Exploring Forensic Dental Identification with Deep Learning

Abstract

Dental forensic identification targets to identify persons with dental traces. The task is vital for the investigation of criminal scenes and mass disasters because of the resistance of dental structures and the wide-existence of dental imaging. However, no widely accepted automated solution is available for this labour-costly task. In this work, we pioneer to study deep learning for dental forensic identification based on panoramic radiographs. We construct a comprehensive benchmark with various dental variations that can adequately reflect the difficulties of the task. By considering the task's unique challenges, we propose FoID, a deep learning method featured by: (*i*) clinical-inspired attention localization, (*ii*) domain-specific augmentations that enable instance discriminative learning, and (*iii*) transformer-based self-attention mechanism that dynamically reasons the relative importance of attentions. We show that FoID can outperform traditional approaches by at least **22.98%** in terms of Rank-1 accuracy, and outperform strong CNN baselines by at least **10.50%** in terms of mean Average Precision (mAP). Moreover, extensive ablation studies verify the effeteness of each building blocks of FoID. Our work can be a first step towards the automated system for forensic identification among large-scale multi-site databases. Also, the proposed techniques, *e.g.*, self-attention mechanism, can also be meaningful for other identification tasks, *e.g.*, pedestrian re-identification.

1 Introduction

Forensic identification targets to identify living or deceased persons by analyzing their trace evidences. The task is vital for the investigation of criminal scenes, accidents and mass disasters [31, 28] for at least two reasons: (*i*) dental patterns can be highly identifying while their traces are widely archived than other methodologies *e.g.,* DNA profiling [4, 46, 59]. For instance, around 1.4 billion dental X-rays were performed in 2019 in the U.S.[1]; (*ii*) dental structures are more resistant to damages than other body tissues including bones [7, 47]. In the current practice, forensic examinations are mostly done by the visual comparison of dental radiographs [47, 46] between a target entity (person) and those from databases. Due to the lack of widely accepted automated solutions, such examination cannot scale up to large databases, and its results are vulnerable to oversights and/or mistakes [19, 40]. This work pioneers to study deep learning for forensic identification with dental panoramic radiographs — one of the most common dental traces nowadays [59].

There have been a few attempts for forensic dental identification, most of which take the approaches of matching handcrafted feature [1, 78, 9]. According to our best knowledge, only one work utilizes off-the-shelf convolutional neural networks (CNNs) for learning discriminative representations of

---

[1]https://idataresearch.com/product/dental-imaging-market/

Figure 1: A challenging case of dental identification with two dental radiographs captured from a same person. The case exists large anatomical variations including tooth reduction (d), the addition of braces and implants (e1, e2), and the change of teeth alignment (f1, f2). In the forensic practice, teeth, condyle (a), angle of mandible (b), and maxillary sinus (c) are the key anatomies for dentists.

a dental radiograph for identification [40]. However, the work is preliminary since it is based on a *small-scale* dataset with both *temporal* and *heterogeneous* limitations — it is different from the applied situation where significant intra-entity variations in dental structures can exist because of external factors, *e.g.*, interventions, and internal factors, *e.g.*, decaying, over long scanning intervals [47, 1]. Moreover, no architecture exploration was made for this unique identification task.

We performed a formative study with two board-certified dentists, and outlined the distinct challenges of forensic dental identification: (*C1*) the lack of paired dental radiographs for metric learning; (*C2*) sparseness of identification information in high-resolution radiographs; and (*C3*) dental variations can be heterogeneous but useful as *inclusion* or *exclusion* criteria for identifying. To study the task, we construct a comprehensive benchmark: it involves 583 persons, and comes with a challenging testing set spanning over 21.0±11.5 months of scanning intervals, covering a wide range of dental variations including orthodontics, tooth loss, and implanting/filling. Moreover, we propose the first optimized deep learning **Fo**rensic **ID**entification solution, named **FoID**. In specific, to take the advantage of overwhelmingly unpaired radiographs (*C1*), we develop a set of domain-specific augmentations (DSA) for effective self-supervised metric learning. To focus on meaningful areas, FoID incorporates hard attention extraction and alignment guided by semantic segmentation and anatomical registration (*C2*). Moreover, FoID introduces a novel transformer-based self-attention mechanism, as inspired by dentist's practice, to dynamically reason the optimal aggregation of partial attentions for representation (*C3*). Overall, the main contributions of our work are three folds:

- We give the first in-depth study of deep learning for dental forensic identification. The formative study with dentists outlines the unique challenges and offers insights into solutions.
- We construct a comprehensive dental forensic benchmark, which covers a wide range of dental variations to reflect the realistic scenario of the task.
- We present the first deep learning solution FoID, which achieves an mAP of 59.62%, and largely outperforms the existing dental identification models and strong CNN baselines. Ablation studies show that the proposed DSA enables effective representation learning from unpaired data, boosting models by up to 12.33% in terms of mAP; Meanwhile, the proposed transformer-based self-attention outperforms state-of-the-art attention models by at least 4.82% in terms of mAP.

2 Formative Study

Challenge 1: paired scan instances are scarce With the high radiation of dental imaging, overwhelming cases from dental clinics contain only one scan instance per person. As such, it poses as a challenge for metric learning without positive instance pairs. To tackle it, we develop a set of domain-specific augmentations (DSA) by working with dentists to simulate potential dental anatomical variations. Different views of one entity are generated on the fly, which enables effective intra-/inter-reasoning in a self-supervised manner.

Challenge 2: identification information is sparse   Forensic dentists mostly focus on several key anatomies on panoramic imaging for identification, since others are either non-discriminative or not well approximated on radiographs. As such, models should focus on such regions for image embedding to avoid over-fitting. Accordingly, as shown in Figure 1, our method such incorporate domain knowledge by utilizing a hard attention mechanism on teeth, condyle (Figure 1(a)), angle of mandible (Figure 1(b)), and maxillary sinus (Figure 1(c)). A combination of semantic segmentation and registration is applied for efficient key-point localization.

Challenge 3: dental variations are heterogeneous but can be useful   There can exist both partial and global anatomical changes over two scanning. As demonstrated by a typical case in Figure 1, two scans of a same entity can see anatomy loss (Figure 1(d)), artifact implanting (Figure 1(e1, e2)), structural changes (Figure 1(f1, f2)). In the forensic practice, dentists commonly look through all key anatomies in a scan, determine most discriminative features among them according to experience, and then apply those as indexes for matching. Our method follows the philosophy by introducing a transformer-based self-attention module, which dynamically reasons the relative importance of attentions among a set of them for representation learning.

