Secure Domain Adaptation with Multiple Sources

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Abstract

Multi-source unsupervised domain adaptation (MUDA) is a recently explored learning framework within UDA, with the goal of addressing the challenge of annotated data scarcity in a target domain via transferring knowledge from multiple source domains with annotated data. When the source domains are distributed, data privacy and security can become significant concerns and protocols may limit data sharing, yet existing MUDA methods overlook these constraints. We develop an algorithm to address MUDA when source domain data cannot be shared with the target or across the source domains. Our method is based on aligning the distributions of source domains and the target domain indirectly via internally learned representations in an intermediate embedding space. We provide theoretical analysis to support our approach and conduct extensive empirical experiments to demonstrate that our algorithm is effective and compares favorably against existing MUDA methods.

1 Introduction

Advances in deep learning have led to significant increase in the performance of machine learning (ML) algorithms in a wide range of applications (Russakovsky et al. (2015)). However, deep learning relies on access to large quantities of labeled data for extracting informative representations from the inputs through end-to-end training. Due to the complexity of state-of-the-art neural networks, deep learning struggles in domains where annotated data is scarce. Even if a neural model is trained using annotated data, in settings where domain-shift (Torralba & Efros (2011)), i.e., distributional differences in the input space, exists between the training domain and deployment domain, neural models have been shown to suffer from sub-optimal performance. In such scenarios, the naive solution is to retrain the models on each domain where the input data distribution differs from that of the original training dataset. This operation however necessitates annotating large databases persistently, which has proven to be a time-consuming and expensive manual process. Unsupervised Domain Adaptation (UDA) (Long et al. (2016)) is a learning framework developed to address the challenge of domain-shift and permit model generalization between a *source domain* which has access to *labeled data* and a related *target domain* in which only *unannotated data* is accessible.

UDA has been explored using various approaches. An effective technique to address UDA is to map data points from a source domain and a target domain into a shared latent embedding space at which distributions for both domains are aligned. Since domain-shift is mitigated in the latent space, a source-trained classifier receiving latent features as input would successfully generalize on the target domain. The latent embedding space is often modeled as the output-space of a deep encoder network, trained to produce a shared representation for the source and target. This outcome can be achieved using adversarial learning (Hoffman et al. (2018); Dou et al. (2019); Tzeng et al. (2017); Bousmalis et al. (2017)), where the distributions are matched indirectly through generator and discriminator networks that are trained to compete against each other such that the generator network extracts domain-agnostic discriminative features from both domains. The challenge of using adversarial learning is it often requires careful optimization initialization and is dependant on optimal hyper-parameters. Alternatively, a probability metric can be selected and then minimized to align the distributions directly in the embedding space(Chen et al. (2019); Sun et al. (2017); Lee et al. (2019)).

Most existing UDA algorithms consider a single source domain for knowledge transfer. Recently, single-source unsupervised domain adaptation (SUDA) has been extended to multi-source unsupervised domain adaptation (MUDA), where several distinct sources of knowledge are available for model training (Xu et al.

(2018); Guo et al. (2018); Peng et al. (2019a); Redko et al. (2019); Zhao et al. (2020); Wen et al. (2020b); Lin et al. (2020); Guo et al. (2020); Tasar et al. (2020); Venkat et al. (2020a)). The goal in MUDA is to benefit from the collective information encoded in several distinct annotated source domains to improve model generalization on an unannotated target domain. Compared to SUDA, MUDA algorithms require leveraging data distribution discrepancies between pairs of source domains, as well as between the sources and the target. Thus, an assumption in most MUDA algorithms is that the annotated source datasets are centrally accessible. Such a premise however ignores privacy/security regulations, or limitations in bandwidth, that may constrain or outright remove the possibility of joint data access between source domains.

In practice, it is natural to assume source datasets are distributed amongst independent entities, and sharing data between them may constitute a privacy violation. For example, improving mobile keyboard predictions is performed by securely training models on independent computing nodes without centrally collecting user data (Yang et al. (2018)). Similarly, in medical image processing applications, data is often distributed amongst different medical institutions. Due to privacy regulations (Yan et al. (2021)) sharing data can be prohibited, and hence central access to data for all the source domains simultaneously becomes infeasible. MUDA algorithms can offer privacy between the sources and target by operating in a source-free regime (Ahmed et al. (2021)), i.e., during the adaptation process source samples are considered to be unavailable, and only the source trained model or source data statistics are assumed to be accessible. However, approaches operating under this premise require retraining if new source domains become available, or if a set of source domains becomes inaccessible. This downside leads to increased time and computational resource cost.

We develop an algorithm capable of relaxing the need for centralized processing of source data in the MUDA setting, while also maintaining privacy between the source domains and the target domain. Additionally, our approach is robust to changes in the accessibility of different source domains, allowing for relearning the target decision function without the need of end-to-end retraining. We relax the need for directly accessing source domain samples via learning latent estimations of domain specific source features via a distribution estimation approach after processing each source domain. We perform source free adaptation with respect to each source domain, and propose a novel confidence based pooling mechanism to estimate the target feature distribution to broaden the applicability of the MUDA setting. Our main contributions are as follows:

1. We address the challenge of data privacy for MUDA by maintaining full privacy between pairs of source domains, and between source domains and the target domain.

2. We propose an efficient distributed optimization process for MUDA to process each dataset locally while encoding high-level learned knowledge in a shared latent embedding space.

3. We provide theoretical justification for our method by proving that our algorithm minimizes an upper-bound of the target error. We conduct extensive empirical experimental results on five standard MUDA benchmark datasets to demonstrate the effectiveness of our approach.

2 Related work

Our work is related to several subareas of the domain adaptation literature.

Single-Source UDA: Single source UDA is the most common setting of UDA and aims to improve model generalization for an unlabeled target domain using only a single source domain with annotated data. SUDA has been studied extensively, with many algorithms being explored in literature. A primary workflow employed in recent UDA works consists of training a deep neural network jointly on the labeled source domain and the unlabeled target domain to achieve distribution alignment between both domains in a latent embedding space. This goal has been achieved by employing generative adversarial networks (Goodfellow et al. (2014)) to encourage domain alignment (Hoffman et al. (2018); Dhouib et al. (2020); Luc et al. (2016); Tzeng et al. (2017); Sankaranarayanan et al. (2018)) as well as directly minimizing an appropriate distributional distance between the source and target embeddings (Long et al. (2015; 2017b); Morerio et al. (2018)). However, SUDA algorithms do not leverage inter-domain statistics in the presence of several source domains, and thus extending single-source UDA algorithms to a multi-source setting is a nontrivial task.

