SURPRISING EFFECTIVENESS OF PRETRAINING TERNARY LANGUAGE MODELS AT SCALE

Anonymous authors
Paper under double-blind review

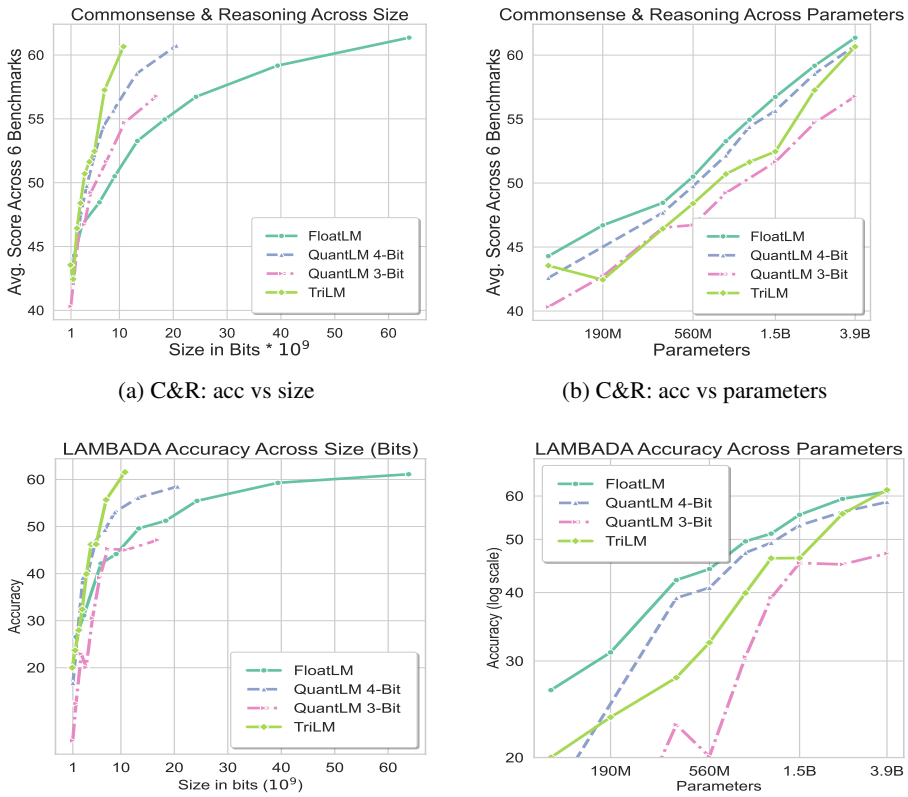
ABSTRACT

Rapid advancements in GPU computational power has outpaced memory capacity and bandwidth growth, creating bottlenecks in Large Language Model (LLM) inference. Post-training quantization is the leading method for addressing memory-related bottlenecks in LLM inference, but it suffers from significant performance degradation below 4-bit precision. This paper addresses these challenges by investigating the pretraining of low-bitwidth models specifically *Ternary Language Models (TriLMs)* as an alternative to traditional floating-point models (FloatLMs) and their post-training quantized versions (QuantLMs). We present *Spectra LLM suite*, the first open suite of LLMs spanning multiple bit-widths, including FloatLMs, QuantLMs, and TriLMs, ranging from 99M to 3.9B parameters trained on 300B tokens. Our comprehensive evaluation demonstrates that TriLMs offer superior scaling behavior in terms of model size (in bits). Surprisingly, at scales exceeding one billion parameters, TriLMs consistently outperform their QuantLM and FloatLM counterparts for a given bit size across various benchmarks. Notably, the 3.9B parameter TriLM matches the performance of the FloatLM 3.9B across all benchmarks, despite having fewer bits than FloatLM 830M. Overall, this research provides valuable insights into the feasibility and scalability of low-bitwidth language models, paving the way for the development of more efficient LLMs.

1 INTRODUCTION

The computational power of GPUs, measured in FLOPs, is increasing exponentially, doubling approximately every 1.26 years. In contrast, memory capacity and bandwidth are growing at a slower pace, doubling every 2 and 2.9 years, respectively (Gholami et al., 2024). This disparity highlights that computing capabilities are outpacing advances in memory technology. In Large Language Models (LLMs) inference, the primary bottlenecks are caused by model size (bits), which affects memory usage (memory capacity) and data transfer to processors (memory bandwidth). These issues are becoming more critical than the growing number of model parameters which affect the computational limits (FLOPs). For instance, state-of-the-art LLMs such as 340B Nemotron 4 (Nvidia et al., 2024) have sizes (in bits) exceeding the memory capacity of data center GPUs, such as 8xH100s. Token generation speed, or latency, is now limited by memory bandwidth (Kim et al., 2024). Addressing these bottlenecks requires more expensive training, exceeding Chinchilla's compute-optimal regime (Hoffmann et al., 2022), with less than 10B parameter models being trained on up to 15 trillion tokens (Touvron et al., 2023b; AI@Meta, 2024; Team et al., 2024). Another widely used technique is post-training quantization during deployment (Zhu et al., 2023); however, we demonstrate in Section 5 that this approach is sub-optimal.

In post-training quantization, LLMs initially trained using 16-bit floating point precision (referred to as FloatLMs) undergo parameter quantization, and the resulting models are termed QuantLMs. These models use optimized kernels for deployment, offering speedups nearly proportional to the compression factor (Frantar & Alistarh, 2024). However, quantizing to very low bitwidths creates a significant mismatch between the representations of pretrained FloatLM and the deployable QuantLM, resulting in undesired behavior and quality degradation (Li et al., 2024; Huang et al., 2024). Some state-of-the-art methods (Frantar et al., 2022; Egiazarian et al., 2024) mitigate this issue by using calibration and re-training data from target domains; however, this approach increases sensitivity to the calibration data. For instance, seemingly simple choices, like whether to length-normalize the calibration data, can significantly impact QuantLM's performance (Malinovskii et al., 2024). Other



(a) C&R: acc vs size

(b) C&R: acc vs parameters

(c) LAMBADA: acc vs size

(d) LAMBADA: acc vs parameters

Figure 1: Common Sense and Reasoning (C&R) & LAMBADA Accuracy for ternary TriLM, FP16 FloatLM and quantized QuantLM models across different model sizes, in bits and number of parameters. C&R scores are averaged across 6 benchmarks. At 3B+ scales, TriLMs demonstrate better performance for their size than QuantLM and competitive performance to FloatLM of the same parameters. See Tables 7, 8 and 10 for details.

works have observed that QuantLM at 4 bits (4-bit QuantLMs) have about 65% lower knowledge capacity per parameter compared to trained and aligned FloatLMs (Allen-Zhu & Li, 2024).

An alternate approach to reducing model bitsize while maintaining parameter count involves training neural networks with low effective bitwidths (Zhou et al., 2018). This approach offers compression benefits beyond post-training quantization without its associated drawbacks. While low-bitwidth approaches typically employ binary (1-bit) or ternary quantization (1.58-bit), binary quantization generally underperforms compared to regular FP16 models (Liu et al., 2023a) (see Appendix B). In contrast, ternary modeling can match performance while significantly reducing memory requirements (as we demonstrate in section 5). Nevertheless, *the relative performance of pretrained low-bitwidth language models compared to QuantLMs across similar sizes (in bits) and similar parameter counts remains unclear*. This is a crucial unanswered question, given the high inference costs during the deployment of very large-scale LLMs. Moreover, *the training dynamics and scaling law of these low-bitwidth models are also poorly understood, partly due to the lack of publicly available systematic suites and associated comparative studies*.

Motivated by these challenges, we make the following contributions in this paper:

Feasibility and Scalability of Training Ternary Language Models (TriLMs) We discuss the deployment advantages (in section 2.1) and theoretical feasibility (in section 2.2) of training low-bitwidth models at scale. We then introduce ternary language models (TriLMs) and systematically study their scaling laws compared to FloatLMs. Our analysis reveals that TriLMs offer better scaling behavior in terms of model size, measured in bits (refer to Section 4.3). Moreover, as the number of parameters increases, the difference in validation loss between TriLMs and FloatLMs becomes insignificant, indicating TriLM's competitive performance at scale.

Spectra LLM suite. We present **Spectra**, the first open suite of LLMs spanning many bit-widths. This suite includes FloatLMs, the corresponding QuantLMs at 3, 4, 6, and 8 bits, and ternary LLMs (TriLMs). The latter uses ternary weights {-1, 0, +1}. The suite features 9 models ranging from 99M to 3.9B parameters, all trained on the same 300B token dataset, totalling 54 models. We believe that the Spectra LLM suite makes a valuable contribution to the LLM research community by facilitating comparative studies, exploring the scalability and efficiency of ternary modeling, and improving interpretability from neuronal to connection levels.

Evaluation and comparative analysis of TriLMs, FloatLMs, and QuantLMs at different scales. We evaluate TriLMs, FloatLMs, and QuantLMs across multiple benchmarks, spanning commonsense, reasoning, knowledge capacity and toxicity. At the billion parameter scale, TriLMs consistently outperform their QuantLM and FloatLM counterparts of the same bit-size across all the aforementioned benchmarks (see Figure 1). Surprisingly, TriLM 3.9B matches the performance of FloatLM 3.9B across all benchmarks, despite getting a higher perplexity and being 5.9 times smaller in bitsize.

However, we also note that certain challenges remain in TriLMs. For instance, TriLM 3.9B exhibits the same level of toxicity and stereotyping as FloatLM 3.9B, significantly higher than a similarly sized FloatLM 830M when measured in bits. While TriLM 3.9B and FloatLM 3.9B show similar validation perplexity on some datasets, such as Penn Tree Bank and Lambada, a gap persists at this scale on web corpora, both in-domain (i.e., on a test subset of SlimPajama, the same domain used to train the models) and out-of-domain (e.g., on Dolma, C4 and RefinedWeb datasets). We provide detailed perplexity results in the appendix D.4.

2 Motivation for Low-Bitwidt Models

2.1 Memory Bottlenecks and Language Model Deployment

Memory Capacity of GPGPUs and Model Size (in Bits): Figure 24a in Appendix G reveal that memory capacity has consistently lagged behind computational power across various accelerators, including recent hardware like Blackwell (Nvidia Team, 2024), MI325X (AMD Team, 2024), and Gaudi3 (Intel Gaudi Team, 2024). This gap is further exacerbated by advanced computational techniques like Ampere sparse or FP8. As shown in Figure 25a of Appendix G, the model sizes (in GB) for TriLM, QuantLM 4-Bit, and FloatLM scale differently with parameter counts. For simplicity, the figure excludes overhead from KV Cache, activations, and compilation during model deployment. FloatLM reaches the memory capacity of a single H100 at 34B parameters, with larger models exceeding the capacity of multiple GPUs. In contrast, QuantLM 4-Bit supports up to 300B parameters on a single MI300X. TriLMs, with over 300B parameters and appropriate packing, can fit on a single H100, making them not only efficient for GPU deployment but also ideal for edge devices.

Memory bandwidth of GPGPUs and model inference speedup: Figure 24b in Appendix G demonstrate the trends of Memory Bandwidth over FLOPs for accelerators over the years, highlighting the slower growth of memory bandwidth compared to computation. This trend, indicating a downward slope, aligns with Kim et al. (2024)'s establishment of the memory wall in autoregressive LLM computation. They found that the speed of token generation is bottlenecked by the rate at which data is fed from memory to processors, rather than the processing speed of the hardware. Consequently, the autoregressive decoding of LLM inference can theoretically achieve speedup proportional to its compression factor. Figure 25b in Appendix G illustrates the maximum possible speedup for QuantLM 4-Bit and TriLM compared to FP16 at different parameter counts. Even at 7 billion parameters, TriLMs can be more than 4 times faster at autoregressive decoding than FloatLM and 2 times faster than QuantLM 4-bit. While QuantLM 4-Bit plateaus at a maximum possible speedup factor of 4x, TriLMs plateau much higher at 10x for FloatLM.

2.2 Low bits can capture weight variance effectively at scale

In this section, we use information theory to support our hypothesis: *as the number of parameters increases, training language models with low-bitwidth can effectively capture the necessary weight*

variance without significant information loss. Assuming a fixed training dataset, we base this hypothesis on analyzing weight distributions in FloatLMs ranging from 99M to 3.9B parameters.

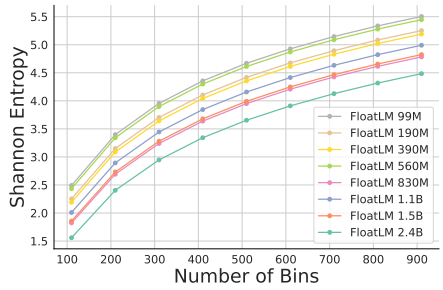


Figure 2: Shannon entropy (in bits) of discretized weight distribution with increasing number of bins.

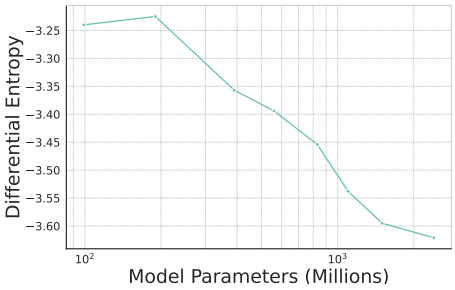


Figure 3: Differential entropy of Gaussian fits on weight distributions across different scales.

Assuming that the weights of a trained model follow a Gaussian distribution (see Appendix E), we fit a Gaussian to these weights to understand their statistical behavior across model scales. The differential entropy is calculated using the expression: $H(W) = \frac{1}{2}\log_2(2\pi e\sigma_W^2)$ where σ_W is the standard deviation of the weights (Papoulis & Pillai, 2002). As shown in Figure 3, differential entropy decreases with an increase in the number of parameters. This decrease indicates that the weights become more concentrated around the mean as the model size increases, suggesting higher predictability and less variability (MacKay, 2003). This reduced variability is due to overparameterization, which leads to redundancy in the weights Zhang et al. (2017); Neyshabur et al. (2018).

Additionally, we also use Shannon entropy, calculated by discretizing the weight distribution into (N) bins and computing $H_{Shannon} = -\sum_{i=1}^{N} p_i \log_2 p_i$, where p_i is the probability of the weights falling into the i-th bin. The probability is given by the normalized frequency of weights within each bin. Discretization allows us to apply discrete entropy measures to continuous data, with the number of bins determining the representation granularity. Shannon entropy measures the average minimum number of bits needed to encode the weight values based on their distribution, providing a quantifiable measure of their "information content" (Shannon, 1948). Lower Shannon entropy indicates a more predictable, less diverse distribution that can be effectively encoded using fewer bits. Examining Shannon entropy across scales and bin sizes, we validate our finding that larger models require fewer bits for effective representation. As plotted in Figure 2, there is a general trend of decreasing Shannon entropy with increasing parameter count for a given number of bins.

These analyses support the potential of low-bitwidth models to match full-precision performance, especially as model sizes grow. In Section 4.3, we further substantiate this by analyzing the scaling behavior of our low-bitwidth TriLMs compared to FloatLMs.

2.3 Selecting the Appropriate Low-Bitwidth Model

Selecting the appropriate quantization level is crucial for balancing computational efficiency and performance in low-bitwidth models. Binary models quantize weights to $\{-1, 1\}$, simplifying multiplications to efficient XOR operations (Courbariaux et al., 2016a), making them suitable for resource-constrained environments (Hubara et al., 2017). Ternary models introduce a zero state $\{-1, 0, +1\}$), replacing multiplications with additions and subtractions (Li et al., 2016), and improve efficiency by skipping calculations when weights are zero (Zhu et al., 2017). Conversely, models quantized to 2, 3, or 4 bits require more complex operations, including full multiplications, which are computationally more demanding than those required for binary and ternary models (Zhou et al., 2016). Therefore, this work only considers binary and ternary language models for further analysis.

The reduction in computational complexity in binary models often comes at the cost of significant performance degradation (Rastegari et al., 2016). In contrast, ternary quantization adds a zero state, better approximating weight distributions without significantly increasing computational demands (Li et al., 2016), making them a sweet spot for balancing performance with efficiency gains (Zhu et al., 2017). Our observations align with these, as the scaling trends for given data size for our TriLMs

consistently outperform those of BiLMs (Binary LLMs) across all parameter counts and bit sizes considered in this work, as shown in Appendix B and Figure 12. As a result, this work primarily focuses on the TriLM model, which we describe in the next section.

3 TriLM: Ternary Language Model

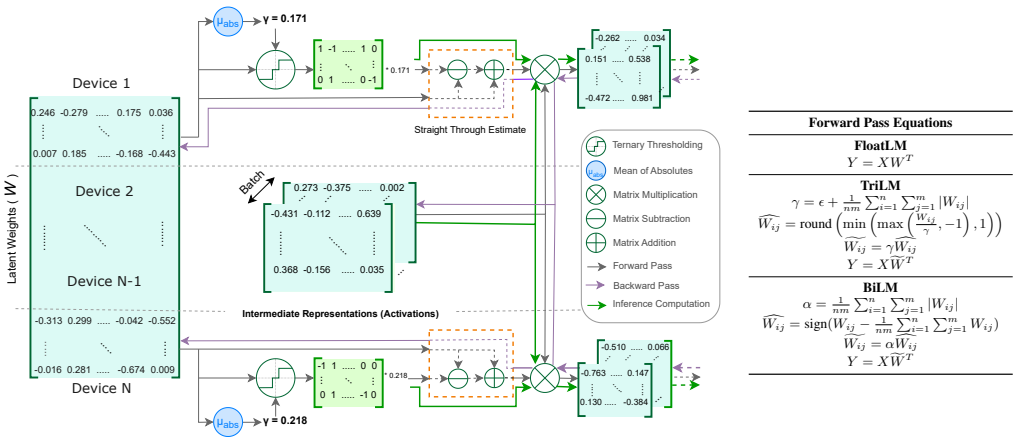


Figure 4: The computational flow of the forward, backward, and inference processes in TriLM's linear layer with N-Way model parallelism is shown on the left. Additionally, we provide the equations (on left) for the forward pass during the training of our FloatLM, TriLM, and BiLM (for details, see 1).

TriLM is a LLaMa-style (Touvron et al., 2023a) autoregressive transformers (Vaswani et al., 2017) model with RMSNorm (Zhang & Sennrich, 2019), SwiGLU Gated MLP (Shazeer, 2020), Rotary Position Embedding (RoPE) (Su et al., 2021), Multi-Headed Attention and no bias terms. In TriLMs, we represent the weights of all the linear layers in one of three possible ternary states $\{-1, 0, 1\}$, along with an additional floating-point number called 'scale value' shared across the matrix. During training, we maintain the *latent* (or master) weights in floating point precision, allowing for the accumulation of small updates over iterations that eventually contribute to a transition in the estimated ternary state of a parameter. As shown in Figure 4, during the forward pass, we ternarize the floating point latent weights on-the-fly. This process involves calculating the scale value to the absolute mean of the latent weights. After scaling, we estimate the ternary state of each parameter by rounding off to the nearest ternary state. In the backward pass, we use a straight-through estimator to compute gradients of the floating point latent weights (Bengio et al., 2013). Since we only need the scale values and the ternarized states during inference, we achieve a significant reduction in both model size and inference time at larger scales compared to FloatLMs. We provide a formal description of these forward pass, backward pass, and inference time equations in the Appendix (§A.1). We represent the embedding and language model head in half-precision floating point across all our experiments.

Since, training of TriLMs requires on-the-fly computation of scale values, synchronizing for a single scalar across devices in model parallel training (Shoeybi et al., 2019) can cause significant communication overhead. To address this, we allow each device to independently compute these scale values over its own matrix shard. This approach introduces additional artifacts, where the number of scalar values for each matrix is the same as the degree of model parallelism used during training (see appendix A.6). However, the impact on modelsize is negligible, for matrices with millions of parameters, we only add 6 scalar values each.

Concurrent research on low-bit LLMs, like BitNet 1.58 (Ma et al., 2024), also demonstrates the feasibility of training LLMs with ternary weights. Our experiments demonstrate that TriLM's architecture not only outperforms BitNet b1.58 but is also simpler and more stable. Moreover, both the larger BitNet 1.3B model presented in their paper and our replication of the BitNet 1.1B model underperform compared to our TriLM 1.1B on commonsense and reasoning benchmarks. We provide further details on these comparisons in Appendix A.7.

4 SPECTRA SUITE: SPANNING PARAMETERS AND BITWIDTHS

The Spectra suite includes comprehensive families of large language models designed to span different parameter counts and bit-widths. This suite includes three main model families: *TriLMs*, *FloatLMs*, and *QuantLMs* (3, 4, 6, and 8 bits). Drawing inspiration from established model suites such as those by Biderman et al. (2023), Liu et al. (2023c), and Groeneveld et al. (2024), Spectra aims to facilitate scientific research on low-bitwidth LLMs, interpretability, and safety.

4.1 OVERVIEW OF SPECTRA SUITE

The spectra suite of LLMs is distinguished by several key attributes listed below.

1. **Scale.** The open suite spans a broad spectrum of scales across parameter count (99M to 3.9B), sizes ($9 * 10^8$ to $6.4 * 10^{10}$ bits) and bitwidths (1.58 bits to 16 bits).
2. **Uniform Training.** All the TriLMs and FloatLMs are trained on identical data sequences, specifically a 300B subset of Slim Pajama (Soboleva et al., 2023) dataset (see Appendix A.2), ensuring training consistency. Data ordering and batch sizes are also kept consistent within each model family. All QuantLMs undergo quantization using the same calibration data on identical data sequences, maintaining uniformity in model quantization procedures.
3. **Public Accessibility.** Training data as well as intermediate training checkpoints of TriLMs and FloatLms are publicly available for future research.
4. **Consistent Model Parameter Mapping.** All the model families maintain a consistent one-to-one mapping in terms of parameter count for studying scaling phenomena.

Figure 11 demonstrates the Spectra LM suite spanning across two dimensions - size (bits) and parameters. For each parameter count, we have 6 models across different bitwidths. Due to the availability of FloatLM, Spectra can easily be extended with new QuantLMs by using different Post Training Quantization methods. We provide details on the dataset and tokenizer, pretraining setup, hyperparameters, and optimization schedule across the families of models in Appendix A. Moreover, we describe our FloatLMs and their quantized versions in the next section.

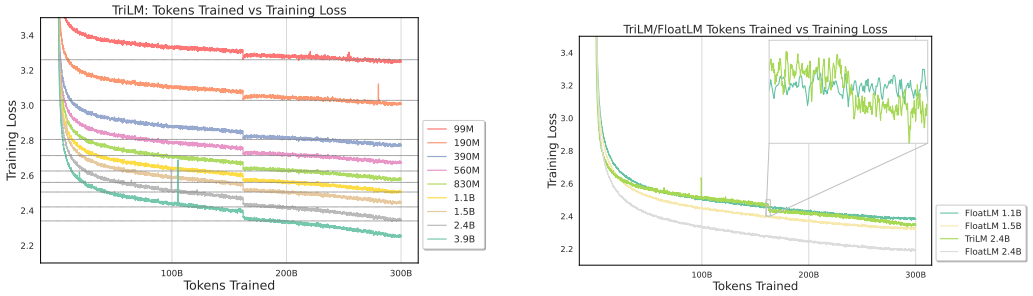
4.2 FLOATLMS AND QUANTLMS

Family of FloatLMs. We utilize LLaMa-style (Touvron et al., 2023a) architecture akin to TriLM. In FloatLMs, we represent the parameters in the weight matrices of linear layers as floating-point numbers (FP16/BF16). The optimization schedule for FloatLM follows a cosine decay scheduling with weight decay and includes a learning rate warmup. This is consistent with the practices established in models such as Pythia, OLMo, LLM360. For more details, refer to the Appendix (A.4).

Family of QuantLMs. Recently, data-aware quantization techniques like GPTQ (Frantar et al., 2022) have emerged as efficient solutions for near-lossless weight quantization down to 4-bit precision (Dettmers & Zettlemoyer, 2023). In this work, we implement GPTQ post-training quantization to FloatLM, creating the QuantLM family of models across 3, 4, 6, and 8 bits. We quantize all transformer layer weights. For 3-bit and 4-bit quantization, we employ a group size of 128, which results in effective bit rates of 3.25 and 4.25 bits per parameter, respectively. We refine our approach by incorporating best practices from recent research by Malinovskii et al. (2024), particularly in terms of calibration data and scaling it to a million tokens for improved reconstruction. To ensure a fair comparison with TriLM, we maintain certain components in their original precision. Specifically, we do not quantize the embedding, language model head, or activations. Additionally, we employ symmetric quantization (without zero offset) for its simplicity, fast inference kernels support (Frantar & Alistarh, 2024), and comparable performance to asymmetric quantization, which uses separate zero offsets and scale values for each group. This approach also ensures consistency and facilitates a fair comparison with TriLMs. Notably, our Spectra suite is designed with flexibility in mind, allowing for easy extension to other quantization methods as needed.

4.3 TRAINING DYNAMICS

Optimizing low bitwidth neural networks, such as in Quantization Aware Training (Liu et al., 2023b; Yuan et al., 2024; Bethge et al., 2018; Le & Li, 2023), requires specific considerations like higher



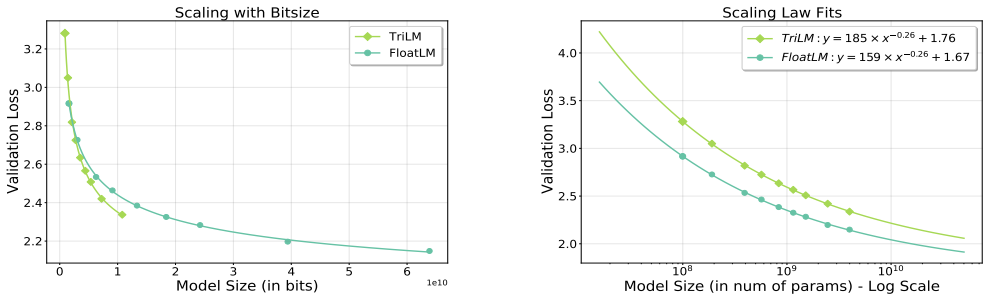
(a) Training loss over time for TriLMs.