3   Related Works

Person identification with deep learning   Person identification tasks such as face recognition [56, 52, 44, 48, 8] and pedestrian re-identification [13, 51, 63, 60] have been widely studied by the computer vision community. Current solutions either optimize a discriminant distance metric that takes a pair of instances [69, 79, 61, 3] as input, or learn an identity-sensitive encoder that maps an input instance to representations [74, 51, 77, 57]. Our method follows the later approach for its efficiency of inference within large-scale galleries.

Attention mechanism has been widely explored for pedestrian re-identification to enforce models to focus on key body parts, such that representations are robust against background clutter, occlusion, and unconstrained human poses in surveillance images. For example, existing works [41, 11, 54, 62, 63, 34, 66, 49, 74] extract part-based features with either soft or hard attentions, guided by human pose estimations, and align/aggregate them for the final representation. Works [36, 53, 60] further propose to mine useful partial attentions from the end-to-end training. Our work follows the approach by introducing an attention mechanism, but differs in two ways. First, the key areas are partially localized with non-rigid image registration [5], which effectively reduces the cost of manual annotations. Second, more importantly, we propose a novel self-attention module to dynamically reason the relative importance of each attention for the final representation by learning from training cases. Such self-attention is inspired by the practice of experts, where unique features of dental structures is searched, and used as matching criteria.

Unsupervised person identification has also been recently discussed in pedestrian re-identification in order to train models with the widely available unlabeled surveillance videos. The current solutions can be categorized into clustering and fine-tuning [22, 75, 17, 20, 72], negative instance pair mining [70, 38], and image translation [6, 64, 77, 65]. However, the challenge of forensic dental identification is different from the above scenario: within a dental image database, each entity (person) has only one scan instance (scan), and the method should learn representations from such set of instances. As such, we take the instance discriminative approach [10, 45, 22], and generate different views of the same entity with the proposed domain-specific augmentations (DSA) for the contrastive intra-reasoning.

Transformer for image retrieval   Transformer has been recently applied to computer vision tasks [15, 71, 73]. Since our task is image retrieval in nature, we briefly review the related transformer works: Gkelios *et al.* [23] and El-Nouby *et al.* [16] directly replace CNNs with pure transformer models for image embedding; He *et al.* [26] further incorporates encoding of meta information, (*e.g.,* camera viewpoints), into the sequence of inputs; Yang *et al.* [67] utilizes query and gallery images as transformer's query and key inputs respectively for modeling spatial attention between them. Different from the above works, we propose to utilize a transformer for aggregating a set of model attentions: the self-attention characteristic of transformer enables the dynamic reasoning of attentions' importance for embedding by comparison, and its permutation-invariance [33] can relieve the attention misalignment caused by the imperfect key-point localization.

Figure 2: Overall architecture of FoID, the key components of which consist of attention localization and alignment, domain-specific augmentations, and feature aggregation with self-attention. The objective function includes three types of losses that are complementary for representation learning.

4 Methodologies

We present FoID by first describing its building components and then the multi-task learning strategy. As shown in Figure 2, FoID maps each scan instance into an embedding. Given a query instance, we calculate the similarities between the query and all the gallery instances in the embedding space and return the ranked retrieval list.

4.1 Attention Localization & Alignment

Inspired by the dentists' practice, FoID employs a hard attention mechanism to focus on (*i*) teeth and (*ii*) landmarks of condyle, angle of mandible, and maxillary sinus to avoid over-fit to unrelated regions. For teeth localization, FoID formulates it as semantic segmentation, and applies a mask-RCNN [24] pre-trained on the existing panoramic segmentation dataset of UFBA_UESC [30]. Given an input instance I, a teeth segmentation map $T^{H \times W \times 32}$ is estimated (Figure 2(a)), where H and W are instance height and width, and a channel size is 32 for the number of teeth categories of an adult. The raw mask-RCNN outputs are filtered for the largest connected mask with a minimal size threshold for each tooth to denoise. For landmark localization, since the landmarks are largely separated and establish no accurate boundary, FoID employs a registration-based method to efficiently detect them from an atlas, with one pair of radiograph and its manual annotation with $M{=}6$ landmarks manually created (Figure 2(b)). For each input instance, the atlas is aligned to the instance with Syn registration [5], with the annotation deformed accordingly for the landmark estimation (Figure 2(c)). Based on the teeth and landmark localization, the input is cropped to attention patches with a constant spatial dimension of $h \times w$, and then sequentially piled as the attention stack $S^{h \times w \times 38}$ for the representation representation. In the case of missing anatomies, zero-valued patches are correspondingly padded.

4.2 Contrastive Learning with DSA

In order to build useful representations from overwhelming unpaired instances, FoID adapts a self-supervised approach with the proposed domain-specific augmentations (DSA). In specific, a set of structure-aware and forensic-realistic augmentations is stochastically applied to an instance to generate different views, which are in turn used for intra-reasoning. In the practice, given a mini-batch of stacked attentions from N entities $B = \{S_n\}_{n=1}^N$, K times of DSA are repeatedly applied to B. Denote $S_n^{(i)}$ as the i-th sample from augmented view of S_n: an instance group $\{S_n^{(i)}, S_n^{(j)}\}$ is taken as positive pair, while $\{S_n^{(i)}, S_{\backslash n}^{(j)}\}$ is taken as a negative pair, where $\backslash n$ can be any index from $\{1, 2, ..., N\}\backslash\{n\}$. The learning strategy does not relay on any paired instances or identification annotation, but can be easily extended when such data is available by including different augmented inputs belonging to the same identification as positive pairs.

To achieve effective representation learning, augmentations that cover the potential anatomical variations as in clinics is the key. As showcased in Figure 2, the proposed DSA consists fours types of augmentations inspired by forensic observations, and is independently applied to each attention patch

on the fly. (*i*) Random tooth reduction that aims to simulate tooth loss caused by injury or inventions (*e.g.*, Figure 2(e)). (*ii*) Random artifact addition that adds patches of flexible shapes to crown (Figure 2(e,f)) or tooth regions (Figure 2(g,h)). Such augmentation aims to simulate the common artifacts of dental filling, implant, and brace. (*iii*) Random rigid patch transform within a range of angles and displacements. The augmentation not only enforces view comparison as in the standard instance discrimination learning [10, 45], but also simulates global teeth arrangement changes (*e.g.,* caused by orthodontics), since the transform is performed for patches independently. (*iv*) Random color disturbance of contrast shifting and gaussian noise within designed ranges for simulating different scanning setup and machine noises. More details about the implementation of DSA is reported in **Appendix I**.

