alan Karthikesalingam, and Vivek Natarajan. Large language models encode clinical knowledge. *Nature*, 620(7972):172–180, Aug 2023. ISSN 1476-4687. doi: 10.1038/s41586-023-06291-2. URL https://doi.org/10.1038/s41586-023-06291-2.

Rohan Taori, Ishaan Gulrajani, Tianyi Zhang, Yann Dubois, Xuechen Li, Carlos Guestrin, Percy Liang, and Tatsunori B. Hashimoto. Stanford alpaca: An instruction-following llama model. https://github.com/tatsu-lab/stanford_alpaca, 2023.

Shubham Vatsal and Harsh Dubey. A survey of prompt engineering methods in large language models for different nlp tasks. *arXiv preprint arXiv:2407.12994*, 2024.

Xuezhi Wang, Jason Wei, Dale Schuurmans, Quoc Le, Ed Chi, Sharan Narang, Aakanksha Chowdhery, and Denny Zhou. Self-consistency improves chain of thought reasoning in language models. *arXiv preprint arXiv:2203.11171*, 2022a.

Yizhong Wang, Swaroop Mishra, Pegah Alipoormolabashi, Yeganeh Kordi, Amirreza Mirzaei, Atharva Naik, Arjun Ashok, Arut Selvan Dhanasekaran, Anjana Arunkumar, David Stap, Eshaan Pathak, Giannis Karamanolakis, Haizhi Lai, Ishan Purohit, Ishani Mondal, Jacob Anderson, Kirby Kuznia, Krima Doshi, Kuntal Kumar Pal, Maitreya Patel, Mehrad Moradshahi, Mihir Parmar, Mirali Purohit, Neeraj Varshney, Phani Rohitha Kaza, Pulkit Verma, Ravsehaj Singh Puri, Rushang Karia, Savan Doshi, Shailaja Keyur Sampat, Siddhartha Mishra, Sujan Reddy A, Sumanta Patro, Tanay Dixit, and Xudong Shen. Super-NaturalInstructions: Generalization via declarative instructions on 1600+ NLP tasks. In Yoav Goldberg, Zornitsa Kozareva, and Yue Zhang (eds.), *Proceedings of the 2022 Conference on Empirical Methods in Natural Language Processing*, pp. 5085–5109, Abu Dhabi, United Arab Emirates, December 2022b. Association for Computational Linguistics. doi: 10.18653/v1/2022.emnlp-main.340. URL https://aclanthology.org/2022.emnlp-main.340.

Jason Wei, Maarten Bosma, Vincent Zhao, Kelvin Guu, Adams Wei Yu, Brian Lester, Nan Du, Andrew M. Dai, and Quoc V Le. Finetuned language models are zero-shot learners. In *International Conference on Learning Representations*, 2022a. URL https://openreview.net/forum?id=gEZrGCozdqR.

Jason Wei, Xuezhi Wang, Dale Schuurmans, Maarten Bosma, brian ichter, Fei Xia, Ed Chi, Quoc V Le, and Denny Zhou. Chain-of-thought prompting elicits reasoning in large language models.

In S. Koyejo, S. Mohamed, A. Agarwal, D. Belgrave, K. Cho, and A. Oh (eds.), *Advances in Neural Information Processing Systems*, volume 35, pp. 24824–24837. Curran Associates, Inc., 2022b. URL https://proceedings.neurips.cc/paper_files/paper/2022/file/9d5609613524ecf4f15af0f7b31abca4-Paper-Conference.pdf.

Sean Welleck, Amanda Bertsch, Matthew Finlayson, Hailey Schoelkopf, Alex Xie, Graham Neubig, Ilia Kulikov, and Zaid Harchaoui. From decoding to meta-generation: Inference-time algorithms for large language models, 2024. URL https://arxiv.org/abs/2406.16838.

Thomas Wolf, Lysandre Debut, Victor Sanh, Julien Chaumond, Clement Delangue, Anthony Moi, Pierric Cistac, Tim Rault, Rémi Louf, Morgan Funtowicz, Joe Davison, Sam Shleifer, Patrick von Platen, Clara Ma, Yacine Jernite, Julien Plu, Canwen Xu, Teven Le Scao, Sylvain Gugger, Mariama Drame, Quentin Lhoest, and Alexander M. Rush. Transformers: State-of-the-art natural language processing. In *Proceedings of the 2020 Conference on Empirical Methods in Natural Language Processing: System Demonstrations*, pp. 38–45, Online, October 2020. Association for Computational Linguistics. URL https://www.aclweb.org/anthology/2020.emnlp-demos.6.

