Dual-Curriculum Contrastive Multi-Instance Learning for Cancer Prognosis Analysis with Whole Slide Images

Abstract

The multi-instance learning (MIL) has advanced cancer prognosis analysis with whole slide images (WSIs). However, current MIL methods for WSI analysis still confront unique challenges. Previous methods typically generate instance representations via a pre-trained model or a model trained by the instances with bag-level annotations, which, however, may not generalize well to the downstream task due to the introduction of excessive label noises and the lack of fine-grained information across multi-magnification WSIs. Additionally, existing methods generally aggregate instance representations as bag ones for prognosis prediction and have no consideration of intra-bag redundancy and inter-bag discrimination. To address these issues, we propose a dual-curriculum contrastive MIL method for cancer prognosis analysis with WSIs. The proposed method consists of two curriculums, i.e., saliency-guided weakly-supervised instance encoding with cross-scale tiles and contrastive-enhanced soft-bag prognosis inference. Extensive experiments on three public datasets demonstrate that our method outperforms state-of-the-art methods in this field. The code is available.

1 Introduction

Cancer prognosis analysis is of great significance for risk-benefit assessment and clinical decision [1]. Computational whole slide image (WSI), which entails the quantitative profiling of spatial patterns and tumor microenvironments in tissue slides, has advanced the application of deep learning in cancer prognosis analysis [2, 3]. However, deep learning in WSIs is often hindered by the gigapixel size and the lack of pixel-level annotations [4]. Recently, multi-instance learning (MIL) methods have attracted increasing attention to performing inference in a weakly-supervised manner and have been successfully applied to WSI analysis [5, 6, 7].

In general, the MIL consists of two stages, i.e., instance encoding and aggregation stages [8, 9]. In the encoding stage, several methods have utilized the pre-trained model (e.g., ResNet on ImageNet) to extract instance representations in an unsupervised way (i.e., without the reference of outcome labels) [10, 11, 12]. However, recent studies have demonstrated that the pre-trained model may not generalize well to the downstream tasks as it is task-agnostic[1] and inclined to overfit the pretraining objective [13, 14, 15]. Alternatively, some studies directly assigned each instance the bag-level annotation (i.e., the survival time of the patient) for network training, which introduces task-specific[1] supervision and

---

[1]The "task-specific" and "task-agnostic" refer to a training manner that is oriented by the task target or not. This work aims to conduct cancer prognosis. The "task-specific" means using prognosis labels (e.g. survival time or death risk) as supervision to train the model, while the "task-agnostic" means unsupervised or using prognosis-irrelevant annotations as supervision.

improves model's generalisability [16, 17, 18]. Actually, the prognosis evaluation is primarily and comprehensively determined by certain representative regions, yet those regions might only occupy a small portion of WSI [17]. As a result, the strong supervision on all instances, especially on prognosis-irrelevant tiles, will introduce excessive label noises and limit model's performance [19, 20]. For alleviating this issue, a feasible way is to supervise the instance encoding in a weak and easy-to-hard manner. On the other hand, existing methods often generate mono-scale instance representations [11, 21] or typically concatenate multi-scale information from multi-magnification WSIs [22, 23], which may result in feature redundancy and ignore fine-grained details across multi-magnification images.

In the aggregation stage, most previous studies aggregate instance representations within a bag for prognosis estimation by certain fusion strategies (e.g., pooling operation and attention mechanism) [24, 25]. However, it may overwhelm prognosis-relevant information, cause intra-bag redundancy, and reduce inter-bag discrimination, if many instances from irrelevant regions are enrolled [12, 26]. To address the above-mentioned issues, we arm MIL with a dual-curriculum strategy and propose a dual-curriculum contrastive MIL method for cancer prognosis analysis with WSIs. The proposed method consists of two easy-to-hard curriculums, i.e., saliency-guided weakly-supervised instance encoding with cross-scale tiles and contrastive-enhanced soft-bag prognosis inference. The main contributions are summarized as follows:

1) We present a dual-curriculum contrastive MIL method which includes two easy-to-hard curriculums. We first conduct a preliminary task to learn instance representations by considering risk stratification status (degraded from survival time) as the annotation, followed by the prognosis inference with survival time as supervision.