4.3 Self-Attention for Feature Aggregation

To build the representation of an instance from its attention stack, FoID consists a CNN encoder f (Figure 2(i)) to embed each attention patch, followed by a transformer-based self-attention module (Figure 2(j)) for aggregating the attention embeddings. The encoder f targets to extract salient features for an input patch with the existence of possible anatomical variations, and it can be adapted from any convolutional encoders. The output attention embeddings from the CNN encoder can be denoted as $Z^{38 \times C}$, where C is the embedding length.

To aggregate the generated multiple embeddings of attentions, we propose to utilize a transformer to dynamically reason the importance of each attention among the set of them: dental structures that falls into the general distribution of populations should take less attentions, while the ones that are more identifying should take more attentions. More importantly, such importance of attentions should be relative based on the experience of forensic dentists: the more discriminating anatomies in an instance are more often selected as index for matching. This differs from the existing pedestrian re-identification works [11, 34, 74], where the attention to a body parts is modeled without conditioning on its comparison among all body parts. As shown in Figure 2, the sequence of attentions $Z^{38 \times C} = [z_1^C, z_2^C, ..., z_{38}^C]$ is first projected into a constant token dimension C' with a linear encoder α, and then is fed into a two-layer BERT encoders [58, 14] for unidirectional context learning. Note that *no* positional information [15] is injected to attention embeddings for two reasons: (*i*) we assume that the semantic category of anatomies sets no prior for reasoning the importance, (*ii*) teeth can be often mis-classified due to their similarity in patterns (see **Appendix II** for examples), which can in turn pose as noise when positions are modeled. The feature outputs from the last transformer layer are further encoded into a reduced dimension C'' as regularization with a non-linear encoder β, and then concatenated as the final embedding $Y = cat(y_1^{C''}, y_2^{C''}, ..., y_{38}^{C''})$ for the instance. Moreover, a learnable $[class]$ token $z_0^{C'}$ is prepended to the transformer's input sequence, the embedding of which at the output $y_0^{C'}$ serves as a complementary instance embedding for the purpose of multi-task learning.

4.4 Objective Function & Training

To learn discriminative representations, we adopt three complementary optimization tasks to train FoID: a contrastive loss, an identification loss, and a deep supervision loss.

Contrastive loss Given a pair of instance embeddings $\{Y_i, Y_j\}$, the contrastive loss $L_{contrast}$ is defined as: $L_{contrast} = \mathbb{1}_{l_i=l_j}[m_{pos} - S(Y_i, Y_j)]_+ + \mathbb{1}_{l_i \neq l_j}[S(Y_i, Y_j) - m_{neg}]_+$, where $[x]_+$ equals $max(x, 0)$, and l_i denotes the instance's id category of representation $\{Y_i\}$ among the training set; m_{pos} and m_{neg} are similarity margins for positive and negative pairs; $S(.,.)$ is the pre-defined similarity measure, and cosine distance is used in this work. Online mining is applied to train on challenging positive (views of one instance) and negative (views of different instances) pairs.

Identification loss An identification loss L_{id} is applied to all samples within a mini-batch for the prediction of ID category from the transformer's $[class]$ embedding output. In specific, $L_{id} = CE(softmax(r_{id}(y_0^{C'})), l)$, where CE denotes cross entropy loss; $y_0^{C'}$ and and l are the sample's transformer's $[class]$ output and id category label, respectively; r_{id} is a regressor that transfer the embedding dimension from c' to the total training id count. The identification loss and contrastive loss are applied on different embeddings and have a diverged objective, which can possibly serve as a strong regularization for the transformer.

Table 1: Demographic and dental variation information of the testing set. Scan interval is the average of largest time interval between any two radiographs of an entity. The numbers of entity presenting the dental variations and their proportions are shown.

Demographic			Dental Variations			
Age	Gender	Scan Interval	Orthodontics	Filling/Implant	Brace	Tooth Loss
10~55	F:23; M:17	21.0±11.5 mo.	25 (62.5%)	10 (25.0%)	16 (40.0%)	18 (45.0%)

Deep supervision loss   The CNN encoder f is expected to extract salient features that are discriminative for identification from a given attention patch. Since the target diverges from the contrastive loss and identification loss that directly optimize on the aggregated embeddings, we incorporates a deep supervision signal for f. In specific, we formulate the deep supervision loss L_{sup} as a cross entropy loss: $L_{sup} = CE(softmax(r_{sup}(cat(y_1^C, y_2^C, ..., y_{38}^C))), l)$, where r_{sup} is a regressor that maps the concatenation of a sample's attention embeddings to a vector, the dimension of which equals the total count of training instances.

The final objective function for training FoID is the unweighted sum of the three types of loss: $L = L_{contrastive} + L_{id} + L_{sup}$. During the training, the whole model can be optimized from end-to-end, while the transformer's non-class embeddings $cat(y_1^{C''}, y_2^{C''}, ..., y_{38}^{C''})$ is taken as the representation of an instance during the inference.

5   Benchmark Construction

Similar to the setup of existing image retrieval datasets [35, 76, 37], our benchmark consists of a training set and a testing set. The training set is derived from an existing DNS Panoramic dataset [50], which contains 543 panoramic radiographs and exist common dental variations of tooth reduction and artifact addition. Each of the radiographs is scanned from a separate identity, which resembles the practical situation of dental forensic where there is a lack of paired data for metric learning. The testing set is collected by us from [*anonymous sites*], which contains 87 panoramic radiographs scanned with 40 identities, among which 33 identities hold 2 radiographs and 7 identities hold 3 radiographs. For covering comprehensive dental variations to make it sufficient for reflecting the difficulty of dental forensic, the testing set are selected from both endodontics and orthodontics departments. The method is distinct from previous dental forensic studies that either construct testing cases without controlling data variety [18, 1, 27], or consider only a specific dental variation over a short scanning interval (*i.e.*, single tooth extraction over 64.0 days [40]). Table 1 describes the profile of the testing set, and Figure 1 shows one typical case. All the data has been anonymized. To evaluate a model, we apply an *one*-against-*all* strategy for the efficient use of data. In specific, one instance from the testing set is used as the query, while the union of training set and the rest of testing set is used as the gallery set. The average results among all testing instances is reported as the final accuracy measurement.