(b) Training loss of TriLM vs FloatLM.

Figure 5: Training Cross Entropy Loss across steps for the TriLM family of models. At the halfway point (150B tokens) when we lower the peak learning rate, we observe a sudden drop in training loss. In the two-third way, removing weight decay leads to faster convergence.

initial learning rates and reduced weight decay. Our optimization schedule for TriLM incorporates two key interventions within a standard linear decay learning rate schedule with warmup and weight decay (L2 regularization). First, we reduce the peak learning rate at approximately the halfway point of training. Second, we remove the weight decay regularization about two-thirds into the training, as ternarization provides sufficient regularization (Courbariaux et al., 2016b). Figure 9 in Appendix A.5 shows an ablation study for a 1.1B parameter model trained on 100B tokens, demonstrating that both interventions are necessary to achieve the lowest validation perplexity.

Figure 5a illustrates the training loss curves for all the TriLMs trained and Figure 5b shows the relative training loss of a TriLM in comparison to two smaller FloatLMs. The loss curves demonstrate a continuous and consistent improvement in TriLMs with an increase in parameter count. During training, we make several key observations. First, minor spikes and drops in training loss occurred consistently across different TriLM scales at the same token counts, as all models were trained on identical data with the same ordering. Notably, the two largest models—TriLM 2.4B and TriLM 3.9B—each experienced a large loss spike in the first half of training. Second, adjusting the learning rate at the midpoint led to a sharp decline in training loss over a few hundred million tokens, though its impact varied by model size: for the larger models (2.4B and 3.9B), the rate of loss reduction returned to the prior pace after the initial sharp drop, while for smaller models (1.1B and 1.5B), the loss reduction plateaued, and models below 1B parameters saw an increase in training loss. Lastly, the removal of weight decay at the two-thirds mark accelerated convergence for all models, with the effect being most pronounced in the largest TriLM models.



(a) Scaling laws - perplexity across size (bits).

(b) Scaling laws - perplexity across parameters.

Figure 6: Final validation loss across sizes (in bits) and parameters. TriLMs with increasing size offer better performance than FloatLMs of the same number of bits; and the gap in validation perplexity closes at scale.

4.4 Scaling Laws

In this section, we derive the scaling law for TriLMs and compare it to that of FloatLMs. All models, including our largest 3.9B parameter model, are trained on 300B tokens, placing them in

the overtrained regime as determined by Chinchilla's Hoffmann et al. (2022) compute-optimal token calculation. Figures 6a and 6b illustrate the final validation loss across different model size in terms of bits and number of parameters (N) respectively. In terms of effective model size in bits (6a), which is crucial during inference, TriLMs exhibit significantly better scaling than FloatLMs. Notably, TriLM 3.9B validation error matches with FloatLMs 1.1B, which is nearly 1.7 times larger in terms of effective bit size. To investigate the scaling behaviour in terms of N with fixed data, we fit the validation loss to a power-law with offset[1] Hoffmann et al. (2022) (see Figure 6b and Appendix C):

$$\mathcal{L}_{\text{type}}(N) = \frac{A_{\text{type}}}{N^{\alpha_{\text{type}}}} + \epsilon_{\text{type}}, \text{ where } \begin{cases} A_{\text{TriLM}} = 185, & \alpha_{\text{TriLM}} = 0.26, & \epsilon_{\text{TriLM}} = 1.76 \\ A_{\text{FloatLM}} = 159, & \alpha_{\text{FloatLM}} = 0.26, & \epsilon_{\text{FloatLM}} = 1.67 \end{cases} \tag{1}$$

We employ the Levenberg-Marquardt algorithm (Levenberg (1944); Marquardt (1963)) for efficient non-linear least squares fitting. Both FloatLM and TriLM share the scaling exponent $\alpha = 0.26$, indicating similar scaling behavior with the number of parameters N. However, the offset terms $\epsilon_{\text{TriLM}} = 1.76$ and $\epsilon_{\text{FloatLM}} = 1.67$ reveal that their validation losses converge as N increases. Although TriLM starts with a higher coefficient $A = 185$, suggesting greater initial validation loss than FloatLM ($A = 159$), this difference becomes insignificant with larger N, aligning their performance at asymptotic scales as shown in Figure 6b and 17.

Despite the observed differences in validation loss at the scale of models considered in this work, we demonstrate in Section 5 that at 3.9B parameters, TriLM offers competitive downstream performance compared to a FloatLM of the same parameter count across a variety of benchmarks in commonsense reasoning and knowledge-based tasks. Moreover, as discussed in Appendix §D.4, both models show similar perplexity on clean datasets such as Penn Tree Bank and OpenAI's Lambda. However, the gap in perplexity is observed in overlapping web-based datasets like Dolma and RefinedWeb.

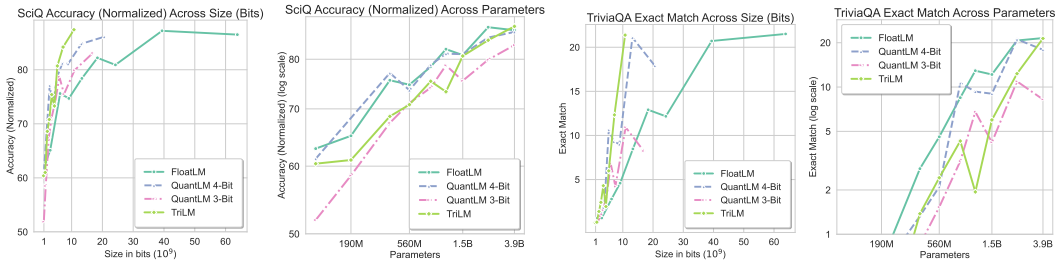
5 Results

We evaluate the families of LLMs on three aspects - commonsense & reasoning tasks, knowledge-based tasks, and toxicity, all of which are crucial measures of their downstream performance. Readers may refer to the appendix for more details regarding the benchmarks (§D).

Commonsense and Reasoning. We evaluate Spectra Suite models using eight distinct commonsense and reasoning benchmarks consisting of tasks from logical and reasoning questions to grounded and physical commonsense tasks: Arc Easy, Arc Challenge (Clark et al., 2018), BoolQ (Clark et al., 2019), HellaSWAG (Zellers et al., 2019), WinoGrande (Sakaguchi et al., 2021), PIQA (Bisk et al., 2019), LAMBADA (Paperno et al., 2016), LogiQA (Liu et al., 2021), all under zero-shot settings. Figures 1a and 1b display the average performance of the LLMs on the first six benchmarks across size in bits and number of params. Figures 1c and 1d present the performance for the LAMBADA dataset. The results show that TriLMs consistently demonstrate superior performance for their size across all benchmarks at the 2.4B and 3.9B parameter scales. At the largest scale of 3.9B, TriLM surpasses FloatLM on LAMBADA and achieves competitive average scores across six benchmarks. Additionally, TriLMs at the largest scales consistently outperform 4-bit QuantLMs of equivalent parameter count. However, across the considered scales, all LLMs show poor performance on LogiQA, making it difficult to identify a clear performance trend. For detailed benchmarking across all datasets –see Tables 7, 8 and 10.

Knowledge. Several downstream practical uses of LLMs require them to have knowledge about common subjects like science or politics. To evaluate the performance of LLMs on these subjects, we use SciQ (Welbl et al., 2017), TriviaQA (Joshi et al., 2017) and MMLU (Hendrycks et al., 2021) benchmarks in zero-shot settings. Figures 7a and 7b show the accuracy of the Spectra suite LLMs on SciQ across size in bits and parameter counts. Figures 21c and 21d depict the accuracy for TriviaQA, while 8a and 8b do the same for MMLU. Across both benchmarks, at large 2.4B+ scales, TriLMs offer the best performance at a given size (bits). Surprisingly, despite having fewer bits, the knowledge capacity of TriLM does not have any significant degradation as observed in the case of QuantLMs (Allen-Zhu & Li, 2024). This indicates that low-bitwidth LLMs like TriLMs have similar knowledge

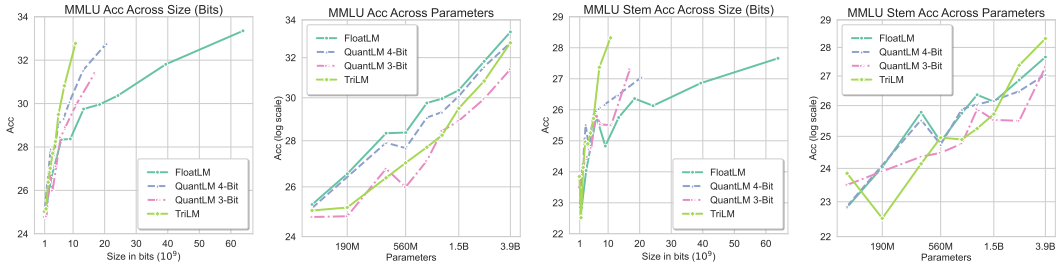
[1]derived using a fixed data regime of 300B tokens



(a) vs. Size in SciQ (b) vs. Params in SciQ (c) vs. Size in TriviaQA (d) vs. Params in TriviaQA

Figure 7: Performance of ternary TriLM, FloatLM and quantized QuantLM (3-bit & 4-bit) models on SciQ and TriviaQA tasks across Size (Bits) and Parameters. Refer to Tables 10 and 17 for details.

capacity to FloatLMs, indicating that knowledge capacity is parameterized via the presence and nature of a connection (+1 or -1), rather than its strength. Tables 10 and 17 expand on these results.



(a) Vs. Size (Bits)- Avg (b) Vs. Parameters- Avg (c) Vs. Size- STEM (d) Vs. Parameters- STEM

Figure 8: MMLU Accuracy for ternary TriLM, FloatLM and quantized QuantLM (3-bit & 4-bit) models across Size and Parameters. Please refer to Table 18 for details.

Toxicity. We evaluate the Spectra suite across various safety and toxicity benchmarks of TruthfulQA (Lin et al., 2021), Big Bench BBQ Lite (Parrish et al., 2022) and CrowsPairs (Nangia et al., 2020). These scores are listed in the Appendix in Table 17. We observe that none of the LLMs, even those with up to 3.9 billion parameters and trained on 300 billion tokens, perform significantly better than random guessing on the TruthfulQA benchmark. For the other two datasets, there is a noticeable correlation between the occurrence of toxicity and stereotypes and the LLMs' performance on various tasks. In particular, TriLMs with fewer than one billion parameters exhibit less stereotyping than FloatLMs with a similar parameter count. However, this difference diminishes as the scale increases, with TriLM 2.4B and TriLM 3.9B exhibiting biases comparable to those of FloatLM 2.4B and FloatLM 3.9B, respectively, on these benchmarks. This suggests that, although TriLMs initially show reduced bias compared to similarly sized FloatLMs, their performance aligns with FloatLMs of equivalent parameter counts at larger scales. This also highlights that TriLMs exhibit considerably more stereotyping than FloatLMs of comparable size (measured in bits), yet perform comparably to FloatLMs with similar parameter counts.

6 Related Work

Quantization of Large Language Models after Training. Post-training quantization (PTQ) algorithms convert a pretrained high-precision model (FP32 / FP16 / BF16) into a lower precision format without requiring the original training process (Cai et al., 2020; Hubara et al., 2020; Choukroun et al., 2019). These methods can be either data-independent or need a small calibration dataset. Additionally, PTQ for LLMs presents unique challenges due to numerical outliers in both weights and activations (Bondarenko et al., 2021). GPTQ (Frantar et al., 2022) is a state-of-the-art one-shot weight quantization method aimed at finding a matrix of quantized weights (say $\hat{W}$) that minimizes the squared error relative to the full precision layer output. By leveraging second-order information, GPTQ derives a closed-form solution to this optimization problem, making it scalable to large LLMs.

Other methods (Dettmers et al., 2023; Lin et al., 2024; Lee et al., 2024) emphasize the importance of outlier weights that correspond to high-magnitude activations. Some recent methods also quantized activation along with the weights (Xiao et al., 2024; Yao et al., 2022; 2023). Ahmadian et al. (2023) demonstrate that large activation outliers can be effectively mitigated at scale by making appropriate optimization decisions during the pretraining phase.

Training Language Models At Lower Precision. Several prominent language models such as GPT (Brown et al., 2020a), NeoX (Black et al., 2022), Llama and Pythia families have been traditionally trained using mixed precision (FP32/FP16 or FP32/BF16) (Micikevicius et al., 2018) or half-precision (FP16/BF16) (Kalamkar et al., 2019). Recently, Tao et al. (2022) introduced QuantGPT, a model that incorporates contrastive and logit distillation from a full-precision teacher to a quantized student model during pretraining. Further developments, such as BitNet (Wang et al., 2023) and BitNet b1.58 (Ma et al., 2024), have specifically focused on quantization-aware training for extremely low-bitwidth networks in transformer-based models. In their work, models are trained at low "effective" precision of binary and ternary respectively - where the latent (or master) weights during training are maintained in higher precision like FP16. The model weights are binarized or ternarized on the fly during the forward pass and gradients are backpropagated for the latent weights using the straight-through estimator (Courbariaux et al., 2016b). Prior works emphasize the importance of maintaining latent (or master) weights at high precision to allow accumulation of small updates during training - for example, Peng et al. (2023) observed a significant performance drop on the language model when the latent (or master) model weights were switch from 16-bits (FP16/BF16) to 8-bits (FP8) during training. Concurrent architectural improvements such as Flash Attention (Dao et al., 2022; Dao, 2023), the mixture of experts (Zoph et al., 2022), xLSTM Beck et al. (2024) and state space models (Gu & Dao, 2024; Dao & Gu, 2024; Gu et al., 2022) complement these advancements in lower precision modeling.

7 Conclusion and Future Work

In this work, we address memory limitations in large language model (LLM) deployment by exploring both post-training quantization and direct low-bitwidth training. We introduce the Spectra LLM suite, featuring 54 models ranging from 99 million to 3.9 billion parameters, trained on 300 billion tokens. This suite includes Float16 LLMs (FloatLMs), quantized QuantLMs (3–8 bits), and our proposed ternary LLMs (TriLMs). Our findings reveal that TriLMs scale better than their half-precision Float16 counterparts in terms of effective model bit size, and they can achieve comparable validation loss when scaled to a large number of parameters. Additionally, our results demonstrate that TriLMs surpass other models in bit-size efficiency and achieve performance comparable to FloatLMs at 3 billion+ parameters across multiple benchmarks.

Future work should address the remaining challenges of toxicity, stereotyping, and performance gaps on web corpora associated with low-bitwidth models. Investigating scaling laws across diverse data regimes and bit sizes in low-bitwidth models trained with quantization-aware training can provide deeper insights into their behavior and limitations. Additionally, combining these models with state-space architectures like Mamba Gu & Dao (2024) could further enhance efficiency and performance without sacrificing accuracy. These research directions hold promise in advancing efficient language modeling further.

References

Arash Ahmadian, Saurabh Dash, Hongyu Chen, Bharat Venkitesh, Stephen Gou, Phil Blunsom, Ahmet Üstün, and Sara Hooker. Intriguing properties of quantization at scale, 2023. URL https://arxiv.org/abs/2305.19268.

AI@Meta. Llama 3 model card. 2024. URL https://github.com/meta-llama/llama3/blob/main/MODEL_CARD.md.

Zeyuan Allen-Zhu and Yuanzhi Li. Physics of language models: Part 3.3, knowledge capacity scaling laws, 2024. URL https://arxiv.org/abs/2404.05405.

AMD Team. Amd instinct mi210 accelerator. https://www.amd.com/en/products/accelerators/instinct/mi200/mi210.html, 2022a. Accessed: July 3, 2024.

AMD Team. Amd instinct mi250 and mi250x accelerators. https://www.amd.com/system/files/documents/amd-instinct-mi200-datasheet.pdf, 2022b. Accessed: July 3, 2024.

AMD Team. Amd instinct mi300a accelerator. https://www.amd.com/en/products/accelerators/instinct/mi300/mi300a.html, 2023a. Accessed: July 3, 2024.

AMD Team. Amd instinct mi300x accelerator. https://www.amd.com/en/products/accelerators/instinct/mi300/mi300x.html, 2023b. Accessed: July 3, 2024.

AMD Team. Amd instinct mi325x accelerator. https://ir.amd.com/news-events/press-releases/detail/1201/amd-accelerates-pace-of-data-center-ai-innovation-and, 2024. Accessed: July 3, 2024.

Alex Andonian, Quentin Anthony, Stella Biderman, Sid Black, Preetham Gali, Leo Gao, Eric Hallahan, Josh Levy-Kramer, Connor Leahy, Lucas Nestler, Kip Parker, Michael Pieler, Jason Phang, Shivanshu Purohit, Hailey Schoelkopf, Dashiell Stander, Tri Songz, Curt Tigges, Benjamin Thérien, Phil Wang, and Samuel Weinbach. GPT-NeoX: Large Scale Autoregressive Language Modeling in PyTorch, 9 2023. URL https://www.github.com/eleutherai/gpt-neox.

Maximilian Beck, Korbinian Pöppel, Markus Spanring, Andreas Auer, Oleksandra Prudnikova, Michael Kopp, Günter Klambauer, Johannes Brandstetter, and Sepp Hochreiter. xlstm: Extended long short-term memory. *arXiv preprint arXiv:2405.04517*, 2024.

Yoshua Bengio, Nicholas Léonard, and Aaron Courville. Estimating or propagating gradients through stochastic neurons for conditional computation, 2013.

Joseph Bethge, Marvin Bornstein, Adrian Loy, Haojin Yang, and Christoph Meinel. Training competitive binary neural networks from scratch. *ArXiv*, abs/1812.01965, 2018. URL https://api.semanticscholar.org/CorpusID:54458838.

Stella Biderman, Hailey Schoelkopf, Quentin Anthony, Herbie Bradley, Kyle O'Brien, Eric Hallahan, Mohammad Aflah Khan, Shivanshu Purohit, USVSN Sai Prashanth, Edward Raff, Aviya Skowron, Lintang Sutawika, and Oskar van der Wal. Pythia: A suite for analyzing large language models across training and scaling, 2023.

Lukas Biewald. Experiment tracking with weights and biases, 2020. URL https://www.wandb.com/. Software available from wandb.com.

Yonatan Bisk, Rowan Zellers, Ronan Le Bras, Jianfeng Gao, and Yejin Choi. Piqa: Reasoning about physical commonsense in natural language. In *AAAI Conference on Artificial Intelligence*, 2019. URL https://api.semanticscholar.org/CorpusID:208290939.

Sid Black, Stella Biderman, Eric Hallahan, Quentin Anthony, Leo Gao, Laurence Golding, Horace He, Connor Leahy, Kyle McDonell, Jason Phang, Michael Pieler, USVSN Sai Prashanth, Shivanshu Purohit, Laria Reynolds, Jonathan Tow, Ben Wang, and Samuel Weinbach. Gpt-neox-20b: An open-source autoregressive language model, 2022. URL https://arxiv.org/abs/2204.06745.

Yelysei Bondarenko, Markus Nagel, and Tijmen Blankevoort. Understanding and overcoming the challenges of efficient transformer quantization, 2021. URL https://arxiv.org/abs/2109.12948.

Tom B. Brown, Benjamin Mann, Nick Ryder, Melanie Subbiah, Jared Kaplan, Prafulla Dhariwal, Arvind Neelakantan, Pranav Shyam, Girish Sastry, Amanda Askell, Sandhini Agarwal, Ariel Herbert-Voss, Gretchen Krueger, Tom Henighan, Rewon Child, Aditya Ramesh, Daniel M. Ziegler, Jeffrey Wu, Clemens Winter, Christopher Hesse, Mark Chen, Eric Sigler, Mateusz Litwin, Scott Gray, Benjamin Chess, Jack Clark, Christopher Berner, Sam McCandlish, Alec Radford, Ilya Sutskever, and Dario Amodei. Language models are few-shot learners, 2020a. URL https://arxiv.org/abs/2005.14165.

Tom B. Brown, Benjamin Mann, Nick Ryder, Melanie Subbiah, Jared Kaplan, Prafulla Dhariwal, Arvind Neelakantan, Pranav Shyam, Girish Sastry, Amanda Askell, Sandhini Agarwal, Ariel Herbert-Voss, Gretchen Krueger, Tom Henighan, Rewon Child, Aditya Ramesh, Daniel M. Ziegler, Jeffrey Wu, Clemens Winter, Christopher Hesse, Mark Chen, Eric Sigler, Mateusz Litwin, Scott Gray, Benjamin Chess, Jack Clark, Christopher Berner, Sam McCandlish, Alec Radford, Ilya Sutskever, and Dario Amodei. Language models are few-shot learners, 2020b.

Yaohui Cai, Zhewei Yao, Zhen Dong, Amir Gholami, Michael W. Mahoney, and Kurt Keutzer. Zeroq: A novel zero shot quantization framework, 2020. URL https://arxiv.org/abs/2001.00281.

Yoni Choukroun, Eli Kravchik, Fan Yang, and Pavel Kisilev. Low-bit quantization of neural networks for efficient inference, 2019. URL https://arxiv.org/abs/1902.06822.

Christopher Clark, Kenton Lee, Ming-Wei Chang, Tom Kwiatkowski, Michael Collins, and Kristina Toutanova. BoolQ: Exploring the surprising difficulty of natural yes/no questions. In Jill Burstein, Christy Doran, and Thamar Solorio (eds.), *Proceedings of the 2019 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, Volume 1 (Long and Short Papers)*, pp. 2924–2936, Minneapolis, Minnesota, June 2019. Association for Computational Linguistics. doi: 10.18653/v1/N19-1300. URL https://aclanthology.org/N19-1300.

Peter Clark, Isaac Cowhey, Oren Etzioni, Tushar Khot, Ashish Sabharwal, Carissa Schoenick, and Oyvind Tafjord. Think you have solved question answering? try arc, the ai2 reasoning challenge, 2018. URL https://api.semanticscholar.org/CorpusID:3922816.

Matthieu Courbariaux, Yoshua Bengio, and Jean-Pierre David. Binaryconnect: Training deep neural networks with binary weights during propagations. *Advances in neural information processing systems*, 28:3123–3131, 2016a.

Matthieu Courbariaux, Yoshua Bengio, and Jean-Pierre David. Binaryconnect: Training deep neural networks with binary weights during propagations, 2016b. URL https://arxiv.org/abs/1511.00363.

Tri Dao. Flashattention-2: Faster attention with better parallelism and work partitioning, 2023. URL https://arxiv.org/abs/2307.08691.

Tri Dao and Albert Gu. Transformers are ssms: Generalized models and efficient algorithms through structured state space duality, 2024. URL https://arxiv.org/abs/2405.21060.

Tri Dao, Daniel Y. Fu, Stefano Ermon, Atri Rudra, and Christopher Ré. Flashattention: Fast and memory-efficient exact attention with io-awareness, 2022. URL https://arxiv.org/abs/2205.14135.

Tim Dettmers and Luke Zettlemoyer. The case for 4-bit precision: k-bit inference scaling laws, 2023.

Tim Dettmers, Ruslan Svirschevski, Vage Egiazarian, Denis Kuznedelev, Elias Frantar, Saleh Ashkboos, Alexander Borzunov, Torsten Hoefler, and Dan Alistarh. Spqr: A sparse-quantized representation for near-lossless llm weight compression, 2023. URL https://arxiv.org/abs/2306.03078.

Vage Egiazarian, Andrei Panferov, Denis Kuznedelev, Elias Frantar, Artem Babenko, and Dan Alistarh. Extreme compression of large language models via additive quantization, 2024. URL https://arxiv.org/abs/2401.06118.

Elias Frantar and Dan Alistarh. Marlin: a fast 4-bit inference kernel for medium batchsizes. https://github.com/IST-DASLab/marlin, 2024.

Elias Frantar, Saleh Ashkboos, Torsten Hoefler, and Dan Alistarh. GPTQ: Accurate post-training compression for generative pretrained transformers. *arXiv preprint arXiv:2210.17323*, 2022.

Leo Gao, Stella Biderman, Sid Black, Laurence Golding, Travis Hoppe, Charles Foster, Jason Phang, Horace He, Anish Thite, Noa Nabeshima, Shawn Presser, and Connor Leahy. The pile: An 800gb dataset of diverse text for language modeling, 2020.

Leo Gao, Jonathan Tow, Baber Abbasi, Stella Biderman, Sid Black, Anthony DiPofi, Charles Foster, Laurence Golding, Jeffrey Hsu, Alain Le Noac'h, Haonan Li, Kyle McDonell, Niklas Muennighoff, Chris Ociepa, Jason Phang, Laria Reynolds, Hailey Schoelkopf, Aviya Skowron, Lintang Sutawika, Eric Tang, Anish Thite, Ben Wang, Kevin Wang, and Andy Zou. A framework for few-shot language model evaluation, 12 2023. URL https://zenodo.org/records/10256836.

Amir Gholami, Zhewei Yao, Sehoon Kim, Coleman Hooper, Michael W. Mahoney, and Kurt Keutzer. Ai and memory wall, 2024. URL https://arxiv.org/abs/2403.14123.

Google TPU Team. Google cloud tpu v3. https://cloud.google.com/tpu/docs/v3, 2018. Accessed: July 3, 2024.

Google TPU Team. Google cloud tpu v4. https://cloud.google.com/tpu/docs/v4, 2021. Accessed: July 3, 2024.

Google TPU Team. Google cloud tpu v5e. https://cloud.google.com/tpu/docs/v5e, 2023a. Accessed: July 3, 2024.

Google TPU Team. Google cloud tpu v5p. https://cloud.google.com/tpu/docs/v5p, 2023b. Accessed: July 3, 2024.

