OCD: LEARNING TO OVERFIT WITH CONDITIONAL DIFFUSION MODELS

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ABSTRACT

We present a dynamic model in which the weights are conditioned on an input sample x and are learned to match those that would be obtained by finetuning a base model on x and its label y. This mapping between an input sample and network weights is shown to be approximated by a linear transformation of the sample distribution, which suggests that a denoising diffusion model can be suitable for this task. The diffusion model we therefore employ focuses on modifying a single layer of the base model and is conditioned on the input, activations, and output of this layer. Our experiments demonstrate the wide applicability of the method for image classification, 3D reconstruction, tabular data, and speech separation. Our code is attached as supplementary.

1 INTRODUCTION

> "Here is a simple local algorithm: For each testing pattern, (1) select the few training examples located in the vicinity of the testing pattern, (2) train a neural network with only these few examples, and (3) apply the resulting network to the testing pattern."
>
> Bottou & Vapnik (1992)

Thirty years after the local learning method in the epigraph was introduced, it can be modernized in a few ways. First, instead of training a neural network from scratch on a handful of samples, the method can finetune, with the same samples, a base model that is pretrained on the entire training set. The empirical success of transfer learning methods (Han et al., 2021) suggests that this would lead to an improvement.

Second, instead of retraining a neural network each time, we can learn to predict the weights of the locally-trained neural network for each input sample. This idea utilizes a dynamic, input-dependent architecture, also known as a hypernetwork (Ha et al., 2016).

Third, we can take the approach to an extreme and consider local regions that contain a single sample. During training, we finetune the base model for each training sample separately. In this process, which we call "overfitting", we train on each specific sample $s = (x, y)$ from the training set, starting with the weights of the base model and obtaining a model f_{θ_s}. We then learn a model g that maps between x (without the label) and the shift in the weights of f_{θ_s} from those of the base model. Given a test sample x, we apply the learned mapping g to it, obtain model weights, and apply the resulting model to x.

The overfitted models are expected to be similar to the base model, since the samples we overfit are part of the training set of the base model. We provide theoretical arguments that support that the mapping from the x part of s to f_{θ_s} can be approximated by a locally convex transformation. As a result, it is likely that a diffusion process that is able to generate samples in the domain of x would also work for generating the weights of the fine-tuned networks. Recently, diffusion models, such as DDPM (Ho et al., 2020) and DDIM (Song et al., 2020) were shown to be highly successful in generating perceptual samples (Dhariwal & Nichol, 2021b; Kong et al., 2021). We, therefore, employ a conditional diffusion model to model g.

In order to make the diffusion models suitable for predicting network weights, we make three adjustments. First, we automatically select a specific layer of the neural model and modify only this

layer. This considerably reduces the size of the generated data and, in our experience, is sufficient for supporting the overfitting effect. Second, we condition the diffusion process on the input of the selected layer, its activations, and its output. Third, since the diffusion process assumes unit variance scale (Ho et al., 2020), we separately learn the scale of the weight modification.

Our method is widely applicable, and we evaluate it across four very different domains: image classification, image synthesis, regression in tabular data, and speech separation. In all cases, the results obtained by our method improve upon the non-local use of the same underlying architecture.

2 Related Work

Local learning approaches perform inference with models that are focused on training samples in the vicinity of each test sample. This way, the predictions are based on what is believed to be the most relevant data points. K-nearest neighbors, for example, is a local learning method. Bottou & Vapnik (1992) have presented a simple algorithm for adjusting the capacity of the learned model locally, and discuss the advantages of such models for learning with uneven data distributions. Alpaydin & Jordan (1996) combine multiple local perceptrons in either a cooperative or a discriminative manner, and Zhang et al. (2006) combine multiple local support vector machines. These and other similar contributions rely on local neighborhoods containing multiple samples. The one-shot similarity kernel of Wolf et al. (2009) contrasts a single test sample with many training samples. We are unaware of any previous contribution that finetunes a model based on a single sample or any local learning approach that involves hypernetworks.

Hypernetworks (Ha et al., 2016) are neural models that generate the weights of a second *primary* network, which performs the actual prediction task. Since the inferred weights are multiplied by the activations of the primary network, hypernetworks are a form of multiplicative interactions (Jayakumar et al., 2020), and extend layer-specific dynamic networks, which have been used to adapt neural models to the properties of the input sample (Klein et al., 2015; Riegler et al., 2015).

Hypernetworks benefit from the knowledge-sharing ability of the weight-generating network and are therefore suited for meta-learning tasks, including few-shot learning (Bertinetto et al., 2016), continual learning (von Oswald et al., 2020), and model personalization Shamsian et al. (2021). When there is a need to repeatedly train similar networks, predicting the weights can be more efficient than backpropagation. Hypernetworks have, therefore, been used for neural architecture search (Brock et al., 2018; Zhang et al., 2019), and hyperparameter selection (Lorraine & Duvenaud, 2018).

MEND by Mitchell et al. (2021) explores the problem of model editing for large language models, in which the model's parameters are updated after training to incorporate new data. In our work, the goal is to predict the label of the new sample and not to update the model. Unlike MEND, our method does not employ the label of the new sample.

Diffusion models Many of the recent generative models for images (Ho et al., 2022; Chen et al., 2020; Dhariwal & Nichol, 2021a) and speech (Kong et al., 2021; Chen et al., 2020) are based on a degenerate form of the Focker-Planck equation. Sohl-Dickstein et al. (2015) showed that complicated distributions could be learnt using a simple diffusion process. The Denoising Diffusion Probablistic Models (DDPM) of Ho et al. (2020) extend the framework and present high quality image synthesis. Song et al. (2020) sped up the inference time by an order of magnitude using implicit sampling with their DDIM method. Watson et al. (2021) propose a dynamic programming algorithm to find an efficient denoising schedule and San-Roman et al. (2021) apply a learned scaling adjustments to the noise scheduling. Luhman & Luhman (2021) combined knowledge distillation with DDPMs.

The iterative nature of the denoising generation scheme creates an opportunity to steer the process, by considering the gradients of additional loss terms. The Iterative Latent Variable Refinement (ILVR) method Choi et al. (2021) does so for images by directing the generated image toward a low-resolution template. A similar technique was subsequently employed for voice modification Levkovitch et al. (2022). Direct conditioning is also possible: Saharia et al. (2022) generate photo-realistic text-to-image scenes by conditioning a diffusion model on text embedding; Amit et al. (2021) repeatedly condition on the input image to obtain image segmentation. In voice generation, the mel-spectrogram can be used as additional input to the denoising network Chen et al. (2020); Kong et al. (2021); Liu et al. (2021), as can the input text for a text-to-speech diffusion model Popov et al. (2021).

3 PROBLEM SETTING AND ANALYSIS

We are given a dataset S of samples $x_i \in \mathcal{X}$, for $i = 1..n$, and the associated labels $y_i \in \mathcal{Y}$ sampled i.i.d from some distribution $\mathcal{P}_{X\times Y}$ over the composite domain $\mathcal{X} \times \mathcal{Y}$. We consider prediction models $f : \mathcal{X} \times \Theta \to \mathcal{Y}$ that are parameterized by weight vectors in the domain Θ. Specifically, we first learn a base model $f_\theta(x) = f(x, \theta)$, which is trained over the entire training set S.

For every sample $s \sim \mathcal{P}_{X\times Y}$, we further consider a finetuned version of f_θ that is optimized to overfit on the sample $s = (x, y)$, i.e., we minimize the loss of the single sample s, initializing the optimization process with θ. We denote the obtained parameters as $\theta_s \in \Theta$ and the obtained network as f_{θ_s}. Naturally, the prediction error of f_{θ_s} on the sample s is expected to be small, improving upon that f_θ for that specific sample.

The meta-learning problem we consider is the one of learning a model g, that maps x (the input domain of sample s) and potentially multiple latent representations of x in the context of f_θ, collectively denoted as $I(x)$, to a vector of weight differences, such that the following loss is minimized

$$\mathcal{L}(s) = MSE(\theta_s, \theta + g(x, I(x)))\,, \tag{1}$$

where MSE is the mean squared error. If g generalizes well to **unseen** samples $s^* = (x^*, y^*)$, we would expect $f(x^*, \theta + g(x^*, I(x^*)))$ to be a better prediction of y^* than $f(x^*, \theta)$.