6   Experimental Results

6.1   Implementation Details

We adopt two mostly used CNN architectures in re-identification works, ResNet-34 [25] and Inception-ResNet [55], for the CNN encoder f. Both models drop the final fully connected layer, and are initialized by pre-training on the ImageNet [12] and the face recognition dataset LFW by following [48], respectively. The output embedding of both encoders has a 512 channels per input attention patch. By following [15], the single layer linear encoder α maps an attention embedding to 128 channels; The transformer holds a hidden embedding dimension of 128 and a multi-attention head number of 4; Meanwhile, the final encoder β consists a fully connected layer and batch normalization, mapping the transform's outputs to 13 channels per attention patch, and thus leading to a dimension of 494 for the final instance embedding. The deep supervision regressor and [*class*] embedding regressor are both implemented with two fully connected layers, the output feature dimensions of which are 256 and the total count of training instances respectively. Batch normalization and ReLU activation are applied in both regressors.

Table 2: Comparison to the existing dental forensic identification approaches and strong CNN baselines. AHI [27] is not designed to rank all gallery instances, and thus mAP cannot be measured.

Methods	Backbone	mAP	Rank-1	Rank-5	Rank-10
AHI [27]	-	-	0.2759	0.4483	0.5287
HIDPR [43]	-	0.3018	0.2759	0.4138	0.4713
classification	ResNet-34	0.4912	0.4253	0.6437	0.7356
contrastive	ResNet-34	0.4072	0.3218	0.5977	0.6322
triplet	ResNet-34	0.4723	0.4253	0.6092	0.6667
reconstruction	ResNet-34	0.3537	0.3333	0.4943	0.6092
classification	Inception-ResNet	0.3638	0.2644	0.5287	0.5862
contrastive	Inception-ResNet	0.3854	0.3448	0.4943	0.6092
triplet	Inception-ResNet	0.3609	0.2989	0.5172	0.6437
reconstruction	Inception-ResNet	0.2912	0.2299	0.5172	0.5862
FoID (ours)	ResNet-34	0.5465	0.4817	0.6897	0.7471
FoID (ours)	Inception-ResNet	**0.5962**	**0.5057**	**0.7586**	**0.7816**

Regarding data pre-processing, all the radiography instances are normalized to a pixel spacing of $0.11mm \times 0.11mm$, and are normalized to a same color space with histogram matching. The attention patch dimensions h and w are set as the minimal embodying size for all anatomies, which are $28.16mm$ and $21.56mm$ respectively. Unless otherwise specified, the batch size is set to 6 and the augmentation repeat is set to 5 per instance for all the training. Unless otherwise specified, Adam optimizer is employed with an initial learning rate of $1e$-4, and is reduced to a half every 30 epochs. All the methods are trained for 100 epochs. For the online hard pair mining, the positive and negative similarity margins are set to 0.6 and 0.4 respectively. All experiments are conducted on servers with three GeForce GTX 1080 Ti GPUs. Cosine similarity is applied to rank the retrievals given a query instance. Rank-k retrieval accuracy ($k \in \{1, 5, 10\}$) and mean average precision (mAP) are used as evaluation metrics.

6.2 Comparison to Existing Approaches

We compare our method to both: (*i*) key-point matching based on handcrafted descriptors, and (*ii*) strong CNN baselines. For the key-point matching, it is the most studied approach for forensic dental identification. Two recent methods of AHI [27] and HIDPR [43] are included in comparison, which are based on the matching of Speeded Up Robust Features and tooth-aware appearance and positional similarity, respectively. Both methods have achieved satisfying identification accuracies with panoramic radiographs based on their own in-house datasets. For the CNN approach, few study has investigated it possibly due to the challenge of learning from the overwhelming unpaired data. For fair comparison, we enable the proposed domain-specific augmentations for all the training, and include four most commonly used representation learning methods as the strong baselines, the objective functions of which are id classification loss [56, 77], contrastive loss [52, 57, 13], triplet loss [44, 48, 51], and reconstruction loss [32]. As reported in a recent comparison study on pedestrian re-identification [42], the above baselines can already achieve accuracy comparable to the state-of-the-arts. Note that all the CNN baselines take a whole radiograph as input without attention mechanism, and apply the same backbone architectures of ResNet-34 and Inception-ResNet as FoID. According to Table 2, our method significantly outperforms all the existing approaches, achieving up to 59.62% in terms of mAP and 50.57% in terms of rank-1 accuracy. Compared to the key-point matching approach, the improvement shows that the proposed augmentation strategy enables effective representation learning from unpaired data. Compared to CNN baselines, our method surpass by incorporating domain knowledge with attentions — the accuracy boost of at least 10.50% in terms of mAP indicates that the localized attention regions are valid for identification, and can obviously reduce the over-fitting to the non-related areas. Visualizations of FoID's retrievals with examples queries can be found in **Appendix III**.

6.3 Ablation Studies

Self-attention with transformer   FoID incorporates a novel transformer-based self-attention mechanism to reason the relative importance of attentions for the feature aggregating. In order to verify its effectiveness, we first compare with the state-of-the-art attention mechanisms introduced in pedestrian re-identification: PartReID [74], PGFA [41], and Mancs [60]. To adapt those methods to our task, the original human body attention localization is replaced by the dental one as beforehand described in

Table 3: Ablation studies of our proposed self-attention by comparing with the state-of-the-art attention-based identification methods and common aggregation mechanisms.

Methods	Backbone	mAP	Rank-1	Rank-5	Rank-10
PDC [74]	-	0.4556	0.4253	0.5632	0.6322
PGFA [41]	-	0.4982	0.4598	0.5862	0.6092
Mancs [60]	-	0.4723	0.4368	0.5747	0.6092
Avg Pool.	ResNet-34	0.3707	0.3103	0.5057	0.5977
Max Pool.	ResNet-34	0.2519	0.2069	0.3793	0.4253
FC	ResNet-34	0.4000	0.2989	0.5517	0.6667
Att	ResNet-34	0.4085	0.3563	0.5172	0.5632
Gated Att	ResNet-34	0.4268	0.4023	0.4828	0.5060
FoID (ours)	ResNet-34	**0.5465**	**0.4817**	**0.6897**	**0.7471**
Avg Pool.	Inception-ResNet	0.3824	0.2989	0.5517	0.6092
Max Pool.	Inception-ResNet	0.2654	0.1954	0.3793	0.5172
FC	Inception-ResNet	0.3007	0.2414	0.4138	0.5172
Att	Inception-ResNet	0.3527	0.2989	0.5172	0.5517
Gated Att	Inception-ResNet	0.3741	0.3103	0.5287	0.6322
FoID (ours)	Inception-ResNet	**0.5962**	**0.5057**	**0.7586**	**0.7816**

Table 4: Ablation studies of the objective function. Our proposed function combining three complementary types of losses leads to the overall highest accuracy as indicated by mAP.