2) We design the first curriculum of saliency-guided weakly-supervised instance encoding with cross-scale tiles. It is supervised by the relatively weak annotations so as to reduce label noises and maintain prognosis-related guidance. Additionally, to imitate the reviewing procedure of pathologists, we leverage the low-magnification saliency map to guide the encoding of high-magnification instances for exploring fine-grained information across multi-magnification WSIs.

3) We develop the second curriculum of contrastive-enhanced soft-bag prognosis inference. Instead of enrolling all instances, we adaptively identify and integrate representative instances within a bag (as the soft-bag) for prognosis inference and leverage the constrained self-attention strategy to obtain extra sparseness for soft-bag representations, which can help reduce intra-bag redundancy in both instance and feature levels. Meanwhile, we improve the Cox loss with two-tier contrastive learning for enhancing intra-bag and inter-bag discrimination.

4) We evaluate the proposed method on three public cancer datasets and extensive experiments demonstrate that our method outperforms state-of-the-art methods in cancer prognosis analysis with WSIs.

2 Related Work

2.1 WSI-based Cancer Prognosis Model

In recent years, many methods, especially convolutional neural networks (CNNs), have been proposed for cancer prognosis evaluation with WSIs [27, 28, 29]. Due to the gigapixel size of WSI, some methods took small-size ROIs selectively sampled from WSIs as the input of the network for training and inference, in which all ROIs were assigned with patient-level outcome labels [30, 31]. However, these methods generally require prior knowledge from pathologists, which are experience-dependent and may suffer from high inter-observer variation. Therefore, current researches have proposed to crop the entire WSI into many tiles for the model's input so as to make full use of available information contained by WSI [10, 32, 33]. However, these methods often confront the lack of tile-level annotations and may result in a sub-optimal solution. To this end, MIL methods have been proposed to perform cancer prognosis analysis in a weakly-supervised manner and have shown promising performance in this field [5, 28].

2.2 Multi-instance Learning in WSI Analysis

The MIL methods in WSI analysis can be roughly divided into two categories according to the way instances are leveraged in the model [12, 17]. The one infers bag-level ones from instance-level

prediction via average pooling, maximum pooling, or other ensemble strategies [34, 35]. In contrast, the other one, referred to as the bag embedding method, aggregates instance representations as bag ones, upon which a model is constructed for bag-level prediction [36, 37]. The former is simple and straightforward but empirically proven to be inferior to the latter in terms of generalization performance. Therefore, the bag embedding method has attracted extensive attention in WSI analysis [17]. For example, Courtiol et al. [6] developed a MIL method based on CNN, called MesoNet, to accurately predict the overall survival of mesothelioma patients with WSIs. Yao et al. [5] proposed deep attention multiple instance survival learning to efficiently learn features from the WSI and aggregated them for prognosis prediction. Our method essentially belongs to the bag embedding method. Different from previous methods, the proposed method consists of two easy-to-hard curriculums, in which fine-grained information across multi-magnification WSIs, intra-bag redundancy, and inter-bag discrimination are comprehensively considered.