Can Xu, Qingfeng Sun, Kai Zheng, Xiubo Geng, Pu Zhao, Jiazhan Feng, Chongyang Tao, and Daxin Jiang. Wizardlm: Empowering large language models to follow complex instructions. *arXiv preprint arXiv:2304.12244*, 2023.

Shengyu Zhang, Linfeng Dong, Xiaoya Li, Sen Zhang, Xiaofei Sun, Shuhe Wang, Jiwei Li, Runyi Hu, Tianwei Zhang, Fei Wu, et al. Instruction tuning for large language models: A survey. *arXiv preprint arXiv:2308.10792*, 2023.

Tianyi Zhang, Varsha Kishore, Felix Wu, Kilian Q. Weinberger, and Yoav Artzi. Bertscore: Evaluating text generation with bert. In *International Conference on Learning Representations*, 2020. URL https://openreview.net/forum?id=SkeHuCVFDr.

Lianmin Zheng, Wei-Lin Chiang, Ying Sheng, Siyuan Zhuang, Zhanghao Wu, Yonghao Zhuang, Zi Lin, Zhuohan Li, Dacheng Li, Eric Xing, Hao Zhang, Joseph E. Gonzalez, and Ion Stoica. Judging LLM-as-a-judge with MT-bench and chatbot arena. In *Thirty-seventh Conference on Neural Information Processing Systems Datasets and Benchmarks Track*, 2023. URL https://openreview.net/forum?id=uccHPGDlao.

Jeffrey Zhou, Tianjian Lu, Swaroop Mishra, Siddhartha Brahma, Sujoy Basu, Yi Luan, Denny Zhou, and Le Hou. Instruction-following evaluation for large language models. *arXiv preprint arXiv:2311.07911*, 2023a.

Jeffrey Zhou, Tianjian Lu, Swaroop Mishra, Siddhartha Brahma, Sujoy Basu, Yi Luan, Denny Zhou, and Le Hou. Instruction-following evaluation for large language models, 2023b. URL https://arxiv.org/abs/2311.07911.

Appendix

A STATISTICS OF MANYIFEVAL.

Table 3 describes Statistics of ManyIFEval.

Table 3: A overview of ManyIFEval.

#Samples	#Prompts	Avg. Len (word)
1000	100	92.3

B INSTRUCTIONS IN MANYIFEVAL

Table 4 summarizes a list of Instructions in ManyIFEval.

Table 4: The list of 15 verifiable instructions, with brief descriptions from IFEval paper and Inst-level accuracy by gpt-4o-2024-05-13.

Instruction Group	Instruction	Description	Inst-level acc
Keywords	Include Keywords	Include keywords {keyword1}, {keyword2} in your response.	98%
Keywords	Keyword Frequency	In your response, the word should appear N times.	96%
Keywords	Forbidden Words	Do not include keywords (forbidden words) in the response.	95%
Keywords	Letter Frequency	In your response, the letter {letter} should appear N times.	62%
Length Constraints	Number Paragraphs	Your response should contain N paragraphs. You separate paragraphs using the markdown divider \\.	87%
Length Constraints	Number Words	Answer with at least/around/at most N words.	81%
Length Constraints	Number Sentences	Answer with at least/around/at most N sentences.	73%
Detectable Content	Number Placeholder	The response must contain at least N placeholders represented by square brackets, such as [address].	95%
Detectable Format	Number Bullets	Your answer must contain exactly N bullet points. Use the markdown bullet points such as `- This is a point.`	88%
Detectable Format	Title	Your answer must contain a title, wrapped in double quotation marks, such as "{title of your response}."	100%
Change Cases	All Uppercase	Your entire response should be in English, and all capital letters only.	97%
Change Cases	All Lowercase	Your entire response should be in English, and in all lowercase letters.	97%
Change Cases	Frequency of all-capital words	In your response, words in all capital letters should appear at least/around/at most N times.	87%
Start with / End with	Quotation	Wrap your entire response with double quotation marks.	100%
Punctuation	No Commas	In your entire response, refrain from the use of any commas.	100%

C EFFECT OF MULTIPLE UNIQUE INSTRUCTIONS ON PERFORMANCE

Previous studies have shown that increasing the input token length can negatively impact a model's reasoning capabilities (Levy et al., 2024; Liu et al., 2024). To determine whether the observed degradation was due to the increased number of instructions or simply the longer input sequences, we conducted an experiment where we repeated the same instructions to match the input length of prompts with multiple unique instructions. By measuring instruction-following performance with repeated instructions, we isolated the effect of input length from the effect of instruction variety. As shown in Figure 8, the degradation in performance with repeated instructions was less severe compared to when the number of unique instructions increased. In some cases, models even demonstrated improved instruction-following when instructions were repeated. These findings suggest that the negative impact on instruction-following performance is more attributable to the increased number of unique instructions rather than the overall input length, highlighting a limitation in the models' capacity to handle multiple instructions simultaneously.