Multi-Source UDA: The MUDA setting is a recent extension of SUDA, where multiple streams of data are concomitantly leveraged for improved target domain generalization. Xu et al. (2018) minimize discrepancy between source and target domains by optimizing an adversarial loss. Peng et al. (2019a) adapt on multiple domains by aligning inter-domain statistics of the source domains in an embedding space. Guo et al. (2018) learn to combine domain specific predictions via meta-learning. Venkat et al. (2020a) use pseudo-labels to improve domain alignment. The increased amount of source data in MUDA is not necessarily an advantage over SUDA, as negative transfer between domains needs to be controlled during adaptation. Li et al. (2018) exploit domain similarity to avoid negative transfer by leveraging model statistics in a shared embedding space. Zhu et al. (2019) achieve domain alignment by adapting deep networks at various levels of abstraction. Zhao et al. (2020) align target features against source trained features via optimal transport, then combine source domains proportionally to Wasserstein distance. Wen et al. (2020a) use a discriminator to exclude data samples with negative generalization impact. Such approaches admit joint access to source domains during the training process, making them infeasible in settings where data privacy and security are of concern.

Privacy in Domain Adaptation: The importance of inter-domain privacy has been recognized and explored for single-source UDA, specifically in source-free adaptation. Note this framework is relevant in many important practical settings even for SUDA, where privacy regulations limit the possibility of sharing data (Peng et al. (2019b); Li et al. (2020); Liang et al. (2020; 2021)). Privacy preserving for MUDA is a relatively unexplored problem. Peng et al. (2019b) perform collaborative adaptation under privacy restrictions between source domains under the framework of federated learning. Ahmed et al. (2021) approach privacy-preserving MUDA via information maximization and pseudo-labeling. Unlike our approach, Ahmed et al. (2021) require simultaneous access to all source trained models during adaptation, which may lead to privacy violations. We address a more constrained yet practical setting, where privacy should be preserved both between pairs of source domains and with respect to the target. This assumption is more practical because if privacy is a concern, it should be preserved irrespective of a domain being a source or a target domain. Additionally, our approach allows for efficient distributed optimization, not requiring end-to-end retraining if different source domains become inaccessible due to privacy obligations, or more source domains become available after initial training has finished, allowing for accumulative learning from several domains.

Our approach builds on extending the idea of probability metric minimization, explored in UDA (Morerio et al. (2018); Bhushan Damodaran et al. (2018); Chen et al. (2019); Sun et al. (2017); Lee et al. (2019); Redko et al. (2019)) to MUDA. The latent source and target features are represented via the output space of a neural encoder. Domain alignment implies a shared embedding space for these representations. To achieve this, a suitable distributional distance metric is chosen between these two sets of embeddings and minimized. In this work, we used the Sliced Wasserstein Distance (SWD) (Rabin et al. (2011); Bonneel et al. (2015)) for this purpose. SWD is a metric for approximating the optimal transport metric (Redko et al. (2019)). It is a suitable choice for UDA because: i) It possesses non-vanishing gradients for two high-dimensional distributions with non-overlapping supports through exploiting the geometry of the embedding space. As a result, it is a suitable objective function for deep learning optimization which allows empirical minimization by using gradient-based techniques, e.g., stochastic gradient descent. ii) It can be computed efficiently based on a closed-form solution using only empirical samples, drawn from the two probability distributions.

3 Problem formulation

Let $\mathcal{S}_1, \mathcal{S}_2 \dots \mathcal{S}_n$ be the data distributions of n annotated source domains and $\mathcal{T}$ be the data distribution of an unannotated target domain. Assume the source and target domains share the same feature space $\mathbb{R}^{W \times H \times C}$, where W, H, C describe an image by width, height and number of channels respectively. We consider all domains having a common label-space $\mathcal{Y}$, but not necessarily sharing the same label distribution. For each source domain k, we observe the labeled samples $\{(\boldsymbol{x}^s_{k,1}, \boldsymbol{y}_{k,1}), \dots, (\boldsymbol{x}^s_{k,n^s_k}, \boldsymbol{y}_{k,n^s_k})\}$, where $\boldsymbol{x}^s_k \sim \mathcal{S}_k$. We only observe unlabeled samples $\{\boldsymbol{x}^t_1, \dots, \boldsymbol{x}^t_{n^t}\}$ from the target domain $\mathcal{T}$. The goal is to train a model $f_\theta : \mathbb{R}^{W \times H \times C} \to \mathbb{R}^{|\mathcal{Y}|}$ capable of inferring target labels, where $|\mathcal{Y}|$ is the number of inference classes. The first step in our approach is to independently train decision models for each source domain via empirical risk

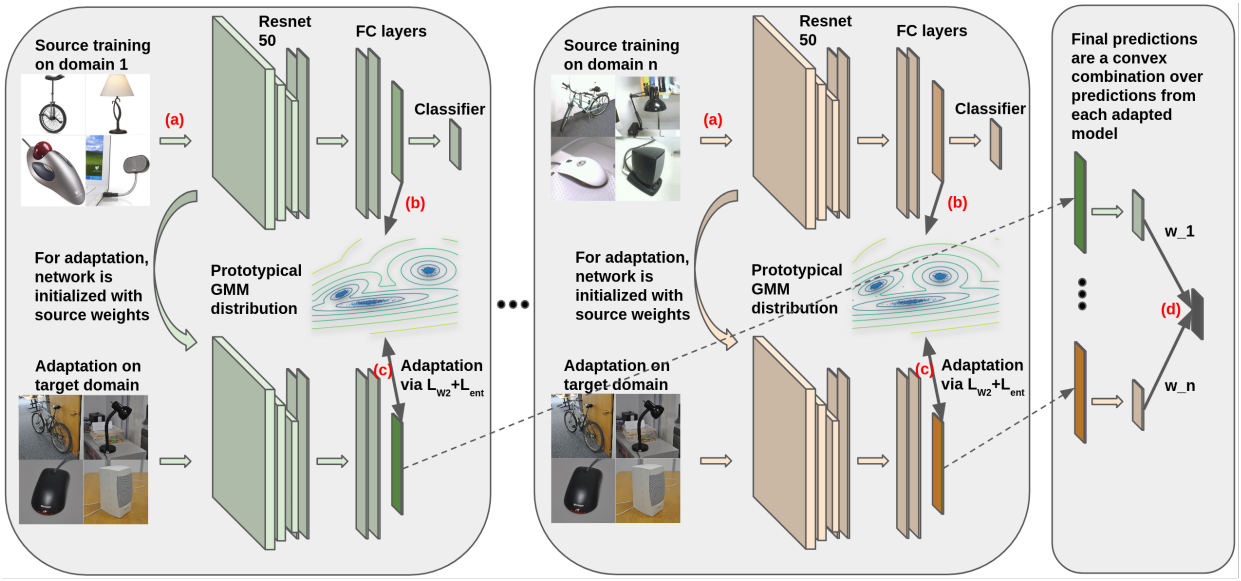

Figure 1: Block-diagram of our proposed approach: (a) source specific model training is done independently for each source domain (b) the distribution of latent embeddings of each source domain is estimated via a mixture of Gaussians, (c) for each source trained model, adaptation is performed by minimizing the distributional discrepancy between the learnt GMM distribution and the target encodings (d) the final target domain predictions are obtained via a learnt convex combinations of logits for each adapted model

minimization (ERM). We thus minimize the cross-entropy loss for the labeled source datasets:

$$\theta_k = \arg\min_{\theta} \frac{1}{n_k^s} \sum_{i=1}^{n_k^s} \mathcal{L}_{ce}(f_\theta(\boldsymbol{x}_{k,i}^s), \boldsymbol{y}_{k,i}) \tag{1}$$

Since under our considered setting the target and source domains share a common input and label space, these models can be directly used on the target to derive a naive solution. However, given the distributional discrepancy between source domains and target, e.g., real world images versus clip art, generalization performance will be poor. The goal of our MUDA approach is to benefit from the unannotated target dataset and the source-trained models in order to improve upon model generalization while avoiding negative transfer.