3 Method

3.1 Problem Formulation

Denote the triplet $\{\mathbf{X}_n, \mathbf{T}_n, \boldsymbol{\delta}_n\}_{n=1}^N$ as the dataset consisting of N patients, where $\mathbf{X}_n$ is the n-th patient with one or more WSIs, $\mathbf{T}_n$ and $\boldsymbol{\delta}_n$ are its observed survival time and event indicator (viz. equals to 1 and 0 for uncensored and censored samples, respectively). Prognosis analysis is an ordinal regression task that models time-to-event distribution, which is formulated as

$$\hat{\mathbf{T}}_n = \mathbb{S}(\mathbf{X}_n), \tag{1}$$

where $\mathbb{S}$ and $\hat{\mathbf{T}}_n$ denote the prognosis inference function and the estimated survival time, respectively. In practice, it is difficult to directly feed the whole WSI into the model due to its gigapixel size. Accordingly, many studies [10, 32, 33] have cropped WSIs into many tiles and generated bag $\mathbf{X}_n = \{\mathbf{x}_{n,i}\}_{i=1}^{N_n}$ which contains N_n instances (tiles) for the n-th patient. Then, MIL is leveraged to construct the prognosis model as follows:

$$\hat{\mathbf{T}}_n = \mathbb{S}(\mathbb{A}\{\mathbb{E}(\mathbf{x}_{n,i}) : \mathbf{x}_{n,i} \in \mathbf{X}_n\}), \tag{2}$$

where $\mathbb{E}$ is an instance encoding function that extracts feature representation for each instance, and $\mathbb{A}$ is a permutation-invariant instance aggregation function that pools the instance representations into the bag ones. However, previous studies [10, 11, 12, 16, 17, 18] typically generate instance representations via a pre-trained model or a model trained by the instances with bag-level annotations, which may not generalize well to the downstream task. As a result, we decompose the model into two easy-to-hard curriculums, including (1) Curriculum I (C-I): instance encoding (via $\mathbb{E}$) during preliminary risk stratification (via $\mathbb{C}$, a risk stratification function), and (2) Curriculum II (C-II): prognosis inference (via $\mathbb{S}$) after instance aggregation (via $\mathbb{A}$). Formally, the optimization process can be formulated as

$$\begin{cases} \text{C-I} : \hat{\mathbb{E}}, \hat{\mathbb{C}} = \arg\min_{\mathbb{E}, \mathbb{C}} \sum_{n=1}^N \dagger(\mathbf{Y}_n == 1 \| 0) \sum_{i=1}^{N_n} [\mathbb{C}\{\mathbb{E}(\mathbf{x}_{n,i}) : \mathbf{x}_{n,i} \in \mathbf{X}_n\}, \mathbf{Y}_n]_{\mathcal{L}_{\text{I}}} \\ \text{C-II} : \hat{\mathbb{S}}, \hat{\mathbb{A}} = \arg\min_{\mathbb{S}, \mathbb{A}} \sum_{n=1}^N [\mathbb{S}(\mathbb{A}\{\hat{\mathbb{E}}(\mathbf{x}_{n,i}) : \mathbf{x}_{n,i} \in \mathbf{X}_n\}), \mathbf{T}_n, \boldsymbol{\delta}_n]_{\mathcal{L}_{\text{II}}} \end{cases}, \tag{3}$$

where $\dagger(\cdot)$ outputs 1 (0) if true (false), and $\mathcal{L}_{\text{I}}$ and $\mathcal{L}_{\text{II}}$ denote the loss functions for C-I and C-II, respectively. The risk stratification status $\mathbf{Y}_n$ is determined by $\{\mathbf{T}_n, \boldsymbol{\delta}_n\}$ with a three-year time threshold (denoted as $\mathbf{T}_r$) as follows:

$$\mathbf{Y}_n = \begin{cases} 1 & , \mathbf{T}_n \leq \mathbf{T}_r \ \&\& \ \boldsymbol{\delta}_n == 1 \\ 0 & , \mathbf{T}_n > \mathbf{T}_r \\ - & , \text{others} \end{cases}. \tag{4}$$

3.2 Curriculum I: Saliency-guided Weakly-supervised Instance Encoding with Cross-scale Tiles

In this section, we introduce the first curriculum of saliency-guided weakly-supervised instance encoding with cross-scale tiles, as shown in Figure 1. Given the input instance with S magnifications

Figure 1: The pipeline of the proposed dual-curriculum contrastive MIL method for cancer prognosis analysis with WSIs. The left is saliency-guided weakly-supervised instance encoding with cross-scale tiles (Curriculum I), while the right one is contrastive-enhanced soft-bag prognosis inference (Curriculum II).

