On the Effectiveness of Lipschitz-Driven Rehearsal in Continual Learning

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Abstract

Rehearsal approaches enjoy immense popularity with Continual Learning (CL) practitioners. These methods collect samples from previously encountered data distributions in a small memory buffer; subsequently, they repeatedly optimize on the latter to prevent catastrophic forgetting. This work draws attention to a hidden pitfall of this widespread practice: repeated optimization on a small pool of data inevitably leads to tight and unstable decision boundaries, which are a major hindrance to generalization. To address this issue, we propose Lipschitz-DrivEn Rehearsal (LiDER), a surrogate objective that induces smoothness in the backbone network by constraining its layer-wise Lipschitz constants w.r.t. replay examples. By means of extensive experiments, we show that applying LiDER delivers a stable performance gain to several state-of-the-art rehearsal CL methods across multiple datasets, both in the presence and absence of pre-training. Through additional ablative experiments, we highlight peculiar aspects of buffer overfitting in CL and better characterize the effect produced by LiDER.

1 Introduction

The last few years have seen a renewed interest in aiding Deep Neural Networks (DNNs) to acquire new knowledge and, at the same time, retain high performance on previously encountered data. In this regard, the mitigation of *catastrophic forgetting* [44] has driven the recent research towards novel incremental methods [35, 56], often framed under the field of Continual Learning (CL).

Among other valid strategies, *rehearsal approaches* caught the attention of a large body of literature [52, 18, 12] thanks to their advantages. Simply, they maintain a small fixed-size buffer containing a fraction of examples from previous tasks; afterward, these examples are mixed together with the ones of the current task, hence provided continuously as training data. In this respect, different approaches establish different regularization strategies on top of the retained examples [53, 42], as well as which kind of information to store (*e.g.* model responses [12, 10], explanations [22], etc.).

In spite of their widespread application, these approaches fall into a common pitfall: as the memory buffer holds only a small fraction of past examples, there is a high risk of overfitting on that memory [62], thus harming generalization. Several approaches mitigate such an issue through data-augmentation techniques, either by generating different versions of the same buffer datapoint [6, 12] or by combining different examples into a single one [11, 9]. Other works [3, 4, 13, 70], instead, select carefully the valuable samples that should be inserted into the buffer: they argue that random selection may pick non-informative and noisy instances, affecting the model generalization.

This work tackles the issue described above from a different perspective, viewing *catastrophic forgetting* in the light of the progressive deterioration of decision boundaries between classes. Indeed, while for the examples of the current task we expect the decision boundaries to be already smooth and

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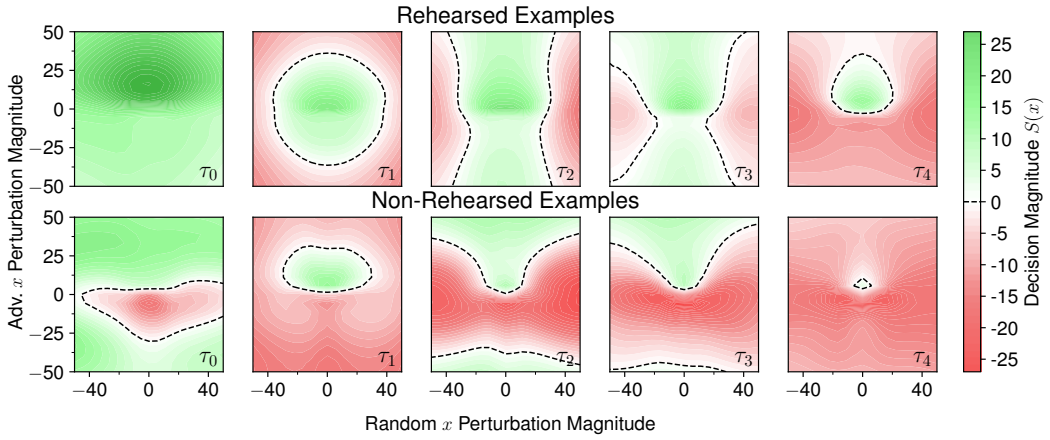
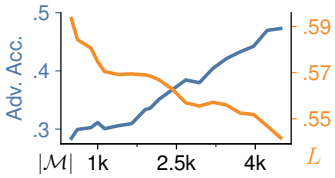


Figure 1: Diagrams derived from [72] describing how the magnitude of an input perturbation affects the model's prediction, measured as the difference between the correct logit and the maximum one. The dashed lines delimit the green areas, where the correct response is preserved. The analysis is carried out on the examples of the first task of Split CIFAR-10 and spans across tasks progressing, from τ_0 (left) to τ_4 (right). In different rows, the decision surfaces around datapoints either contained in the memory buffer (first) or non-rehearsed (second). We refer to Sec. 5.5 for additional insights.