To this end, we decompose the model f_θ into a feature extractor $g_{\boldsymbol{u}}(\cdot) : \mathbb{R}^{W \times H \times C} \to \mathbb{R}^{dz}$ and a classifier subnetwork $h_{\boldsymbol{v}}(\cdot) : \mathbb{R}^{dz} \to \mathbb{R}^{|\mathcal{Y}|}$ with learnable parameters $\boldsymbol{u}$ and $\boldsymbol{v}$, such that $f(\cdot) = (h \circ g)(\cdot)$. We assume input data points are images of size $W \times H \times C$ and the latent embedding shape is of size d_Z. In a SUDA setting, we can improve generalization of each source-specific model on the target domain by aligning the distributions of the source and the target domain in the latent embedding space. Specifically, we can minimize a distributional discrepancy metric $D(\cdot, \cdot)$ across both domains, e.g., SWD loss, to update the learnable parameters: $\boldsymbol{u}_k^A = \arg\min_{\boldsymbol{u}} D(g_{\boldsymbol{u}}(\mathcal{S}_k), g_{\boldsymbol{u}}(\mathcal{T}))$. By aligning the distributions the source trained classifier h_k will generalize well on the target domain $\mathcal{T}$. In the MUDA setting, the goal is improving upon SUDA by benefiting from the collective knowledge of the source domains to make predictions on the target. This can be done via a weighted average of predictions made by each of the domain-specific models, i.e., models with learnable parameters $\theta_k^A = (\boldsymbol{u}_k^A, \boldsymbol{v}_k)$. For a sample $\boldsymbol{x}_i^t$ in the target domain, the model prediction will be $\sum_{k=1}^{n} w_k f_{\theta_k^A}(X_i^t)$, where w_k denotes a set of learnable weights associated with the source domains.

We note the above general approach requires simultaneous access to source and target data during adaptation. We relax this constraint and consider the more challenging setting of source-free adaptation, where we lose access to the source domains once source training finishes. To account for applications with sensitive data, e.g. medical domains, we also forbid interaction between source models during adaptation. Hence, the source distributions S_k and their representations in the embedding space, i.e., $g(\mathcal{S}_k)$, will become inaccessible. To circumvent this challenge, we rely on intermediate distributional estimates of the source latent embeddings.

4 Proposed algorithm

Our proposed approach for MUDA with private data is visualized in Figure 1. We base our algorithm on two levels of hierarchies. First, we adapt each source-trained model while preserving privacy (left and middle subfigures). We then combine predictions of the source-specific models on the target domain according to their reliability (right subfigure). To tackle the challenge of data privacy, we approximate the distributions of the source domains in the embedding space as a multi-modal distribution and use these distributional estimates for domain alignment (Figure 1, left). We can benefit from these estimates because once source training is completed, the input embedding distribution should be mapped into a $|\mathcal{Y}|-$modal distribution to enable the classifier subnetwork to separate the classes. Note, each separated distributional mode encodes one of the classes (see Figure 1, left). To approximate these internal distributions we employ Gaussian Mixture Models (GMM), with learnable mean and covariance parameters μ_k, Σ_k. Since we have access to labeled source data points, we can learn μ_k and Σ_k in a supervised fashion. Let $\mathbb{1}_c(x)$ denotes the indicator function for $x = c$, then the maximum likelihood estimates for the GMM parameters would be:

$$\mu_{k,c} = \frac{\sum_{i=1}^{n_k^s} \mathbb{1}_c(\boldsymbol{y}_{k,i}) g_{\boldsymbol{u}_k}(\boldsymbol{x}_{k,i}^s)}{\sum_{i=1}^{n_k^s} \mathbb{1}_c(\boldsymbol{y}_{k,i})}, \quad \Sigma_{k,c} = \frac{\sum_{i=1}^{n_k^s} \mathbb{1}_c(\boldsymbol{y}_{k,i})(g_{\boldsymbol{u}_k}(\boldsymbol{x}_{k,i}^s) - \mu_{k,c})(g_{\boldsymbol{u}_k}(\boldsymbol{x}_{k,i}^s) - \mu_{k,c})^T}{\sum_{i=1}^{n_k^s} \mathbb{1}_c(\boldsymbol{y}_{k,i})} \tag{2}$$

Learning μ_k and Σ_k for each domain k enables us to sample class conditionally from the GMM distributional estimates and approximate the distribution $g(\mathcal{S}_k)$ in the absence of the source dataset.

We adapt the source-trained model by aligning the target distribution $\mathcal{T}$ and the GMM distribution in the embedding space. To preserve privacy, for each source domain k we generate intermediate pseudo-domains A_k with pseudo-samples $\{\boldsymbol{z}_{k,1}^a, \ldots, \boldsymbol{z}_{k,n_k^a}^a\}$ by drawing random samples from the estimated GMM distribution. The pseudo-domain is used as an approximation of the corresponding source embeddings. To align the two distribution, a suitable distance metric $D(\cdot,\cdot)$ needs to be used. We rely on the SWD due to its mentioned appealing properties. The SWD acts as an estimate for the Wasserstein Distance (WD) between two distributions (Rabin et al. (2011)), by aggregating the tractable $1-$dimensional WD over L projections onto the unit hypersphere. In the context of our algorithm, the SWD discrepancy measure becomes:

$$D(g(\mathcal{T}), A_k) = \frac{1}{L} \sum_{l=1}^{L} |\langle g(x_{i_l}^t), \phi_l \rangle - \langle z_{k,j_l}^a, \phi_l \rangle|^2 \tag{3}$$

where ϕ_l is a projection direction, and i_l, j_l are indices corresponding to the sorted projections. While the source and target domains share the same label space $\mathcal{Y}$ they do not necessarily share the same distribution of labels. Since the prior probabilities on classes are not known in the target domain, minimizing the SWD at the batch level may lead to incorrectly clustering samples from different classes together, depending on the discrepancy between the label distributions. To address this challenge, we take advantage of the conditional entropy loss (Grandvalet & Bengio (2004)) as a regularization term based on information maximization. The conditional entropy acts as a soft clustering objective that ensures aligning target samples to the wrong class via SWD will be penalized. We follow the approximation presented in Eq. 6 in Grandvalet & Bengio (2004):

$$\mathcal{L}_{ent}(f_\theta(\mathcal{T})) = \frac{1}{n^t} \sum_{i=1}^{n^t} \mathcal{L}_{ce}(f_\theta(x_i^t), f_\theta(x_i^t)) \tag{4}$$