$\{\mathbf{x}_{n,i}^s\}_{s=1}^S$ ($S = 3$ in this work), the proposed method contains S branches and each branch takes different-magnification tiles as input, which aims to explore multi-scale information from multi-magnification images. For the s-th branch, it mainly consists of a feature extractor $\mathbb{F}^s$, a feature aggregator $\mathbb{G}^s$ and a classifier $\mathbb{C}^s$. And $\{\mathbb{F}^s\}_{s=1}^S$ and $\{\mathbb{G}^s\}_{s=1}^S$ form $\mathbb{E}$, while $\{\mathbb{C}^s\}_{s=1}^S$ constitute $\mathbb{C}$ in Eq.(3). The feature extractor $\mathbb{F}^s$ contains s residual modules with the parameters $\{\boldsymbol{\theta}_{\mathbb{F}^s}^1, \cdots, \boldsymbol{\theta}_{\mathbb{F}^s}^s\}$, and the first $s - 1$ modules share the same architecture with $\mathbb{F}^{s-1}$ if $s > 1$. Figure 2 illustrates the architecture details [2]. Different from previous studies [22, 23] that separately feed $\{\mathbf{x}_{n,i}^s\}_{s=1}^S$ into the network and ignore fine-grained details across multi-magnification images, we encourage the network to focus on salient regions by utilizing the prior knowledge of the $(s-1)$-th branch to highlight the input $\mathbf{x}_{n,i}^s$, which can be formulated as

$$\hat{\mathbf{x}}_{n,i}^s = \begin{cases} \mathbf{x}_{n,i}^s & , s = 1 \\ \mathbf{m}_{n,i}^{s-1} \otimes \mathbf{x}_{n,i}^s & , s > 1 \end{cases}, \tag{5}$$

where $\otimes$ denotes the element-wise multiplication operator, and $\mathbf{m}_{n,i}^{s-1}$ is the salient mask indicating high-risk regions. For convenience, we introduce how to acquire $\mathbf{m}_{n,i}^s$, which is easily generalized to $\mathbf{m}_{n,i}^{s-1}$. Specifically, $\mathbf{m}_{n,i}^s$ is computed by Class Activation Map [38] as follows:

$$\mathbf{m}_{n,i}^s = \boldsymbol{\omega}^s \odot \mathbb{F}^s(\hat{\mathbf{x}}_{n,i}^s), \tag{6}$$

where $\odot$ is the channel-wise multiplication operator, and $\boldsymbol{\omega}^s$ indicates the importance of channel of feature maps for risk stratification prediction in the s-th branch. To obtain $\boldsymbol{\omega}^s$, we first generate an instance embedding vector $\mathbf{z}_{n,i}^s$ by

$$\mathbf{z}_{n,i}^s = \mathbb{G}^s(\mathbb{F}^s(\hat{\mathbf{x}}_{n,i}^s)), \tag{7}$$

where $\mathbb{G}^s$ is a feature aggregator that performs channel-direction attention (as shown in Figure 2). Incorporating comprehensive information from current and previous branches, we subsequently feed instance embeddings $\{\mathbf{z}_{n,i}^j\}_{j=1}^s$ into the classifier $\mathbb{C}^s$ for predicting high-risk probability $\mathbf{p}_{n,i}^s$, which is computed by

$$\mathbf{p}_{n,i}^s = \mathbb{C}^s(\{\mathbf{z}_{n,i}^j\}_{j=1}^s) = \phi(\overline{\boldsymbol{\omega}}^s \times [\mathbf{z}_{n,i}^1, \cdots, \mathbf{z}_{n,i}^{s-1}]^T + \boldsymbol{\omega}^s \times [\mathbf{z}_{n,i}^s]^T), \tag{8}$$

where $\mathbb{C}^s$ is implemented by a linear layer with the parameters $\{\overline{\boldsymbol{\omega}}^s, \boldsymbol{\omega}^s\}$ (as shown in Figure 2), and ϕ and T denote softmax activation function and transposition operation, respectively.