robust against local perturbations, the same could not be said for past examples. Indeed, the restrained access to only a small portion of past tasks increases the epistemic uncertainty [32] of the model: as a consequence, we expect the decision surfaces tied to past classes to slowly erode everywhere, with the exception of certain input regions *i.e.*, those close to the neighborhood of buffer datapoints (thanks to their repeated optimization). We refer to Fig.1 for a visualization of such phenomenon, which shows the evolution of the decision surfaces around the points of the first task of Split CIFAR-10, from the first (*left*) to the last one (*right*). We differentiate the target of the analysis (rehearsed examples *vs.* non-rehearsed examples) in distinct rows: as can be seen, the green area – the input region where the model outputs correct predictions against local input perturbations [72]) – tightens around buffer datapoints (*first row*) and erodes for non-rehearsed examples (*second row*).

Such an intuition motivates our research of novel mechanisms for guaranteeing the robustness of the decision boundaries. To this aim, we resort to enforcing the Lipschitz continuity of the model w.r.t. its input: indeed, a long-standing research trend [69, 59, 38, 39, 67, 25] has pointed out that such a property favors generalization capabilities and robustness to adversarial attacks. In particular, constraining the Lipschitz constant of a model – intuitively, a bound on how much the model's response can change in proportion to a change in its input [5] – has proven to strengthen the decision surface around a point [19, 38, 39, 67, 76], preventing attacks of a given magnitude from changing the output of the classifier.



While these works assessed Lipschitz regularization in the classical scenario (*i.e.*, single joint i.i.d. task), we advocate that it is even more beneficial in continual learning, particularly for those approaches based on replay memories. As shown in the inset figure, without explicit regularization, the Lipschitz constant of a model increases for smaller memory buffers: in other terms, its corresponding function space becomes increasingly sensitive w.r.t. local input perturbations (as also highlighted by the lower accuracy attained in presence of adversarial attacks). In light of the above considerations, we ascribe such a tendency to the higher uncertainty, which derives from subjecting the model to a low-data training regime.

To the best of our knowledge, our work is the first attempt to assess the effectiveness of Lipschitz-constrained DNNs in continual learning, with several experiments and ablative studies supporting our intuition. In particular, we have equipped several widely-known and state-of-the-art rehearsal approaches with our Lipschitz-guided optimization objective named **Lipschitz-DrivEn Rehearsal (LiDER)**, showing that it systematically leads to better results in several benchmarks.

2 Related works

Continual Learning CL examines the capability of a deep model to learn from a sequence of non-i.i.d. classification tasks [20, 49] while preventing the onset of *catastrophic forgetting* [44]. To achieve this goal, models are trained according to specifically designed strategies, meant to influence their evolution and maximize the retention of previously acquired knowledge.

Among them, *regularization methods* work by introducing additional constraints in the form of loss terms; they are designed to limit the amount of total change either in parameter space [35, 74, 16, 2] or functional space [40, 8]. Differently, *structural methods* purposefully organize the allocation of model capacity to prevent interference and facilitate parameter sharing [1, 43, 54, 31]. Lastly, *rehearsal methods* store and reuse a subset of previously seen data-points to prevent overfitting on current data and avert forgetting [13, 42, 4, 3]. While *rehearsal* strategies are by far the most frequently adopted thanks to their effectiveness and flexibility [23, 4], it is not uncommon to adopt solutions combining multiple approaches [28, 1, 12, 50, 15]. In this paper, we similarly propose a strategy that leverages an existing replay memory buffer to compute an additional regularization term, aimed at conditioning the learning dynamics and avoiding overfitting.

CL evaluations are often carried out in the so-called Task-Incremental setting (TIL) [35, 74, 42, 20, 16] – that is, the model is provided a *task identifier* at test time to restrict its predictions and avoid interference across logits of distinct tasks. However, recent works put an increasing focus on the harder Class-Incremental setting (CIL) [4, 28, 12, 68], which entails the production of a unified prediction encompassing all seen classes. W.r.t. the latter, TIL has been criticized as a less challenging and realistic benchmark [23, 61, 4]; we therefore conduct our main experiments on state-of-the-art CL models in the CIL setting[1].

Lipschitz-based Regularization Naturally trained DNNs typically suffer from their overparametrization [75, 48], leading to the tendency to overfitt the training data by producing jagged decision boundaries that closely fit the seen examples. On the contrary, a model's reliability depends on its capability for generalization, which is linked to the appearance of smooth decision boundaries [69, 7, 71, 25]. Starting from the first studies focusing on this simple dichotomy, the Lipschitz constant L of a DNN has been established as a commonplace measure of both smoothness and generalization [69, 59, 33] and still constitutes a key ingredient for current evaluations of model capacity [7, 26].