Dirk Groeneveld, Iz Beltagy, Pete Walsh, Akshita Bhagia, Rodney Kinney, Oyvind Tafjord, Ananya Harsh Jha, Hamish Ivison, Ian Magnusson, Yizhong Wang, Shane Arora, David Atkinson, Russell Authur, Khyathi Raghavi Chandu, Arman Cohan, Jennifer Dumas, Yanai Elazar, Yuling Gu, Jack Hessel, Tushar Khot, William Merrill, Jacob Morrison, Niklas Muennighoff, Aakanksha Naik, Crystal Nam, Matthew E. Peters, Valentina Pyatkin, Abhilasha Ravichander, Dustin Schwenk, Saurabh Shah, Will Smith, Emma Strubell, Nishant Subramani, Mitchell Wortsman, Pradeep Dasigi, Nathan Lambert, Kyle Richardson, Luke Zettlemoyer, Jesse Dodge, Kyle Lo, Luca Soldaini, Noah A. Smith, and Hannaneh Hajishirzi. Olmo: Accelerating the science of language models, 2024. URL https://arxiv.org/abs/2402.00838.

Albert Gu and Tri Dao. Mamba: Linear-time sequence modeling with selective state spaces, 2024. URL https://arxiv.org/abs/2312.00752.

Albert Gu, Karan Goel, and Christopher Ré. Efficiently modeling long sequences with structured state spaces. In *The International Conference on Learning Representations (ICLR)*, 2022.

Dan Hendrycks, Collin Burns, Steven Basart, Andy Zou, Mantas Mazeika, Dawn Song, and Jacob Steinhardt. Measuring massive multitask language understanding. *Proceedings of the International Conference on Learning Representations (ICLR)*, 2021.

Jordan Hoffmann, Sebastian Borgeaud, Arthur Mensch, Elena Buchatskaya, Trevor Cai, Eliza Rutherford, Diego de Las Casas, Lisa Anne Hendricks, Johannes Welbl, Aidan Clark, Tom Hennigan, Eric Noland, Katie Millican, George van den Driessche, Bogdan Damoc, Aurelia Guy, Simon Osindero, Karen Simonyan, Erich Elsen, Jack W. Rae, Oriol Vinyals, and Laurent Sifre. Training compute-optimal large language models, 2022. URL https://arxiv.org/abs/2203.15556.

Shengding Hu, Yuge Tu, Xu Han, Chaoqun He, Ganqu Cui, Xiang Long, Zhi Zheng, Yewei Fang, Yuxiang Huang, Weilin Zhao, Xinrong Zhang, Zheng Leng Thai, Kaihuo Zhang, Chongyi Wang, Yuan Yao, Chenyang Zhao, Jie Zhou, Jie Cai, Zhongwu Zhai, Ning Ding, Chao Jia, Guoyang Zeng, Dahai Li, Zhiyuan Liu, and Maosong Sun. Minicpm: Unveiling the potential of small language models with scalable training strategies, 2024. URL https://arxiv.org/abs/2404.06395.

Wei Huang, Xudong Ma, Haotong Qin, Xingyu Zheng, Chengtao Lv, Hong Chen, Jie Luo, Xiaojuan Qi, Xianglong Liu, and Michele Magno. How good are low-bit quantized llama3 models? an empirical study, 2024. URL https://arxiv.org/abs/2404.14047.

Itay Hubara, Matthieu Courbariaux, Daniel Soudry, Ran El-Yaniv, and Yoshua Bengio. Binarized neural networks. *Neural Computation*, 29(1):322–344, 2017.

Itay Hubara, Yury Nahshan, Yair Hanani, Ron Banner, and Daniel Soudry. Improving post training neural quantization: Layer-wise calibration and integer programming, 2020. URL https://arxiv.org/abs/2006.10518.

Intel Gaudi Team. Intel gaudi 2 and gaudi 3 ai accelerators. https://cdrdv2-public.intel.com/817486/gaudi-3-ai-accelerator-white-paper.pdf, 2024. Accessed: July 3, 2024.

Mandar Joshi, Eunsol Choi, Daniel Weld, and Luke Zettlemoyer. TriviaQA: A large scale distantly supervised challenge dataset for reading comprehension. In Regina Barzilay and Min-Yen Kan (eds.), *Proceedings of the 55th Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers)*, pp. 1601–1611, Vancouver, Canada, July 2017. Association for Computational Linguistics. doi: 10.18653/v1/P17-1147. URL https://aclanthology.org/P17-1147.

Dhiraj Kalamkar, Dheevatsa Mudigere, Naveen Mellempudi, Dipankar Das, Kunal Banerjee, Sasikanth Avancha, Dharma Teja Vooturi, Nataraj Jammalamadaka, Jianyu Huang, Hector Yuen, Jiyan Yang, Jongsoo Park, Alexander Heinecke, Evangelos Georganas, Sudarshan Srinivasan, Abhisek Kundu, Misha Smelyanskiy, Bharat Kaul, and Pradeep Dubey. A study of bfloat16 for deep learning training, 2019. URL https://arxiv.org/abs/1905.12322.

Jared Kaplan, Sam McCandlish, Tom Henighan, Tom B. Brown, Benjamin Chess, Rewon Child, Scott Gray, Alec Radford, Jeffrey Wu, and Dario Amodei. Scaling laws for neural language models, 2020. URL https://arxiv.org/abs/2001.08361.

Sehoon Kim, Coleman Hooper, Amir Gholami, Zhen Dong, Xiuyu Li, Sheng Shen, Michael W. Mahoney, and Kurt Keutzer. Squeezellm: Dense-and-sparse quantization, 2024.

Diederik P. Kingma and Jimmy Ba. Adam: A method for stochastic optimization, 2017.

Phuoc-Hoan Charles Le and Xinlin Li. Binaryvit: Pushing binary vision transformers towards convolutional models. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition (CVPR) Workshops*, pp. 4664–4673, June 2023.

Changhun Lee, Jungyu Jin, Taesu Kim, Hyungjun Kim, and Eunhyeok Park. Owq: Outlier-aware weight quantization for efficient fine-tuning and inference of large language models, 2024. URL https://arxiv.org/abs/2306.02272.

Kenneth Levenberg. A method for the solution of certain non-linear problems in least squares. *Quarterly of Applied Mathematics*, 2:164–168, 1944.

Fengfu Li, Bo Zhang, and Bin Liu. Ternary weight networks. *arXiv preprint arXiv:1605.04711*, 2016.

Jason Li. Mechanistic interpretability of binary and ternary transformers, 2024. URL https://arxiv.org/abs/2405.17703.

Shiyao Li, Xuefei Ning, Luning Wang, Tengxuan Liu, Xiangsheng Shi, Shengen Yan, Guohao Dai, Huazhong Yang, and Yu Wang. Evaluating quantized large language models, 2024. URL https://arxiv.org/abs/2402.18158.

Ji Lin, Jiaming Tang, Haotian Tang, Shang Yang, Wei-Ming Chen, Wei-Chen Wang, Guangxuan Xiao, Xingyu Dang, Chuang Gan, and Song Han. Awq: Activation-aware weight quantization for llm compression and acceleration, 2024. URL https://arxiv.org/abs/2306.00978.

Stephanie Lin, Jacob Hilton, and Owain Evans. Truthfulqa: Measuring how models mimic human falsehoods, 2021.

Jian Liu, Leyang Cui, Hanmeng Liu, Dandan Huang, Yile Wang, and Yue Zhang. Logiqa: a challenge dataset for machine reading comprehension with logical reasoning. In *Proceedings of the Twenty-Ninth International Joint Conference on Artificial Intelligence*, IJCAI'20, 2021. ISBN 9780999241165.

Zechun Liu, Barlas Oguz, Aasish Pappu, Yangyang Shi, and Raghuraman Krishnamoorthi. Binary and ternary natural language generation, 2023a. URL https://arxiv.org/abs/2306.01841.

Zechun Liu, Barlas Oguz, Changsheng Zhao, Ernie Chang, Pierre Stock, Yashar Mehdad, Yangyang Shi, Raghuraman Krishnamoorthi, and Vikas Chandra. Llm-qat: Data-free quantization aware training for large language models. *arXiv preprint arXiv:2305.17888*, 2023b.

Zhengzhong Liu, Aurick Qiao, Willie Neiswanger, Hongyi Wang, Bowen Tan, Tianhua Tao, Junbo Li, Yuqi Wang, Suqi Sun, Omkar Pangarkar, Richard Fan, Yi Gu, Victor Miller, Yonghao Zhuang, Guowei He, Haonan Li, Fajri Koto, Liping Tang, Nikhil Ranjan, Zhiqiang Shen, Xuguang Ren, Roberto Iriondo, Cun Mu, Zhiting Hu, Mark Schulze, Preslav Nakov, Tim Baldwin, and Eric P. Xing. Llm360: Towards fully transparent open-source llms, 2023c.

Shuming Ma, Hongyu Wang, Lingxiao Ma, Lei Wang, Wenhui Wang, Shaohan Huang, Li Dong, Ruiping Wang, Jilong Xue, and Furu Wei. The era of 1-bit llms: All large language models are in 1.58 bits, 2024.

David J. C. MacKay. *Information Theory, Inference, and Learning Algorithms*. Cambridge University Press, 2003. ISBN 978-0521642989.

Vladimir Malinovskii, Denis Mazur, Ivan Ilin, Denis Kuznedelev, Konstantin Burlachenko, Kai Yi, Dan Alistarh, and Peter Richtarik. Pv-tuning: Beyond straight-through estimation for extreme llm compression, 2024. URL `https://arxiv.org/abs/2405.14852`.

Donald Marquardt. An algorithm for least-squares estimation of nonlinear parameters. *Journal of the Society for Industrial and Applied Mathematics*, 11(2):431–441, 1963.

Paulius Micikevicius, Sharan Narang, Jonah Alben, Gregory Diamos, Erich Elsen, David Garcia, Boris Ginsburg, Michael Houston, Oleksii Kuchaiev, Ganesh Venkatesh, and Hao Wu. Mixed precision training, 2018. URL `https://arxiv.org/abs/1710.03740`.

Tomas Mikolov, Kai Chen, Greg Corrado, and Jeffrey Dean. Efficient estimation of word representations in vector space, 2013. URL `https://arxiv.org/abs/1301.3781`.

Nikita Nangia, Clara Vania, Rasika Bhalerao, and Samuel R. Bowman. CrowS-Pairs: A Challenge Dataset for Measuring Social Biases in Masked Language Models. In *Proceedings of the 2020 Conference on Empirical Methods in Natural Language Processing*, Online, November 2020. Association for Computational Linguistics.

Behnam Neyshabur, Zhiyuan Li, Srinadh Bhojanapalli, Yann LeCun, and Nathan Srebro. Towards understanding the role of over-parametrization in generalization of neural networks. In *Proceedings of the International Conference on Learning Representations (ICLR)*, 2018.

Nvidia, :, Bo Adler, Niket Agarwal, Ashwath Aithal, Dong H. Anh, Pallab Bhattacharya, Annika Brundyn, Jared Casper, Bryan Catanzaro, Sharon Clay, Jonathan Cohen, Sirshak Das, Ayush Dattagupta, Olivier Delalleau, Leon Derczynski, Yi Dong, Daniel Egert, Ellie Evans, Aleksander Ficek, Denys Fridman, Shaona Ghosh, Boris Ginsburg, Igor Gitman, Tomasz Grzegorzek, Robert Hero, Jining Huang, Vibhu Jawa, Joseph Jennings, Aastha Jhunjhunwala, John Kamalu, Sadaf Khan, Oleksii Kuchaiev, Patrick LeGresley, Hui Li, Jiwei Liu, Zihan Liu, Eileen Long, Ameya Sunil Mahabaleshwarkar, Somshubra Majumdar, James Maki, Miguel Martinez, Maer Rodrigues de Melo, Ivan Moshkov, Deepak Narayanan, Sean Narenthiran, Jesus Navarro, Phong Nguyen, Osvald Nitski, Vahid Noroozi, Guruprasad Nutheti, Christopher Parisien, Jupinder Parmar, Mostofa Patwary, Krzysztof Pawelec, Wei Ping, Shrimai Prabhumoye, Rajarshi Roy, Trisha Saar, Vasanth Rao Naik Sabavat, Sanjeev Satheesh, Jane Polak Scowcroft, Jason Sewall, Pavel Shamis, Gerald Shen, Mohammad Shoeybi, Dave Sizer, Misha Smelyanskiy, Felipe Soares, Makesh Narsimhan Sreedhar, Dan Su, Sandeep Subramanian, Shengyang Sun, Shubham Toshniwal, Hao Wang, Zhilin Wang, Jiaxuan You, Jiaqi Zeng, Jimmy Zhang, Jing Zhang, Vivienne Zhang, Yian Zhang, and Chen Zhu. Nemotron-4 340b technical report, 2024. URL `https://arxiv.org/abs/2406.11704`.

Nvidia Team. Nvidia tesla v100 gpu accelerator. `https://images.nvidia.com/content/technologies/volta/pdf/tesla-volta-v100-datasheet-letter-fnl-web.pdf`, 2018. Accessed: July 3, 2024.

Nvidia Team. Nvidia a100 tensor core gpu. https://www.nvidia.com/content/dam/en-zz/Solutions/Data-Center/a100/pdf/nvidia-a100-datasheet-us-nvidia-1758950-r4-web.pdf, 2020. Accessed: July 3, 2024.

Nvidia Team. Nvidia h100 tensor core gpu. https://resources.nvidia.com/en-us-tensor-core/nvidia-tensor-core-gpu-datasheet, 2022. Accessed: July 3, 2024.

Nvidia Team. Nvidia h200 tensor core gpu. https://nvdam.widen.net/s/nb5zzzsjdf/hpc-datasheet-sc23-h200-datasheet-3002446, 2023. Accessed: July 3 2024. Redirected from https://www.nvidia.com/en-in/data-center/h200/.

Nvidia Team. Nvidia blackwell architecture. https://resources.nvidia.com/en-us-blackwell-architecture, 2024. Accessed: July 3, 2024.

Denis Paperno, Germán Kruszewski, Angeliki Lazaridou, Ngoc Quan Pham, Raffaella Bernardi, Sandro Pezzelle, Marco Baroni, Gemma Boleda, and Raquel Fernández. The LAMBADA dataset: Word prediction requiring a broad discourse context. In Katrin Erk and Noah A. Smith (eds.), *Proceedings of the 54th Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers)*, pp. 1525–1534, Berlin, Germany, August 2016. Association for Computational Linguistics. doi: 10.18653/v1/P16-1144. URL https://aclanthology.org/P16-1144.

Athanasios Papoulis and S. Unnikrishna Pillai. *Probability, Random Variables, and Stochastic Processes*. McGraw-Hill, 4 edition, 2002. ISBN 978-0071226615.

Alicia Parrish, Angelica Chen, Nikita Nangia, Vishakh Padmakumar, Jason Phang, Jana Thompson, Phu Mon Htut, and Samuel Bowman. BBQ: A hand-built bias benchmark for question answering. In Smaranda Muresan, Preslav Nakov, and Aline Villavicencio (eds.), *Findings of the Association for Computational Linguistics: ACL 2022*, pp. 2086–2105, Dublin, Ireland, May 2022. Association for Computational Linguistics. doi: 10.18653/v1/2022.findings-acl.165. URL https://aclanthology.org/2022.findings-acl.165.

Houwen Peng, Kan Wu, Yixuan Wei, Guoshuai Zhao, Yuxiang Yang, Ze Liu, Yifan Xiong, Ziyue Yang, Bolin Ni, Jingcheng Hu, Ruihang Li, Miaosen Zhang, Chen Li, Jia Ning, Ruizhe Wang, Zheng Zhang, Shuguang Liu, Joe Chau, Han Hu, and Peng Cheng. Fp8-lm: Training fp8 large language models, 2023. URL https://arxiv.org/abs/2310.18313.

Ofir Press and Lior Wolf. Using the output embedding to improve language models, 2017. URL https://arxiv.org/abs/1608.05859.

Samyam Rajbhandari, Jeff Rasley, Olatunji Ruwase, and Yuxiong He. Zero: memory optimizations toward training trillion parameter models. In *Proceedings of the International Conference for High Performance Computing, Networking, Storage and Analysis*, SC '20. IEEE Press, 2020. ISBN 9781728199986.

Jeff Rasley, Samyam Rajbhandari, Olatunji Ruwase, and Yuxiong He. Deepspeed: System optimizations enable training deep learning models with over 100 billion parameters. In *Proceedings of the 26th ACM SIGKDD International Conference on Knowledge Discovery & Data Mining*, KDD '20, pp. 3505–3506, New York, NY, USA, 2020. Association for Computing Machinery. ISBN 9781450379984. doi: 10.1145/3394486.3406703. URL https://doi.org/10.1145/3394486.3406703.

Mohammad Rastegari, Vicente Ordonez, Joseph Redmon, and Ali Farhadi. Xnor-net: Imagenet classification using binary convolutional neural networks. *European Conference on Computer Vision*, pp. 525–542, 2016.

Keisuke Sakaguchi, Ronan Le Bras, Chandra Bhagavatula, and Yejin Choi. Winogrande: an adversarial winograd schema challenge at scale. *Commun. ACM*, 64(9):99–106, aug 2021. ISSN 0001-0782. doi: 10.1145/3474381. URL https://doi.org/10.1145/3474381.

Claude E. Shannon. A mathematical theory of communication. *The Bell System Technical Journal*, 27(3):379–423, 623–656, 1948.

Wenqi Shao, Mengzhao Chen, Zhaoyang Zhang, Peng Xu, Lirui Zhao, Zhiqian Li, Kaipeng Zhang, Peng Gao, Yu Qiao, and Ping Luo. Omniquant: Omnidirectionally calibrated quantization for large language models, 2024. URL https://arxiv.org/abs/2308.13137.

Noam Shazeer. Glu variants improve transformer, 2020.

Mohammad Shoeybi, Mostofa Patwary, Raul Puri, Patrick LeGresley, Jared Casper, and Bryan Catanzaro. Megatron-lm: Training multi-billion parameter language models using model parallelism, 2019.

Daria Soboleva, Faisal Al-Khateeb, Robert Myers, Jacob R Steeves, Joel Hestness, and Nolan Dey. Slimpajama: A 627b token cleaned and deduplicated version of redpajama, 2023. URL https://www.cerebras.net/blog/slimpajama-a-627b-token-cleaned-and-deduplicated-version-of-redpajama.

Jianlin Su, Yu Lu, Shengfeng Pan, Ahmed Murtadha, Bo Wen, and Yunfeng Liu. Roformer: Enhanced transformer with rotary position embedding, 2021.

Chaofan Tao, Lu Hou, Wei Zhang, Lifeng Shang, Xin Jiang, Qun Liu, Ping Luo, and Ngai Wong. Compression of generative pre-trained language models via quantization. In Smaranda Muresan, Preslav Nakov, and Aline Villavicencio (eds.), *Proceedings of the 60th Annual Meeting of the Association for Computational Linguistics (Volume 1: Long Papers)*, pp. 4821–4836, Dublin, Ireland, May 2022. Association for Computational Linguistics. doi: 10.18653/v1/2022.acl-long.331. URL https://aclanthology.org/2022.acl-long.331.

Gemma Team, Thomas Mesnard, Cassidy Hardin, Robert Dadashi, Surya Bhupatiraju, Shreya Pathak, Laurent Sifre, Morgane Rivière, Mihir Sanjay Kale, Juliette Love, Pouya Tafti, Léonard Hussenot, Pier Giuseppe Sessa, Aakanksha Chowdhery, Adam Roberts, Aditya Barua, Alex Botev, Alex Castro-Ros, Ambrose Slone, Amélie Héliou, Andrea Tacchetti, Anna Bulanova, Antonia Paterson, Beth Tsai, Bobak Shahriari, Charline Le Lan, Christopher A. Choquette-Choo, Clément Crepy, Daniel Cer, Daphne Ippolito, David Reid, Elena Buchatskaya, Eric Ni, Eric Noland, Geng Yan, George Tucker, George-Christian Muraru, Grigory Rozhdestvenskiy, Henryk Michalewski, Ian Tenney, Ivan Grishchenko, Jacob Austin, James Keeling, Jane Labanowski, Jean-Baptiste Lespiau, Jeff Stanway, Jenny Brennan, Jeremy Chen, Johan Ferret, Justin Chiu, Justin Mao-Jones, Katherine Lee, Kathy Yu, Katie Millican, Lars Lowe Sjoesund, Lisa Lee, Lucas Dixon, Machel Reid, Maciej Mikuła, Mateo Wirth, Michael Sharman, Nikolai Chinaev, Nithum Thain, Olivier Bachem, Oscar Chang, Oscar Wahltinez, Paige Bailey, Paul Michel, Petko Yotov, Rahma Chaabouni, Ramona Comanescu, Reena Jana, Rohan Anil, Ross McIlroy, Ruibo Liu, Ryan Mullins, Samuel L Smith, Sebastian Borgeaud, Sertan Girgin, Sholto Douglas, Shree Pandya, Siamak Shakeri, Soham De, Ted Klimenko, Tom Hennigan, Vlad Feinberg, Wojciech Stokowiec, Yu hui Chen, Zafarali Ahmed, Zhitao Gong, Tris Warkentin, Ludovic Peran, Minh Giang, Clément Farabet, Oriol Vinyals, Jeff Dean, Koray Kavukcuoglu, Demis Hassabis, Zoubin Ghahramani, Douglas Eck, Joelle Barral, Fernando Pereira, Eli Collins, Armand Joulin, Noah Fiedel, Evan Senter, Alek Andreev, and Kathleen Kenealy. Gemma: Open models based on gemini research and technology, 2024. URL https://arxiv.org/abs/2403.08295.

Hugo Touvron, Thibaut Lavril, Gautier Izacard, Xavier Martinet, Marie-Anne Lachaux, Timothée Lacroix, Baptiste Rozière, Naman Goyal, Eric Hambro, Faisal Azhar, Aurelien Rodriguez, Armand Joulin, Edouard Grave, and Guillaume Lample. Llama: Open and efficient foundation language models, 2023a.

Hugo Touvron, Louis Martin, Kevin Stone, Peter Albert, Amjad Almahairi, Yasmine Babaei, Nikolay Bashlykov, Soumya Batra, Prajjwal Bhargava, Shruti Bhosale, Dan Bikel, Lukas Blecher, Cristian Canton Ferrer, Moya Chen, Guillem Cucurull, David Esiobu, Jude Fernandes, Jeremy Fu, Wenyin Fu, Brian Fuller, Cynthia Gao, Vedanuj Goswami, Naman Goyal, Anthony Hartshorn, Saghar Hosseini, Rui Hou, Hakan Inan, Marcin Kardas, Viktor Kerkez, Madian Khabsa, Isabel Kloumann, Artem Korenev, Punit Singh Koura, Marie-Anne Lachaux, Thibaut Lavril, Jenya Lee, Diana Liskovich, Yinghai Lu, Yuning Mao, Xavier Martinet, Todor Mihaylov, Pushkar Mishra, Igor Molybog, Yixin Nie, Andrew Poulton, Jeremy Reizenstein, Rashi Rungta, Kalyan Saladi, Alan Schelten, Ruan Silva, Eric Michael Smith, Ranjan Subramanian, Xiaoqing Ellen Tan, Binh Tang, Ross Taylor, Adina Williams, Jian Xiang Kuan, Puxin Xu, Zheng Yan, Iliyan Zarov, Yuchen

Zhang, Angela Fan, Melanie Kambadur, Sharan Narang, Aurelien Rodriguez, Robert Stojnic, Sergey Edunov, and Thomas Scialom. Llama 2: Open foundation and fine-tuned chat models, 2023b.

Ashish Vaswani, Noam Shazeer, Niki Parmar, Jakob Uszkoreit, Llion Jones, Aidan N Gomez, Ł ukasz Kaiser, and Illia Polosukhin. Attention is all you need. In I. Guyon, U. Von Luxburg, S. Bengio, H. Wallach, R. Fergus, S. Vishwanathan, and R. Garnett (eds.), *Advances in Neural Information Processing Systems*, volume 30. Curran Associates, Inc., 2017. URL https://proceedings.neurips.cc/paper_files/paper/2017/file/3f5ee243547dee91fbd053c1c4a845aa-Paper.pdf.

Hongyu Wang, Shuming Ma, Li Dong, Shaohan Huang, Huaijie Wang, Lingxiao Ma, Fan Yang, Ruiping Wang, Yi Wu, and Furu Wei. Bitnet: Scaling 1-bit transformers for large language models, 2023.

Johannes Welbl, Nelson F. Liu, and Matt Gardner. Crowdsourcing multiple choice science questions. *ArXiv*, abs/1707.06209, 2017. URL https://api.semanticscholar.org/CorpusID:1553193.

Thomas Wolf, Lysandre Debut, Victor Sanh, Julien Chaumond, Clement Delangue, Anthony Moi, Pierric Cistac, Tim Rault, Rémi Louf, Morgan Funtowicz, Joe Davison, Sam Shleifer, Patrick von Platen, Clara Ma, Yacine Jernite, Julien Plu, Canwen Xu, Teven Le Scao, Sylvain Gugger, Mariama Drame, Quentin Lhoest, and Alexander M. Rush. Transformers: State-of-the-art natural language processing. In *Proceedings of the 2020 Conference on Empirical Methods in Natural Language Processing: System Demonstrations*, pp. 38–45, Online, October 2020. Association for Computational Linguistics. URL https://www.aclweb.org/anthology/2020.emnlp-demos.6.

Guangxuan Xiao, Ji Lin, Mickael Seznec, Hao Wu, Julien Demouth, and Song Han. Smoothquant: Accurate and efficient post-training quantization for large language models, 2024. URL https://arxiv.org/abs/2211.10438.

Zhewei Yao, Reza Yazdani Aminabadi, Minjia Zhang, Xiaoxia Wu, Conglong Li, and Yuxiong He. Zeroquant: Efficient and affordable post-training quantization for large-scale transformers, 2022. URL https://arxiv.org/abs/2206.01861.

Zhewei Yao, Xiaoxia Wu, Cheng Li, Stephen Youn, and Yuxiong He. Zeroquant-v2: Exploring post-training quantization in llms from comprehensive study to low rank compensation, 2023. URL https://arxiv.org/abs/2303.08302.