---

[2] The feature extractor $\mathbb{F}^1$ shares the same architecture with the top-14 layers of ResNet-18, upon which $\mathbb{F}^2$ additionally deepens the network by introducing two identify blocks with the modification of the number of kernel (from [128, 128, 512] to [128, 128, 256]). And $\mathbb{F}^3$ deepens the architecture using the same way with $\mathbb{F}^2$.

Figure 2: The detailed architectures of some modules in the model. The first row show the architectures of the feature extractor $\mathbb{F}$, the feature aggregator $\mathbb{G}$ and classifier $\mathbb{C}$ In Curriculum I, while the second row illustrates the architectures of soft-bag learning model $\mathbb{B}$, the constrained self-attention module $\mathbb{D}$ and contrastive-enhanced prognosis inference function $\mathbb{S}$ in Curriculum II.

We introduce a hierarchical transfer strategy to leverage the prior from different-magnification images, accelerate network convergence, and maintain the specificity of current branch. Specifically, as shown in Figure 1, the parameter $\boldsymbol{\theta}_{\mathbb{F}^s}^s$ (for any s) of the s-th module in $\mathbb{F}^s$ is completely learnable and has not any constraints, while $\boldsymbol{\theta}_{\mathbb{F}^s}^{s-1}$ (for $s > 1$) is also learnable but constrained to approximate $\boldsymbol{\theta}_{\mathbb{F}^{s-1}}^{s-1}$ by the structural loss $\mathcal{L}_\Omega$ as follows:

$$\mathcal{L}_\Omega = \left\| \boldsymbol{\theta}_{\mathbb{F}^s}^{s-1} - \boldsymbol{\theta}_{\mathbb{F}^{s-1}}^{s-1} \right\|_2. \tag{9}$$

For the remaining parameters $\{\boldsymbol{\theta}_{\mathbb{F}^s}^1, \cdots, \boldsymbol{\theta}_{\mathbb{F}^s}^{s-2}\}$ (for $s > 2$) in $\mathbb{F}^s$, they are first initialized with $\{\boldsymbol{\theta}_{\mathbb{F}^{s-1}}^1, \cdots, \boldsymbol{\theta}_{\mathbb{F}^{s-1}}^{s-2}\}$, and then are frozen. Furthermore, we propose a hybrid loss function $\mathcal{L}_\mathrm{I}$ that contains two parts, i.e., empirical loss $\mathcal{L}_\ell$ and structural loss $\mathcal{L}_\Omega$, to train the network:

$$\mathcal{L}_\mathrm{I} = \mathcal{L}_\ell + \beta_\Omega \mathcal{L}_\Omega, \tag{10}$$

where β_Ω is the weight coefficient, and the empirical loss $\mathcal{L}_\ell$ is defined as

$$\mathcal{L}_\ell = -\frac{1}{NN_n} \sum_{n=1}^{N} \sum_{i=1}^{N_n} \mathbf{y}_{n,i}^s \log(\mathbf{p}_{n,i}^s) + (1 - \mathbf{y}_{n,i}^s) \log(1 - \mathbf{p}_{n,i}^s), \tag{11}$$

where $\mathbf{y}_{n,i}^s \in \mathbf{Y}_n$ denotes the risk stratification status of the i-th instance in the n-th bag.

Finally, we can obtain the multi-scale instance representation $\mathbf{z}_{n,i}$ for subsequent prognosis inference task by $\mathbf{z}_{n,i} = [\mathbf{z}_{n,i}^1, \cdots, \mathbf{z}_{n,i}^S]$.