To guarantee this added loss term influences the latent representations produced by the feature extractor, the classifier is frozen during model adaptation. Our final combined adaptation loss is descrbied as:

$$D(g(\mathcal{T}), A) + \gamma \mathcal{L}_{ent}(f_\theta(\mathcal{T})) \tag{5}$$

for a regularizer γ. Once the source-specific adaptation is completed across all domains, the final model predictions on the target domain are obtained by combining probabilistic predictions returned by each of the n domain-specific models. The mixing weights are chosen as a convex vector $\boldsymbol{w} = (w_1 \dots w_n)$, i.e., $w_i > 0$ and $\sum_i w_i = 1$, with final predictions taking the form $\sum_{i=1}^{k} w_i f_{\theta_i}$. The choice of w is critical, as assigning large weights to a model which does not generalize well will harm inference power. We utilize the source model *prediction confidence* on the target domain as a proxy for generalization performance. We have provided empirical evidence for this choice in Section 6. We thus set a confidence threshold λ and assign w_k:

$$\tilde{w}_k \sim \sum_{i=1}^{n^t} \mathbb{1}(f_{\theta_k}(\boldsymbol{x}_i^t) > \lambda), \quad w_k = \tilde{w}_k / \sum \tilde{w}_k \tag{6}$$

Note the only cross-domain information transfer in our framework is communicating the latent means and covariance matrices of the estimated GMMs plus the domain-specific model weights which provide a warm start for adaptation. Data samples are never shared between any two domains during pretraining and adaptation. As a result, our approach preserves data privacy for scenarios at which the source datasets are distributed across several entities. Additionally, the adaptation process for each source domain is performed independently. As a result, our approach can be used to incorporate new source domains as they become available over time without requiring end-to-end retraining from scratch. We will only require to update the normalized mixing weights via Equation 6, which takes negligible runtime compared to model training. Our proposed privacy preserving approach, named Secure MUDA (SMUDA), is presented in Algorithm 1 .

Algorithm 1 Secure Multi-source Unsupervised Domain Adaptation (SMUDA)

procedure SMUDA($\mathcal{S}_1 \dots \mathcal{S}_n, \mathcal{T}, L, \gamma$)
  for $k \leftarrow 1$ to n **do**
    $\mu_k, \Sigma_k, \theta_k = Train(\mathcal{S}_k)$
    Generate A_k based on μ_k, Σ_k
    Compute w_k (Eq. 6)
    $\theta_k^A = Adapt(\theta_k, A_k, \mathcal{T}, L, \gamma)$
  return $w_1 \dots w_n, \theta_1^A \dots \theta_n^A$
procedure TRAIN($\mathcal{S}_i$)
  Learn $\theta_k = (u_k, v_k)$ by min. $\mathcal{L}_{CE}(f_{\theta_k}(\mathcal{S}_k), \cdot)$ (Eq. 1)
  Learn parameters μ_k, Σ_k (Eq. 2)
  return $\mu_k, \Sigma_k, \theta_k$
procedure ADAPT($\theta_k, A_k, \mathcal{T}, L, \gamma$)
  Initialize network with weights θ_k
  $\theta_k^A = \arg\min_\theta D(g_u(\mathcal{T}), A_k) + \gamma \mathcal{L}_{ent}(f_\theta(\mathcal{T}))$ (Eq. 5)
  return θ_k^A

5 Theoretical analysis

We provide an analysis to demonstrate that our algorithm minimizes an upper bound for the target domain error. We adopt the framework developed by Redko & Sebban (2017) for *single source UDA using Wasserstein distance* to provide a theoretical justification for the algorithm we proposed. Our analysis is performed in the latent embedding space. Let $\mathcal{H}$ represent the hypothesis space of all classifier subnetworks. Let $h_k(\cdot)$ denote the model learnt by each domain-specific model. We also set $e_{\mathcal{D}}(\cdot)$, where $\mathcal{D} \in \{\mathcal{S}_1 \dots \mathcal{S}_n, \mathcal{T}\}$, to be the true expected error returned by some model $h(\cdot) \in \mathcal{H}$ in the hypothesis space on the domain $\mathcal{D}$. Additionally, let $\hat{\mu}_{\mathcal{S}_k} = \frac{1}{n_k^s} \sum_{i=1}^{n_k^s} f(g(\boldsymbol{x}_{k,i}^s))$, $\hat{\mu}_{\mathcal{P}_k} = \frac{1}{n_k^a} \sum_{i=1}^{n_k^a} \boldsymbol{x}_{k,i}^a$, and $\hat{\mu}_{\mathcal{T}} = \frac{1}{n^t} \sum_{i=1}^{n_k^s} f(g(\boldsymbol{x}_i^t))$ denote the empirical distributions that are built using the samples for the source domain, the intermediate pseudo-domain, and the target domain in the latent space. Then the following theorem holds for the MUDA setting:

Theorem 1. *Consider Algorithm 1 for MUDA under the explained conditions, then the following holds*

$$e_{\mathcal{T}}(h) \leq \sum_{k=1}^{n} w_k(e_{\mathcal{S}_k}(h_k) + D(\hat{\mu}_{\mathcal{T}}, \hat{\mu}_{\mathcal{P}_k}) + D(\hat{\mu}_{\mathcal{P}_k}, \hat{\mu}_{\mathcal{S}_k}) + \sqrt{\left(2\log(\frac{1}{\xi})/\zeta\right)}\left(\sqrt{\frac{1}{N_k}} + \sqrt{\frac{1}{M}}\right) + e_{\mathcal{C}_k}(h_k^*)) \quad (7)$$

where $\mathcal{C}_k$ is the combined error loss with respect to domain k, and h_k^* is the optimal model with respect to this loss when a shared model is trained jointly on annotated datasets from all domains simultaneously.

Proof: the complete proof is included in the Appendix.

We see the target domain error is upperbounded by the convex combination of the domain-specific adaptation errors. Algorithm 1 minimizes the right-hand side of Equation 7 as follows: for each source domain, our method minimizes the source expected error by training the models on each domain using ERM. The second term is minimized because the distance between the distributions of the intermediate pseudo-domain and the target domain is directly minimized in the latent space. The third term corresponds to how well the GMM distribution approximates the latent source samples. Our algorithm does not minimize this term, however if the model performs well on the source domain and a multi-modal distribution is formed in the embedding space, necessary for good performance, this term will be small. The second to last term is dependent on the number of available samples in the adaptation problem, and becomes negligible when sufficient number of samples are accessible. The final term measures the difficulty of the optimization, and is dependent only on the structure of the data. For related domains, this term will also be negligible.