We rewrite the mapping function $g(x, I(x))$ as a unit-norm component $g_u(x, I(x))$, and a scale factor $\rho(x, I(x))$, i.e.,

$$g(x, I(x)) = \rho(x, I(x)) \cdot g_u(x, I(x))\,, \text{ where} \tag{2}$$

$$||g_u(x, I(x))||_2 = 1 \tag{3}$$

Denote the mapping between a sample $s = (x, y)$ and $\frac{\theta_s - \theta}{||\theta_s - \theta||}$ as $H : \mathcal{X} \times \mathcal{Y} \to \Theta$. Let $H_1 : \mathcal{X} \times \mathcal{Y} \to \mathcal{X} \times \mathcal{Y} \times \Theta$ be the linear approximation of the operator H, i.e., $H(s + \delta s) = H(s) + H_1(s) \otimes \delta s + O(\delta s \otimes \delta s)$, where $\otimes$ denotes the tensor product along the sample dimensions.

Next, we provide two theoretical arguments without concrete quantization. First, following Kleinberg et al. (2018), if θ is near a local minima or an inflection point of the finetuning loss, then θ_s would converge to this point and $H(s + \delta s)$ is expected to be convex.

Second, since θ is obtained via an SGD optimization process over a sample from the distribution $\mathcal{P}_{X\times Y}$, and since $s \sim P_{X\times Y}$, it is near either a local minima or an inflection point for the training loss of finetuning with sample s. See, for example, Kleinberg et al. (2018).

Combining the two claims, we can expect H to be locally convex.

Lemma 1. *Since H is locally convex, it follows that the distribution $\mathcal{P}_{H_1(s)}$ in the domain Θ obtained when applying H_1 to samples $s \sim \mathcal{P}_{X\times Y}$ takes the following form:*

$$\mathcal{P}_{H_1(s)} = \mathcal{P}_{X\times Y}({H_1}^{-1}(s) \otimes s)|det(H_1^{-1})|\,, \tag{4}$$

where $H_1^{-1}(s) : (\mathcal{X} \times \mathcal{Y} \times \Theta) \times (\mathcal{X} \times \mathcal{Y})$ is the pseudoinverse of the tensor $H_1(s)$ (first we compute H_1 at given s, and then compute the tensor pseudoinverse).

Proof. For any random variable r, and a mapping function M that is monotonic and with a countable number of zeros, the following holds (Rosenblatt (1974)):

$$\mathcal{P}_{M(r)} = \mathcal{P}_r(M^{-1}(r))|\frac{dM^{-1}(r)}{dr}| \tag{5}$$

Where M^-1 is the pseudoinverse of M. From the local convexity of H, we have that its' Hessian is nonnegative.

$$\text{H is locally convex} \to \nabla^2 H(s + \delta s) \geq 0; \forall \delta s \to 0 \tag{6}$$

Recall that the Hessian of H is the gradient of H_1, thus its gradient is non-negative, leading to monotonicity.

$$H_1(s) = \nabla H(s) \to \nabla H_1(s) = \nabla^2 H(s) \tag{7}$$

$$\nabla H_1(s) \geq 0 \tag{8}$$

In addition, since H_1 is a linear operator with finite size, it must have a finite dimension of null space.

$$Ker(H_1) \leq dim(H_1)\,, \tag{9}$$

where Ker is the tensor null space, dim is the tensor dimensions. This fulfils the second condition of the mapping function having countable number of zeros. □

Therefore, the distribution of H_1 is a linear transformation of the distribution of s. Ho et al. (2020) showed that a diffusion process is suitable for estimating samples from complicated sample distributions. Assume that there exists a diffusion process, with weights γ, over the sample distribution, such that the variational bound is maximized

$$\max_{\gamma} E_q(log(p_\gamma(x_{0:T})) - log(q(x_{1:T}|x_0)))\,, \tag{10}$$

where p_γ is the model distribution, $q(x_0)$ is the data distribution, and $x_{0:T}$ forms a Markov chain. From Lemma. 1 we have that the image of the distribution of H_1 is contained in the image of q, with the same input set. Thus, if a diffusion model has the capacity to capture q, it will also capture H_1, which is a subset of q.

4 METHOD

Our method is based on a modified diffusion process. Recall that we denote the training dataset as $S = \{(x_i, y_i)\}_{i=1}^n$, and that for every training sample $s \in S$ we run fine-tuning based on that single sample to obtain the overfitted parameters (function) as θ_s (f_{θ_s}). In our method, $\theta_s = \theta + g(x, I(x))$, where θ are the base model's parameters which are trained over S, and $g(x, I(x))$ is a mapping function that maps the input, i.e., the x part of s, and multiple latent representations of it, $I(x)$, to the desired shift in the model parameters.

Layer selection Current deep neural networks can have millions or even billions of parameters. Thus, learning to modify all network parameters can be a prohibitive task. Therefore, we opt to modify, via function g, on a single layer of f_θ.

To select this layer, we follow Lutati & Wolf (2021) and choose the layer that presents the maximal entropy of the loss, when fixing the samples s, and perturbing the layer's parameters. Denote the perturbed weights, in which only layer L is perturbed, as θ^L. The score used for selection is

$$\sum_{(x,y)\in S} \text{Entropy}_{\theta_L}(\mathcal{L}(f(x, \theta^L), y))\,, \tag{11}$$

where $\mathcal{L}$ is the loss objective on which the function of f_θ is trained on, and the entropy is computed over multiple draws of θ^L. The entropy is computed by fitting a Gaussian Kernel Density Estimation (GKDE) (Silverman, 1986) to the obtained empirical distribution of the loss function. Since sampling does not involve a backpropagation computation, the process is not costly, so $10,000$ samples are used.

The conditioning signal The latent representations, $I(x)$, has three components. Given a selected layer, L, we denote the input to this layer (when passing a sample x to $f(x, \theta)$), as $i_L(x)$ and the activation of this layer as $a_L(x)$. We also use the output of the base function $f_\theta(x)$. $I(x)$ is, therefore, the tuple

$$I(x) = [i_L(x), a_L(x), f_\theta(x)] \tag{12}$$

4.1 DIFFUSION PROCESS

The diffusion goal is to reconstruct the mapping function $g_u(x, I(x))$. The process iteratively starts a random Ω_T, iterates with Ω_t, where t is decreasing and is the diffusion step, and returns Ω_0.

The diffusion error estimation network, ϵ_Ω is a function of the current estimation, Ω_t, the latent representation tuple, $I(x)$, and the diffusion timestep, t. The latter is encoded through a positional encoding network (Vaswani et al., 2017), PE. All inputs, except for Ω_t are combined into one vector: $e = PE(t) + E_i(i_L) + E_a(a_L) + E_o(f_\theta(x))$, where E_i, E_a, E_o are the encodings of the layer input, layer activations and network output. Note that most of the components of e do not

Algorithm 1 Training Algorithm.
Input: S training set, θ base network parameters, $\mathcal{L}$ the loss of the primary task, T diffusion steps
Output: ϵ_Ω diffusion network (including E_i,E_a, and E_o).

1: **repeat**
2: sample $(x, y) \sim S$
3: $\theta_s = \theta$
4: **repeat**
5: Take a gradient step on $\nabla\mathcal{L}(y, f_{\theta_s}(x))$, updating θ_s
6: **until** $\mathcal{L}(y, f_{\theta_s}(x))$ converges
7: $\theta_s^{\text{norm}} = \frac{\theta_s - \theta}{||\theta_s - \theta||}$
8: $t \sim Uniform(1...T)$
9: $\epsilon = N(\mathbf{0}, \mathbf{1})$
10: $\beta_t = \frac{10^{-4}(T-t)+10^{-2}(t-1)}{T-1}$,$\alpha_t = 1 - \beta_t$, $\bar{\alpha}_t = \Pi_{k=0}^{k=t}\alpha_k$
11: $\Omega_t = \sqrt{\bar{\alpha}_t}\theta_s^{\text{norm}} + \sqrt{1 - \bar{\alpha}_t{}^2}\epsilon$
12: Take a gradient step on $\nabla||\epsilon - \epsilon_\Omega(\Omega_t, (I(x), t))||$, updating ϵ_Ω, PE and the components of I
13: **until** $||\epsilon - \epsilon_\Omega(\Omega_t, (I(x), t))||$ converges

change during the diffusion process, and can be computed only once. This way, the conditioning overhead is reduced to minimum. The conditional diffusion process is depicted in Fig 1.