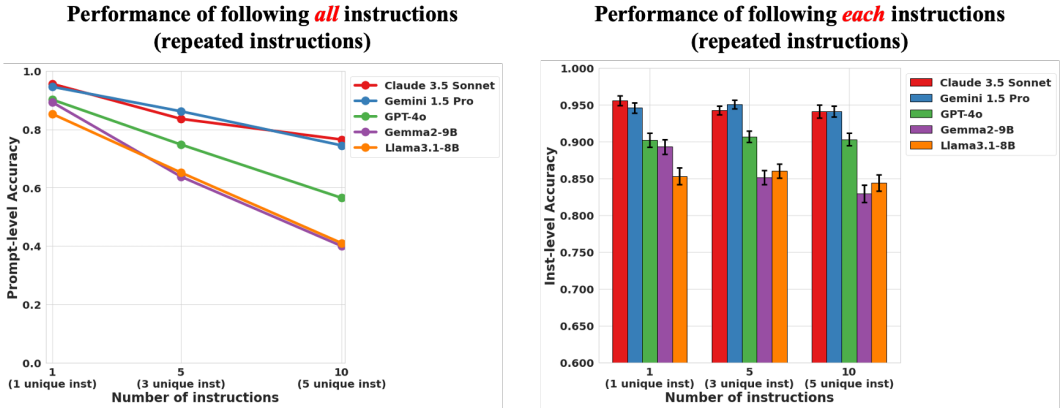

Figure 8: Multiple unique instructions affect performance.

D ADDITIONAL EXPERIMENT RESULTS ON METHOD COMPARISON

Table 5 describes additional experiment results on method comparison.

Table 5: Result of Gemini 1.5 Pro. **Bold** means the best and underline means the second best score.

Method	Prompt-level Accuracy	Inst-level Accuracy	Feedback Performance		
			Precision	Recall	F1 Score
zero-shot	0.677	0.928	-	-	-
refinement w/o feedback	0.648	0.913	-	-	-
refinement w/ feedback	0.677	0.927	0.58	0.62	0.60
refinement w/ feedback+each	**0.692**	**0.929**	**0.92**	0.12	0.21
refinement w/ feedback+each+cot (**Ours**)	0.678	0.928	0.85	**0.63**	**0.72**
refinement w/ oracle	0.763	0.945	1.0	1.0	1.0
refinement w/ all false	0.730	0.940	1.0	0	0

E CONFUSION MATRIX OF ZERO-SHOT-COT-EACH.

Figure 9 describes a confusion matrix of zero-shot-cot-each method. The result shows that zero-shot-cot-each is a high precision approach.

zero-shot-cot Recall is high		Prediction	
		following	
		TRUE	FALSE
Label: following	TRUE	98	2
	FALSE	65	35

zero-shot-cot-each Precision is high		Prediction	
		following	
		TRUE	FALSE
Label: following	TRUE	76	24
	FALSE	17	83

Figure 9: zero-shot-cot-each is high precision approach.

F THE DETAIL EXPERIMENT RESULT OF CURSE OF INSTRUCTIONS

Figure 10 describes the detail experiment result of curse of instructions.