Most notably, *Szegedy et al.* [59] verify that constraining L reduces the model's vulnerability to adversarial perturbations. Many current approaches to Adversarial Learning similarly operate either by minimizing L at the *global* or *local* level [39, 60, 38] or by devising models characterized by a small L by design [19, 29]. In other areas, the smoothing effect of L-based regularization has been favorably applied to both GAN training [46] and neural fields [41].

3 Method

A CL problem usually involves learning a function f from a stream of data, which we formalize as a succession of separate datasets $T = \{\tau_0, \tau_1, \dots, \tau_{|T|}\}$, where $\tau_t = \{(\mathbf{x_i}, y_i)\}_{i=1}^{N_t}$ and $\tau_i \cap \tau_j = \varnothing$; the label set Y_t for each τ_t are non-overlapping. In this setting, the ideal objective consists in minimizing the overall loss over all tasks experienced, formally:

$$f^* = \underset{f}{\operatorname{argmin}}\, \mathbb{E}_{t=0}^{|T|}\Big[\mathbb{E}_{(\mathbf{x},y)\sim\tau_t}\Big[\mathcal{L}(f(\mathbf{x}), y)\Big]\Big], \tag{1}$$

where $\mathcal{L}$ is an appropriate loss for solving the task at hand. In a continual scenario, only data from the current task τ_t is freely available; therefore, CL methods need to maintain knowledge from the past $t-1$ tasks in order to solve the overall problem.

For the sake of simplicity, we consider a feed forward neural network $f(\cdot) = (H^K \circ \sigma^K \circ H^{K-1} \circ \sigma^{K-1} \circ \dots H^1)(\cdot)$, *i.e.*, a sequence of σ-activated linear functions $H^k(\mathbf{h}) = \mathbf{W}_k^T\mathbf{h}$ (biases are omitted). A final projection head $g(\cdot) = \mathrm{softmax}(\cdot)$ is applied to produce per-class output probabilities. As stated in other works [25], other common transformations that make up DNNs (*e.g.*, convolutions,

[1] However, we remark that TIL can also be useful, as it reveals *forgetting* disentangled from other incremental learning effects. This motivates us to adopt TIL in some of our additional experiments.

max-pool) can also be seen in terms of matrix multiplications, thus making our approach applicable to more complex networks.

Lipschitz continuity. A function f is said to be *Lipschitz continuous* if there exists a value $L \in \mathbb{R}^+$ such that the following inequality holds:

$$||f(\mathbf{x}) - f(\mathbf{y})||_2 \leq L||\mathbf{x} - \mathbf{y}||_2, \quad \forall \mathbf{x}, \mathbf{y} \in \mathbb{R}^n. \tag{2}$$

If such a value exists, the smallest L that satisfies the condition is usually referred to as the Lipschitz norm $||f||_L$. Therefore, for a single point $x \in \mathbb{R}^n$, we obtain:

$$||f||_L = \sup_{x \neq y; y \in \mathbb{R}^n} \frac{||f(\mathbf{x}) - f(\mathbf{y})||_2}{||\mathbf{x} - \mathbf{y}||_2}. \tag{3}$$

Unfortunately, computing the Lipschitz constant of even the most simple multi-layer perceptron is a NP-hard problem [64]. Therefore, several works relied on its estimation by computing reliable upper bounds. As stated in [71, 55], an effective way to bound the Lipschitz constant of $f(\cdot)$ is to compute the constants of each linear projections H^k and then aggregate them. In more details:

$$||H^k||_L = \sup_{x \neq y; y \in \mathbb{R}^n} \frac{||W^T\mathbf{x} - W^T\mathbf{y}||_2}{||\mathbf{x} - \mathbf{y}||_2} = \sup_{\xi \neq 0; \xi \in \mathbb{R}^n} \frac{||\mathbf{W}_k \xi||_2}{||\xi||_2} = \sigma_{\max}(\mathbf{W}_k), \tag{4}$$

where $\sigma_{\max}(\mathbf{W}_k)$ is the largest singular value of the weight matrix $\mathbf{W}_k$ (also know as its spectral norm $||\mathbf{W}_k||_{SN}$). To account for non-linear composite functions (*e.g.*, the residual building blocks of most convolutional architecture), we leverage the following inequality:

$$\begin{aligned} ||g(z(\mathbf{x})) - g(z(\mathbf{y}))||_2 &\leq ||g||_L ||z(\mathbf{x}) - z(\mathbf{y})||_2 \\ &\leq ||g||_L ||z||_L ||\mathbf{x} - \mathbf{y}||_2 \Rightarrow ||z \circ g||_L \leq ||g||_L ||z||_L, \end{aligned}$$

where $\mathbf{g}(\cdot)$ and $\mathbf{z}(\cdot)$ are two Lipschitz continuous functions characterized by the constants $||g||_L$ and $||z||_L$. In the case of ReLU-activated networks (but the following result can be extended to other common non-linear functions), the forward pass through σ^l $l = 1, 2, \ldots, L$ can be re-arranged as a matrix multiplication by a diagonal matrix $D^l \in \mathbb{R}^{d_l \times d_{l+1}}$ whose diagonal elements equal either zero or one. Therefore, their corresponding Lipschitz constant $||\sigma^l||_L \leq 1$. On top of that, we can compute an upper bound on the Lipschitz constant of the entire network:

$$||f||_L \leq ||H^K||_L \cdot ||\sigma^K||_L \cdot \ldots \cdot ||H^1||_L \leq \prod_{k=1}^{K} ||H^k||_L = \prod_{k=1}^{K} ||\mathbf{W}^k||_{SN}. \tag{5}$$