#	$L_{contrast}$	L_{id}	L_{sup}	mAP	Rank-1	Rank-5	Rank-10
		ResNet-34 as backbone					
1	✓			0.4760	0.4253	0.6303	0.6811
2		✓		0.3196	0.2874	0.4598	0.5434
3	✓	✓		0.5394	0.4598	0.6782	0.7356
4	✓	✓	✓	**0.5465**	**0.4817**	**0.6897**	**0.7471**
		Inception-ResNet as backbone					
5	✓			0.4438	0.3793	0.5747	0.6092
6		✓		0.2808	0.1609	0.4828	0.5517
7	✓	✓		0.5394	0.4368	0.7356	**0.8046**
8	✓	✓	✓	**0.5962**	**0.5057**	**0.7586**	0.7816

Figure 3: Visualization of the dynamic self-attentions captured by the transformer for four typical instances. Attention rollout is performed to infer the attentions on input patches. View in color and zooming in for the best quality. More attention visualizations can be found in **Appendix III**.

subsection 4.1. For fair comparison, the same DSA and training strategy as FoID are applied. Table 3 shows that FoID can outperform all the methods, exceeding by up to 9.80% and 8.04% in terms of mAP and rank-1 accuracy respectively. Different from the observation in [60, 74], FoID outperforms Mancs and ParrReID by applying hard attentions over soft attentions, possibly due to the accurate definition of key anatomies informed from the formative study, and the improved training efficiency with patches cropped out of large unrelated regions. More importantly, the results also indicate that modeling inter-attention can potentially lead to better aggregation results. To verify, we ablate the effect of self-attention by replacing the transformer with the existing aggregation modules of average pooling (Avg Pool.) [], max pooling (Max Pool.) [], fully connected layers (FC) [], weighted attention (Att) [29], and gated attention (Gated att) [68, 29], meanwhile fixing all other setups. As Table 2 confirms, by consistently achieving the highest accuracy according to all metrics on both backbone CNNs, reasoning the relative importance of various attentions is important for representation learning, and the proposed transformer approach can fulfill the goal. More details on PartReID, PGFA, Mancs, and the adaptations we performed can be found in **Appendix IV**.

Self-attention visualization We further look into the self-attention reasoning by visualizing raw images and their corresponding self-attention weight maps. In specific, we roll out the attention weights of the transformer encoder layers to capture the propagation of information from input tokens to the final representation [2]. In FoID, each input token is the embedding of a cropped attention patch encoded by the upstream CNN encoder. Figure 3 demonstrates the visualization results of four typical cases. We can obviously see that, in each case, FoID can localize certain identifying anatomies with higher attentions than the others. Such pattern is clear to include tooth with a unique shape (Figure 3(a1)), wise tooth (Figure 3(a2, b3)), tooth with a distinct artifact (Figure 3(c4,d5)), and condyle of uncommon structure (Figure 3(d6)). The phenomenon proves that our method can dynamically compare between the captured attentions, and highlight discriminative ones to boost recognition performance. Moreover, it also shows that the approach has a chance to improve the model explainability, which can be vital when dentists are making final forensic decisions based on deep learning predictions. Nonetheless, we should note that such attention reasoning results is learnt based on our specific training dataset, which can be limited in both size and variety when compared to a real clinical database. As such, more robust attention reasoning can possibly be learnt when the method is applied to large scale databases, and accordingly a higher identification accuracy can also

possibly be achieved. More visualization results for both success and failure cases of FoID as well as the detailed analysis can be found in **Appendix III**.

Domain-specific augmentations We introduce the DSA to generate forensic-realistic views of an instance for the effective instance discriminative learning. To verify the effeteness of DSA compared to basic augmentations, we perform the ablation study based on both FoID and the CNN baselines. We define a set of basic augmentations (BA) by following existing self-supervised contrastive approaches [45, 10], which include random displacements, rotations, and gaussian noises. Details about BA can be found in **Appendix I**. Figure 4 shows that DSA consistently outperforms BA, achieving mAP improvements ranging from 3.28% to 15.32%.

Figure 4: Ablation studies on the proposed domain-specific augmentations for the model training. Various methods are included in comparison. A set of basic augmentations is used as the baseline.

Objective function design Three types of losses are included in FoID to complement for the representation learning. In order to understand the effect of each loss type, an ablation study is performed based on both CNN encoders of ResNet-34 and Inception-ResNet. Table 4 indicates that contrastive loss and id classification losses alone can have inferior performance, while the combining of the two leads to largely improved accuracy in terms of mAP (ResNet-34 as backbone: 0.4760/0.3196→0.5394; Inception-ResNet as backbone: 0.4438/0.2808→0.5394). Such phenomenon has been observed by several previous studies on pedestrian re-identification, but the accuracy boosts in our work seem to be more significant (*e.g.*, 0.817→0.859 and 0.706→0.764 as in [39]). This can possibly due to that two losses in FoID optimize two less correlated tasks, which makes it more effective for regularizing the transformer. Besides, plugging in the deep supervision signal for the CNN encoder can further increase the accuracy (ResNet-34 as backbone: 0.5394→0.5465; Inception-ResNet as backbone: 0.5394→0.5962), possibly by the improved back-propagation and the direct regularization of the CNN encoder.

7 Discussion and Conclusion

Dental forensic identification has always been an important part of criminal/disaster investigation, but is challenging and labour-consuming by relying on expert's visual comparison. Our work is the first in-depth study on automating the task with deep learning, and its inspiring result can possibly lead to future systems that can work with large-scale multi-site databases. No potential societal impact of the work has been seen, and the task is less privacy-sensitive than other identification tasks (*e.g.*, pedestrian re-identification from RGB photos), since medical scans are under the protection of licensed institutions.