6 Experimental validation

Datasets We validate our algorithm on five domain adaptation benchmark datasets: *Office-31*, *Office-Home*, *Office-Caltech*, *Image-Clef* and *DomainNet*.

Office-31 (Saenko et al. (2010)) is a dataset consisting of 4110 images from an office environment pertaining to three domains: Amazon, Webcam and DSLR. Domains differ in image quality, background, number of samples and class distributions. Images in all three domains are categorized under 31 different categories. **Office-Caltech** (Gong et al. (2012)) contains 2533 office related images from four domains: Amazon, Webcam, DSLR, Caltech, falling under 10 categories. **Office-Home** (Venkateswara et al. (2017)) contains 30475 from four different domains: Art (stylized images), Clipart (clip art sketches), Product (images with no background) and Real-World (realistic images). Each domain contains images from 65 shared classes. Compared to the other *Office* datasets, *Office-home* presents a larger number of samples, domains and categories, making it more difficult for adaptation. **Image-Clef** (Long et al. (2017a)) contains 1800 images under 12 generic categories sourced from three domains: Caltech, Imagenet and Pascal. **DomainNet** (Peng et al. (2019a)) is a larger, more recent dataset containing 586,575 images from 345 general classes, with different class distributions for each of its six domains: Quickdraw, Clipart, Painting, Infograph, Sketch, Real. Given the size and scope of this dataset, it is arguably the most difficult for the MUDA task.

Preprocessing & Network structure: we follow the literature for fair comparison. For each domain we re-scale images to a standard size of $(224, 224, 3)$. We use a ResNet50 (He et al. (2016)) network as a backbone for the feature extractor, followed by four fully connected layers. The network classification head consists of a linear layer, and source-training is performed using cross-entropy loss. The ResNet layers of the feature extractor are frozen during adaptation. We report classification accuracy, averaged across five runs. Our code is provided as part of the supplementary material, and was run on a NVIDIA Titan Xp GPU.

To test the effectiveness of our privacy preserving approach for MUDA, we compare our method against state-of-the art SUDA and MUDA approaches. Benchmarks for single best (SB), source combined (SC) and multi source (MS) performance are reported based on DAN (Long et al. (2015)), D-CORAL (Sun & Saenko (2016)), RevGrad (Ganin & Lempitsky (2015)). We include most existing MUDA algorithms: DCTN (Xu et al. (2018)), FADA (Peng et al. (2019b)), MFSAN (Zhu et al. (2019)), MDDA (Zhao et al. (2020)), SimpAl (Venkat et al. (2020b)), JAN (Long et al. (2017b)), MEDA (Wang et al. (2018)), MCD (Saito et al. (2018)), M3SDA (Peng et al. (2019a)), MDAN (Zhao et al. (2018)), MDMN (Li et al. (2018)), DARN (Wen et al. (2020a)), DECISION (Ahmed et al. (2021)). Note that we maintain full domain privacy throughout training

and adaptation. Hence, most of the above works should be considered as **upperbounds** in performance, as they address a more relaxed problem, by allowing joint and persistent access to source data. While Ahmed et al. (2021) also performs source-free adaptation, they benefit from jointly accessing the source trained models during adaptation, while our method only assumes joint access when pooling predictions. Despite this additional constraint, results prove our algorithm is competitive and at times outperforming the aforementioned methods. We next present quantitative and qualitative analysis of our work.

6.1 Performance Results

Main numerical results are presented in Table 1. In the case of **Office-31**, we observe state-of-the-art performance (SOTA) on the $\rightarrow D, \rightarrow A$ tasks and near SOTA performance on the remaining task. Note that the domains *DSLR* and *Webcam* share similar distributions, as exemplified through the Source-Only results, and for these domains obtaining a good adaptation performance involves minimizing negative transfer, which our method successfully achieves. In the case of **Image-clef**, we obtain SOTA performance on all tasks, even though the methods we compare against are not source-free. On the **Office-caltech** dataset, we obtain SOTA performance on the $\rightarrow A$ task, with close to SOTA performance on the three other tasks. The domains of the **Office-home** dataset have larger domain gaps with more classes compared to the three previous datasets. Our approach obtains near SOTA performance on the $\rightarrow P$ and $\rightarrow R$ tasks and competitive performance on the remaining tasks. Finally, the **DomainNet** dataset contains a much larger number of classes and variation in class distributions compared to the other datasets, making it the most challenging considered task in our experiments. Even so, we are able to obtain SOTA performance on three of the six tasks with competitive results on the other three. We reiterate most other MUDA algorithms serve as upper-bounds to our work, as they either access source data directly, simultaneously use models from all sources for adaptation, or both. Results across all tasks demonstrate that not only are we able to compare favorably against these methods while preserving data privacy, but we also set new SOTA on several tasks.

	Method	→D	→W	→A	Avg.
SB	Source Only	99.3	96.7	62.5	86.2
	DAN	99.7	98.0	65.3	87.7
	D-CORAL	99.7	98.0	65.3	87.7
	RevGrad	99.1	96.9	66.2	87.5
SC	DAN	99.6	97.8	67.6	88.3
	D-CORAL	99.3	98.0	67.1	88.1
	RevGrad	99.7	98.1	67.6	88.5
MS	MDDA	99.2	97.1	56.2	84.2
	DCTN	99.3	98.2	64.2	87.2
	MFSAN	99.5	98.5	72.7	90.2
	SImpAl	99.2	97.4	70.6	89.0
	DECISION*	99.6	**98.4**	**75.4**	91.1
	SMUDA (ours)*+	**99.8**	98.2	**75.4**	91.3

(a) Office-31

	Method	→P	→C	→I	Avg.
SB	Source Only	74.8	91.5	83.9	83.4
	DAN	75.0	93.3	86.2	84.8
	D-CORAL	76.9	93.6	88.5	86.3
	RevGrad	75.0	96.2	87.0	86.1
SC	DAN	77.6	93.3	92.2	87.7
	D-CORAL	77.1	93.6	91.7	87.5
	RevGrad	77.9	93.7	91.8	87.8
MS	DCTN	75.0	95.7	90.3	87.0
	MFSAN	79.1	95.4	93.6	89.4
	SImpAl	77.5	93.3	91.0	87.3
	SMUDA (ours)*+	**79.4**	**96.9**	**93.9**	90.1

(b) Image-clef

	Method	→W	→D	→C	→ A	Avg.
SB	Source Only	99.0	98.3	87.8	86.1	92.8
	DAN	99.3	98.2	89.7	94.8	95.5
	JAN	99.4	99.4	91.2	91.8	95.5
MS	DAN	99.5	99.1	89.2	91.6	94.8
	DCTN	99.4	99.0	90.2	91.6	94.8
	MEDA	99.3	99.2	91.4	92.9	95.7
	MCD	99.5	99.1	91.5	92.1	95.6
	M^3SDA	99.4	99.2	91.5	94.1	96.1
	SImpAl	99.3	99.8	92.2	95.3	96.7
	FADA*+	88.1	87.1	88.7	84.2	87.1
	DECISION*	**99.6**	**100**	**95.9**	**95.9**	98.0
	SMUDA (ours)*+	99.3	97.6	93.9	**95.9**	96.6