Training Phase The complete training procedure of ϵ_Ω is depicted in Alg. 1. The first phase is overfitting, using simple gradient decent over a single input-output pair, see line 5. The overfitting phase is not demanding, since the backpropagation is conducted only over the selected layer and a single sample.

As stated in Sec. 4.2, while regular diffusion assumes that the input has unit variance, when estimating network weights, scaling has a crucial impact. This normalization ensures that the diffusion is trained over unit-variance input. We denote by θ_s^{norm} the normalized difference between θ_s and the parameters θ of the base model (line 7).

Following Song et al. (2020), linear scheduling is used for the diffusion process, and β_t, α_t, $\bar{\alpha}_t$, $\tilde{\beta}_t$ are set in line 10. A training example is then sampled:

$$\Omega_t = \sqrt{\bar{\alpha}_t}\theta_s^{\text{norm}} + \sqrt{1 - \bar{\alpha}_t{}^2}\epsilon\,, \tag{13}$$

where $\epsilon \sim \mathcal{N}(0, 1)$ is normal noise. Since our goal is to recover the noiseless θ_s^{norm}, the objective is

$$||\epsilon - \epsilon_\Omega(\Omega_t, (I(x), t))|| \tag{14}$$

A gradient step is taken in order to optimize this objective, see line. 12.

Inference Phase Given an unseen input x, $I(x)$ is computed using the base network $f(x, \theta)$ and is used for all calls to the diffusion network ϵ_Ω. The exact diffusion steps are depicted in Alg. 2.

4.2 Scale Estimation

The Evidence Lower Bound (ELBO) used in Ho et al. (2020) assumes that the generated data has unit variance. In our case, in which the generated data reflects a difference in the layer's weights, the scale of the data presents considerable variation. Naturally, shifting the weights of a network by some vector d or by some scale times d can create a significant difference.

We, therefore, as indicated in Eq. 2, use an MLP network $\rho(x, I(x))$ to estimate the appropriate scale factor, based on the same conditioning signal that is used for the network ϵ_Ω that implements g_u as a diffusion process.

When learning network ρ, the following objective function is used

$$\mathcal{L}_{\text{scale}} = \sum_{s=(x,y)\in S} 10 \cdot log_{10}(\frac{|\rho(x, I(x)) - \rho_s|^2}{\rho_s})\,, \tag{15}$$

where $\rho_s = ||\theta_s - \theta||$.

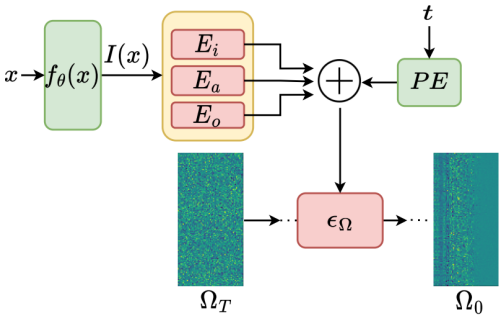


Figure 1: The diffusion process. x is the input of the base network, $f_\theta(x)$. $I(x)$ is a tuple of latent representations of x. E_i,E_a, and E_o are the input, activation, and output encoders, respectively, of the selected layer that is being modified. t is the diffusion step, and Ω_t is the current diffusion estimation.

Algorithm 2 Inference Algorithm.
Input: x input sample, θ the parameters of the base network, ϵ_Ω diffusion network, T diffusion steps.
Output: $g_u(x, I(x))$ estimated normalized $(\theta_s - \theta)$ for s associates with x.

1: $t = T$
2: $\epsilon = N(\mathbf{0}, \mathbf{1})$
3: **while** $t \geq 0$ **do**
4: $\beta_t = \frac{10^{-4}(T-t)+10^{-2}(t-1)}{T-1}$, $\alpha_t = 1 - \beta_t$, $\bar{\alpha}_t = \Pi_{k=0}^{k=t}\alpha_k$, $\tilde{\beta}_t = \frac{1-\bar{\alpha}_{t-1}}{1-\bar{\alpha}_t}\beta_t$
5: $\Omega_{t-1} = \frac{\Omega_t - \frac{1-\alpha_t}{\sqrt{1-\bar{\alpha}_t}}\epsilon_\Omega(\Omega_t, I(x), t)}{\sqrt{\alpha_t}} + \mathbf{1}_{t>1}\sqrt{\tilde{\beta}_t}$
6: $t = t - 1$
7: **end while**
8: **return** Ω_0

4.3 Architecture

The network ϵ_Ω is a U-Net (Ronneberger et al., 2015), following Ho et al. (2020). Each resolution level has residual blocks, and an attention layer. The bottleneck contains two attention layers.

The positional encoder is composed of stacked sine and cosine encodings, following Vaswani et al. (2017). The encoders of i_L, a_L are both single fully-connected layers, with dimensions to match the positional embedding. The encoder of the base network's output $f_\theta(x)$ depends on the output type. In the case of a classification network, where the output is a vector in $\mathbb{R}^{\mathbb{C}}$, where C is the number of classes, the encoder E_O is a single fully-connected layer. In the case of image generation, the output image is first encoded using a VGG11 encoder (Simonyan & Zisserman, 2014), and then the latent representation is passed through a single fully-connected layer, again matching the dimension of the positional encoder. For speech separation, the estimated speech is first transformed to a spectogram with 1024 bins of FFT, then encoded using the same VGG11.

5 Experiments

In all experiments the UNet ϵ_Ω has 128 channels and five downsampling layers. The Adam optimizer (Kingma & Ba, 2014), with a learning rate of 10^{-4}, is used. A linear noise schedule is used based on Song et al. (2020), and the number of diffusion steps is 10. All experiments are repeated three times to report the standard deviation (SD) of the success metrics. The inference overhead due to a U-Net forward pass is 27[ms] on a low-end Nvidia RTX2060 GPU (there are ten such passes, one per diffusion step).

In addition to the full method, we also show results for the network that overfits on the test data, which serves as an upper bound that cannot be applied without violating the train/test protocol. On some datasets we check to what extent selecting a single layer limits our results, by performing the overfitting process on all of the model weights. On all datasets, we ablate the scale component of our "Overfit with Conditional Diffusion models" (OCD) method, by estimating a fixed global scale factor $\bar{\rho} = \mathbb{E}_{s \in S}(\rho_s)$ as the mean value of the scale factor ρ_s over the train-set. An additional ablation selects the model f_{θ_s} of the training sample s with the closest x to the test sample. This "nearest neighbor" ablation can be seen as the simplest way to implement the concept of OCD. Finally, we present an ablation that selects the layer with the second highest layer selection score, to evaluate the significance of the selection criterion.

Image Classification Results for the MNIST dataset (LeCun & Cortes, 2010) are obtained with the LeNet5 architecture (Lecun et al., 1998). The selected layer is the one next to the last fully connected layer, which, as can be seen in Fig. 2(a) has the maximal entropy among LeNet5's layers. CIFAR10 images (Krizhevsky et al., 2009) are classified using GoogleNet (Szegedy et al., 2015).