Computing the spectral norm of weights matrices. The computation of $||\mathbf{W}_k||_{SN}$ can be done [46, 25] naively through the Singular Value Decomposition (SVD), yielding, among the others, the largest singular value. Such approach has been applied in recent works [46, 25]; however, for complex structures (*e.g.*, convolutions or entire residual blocks) the SVD decomposition is inaccessible. Hence, we rely on the approximation introduced in [55] and compute the largest eigenvalue λ_1^k of the Transmitting Matrix $\mathbf{TM}^k$ (which represents a good proxy of $||\mathbf{W}^k||_{SN}$[2]):

$$\mathbf{TM}^k \triangleq \left[(\mathbf{F}^k)^T(\mathbf{F}^{k-1})\right]^T \left[(\mathbf{F}^k)^T(\mathbf{F}^{k-1})\right], \tag{6}$$

where $\mathbf{F}^k \in \mathbb{R}^{B \times d_k}$ is the L2-normalized feature map produced by the l-th layer from a batch of B samples. Finally, our approach exploits the power iteration method [47] to compute the largest eigenvalue of $\mathbf{TM}^k$, which is backpropagation-friendly.

3.1 Lipschitz-Driven Rehearsal

In a continual setting, a model is asked *i)* to be adaptable to incoming samples from the stream (plasticity), and *ii)* to be accurate on past tasks (stability). We seek to ensure a balance between these clashing objectives through the two following loss terms.

Controlling Lipschitz-continuity. To mitigate overfitting on buffer datapoints, we firstly impose that each layer behaves as a c-Lipschitz continuous function, for a given real positive target constant c_k:

$$\mathcal{L}_{\text{c-Lip}} = \frac{1}{K} \sum_{k=0}^{K} |\lambda_1^k - c_k|. \tag{7}$$

[2]We refer the reader to [55] for additional justifications for this step.

During the computation of each λ_1^k, we discard the activation maps incoming from the examples of the current task. Indeed, as we have access to the entire training set (and not a subset as holds for old tasks), additional regularization is not needed: the decision boundaries tied to the current task are less prone to the risk of over-adapting to certain points. Regarding the target constants c_k, we could fix them as hyperparameters of our learning objective (as done in [41]) and exploit them as a sort of budget assigned to each layer; however, we empirically observed that it is beneficial, instead, learning these targets by means of gradient descent (see Sec. 5.4), especially in a CL scenario where there is no access to the full data distribution. Indeed, these can be interpreted as additional learnable parameters, which represent the appropriate level of strictness each layer should be subjected to.

Therefore, to avoid trivial solutions, we add another regularization term, which asks these constant to be as much as possible close to zero:

$$\mathcal{L}_{\text{0-Lip}} = \frac{1}{K} \sum_{k=0}^{K} |c_k|. \tag{8}$$

Intuitively, when $\lambda_1^k \to 0$, the outputs of the corresponding k-th layer has low sensitivity to changes in its input. In our intentions, this could relieve continuous rehearsal from eroding the decision surface in a way that fits well only certain examples (*i.e.*, those retained in the memory buffer).

Overall objective. The overall objective of LiDER combines the two introduced loss terms; formally:

$$\mathcal{L}_{\text{LiDER}} = \alpha \mathcal{L}_{\text{c-Lip}} + \beta \mathcal{L}_{\text{0-Lip}}. \tag{9}$$

This objective can be plugged in almost any rehearsal approach. For such a reason, we keep it general and avoid reporting the common loss terms asking for accurate predictions, as their form depend on the specific choices made by each approach. Finally, we further remark that the introduced loss terms require minimal additional computation. Moreover, they do not need additional samples to be retained, besides those that are already present in the memory buffer.

4 Experiments

To assess the effectiveness of our proposal, we introduce a suite of experiments encompassing the prevalent applications of rehearsal in modern literature. In particular, we show that our method can be easily applied to state-of-the-art replay methods and enhance their performance in a wide variety of challenging settings and backbone architectures. Moreover, we show that our proposal remains rewarding and can improve the generalization capabilities of CL models even when a pre-trained model is employed. Such scenario is important for a twofold reason: i) as shown in [45], pre-training implicitly mitigates forgetting by widening the local minima found in function space, thus making the model more robust to input perturbations; additionally, ii) we accommodate for real-world scenarios where pre-training is usually involved as an initial step. Due to space constraints, for additional experimental details we kindly refer the reader to the supplementary material.