Zhihang Yuan, Yuzhang Shang, and Zhen Dong. PB-LLM: Partially binarized large language models. In *The Twelfth International Conference on Learning Representations*, 2024. URL https://openreview.net/forum?id=BifeBRhikU.

Rowan Zellers, Ari Holtzman, Yonatan Bisk, Ali Farhadi, and Yejin Choi. HellaSwag: Can a machine really finish your sentence? In Anna Korhonen, David Traum, and Lluís Màrquez (eds.), *Proceedings of the 57th Annual Meeting of the Association for Computational Linguistics*, pp. 4791–4800, Florence, Italy, July 2019. Association for Computational Linguistics. doi: 10.18653/v1/P19-1472. URL https://aclanthology.org/P19-1472.

Biao Zhang and Rico Sennrich. Root mean square layer normalization. In *Proceedings of the 33rd International Conference on Neural Information Processing Systems*, Red Hook, NY, USA, 2019. Curran Associates Inc.

Chiyuan Zhang, Samy Bengio, Moritz Hardt, Benjamin Recht, and Oriol Vinyals. Understanding deep learning requires rethinking generalization. In *International Conference on Learning Representations (ICLR)*, 2017.

Shuchang Zhou, Yuxin Wu, Zekun Ni, Xinyu Zhou, He Wen, and Yuheng Zou. Dorefa-net: Training low bitwidth convolutional neural networks with low bitwidth gradients. *arXiv preprint arXiv:1606.06160*, 2016.

Shuchang Zhou, Yuxin Wu, Zekun Ni, Xinyu Zhou, He Wen, and Yuheng Zou. Dorefa-net: Training low bitwidth convolutional neural networks with low bitwidth gradients, 2018. URL https://arxiv.org/abs/1606.06160.

Chenzhuo Zhu, Song Han, Huizi Mao, and William J Dally. Trained ternary quantization. *arXiv preprint arXiv:1612.01064*, 2017.

Xunyu Zhu, Jian Li, Yong Liu, Can Ma, and Weiping Wang. A survey on model compression for large language models, 2023. URL https://arxiv.org/abs/2308.07633.

Barret Zoph, Irwan Bello, Sameer Kumar, Nan Du, Yanping Huang, Jeff Dean, Noam Shazeer, and William Fedus. St-moe: Designing stable and transferable sparse expert models, 2022. URL https://arxiv.org/abs/2202.08906.

A ARCHITECTURE AND PRETRAINING DETAILS

This section provides a comprehensive overview of the architectural design and pretraining for TriLM (Ternary Language Model) and FloatLM (Floating Point Language Model). We outline the forward and backward pass equations specific to their linear layers, highlighting the contrast between the FP16 matrices in FloatLM and the ternary matrices with scalar scaling in TriLM. Additionally, it covers dataset selection, tokenizer usage, and preprocessing methods employed for training data preparation. These discussions provide information on pretraining setups, implementation nuances, and key hyperparameters critical to the models' development.

A.1 FORWARD PASS, BACKWARD PASS AND INFERENCE EQUATIONS

Table 1 shows the equations across TriLM vs FloatLM for forward pass, backward pass and inference.

Type	Forward Pass	Backward Pass	Inference
FloatLM	$Y = XW^T$	$\frac{\partial L}{\partial X} = \frac{\partial L}{\partial Y} W$ $\frac{\partial L}{\partial W} = \frac{\partial L}{\partial Y}^T X$	$Y = XW^T$
TriLM	$\gamma = \epsilon + \frac{1}{nm}\sum_{i=1}^{n}\sum_{j=1}^{m}\lvert W_{ij}\rvert$ $\widehat{W_{ij}} = \text{round}\left(\min\left(\max\left(\frac{W_{ij}}{\gamma}, -1\right), 1\right)\right)$ $\widetilde{W_{ij}} = \gamma\widehat{W_{ij}}$ $Y = X\widetilde{W}^T$	$\frac{\partial L}{\partial X} = \frac{\partial L}{\partial Y}\widetilde{W}$ $\frac{\partial L}{\partial W} = \frac{\partial L}{\partial Y}^T X$	Compute $\widehat{W}$ and γ once and cache $\widetilde{W_{ij}} = \gamma\widehat{W_{ij}}$ $Y = X\widetilde{W}^T$
BiLM	$\alpha = \frac{1}{nm}\sum_{i=1}^{n}\sum_{j=1}^{m}\lvert W_{ij}\rvert$ $\widehat{W_{ij}} = \text{sign}(W_{ij} - \frac{1}{nm}\sum_{i=1}^{n}\sum_{j=1}^{m} W_{ij})$ $\widetilde{W_{ij}} = \alpha\widehat{W_{ij}}$ $Y = X\widetilde{W}^T$	$\frac{\partial L}{\partial X} = \frac{\partial L}{\partial Y}\widetilde{W}$ $\frac{\partial L}{\partial W} = \frac{\partial L}{\partial Y}^T X$	Compute $\widehat{W}$ and α once and cache $\widetilde{W_{ij}} = \alpha\widehat{W_{ij}}$ $Y = X\widetilde{W}^T$

Table 1: Equations in the Linear Layer of TriLMs and FloatLMs.

Reason for restricting the quantization approach to linear weights in TriLMs. In developing extremely large language models like TriLMs, a key architectural strategy is to quantize only the linear layer weights while keeping the embedding layers and language model head in higher precision. This is driven by the need to reduce model size while maintaining performance. Linear layers (dense layers) hold the bulk of the parameters in transformer models (Vaswani et al., 2017). Quantizing these weights to ternary states significantly reduces the model size, facilitating deployment on memory-constrained hardware. However, the embedding layers and language model head remain in higher precision (e.g., half-precision floating point) to preserve critical functions in language understanding and generation. Embedding layers encode important semantic and syntactic information, and quantizing them would degrade performance (Mikolov et al., 2013). Similarly, the language model head, which maps internal representations to the vocabulary space, requires high precision to maintain prediction quality (Press & Wolf, 2017)

A.2 DATA AND TOKENIZER

Dataset Selection: Let input be $X \in R_{b\times n}$ for a linear layer with FP16 weight matrix $W \in R_{m\times n}$ and $Y \in R_{b\times m}$ be the output. The same matrix W is also used to denote latent weights in TriLMs during training.

For ternarized layers in TriLMs, we also have a scalar scale $\gamma \in R$, matrix with ternarized states $\widehat{W} \in \{-1, 0, 1\}_{n\times m}$ and ternarized matrix $\widetilde{W} \in R_{n\times m}$. We set $\epsilon = 1e-5$.

Due to lack of availability of Pile 300B (Gao et al., 2020) used in Pythia, we opted to use a 300B token sample of deduplicated Slim Pajama dataset[2]. We sample from each subset with the probability proportional to its size.

[2]We also make this subset public

Training Data Preparation:

- **Main experiments (Spectra suite)**: We used the full 300B token sample.
- **Ablation studies**: Training runs with 100B tokens, we sample from these 300B tokens with equal probability weight to each data-point.
- **Fine-Web Edu experiments**: We tokenized one-third of a 350B token sample, from which we then sampled 100B tokens for our experiments.

QuantLM: For the creation of QuantLM, we utilized a subset of the Slimpajama-627B dataset, consisting of 512 samples with a sequence length of 2048. These samples were normalized for length. Our approach closely follows the methodology outlined in (Malinovskii et al., 2024).

Tokenizer and Optimization Techniques: We use the GPT-NeoX 20B tokenizer following Pythia. For speeding up training, we round embedding rounding of to the nearest multiple of 128 times the model parallel size.

Dataset	Size (Tokens)
Arxiv	13B
Book	13B
C4	80B
Common Crawl	156B
GitHub	16B
Stack Exchange	10B
Wikipedia	12B
Total	300B

Table 2: 300B Subset of Slim Pajama

A.3 PreTraining Setup

We scale using 2D-parallelism with Megatron-style sharding (Shoeybi et al., 2019) and use ZeRO stage 2 Deepspeed (Rasley et al., 2020) for ZeRO (Rajbhandari et al., 2020). Our implementation was based on GPT NeoX Codebase (Andonian et al., 2023). We use AdamW (Kingma & Ba, 2017) for optimization. We train on nodes with IBM Power9 PC CPUs and 6x16GB V100. Due to the lack of BFloat16 support in V100, we train both TriLM and FloatLM in FP16 using Mixed Precision Training and Dynamic Loss Scaling. Please refer to §A.6 for more implementation specific details. We extensively use Huggingface (Wolf et al., 2020) and Wandb (Biewald, 2020) for handling the checkpoints and experiment tracking.

A.4 Hyperparameters

Table 3 shows the hyperparameters for TriLM and FloatLM's transformer architecture and their learning rate. We set Adam β are set to (0.9, 0.95) for both families of models and all the reported runs are trained to 2048 sequence length. FloatLM and TriLM are respectively trained with batch sizes of $2M$ and $1M$ tokens respectively.

Params	Hidden	GLU	Heads	Layers	MP	FloatLM LR	TriLM LR
99.74M (99M)	512	1280	8	16	1	$4.0 * 10^{-4}$	$2.4 * 10^{-3} \rightarrow 1.5 * 10^{-3}$
190.0M (190M)	768	2048	12	16	1	$4.0 * 10^{-4}$	$2.4 * 10^{-3} \rightarrow 1.5 * 10^{-3}$
392.4M (390M)	1024	2560	16	24	1	$3.0 * 10^{-4}$	$1.8 * 10^{-3} \rightarrow 1.2 * 10^{-3}$
569.2M (560M)	1280	3072	20	24	1	$2.8 * 10^{-4}$	$1.6 * 10^{-3} \rightarrow 1.1 * 10^{-3}$
834.0M (830M)	1536	4096	24	24	1	$2.5 * 10^{-4}$	$1.5 * 10^{-3} \rightarrow 1.0 * 10^{-3}$
1.149B (1.1B)	1792	5120	28	24	2	$2.2 * 10^{-4}$	$1.3 * 10^{-3} \rightarrow 9.0 * 10^{-4}$
1.515B (1.5B)	2048	6144	32	24	2	$2.0 * 10^{-4}$	$1.2 * 10^{-3} \rightarrow 8.0 * 10^{-4}$
2.461B (2.4B)	2304	7680	36	30	3	$2.0 * 10^{-4}$	$1.2 * 10^{-3} \rightarrow 8.0 * 10^{-4}$
3.989B (3.9B)	3072	9216	24	30	6	$1.5 * 10^{-4}$	$1.2 * 10^{-3} \rightarrow 8.0 * 10^{-4}$

Table 3: Hyperparameters across model sizes for TriLM and FloatLM.

A.5 Optimization Schedule

In this section, we ablate the two interventions in a vanilla linear decay learning rate scheduling with warmup and weight decay (L2 Regularization). (1) *Peak LR* - at roughly the halfway point, we reduce the peak learning rate. (2) *L2 Reg.* - at roughly two-thirds of the training, we remove the weight decay regularization as ternarization provides sufficient regularization (Courbariaux et al., 2016b).

Params	99M	190M	390M	560M	830M	1.1B	1.5B	2.4B	3.9B
FloatLM	1.60	3.05	6.28	9.11	13.34	18.39	24.23	39.38	63.83
QuantLM 8-Bit	1.21	2.14	3.96	5.58	7.91	10.64	13.77	21.55	34.39
QuantLM 6-Bit	1.11	1.92	3.38	4.70	6.55	8.70	11.15	17.09	27.03
QuantLM 4-Bit	1.03	1.72	2.88	3.93	5.36	7.00	8.86	13.18	20.59
QuantLM 3-Bit	0.98	1.60	2.59	3.49	4.68	6.03	7.55	10.95	16.91
TriLM	0.90	1.42	2.11	2.76	3.55	4.42	5.36	7.23	10.76

Table 4: Sizes in bits (*10^9) for Spectra suite of LLMs across varying parameter counts.

Figure 9 demonstrates the ablation run performed for a 1.1B parameter model on 100B tokens with both, only one and neither of these interventions.

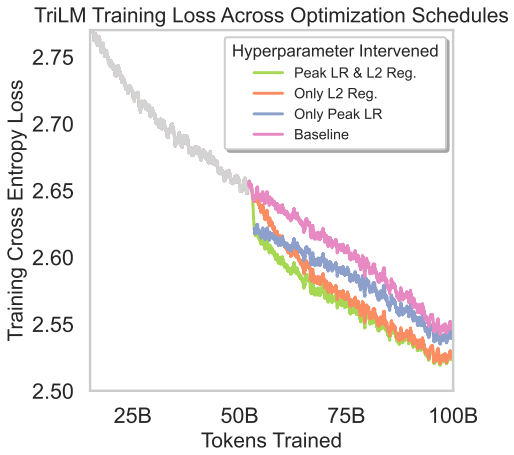


Figure 9: Training loss for a 1.1B parameter TriLM, across different optimization schedules. We intervene for combinations of two hyperparameters peak learning rate and L2 regularization. Intervention for both hyperparameters given best training loss.

Among these four runs, we notice the lowest final training loss when both, the L2 Regularization and Peak LR are intervened, closely followed only L2 Regularization (at 1/2 and 2/3) being intervened and then only Peak LR being intervened. Dropping the peak LR at the halfway point leads to a quick sharp drop in training loss. Similar phenomena have also been observed in schedules with small episodes of fast learning rate decaying like MiniCPM (Hu et al., 2024). On the other hand, removing L2 regularization, or weight decay, leads to accelerated convergence, which can even mostly have the same effect as lowering peak LR leading to a quick drop in loss. These relative training loss observation at 100B tokens also go hand in hand with relative downstream performance across commonsense and reasoning tasks, which are listed in Table 16 and 15. Thus, we fix the TriLM optimization schedule where we drop in the peak learning rate at the halfway mark and the weight decay is removed at the two-thirds mark.

A.6 Known Implementation Artifacts

Similar to BitNet (Wang et al., 2023), our models exhibit artifacts resulting from model parallelism. A key issue arises when computing the scale, γ, across the entire weight matrix, which is sharded across multiple devices. This process introduces a significant communication overhead due to the all-reduce operations. In our implementation, we address this by computing the scales over the portion of the weight matrix local to each device. Consequently, during inference with TriLM models, scales are computed independently within each model parallel group. Importantly, this modification has a negligible impact on the bits per parameter, amounting to less than 10^{-5}, even at the highest model parallelism level of 6 for our largest model.

Given that we train in FP16, some artifacts are expected as a result of this training method. However, we do not anticipate significant performance differences when comparing mixed precision training with BF16 or even FP32. This expectation is based on the observation that the lowest loss scales recorded during our runs were consistently at or above the recommended value of 128 (Micikevicius et al., 2018) (refer to Table 5).

Model	Min. Loss-Scale	# Skipped Batches	# Skipped Tokens
FloatLM 99M	256.0	181	0.37B
TriLM 99M	1024.0	303	0.33B
FloatLM 190M	512.0	168	0.35B
TriLM 190M	512.0	305	0.33B
FloatLM 390M	1024.0	170	0.35B
TriLM 390M	512.0	312	0.34B
FloatLM 560M	256.0	164	0.33B
TriLM 560M	512.0	294	0.32B
FloatLM 830M	2048.0	175	0.36B
TriLM 830M	128.0	307	0.33B
FloatLM 1.1B	2048.0	158	0.32B
TriLM 1.1B	512.0	306	0.33B
FloatLM 1.5B	256.0	170	0.35B
TriLM 1.5B	512.0	318	0.34B
FloatLM 2.4B	1024.0	165	0.34B
TriLM 2.4B	256.0	294	0.32B
FloatLM 3.9B	256.0	164	0.34B
TriLM 3.9B	128.0	309	0.33B

Table 5: Final loss-scale and number of batches skipped across TriLM and FloatLM training runs - We are able to maintain above the recommended loss scales of 128 for mixed precision training (Micikevicius et al., 2018).

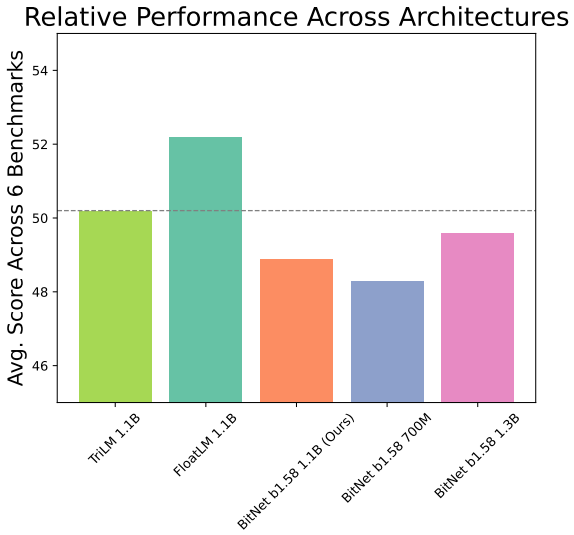


Figure 10: Performance across various architectures - TriLM 1.1B, FloatLM 1.1B, BitNet b1.58 1.1B (our replication) along with reported scores of BitNet b1.58 at 700M and 1.3B params. Scores are averaged across 6 common sense and reasoning benchmarks, mentioned in Table 16 and 15.

A.7 Differences from BitNet Architecture

TriLM differs from BitNet b1.58 in several ways for better performance as well as for fairer comparison with FloatLMs. Adopting the GPT-3's Pre-Normalization approach as outlined by (Brown et al., 2020b), normalization is applied prior to each linear layer. This method has proven essential for

maintaining stable training under FP16 precision (Wang et al., 2023). Consequently, normalization occurs twice within each transformer layer: once at the input representations to the attention sub-layer and again at the input representations to the Gated MLP sub-layer. This approach contrasts with BitNet, where activation or intermediate representations are normalized, scaled, and quantized to 8 bits before each linear layer, which occurs between 4 to 7 times per transformer layer depending on the specific implementation. Furthermore, TriLM employs RMSNorm with a scale parameter over the parameterless RMSNorm.

Figure 10 shows the commonsense and reasoning performance of TriLM 1.1B, FloatLM 1.1B and our replication of BitNet b1.58's architecture at 1.1B scale, along with the reported performance for BitNet b1.58 700M and 1.3B. All these models have been trained for 100B tokens. Our BitNet replication achieves performance between the 700M and 1.3B models. However, all the BitNet models, including the larger 1.3B parameter model perform worse than TriLM 1.1B. It should be noted that at this 1.1B scale, TriLMs do not achieve parity with FloatLMs of the same parameter count. Table 16 and 15lists the detailed performance of these models across common sense benchmarks.

A.8 Spectra Suite of LLMs: Parameter Scaling and Bitwidth Variations

Figure 11 illustrates the Spectra LM suite spanning two key dimensions: bitwidth and the number of parameters. The suite includes the TriLM, FloatLM, and QuantLM model families (in 3, 4, 6, and 8 bits). The suite features 9 different parameter scales ranging from 99M to 3.9B parameters. In total, the suite comprises 54 models.

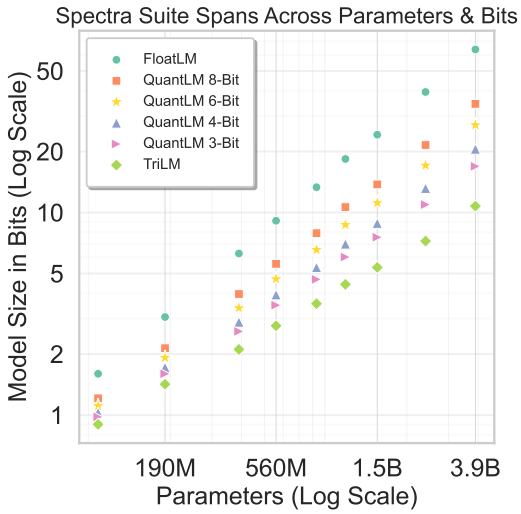


Figure 11: The Spectra Suite spans across two dimensions: parameters and bitwidth. Each point corresponds to a language model in the suite.

A.9 Details on the Selection of Hyperparameters

Model architecture hyperparameters. To ensure stable training and mitigate risks of loss spikes or slow convergence, we carefully selected key architectural hyperparameters such as layer normalization techniques and other training parameters. To optimize hardware efficiency, we padded the vocabulary size and rounded the hidden dimensions to the nearest power of two, facilitating alignment with accelerator constraints. Given computational limitations, our scaling and coefficient analyses were conducted with nine data points within the 4-billion-parameter range, each trained on datasets containing 300 billion tokens. These constraints directly influenced the design choices for the number of layers, hidden dimensions, embedding size, feedforward network dimensions, and attention heads across model variants.

Training hyperparameters. We adopted a rigorous evaluation-driven approach to refine training hyperparameters, encompassing model initialization, optimizers, and learning rate schedules. This

methodology mirrors the training-time evaluations utilized in other model suites such as those by Biderman et al. (2023) and Groeneveld et al. (2024). To systematically explore the hyperparameter space, we employed a grid search over configurations, including learning rate, weight decay, batch size, and optimizer variants. Evaluations are conducted at different stages of training, from 4 billion up to 20 billion tokens, providing continuous and early-stage feedback on model performance. The key metrics evaluated include validation loss, commonsense reasoning, knowledge-based task performance, and toxicity assessments, as outlined in the paper.

A.10 Perplexity for Increasing Training Tokens in TriLM Models

Impact of Training Tokens on Perplexity in TriLM Models. The performance of language models generally improves with an increased number of training tokens, as demonstrated in prior work (Hoffmann et al., 2022; Kaplan et al., 2020). This trend is clearly reflected in the validation perplexity of our TriLM models across varying training token counts. The results, summarized in Table 6, highlight the critical role of scaling up training data to reduce perplexity. Notably, the larger model—TriLM 560M—consistently achieves lower perplexity at all token scales. This reinforces the scaling law relationship among larger model sizes, more extensive training data, and reduced validation perplexity, mirroring the scaling laws observed for FloatLMs.

Training Tokens	Perplexity of TriLM 99M	Perplexity of TriLM 560M
50B	27.11	15.48
150B	26.30	14.50
300B	25.70	14.01

Table 6: Perplexity comparison for TriLM models with 99M and 560M parameters across different training token counts.

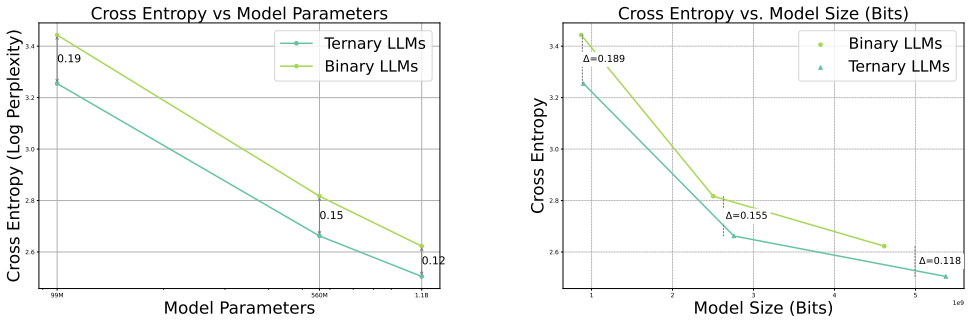
Impact of Token-to-Parameter. The reduction in validation perplexity, even after training on over 3000 times the number of tokens relative to the number of parameters, is particularly evident in the smallest model (99M) of our suite. As shown in Table 6, the 99M model continues to demonstrate improvement with up to 300B tokens, suggesting that TriLM remains effective even at higher training token-to-parameter ratios. Extrapolating from this trend, our largest model (3.9B) could theoretically train on up to 11.8 trillion tokens without reaching convergence. This scale is comparable to the magnitude of training tokens used for LLaMA 3, a state-of-the-art open-source language model AI@Meta (2024). However, due to resource constraints, training at such a scale remains a direction for future work.

B BINARY VS TERNARY LARGE LANGUAGE MODELS

In this section, we will comprehensively compare Binary Large Language Models (BiLMs) with Ternary Large Language Models (TriLMs). We will start by describing BiLMs, followed by studying scaling laws and presenting results on various benchmarks, as well as comparisons with TriLMs across parameter count and model size (in bits).

B.1 BILM: BINARY LARGE LANGUAGE MODEL

In Binary Large Language Models (BiLMs), the weights of the linear layers are represented by binary values of -1 or 1, with an accompanying floating-point scaling factor, similar to the method employed in TriLMs. Comprehensive formal descriptions of the forward pass, backward pass, and inference time calculations are provided in Appendix (§A). We have trained three BiLM models of distinct sizes: 99M, 560M, and 1.1B parameters. These models were trained on the same dataset and in the same sequence as the TriLMs, adhering to the identical optimization schedule detailed in Appendix A.5.



(a) Vs. Params

(b) Vs. Size (in Bits)

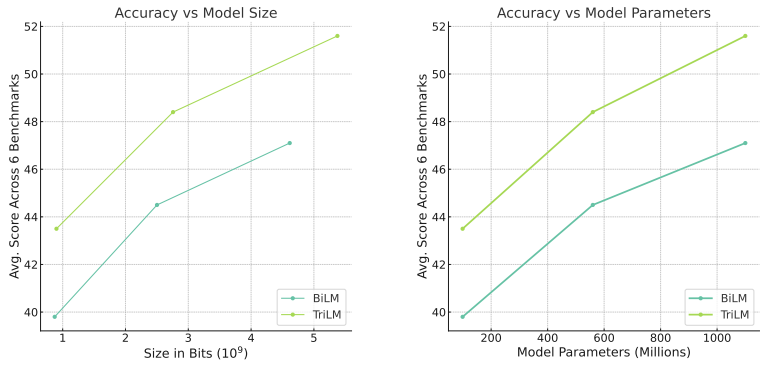
Figure 12: Final Validation loss across size (measure in bits) and parameters.

B.2 SCALING BINARY VS TERNARY MODEL

Figures 12a and 12b show the final validation loss across model sizes (in bits) and parameter counts, respectively for the three distinct sizes previously mentioned. At the Billion+ model scale, Ternary Models appear to be preferable in terms of both the number of parameters and model size (in bits). However, the gap seems to be narrowing, which suggests that BiLMs have the potential to be competitive with TriLMs at higher parameter counts (100B+). Therefore, we decide to only scale TriLMs further to study the scaling laws of FloatLMs vs TriLMs up to 3.9B parameters.