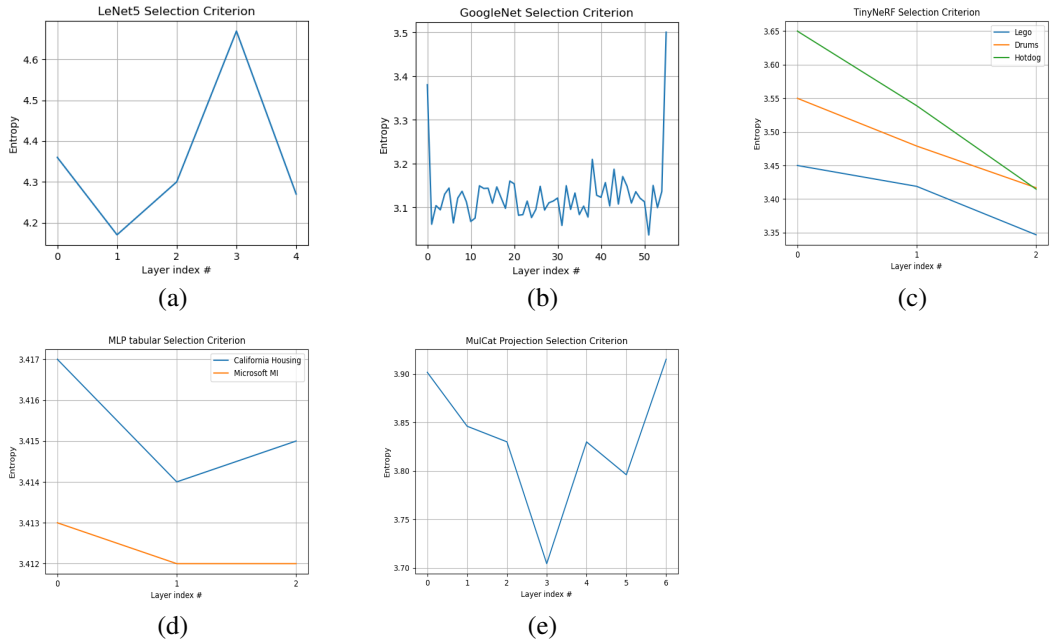


Figure 2: Layer Selection Criterion for different experiments. (a) For LeNet5 on MNIST, the next to last Fully-Connected layer is selected since it has the maximal entropy. (b) For GoogleNet on CIFAR10, the last Fully-Connected layer is selected. (c) For TinyNeRF (three datasets), the first Fully-Connected layer is selected. (d) For Tabular MLP the first layer is selected. (e) For MulCat the last projection layer is selected.

The selected layer was the last fully-connected layer, see Fig. 2(b). For both architectures, the three encoders E_{L_i}, E_{L_o}, E_O are simple fully-connected layers, with dimensions to match the number of channels in the UNet (128).

For classification experiments we measure both the binary cross entropy (evaluted on the test set) and the test accuracy. As can seen in Tab. 1, our method reduces the CE loss by a factor of 8 in comparison to the base network and there is a improvement of 0.5% in accuracy. Ablating the scale prediction, the results considerably degrade in comparison to the full method. The Nearest-Neighbor ablation yields slightly better results than the base network. The ablation that selects an alternative layer results in performance that is similar or slightly better than the base network. This is congruent with the small difference between fitting the selected layer and fitting all layers, which may suggest that much of the benefit of overfitting occurs in the selected layer.

On CIFAR10, our method improves classification accuracy from 92.9% to 93.7%. As in MNIST, much of the improvement is lost when running the three ablations.

In both MNIST and CIFAR, when using the ground truth to overfit a specific example, the accuracy becomes, as expected, 100%. Considering the CE loss, overfitting the entire model instead of the selected layers yields only mild improvement (for MNIST below the standard deviation). This indicates that the added improvement gained by applying our method to all layers (and not just to the selected one) may not justify the additional resources required.

Image Synthesis We further tested our method on the image generation task of novel view synthesis, using a NeRF architecture (Mildenhall et al., 2021) and the "Synthetic-Blender" dataset. The Tiny-NeRF architecture (Murthy, 2020) employs an MLP network consisting of three fully-connected layers. The input is a 3D ray as a 5D coordinate (spatial location and viewing direction). The output is the corresponding emitted radiance. For each view, a batch of 4096 rays is computed, from which the interpolated image is synthesized.

Table 1: Performance on classification tasks. CE=Cross Entropy

	MNIST (LeNet5)		CIFAR10 (GoogleNet)	
Method	Test-CE (↓)	Accuracy %(↑)	Test-CE (↓)	Accuracy %(↑)
Base network	0.080 ± 0.009	99.2 ± 0.1	0.085 ± 0.01	92.85 ± 0.40
Overfitting on test	0.002 ± 0.0001	100	0.075 ± 0.005	100
Overfitting on test (All Layers)	0.002 ± 0.0001	100	0.073 ± 0.003	100
OCD nearest neighbor ablation	0.073 ± 0.010	99.3 ± 0.1	0.082 ± 0.02	93.03 ± 0.40
OCD no scaling ablation	0.069 ± 0.010	99.3 ± 0.1	0.084 ± 0.02	93.01 ± 0.35
OCD alternative layer ablation	0.078 ± 0.010	99.2 ± 0.1	0.084 ± 0.01	92.96 ± 0.27
OCD (ours)	$\mathbf{0.010 \pm 0.006}$	$\mathbf{99.7 \pm 0.1}$	$\mathbf{0.080 \pm 0.01}$	$\mathbf{93.68 \pm 0.38}$

Table 2: Performance (MSE±SD, lower is better) for the TinyNeRF network.

Method	Lego	Hotdog	Drums
Base model	0.076 ± 0.004	0.063 ± 0.007	0.068 ± 0.006
Overfitting on test	0.043 ± 0.005	0.032 ± 0.005	0.049 ± 0.003
OCD no scaling ablation	0.070 ± 0.008	0.060 ± 0.005	0.064 ± 0.008
OCD (ours)	$\mathbf{0.052 \pm 0.006}$	$\mathbf{0.047 \pm 0.004}$	$\mathbf{0.057 \pm 0.006}$

We experimented with three objects from the dataset: Lego, Hotdog, and Drums. For each object a different TinyNeRF base model is trained over the corresponding training set. A single overfitting example is produced by considering a batch of 4096 rays from the same viewpoint.

Based on the data in Fig. 2(c), the first layer is selected. We, therefore, changed the layer-input encoder, E_i, such that the input image is first encoded by the VGG-11 encoder of Simonyan & Zisserman (2014) (pretrained over ImageNet-1k), followed by a fully-connected layer, to match the dimensions of UNet channels. The encoders E_a, E_o are simple fully-connected layers, with dimensions to match the number of channels in the UNet (128).

As can seen in Tab. 2, our method improves the MSE by 31% on the Lego model, by 25% for Hotdog, and 16% for Drums. Without input-dependent scaling, the performance is much closer to the base network than to that of our complete method. Sample test views are shown in Fig. 3 and in Appendix A. Evidently, our method improves both image sharpness and color palette, bringing the synthesized image closer to the one obtained by overfitting the test image.

Tabular Data Gorishniy et al. (2021) have extensively benchmarked various architectures and tabular datasets. We use their simple MLP architecture as a base network (3 Layers). We were unable to reproduce the reported transformer, since the hyperparameters are not provided, and our resources did not allow us to run a neural architecture search, as Gorishniy et al. (2021) did. We run on two of the benchmarks listed: California Housing Kelley Pace & Barry (1997) (CA), which is the first listed and has the least number of samples, and Microsoft LETOR4.0(MI) (Qin & Liu, 2013), which is the last listed and has the largest number of samples.

Fig. 2(d) presents the layer selection criterion, with the first layer chosen for both datasets. As can seen in Tab. 3, for CA the base MLP model falls behind ResNet. Applying our method, the simple architecture achieves better results. For MI when applying our method, the simple baseline achieves a record MSE of 0.743, surpassing the current best record on this dataset, which is 0.745 (Popov et al., 2020). The ablation that removes input-dependent scaling degrades the performance of the base network, emphasizing the importance of accurate scaling per sample.

Speech Separation To tackle the task of single microphone speech separation of multiple speakers, Nachmani et al. (2020) introduce the Gated-LSTM architecture with MulCat block and Dovrat et al. (2021) introduced a permutation-invariant loss based on the Hungarian matching algorithm, using the same architecture. Lutati et al. (2022) further improved results for this architecture, by employing an iterative method based on a theoretical upper bound, achieving state-of-the-art results.

Table 3: Tabular benchmarks by Gorishniy et al. (2021). $MSE \pm SD$, lower is better.