Limitations There exist two known gaps between our proposed method and the clinical practice of forensic dentists. First, forensic dentists can take advantages of ***multi-modality*** scans, *e.g.,* by matching certain structures between bitewing and panoramic radiographs. Second, dentists can also utilize ***medical records as priors*** for imaging matching. For example, if a medical record indicates an entity was receiving dental fillings, a shape difference at certain location can thus be expected between the preoperative scan in the database and a query scan. As such, how to design deep learning methods to overcome the two gaps is open to explore.

Broad impact FoID can be meaningful for the general forensic with medical scans, *e.g.*, cranium imaging [21]. All those tasks can share similar challenges, *i.e.,* the lack of paired data, sparseness of identifying information, and selecting proper indexing anatomies. Moreover, we propose a novel transformer-based self-attention module for aggregating various attentions. Our experiment shows that the module can outperform the existing aggregating methods by automatically learning the importance of attentions. Such method is also promising for the pedestrian re-identification task, where different attentions (body key-points) can be assigned with different weights for representation based on the relative importance of body parts under certain circumstances (*e.g.,* occlusions).

References

[1] Mohamed Abdel-Mottaleb, Omaima Nomir, Diaa Eldin Nassar, Gamal Fahmy, and Hany H Ammar. Challenges of developing an automated dental identification system. In *2003 46th Midwest Symposium on Circuits and Systems*, volume 1, pages 411–414. IEEE, 2003.

[2] Samira Abnar and Willem Zuidema. Quantifying attention flow in transformers. *arXiv preprint arXiv:2005.00928*, 2020.

[3] Ejaz Ahmed, Michael Jones, and Tim K Marks. An improved deep learning architecture for person re-identification. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 3908–3916, 2015.

[4] Javier Ata-Ali and Fadi Ata-Ali. Forensic dentistry in human identification: A review of the literature. *Journal of clinical and experimental dentistry*, 6(2):e162, 2014.

[5] Brian B Avants, Charles L Epstein, Murray Grossman, and James C Gee. Symmetric diffeomorphic image registration with cross-correlation: evaluating automated labeling of elderly and neurodegenerative brain. *Medical image analysis*, 12(1):26–41, 2008.

[6] Slawomir Bak, Peter Carr, and Jean-Francois Lalonde. Domain adaptation through synthesis for unsupervised person re-identification. In *Proceedings of the European Conference on Computer Vision (ECCV)*, pages 189–205, 2018.

[7] Juliana Baranova, Dominik Büchner, Werner Götz, Margit Schulze, and Edda Tobiasch. Tooth formation: Are the hardest tissues of human body hard to regenerate? *International Journal of Molecular Sciences*, 21(11):4031, 2020.

[8] Qiong Cao, Li Shen, Weidi Xie, Omkar M Parkhi, and Andrew Zisserman. Vggface2: A dataset for recognising faces across pose and age. In *2018 13th IEEE international conference on automatic face & gesture recognition (FG 2018)*, pages 67–74. IEEE, 2018.

[9] Hong Chen and Anil K Jain. Dental biometrics: Alignment and matching of dental radiographs. *IEEE transactions on pattern analysis and machine intelligence*, 27(8):1319–1326, 2005.

[10] Ting Chen, Simon Kornblith, Mohammad Norouzi, and Geoffrey Hinton. A simple framework for contrastive learning of visual representations. In *International conference on machine learning*, pages 1597–1607. PMLR, 2020.

[11] De Cheng, Yihong Gong, Sanping Zhou, Jinjun Wang, and Nanning Zheng. Person re-identification by multi-channel parts-based cnn with improved triplet loss function. In *Proceedings of the iEEE conference on computer vision and pattern recognition*, pages 1335–1344, 2016.

[12] Jia Deng, Wei Dong, Richard Socher, Li-Jia Li, Kai Li, and Li Fei-Fei. Imagenet: A large-scale hierarchical image database. In *2009 IEEE conference on computer vision and pattern recognition*, pages 248–255. Ieee, 2009.

[13] Weijian Deng, Liang Zheng, Qixiang Ye, Guoliang Kang, Yi Yang, and Jianbin Jiao. Image-image domain adaptation with preserved self-similarity and domain-dissimilarity for person re-identification. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 994–1003, 2018.

[14] Jacob Devlin, Ming-Wei Chang, Kenton Lee, and Kristina Toutanova. Bert: Pre-training of deep bidirectional transformers for language understanding. *arXiv preprint arXiv:1810.04805*, 2018.

[15] Alexey Dosovitskiy, Lucas Beyer, Alexander Kolesnikov, Dirk Weissenborn, Xiaohua Zhai, Thomas Unterthiner, Mostafa Dehghani, Matthias Minderer, Georg Heigold, Sylvain Gelly, et al. An image is worth 16x16 words: Transformers for image recognition at scale. *arXiv preprint arXiv:2010.11929*, 2020.

[16] Alaaeldin El-Nouby, Natalia Neverova, Ivan Laptev, and Hervé Jégou. Training vision transformers for image retrieval. *arXiv preprint arXiv:2102.05644*, 2021.

[17] Hehe Fan, Liang Zheng, Chenggang Yan, and Yi Yang. Unsupervised person re-identification: Clustering and fine-tuning. *ACM Transactions on Multimedia Computing, Communications, and Applications (TOMM)*, 14(4):1–18, 2018.

[18] Diane J Flint, Stephen Brent Dove, Paula C Brumit, Marea White, and David R Senn. Computer-aided dental identification: an objective method for assessment of radiographic image similarity. *Journal of forensic sciences*, 54(1):177–184, 2009.

[19] Alexander S Forrest. Collection and recording of radiological information for forensic purposes. *Australian dental journal*, 57:24–32, 2012.

[20] Yang Fu, Yunchao Wei, Guanshuo Wang, Yuqian Zhou, Honghui Shi, and Thomas S Huang. Self-similarity grouping: A simple unsupervised cross domain adaptation approach for person re-identification. In *Proceedings of the IEEE/CVF International Conference on Computer Vision*, pages 6112–6121, 2019.

[21] Heather M Garvin and Michala K Stock. The utility of advanced imaging in forensic anthropology. *Academic forensic pathology*, 6(3):499–516, 2016.