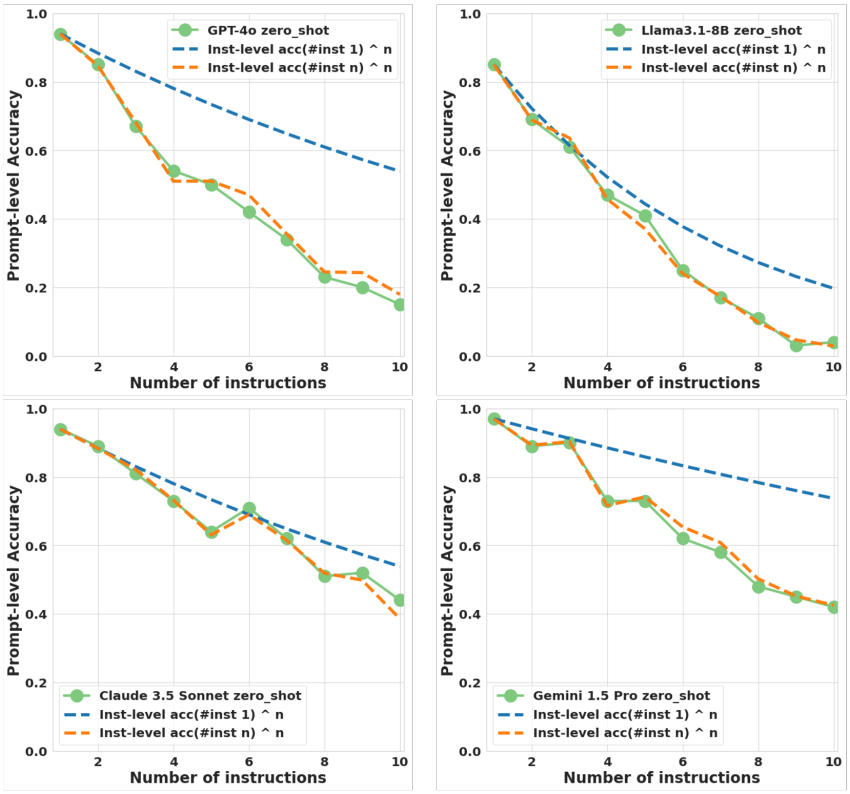

Figure 10: As the number of instructions increases, the models' ability to follow individual instruction deteriorates gradually but constantly. As a result, the models' ability to follow all the instructions significantly drops: the success rate of all the instructions is precisely explained by the success rate of individual instructions to the power of total number of instructions.

G EXAMPLE OF GENERATION

Table 6 and Table 7 describes Examples of prompts and LLMs' response for each method.

Table 6: Example response of GPT-4o zero-shot for 10 instructions. Red text indicates instructions that are not being followed.

Example response of GPT-4o zero-shot for 10 instructions	
Prompt	Are the weather conditions in the Arctic very cold most of the year? Your response should follow the instructions below: - The response must contain at least 3 placeholders represented by square brackets, such as [address]. - Your answer must contain exactly 2 bullet points. Use the markdown bullet points such as: * This is point 1. * This is point 2 - Wrap your entire response with double quotation marks. - In your response, the word fail should appear less than 2 times. - In your response, the letter b should appear less than 8 times. - Your answer must contain a title, wrapped in double angular brackets, such as <<poem of joy>>. - In your response, words with all capital letters should appear at least 14 times. - In your entire response, refrain from the use of any commas. - There should be 2 paragraphs. Paragraphs are separated with the markdown divider: *** - Do not include keywords ['no', 'yes'] in the response.
Response	"<<ARCTIC WEATHER CONDITIONS>>" "The weather conditions in the Arctic are EXTREMELY COLD for most of the year. The region experiences long periods of DARKNESS during the winter months which contributes to the FRIGID temperatures. The average temperature in the Arctic can drop to as low as [temperature] degrees Fahrenheit during the winter. *** * The summer months in the Arctic are SHORT and the temperatures rarely rise above [temperature] degrees Fahrenheit. Even during this time the weather can be quite CHILLY. The ARCTIC is known for its ICE and SNOW which cover the landscape for the majority of the year. The harsh conditions make it a CHALLENGING environment for both humans and wildlife."

Table 7: Example response of GPT-4o feedback+cot+each for 10 instructions. All instructions are followed by feedback+each+cot.

Example response of GPT-4o feedback+cot+each for 10 instructions	
Prompt	Are the weather conditions in the Arctic very cold most of the year? Your response should follow the instructions below: - The response must contain at least 3 placeholders represented by square brackets, such as [address]. - Your answer must contain exactly 2 bullet points. Use the markdown bullet points such as: * This is point 1. * This is point 2 - Wrap your entire response with double quotation marks. - In your response, the word fail should appear less than 2 times. - In your response, the letter b should appear less than 8 times. - Your answer must contain a title, wrapped in double angular brackets, such as <<poem of joy>>. - In your response, words with all capital letters should appear at least 14 times. - In your entire response, refrain from the use of any commas. - There should be 2 paragraphs. Paragraphs are separated with the markdown divider: *** - Do not include keywords ['no', 'yes'] in the response.
Response	"<<ARCTIC WEATHER CONDITIONS>>" "The weather conditions in the Arctic are EXTREMELY COLD for most of the year. The region experiences LONG WINTERS with temperatures often dropping to EXTREMELY LOW levels. During the summer months the temperatures may rise slightly but they remain quite chilly compared to other regions like [location1]. The EXTREME COLD can be quite UNFORGIVING. *** * The Arctic is known for its HARSH CLIMATE which includes STRONG WINDS and HEAVY SNOWFALL. This makes [activity1] particularly challenging. The EXTREME COLD and STRONG WINDS can make it difficult to perform even simple tasks. * Due to the EXTREME COLD and ISOLATED LOCATION the Arctic is a challenging environment for both humans and wildlife. The conditions can be quite UNFORGIVING and require SPECIALIZED EQUIPMENT and clothing to navigate safely. For instance [item1] is essential for survival in the EXTREME COLD. Overall the Arctic's weather is characterized by its EXTREME COLD and LONG WINTERS making it a unique and challenging environment."