Benchmarked models. We conduct experiments on multiple state-of-the-art rehearsal-based models. If not specified, all methods use reservoir sampling [65] to update the memory buffer.

- **Experience Replay with Asymmetric Cross-Entropy (ER-ACE)** [14]: the authors devise an improvement over standard ER with a separate loss for data coming from the stream and from the buffer. Consequently, they observe a significant performance gain, which shows the importance of reducing the drift in incrementally learned representations.
- **Dark Experience Replay (DER)** [12]: the authors propose an improvement over ER to take advantage high-level knowledge previously learned by means of self-distillation [24]. In addition to storing the one-hot labels, they also include the pre-softmax activations (logits) of the model sampled along the optimization trajectory; subsequently, they enforce consistent responses through time by minimizing the L2 norm between current and past logits. In this work, we use DER++, a stronger baseline that combines standard replay and self-distillation.
- **Incremental Classifier and Representational Learning (iCaRL)** [52]: instead of training a classifier to solve the task directly, the authors propose to learn a representation suitable for a nearest-neighbor classification w.r.t. class prototypes stored in the buffer. Additionally, forgetting is prevented by distilling the responses of the model's snapshot at the previous task to both current

and replay examples. Since samples in the buffer have a major role as anchors for classifications, the buffer is managed through the herding strategy.

- **Greedy Sampler and Dumb Learner (GDumb)** [51]: the authors challenge the improvements made on CL literature, in which the authors propose to simply train the model at the task boundary solely on data from the buffer.

4.1 Datasets & measures

We focus our evaluation on the CIL setting and rely on commonly used and challenging image classification tasks. In each experiment, classes from the main dataset are split into separate and disjoint sets, which are then used sequentially to train the evaluated models.

Split CIFAR-100. An initial evaluation is carried by splitting the 32×32 images from the 100 classes of CIFAR-100 [36] into 10 tasks. In detail, we run two tests: *i)* using a randomly initialized ResNet18 [27] – which constitutes a common scenario in literature [74, 52, 18, 13]; *ii)* adopting the same backbone but with its parameters pre-trained on Tiny ImageNet [58].

Split *mini*ImageNet. This setting is designed to evaluate the robustness of models on longer sequences of tasks, by splitting the 100 classes of *mini*ImageNet [63] – a subset of the ImageNet dataset, where each image is resized to 84×84 – into 20 consecutive tasks. For this test, we opt for an EfficientGCN-B2 [57] backbone with no pre-train.

Split CUB-200. A final, more challenging benchmark involves classifying large-scale 224×224 images from the Caltech-UCSD Birds-200-2011 [66] dataset, organized in a stream of 10 20-fold classification tasks. This evaluation is designed to highlight the importance of protecting pre-trained weights from forgetting. Indeed, due to the limited size of the training set, competitive performance can only be achieved if each task can benefit from the initialization [17, 73]. As backbone network, we opt for the commonly available ResNet50 architecture pre-trained on the ImageNet dataset [21].

For each benchmark we measure performance in terms of the classification accuracy averaged across all seen tasks (Final Average Accuracy - FAA) and of Final Forgetting (FF) [16], formally defined as:

$$\text{FF} \triangleq \frac{1}{|T|-1} \sum_{i=0}^{|T|-2} \max_{t \in \{0,\dots,|T|-2\}} \{a_i^t - a_i^{|T|-1}\}, \tag{10}$$

where a_i^t indicates the accuracy on task τ_i after training on the tth task.

4.2 Results

Results of our evaluation on Split CIFAR-100 can be found in Tab. 1, while results on Split CIFAR-100, and Split *mini*ImageNet are in Tab. 2. For further reference, each table includes the results of a model jointly trained on all classes – which represents an ideal non-CL upper bound – and of a model sequentially trained on each task, with no countermeasure to forgetting.

Across the board, we find LiDER to be capable of improving the performance of all base methods in all evaluated scenarios, both in terms of FAA and FF metrics. Most notably, we find it especially beneficial for methods that feature the most compelling results – usually DER++ and iCaRL –, suggesting that their higher generalization capability can still benefit from increased smoothness in latent space. Differently, scenarios where a method fail to prevent forgetting *i.e.* GDumb with a reduced buffer size usually feature a lower degree of benefit from LiDER but still a notable improvement. However, as it takes advantage both from increased buffers and pre-trained initialization, we observe a considerable performance gap with our proposal. Notably, on Split CIFAR-100, GDumb with a buffer size of 500 moves from a performance gain of $+0.98\%$ to $+6.46\%$ when increasing the buffer to 2000 samples and $+2.99\%$ with pre-train.