3.3 Curriculum II: Contrastive-enhanced Soft-bag Prognosis Inference

In this section, we develop the second curriculum of contrastive-enhanced soft-bag prognosis inference, as shown in Figure 1. Given a set of instance representations from the n-th bag, i.e., $\mathbf{Z}_n = [\mathbf{z}_{n,1}; \mathbf{z}_{n,2}; \cdots; \mathbf{z}_{n,N_n}]^T \in \mathbb{R}^{N_n \times C}$, where C denotes the feature dimension, the proposed method mainly consists of a soft-bag learning module $\mathbb{B}$, a constrained self-attention module $\mathbb{D}$, a contrastive-enhanced prognosis inference function $\mathbb{S}$, where $\mathbb{B}$ and $\mathbb{D}$ form $\mathbb{A}$ in Eq.(3).

For the soft-bag learning module $\mathbb{B}$ (as shown in Figure 2), it first learns new bag representation $\mathbf{E}_n \in \mathbb{R}^{N_n \times D}$ (where D denotes the feature dimension) from $\mathbf{Z}_n$ via a linear layer. Instead of enrolling all instances, we adaptively identify and integrate representative instances within a bag by introducing the function $\mathbb{H}$:

$$\hat{\mathbf{E}}_n = \mathbb{H}(\mathbf{E}_n, \hat{\mathbf{h}}_n) = \phi\left(diag\{\hat{\mathbf{h}}_n\} \times \mathbf{W}_n\right)^T \times \left(diag\{\hat{\mathbf{h}}_n\} \times \mathbf{E}_n\right), \tag{12}$$

where $\hat{\mathbf{E}}_n \in \mathbb{R}^{N_B \times D}$ (N_B is the number of selected instances in each bag, and $N_B \ll N_n$) is the feature representation of those selected instances, and $\mathbf{W}_n \in \mathbb{R}^{N_n \times N_B}$ denotes the weight matrix that is generated by feeding $\mathbf{E}_n$ into two linear layers (as shown in Figure 2). And $\hat{\mathbf{h}}_n \in \mathbb{R}^{N_n \times 1}$ is an

indicator vector that adaptively selects N_B representative instances and is computed by

$$\hat{\mathbf{h}}_n = \arg\max_{\mathbf{h}_n} \mathbb{S}\left(\mathbb{D}\left(\mathbb{H}(\mathbf{E}_n, \mathbf{h}_n)\right)\right), \quad s.t. \sum_{i=1}^{N_n} \mathbf{h}_{n,i} = N_B. \tag{13}$$

The constrained self-attention module $\mathbb{D}$ and contrastive-enhanced prognosis inference function $\mathbb{S}$ are introduced below.

We leverage $\mathbb{D}$ to obtain extra sparseness for soft-bag representations. Given the input $\hat{\mathbf{E}}_n$, it first linearly projects $\hat{\mathbf{E}}_n$ into three feature spaces (i.e., $\mathbf{Q}_n \in \mathbb{R}^{N_B \times \hat{D}}$, $\mathbf{K}_n \in \mathbb{R}^{N_B \times \hat{D}}$, and $\mathbf{V}_n \in \mathbb{R}^{N_B \times \hat{D}}$, and $\hat{D}$ is the feature dimension) via three mapping matrices (i.e., $\mathbf{W}_Q \in \mathbb{R}^{D \times \hat{D}}$, $\mathbf{W}_K \in \mathbb{R}^{D \times \hat{D}}$, and $\mathbf{W}_V \in \mathbb{R}^{D \times \hat{D}}$), in which the mapping matrices are constrained by

$$\mathcal{L}_s = (\|\mathbf{W}_Q\|_1 + \|\mathbf{W}_K\|_1 + \|\mathbf{W}_V\|_1). \tag{14}$$

Then, the sparse soft-bag representation $\mathbf{B}_n \in \mathbb{R}^{1 \times D_B}$ (where D_B is the feature dimension) can be obtained by the correlation-based activation mechanism [39], as illustrated in Figure 2. It is worth mentioning that the collaboration of $\mathbb{B}$ and $\mathbb{D}$ can significantly help reduce intra-bag redundancy in both instance and feature levels so as to improve the model's generalization.