[22] Yixiao Ge, Feng Zhu, Dapeng Chen, Rui Zhao, and Hongsheng Li. Self-paced contrastive learning with hybrid memory for domain adaptive object re-id. *arXiv preprint arXiv:2006.02713*, 2020.

[23] Socratis Gkelios, Yiannis Boutalis, and Savvas A Chatzichristofis. Investigating the vision transformer model for image retrieval tasks. *arXiv preprint arXiv:2101.03771*, 2021.

[24] Kaiming He, Georgia Gkioxari, Piotr Dollár, and Ross Girshick. Mask r-cnn. In *Proceedings of the IEEE international conference on computer vision*, pages 2961–2969, 2017.

[25] Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 770–778, 2016.

[26] Shuting He, Hao Luo, Pichao Wang, Fan Wang, Hao Li, and Wei Jiang. Transreid: Transformer-based object re-identification. *arXiv preprint arXiv:2102.04378*, 2021.

[27] Andreas Heinrich, Felix V Güttler, Sebastian Schenkl, Rebecca Wagner, and Ulf K-M Teich-gräber. Automatic human identification based on dental x-ray radiographs using computer vision. *Scientific reports*, 10(1):1–13, 2020.

[28] Anastasia Holobinko. Forensic human identification in the united states and canada: A review of the law, admissible techniques, and the legal implications of their application in forensic cases. *Forensic Science International*, 222(1-3):394–e1, 2012.

[29] Maximilian Ilse, Jakub Tomczak, and Max Welling. Attention-based deep multiple instance learning. In *International conference on machine learning*, pages 2127–2136. PMLR, 2018.

[30] Gil Jader, Jefferson Fontineli, Marco Ruiz, Kalyf Abdalla, Matheus Pithon, and Luciano Oliveira. Deep instance segmentation of teeth in panoramic x-ray images. In *Conference on Graphics, Patterns and Images (SIBGRAPI)*, pages 400–407. IEEE, 2018.

[31] T Kahana and J Hiss. Identification of human remains: forensic radiology. *Journal of clinical forensic medicine*, 4(1):7–15, 1997.

[32] Daisuke Komura, Keisuke Fukuta, Ken Tominaga, Akihiro Kawabe, Hirotomo Koda, Ryohei Suzuki, Hiroki Konishi, Toshikazu Umezaki, Tatsuya Harada, and Shumpei Ishikawa. Luigi: Large-scale histopathological image retrieval system using deep texture representations. *biorxiv*, page 345785, 2018.

[33] Juho Lee, Yoonho Lee, Jungtaek Kim, Adam Kosiorek, Seungjin Choi, and Yee Whye Teh. Set transformer: A framework for attention-based permutation-invariant neural networks. In *International Conference on Machine Learning*, pages 3744–3753. PMLR, 2019.

[34] Dangwei Li, Xiaotang Chen, Zhang Zhang, and Kaiqi Huang. Learning deep context-aware features over body and latent parts for person re-identification. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 384–393, 2017.

[35] Wei Li, Rui Zhao, Tong Xiao, and Xiaogang Wang. Deepreid: Deep filter pairing neural network for person re-identification. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 152–159, 2014.

[36] Hao Liu, Jiashi Feng, Meibin Qi, Jianguo Jiang, and Shuicheng Yan. End-to-end comparative attention networks for person re-identification. *IEEE Transactions on Image Processing*, 26(7):3492–3506, 2017.

[37] Hongye Liu, Yonghong Tian, Yaowei Yang, Lu Pang, and Tiejun Huang. Deep relative distance learning: Tell the difference between similar vehicles. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 2167–2175, 2016.

[38] Zimo Liu, Dong Wang, and Huchuan Lu. Stepwise metric promotion for unsupervised video person re-identification. In *Proceedings of the IEEE international conference on computer vision*, pages 2429–2438, 2017.

[39] Hao Luo, Youzhi Gu, Xingyu Liao, Shenqi Lai, and Wei Jiang. Bag of tricks and a strong baseline for deep person re-identification. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition Workshops*, pages 0–0, 2019.

[40] Shinpei Matsuda, Takashi Miyamoto, Hitoshi Yoshimura, and Tatsuhito Hasegawa. Personal identification with orthopantomography using simple convolutional neural networks: a preliminary study. *Scientific reports*, 10(1):1–7, 2020.

[41] Jiaxu Miao, Yu Wu, Ping Liu, Yuhang Ding, and Yi Yang. Pose-guided feature alignment for occluded person re-identification. In *Proceedings of the IEEE/CVF International Conference on Computer Vision*, pages 542–551, 2019.

[42] Kevin Musgrave, Serge Belongie, and Ser-Nam Lim. A metric learning reality check. In *European Conference on Computer Vision*, pages 681–699. Springer, 2020.

[43] Ayse Betul Oktay. Human identification with dental panoramic radiographic images. *IET Biometrics*, 7(4):349–355, 2018.

[44] Omkar M Parkhi, Andrea Vedaldi, and Andrew Zisserman. Deep face recognition. 2015.

[45] Massimiliano Patacchiola and Amos Storkey. Self-supervised relational reasoning for representation learning. In *Advances in Neural Information Processing Systems*, 2020.

[46] Jahagirdar B Pramod, Anand Marya, and Vidhii Sharma. Role of forensic odontologist in post mortem person identification. *Dental research journal*, 9(5):522, 2012.

[47] IA Pretty and D Sweet. A look at forensic dentistry–part 1: The role of teeth in the determination of human identity. *British dental journal*, 190(7):359–366, 2001.

[48] Florian Schroff, Dmitry Kalenichenko, and James Philbin. Facenet: A unified embedding for face recognition and clustering. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 815–823, 2015.

[49] Jianlou Si, Honggang Zhang, Chun-Guang Li, Jason Kuen, Xiangfei Kong, Alex C Kot, and Gang Wang. Dual attention matching network for context-aware feature sequence based person re-identification. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pages 5363–5372, 2018.

[50] Bernardo Silva, Laís Pinheiro, Luciano Oliveira, and Matheus Pithon. A study on tooth segmentation and numbering using end-to-end deep neural networks. In *Conference on Graphics, Patterns and Images (SIBGRAPI)*. IEEE, 2020.

[51] Chunfeng Song, Yan Huang, Wanli Ouyang, and Liang Wang. Mask-guided contrastive attention model for person re-identification. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pages 1179–1188, 2018.

[52] Yi Sun, Xiaogang Wang, and Xiaoou Tang. Deep learning face representation from predicting 10,000 classes. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 1891–1898, 2014.