Finally, we observe an average performance gain of 2.32%, 2.08%, and 4.36% on Split CIFAR-100, Split *mini*ImageNet, and Split CUB-200 respectively.

5 Ablation studies

In the following sections we provide further insights on the effectiveness of our proposal in controlling and improving the generalization capabilities of the base models.

Table 1: Final Average Accuracy (FAA) [↑] and Final Forgetting (FF) [↓] on Split CIFAR-100.

CIL FAA (FF)	**Split CIFAR-100**			
Method	*w/o pre-training*		*pre-tr. Tiny ImageNet*	
Joint (UB)	73.29 (–)		75.20 (–)	
Finetune	09.29 (86.62)		09.52 (92.31)	
Buffer Size	500	2000	500	2000
iCaRL [52]	44.04 (21.70)	50.23 (17.92)	56.00 (19.27)	58.10 (16.89)
+ **LiDER**	47.02 (21.89)	51.21 (17.13)	57.24 (19.16)	60.97 (15.49)
DER++ [12]	37.13 (49.80)	52.08 (31.10)	43.65 (48.72)	58.05 (29.65)
+ **LiDER**	39.25 (45.50)	53.27 (27.51)	45.37 (48.16)	60.88 (25.16)
GDumb [51]	09.28 (–)	19.69 (–)	23.09 (–)	36.05 (–)
+ **LiDER**	10.22 (–)	26.15 (–)	26.09 (–)	41.98 (–)
ER-ACE [14]	36.48 (38.21)	48.41 (27.90)	48.19 (31.84)	57.34 (25.48)
+ **LiDER**	38.43 (36.00)	50.32 (28.30)	48.97 (28.58)	57.39 (25.37)

Table 2: Final Avg. Accuracy (FAA) [↑] and Final Forgetting (FF) [↓] on Split *mini*ImageNet and Split CUB-200.

CIL FAA (FF)	**Split *mini*ImageNet**		**Split CUB-200**	
Method	*w/o pre-training*		*pre-tr. ImageNet*	
Joint (UB)	53.55 (–)		78.54 (–)	
Finetune	04.51 (77.38)		08.56 (82.38)	
Buffer Size	2000	5000	400	1000
iCaRL [52]	22.58 (16.46)	22.78 (16.37)	56.52 (13.43)	60.09 (11.41)
+ **LiDER**	23.22 (11.21)	23.95 (11.18)	57.12 (14.31)	60.37 (10.89)
DER++ [12]	23.44 (46.69)	30.43 (37.11)	49.30 (36.05)	61.42 (19.95)
+ **LiDER**	28.33 (36.29)	35.04 (25.02)	57.90 (27.55)	67.97 (14.44)
GDumb [51]	15.22 (–)	27.79 (–)	09.36 (–)	18.98 (–)
+ **LiDER**	15.24 (–)	29.49 (–)	09.67 (–)	19.51 (–)
ER-ACE [14]	22.60 (23.74)	27.92 (19.72)	41.83 (26.42)	51.98 (18.79)
+ **LiDER**	24.13 (25.97)	30.00 (19.99)	50.89 (20.79)	60.92 (14.62)

5.1 Buffer Poisoning

To evaluate the performance of a ML model, practitioners usually resort to synthetic benchmarks that simulate the progressive arrival of novel knowledge from an unknown source. While this methodology is useful to compare the effectiveness of new proposals a key element is usually neglected: the labels given to each sample may – and in the real-world usually does – be incorrect. Notably, this aspect is even more relevant in a CL scenario and especially when a rehearsal strategy is employed. As previously shown, samples included in the buffer are the ones that are most likely to be overfitted, which would induce a severe loss of performance if the label is incorrect.

In the following, we propose to measure the negative effect of overfitting the wrong label for samples included in the memory buffer. Specifically, we simulate noise in the labels by randomly assigning with probability p a new label to the samples as these are added in the buffer, a technique which we name *label poisoning*. To better suit a CL scenario, poisoned labels are chosen from those of the current task.

Results reported in Tab. 3 show the evaluation performed on top of DER++ for the Split CIFAR-100 benchmark. As one could expect, performance degrades as p increases; however, we also observe that LiDER retains an higher level of accuracy against poisoning. This effect suggests that our proposal leads to a looser decision boundary around the items store in the buffer.

Table 3: FAA after poisoning the buffer for DER++ with and without LiDER.

p	DER++	+LiDER
.0%	37.14	39.25
.01%	36.13	38.08
.1%	31.35	35.53
.25%	28.74	30.78

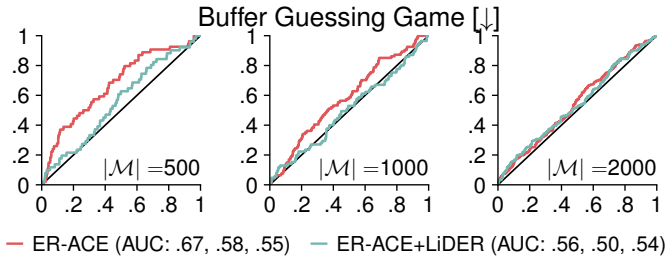


Figure 2: ROC curves for the Buffer Guessing Game, showing the likelihood of a given sample belonging in $\mathcal{M}$.