Method	CA	MI
MLP	0.4990 ± 0.0030	$0.7470 \pm .0004$
ResNet	0.4860 ± 0.0030	$0.7480 \pm .0003$
Overfit MLP on test	$0.4750 \pm .0020$	$0.7410 \pm .0003$
OCD + MLP no scale	$0.5000 \pm .0030$	$0.7490 \pm .0006$
OCD + MLP (ours)	$\mathbf{0.4800 \pm .0020}$	$\mathbf{0.7430 \pm .0004}$

Table 4: Performance of Gated-LSTM with the Hungarian loss on Libri5Mix.

Method	SI-SDRi[dB] (↑)
Dovrat et al. (2021)	12.7 ± 0.1
Lutati et al. (2022)	13.2 ± 0.2
Overfit on test	13.5 ± 0.1
OCD no scale	12.8 ± 0.3
OCD (ours)	$\mathbf{13.4 \pm 0.1}$

Table 5: Classification accuracy for the NLP task of few-shot classification with 8 samples per class.

Method	SST-5	AmazonCF	CR	Emotion	EnronSpam	Average
T-few 3B (Liu et al., 2022)	55.0	19.0	92.1	57.4	93.1	63.32
SetFit (Tunstall et al., 2022)	43.6	40.3	88.5	48.8	90.1	62.26
SetFit + OCD	47.8	41.0	90.5	50.2	92.2	**64.34**
Ensemble of SetFit + OCD	48.6	**41.2**	91.2	50.5	92.7	**64.84**

The same backbone and Hungarian-method loss are used in our experiments, which run on the Libri5Mix dataset without augmentations, measuring the SI-SDRi score. The selected layer was the projection layer of the last MulCat block (Fig. 2(e)). The output of the Gated-LSTM is the separated sounds, and to encode it, we apply the audio encoding described in Sec. 4.3 to each output channel separately and concatenate before applying the linear projection to $\mathbb{R}^{128}$.

As can seen in Tab. 4, applying our diffusion model over the Gated-LSTM model, we achieve $13.4dB$, surpassing current state-of-the-art results and approaching the results obtained by overfitting on the test data. The ablation that removes input-dependent scaling is much closer in performance to the base network than to our complete method.

Prompt-free Few-Shot NLP Classification Recent few-shot methods have achieved impressive results in label-scarce settings. However, they are difficult to employ since they require language models with billions of parameters and hand-crafted prompts. Very recently, Tunstall et al. (2022) introduced a lean architecture, named SetFit, for finetuning a pretrained sentence transformer over a small dataset (8 examples per class), and then employing logistic regression over the corresponding embedding.

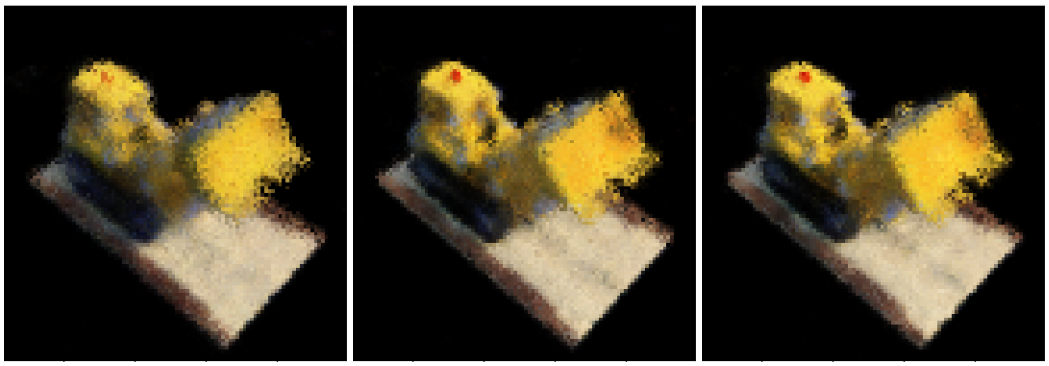
In our experiments, we apply OCD to the last linear layer of the SetFIT sentence transformer. The U-Net has 64 channels, with 5 downsample layers. The size of the last linear layer is $768x768$. $I(x) \in \mathbb{R}^{768x1}$ is the embedding of the Sentence Transformer.

As can be seen in Tab. 5 using OCD and this lean architecture (with 110M parameters) outperforms, on average, the state-of-the-art model of Liu et al. (2022), which has 3B parameters. The mean performance across the datasets is improved by 1.0% over the state-of-the-art and by 2.1% over the SetFIT model we build upon.

Since the weights in the OCD hypernetworks are obtained by a diffusion process, one can draw multiple networks for each sample x. The variability that arises from the random initialization of the diffusion process allows us to use an ensemble. As can be seen in Tab. 5, when applying an ensemble of five inferences, the results of OCD further improve by 0.4% (on average) to a gap of 1.5% over the state-of-the-art.

Table 6: The Cross-Entropy loss for the NLP task of few-shot classification with 8 samples per class using SetFIT + OCD, comparing one instance to the mean network obtained with 5 instances.

Method	SST-5	AmazonCF	CR	Emotion	EnronSpam
One instance	0.45 ± 0.19	0.65 ± 0.30	0.41 ± 0.11	0.63 ± 0.31	0.39 ± 0.20
Mean network of 5 instances	0.42 ± 0.20	0.61 ± 0.25	0.39 ± 0.11	0.59 ± 0.32	0.38 ± 0.19



(a) (b) (c)

Figure 3: Sample TinyNeRF results (Lego model). More results can be found in Appendix A. (a) Base model on a test view. (b) Same test view, overfitted using the ground truth (c) OCD (ours).

Table 7: The runtime of the various experiments on a low-end Nvidia RTX2060GPU. The training is composed out of the base model training, the collection for data for OCD by overfitting each sample in the training set, and the training of the diffusion model. The main overhead between the base model and the OCD one during inference is a result of running the UNet of the diffusion process for ten iterations.

	Training [hrs]			Inference [ms]	
Architecture	Base	Overfitting	Diffusion	Base	OCD
LeNet5	0.5	1.0	6.0	15	288
GoogleNet	2.5	1.0	5.0	20	298
TinyNeRF	1.1	0.2	5.2	230	510
MLP	1.2	0.1	6.2	75	355
Gated-LSTM	30	2.5	6.8	450	730
SetFit	0.2	0.1	5.1	125	401

Interestingly, when testing the average network weights of the five networks, the accuracy is virtually identical to the one obtained with a single OCD network (omitted from the table). However, there is some reduction in the Cross-Entropy when comparing the mean network obtained to a single OCD instance (Tab. 6).

Runtime Tab. 7 lists the clock time with and without OCD for both training and inference. Since overfitting each sample includes only 3 gradient descent steps over a single layer, most of the data collection results are shorter than the training time of the base model, with the exception of LeNet5 training that used a batch size of 16 versus batch size of 1 in the overfitting stage. Training the diffusion model is slower in most experiments than training the base model, except for the speech model, in which training the base model is lengthy. The inference overhead is almost constant across the six models since it consists of running the UNet ϵ_Ω ten times. In absolute terms, the overhead incurred by OCD, even on a very modest GPU, is only a quarter of a second, while improving the results substantially. We note that the same ϵ_Ω is used for all experiments, padding the actual weight matrix, which induces an unnecessary computational cost in the case of small networks.

6 Conclusions

We present what is, as far as we can ascertain, the first diffusion-based hypernetwork and show that learning the scale independently is required for best performance. The hypernetwork is studied in the specific context of local learning, in which a dynamic model is conditioned on a single input sample. This, too, seems to be a novel contribution. Using the diffusion architecture for the local learning

task is justified by a first-order analysis of the change to a network's weights when performing limited finetuning.

The training samples for the hypernetwork are collected by finetuning a model on each specific sample from the training set used by the base model. By construction, this is only slightly more demanding than fitting the base model on the training set. More limiting is the size of the output of the hypernetwork, which for modern networks can be larger than the output dimensions of other diffusion processes. We, therefore, focus on a single layer, which is selected as the one that is most affected by weight perturbations. We extensively tested our method, tackling a very diverse set of tasks, using the same set of hyperparameters. We are yet to find a single dataset or architecture on which our OCD method does not significantly improve the results of the baseline architecture.