[53] Yifan Sun, Qin Xu, Yali Li, Chi Zhang, Yikang Li, Shengjin Wang, and Jian Sun. Perceive where to focus: Learning visibility-aware part-level features for partial person re-identification. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 393–402, 2019.

[54] Yifan Sun, Liang Zheng, Yi Yang, Qi Tian, and Shengjin Wang. Beyond part models: Person retrieval with refined part pooling (and a strong convolutional baseline). In *Proceedings of the European conference on computer vision (ECCV)*, pages 480–496, 2018.

[55] Christian Szegedy, Sergey Ioffe, Vincent Vanhoucke, and Alexander Alemi. Inception-v4, inception-resnet and the impact of residual connections on learning. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 31, 2017.

[56] Yaniv Taigman, Ming Yang, Marc'Aurelio Ranzato, and Lior Wolf. Deepface: Closing the gap to human-level performance in face verification. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 1701–1708, 2014.

[57] Rahul Rama Varior, Bing Shuai, Jiwen Lu, Dong Xu, and Gang Wang. A siamese long short-term memory architecture for human re-identification. In *European conference on computer vision*, pages 135–153. Springer, 2016.

[58] Ashish Vaswani, Noam Shazeer, Niki Parmar, Jakob Uszkoreit, Llion Jones, Aidan N Gomez, Lukasz Kaiser, and Illia Polosukhin. Attention is all you need. *arXiv preprint arXiv:1706.03762*, 2017.

[59] Anoop K Verma, Sachil Kumar, Shiuli Rathore, and Abhishek Pandey. Role of dental expert in forensic odontology. *National journal of maxillofacial surgery*, 5(1):2, 2014.

[60] Cheng Wang, Qian Zhang, Chang Huang, Wenyu Liu, and Xinggang Wang. Mancs: A multi-task attentional network with curriculum sampling for person re-identification. In *Proceedings of the European Conference on Computer Vision (ECCV)*, pages 365–381, 2018.

[61] Faqiang Wang, Wangmeng Zuo, Liang Lin, David Zhang, and Lei Zhang. Joint learning of single-image and cross-image representations for person re-identification. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pages 1288–1296, 2016.

[62] Guan'an Wang, Shuo Yang, Huanyu Liu, Zhicheng Wang, Yang Yang, Shuliang Wang, Gang Yu, Erjin Zhou, and Jian Sun. High-order information matters: Learning relation and topology for occluded person re-identification. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 6449–6458, 2020.

[63] Guanshuo Wang, Yufeng Yuan, Xiong Chen, Jiwei Li, and Xi Zhou. Learning discriminative features with multiple granularities for person re-identification. In *Proceedings of the 26th ACM international conference on Multimedia*, pages 274–282, 2018.

[64] Yanan Wang, Shengcai Liao, and Ling Shao. Surpassing real-world source training data: Random 3d characters for generalizable person re-identification. In *Proceedings of the 28th ACM International Conference on Multimedia*, pages 3422–3430, 2020.

[65] Longhui Wei, Shiliang Zhang, Wen Gao, and Qi Tian. Person transfer gan to bridge domain gap for person re-identification. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 79–88, 2018.

[66] Longhui Wei, Shiliang Zhang, Hantao Yao, Wen Gao, and Qi Tian. Glad: Global-local-alignment descriptor for pedestrian retrieval. In *Proceedings of the 25th ACM international conference on Multimedia*, pages 420–428, 2017.

[67] Fuzhi Yang, Huan Yang, Jianlong Fu, Hongtao Lu, and Baining Guo. Learning texture transformer network for image super-resolution. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 5791–5800, 2020.

[68] Jiawen Yao, Xinliang Zhu, Jitendra Jonnagaddala, Nicholas Hawkins, and Junzhou Huang. Whole slide images based cancer survival prediction using attention guided deep multiple instance learning networks. *Medical Image Analysis*, 65:101789, 2020.

[69] Jinjie You, Ancong Wu, Xiang Li, and Wei-Shi Zheng. Top-push video-based person re-identification. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pages 1345–1353, 2016.

[70] Hong-Xing Yu, Wei-Shi Zheng, Ancong Wu, Xiaowei Guo, Shaogang Gong, and Jian-Huang Lai. Unsupervised person re-identification by soft multilabel learning. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 2148–2157, 2019.

[71] Li Yuan, Yunpeng Chen, Tao Wang, Weihao Yu, Yujun Shi, Francis EH Tay, Jiashi Feng, and Shuicheng Yan. Tokens-to-token vit: Training vision transformers from scratch on imagenet. *arXiv preprint arXiv:2101.11986*, 2021.

[72] Kaiwei Zeng, Munan Ning, Yaohua Wang, and Yang Guo. Hierarchical clustering with hard-batch triplet loss for person re-identification. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 13657–13665, 2020.

[73] Hengshuang Zhao, Jiaya Jia, and Vladlen Koltun. Exploring self-attention for image recognition. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 10076–10085, 2020.

[74] Liming Zhao, Xi Li, Yueting Zhuang, and Jingdong Wang. Deeply-learned part-aligned representations for person re-identification. In *Proceedings of the IEEE international conference on computer vision*, pages 3219–3228, 2017.

[75] Rui Zhao, Wanli Ouyang, and Xiaogang Wang. Unsupervised salience learning for person re-identification. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 3586–3593, 2013.

[76] Liang Zheng, Liyue Shen, Lu Tian, Shengjin Wang, Jingdong Wang, and Qi Tian. Scalable person re-identification: A benchmark. In *Proceedings of the IEEE international conference on computer vision*, pages 1116–1124, 2015.

[77] Zhedong Zheng, Liang Zheng, and Yi Yang. Unlabeled samples generated by gan improve the person re-identification baseline in vitro. In *Proceedings of the IEEE International Conference on Computer Vision*, pages 3754–3762, 2017.

[78] Jindan Zhou and Mohamed Abdel-Mottaleb. A content-based system for human identification based on bitewing dental x-ray images. *Pattern Recognition*, 38(11):2132–2142, 2005.

[79] Xiaoke Zhu, Xiao-Yuan Jing, Xinge You, Xinyu Zhang, and Taiping Zhang. Video-based person re-identification by simultaneously learning intra-video and inter-video distance metrics. *IEEE Transactions on Image Processing*, 27(11):5683–5695, 2018.