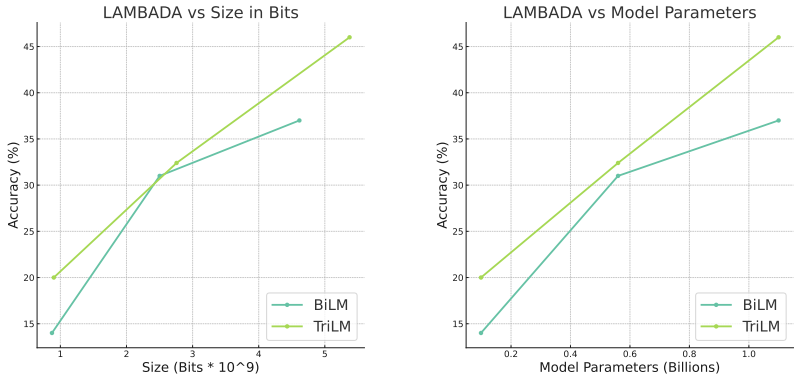
B.3 RESULTS

We conducted a comprehensive benchmark analysis of Binary Large Language Models (BILMs) across three key dimensions: commonsense and reasoning tasks, knowledge-based tasks, and toxicity evaluation, as detailed in Tables 7, 810, and 17



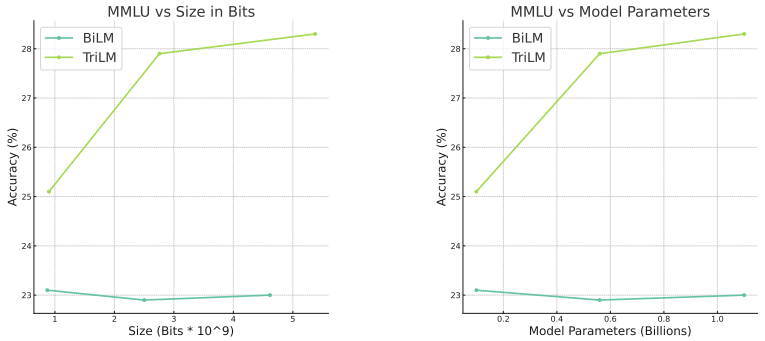
(a) vs. Size in C & R (b) vs. Params in C & R

Figure 13: Performance of ternary TriLMs and BiLMs models on commonsense and Reasoning and MMLUs tasks across Size (Bits) and Parameters. Refer to Tables 7 and 8 for details.



(a) vs. Size in LAMBADA (b) vs. Params in LAMBADA

Figure 14: Performance of ternary TriLMs and BiLMs models on LAMBADA tasks across Size (Bits) and Parameters. Refer to Tables 7, and 8 for details.



(a) vs. Size in MMLU (b) vs. Params in MMLU

Figure 15: Performance of ternary TriLMs and BiLMs models on MMLU across Size (Bits) and Parameters. Refer to Tables 17 for details.

C SCALING LAW

In this section, we provide additional insights into the scaling fits discussed in Section 4.3. In addition to fitting a power law with an offset, we also explore a standard power law following Kaplan et al. (2020). Our findings suggest that the standard power law fits are slightly less precise than those incorporating an offset term. However, both models indicate a decreasing difference in validation loss as the number of parameters (N) increases.

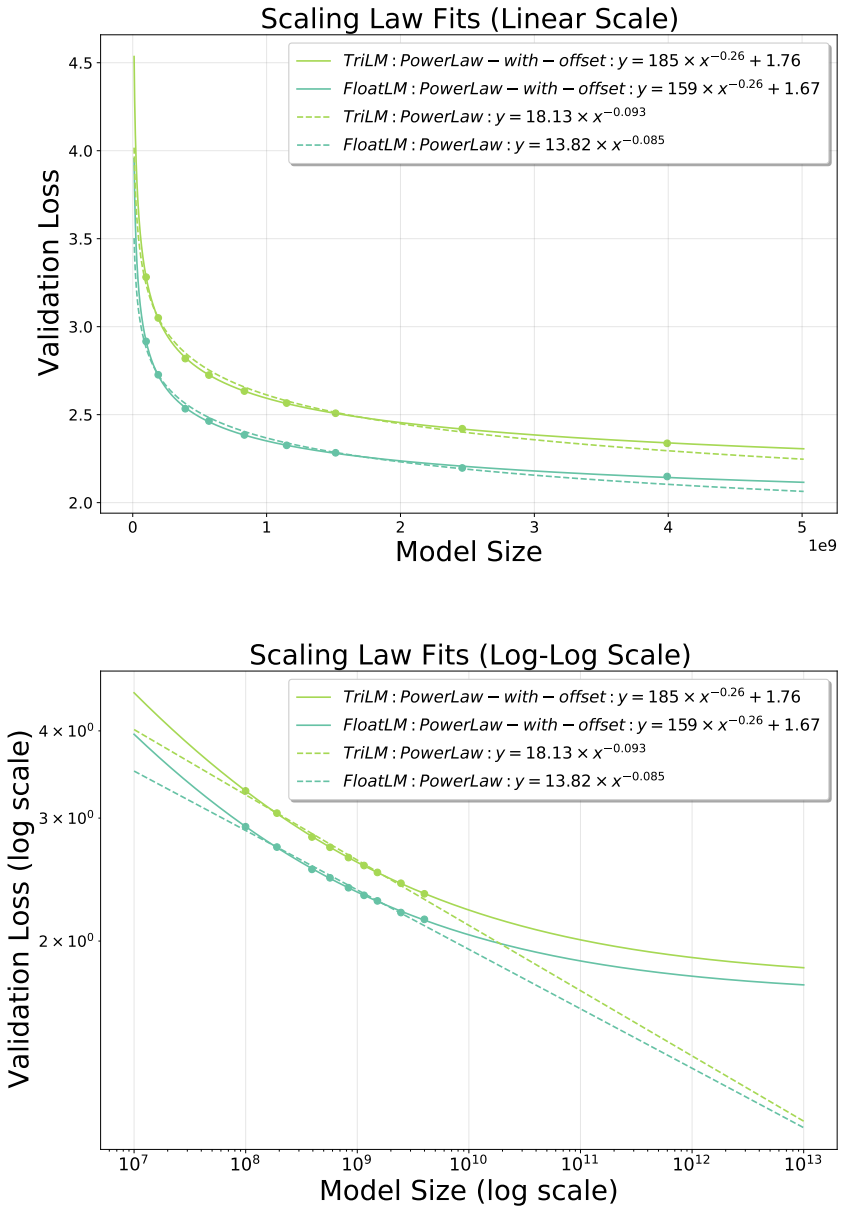


Figure 16: Comparison of Power Law and Power Law-with-offset Fits for TriLM and FloatLM.

As shown in Figure 17, using the scaling equations for TriLMs and FloatLMs, we derive the relationship between parameter count and the percentage difference in validation loss relative to FloatLMs. We observe that at 330B and 15.6B parameters, the validation losses for TriLMs are

within 6% and 7% of FloatLMs' validation losses, respectively. This indicates that TriLMs are likely to closely match the performance of FloatLMs at larger scales.

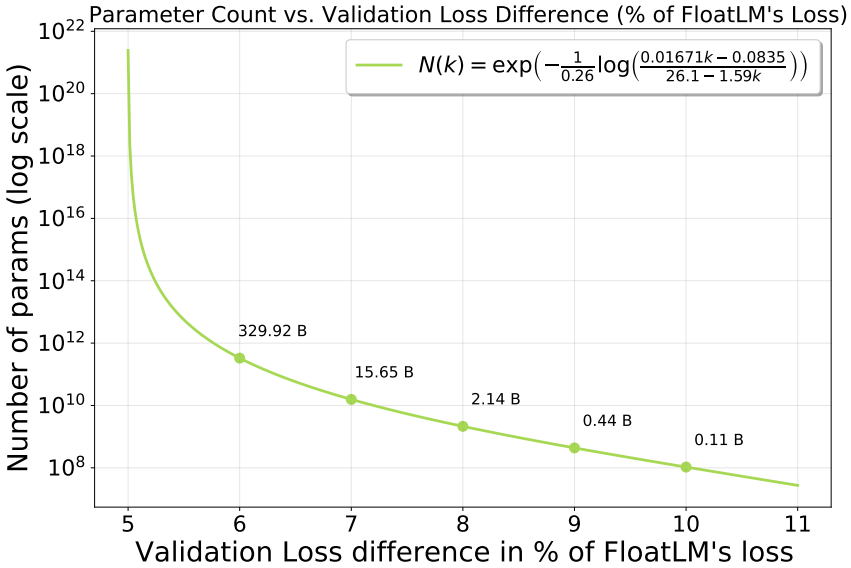


Figure 17: Comparison of Power Law and Power Law-with-offset Fits for TriLM and FloatLM.

D BENCHMARK DETAILS

We benchmark TriLM, FloatLM and QuantLM across Knowledge, Commonsense, Reasoning and Toxicity benchmarks. We average our scores across 3 different 'seeds' by preparing three different QuantLM models quantized using different calibration sets. We also add Pythia (deduplicated with consistent $2M$ batch size across families) suite of models (70M to 2.8B params) and BitNet b.158 performance scores from their paper for comparison. We use the LM Evaluation Harness (Gao et al., 2023) to benchmark.

D.1 COMMONSENSE AND REASONING

We report commonsense and reasoning benchmark scores across 6 benchmarks previously considered by BitNet b.158 in Table 7, 8 and rest in Table 10. Each is considered in a zero-shot setting. Following are the details of each of the benchmarks considered:

- **ARC Challenge and Easy**: (Clark et al., 2018) ARC dataset comprises 7787 multiple-choice science questions divided into two sets: Challenge and Easy. We calculate accuracy and normalised accuracy across both of these sets.
- **BoolQ**: (Clark et al., 2019) BoolQ is a reading comprehension dataset consisting of naturally occurring yes/no questions. We calculate the accuracy of this task.
- **HellaSwag**: (Zellers et al., 2019) HellaSWAG is a dataset of multiple choice questions for testing grounded commonsense. The incorrect options are generated through Adversarial Filtering (AF) to fool machines but not humans. We calculate the accuracy and normalized accuracy on this task.
- **WinoGrande**: (Sakaguchi et al., 2021) WinoGrande is a collection of 44k problems for testing commonsense reasoning formulated as a fill-in-a-blank task with binary options. We report the accuracy on this task.
- **PIQA**: (Bisk et al., 2019) Physical Interaction Question Answering (PIQA) is a physical commonsense reasoning benchmark dataset to test the physical knowledge of language models. We calculate the accuracy and normalized accuracy on this task.
- **LAMBADA OpenAI**: (Paperno et al., 2016) LAMBADA is a dataset to evaluate text understanding by next-word prediction. It is a collection of narrative passages BooksCorpus To succeed on LAMBADA, models must integrate broader discourse information, not solely rely on local context. We calculate the perplexity and the accuracy of the model on this task.
- **LogiQA**: (Liu et al., 2021) LogiQA is a dataset for testing human logical reasoning. It contains questions spanning multiple types of deductive reasoning. We calculate the accuracy and normalized accuracy on this task.

D.2 KNOWLEDGE

We report performance on SciQ, TriviaQA in Tables 10, 17 and 18. Each is considered in a zero-shot setting. Following are the details of each of the benchmarks considered:

The knowledge-based evaluation included the following tasks:

- **SciQ**: (Welbl et al., 2017) The SciQ dataset contains multiple-choice questions with 4 answer options from crowd-sourced science exams. The questions range from Physics, Chemistry and Biology and several other fields. We calculate the accuracy and length normalized accuracy on this task.
- **TriviaQA**: (Joshi et al., 2017) TriviaQA is a reading comprehension dataset containing question-answer-evidence triples. We calculate the exact match accuracy on this task.
- **MMLU** (Hendrycks et al., 2021): The benchmark aims to assess the knowledge gained during pretraining by evaluating models solely in zero-shot and few-shot scenarios. It spans 57 subjects, including STEM fields, humanities, social sciences, and more.

Models	Arc Challenge		Arc Easy		BoolQ
	Acc Norm.	Acc	Acc Norm.	Acc	Acc
Pythia 70M	22.0± 1.2	22.1± 1.2	24.8± 0.9	24.8± 0.9	38.5± 0.9
FloatLM 99M	23.8± 1.2	19.9± 1.2	39.1± 1.0	45.1± 1.0	58.2± 0.9
QuantLM 99M 8-Bit	23.8± 1.2	19.6± 1.2	39.4± 1.0	45.3± 1.0	58.5± 0.9
QuantLM 99M 6-Bit	23.2± 1.2	19.7± 1.2	38.8± 1.0	44.8± 1.0	58.9± 0.9
QuantLM 99M 4-Bit	22.6± 1.2	18.0± 1.1	37.1± 1.0	41.7± 1.0	52.2± 0.9
QuantLM 99M 3-Bit	23.2± 1.2	19.5± 1.2	34.8± 1.0	36.1± 1.0	48.4± 0.9
TriLM 99M	24.1± 1.3	19.1± 1.1	36.6± 1.0	39.8± 1.0	61.3± 0.9
Binary 99M	20.8± 1.2	18.3± 1.1	35.8± 0.9	40.1± 1.0	61.0± 0.8
Pythia 160M	23.8± 1.2	23.1± 1.2	26.7± 0.9	26.6± 0.9	38.3± 0.9
FloatLM 190M	24.1± 1.3	20.5± 1.2	43.0± 1.0	48.4± 1.0	59.1± 0.9
QuantLM 190M 8-Bit	24.4± 1.3	20.3± 1.2	43.0± 1.0	48.5± 1.0	59.3± 0.9
QuantLM 190M 6-Bit	23.8± 1.2	20.0± 1.2	42.0± 1.0	48.0± 1.0	59.1± 0.9
QuantLM 190M 4-Bit	25.2± 1.3	19.9± 1.2	26.5± 0.9	26.8± 0.9	40.9± 0.9
QuantLM 190M 3-Bit	22.5± 1.2	19.4± 1.2	37.1± 1.0	39.7± 1.0	56.5± 0.9
TriLM 190M	23.0± 1.2	19.5± 1.2	39.6± 1.0	43.9± 1.0	46.8± 0.9
FloatLM 390M	24.7± 1.3	21.3± 1.2	46.5± 1.0	51.0± 1.0	54.7± 0.9
QuantLM 390M 8-Bit	24.6± 1.3	21.2± 1.2	46.6± 1.0	51.0± 1.0	54.6± 0.9
QuantLM 390M 6-Bit	24.8± 1.3	21.5± 1.2	46.8± 1.0	51.8± 1.0	55.3± 0.9
QuantLM 390M 4-Bit	25.1± 1.3	21.3± 1.2	45.2± 1.0	49.6± 1.0	50.8± 0.9
QuantLM 390M 3-Bit	24.9± 1.3	21.5± 1.2	41.6± 1.0	43.6± 1.0	56.3± 0.9
TriLM 390M	24.5± 1.3	21.2± 1.2	44.1± 1.0	48.6± 1.0	55.1± 0.9
Pythia 410M	24.7± 1.3	21.2± 1.2	45.7± 1.0	51.6± 1.0	60.0± 0.9
FloatLM 560M	26.5± 1.3	23.9± 1.2	48.4± 1.0	54.4± 1.0	57.9± 0.9
QuantLM 560M 8-Bit	26.5± 1.3	23.6± 1.2	48.3± 1.0	54.1± 1.0	57.6± 0.9
QuantLM 560M 6-Bit	26.0± 1.3	23.5± 1.2	47.6± 1.0	54.2± 1.0	57.3± 0.9
QuantLM 560M 4-Bit	25.9± 1.3	23.0± 1.2	46.3± 1.0	52.4± 1.0	58.8± 0.9
QuantLM 560M 3-Bit	24.0± 1.2	21.2± 1.2	42.3± 1.0	45.8± 1.0	59.0± 0.9
TriLM 560M	25.7± 1.3	21.0± 1.2	45.5± 1.0	50.2± 1.0	57.3± 0.9
Binary 560M	24.6± 1.2	20.2± 1.1	41.9± 1.0	47.8± 1.0	61.5± 0.8
FloatLM 830M	28.0± 1.3	24.5± 1.3	51.6± 1.0	57.3± 1.0	61.0± 0.9
QuantLM 830M 8-Bit	28.2± 1.3	25.1± 1.3	51.7± 1.0	57.3± 1.0	60.9± 0.9
QuantLM 830M 6-Bit	27.6± 1.3	24.7± 1.3	51.6± 1.0	57.7± 1.0	61.3± 0.9
QuantLM 830M 4-Bit	27.6± 1.3	23.3± 1.2	50.5± 1.0	56.2± 1.0	58.1± 0.9
QuantLM 830M 3-Bit	27.1± 1.3	22.7± 1.2	46.8± 1.0	50.5± 1.0	56.3± 0.9
TriLM 830M	25.3± 1.3	22.5± 1.2	48.7± 1.0	54.2± 1.0	60.4± 0.9
Pythia 1B	27.0± 1.3	24.4± 1.3	49.0± 1.0	57.0± 1.0	60.8± 0.9
FloatLM 1.1B	29.1± 1.3	26.1± 1.3	54.0± 1.0	60.4± 1.0	62.9± 0.8
QuantLM 1.1B 8-Bit	28.9± 1.3	26.1± 1.3	54.1± 1.0	60.2± 1.0	62.6± 0.8
QuantLM 1.1B 6-Bit	29.8± 1.3	25.5± 1.3	54.3± 1.0	60.2± 1.0	62.9± 0.8
QuantLM 1.1B 4-Bit	30.3± 1.3	26.0± 1.3	53.6± 1.0	59.0± 1.0	61.3± 0.9
QuantLM 1.1B 3-Bit	29.2± 1.3	27.0± 1.3	48.9± 1.0	55.0± 1.0	62.1± 0.8
TriLM 1.1B	26.5± 1.3	24.6± 1.3	49.8± 1.0	56.3± 1.0	59.1± 0.9
Binary 1.1B	24.8± 1.3	22.3± 1.2	46.1± 1.0	52.7± 1.0	56.3± 0.9
Pythia 1.4B	28.7± 1.3	26.0± 1.3	54.0± 1.0	60.4± 1.0	63.2± 0.8
FloatLM 1.5B	29.7± 1.3	26.2± 1.3	56.4± 1.0	62.6± 1.0	63.2± 0.8
QuantLM 1.5B 8-Bit	29.8± 1.3	26.0± 1.3	56.6± 1.0	62.4± 1.0	63.3± 0.8
QuantLM 1.5B 6-Bit	30.1± 1.3	26.0± 1.3	56.8± 1.0	62.2± 1.0	63.4± 0.8
QuantLM 1.5B 4-Bit	29.4± 1.3	26.9± 1.3	55.2± 1.0	60.4± 1.0	62.5± 0.8
QuantLM 1.5B 3-Bit	27.8± 1.3	25.2± 1.3	49.7± 1.0	54.8± 1.0	53.7± 0.9
TriLM 1.5B	28.2± 1.3	24.7± 1.3	53.1± 1.0	59.0± 1.0	54.1± 0.9
FloatLM 2.4B	32.7± 1.4	30.1± 1.3	60.5± 1.0	65.5± 1.0	62.1± 0.8
QuantLM 2.4B 8-Bit	32.6± 1.4	30.0± 1.3	60.3± 1.0	65.7± 1.0	62.1± 0.8
QuantLM 2.4B 6-Bit	32.7± 1.4	30.6± 1.3	60.4± 1.0	65.4± 1.0	62.0± 0.8
QuantLM 2.4B 4-Bit	33.3± 1.4	30.8± 1.3	59.6± 1.0	64.1± 1.0	59.0± 0.9
QuantLM 2.4B 3-Bit	29.7± 1.3	28.4± 1.3	54.2± 1.0	58.4± 1.0	55.7± 0.9
TriLM 2.4B	29.9± 1.3	29.5± 1.3	58.0± 1.0	63.8± 1.0	64.4± 0.8
FloatLM 3.9B	34.6± 1.4	32.1± 1.4	63.0± 1.0	68.3± 1.0	65.9± 0.8
QuantLM 3.9B 8-Bit	34.6± 1.4	31.9± 1.4	63.0± 1.0	68.1± 1.0	65.4± 0.8
QuantLM 3.9B 6-Bit	35.1± 1.4	32.1± 1.4	63.3± 1.0	68.0± 1.0	65.6± 0.8
QuantLM 3.9B 4-Bit	34.7± 1.4	32.9± 1.4	61.2± 1.0	68.3± 1.0	65.4± 0.8
QuantLM 3.9B 3-Bit	32.1± 1.4	29.3± 1.3	55.5± 1.0	62.1± 1.0	60.0± 0.9
TriLM 3.9B	35.3± 1.4	31.9± 1.4	60.8± 1.0	66.0± 1.0	66.5± 0.8

Table 7: Spectra Suite Performance (Part 1): Arc Challenge, Arc Easy, and BoolQ. Additionally, we also include scores on the Pythia LLM suite.

Models	HellaSwag		PIQA		WinoGrande	Avg (HellaSwag, PIQA, WinoGrande,
	Acc Norm.	Acc	Acc Norm.	Acc	Acc	Arc Easy, Arc Challenge, and BoolQ)
Pythia 70M	25.1± 0.4	25.1± 0.4	49.8± 1.2	49.9± 1.2	49.1± 1.4	34.9
FloatLM 99M	31.6± 0.5	29.1± 0.5	62.8± 1.1	63.2± 1.1	50.2± 1.4	44.3
QuantLM 99M 8-Bit	31.7± 0.5	29.0± 0.5	62.6± 1.1	63.0± 1.1	50.0± 1.4	44.3
QuantLM 99M 6-Bit	31.7± 0.5	29.2± 0.5	62.8± 1.1	63.1± 1.1	50.2± 1.4	44.3
QuantLM 99M 4-Bit	31.0± 0.5	28.9± 0.5	62.2± 1.1	60.9± 1.1	50.4± 1.4	42.6
QuantLM 99M 3-Bit	29.2± 0.5	27.7± 0.4	57.2± 1.2	58.2± 1.2	49.2± 1.4	40.3
TriLM 99M	28.4± 0.5	27.6± 0.4	60.1± 1.1	60.4± 1.1	50.7± 1.4	43.5
Binary 99M	27.7± 0.4	27.2± 0.4	59.2± 1.1	59.2± 1.1	48.8± 1.4	39.8
Pythia 160M	25.1± 0.4	25.0± 0.4	53.1± 1.2	53.1± 1.2	47.3± 1.4	35.7
FloatLM 190M	36.6± 0.5	31.4± 0.5	65.6± 1.1	64.8± 1.1	51.9± 1.4	46.7
QuantLM 190M 8-Bit	36.5± 0.5	31.4± 0.5	65.6± 1.1	64.8± 1.1	51.7± 1.4	46.8
QuantLM 190M 6-Bit	36.3± 0.5	31.5± 0.5	65.6± 1.1	64.3± 1.1	51.9± 1.4	46.4
QuantLM 190M 4-Bit	26.0± 0.4	25.7± 0.4	49.3± 1.2	51.7± 1.2	51.0± 1.4	36.5
QuantLM 190M 3-Bit	32.0± 0.5	28.8± 0.5	58.1± 1.2	58.7± 1.1	50.1± 1.4	42.7
TriLM 190M	31.6± 0.5	29.0± 0.5	62.0± 1.1	62.3± 1.1	51.7± 1.4	42.4
FloatLM 390M	44.4± 0.5	35.7± 0.5	68.7± 1.1	68.4± 1.1	51.8± 1.4	48.5
QuantLM 390M 8-Bit	44.5± 0.5	35.7± 0.5	68.8± 1.1	68.6± 1.1	52.6± 1.4	48.6
QuantLM 390M 6-Bit	44.2± 0.5	35.6± 0.5	69.0± 1.1	68.4± 1.1	53.0± 1.4	48.9
QuantLM 390M 4-Bit	43.4± 0.5	35.1± 0.5	68.1± 1.1	68.3± 1.1	53.7± 1.4	47.7
QuantLM 390M 3-Bit	39.5± 0.5	32.9± 0.5	63.8± 1.1	63.2± 1.1	53.0± 1.4	46.5
TriLM 390M	37.9± 0.5	32.0± 0.5	64.7± 1.1	65.0± 1.1	52.2± 1.4	46.4
Pythia 410M	40.3± 0.5	33.8± 0.5	67.2± 1.1	66.3± 1.1	53.5± 1.4	48.6
FloatLM 560M	47.6± 0.5	37.7± 0.5	68.8± 1.1	69.0± 1.1	53.7± 1.4	50.5
QuantLM 560M 8-Bit	47.6± 0.5	37.7± 0.5	68.9± 1.1	68.9± 1.1	53.8± 1.4	50.4
QuantLM 560M 6-Bit	47.6± 0.5	37.7± 0.5	68.7± 1.1	68.8± 1.1	53.5± 1.4	50.1
QuantLM 560M 4-Bit	46.7± 0.5	37.0± 0.5	67.8± 1.1	67.1± 1.1	53.1± 1.4	49.8
QuantLM 560M 3-Bit	41.7± 0.5	33.4± 0.5	63.5± 1.1	63.2± 1.1	49.7± 1.4	46.7
TriLM 560M	41.5± 0.5	33.8± 0.5	67.2± 1.1	67.5± 1.1	53.1± 1.4	48.4
Binary 560M	36.4± 0.4	31.2± 0.4	64.6± 1.1	64.2± 1.1	52.8± 1.4	44.5
FloatLM 830M	51.3± 0.5	40.1± 0.5	71.4± 1.1	71.7± 1.1	56.4± 1.4	53.3
QuantLM 830M 8-Bit	51.4± 0.5	40.1± 0.5	71.2± 1.1	71.7± 1.1	55.9± 1.4	53.2
QuantLM 830M 6-Bit	51.5± 0.5	40.2± 0.5	71.3± 1.1	71.8± 1.0	56.2± 1.4	53.2
QuantLM 830M 4-Bit	50.2± 0.5	39.2± 0.5	70.6± 1.1	71.1± 1.1	56.0± 1.4	52.2
QuantLM 830M 3-Bit	45.5± 0.5	35.9± 0.5	66.1± 1.1	66.6± 1.1	53.5± 1.4	49.2
TriLM 830M	46.0± 0.5	36.8± 0.5	68.2± 1.1	68.4± 1.1	55.6± 1.4	50.7
Pythia 1B	47.2± 0.5	37.7± 0.5	69.3± 1.1	70.8± 1.1	53.2± 1.4	51.1
FloatLM 1.1B	55.2± 0.5	42.6± 0.5	72.2± 1.0	71.3± 1.1	56.3± 1.4	54.9
QuantLM 1.1B 8-Bit	55.2± 0.5	42.6± 0.5	72.1± 1.0	71.2± 1.1	56.2± 1.4	54.8
QuantLM 1.1B 6-Bit	54.9± 0.5	42.6± 0.5	71.9± 1.0	71.2± 1.1	56.1± 1.4	55.0
QuantLM 1.1B 4-Bit	54.9± 0.5	42.0± 0.5	71.6± 1.1	70.4± 1.1	54.8± 1.4	54.4
QuantLM 1.1B 3-Bit	51.3± 0.5	39.4± 0.5	69.4± 1.1	68.4± 1.1	54.8± 1.4	52.6
TriLM 1.1B	49.1± 0.5	38.8± 0.5	69.8± 1.1	69.3± 1.1	55.5± 1.4	51.6
Binary 1.1B	43.4± 0.5	35.1± 0.4	66.9± 1.1	68.3± 1.1	55.3± 1.4	47.1
Pythia 1.4B	52.0± 0.5	40.4± 0.5	70.8± 1.1	70.6± 1.1	57.1± 1.4	54.3
FloatLM 1.5B	57.8± 0.5	44.3± 0.5	73.9± 1.0	73.1± 1.0	59.4± 1.4	56.7
QuantLM 1.5B 8-Bit	57.8± 0.5	44.3± 0.5	73.7± 1.0	73.1± 1.0	59.4± 1.4	56.8
QuantLM 1.5B 6-Bit	57.5± 0.5	44.2± 0.5	74.0± 1.0	73.0± 1.0	59.7± 1.4	56.9
QuantLM 1.5B 4-Bit	56.9± 0.5	43.2± 0.5	72.7± 1.0	72.4± 1.0	57.1± 1.4	55.6
QuantLM 1.5B 3-Bit	53.7± 0.5	41.0± 0.5	70.0± 1.1	69.4± 1.1	55.0± 1.4	51.6
TriLM 1.5B	53.1± 0.5	40.9± 0.5	70.1± 1.1	70.3± 1.1	56.1± 1.4	52.5
FloatLM 2.4B	62.7± 0.5	47.1± 0.5	75.2± 1.0	74.9± 1.0	61.8± 1.4	59.2
QuantLM 2.4B 8-Bit	62.7± 0.5	47.1± 0.5	75.4± 1.0	74.9± 1.0	61.4± 1.4	59.1
QuantLM 2.4B 6-Bit	62.9± 0.5	47.0± 0.5	75.7± 1.0	74.7± 1.0	61.1± 1.4	59.1
QuantLM 2.4B 4-Bit	62.2± 0.5	46.5± 0.5	75.4± 1.0	74.5± 1.0	61.7± 1.4	58.5
QuantLM 2.4B 3-Bit	58.6± 0.5	43.5± 0.5	72.7± 1.0	70.8± 1.1	57.2± 1.4	54.7
TriLM 2.4B	59.0± 0.5	45.3± 0.5	72.6± 1.0	71.4± 1.1	59.7± 1.4	57.3
FloatLM 3.9B	66.1± 0.5	49.7± 0.5	75.8± 1.0	75.4± 1.0	62.8± 1.4	61.4
QuantLM 3.9B 8-Bit	66.0± 0.5	49.7± 0.5	75.9± 1.0	75.5± 1.0	62.9± 1.4	61.3
QuantLM 3.9B 6-Bit	65.9± 0.5	49.7± 0.5	75.5± 1.0	75.6± 1.0	62.2± 1.4	61.3
QuantLM 3.9B 4-Bit	65.0± 0.5	49.0± 0.5	75.5± 1.0	75.6± 1.0	62.7± 1.4	60.7
QuantLM 3.9B 3-Bit	61.2± 0.5	45.9± 0.5	72.6± 1.0	72.3± 1.0	59.3± 1.4	56.8
TriLM 3.9B	64.7± 0.5	48.3± 0.5	74.6± 1.0	74.4± 1.0	62.1± 1.4	60.7