REFERENCES

Ethem Alpaydin and Michael I Jordan. Local linear perceptrons for classification. *IEEE Transactions on Neural Networks*, 7(3):788–794, 1996.

Tomer Amit, Eliya Nachmani, Tal Shaharbany, and Lior Wolf. Segdiff: Image segmentation with diffusion probabilistic models. *arXiv preprint arXiv:2112.00390*, 2021.

Luca Bertinetto, João F Henriques, Jack Valmadre, Philip Torr, and Andrea Vedaldi. Learning feed-forward one-shot learners. In *Advances in Neural Information Processing Systems*, pp. 523–531, 2016.

Léon Bottou and Vladimir Vapnik. Local learning algorithms. *Neural Computation*, 4(6):888–900, 1992. doi: 10.1162/neco.1992.4.6.888.

Andrew Brock, Theo Lim, J.M. Ritchie, and Nick Weston. SMASH: One-shot model architecture search through hypernetworks. In *International Conference on Learning Representations*, 2018. URL `https://openreview.net/forum?id=rydeCEhs-`.

Nanxin Chen, Yu Zhang, Heiga Zen, Ron J Weiss, Mohammad Norouzi, and William Chan. Wavegrad: Estimating gradients for waveform generation. *arXiv preprint arXiv:2009.00713*, 2020.

Jooyoung Choi, Sungwon Kim, Yonghyun Jeong, Youngjune Gwon, and Sungroh Yoon. Ilvr: Conditioning method for denoising diffusion probabilistic models. In *2021 IEEE/CVF International Conference on Computer Vision (ICCV)*, pp. 14347–14356. IEEE, 2021.

Prafulla Dhariwal and Alex Nichol. Diffusion models beat gans on image synthesis. *arXiv preprint arXiv:2105.05233*, 2021a.

Prafulla Dhariwal and Alexander Nichol. Diffusion models beat gans on image synthesis. *Advances in Neural Information Processing Systems*, 34:8780–8794, 2021b.

Shaked Dovrat, Eliya Nachmani, and Lior Wolf. Many-speakers single channel speech separation with optimal permutation training. In *INTERSPEECH*, 2021.

Yury Gorishniy, Ivan Rubachev, Valentin Khrulkov, and Artem Babenko. Revisiting deep learning models for tabular data. *Advances in Neural Information Processing Systems*, 34:18932–18943, 2021.

David Ha, Andrew Dai, and Quoc V Le. Hypernetworks. *arXiv preprint arXiv:1609.09106*, 2016.

Xu Han, Zhengyan Zhang, Ning Ding, Yuxian Gu, Xiao Liu, Yuqi Huo, Jiezhong Qiu, Yuan Yao, Ao Zhang, Liang Zhang, et al. Pre-trained models: Past, present and future. *AI Open*, 2:225–250, 2021.

Jonathan Ho, Ajay Jain, and Pieter Abbeel. Denoising diffusion probabilistic models. *Advances in Neural Information Processing Systems*, 33:6840–6851, 2020.

Jonathan Ho, Chitwan Saharia, William Chan, David J Fleet, Mohammad Norouzi, and Tim Salimans. Cascaded diffusion models for high fidelity image generation. *Journal of Machine Learning Research*, 23(47):1–33, 2022.

Siddhant M. Jayakumar et al. Multiplicative interactions and where to find them. In *International Conference on Learning Representations*, 2020.

R. Kelley Pace and Ronald Barry. Sparse spatial autoregressions. *Statistics Probability Letters*, 33(3):291–297, 1997. ISSN 0167-7152. doi: https://doi.org/10.1016/S0167-7152(96)00140-X. URL https://www.sciencedirect.com/science/article/pii/S016771529600140X.

Diederik P Kingma and Jimmy Ba. Adam: A method for stochastic optimization. *arXiv preprint arXiv:1412.6980*, 2014.

Benjamin Klein, Lior Wolf, and Yehuda Afek. A dynamic convolutional layer for short range weather prediction. In *Proc. IEEE Conference on Computer Vision and Pattern Recognition*, pp. 4840–4848, 2015.

Bobby Kleinberg, Yuanzhi Li, and Yang Yuan. An alternative view: When does sgd escape local minima? In *International Conference on Machine Learning*, pp. 2698–2707. PMLR, 2018.

Zhifeng Kong, Wei Ping, Jiaji Huang, Kexin Zhao, and Bryan Catanzaro. Diffwave: A versatile diffusion model for audio synthesis. In *International Conference on Learning Representations*, 2021.

Alex Krizhevsky, Geoffrey Hinton, et al. Learning multiple layers of features from tiny images. 2009.

Y. Lecun, L. Bottou, Y. Bengio, and P. Haffner. Gradient-based learning applied to document recognition. *Proceedings of the IEEE*, 86(11):2278–2324, 1998. doi: 10.1109/5.726791.

Yann LeCun and Corinna Cortes. MNIST handwritten digit database. http://yann.lecun.com/exdb/mnist/, 2010. URL http://yann.lecun.com/exdb/mnist/.

Alon Levkovitch, Eliya Nachmani, and Lior Wolf. Zero-shot voice conditioning for denoising diffusion tts models. In *INTERSPEECH*, 2022.

Haokun Liu, Derek Tam, Mohammed Muqeeth, Jay Mohta, Tenghao Huang, Mohit Bansal, and Colin Raffel. Few-shot parameter-efficient fine-tuning is better and cheaper than in-context learning. *arXiv preprint arXiv:2205.05638*, 2022.

Jinglin Liu, Chengxi Li, Yi Ren, Feiyang Chen, Peng Liu, and Zhou Zhao. Diffsinger: Singing voice synthesis via shallow diffusion mechanism. *arXiv preprint arXiv:2105.02446*, 2021.

Jonathan Lorraine and David Duvenaud. Stochastic hyperparameter optimization through hypernetworks. *arXiv preprint arXiv:1802.09419*, 2018.

Eric Luhman and Troy Luhman. Knowledge distillation in iterative generative models for improved sampling speed. *arXiv preprint arXiv:2101.02388*, 2021.

Shahar Lutati and Lior Wolf. Hyperhypernetwork for the design of antenna arrays. In *International Conference on Machine Learning*, pp. 7214–7223. PMLR, 2021.

Shahar Lutati, Eliya Nachmani, and Lior Wolf. Sepit: Approaching a single channel speech separation bound. In *INTERSPEECH*, 2022.

Ben Mildenhall, Pratul P Srinivasan, Matthew Tancik, Jonathan T Barron, Ravi Ramamoorthi, and Ren Ng. Nerf: Representing scenes as neural radiance fields for view synthesis. *Communications of the ACM*, 65(1):99–106, 2021.

Eric Mitchell, Charles Lin, Antoine Bosselut, Chelsea Finn, and Christopher D Manning. Fast model editing at scale. *arXiv preprint arXiv:2110.11309*, 2021.

Krishna Murthy. nerf-pytorch. https://github.com/krrish94/nerf-pytorch/blob/master/tiny_nerf.py, 2020.

Eliya Nachmani, Yossi Adi, and Lior Wolf. Voice separation with an unknown number of multiple speakers. In *International Conference on Machine Learning*, pp. 7164–7175. PMLR, 2020.

Sergei Popov, Stanislav Morozov, and Artem Babenko. Neural oblivious decision ensembles for deep learning on tabular data. In *International Conference on Learning Representations*, 2020. URL https://openreview.net/forum?id=r1eiu2VtwH.

Vadim Popov, Ivan Vovk, Vladimir Gogoryan, Tasnima Sadekova, and Mikhail Kudinov. Grad-tts: A diffusion probabilistic model for text-to-speech. In *International Conference on Machine Learning*, pp. 8599–8608. PMLR, 2021.

Tao Qin and Tie-Yan Liu. Introducing letor 4.0 datasets. *arXiv preprint arXiv:1306.2597*, 2013.

Gernot Riegler, Samuel Schulter, Matthias Ruther, and Horst Bischof. Conditioned regression models for non-blind single image super-resolution. In *Proceedings of the IEEE International Conference on Computer Vision*, pp. 522–530, 2015.