(c) Office-caltech

	Method	→A	→C	→P	→ R	Avg.
SB	Source Only	65.3	49.6	79.7	75.4	67.5
	DAN	68.2	56.5	80.3	75.9	70.2
	D-CORAL	67.0	53.6	80.3	76.3	69.3
	RevGrad	67.9	55.9	80.4	75.8	70.0
SC	DAN	68.5	59.4	79.0	82.5	72.4
	D-CORAL	68.1	58.6	79.5	82.7	72.2
	RevGrad	68.4	59.1	79.5	82.7	72.4
MS	MFSAN	72.1	62.0	80.3	81.8	74.1
	M^3SDA	64.1	62.8	76.2	78.6	70.4
	SImpAl	70.8	56.3	80.2	81.5	72.2
	MDAN	68.1	67.0	81.0	82.8	74.8
	MDMN	68.7	67.6	81.4	83.3	75.3
	DARN	70.0	68.4	82.8	83.9	76.26
	DECISION*	**74.5**	59.4	**84.4**	**83.6**	75.5
	SMUDA (ours)*+	69.1	**61.5**	83.5	83.4	74.4

(d) Office-home

	Method	→ Q	→ C	→ P	→ I	→ S	→ R	Avg.
SB	Source Only	11.8	39.6	33.9	8.2	23.1	41.6	26.4
	DAN	16.2	39.1	33.3	11.4	29.7	42.1	28.6
	JAN	14.3	35.3	32.5	9.1	25.7	43.1	26.7
	ADDA	14.9	39.5	29.1	14.5	30.7	41.9	28.4
	MCD	3.8	42.6	42.6	19.6	33.8	50.5	32.2
SC	Source Only	13.3	47.6	38.1	13.0	33.7	51.9	32.9
	DAN	15.3	45.4	36.2	12.8	34.0	48.6	32.1
	JAN	12.1	40.9	35.4	11.1	32.3	45.8	29.6
	ADDA	14.7	47.5	36.7	11.4	33.5	49.1	32.2
	MCD	7.6	54.3	45.7	22.1	43.5	58.4	38.5
MS	DCTN	7.2	48.6	48.8	23.5	47.3	53.5	38.2
	M^3SDA-β	6.3	58.6	52.3	26.0	49.5	62.7	42.6
	FADA*+	7.9	45.3	38.9	16.3	26.8	46.7	30.3
	DECISION*	**18.9**	61.5	**54.6**	21.6	**51**	67.5	45.9
	SMUDA (ours)*+	14.6	**62.4**	53.6	**24.4**	49.9	**68.3**	45.5

(e) DomainNet

Table 1: Results on five benchmark datasets. Single best (SB) represents the best performance with respect to any source, source combined (SC) represents performance obtained by pooling the source data together from different domains, and multi source (MS) represents methods performing multi source adaptation. * indicates source free adaptation, guaranteeing privacy between sources and the target. + indicates privacy between source models. Results in bold correspond to the highest accuracy amongst the source free approaches.

6.2 Ablative Studies

We perform ablative experiments by investigating the effect of each of the two loss terms on performance in our combined loss in Eq. 5. These are presented in Table 2. We observe that except for the *Office-caltech* dataset, combining the two terms yields improved performance for the rest of the datasets. Note however, the effect in the *Office-caltech* dataset is negligible. On the other hand, we see minimizing the SWD loss plays a more dominant role in performance improvements on the *Image-clef* and *Office-home* datasets. In contrast, the conditional entropy contributes more on the *Office-caltech* dataset and some tasks for *Office-31*. Our insight is that the conditional entropy term performs better when the source trained models have higher performance on the target domain prior to the source-level adaptation (e.g., $\rightarrow D, \rightarrow W$ on *Office-31*), while the SWD term is more vital when there is a larger discrepancy between the source domains and the target domain (e.g., $\rightarrow A$ on *Office-31*). Experiments conclude using both terms further improves performance.

Method	**→D**	**→W**	**→A**	**Avg.**
SWD only	92.2	94.1	73.1	86.4
$\mathcal{L}_{ent}$ only	99.8	98.1	66.2	88.1
SMUDA	99.8	97.3	75.7	91.3

(a) Office-31

Method	**→W**	**→D**	**→C**	**→ A**	**Avg.**
SWD only	98.1	97.8	92.1	95.5	95.9
$\mathcal{L}_{ent}$ only	99.4	97.7	94	96	96.8
SMUDA	99.3	97.6	93.9	95.9	96.6

(b) Office-caltech

Method	**→P**	**→C**	**→I**	**Avg.**
SWD only	79.3	96.5	94.2	90
$\mathcal{L}_{ent}$ only	78.5	96	91.7	88.7
SMUDA	79.4	96.9	93.9	90.1

(c) Image-clef

Method	**→A**	**→C**	**→P**	**→ R**	**Avg.**
SWD only	66.6	59.1	80.9	82.2	72.2
$\mathcal{L}_{ent}$ only	64.5	49.4	77.8	72.2	66
SMUDA	69.1	61.5	83.5	83.4	74.4

(d) Office-home

Table 2: Comparison of only using the SWD objective, only using the entropy objective or both (SMUDA). Using both terms of the loss function (Eq. 5) leads to best performance.

6.3 Empirical Analysis

In our empirical analysis we study the effect of hyperparameters on the performance of our method to provide a better understanding of the algorithm.

Dataset	**High confidence**	**W2**	**Uniform**	**Single Best**
office-31	91.3	88.6	85.1	91.3
image-clef	90.1	89.6	89.8	89.6
office-caltech	96.6	96.6	96.6	97
office-home	74.4	74.2	74.2	72.8
total avg.	**88.1**	87.2	86.4	87.6

Table 3: Analytic experiments to study four strategies for combining the individual model predictions. Mixing based on model reliability proves superior to other popular approaches.

We first validate empirically our choice for computing the mixing parameters w_k. We consider four mixing scenarios for combining the models' prediction: (i) Eq. 6, (ii) setting weights proportional to Sliced Wasserstein Distance between the intermediate and the target domains (a cross-domain measure of distributional similarity), (iii) using a uniform average, and (iv) assigning all mixing weight to the model with best target performance. Average performance for tasks of four of the datasets are reported in Table 3. We observe that our choice leads to maximum performance. We note the single best performance is able to slightly outperform our method on one of the tasks, however suffers on datasets where domains have significant pairwise domain gap. This observation is expected, as using several domains is beneficial when they complement each other in terms of available information. Assigning weights proportional to $D(g(\mathcal{T}), A_k)$ may seem a reasonable choice, given that similarity between the pseudo-datasets and the target latent features indicates better classifier generalization. However, this method performs better only compared to uniform averaging.