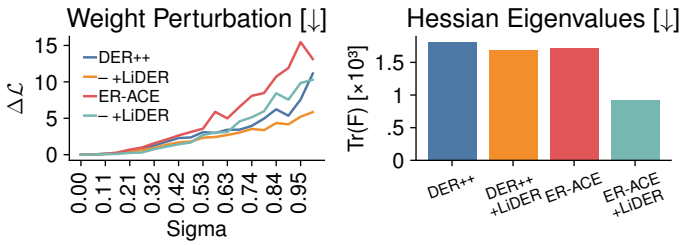


Figure 3: (Left) Robustness of models regularized with LiDER against weight perturbations (best seen in color). (Right) Flatness around the minima found during optimization, measured as the sum of the eigenvalues of the Hessian matrix.

Table 4: Performance comparison between LiDER and a regularization method obtained by fixing the Lipschitz targets in Eq. 7.

	Model	$\lvert\mathcal{M}\rvert$	Fixed tgt	*Eq. 9*
w/o pre-tr.	DER++	500	36.42	39.25
	ER-ACE	2000	34.99	38.43
	DER++	500	51.52	53.27
	ER-ACE	2000	46.70	48.97
pre-tr.	DER++	500	43.16	45.37
	ER-ACE	2000	45.21	48.97
	DER++	500	59.53	60.68
	ER-ACE	2000	54.82	57.39

5.2 Buffer Guessing Game

In this section, we set up a novel experiment aimed at further illustrating the peculiar overfitting behavior of rehearsal-based CL models. As mentioned in Sec. 1, we posit that a substantially different regime affects replay and stream examples: the former plays a much larger role in shaping the decision boundary w.r.t. the latter. To validate this intuition, we propose a simple *buffer guessing game*: given a rehearsal-based model f fully trained on a CL benchmark and the dataset τ_0 used in its first encountered task, we aim to find $\mathcal{M} \cap \tau_0$ (*i.e.* the subset of data-points that are included in the model's buffer).

We approach the game by associating each $x \in \tau_0$ with a score s_x computed as the mean height of the decision surface of f in a neighborhood of x[3]; finally, we evaluate the ROC curve obtained from these scores. In Fig. 2, we report the results obtained for ER-ACE and ER-ACE+LiDER on Split CIFAR-100 across different buffer sizes. We see that: *i)* ER-ACE makes it is easier to reconstruct the content of the buffer, as indicated by larger ROC-AUC scores w.r.t. ER-ACE+LiDER; *ii)* in line with our expectations, this effect is increased when employing smaller memory buffers, as this leads to the repeated optimization of a smaller pool of data.

5.3 Generalization Measures

Previous CL works proposed investigating the generalization capabilities of a CL model by evaluating the flatness of its attained minima [12, 10]. We likewise evaluate the effect of LiDER both in terms of its resilience to weight perturbations [48, 33] and the eigenvalues of the Hessian of the loss function [33, 30] in Fig. 3. We see that DER++ and ER-ACE combined with LiDER see an improvement of both metrics. This is expected, as the Lipschitz constant of a DNN has been commonly interpreted as a generalization measure [69, 59].

[3] We compute the decision surface by leveraging random perturbations as specified in [72] and compute it w.r.t. to the TIL prediction function to avoid the influence of inter-task biase on our results

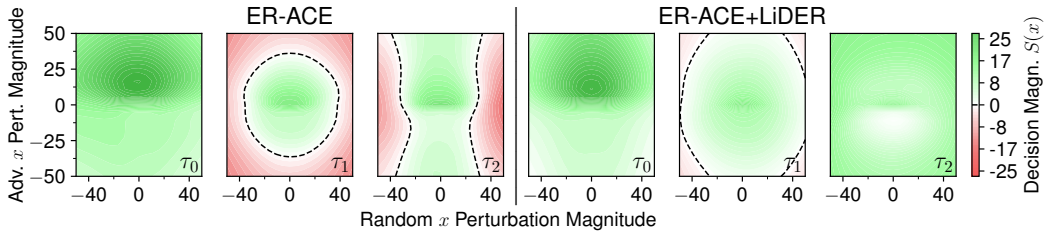


Figure 4: Effect of our proposal on the robustness of the decision boundary produced by ER-ACE across subsequent tasks. Higher values (in green) indicate areas of high confidence and span the possible directions where perturbations are not disruptive (best seen in color).