Olaf Ronneberger, Philipp Fischer, and Thomas Brox. U-net: Convolutional networks for biomedical image segmentation. In *International Conference on Medical image computing and computer-assisted intervention*, pp. 234–241. Springer, 2015.

M. Rosenblatt. *Random Processes*. Springer New York, 1974. doi: 10.1007/978-1-4612-9852-6. URL https://doi.org/10.1007/978-1-4612-9852-6.

Chitwan Saharia, William Chan, Saurabh Saxena, Lala Li, Jay Whang, Emily Denton, Seyed Kamyar Seyed Ghasemipour, Burcu Karagol Ayan, S Sara Mahdavi, Rapha Gontijo Lopes, et al. Photorealistic text-to-image diffusion models with deep language understanding. *arXiv preprint arXiv:2205.11487*, 2022.

Robin San-Roman, Eliya Nachmani, and Lior Wolf. Noise estimation for generative diffusion models. *arXiv preprint arXiv:2104.02600*, 2021.

Aviv Shamsian, Aviv Navon, Ethan Fetaya, and Gal Chechik. Personalized federated learning using hypernetworks. In *International Conference on Machine Learning*, pp. 9489–9502. PMLR, 2021.

B. W. Silverman. *Density Estimation for Statistics and Data Analysis*. Chapman & Hall, London, 1986.

Karen Simonyan and Andrew Zisserman. Very deep convolutional networks for large-scale image recognition. *arXiv preprint arXiv:1409.1556*, 2014.

Jascha Sohl-Dickstein, Eric Weiss, Niru Maheswaranathan, and Surya Ganguli. Deep unsupervised learning using nonequilibrium thermodynamics. In *International Conference on Machine Learning*, pp. 2256–2265. PMLR, 2015.

Jiaming Song, Chenlin Meng, and Stefano Ermon. Denoising diffusion implicit models. *arXiv preprint arXiv:2010.02502*, 2020.

Christian Szegedy, Wei Liu, Yangqing Jia, Pierre Sermanet, Scott Reed, Dragomir Anguelov, Dumitru Erhan, Vincent Vanhoucke, and Andrew Rabinovich. Going deeper with convolutions. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pp. 1–9, 2015.

Lewis Tunstall, Nils Reimers, Unso Eun Seo Jo, Luke Bates, Daniel Korat, Moshe Wasserblat, and Oren Pereg. Efficient few-shot learning without prompts. *arXiv preprint arXiv:2209.11055*, 2022.

Ashish Vaswani, Noam Shazeer, Niki Parmar, Jakob Uszkoreit, Llion Jones, Aidan N Gomez, Łukasz Kaiser, and Illia Polosukhin. Attention is all you need. *Advances in neural information processing systems*, 30, 2017.

Johannes von Oswald, Christian Henning, João Sacramento, and Benjamin F. Grewe. Continual learning with hypernetworks. In *International Conference on Learning Representations*, 2020.

Daniel Watson, Jonathan Ho, Mohammad Norouzi, and William Chan. Learning to efficiently sample from diffusion probabilistic models. *arXiv preprint arXiv:2106.03802*, 2021.

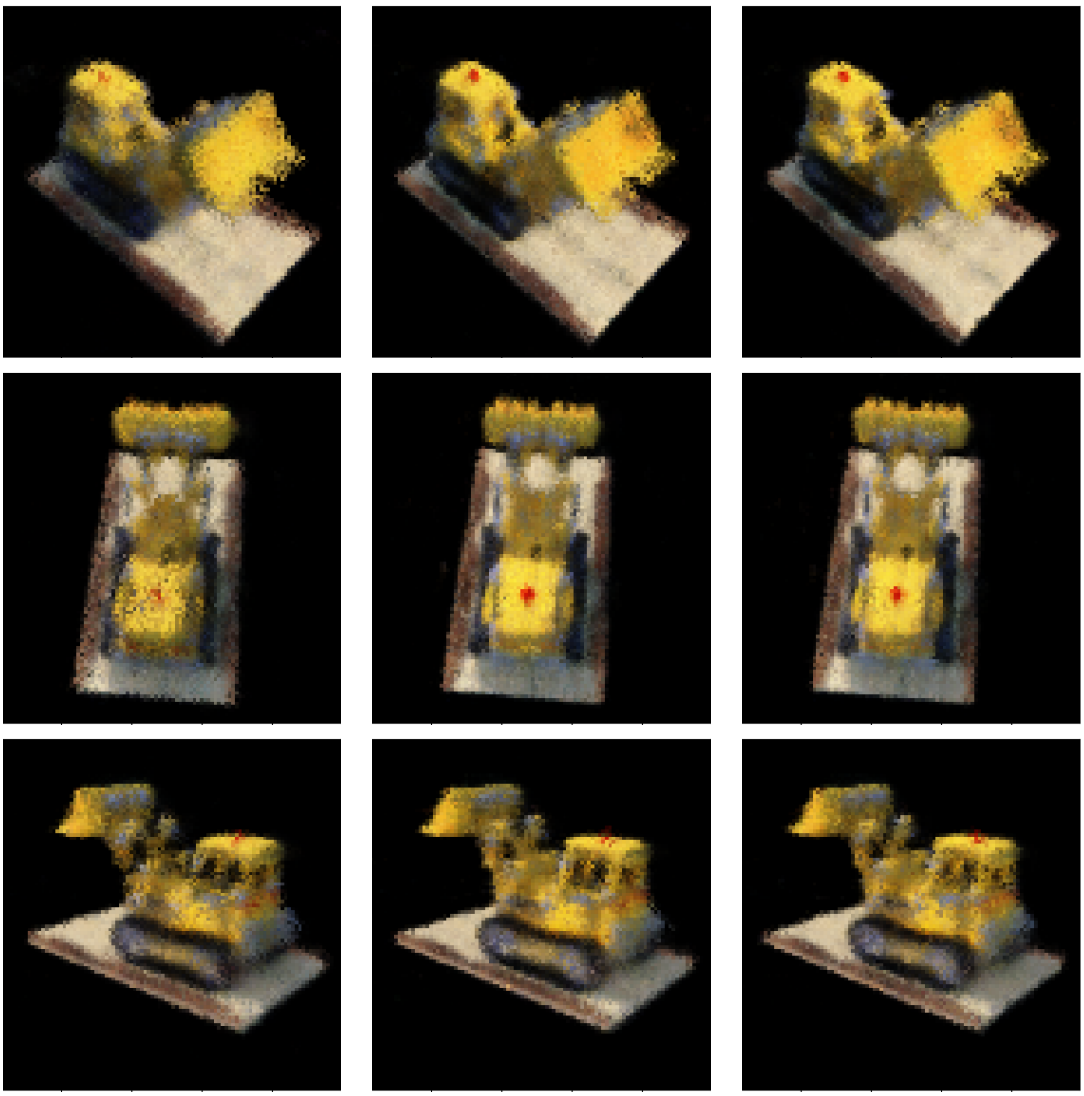
Lior Wolf, Tal Hassner, and Yaniv Taigman. The one-shot similarity kernel. In *2009 IEEE 12th International Conference on Computer Vision*, pp. 897–902. IEEE, 2009.

C. Zhang, M. Ren, and R. Urtasun. Graph hypernetworks for neural architecture search. In *Int. Conf. on Learning Representations*, 2019. URL https://openreview.net/forum?id=rkgW0oA9FX.

Hao Zhang, Alexander C Berg, Michael Maire, and Jitendra Malik. Svm-knn: Discriminative nearest neighbor classification for visual category recognition. In *CVPR*, volume 2, pp. 2126–2136. IEEE, 2006.