Table 8: Spectra Suite Performance (Part 2): HellaSwag, PIQA, WinoGrande, and Average Scores (including Arc Easy, Arc Challenge, and BoolQ). Additionally, we include scores from the Pythia LLM suite.

Models	Arc Challenge		Arc Easy		BoolQ	HellaSwag		PIQA		WinoGrande	Avg
	Acc Norm.	Acc	Acc Norm.	Acc	Acc	Acc Norm.	Acc	Acc Norm.	Acc	Acc	
BitNet 700M	21.4		51.8		58.2	35.1		68.1		55.2	48.3
BitNet 1.3B	24.2		54.9		56.7	37.7		68.8		55.8	49.7
BitNet 3B	28.3		61.4		61.5	42.9		71.5		59.3	54.2
BitNet 3.9B	28.7		64.2		63.5	44.2		73.2		60.5	55.7

Table 9: Performance of BitNet b1.58 on ARC Challenge, ARC Easy, BoolQ, HellaSwag, PIQA, and WinoGrande. The scores are taken from (Ma et al., 2024).

D.3 Toxicity

We report toxicity-based evaluation in 17. Each is considered in a zero-shot setting.

The toxicity-based evaluation included the following tasks:

- **BBQ** (Parrish et al., 2022): The Bias Benchmark for QA (BBQ) dataset, comprises sets of questions developed by its authors, focusing on documented social biases directed towards individuals from protected classes across nine distinct social dimensions pertinent to U.S. English-speaking environments.
- **Crows Pairs** (Nangia et al., 2020): proposed a challenging dataset aimed at quantifying stereotypical biases embedded within language models, with a specific emphasis on U.S. contexts. Hosted on GitHub, this dataset serves as a crucial resource for assessing and addressing biases through paired sentences that illuminate societal stereotypes.
- **TruthfulQA** (Lin et al., 2021): A benchmark designed to evaluate the truthfulness of language models in generating responses to questions. This benchmark includes 817 questions across 38 categories, such as health, law, finance, and politics.

D.4 Perplexity on other datasets

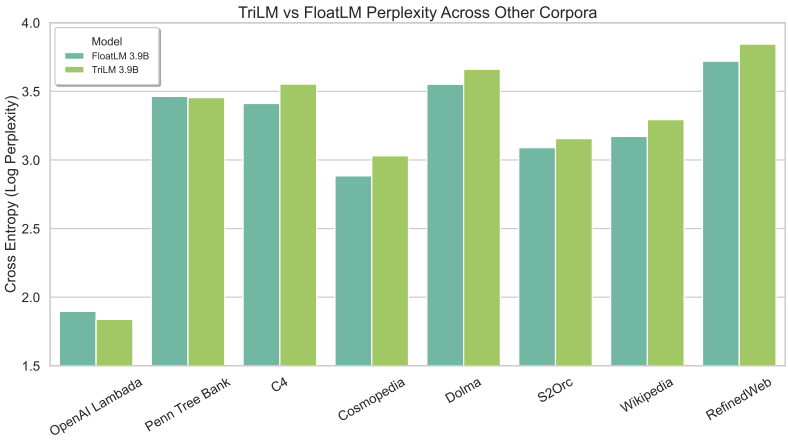


Figure 18: Cross-entropy (log perplexity) comparison between TriLM and FloatLM (both 3.9B parameters) across various datasets apart from SlimPajama.

We measure perplexity using TriLM 3.9B and FloatLM 3.9B across various other corpora than SlimPajama, which was used for training. These corpora include OpenAI Lambada, Penn Tree Bank, C4, Cosmopedia, Dolma, S2Orc, Wikipedia, and RefinedWeb. A portion of Wikipedia, C4 is included in Slim Pajama. Some other corpora like Dolma and RefinedWeb, may also have overlaps from C4, Wikipedia as well as Common Crawl.

Figure 18 demonstrates that while TriLM 3.9B is similar or better than FloatLM 3.9B on PTB and Lambada, across the other datasets, with potential overlaps with SlimPajama, it's performance is consistently worse - indicating lower capability to memorize training data as well as worse in-distribution performance, despite competitive out of distribution performance.

Models	LAMBADA		SciQ		LogiQA	
	Perp.	Acc	Acc Norm.	Acc	Acc Norm.	Acc
FloatLM 99M	85.0± 6.9	26.5± 0.6	62.9± 1.5	73.6± 1.4	27.6± 1.8	21.2± 1.6
QuantLM 99M 8-Bit	85.8± 7.0	26.6± 0.6	62.8± 1.5	73.7± 1.4	27.8± 1.8	21.0± 1.6
QuantLM 99M 6-Bit	89.9± 7.4	26.1± 0.6	61.8± 1.5	73.9± 1.4	28.1± 1.8	20.3± 1.6
QuantLM 99M 4-Bit	211.6± 17.3	16.7± 0.5	61.2± 1.5	70.7± 1.4	24.9± 1.7	20.7± 1.6
QuantLM 99M 3-Bit	4765.4± 413.0	4.5± 0.3	51.9± 1.6	57.0± 1.6	25.3± 1.7	19.8± 1.6
TriLM 99M	172.0± 8.4	20.0± 0.6	60.4± 1.5	67.6± 1.5	25.5± 1.7	21.5± 1.6
Binary 99M	468.3± 24.1	14.0± 0.4	54.4± 1.6	62.5± 1.5	27.0± 1.7	22.3± 1.6
FloatLM 190M	50.3± 2.7	31.1± 0.6	65.1± 1.5	77.3± 1.3	27.2± 1.7	22.1± 1.6
QuantLM 190M 8-Bit	48.7± 2.6	31.5± 0.6	65.5± 1.5	77.1± 1.3	27.0± 1.7	22.3± 1.6
QuantLM 190M 6-Bit	55.3± 3.0	30.0± 0.6	64.2± 1.5	77.0± 1.3	26.1± 1.7	22.4± 1.6
QuantLM 190M 4-Bit	72479077.3	0.00± 0.0	25.6± 1.4	22.9± 1.3	23.3± 1.7	20.7± 1.6
QuantLM 190M 3-Bit	664.5± 41.1	12.4± 0.5	58.5± 1.6	66.4± 1.5	26.3± 1.7	21.0± 1.6
TriLM 190M	130.7± 6.5	23.7± 0.6	61.0± 1.5	72.6± 1.4	25.5± 1.7	21.5± 1.6
FloatLM 390M	21.9± 0.9	42.2± 0.7	75.6± 1.4	84.2± 1.2	28.1± 1.8	23.8± 1.7
QuantLM 390M 8-Bit	21.7± 0.9	42.3± 0.7	75.7± 1.4	84.1± 1.2	28.3± 1.8	24.1± 1.7
QuantLM 390M 6-Bit	24.3± 1.0	40.6± 0.7	75.5± 1.4	83.7± 1.2	27.6± 1.8	23.2± 1.7
QuantLM 390M 4-Bit	30.2± 1.3	39.1± 0.7	77.1± 1.3	84.1± 1.2	25.8± 1.7	23.3± 1.7
QuantLM 390M 3-Bit	115.0± 5.6	23.0± 0.6	67.4± 1.5	76.7± 1.3	25.7± 1.7	21.8± 1.6
TriLM 390M	77.7± 3.8	28.0± 0.6	68.6± 1.5	76.9± 1.3	26.4± 1.7	21.8± 1.6
FloatLM 560M	20.8± 0.9	44.1± 0.7	74.7± 1.4	83.5± 1.2	27.0± 1.7	20.7± 1.6
QuantLM 560M 8-Bit	20.9± 0.9	44.2± 0.7	74.7± 1.4	83.6± 1.2	27.3± 1.7	20.7± 1.6
QuantLM 560M 6-Bit	21.7± 0.9	42.8± 0.7	74.4± 1.4	83.6± 1.2	25.8± 1.7	20.9± 1.6
QuantLM 560M 4-Bit	24.9± 1.1	40.8± 0.7	73.6± 1.4	82.0± 1.2	27.0± 1.7	21.7± 1.6
QuantLM 560M 3-Bit	146.3± 7.1	20.1± 0.6	71.1± 1.4	75.9± 1.4	25.0± 1.7	21.8± 1.6
TriLM 560M	55.6± 2.7	32.4± 0.7	70.8± 1.4	78.7± 1.3	26.1± 1.7	19.8± 1.6
Binary 560M	62.8± 3.0	31.0± 0.6	70.0± 1.4	78.8± 1.3	26.7± 1.7	21.5± 1.6
FloatLM 830M	13.3± 0.5	49.6± 0.7	78.4± 1.3	85.9± 1.1	26.3± 1.7	20.1± 1.6
QuantLM 830M 8-Bit	13.5± 0.5	49.4± 0.7	78.5± 1.3	86.1± 1.1	26.6± 1.7	20.0± 1.6
QuantLM 830M 6-Bit	13.3± 0.5	49.1± 0.7	77.8± 1.3	85.4± 1.1	26.3± 1.7	20.1± 1.6
QuantLM 830M 4-Bit	15.4± 0.6	47.3± 0.7	78.8± 1.3	85.1± 1.1	25.5± 1.7	21.2± 1.6
QuantLM 830M 3-Bit	47.7± 2.0	30.5± 0.6	74.1± 1.4	80.1± 1.3	28.1± 1.8	21.2± 1.6
TriLM 830M	26.0± 1.1	39.9± 0.7	75.4± 1.4	82.8± 1.2	27.6± 1.8	21.4± 1.6
FloatLM 1.1B	11.7± 0.4	51.2± 0.7	82.2± 1.2	88.1± 1.0	27.3± 1.7	20.9± 1.6
QuantLM 1.1B 8-Bit	11.7± 0.4	51.2± 0.7	82.1± 1.2	88.1± 1.0	27.8± 1.8	21.2± 1.6
QuantLM 1.1B 6-Bit	11.7± 0.4	51.0± 0.7	82.3± 1.2	88.1± 1.0	27.5± 1.8	21.5± 1.6
QuantLM 1.1B 4-Bit	13.9± 0.5	49.3± 0.7	81.2± 1.2	87.6± 1.0	28.4± 1.8	20.3± 1.6
QuantLM 1.1B 3-Bit	26.9± 1.1	39.1± 0.7	78.7± 1.3	85.0± 1.1	25.8± 1.7	20.7± 1.6
TriLM 1.1B	17.3± 0.7	46.2± 0.7	73.3± 1.4	81.9± 1.2	26.9± 1.7	22.0± 1.6
Binary 1.1B	33.4± 1.4	37.6± 0.6	71.1± 1.4	81.2± 1.3	28.4± 1.7	23.2± 1.6
FloatLM 1.5B	9.4± 0.3	55.5± 0.7	80.9± 1.2	87.4± 1.0	26.1± 1.7	20.9± 1.6
QuantLM 1.5B 8-Bit	9.5± 0.3	55.5± 0.7	81.3± 1.2	87.5± 1.0	25.7± 1.7	20.6± 1.6
QuantLM 1.5B 6-Bit	9.5± 0.3	55.4± 0.7	81.4± 1.2	87.6± 1.0	25.7± 1.7	20.3± 1.6
QuantLM 1.5B 4-Bit	10.4± 0.4	53.0± 0.7	81.1± 1.2	86.9± 1.1	25.7± 1.7	20.3± 1.6
QuantLM 1.5B 3-Bit	17.8± 0.7	45.3± 0.7	75.5± 1.4	82.1± 1.2	28.4± 1.8	22.7± 1.6
TriLM 1.5B	16.4± 0.7	46.2± 0.7	80.7± 1.2	87.3± 1.1	27.8± 1.8	21.5± 1.6
FloatLM 2.4B	7.7± 0.3	59.3± 0.7	87.2± 1.1	91.0± 0.9	29.5± 1.8	21.5± 1.6
QuantLM 2.4B 8-Bit	7.7± 0.3	59.2± 0.7	87.1± 1.1	91.0± 0.9	29.5± 1.8	21.5± 1.6
QuantLM 2.4B 6-Bit	7.9± 0.3	58.9± 0.7	87.3± 1.1	90.9± 0.9	29.6± 1.8	20.9± 1.6
QuantLM 2.4B 4-Bit	8.9± 0.3	56.1± 0.7	84.8± 1.1	89.7± 1.0	29.6± 1.8	20.9± 1.6
QuantLM 2.4B 3-Bit	15.6± 0.6	45.0± 0.7	79.9± 1.3	86.7± 1.1	28.6± 1.8	21.4± 1.6
TriLM 2.4B	8.6± 0.3	55.7± 0.7	84.2± 1.2	88.7± 1.0	28.6± 1.8	24.3± 1.7
FloatLM 3.9B	6.7± 0.2	61.1± 0.7	86.5± 1.1	90.9± 0.9	26.9± 1.7	20.9± 1.6
QuantLM 3.9B 8-Bit	6.7± 0.2	61.1± 0.7	86.2± 1.1	91.0± 0.9	26.6± 1.7	20.6± 1.6
QuantLM 3.9B 6-Bit	6.8± 0.2	60.8± 0.7	86.6± 1.1	91.3± 0.9	25.8± 1.7	20.4± 1.6
QuantLM 3.9B 4-Bit	7.4± 0.2	58.5± 0.7	86.1± 1.1	90.8± 0.9	28.6± 1.8	20.1± 1.6
QuantLM 3.9B 3-Bit	14.0± 0.5	47.1± 0.7	83.1± 1.2	88.6± 1.0	27.0± 1.7	21.5± 1.6
TriLM 3.9B	6.3± 0.2	61.6± 0.7	87.4± 1.0	90.8± 0.9	27.6± 1.8	22.7± 1.6

Table 10: Spectra Suite Performance (Part 3): LAMBADA OpenAI, SciQ, LogiQA. We additionally also include Pythia's performance scores.

D.5 OMNIQUANT: 3-BIT POST-TRAINING QUANTIZED MODELS

We present additional 3-bit quantized (QuantLM 3-bit) models, which were trained using OmniQuant (Shao et al., 2024) for 5 iterations with a group size of one row. It is important to highlight that the performance benchmarks for these models are consistent with those of GPT-Q, as reported in Tables 7, 8, 10, 17, and 18. Therefore, these results do not affect our findings in the main paper.

Tasks	Metric	99M	190M	390M	560M	1.1B
ARC Challenge	Acc.	0.19 ± 0.01	0.21 ± 0.01	0.22 ± 0.01	0.22 ± 0.01	0.24 ± 0.01
	Acc. (Norm.)	0.23 ± 0.01	0.24 ± 0.01	0.26 ± 0.01	0.24 ± 0.01	0.26 ± 0.01
ARC Easy	Acc.	0.37 ± 0.01	0.41 ± 0.01	0.45 ± 0.01	0.48 ± 0.01	0.55 ± 0.01
	Acc. (Norm.)	0.34 ± 0.01	0.38 ± 0.01	0.41 ± 0.01	0.42 ± 0.01	0.48 ± 0.01
BoolQ	Acc.	0.55 ± 0.01	0.54 ± 0.01	0.62 ± 0.01	0.57 ± 0.01	0.63 ± 0.01
HellaSwag	Acc.	0.28 ± 0.00	0.29 ± 0.00	0.32 ± 0.00	0.34 ± 0.00	0.38 ± 0.00
	Acc. (Norm.)	0.29 ± 0.00	0.32 ± 0.00	0.39 ± 0.00	0.41 ± 0.00	0.48 ± 0.01
LAMBADA	Acc.	0.05 ± 0.00	0.07 ± 0.00	0.23 ± 0.01	0.25 ± 0.01	0.31 ± 0.01
LogiQA	Acc.	0.16 ± 0.01	0.20 ± 0.02	0.23 ± 0.02	0.23 ± 0.02	0.21 ± 0.02
	Acc. (Norm.)	0.23 ± 0.02	0.25 ± 0.02	0.29 ± 0.02	0.28 ± 0.02	0.27 ± 0.02
PIQA	Acc.	0.58 ± 0.01	0.59 ± 0.01	0.63 ± 0.01	0.65 ± 0.01	0.69 ± 0.01
	Acc. (Norm.)	0.58 ± 0.01	0.59 ± 0.01	0.63 ± 0.01	0.66 ± 0.01	0.69 ± 0.01
SciQ	Acc.	0.55 ± 0.02	0.64 ± 0.02	0.74 ± 0.01	0.77 ± 0.01	0.82 ± 0.01
	Acc. (Norm.)	0.49 ± 0.02	0.59 ± 0.02	0.61 ± 0.02	0.68 ± 0.01	0.73 ± 0.01
TriviaQA	Exact Match	0.00 ± 0.00	0.00 ± 0.00	0.01 ± 0.00	0.01 ± 0.00	0.05 ± 0.00
Winogrande	Acc.	0.51 ± 0.01	0.50 ± 0.01	0.51 ± 0.01	0.53 ± 0.01	0.56 ± 0.01
MMLU	Acc.	0.25 ± 0.00	0.25 ± 0.00	0.26 ± 0.00	0.27 ± 0.00	0.29 ± 0.00

Table 11: Model performance of 3-bit post-training quantized models using OmniQuant across various tasks, from 99M to 1.1B parameters, evaluated on different metrics.

Tasks	Metric	1.5B	2.4B
ARC Challenge	Acc.	0.26 ± 0.01	0.27 ± 0.01
	Acc. (Norm.)	0.29 ± 0.01	0.30 ± 0.01
ARC Easy	Acc.	0.56 ± 0.01	0.60 ± 0.01
	Acc. (Norm.)	0.51 ± 0.01	0.53 ± 0.01
BoolQ	Acc.	0.59 ± 0.01	0.63 ± 0.01
HellaSwag	Acc.	0.40 ± 0.00	0.44 ± 0.00
	Acc. (Norm.)	0.51 ± 0.01	0.57 ± 0.00
LAMBADA	Acc.	0.35 ± 0.01	0.44 ± 0.01
LogiQA	Acc.	0.23 ± 0.02	0.19 ± 0.02
	Acc. (Norm.)	0.26 ± 0.02	0.30 ± 0.02
PIQA	Acc.	0.69 ± 0.01	0.71 ± 0.01
	Acc. (Norm.)	0.70 ± 0.01	0.72 ± 0.01
SciQ	Acc.	0.82 ± 0.01	0.86 ± 0.01
	Acc. (Norm.)	0.76 ± 0.01	0.80 ± 0.01
TriviaQA	Exact Match	0.07 ± 0.00	0.07 ± 0.00
Winogrande	Acc.	0.56 ± 0.01	0.58 ± 0.01
MMLU	Acc.	0.28 ± 0.00	0.30 ± 0.00

Table 12: Performance of 3-bit Post-Training Quantized Models using OmniQuant across Various Tasks, from 1.5B to 2.4B parameters, across different tasks and metrics.

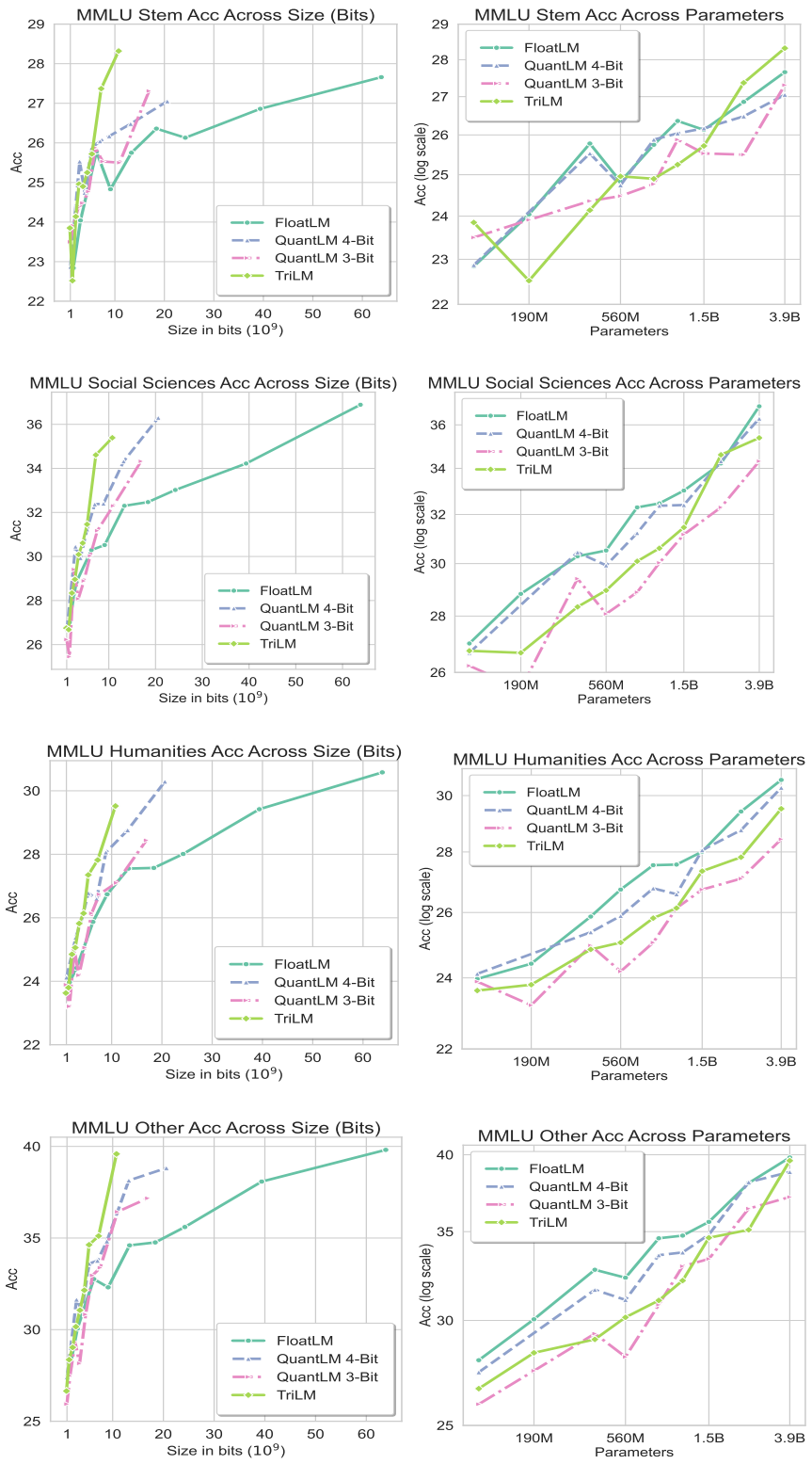


Figure 19: Model performance on MMLU subsets: STEM, Humanities, Social Sciences, and others. Plot accuracy scores against model size in bits (left) and number of parameters (right), ranging from 560M to 3.9B parameters for TriLM (ternary), FloatLM (FP16), and QuantLM (3-bit & 4-bit).