We conclude model reliability is a superior criterion of combining predictions. Uniform averaging leads to decreased generalization on the target domain as it treats all domains equally. As a result, models with the least generalization ability on the target domain harm collective performance.

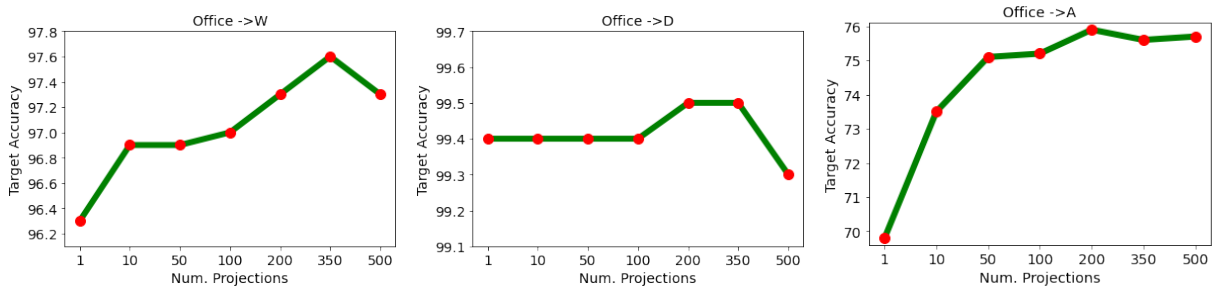

Figure 2: Performance for different numbers of latent projections used in the SWD on Office-31.

We additionally study the effect of the SWD projection hyper-parameter. SWD utilizes L random projections, as detailed in Equation 3. While a large L leads to a tighter approximation of the optimal transport metric, it also incurs a computational resource penalty. We investigate whether there is a range of L values offering sufficient adaptation performance, and analyze the impact of this parameter using the *Office-31* dataset. In Figure 2 we reported performance results for $L \in \{1, 10, 50, 100, 200, 350, 500\}$. The SWD approximation becomes tighter with an increased number of projections, which we see translating on all three tasks. We also note that above a certain threshold, i.e. $L \approx 200$, the gains in performance from increasing L are minimal.

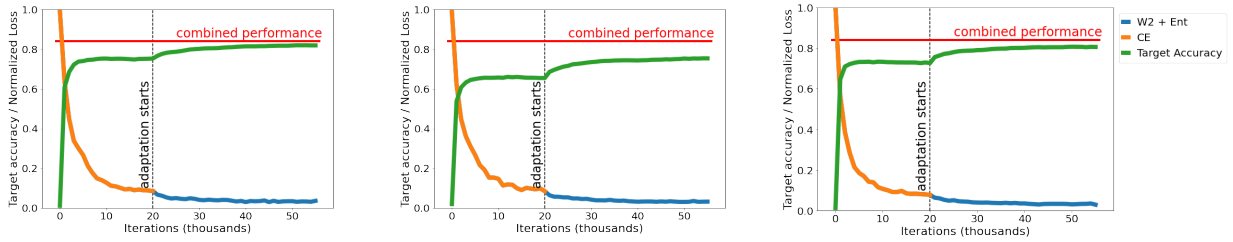

Figure 3: Effect of the adaptation process on the *Office-home* dataset: from left to right, we consider *Art, Clipart* and *Product* as the source domains, and *Real World* as the target domain.

In Figure 3 we explore the behavior of our adaptation strategy with respect to a *Office-home* task. For each of the three source domains, we observe an increase in target accuracy once adaptation starts, which is in line with our previous results. Note this increase in target accuracy also correlates with the minimization of the SWD and entropy losses. We additionally note that the combined multi-source performance using all three source domains outperforms the three SUDA performances. The biggest difference is observed for the *Clipart* trained model, which exhibits the highest discrepancy from the target domain *Real World*.

The confidence threshold λ controls the assignment of mixing weights w_k. For each source domain, the number of target samples with confidence greater than λ is recorded, and these normalized values produce w_k. In order to determine whether a certain value of λ leads to a satisfactory choice of mixing weights, it is important to determine whether the high confidence samples are indeed correctly predicted. Figure 4 provides the prediction accuracy on target domain samples on the *Office-home* dataset for different confidence ranges. We consider 5 different confidence probability ranges: $[0-20, 20-40, 40-60, 60-80, 80-100]$. We observe low-confidence predictions offer poor accuracy for the target domain. For example, in cases when the confidence is less than 0.2, prediction accuracy is below 40%. Conversely, for target samples with a predicted confidence greater than .6, we observe accuracy of more than 90% on all the three tasks of *Office-home*. This experiments supports our intuition that the amount of high confidence target samples can be used as a

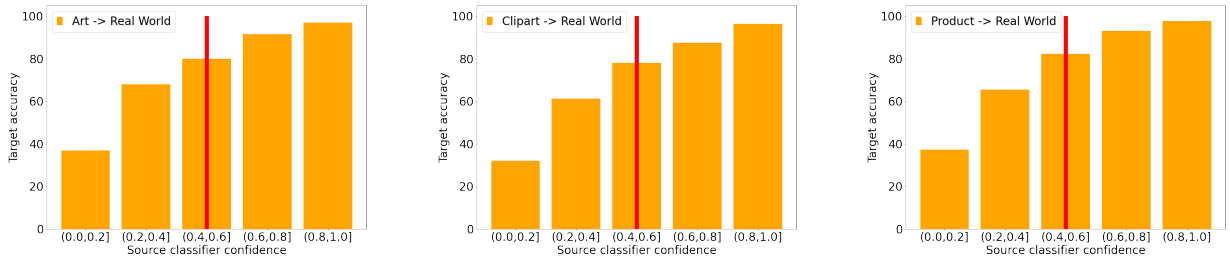

Figure 4: Prediction accuracy on *Office-home* target domain tasks under different levels of source model confidence, and our choice of λ. Target predictions above this threshold attain high accuracy.

proxy for the domain mixing weights w_k. We also note the amount of high confidence samples is calculated using the source only models, as adaptation artificially increase confidence across the whole dataset.