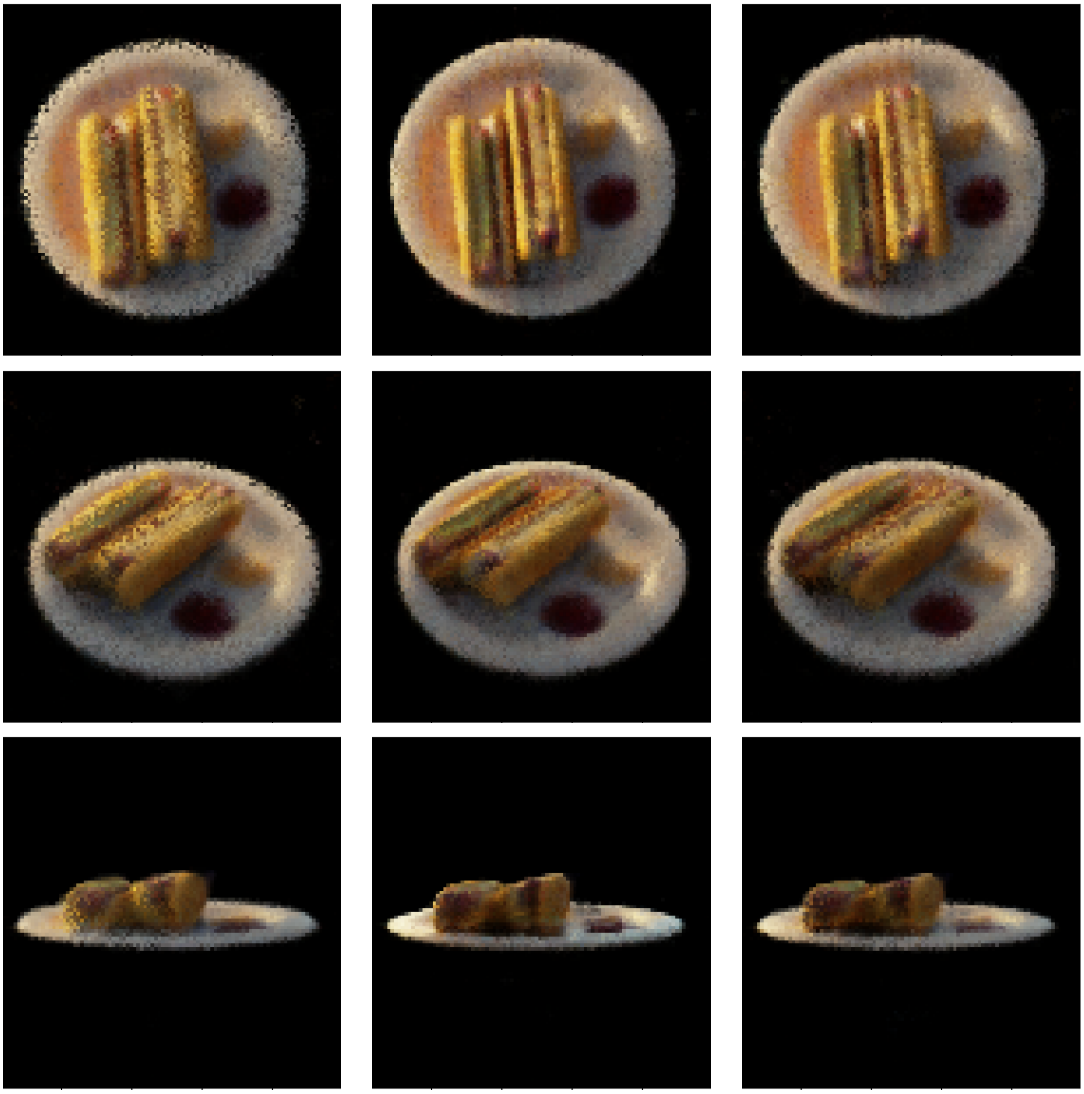
A TINYNERF SAMPLE RESULTS

Fig. 4 presents sample results for the reconstruction of the Lego Model. Fig. 5 presents results for the Hotdog model. Fig. 6 presents sample test views of the Drums model.



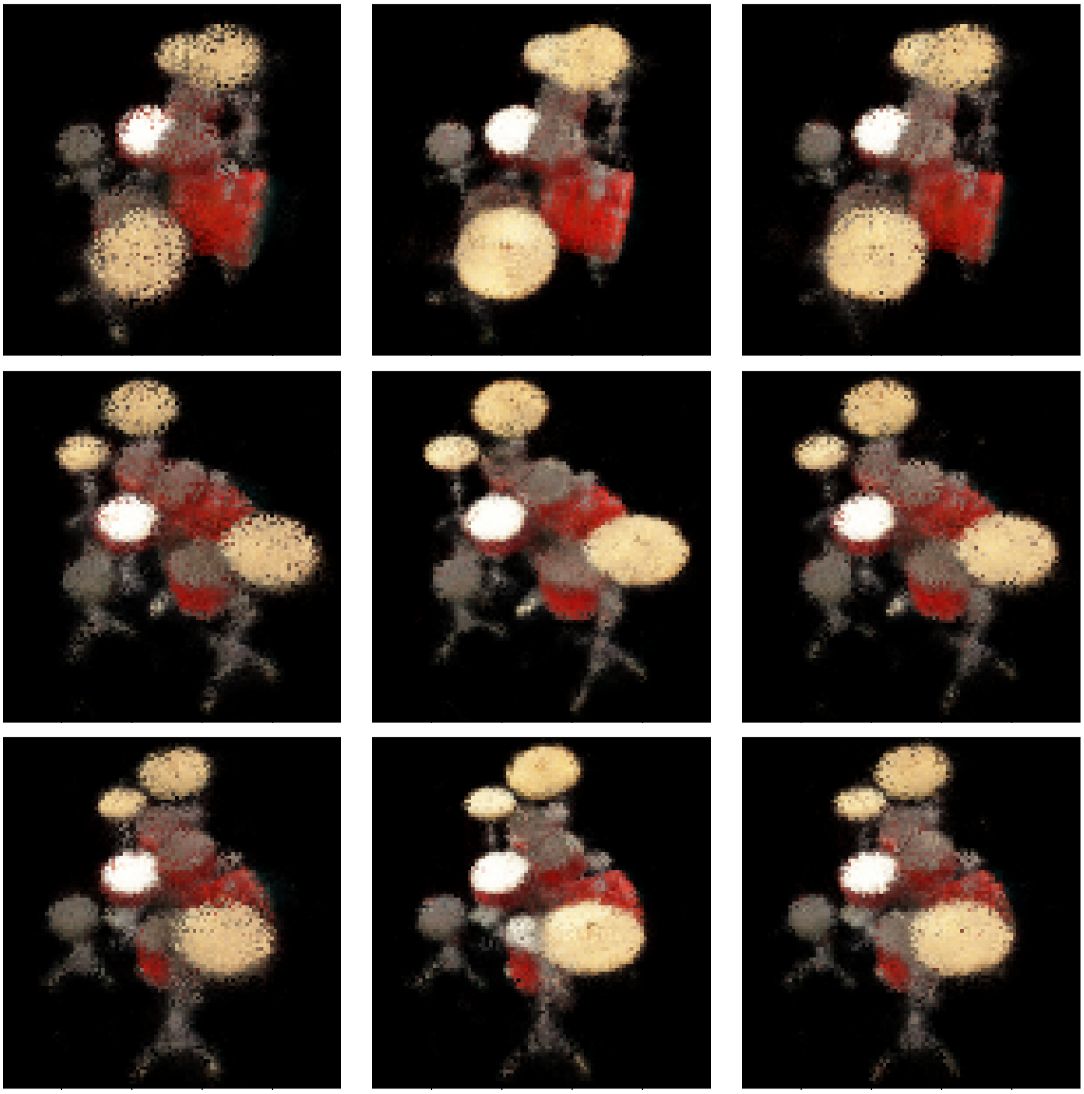
(a) (b) (c)

Figure 4: Sample TinyNeRF results on the Lego model. (a) Base model on a test view. (b) Same test view, overfitted using the ground truth (c) OCD (ours).



(a) (b) (c)

Figure 5: Sample TinyNeRF results on the Hotdog model. (a) Base model on a test view. (b) Same test view, overfitted using the ground truth (c) OCD (ours).



(a) (b) (c)

Figure 6: Sample TinyNeRF results on the Drums model. (a) Base model on a test view. (b) Same test view, overfitted using the ground truth (c) OCD (ours).