5.4 Optimization with a fixed target

Instead of constraining the optimization of the Lipschitz targets of Eq. 7 by an additional contribution, one might argue that a similar effect could be obtained by fixing an initial value and force the model to reduce its capacity until it meets the desiderata [41]. In Tab. 4 we empirically show that such approach does not lead to satisfactory results in a CL setting, with our proposal consistently exceeding its performance on various settings and base methods.

5.5 Decision Landscape of LiDER

In Fig. 1, we presented a pictorial demonstration of a model's tolerance to input perturbations in the form of a decision surface plot [72]. Such a visualization is constructed by focusing on a set of perturbations $x_p \triangleq x + i \cdot \alpha + j \cdot \beta$ computed around a data-point x (α is a random divergence direction and β corresponds to the direction induced by the first step of a non-targeted FGSM attack [37]). The plot shows the respective values of the decision function $S(x_p)$, where $S(x) \triangleq f(x)_t - \max_{i \neq t} f(x)_i$ (with $f(\cdot)$ indicating pre-softmax responses) and highlights decision boundary of the model (*i.e.* the locus of $\{x_p | S(x_p) = 0\}$), in correspondence of which the model accuracy fails.

In Fig. 4, we adopt the same approach to compare the decision boundaries around rehearsed τ_0 examples for ER-ACE with and without LiDER. It can be observed that, while both models start with a similar robust decision landscape in τ_0, later tasks reveal a clear shrinking behavior in ER-ACE. On the contrary, introducing L-based regularization hardens the backbone against adversarial perturbations, leading to minimal decision boundary deterioration in later tasks.

6 Conclusions

We present LiDER, a novel regularization strategy to compensate for the phenomenon of buffer overfitting in rehearsal-based Continual Learning; with its carefully-designed loss term it enforces the decision boundary of replayed samples to be smoother by bounding the complexity of the model. We show that such approach can be readily applied to diverse state-of-the-art models and remains competitive across various settings and backbone architecture. Finally, we provide an extensive investigation to assess the validity of theoretical assumptions.

Limitations & Societal Impact

Our approach heavily relies on the estimation of the Lipschitz constant and, in particular, on its upper bound (as reported in the previous section, the exact computation is a NP-hard problem). We highlight that tighter bounds have been recently proposed, at the expense of higher complexity and hence slower computation speed. Moreover, the approximation exploited in this work cannot be naively applied to those architectures comprising of not-Lipschitz continuous layers (*e.g.*, cross-attention) [34].

Concerning societal impact, we do not feel that this work will have detrimental applications that might affect any public. We only remark that, as our approach is based on rehearsal techniques that store in-plain data, it cannot be used in those scenario where privacy constraints are crucial.

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Checklist

1. For all authors...
   (a) Do the main claims made in the abstract and introduction accurately reflect the paper's contributions and scope? [Yes]
   (b) Did you describe the limitations of your work? [Yes]
   (c) Did you discuss any potential negative societal impacts of your work? [Yes]
   (d) Have you read the ethics review guidelines and ensured that your paper conforms to them? [Yes]
2. If you are including theoretical results...
   (a) Did you state the full set of assumptions of all theoretical results? [Yes]
   (b) Did you include complete proofs of all theoretical results? [Yes]
3. If you ran experiments...
   (a) Did you include the code, data, and instructions needed to reproduce the main experimental results (either in the supplemental material or as a URL)? [Yes] The code for reproducing our experiments can be found in the supplemental material and will be made publicly available at publication.
   (b) Did you specify all the training details (e.g., data splits, hyperparameters, how they were chosen)? [Yes] We cover these aspects in the main paper (Sec. 4) and, more in depth, in the supplemental materials.

(c) Did you report error bars (e.g., with respect to the random seed after running experiments multiple times)? [Yes] Due to space constraints, variance values for our experiments are included in the supplemental material.

(d) Did you include the total amount of compute and the type of resources used (e.g., type of GPUs, internal cluster, or cloud provider)? [No] Experiments were conducted on an on-premise desktop machine, equipped with a RTX 2080 consumer GPU. However, we did not keep a detailed record of total computation time.

4. If you are using existing assets (e.g., code, data, models) or curating/releasing new assets...

(a) If your work uses existing assets, did you cite the creators? [Yes] In our work we use original code, with the only exceptions for the evaluation datasets whose original papers are cited.

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(d) Did you discuss whether and how consent was obtained from people whose data you're using/curating? [N/A]

(e) Did you discuss whether the data you are using/curating contains personally identifiable information or offensive content? [N/A] We use datasets commonly established and used in literature, for which, to the best of our knowledge, the issues mentioned above have never been found to affect them.

5. If you used crowdsourcing or conducted research with human subjects...

(a) Did you include the full text of instructions given to participants and screenshots, if applicable? [N/A]

(b) Did you describe any potential participant risks, with links to Institutional Review Board (IRB) approvals, if applicable? [N/A]

(c) Did you include the estimated hourly wage paid to participants and the total amount spent on participant compensation? [N/A]