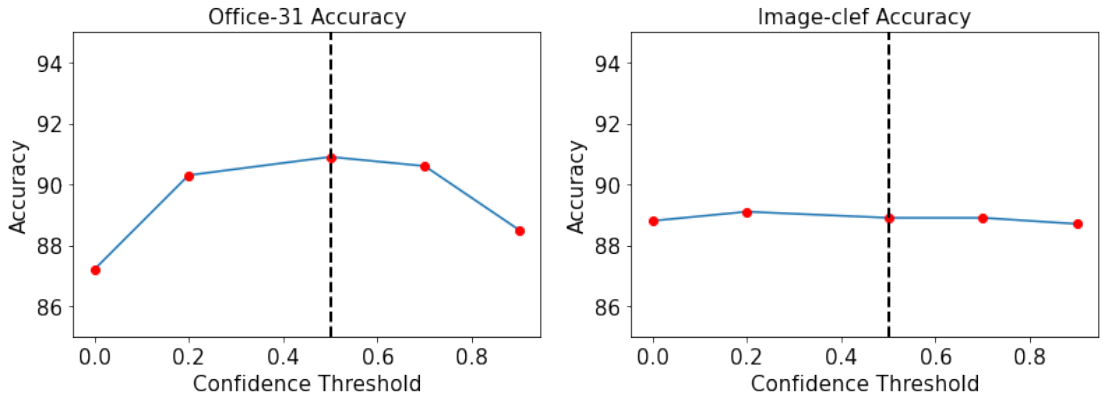

Figure 5: Results on the *Office-31* and *Image-clef* datasets for different values of the confidence parameter λ. The dotted line corresponds to $\lambda = .5$ used for reporting results in Table 1.

We further investigate performance with regard to the parameter λ. While in Figure 5 we observe a target accuracy increase correlated to higher levels of classifier confidence, the amount of high confidence samples proportional to dataset size is equally important for an appropriate choice of confidence threshold. Setting the λ parameter too high may lead to mixing weights that do not capture model behavior on the whole target distribution, just on a small subset of samples, leading to degraded performance. Conversely, a low value of λ will lead to results that are equivalent to uniformly combining predictions. Figure 5 portrays both these behaviors on the *Office-31* and *Image-clef* datasets. We observe our choice of $\lambda = .5$ is able to obtain best performance on the *Office-31* dataset, and close to best performance on the *Image-clef* dataset. We also note the choice of λ is relatively robust, as values in the interval $[.2, .7]$ offer similar performance.

Our adaptation approach attempts to minimize the distributional distance between target latent embeddings and the GMM samples approximating the source latent embeddings. We provide insight into this process in Figure 6. For the purpose of producing an intuitive visualization, we reduced the data representation dimension to two using the UMAP tool (McInnes et al. (2018)). We display the GMM samples, the target latent embeddings before adaptation, and target latent embeddings post-adaptation in Figure 6. We observe that for each different source domain, the adaptation process achieves to reduce the distance between the target domain embeddings (yellow points) and the Gaussian samples (red points). This observation also empirically validates the theoretical justification for our algorithm. Given the classification heads trained on the source domains are able to generalize well on the GMM samples as a result of pretraining, we conclude that source-specific domain alignment translates to an improved collective generalization performance.

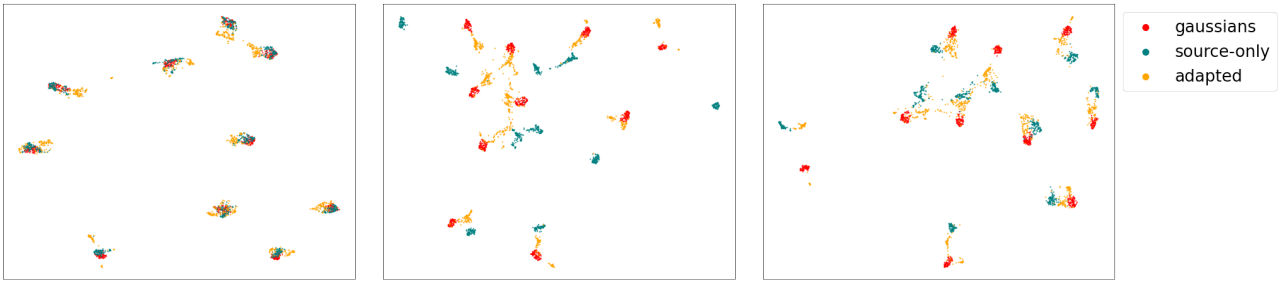

Figure 6: UMAP latent space visualization for *Office-caltech* with *Amazon* as the target. Sources in order: *Caltech, DSLR*, and *Webcam*. Adaptation shifts target embeddings towards the GMM distribution.

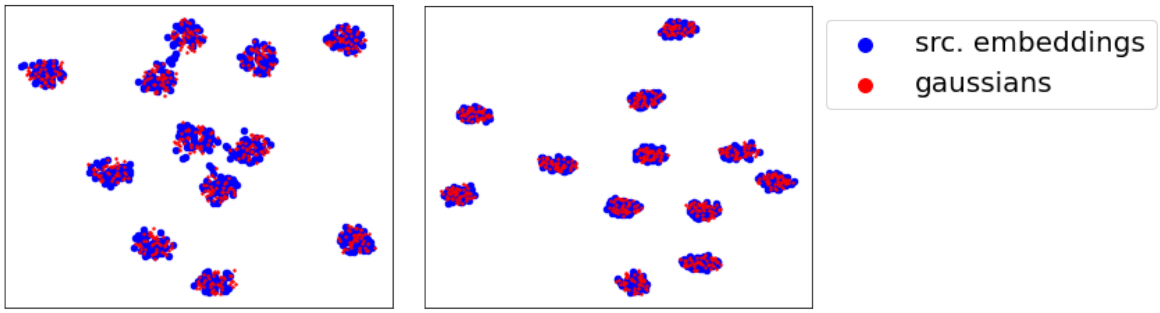

Figure 7: Source and GMM embeddings for the *Image-clef* dataset with *Pascal* and *Caltech* as sources. For both datasets, the GMM samples closely approximate the source embeddings.

Finally, we investigate the representation quality of the intermediate GMM distribution as a surrogate for the source data distribution. Note that a poor approximation of the source latent distribution will lead to decreased adaptation performance. Thus, having the GMMs offer a good approximation of the source latent features is key to our approach. In Figure 7, we present visualized data representations for the estimated GMMs and the source domain distributions for the *Image-clef* dataset. We note that for both source domains, their latent space distributions after pretraining are multi-modal distributions with 12 modes, each corresponding to one of the 12 classes. This observation confirms that we can approximate the source domain distribution with a GMM with 12 modes. We also note that for both source domains the estimated GMM distribution offers a close approximation of the original source distribution. This experiment empirically validates that the third term in Eq. 4, the distributional distance between the source and estimated GMMs, is small in practice and we can use these as intermediate cross-domain distributions.

7 Conclusion

We develop a novel privacy-preserving MUDA algorithm. Our approach is based on the assumption that an input distribution is mapped into a multi-modal distribution in an embedding space as a result of supervised learning. We achieve privacy between each source domain and the target domain by minimizing the SWD loss between an intermediate GMM distribution and the target domain distribution in the latent embedding space. We then combine the source-specific models according to their reliability. We provide theoretical analysis to justify our algorithm. Our experimental results demonstrate that our algorithm performs favorably against SOTA MUDA algorithms on four standard benchmark datasets while preserving privacy. Future direction includes considering setting where the target domain shares different classes with each of the source domains.

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