E WEIGHT DISTRIBUTION OF LINEAR LAYERS

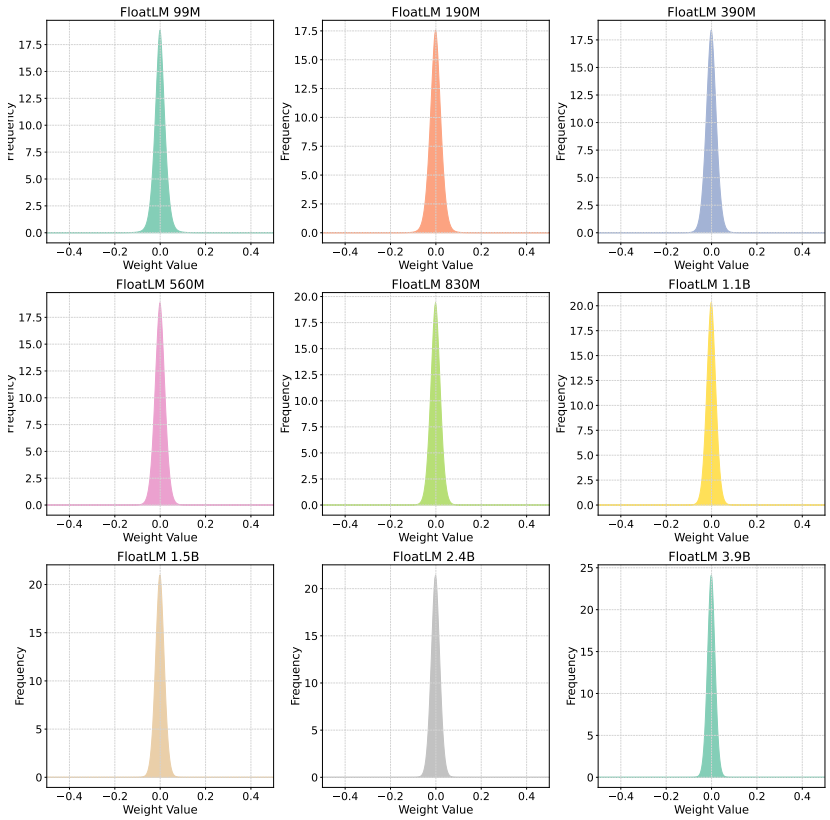


Figure 20: Weight distribution in the linear layers of FloatLM models across various model sizes, ranging from 99M to 3.9B parameters

The observed Gaussian distribution in the weights of our final trained FloatLM models across various scales is supported by both theoretical foundations and empirical evidence. We outline the rationale for the normality of weight distributions as follows:

Empirical Consistency: Across all model scales, ranging from 99 million to 3.9 billion parameters, the weight distributions consistently exhibit Gaussian characteristics, as illustrated in Figure 20. This consistency is visually evident in distribution plots and quantitatively confirmed by fitting Gaussian functions to the weight histograms, demonstrating a good fit across different model sizes.

Theoretical Underpinning: Neural network weight initialization typically follows a Gaussian distribution to facilitate balanced learning dynamics. As training progresses, despite non-linear transformations and complex interactions within the network, the Central Limit Theorem suggests that the aggregation of numerous independent random variables (such as updates during backpropagation) tends toward a normal distribution. This tendency is particularly pronounced given the high dimensionality and extensive data processing involved in training large language models.

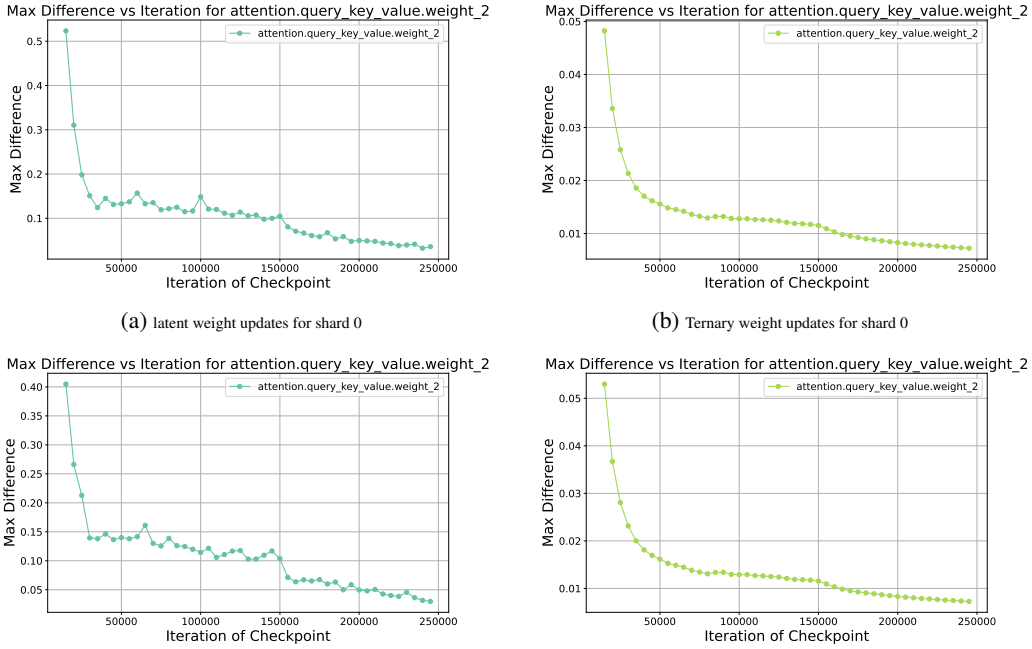
Stabilization through Regularization and Optimization: Techniques such as L2 regularization constrain weight magnitudes, encouraging them towards smaller values and contributing to a peak around zero—a characteristic feature of Gaussian distributions. Additionally, optimization algorithms like Adam, which adjust learning rates based on moving averages of recent gradients, promote smoother updates. This approach maintains the Gaussian form by mitigating the impact of outlier gradients.

Given these, we can assert that the weight distribution of our trained models closely follows a Gaussian distribution which is crucial for understanding the weight variance across different scales.

F LEARNING DYNAMICS ANALYSIS OF PEAK LR DROP AND DECAY STAGE

In this section, we present a concise analysis of our learning dynamics, inspired by Appendix D of MiniCPM (Hu et al., 2024). Specifically, we examine the impact of our two key interventions: the peak learning rate reduction at the halfway point of training and the removal of weight decay regularization at two-thirds of the training stage. This analysis explores loss dynamics through the lens of checkpoint updates and gradient behavior.

We analyze both the latent weights and ternary weights, calculating the maximum weight element update, $\max_{ij}(W^{(t+1)}ij - W^{(t)}ij)$, across all weight matrices in the TriLM-1.5B model for each training step. Our findings, consistent with observations from MiniCPM, reveal a strong correlation between weight updates and the learning rate decay, as depicted in Figure 21. Notably, after the weight decay regularization is removed at approximately 160,000 training iterations, the model checkpoints undergo smaller updates. However, surprisingly during this stage, despite smaller weight changes, the loss decreases at an accelerated pace.



(a) latent weight updates for shard 0

(b) Ternary weight updates for shard 0

(c) latent weight updates for shard 1

(d) Ternary weight updates for shard 1

Figure 21: Max Difference of Checkpoints for Layer 2

Following the methodology of Hu et al. (2024), we examine gradient data by training a 190M parameter TriLM model. We record the gradients at every step to obtain fine-grained values for deriving second-order gradient information. In Figures 22 and 23, we plot the maximum, L_2 norm, first and second-order directional derivatives of the gradient, along with the cosine of the gradient angle and the loss curvature along the training trajectory.

While the L_2 norm and maximum of the gradient do not provide notable insights, the loss curvature and second-order directional derivative show significant correlations with both the peak learning rate reduction at 5000 steps and the removal of weight decay at 7500 steps. Interestingly, we also observe an increase in the cosine of the gradients and a decrease in the first-order directional derivative at both 5000 and 7500 steps, with trends becoming more pronounced after the removal of weight regularization. Moreover, the trends for loss curvature along the parameter trajectory and the second-order directional derivative are opposite for the latent and ternary gradient statistics. A more in dept understanding these trends in the learning dynamics under our current training strategy for TriLM offers a promising direction for future exploration.

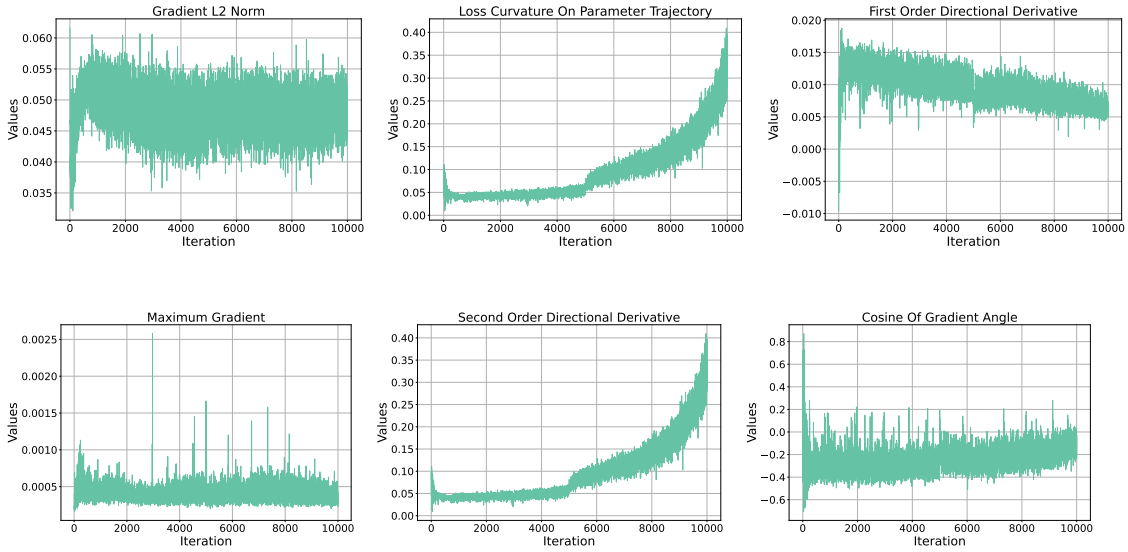


Figure 22: Latent gradient statistics over the training of 190M model. We drop the peaked learning rate at step 5000 and reduce the weight decay to 0 at step 7500

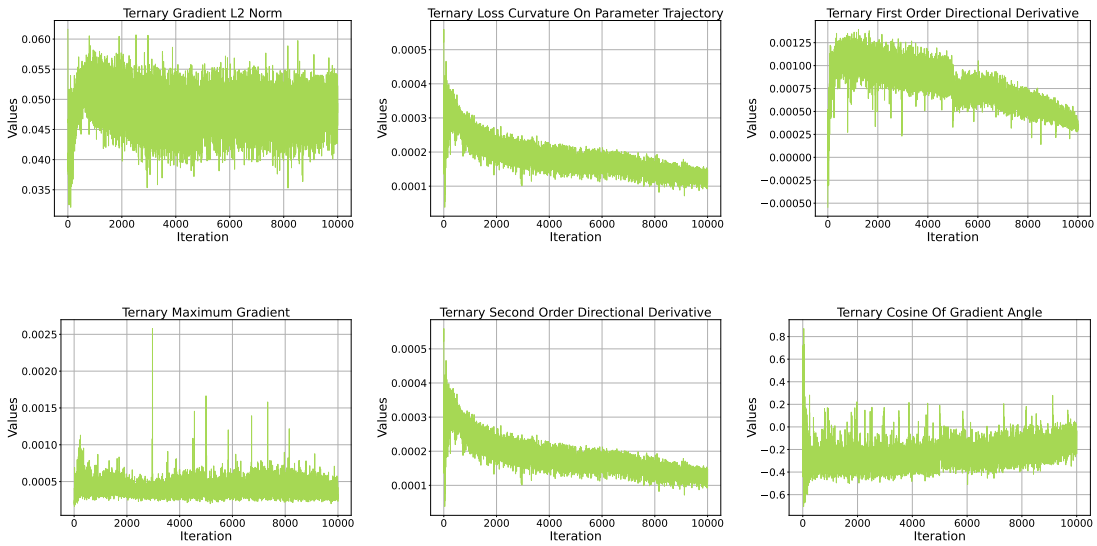


Figure 23: Ternary gradient statistics over the training of 190M model. We drop the peaked learning rate at step 5000 and reduce the weight decay to 0 at step 7500

G MEMORY BOTTLENECKS AND LOW-BITWIDTH LANGUAGE MODELLING

Recent observations (Gholami et al., 2024) suggest that, given the slower pace of improvements in memory and communication compared to compute (FLOPs), the bottleneck continues to shift away from computation towards the memory-related characteristics of hardware for deploying large language models. This shift underscores the importance of exploring solutions that directly address memory constraints. Below, we formally analyze this trend and the impact of low-bitwidth language models on addressing memory bottlenecks during inference.

G.1 OVERVIEW OF RECENT DATACENTER GPUS AND ACCELERATORS.

We begin our analysis by surveying a broad range of recent datacenter General Purpose GPUs (GPGPUs) employed for neural network development and research since 2018. This includes hardware from multiple providers, covering various configurations across the latest microarchitectures.

From Nvidia, we consider the following:

- **Volta**: V100 (SXM/PCIe) (Nvidia Team, 2018),
- **Ampere**: A100 (40GB/80GB SXM/PCIe) (Nvidia Team, 2020),
- **Hopper**: H100 (SXM/PCIe) and H200 (Nvidia Team, 2022; 2023),
- **Blackwell**: This includes preliminary data for Blackwell microarchitectures, which at the time of access were subject to change (Nvidia Team, 2024).

From AMD, we analyze the following models:

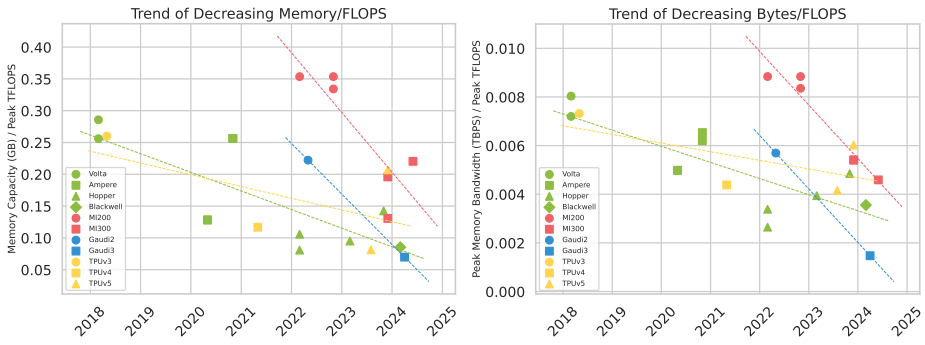
- **MI200 Series**: MI210, MI250, MI250X (AMD Team, 2022a;b),
- **MI300 Series**: MI300A, MI300X, MI325X (AMD Team, 2023a;b; 2024).

Additionally, we include hardware from Intel and Google:

- From Intel, the **Gaudi Series**: Gaudi 2 and Gaudi 3 (Intel Gaudi Team, 2024),
- From Google, the **Tensor Processing Units (TPUs)**: TPUv3 (Google TPU Team, 2018), TPUv4 (Google TPU Team, 2021), and TPUv5 (TPUv5e, TPUv5p) (Google TPU Team, 2023a;b).

All data was sourced from the respective datasheets, technical documentation, or press releases of the cited hardware. Over the past several years, each of these four accelerator families has improved in three areas - FLOPS, memory capacity, and bandwidth.

G.2 MEMORY TRENDS AND SPEEDUP OPPORTUNITIES IN LOW-BITWIDTH LANGUAGE MODELING

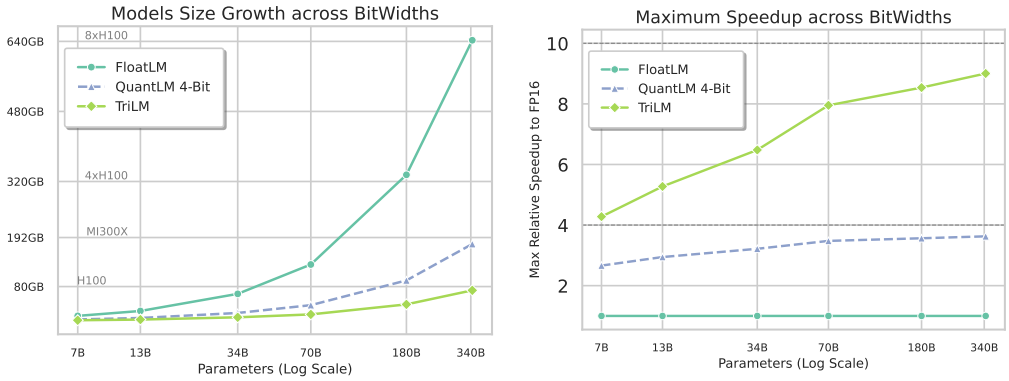


(a) Memory Capacity vs Peak FLOPS (b) Peak Memory Bandwidth vs Peak FLOPS

Figure 24: Trends of Memory/FLOP and Bandwidth/FLOP across different (datacenter) GPGPUs.

Memory Capacity and Bandwidth of GPGPUs Relative to Peak TFLOPs. In Figure 24a, we show the trends of Memory Capacity over Peak TFLOPS (Half Precision - FP16/BF16) for various accelerators over the years. We also perform a linear fit for each family of accelerators separately. The linear fit for all the families has a downward slope, showing that memory capacity is improving at a slower pace than computation capability. This trend holds true even for the most recent hardware, such as Blackwell, MI325X, and Gaudi3. Though we consider Half-Precision TFLOPs, the slope is expected to become steeper when considering peak TFLOPS over Ampere sparse or FP8. Similarly, in Figure 24b, we present the trends of Memory Bandwidth (specifically for DRAM or its equivalent memory) over FLOPs for the accelerators over the years, along with the linear fit for each family. We observe a downward slope here as well, indicating the trend that memory bandwidth is growing much slower than computation.

Comparison of model size and maximum speed up for quantized models: In this analysis, we include transformer configurations from the LLaMa family (Touvron et al., 2023a;b). As larger vocabularies in LLMs are becoming increasingly common for efficient multilingual modeling, we use a vocabulary size of 128k from LLaMa 3 (AI@Meta, 2024) for our analysis. We assume the Embedding and LM Head weights are retained in Half-Precision across all bitwidths. In Figure 25, we provide the scaling plots of FloatLMs, QuantLMs and TriLMs in terms of model size (in GB) and maximum speedup compared to the FloatLM baseline.



(a) Model Size growth at various BitWidths (b) Maximum Possible Speedup at different BitWidths

Figure 25: Expected gains from low bitwidth modeling. TriLMs can fit over 300B parameters on a single H100 and achieve up to a theoretical maximum of 10x faster autoregressive decoding compared to FloatLM.

H LATENCY AND THROUGHPUT ANALYSIS OF TERNARY QUANTIZATION FORMATS

To demonstrate the inference speedup and throughput achieved in real-world scenarios by our ternary language models, we employ llama.cpp kernels[3], an open-source framework specifically designed for optimized and efficient inference.

H.1 PACKING SCHEMES FOR TERNARY WEIGHTS

This section details the packing schemes employed for our ternary quantization formats, TQ1 and TQ2, emphasizing their bit-per-weight (bpw) efficiency and computational implications.

TQ1 Packing (1.6875 bpw)

- **Packing**: The first 240 ternary values are packed with 5 elements per byte, and the remaining 16 are packed with 4 elements per byte.
- **Block Structure**: A block of 256 ternary values is represented in 52 bytes—48 bytes for the first 240 values, 4 bytes for the remaining 16 values, and a float16 scaling factor for the block.
- **Value Mapping**: Ternary values -1, 0, 1 are stored as unsigned integers 0, 1, 2, enabling efficient use of bit space.

TQ2 Packing (2.0625 bpw)

- **Packing**: Each byte encodes 4 ternary values, with 2 bits allocated to each value.
- **Block Structure**: A block of 256 ternary values is stored in 64 bytes, accompanied by a float16 scale.
- **Value Mapping**: The mapping follows the same convention as TQ1.

The use of 256-element blocks ensures compatibility with the row sizes of our models, which are optimized to be multiples of 256. This design decision aligns with the architecture of modern hardware, facilitating efficient computation. The superior performance of TQ2 underscores its suitability for compute-intensive hardware, particularly when paired with optimized kernels.

H.2 EXPERIMENTAL EVALUATION

Throughput Comparison. Table 13 presents the throughput (in GB/s) achieved by various quantization formats on two different hardware configurations. Notably, TQ2 demonstrates the highest throughput, surpassing both q4 and q8, which are designed to optimize inference in 4-bit and 8-bit quantized formats, respectively. The superior performance of TQ2 underscores its advantages over other precision models.

Configuration	Model Size	Apple M3 Pro (GB/s)	Intel Core m3-8100Y (AVX2) (GB/s)
f16	7.99 GB	93.47	30.60
q8	4.24 GB	131.86	67.03
q4	2.42 GB	135.33	64.17
TQ1	994 MB	124.70	70.31
TQ2	**1.17 GB**	**176.43**	**141.83**

Table 13: Throughput Comparison of Quantization Formats

Latency Comparison Across Quantization Formats. Latency experiments, summarized in Table 14, were conducted on the Apple M3 Pro to evaluate token generation efficiency. TQ2 demonstrates the lowest latency, achieving 65.47 tokens per second. It should be noted that inference is not fully optimized for any of the kernels, yet the superior performance of TQ2 underscores its advantages over other precision models.

[3] https://github.com/ggerganov/llama.cpp

Configuration	Total Time (ms)	Tokens Processed	Time per Token (ms)	Tokens per Second
f16	12574.22	260	48.44	20.64
q8	4660.77	260	17.69	56.53
q4	4927.69	261	18.88	52.97
TQ1	7022.70	260	27.01	37.02
TQ2	**3990.42**	**260**	**15.27**	**65.47**

Table 14: Latency Comparison Across Quantization Formats

While our results highlight the practical advantages of ternary formats, further optimization of kernel operations, particularly for GPU architectures, presents a promising direction for achieving additional speedups. The current benchmarking efforts are primarily focused on CPU implementations, leaving substantial potential for future exploration and optimization on GPU-based systems.

I ABLATIONS

Table 16 and 15 shows the performance of ablation 100B token training runs over the six commonsense benchmarks from BitNet b1.58 at 1.1B parameters. The first two rows show the performance of TriLM 1.1B and Float 1.1B at this token count, followed by our replication of BitNet b1.58 (Ours) as well as the scores from BitNet b1.58 over 700M and 1.3B parameters. We observe that at this scale, TriLM does not come close to matching the performance of FloatLM, but it outperforms much larger BitNets. The next two rows show the performance of TriLM 1.1B and FloatLM 1.1B when trained on 100B tokens of FineWeb, instead of SlimPajama. While the performance of both the models improves on FineWeb, the average difference in their performance across datasets remains the same. Lastly, we show the performances across various optimization schedules. A significant drop in averaged performance is noticed when the baseline schedule of linear decay with constant weight decay is used. The gains from dropping l2 regularization in the schedule are more than that of dropping the peak learning rate, however, not enough to match that of TriLM 1.1B's schedule.

Models	HellaSwag		PIQA		WinoGrande
	Acc N.	Acc	Acc N.	Acc	Acc
FloatLM 1.1B	50.0 ± 0.5	39.3 ± 0.5	70.9 ± 1.0	70.1 ± 1.0	55.4 ± 1.4
TriLM 1.1B	46.8 ± 0.5	37.1 ± 0.4	69.4 ± 1.0	69.4 ± 1.0	53.8 ± 1.4
BitNet b1.58 1.1B (Ours)	47.0 ± 0.5	37.1 ± 0.4	69.4 ± 1.0	69.6 ± 1.0	53.4 ± 1.4
BitNet b1.58 700M	35.1		68.1		55.2
BitNet b1.58 1.3B	37.7		68.8		55.8
TriLM 1.1B FineWeb	50.0 ± 0.5	39.2 ± 0.4	70.2 ± 1.0	70.1 ± 1.0	56.6 ± 1.3
FloatLM 1.1B FineWeb	52.7 ± 0.5	41.1 ± 0.4	73.0 ± 1.0	71.3 ± 1.0	56.7 ± 1.3
TriLM 1.1B Only Peak LR Dropped	46.7 ± 0.5	36.8 ± 0.4	68.9 ± 1.0	69.5 ± 1.0	55.4 ± 1.4
TriLM 1.1B Only L2 Reg. Dropped	47.1 ± 0.5	37.5 ± 0.4	68.6 ± 1.0	69.4 ± 1.0	55.2 ± 1.4
TriLM 1.1B Baseline Schedule	46.0 ± 0.5	36.9 ± 0.4	69.3 ± 1.0	69.1 ± 1.0	56.2 ± 1.3

Table 15: Ablation Common Sense Task Performance: HellaSwag, PIQA, WinoGrande, Arc Easy, Arc Challenge, BoolQ (Contd.). BitNet b1.58's scores from Ma et al. (2024). All runs are for 100B tokens on Slim Pajama, except those explicitly stated as FineWeb

Models	Arc Challenge		Arc Easy		BoolQ	Avg (HellaSwag, PIQA, WinoGrande,
	Acc N.	Acc	Acc N.	Acc	Acc	Arc Easy, Arc Challenge, and BoolQ)
FloatLM 1.1B	26.3 ± 1.3	22.5 ± 1.2	50.3 ± 1.0	56.8 ± 1.0	60.6 ± 0.8	52.2
TriLM 1.1B	26.7 ± 1.3	22.9 ± 1.2	49.7 ± 1.0	55.0 ± 1.0	54.9 ± 0.8	50.2
BitNet b1.58 1.1B (Ours)	26.1 ± 1.2	23.6 ± 1.2	47.7 ± 1.0	55.3 ± 1.0	49.7 ± 0.8	48.9
BitNet b1.58 700M	21.4		51.8		58.2	48.3
BitNet b1.58 1.3B	24.2		54.9		56.7	49.6
TriLM 1.1B FineWeb	31.7 ± 1.3	31.9 ± 1.3	63.1 ± 0.9	66.8 ± 0.9	58.3 ± 0.8	54.9
FloatLM 1.1B FineWeb	34.4 ± 1.3	33.0 ± 1.3	65.7 ± 0.9	70.2 ± 0.9	59.3 ± 0.8	56.9
TriLM 1.1B Only Peak LR Dropped	27.4 ± 1.3	23.6 ± 1.2	48.3 ± 1.0	55.1 ± 1.0	51.6 ± 0.8	49.7
TriLM 1.1B Only L2 Reg. Dropped	27.6 ± 1.3	24.8 ± 1.2	49.2 ± 1.0	55.1 ± 1.0	53.1 ± 0.8	50.1
TriLM 1.1B Baseline Schedule	26.2 ± 1.2	23.2 ± 1.2	48.0 ± 1.0	54.0 ± 1.0	49.4 ± 0.8	49.1

Table 16: Ablation Common Sense Task Performance: HellaSwag, PIQA, WinoGrande, Arc Easy, Arc Challenge, BoolQ. BitNet b1.58's scores from Ma et al. (2024). All runs are for 100B tokens on Slim Pajama, except those explicitly stated as FineWeb

Models	TriviaQA	CrowsPairs		Big Bench BBQ Lite	TruthfulQA
	Exact Match	Likelihood diff.	Pct stereotype	Acc	Acc
FloatLM 99M	0.6± 0.1	372.4± 14.6	55.4± 1.2	30.8± 0.4	24.4± 1.5
QuantLM 99M 8-Bit	0.6± 0.1	370.9± 14.6	55.1± 1.2	26.5± 0.3	24.1± 1.5
QuantLM 99M 6-Bit	0.6± 0.1	389.8± 14.8	56.9± 1.2	26.7± 0.3	24.2± 1.5
QuantLM 99M 4-Bit	0.3± 0	425.5± 15.2	54.0± 1.2	26.2± 0.3	22.9± 1.5
QuantLM 99M 3-Bit	0.1± 0	611.1± 18.8	51.0± 1.2	31.4± 0.4	24.6± 1.5
TriLM 99M	0.1± 0	362.4± 10.8	54.2± 1.2	30.8± 0.4	24.2± 1.5
Binary 99M	0.2± 0.0	353.5± 11.1	53.3± 1.2	31.5± 0.3	25.7± 1.5
FloatLM 190M	0.6± 0.1	348.2± 11.3	55.9± 1.2	27.3± 0.4	22.4± 1.5
QuantLM 190M 8-Bit	0.7± 0.1	352.7± 11.4	56.2± 1.2	27.1± 0.4	22.5± 1.5
QuantLM 190M 6-Bit	0.7± 0.1	368.9± 11.7	56.2± 1.2	27.2± 0.4	22.5± 1.5
QuantLM 190M 4-Bit	0.0± 0	961.9± 25.4	43.8± 1.2	35.0± 0.4	24.2± 1.5
QuantLM 190M 3-Bit	0.1± 0	482.7± 15.2	53.7± 1.2	26.4± 0.3	25.0± 1.5
TriLM 190M	0.2± 0	343.5± 10.9	55.5± 1.2	29.7± 0.4	23.9± 1.5
FloatLM 390M	2.8± 0	355.5± 10.4	59.6± 1.2	25.4± 0.3	22.4± 1.5
QuantLM 390M 8-Bit	2.9± 0	355.8± 10.4	59.8± 1.2	25.4± 0.3	22.2± 1.5
QuantLM 390M 6-Bit	2.4± 0	360.5± 10.4	60.6± 1.2	25.3± 0.3	22.8± 1.5
QuantLM 390M 4-Bit	1.3± 0.1	368.2± 10.2	59.4± 1.2	25.5± 0.3	22.8± 1.5
QuantLM 390M 3-Bit	0.8± 0.1	444.4± 12.2	54.3± 1.2	26.3± 0.3	23.0± 1.5
TriLM 390M	1.3± 0.1	344.5± 10.3	58.3± 1.2	26.9± 0.3	24.4± 1.5
FloatLM 560M	4.6± 0.2	351.8± 9.9	58.9± 1.2	25.7± 0.3	21.7± 1.4
QuantLM 560M 8-Bit	4.7± 0.2	352.9± 10.0	59.2± 1.2	25.7± 0.3	21.8± 1.4
QuantLM 560M 6-Bit	3.5± 0.1	353.7± 9.9	59.3± 1.2	25.8± 0.3	22.0± 1.5
QuantLM 560M 4-Bit	2.1± 0.1	372.7± 10.7	59.2± 1.2	27.0± 0.4	22.2± 1.5
QuantLM 560M 3-Bit	1.5± 0.1	411.2± 11.3	57.9± 1.2	29.0± 0.4	22.9± 1.5
TriLM 560M	2.4± 0.1	345.1± 10.1	58.7± 1.2	25.5± 0.3	23.6± 1.5
Binary 560M	0.2± 0.0	356.3± 10.4	58.5± 1.2	26.3± 0.3	23.1± 1.4
FloatLM 830M	8.5± 0.2	354.6± 9.6	62.6± 1.2	25.7± 0.3	23.1± 1.5
QuantLM 830M 8-Bit	8.5± 0.2	354.5± 9.6	62.1± 1.2	25.6± 0.3	23.0± 1.5
QuantLM 830M 6-Bit	8.5± 0.2	354.6± 9.6	62.7± 1.2	25.5± 0.3	22.5± 1.5
QuantLM 830M 4-Bit	10.6± 0.2	364.2± 9.8	59.9± 1.2	25.9± 0.3	21.8± 1.4
QuantLM 830M 3-Bit	3.1± 0.1	389.5± 10.9	59.9± 1.2	30.5± 0.4	24.4± 1.5
TriLM 830M	4.3± 0.2	344.9± 10.0	60.7± 1.2	25.1± 0.3	22.8± 1.5
FloatLM 1.1B	12.9± 0.3	349.2± 9.7	61.2± 1.2	25.4± 0.3	21.4± 1.4
QuantLM 1.1B 8-Bit	12.7± 0.2	349.5± 9.7	61.1± 1.2	25.4± 0.3	21.7± 1.4
QuantLM 1.1B 6-Bit	12.4± 0.2	349.7± 9.6	59.9± 1.2	25.5± 0.3	21.9± 1.4
QuantLM 1.1B 4-Bit	9.3± 0.2	359.1± 10.1	60.9± 1.2	25.4± 0.3	21.3± 1.4
QuantLM 1.1B 3-Bit	6.8± 0.2	422.4± 11.5	58.7± 1.2	29.9± 0.4	24.2± 1.5
TriLM 1.1B	1.9± 0.1	343.4± 9.9	61.4± 1.2	25.8± 0.3	21.5± 1.4
Binary 1.1B	2.2± 0.1	351.6± 9.8	58.3± 1.2	26.4± 0.3	23.2± 1.4
FloatLM 1.5B	12.2± 0.2	351.9± 9.6	61.6± 1.2	26.8± 0.3	21.8± 1.4
QuantLM 1.5B 8-Bit	12.5± 0.2	352.4± 9.6	61.6± 1.2	26.8± 0.3	21.8± 1.4
QuantLM 1.5B 6-Bit	11.3± 0.2	350.9± 9.7	61.9± 1.2	27.1± 0.4	21.5± 1.4
QuantLM 1.5B 4-Bit	9.0± 0.2	357.9± 9.8	60.7± 1.2	25.9± 0.3	20.8± 1.4
QuantLM 1.5B 3-Bit	4.2± 0.1	400.0± 10.6	60.9± 1.2	26.8± 0.3	20.8± 1.4
TriLM 1.5B	5.9± 0.1	348.9± 9.9	59.9± 1.2	25.2± 0.3	21.7± 1.4
FloatLM 2.4B	20.7± 0.3	360.4± 9.4	64.2± 1.2	26.7± 0.3	21.7± 1.4
QuantLM 2.4B 8-Bit	20.7± 0.3	360.5± 9.4	64.2± 1.2	26.5± 0.3	21.9± 1.4
QuantLM 2.4B 6-Bit	20.4± 0.3	360.8± 9.5	63.4± 1.2	26.4± 0.3	21.8± 1.4
QuantLM 2.4B 4-Bit	21.1± 0.3	358.7± 9.6	63.4± 1.2	26.0± 0.3	21.7± 1.4
QuantLM 2.4B 3-Bit	10.9± 0.2	360.2± 9.5	59.9± 1.2	25.8± 0.3	21.5± 1.4
TriLM 2.4B	12.3± 0.1	353.0± 10.0	64.1± 1.2	25.4± 0.3	23.0± 1.5
FloatLM 3.9B	21.5± 0.3	359.2± 9.6	64.7± 1.2	25.4± 0.3	23.6± 1.5
QuantLM 3.9B 8-Bit	21.7± 0.3	359.8± 9.6	64.6± 1.2	25.4± 0.3	23.6± 1.5
QuantLM 3.9B 6-Bit	21.0± 0.3	359.5± 9.6	63.9± 1.2	25.4± 0.3	23.5± 1.5
QuantLM 3.9B 4-Bit	17.9± 0.3	365.5± 9.7	64.8± 1.2	25.3± 0.3	24.2± 1.5
QuantLM 3.9B 3-Bit	8.2± 0.2	365.9± 9.8	64.3± 1.2	25.5± 0.3	21.9± 1.4
TriLM 3.9B	21.3± 0.3	362.4± 9.6	65.4± 1.2	25.9± 0.3	24.1± 1.5

Table 17: Spectra Suite Performance (Part 4): TriviaQA, CrowsPairs, Big Bench BBQ Lite, TruthQA. We additionally also include Pythia's performance scores.

Models	MMLU Accuracy				
	Stem	Humanities	Social Sciences	Other	Avg.
FloatLM 99M	22.8± 0.7	24.0± 0.6	27.0± 0.8	28.0± 0.8	25.3± 0.4
QuantLM 99M 8-Bit	22.9± 0.7	24.2± 0.6	26.9± 0.8	27.9± 0.8	25.3± 0.4
QuantLM 99M 6-Bit	22.7± 0.7	24.1± 0.6	26.6± 0.8	28.2± 0.8	25.2± 0.4
QuantLM 99M 4-Bit	22.9± 0.7	24.1± 0.6	26.7± 0.8	27.4± 0.8	25.1± 0.4
QuantLM 99M 3-Bit	23.5± 0.8	23.9± 0.6	26.2± 0.8	25.9± 0.8	24.8± 0.4
TriLM 99M	23.9± 0.8	23.6± 0.6	26.7± 0.8	26.6± 0.8	25.0± 0.4
Binary 99M	21.6± 0.7	24.3± 0.6	21.8± 0.7	24.0± 0.7	23.1± 0.3
FloatLM 190M	24.0± 0.8	24.4± 0.6	28.8± 0.8	30.1± 0.8	26.5± 0.4
QuantLM 190M 8-Bit	24.1± 0.8	24.5± 0.6	28.9± 0.8	30.0± 0.8	26.6± 0.4
QuantLM 190M 6-Bit	24.1± 0.8	24.5± 0.6	28.3± 0.8	29.8± 0.8	26.4± 0.4
QuantLM 190M 4-Bit	22.9± 0.7	22.9± 0.6	24.5± 0.8	23.4± 0.8	23.4± 0.4
QuantLM 190M 3-Bit	23.9± 0.8	23.2± 0.6	25.4± 0.8	27.5± 0.8	24.8± 0.4
TriLM 190M	22.5± 0.7	23.8± 0.6	26.7± 0.8	28.4± 0.8	25.2± 0.4
FloatLM 390M	25.8± 0.8	25.9± 0.6	30.3± 0.8	32.8± 0.8	28.3± 0.4
QuantLM 390M 8-Bit	25.7± 0.8	25.9± 0.6	30.2± 0.8	32.4± 0.8	28.2± 0.4
QuantLM 390M 6-Bit	26.0± 0.8	25.8± 0.6	30.2± 0.8	32.3± 0.8	28.3± 0.4
QuantLM 390M 4-Bit	25.5± 0.8	25.4± 0.6	30.5± 0.8	31.6± 0.8	27.9± 0.4
QuantLM 390M 3-Bit	24.4± 0.8	25.0± 0.6	29.4± 0.8	29.3± 0.8	26.8± 0.4
TriLM 390M	24.1± 0.8	24.8± 0.6	28.3± 0.8	29.0± 0.8	26.4± 0.4
FloatLM 560M	24.8± 0.8	26.7± 0.6	30.5± 0.8	32.3± 0.8	28.4± 0.4
QuantLM 560M 8-Bit	24.8± 0.8	26.6± 0.6	30.5± 0.8	32.1± 0.8	28.3± 0.4
QuantLM 560M 6-Bit	24.6± 0.8	26.7± 0.6	30.5± 0.8	31.3± 0.8	28.1± 0.4
QuantLM 560M 4-Bit	24.7± 0.8	25.9± 0.6	29.9± 0.8	31.1± 0.8	27.7± 0.4
QuantLM 560M 3-Bit	24.5± 0.8	24.2± 0.6	28.1± 0.8	28.2± 0.8	26.0± 0.4
TriLM 560M	25.0± 0.8	25.1± 0.6	29.0± 0.8	30.2± 0.8	27.0± 0.4
Binary 560M	21.4± 0.7	24.2± 0.6	21.6± 0.7	23.9± 0.7	22.9± 0.3
FloatLM 830M	25.8± 0.8	27.5± 0.6	32.3± 0.8	34.6± 0.8	29.7± 0.4
QuantLM 830M 8-Bit	25.8± 0.8	27.4± 0.6	32.1± 0.8	34.7± 0.8	29.7± 0.4
QuantLM 830M 6-Bit	25.6± 0.8	27.3± 0.6	32.1± 0.8	34.2± 0.8	29.5± 0.4
QuantLM 830M 4-Bit	25.9± 0.8	26.8± 0.6	31.2± 0.8	33.6± 0.8	29.1± 0.4
QuantLM 830M 3-Bit	24.8± 0.8	25.1± 0.6	28.9± 0.8	30.8± 0.8	27.1± 0.4
TriLM 830M	24.9± 0.8	25.8± 0.6	30.1± 0.8	31.1± 0.8	27.7± 0.4
FloatLM 1.1B	26.4± 0.8	27.6± 0.6	32.5± 0.8	34.8± 0.8	30.0± 0.4
QuantLM 1.1B 8-Bit	26.2± 0.8	27.4± 0.6	32.5± 0.8	34.9± 0.8	29.9± 0.4
QuantLM 1.1B 6-Bit	26.0± 0.8	27.5± 0.6	32.7± 0.8	34.9± 0.8	29.9± 0.4
QuantLM 1.1B 4-Bit	26.0± 0.8	26.6± 0.6	32.4± 0.8	33.8± 0.8	29.3± 0.4
QuantLM 1.1B 3-Bit	25.9± 0.8	26.1± 0.6	30.0± 0.8	33.0± 0.8	28.4± 0.4
TriLM 1.1B	25.2± 0.8	26.1± 0.6	30.6± 0.8	32.2± 0.8	28.3± 0.4
Binary 1.1B	21.0± 0.7	24.2± 0.6	21.7± 0.8	24.4± 0.7	23.0± 0.3
FloatLM 1.5B	26.1± 0.8	28.0± 0.7	33.0± 0.8	35.6± 0.8	30.4± 0.4
QuantLM 1.5B 8-Bit	26.1± 0.8	28.1± 0.7	32.9± 0.8	35.5± 0.8	30.3± 0.4
QuantLM 1.5B 6-Bit	26.3± 0.8	28.0± 0.7	33.0± 0.8	35.4± 0.8	30.4± 0.4
QuantLM 1.5B 4-Bit	26.2± 0.8	28.1± 0.7	32.4± 0.8	34.8± 0.8	30.1± 0.4
QuantLM 1.5B 3-Bit	25.5± 0.8	26.7± 0.6	31.2± 0.8	33.4± 0.8	28.9± 0.4
TriLM 1.5B	25.7± 0.8	27.4± 0.6	31.5± 0.8	34.6± 0.8	29.5± 0.4
FloatLM 2.4B	26.9± 0.8	29.4± 0.7	34.2± 0.8	38.1± 0.9	31.8± 0.4
QuantLM 2.4B 8-Bit	27.0± 0.8	29.4± 0.7	34.1± 0.8	38.0± 0.9	31.8± 0.4
QuantLM 2.4B 6-Bit	26.8± 0.8	29.5± 0.7	34.2± 0.8	38.2± 0.9	31.8± 0.4
QuantLM 2.4B 4-Bit	26.5± 0.8	28.8± 0.7	34.3± 0.8	38.1± 0.9	31.5± 0.4
QuantLM 2.4B 3-Bit	25.5± 0.8	27.1± 0.6	32.3± 0.8	36.4± 0.9	29.9± 0.4
TriLM 2.4B	27.4± 0.8	27.8± 0.6	34.6± 0.9	35.1± 0.8	30.8± 0.4
FloatLM 3.9B	27.7± 0.8	30.6± 0.7	36.9± 0.9	39.8± 0.9	33.3± 0.4
QuantLM 3.9B 8-Bit	27.6± 0.8	30.7± 0.7	37.0± 0.9	39.7± 0.9	33.4± 0.4
QuantLM 3.9B 6-Bit	27.3± 0.8	30.3± 0.7	36.9± 0.9	39.3± 0.9	33.1± 0.4
QuantLM 3.9B 4-Bit	27.1± 0.8	30.3± 0.7	36.3± 0.9	38.8± 0.9	32.8± 0.4
QuantLM 3.9B 3-Bit	27.3± 0.8	28.4± 0.7	34.3± 0.9	37.2± 0.9	31.4± 0.4
TriLM 3.9B	28.3± 0.8	29.5± 0.7	35.4± 0.9	39.6± 0.9	32.8± 0.4

Table 18: Spectra Suite Performance (Part 5): MMLU- STEM, Humanities, Social Sciences, Others.

J ILLUSTRATIVE EXAMPLES OF TRILM 3.9B'S COMPLETION CAPABILITIES

We showcase instances of outputs produced by TriLM (3.9B) across diverse tasks, highlighting its proficiency in tasks such as comprehension, prompt completion, and creative composition.

Generated Output on Reading Comprehension by TriLM (3.9B)

Title: The Blitz Background: From the German point of view, March 1941 saw an improvement. The Luftwaffe flew 4,000 sorties that month, including 12 major and three heavy attacks. The electronic war intensified but the Luftwaffe flew major inland missions only on moonlit nights. Ports were easier to find and made better targets. To confuse the British, radio silence was observed until the bombs fell. X- and Y-Gerät beams were placed over false targets and switched only at the last minute. Rapid frequency changes were introduced for X-Gerät, whose wider band of frequencies and greater tactical flexibility ensured it remained effective at a time when British selective jamming was degrading the effectiveness of Y-Gerät.

Q: How many sorties were flown in March 1941?
A: 4,000

Q: When did the Luftwaffe fly inland missions?
A: Only during moonlit nights

Title: Helsinki
Background: Helsinki is the capital and largest city of Finland. It is in the region of Uusimaa, in southern Finland, on the shore of the Gulf of Finland. Helsinki has a population of , an urban population of , and a metropolitan population of over 1.4 million, making it the most populous municipality and urban area in Finland. Helsinki is some north of Tallinn, Estonia, east of Stockholm, Sweden, and west of Saint Petersburg, Russia. Helsinki has close historical connections with these three cities. The Helsinki metropolitan area includes the urban core of Helsinki, Espoo, Vantaa, Kauniainen, and surrounding commuter towns. It is the world's northernmost metro area of over one million people, and the city is the northernmost capital of an EU member state. The Helsinki metropolitan area is the third largest metropolitan area in the Nordic countries after Stockholm and Copenhagen, and the City of Helsinki is the third largest after Stockholm and Oslo. Helsinki is Finland's major political, educational, financial, cultural, and research center as well as one of northern Europe's major cities. Approximately 75% of foreign companies that operate in Finland have settled in the Helsinki region. The nearby municipality of Vantaa is the location of Helsinki Airport, with frequent service to various destinations in Europe and Asia.

Q: What is the most populous municipality in Finland?
A: Helsinki

Q: How many people live there?
A: 1.4 million in the metropolitan area

Q: What percent of the foreign companies that operate in Finland are in Helsinki?
A: 75%

Q: What towns are a part of the metropolitan area?
A: Espoo, Vantaa, Kauniainen, and surrounding commuter towns

Auto-complete on a creative writing task by TriLM (3.9B)

Essay Writing

In the year 2150, humanity had established colonies on Mars. Captain Ramirez was on a routine mission to explore an uncharted region of the planet when he and his crew were attacked by Martian natives who wanted them dead for their technology. The captain's ship crashed into the surface of Mars where it exploded in flames.
The survivors managed to escape from the wreckage but they soon found themselves stranded with no way out or back home. They would have to survive alone until rescue came. But what if there is nothing waiting for them? What if they are trapped forever?

Poem Writing

In a garden where the roses bloom,
Underneath the silver moon,
A gentle breeze begins to sway,
And whispers secrets of the day.
The stars above start to appear,
While shadows dance and disappear,
The night unfolds in its own time.
The sun rises over the horizon,
As it does every morning,
But this is no ordinary dawn.
It's a new beginning for all who are here today.
For those who have come before us,
And those yet to be born.
We celebrate life with music and laughter,
With friends old and new.
This is our moment to shine!

Auto-complete on various prompts by TriLM (3.9B)

Making a cake: Several cake pops are shown on a display. A woman and girl are shown making the cake pops in a kitchen. They use a mixer to mix ingredients, then knead dough by hand. The women roll out the dough with a rolling pin, cut it into shapes using cookie cutters, bake them, and decorate them with frosting or sprinkles.

The energy given up by electrons as they move through the electron transport chain is used to produce ATP. In this process, oxygen and water are produced in a reaction called cellular respiration.

When talking about sensitive topics, it is crucial to be aware of the fact that there are many different types of people. Some will react negatively and others positively. It's important not to take offense when someone says something you don't like.

If someone disagrees with you, it is best to ignore them. The most important thing in life is not what we have but who we are and how we treat others.

K BROADER IMPACT

Interpretability Beyond Neuron Level: While several efforts have been made to understand how language models work and the means to steer them without training, these methods have mostly focussed on intervening at the neuron level. TriLMs open a new degree of interpretability - at the connection level. Here, the connections between any two neurons in a layer are in one of the three states - 0 (no connection), -1 (negative connection) and +1 (positive connection), each with equal strength. This is in sharp contrast to FloatLMs, where these connections can be of varying strengths, making it harder to study interpretability beyond the neuron level. By releasing the checkpoints across our training runs, we facilitate research along these directions.

Environmental Benefits and Resource Efficiency: The open release of our models mitigates future emissions by allowing others to bypass the need for pretraining models from scratch. Moreover, TriLMs need much fewer resources during deployment and can perform the autoregressive generation at a faster pace - making them critical to scenarios demanding strict latency. Additionally, TriLMs represent a substantial advancement in enhancing performance on resource-constrained edge devices, including smartphones, laptops, and automobiles.

Impact on Specialised Hardware: While TriLMs offer significant memory reduction and latency improvements on General Purpose GPUs like H100 and RTX4090, certain specialized hardware benefits more from ternary modeling. Hardware (like Cerabras[4]) that supports high byte-to-flop ratio computations, can leverage the sparsity stemming from ternarization for speedup in both training as well as inference. On the other hand, hardware with limited Memory/SRAM (like Groq[5]), benefits from the reduction in the number of chips needed to deploy an LLM.

Reduced Training Costs: The Chinchilla scaling laws established that for training compute optimality, it may be recommended to train larger LLMs for fewer tokens than smaller LLMs for more tokens to achieve the desired model performance. However, memory requirements and latency associated with deployment of larger models, have motivated costlier training runs that go far beyond Chinchilla optimality. For example, a LLaMa 3 model with only 8B parameters was trained for 15T tokens. Since TriLM and ternary models, in general, can reduce the memory requirements and latency, this can motivate a shift inparameter-token tradeoff for efficient training runs towards Chinchilla's compute-optimal regime.

Advancing Research through Open Access: The open suite of TriLM, FloatLM, and QuantLM families aims to empower researchers to explore the nuanced impacts of precision levels on model performance and efficiency, thereby catalyzing ongoing advancements in the development and deployment of language models, as well as enhancing their interpretability and safety Li (2024). By providing a range of publicly accessible models trained on openly available data, the suite offers unprecedented transparency in the training process. Intermediate checkpoints are available for all models, accompanied by detailed documentation of training procedures and hyperparameters.

[4]https://www.cerebras.net/product-chip/

[5]https://groq.com/