For $\mathbb{S}$, it takes $\mathbf{B}_n$ as input to infer the relative risk $\hat{\mathbf{T}}_n$ via a linear projection matrix $\mathbf{W}_{\mathbb{S}} \in \mathbb{R}^{D_B \times 1}$, as shown in Figure 2. In order to improve the ability of soft-bag inference, we perform two-tier contrastive learning (TCL) to enhance intra-bag and inter-bag discrimination. We assume that a bag $\mathbf{B}_n$ is sampled from the distribution $\mathcal{O} = \{\mathcal{O}^+, \mathcal{O}^-\}$, where the positive source $\mathcal{O}^+$ denotes the distribution of high-hazard samples (i.e. those with survival time $\leq \mathbf{T}_r$), while the negative source $\mathcal{O}^-$ presents the distribution of low-hazard samples (i.e. those with survival time $> \mathbf{T}_r$). We first focus on the inter-bag discrimination. Let $\mathcal{B}_n = \{\mathbf{B}_1, \cdots, \mathbf{B}_{N_{B_n}}\}/\mathbf{B}_n$ present the collection of bags (expect $\mathbf{B}_n$) from the same source $\mathcal{O}^+$ (or $\mathcal{O}^-$) with $\mathbf{B}_n$, where N_{B_n} denotes the number of such bags. We can obtain the representation of $\mathcal{B}_n$ (denoted as $\hat{\mathbf{B}}_n$) by merging the representations of all bags in $\mathcal{B}_n$ via a attention function $\mathbb{K}$ (as illustrated in Figure 2). Inspired by [40], the inter-bag discrimination can be enhanced by maximally preserving the mutual information between $\mathbf{B}_n$ and $\hat{\mathbf{B}}_n$ as follows:

$$\sum_{n \in [N]} \mathbb{I}(\mathbf{B}_n, \hat{\mathbf{B}}_n) = \sum_{n \in [N]} p(\mathbf{B}_n, \hat{\mathbf{B}}_n) \log \frac{p(\mathbf{B}_n|\hat{\mathbf{B}}_n)}{p(\mathbf{B}_n)}. \tag{15}$$

According to Eq.(12), partial instances within a bag are adaptively discarded and the rest remained. However, all instances within the bag belong to homologous tissues sampled from the same patient, which means that it should show potential correlation among these instances. Therefore, similar to Eq.(15), we maximize the following mutual information to improve the intra-bag discrimination:

$$\sum_{n \in [N]} \mathbb{I}(\mathbf{B}_n, \overline{\mathbf{B}}_n) = \sum_{n \in [N]} p(\mathbf{B}_n, \overline{\mathbf{B}}_n) \log \frac{p(\mathbf{B}_n|\overline{\mathbf{B}}_n)}{p(\mathbf{B}_n)}, \tag{16}$$

where $\overline{\mathbf{B}}_n$ is obtained via $\mathbb{K}$ to merge the representation of those discarded instances $\overline{\mathbf{E}}_n$ that has the definition of $\overline{\mathbf{E}}_n = \mathbb{H}(\mathbf{E}_n, \mathbf{1} - \hat{\mathbf{h}}_n)$, as illustrated in Figure 2. To this end, we propose to jointly maximize Eq.(15) and (16), i.e., $max(\sum_{n \in [N]} \mathbb{I}(\mathbf{B}_n, \hat{\mathbf{B}}_n) + \mathbb{I}(\mathbf{B}_n, \overline{\mathbf{B}}_n))$, which is formulated by

$$max\left(\sum_{n \in [N]} \log \frac{p(\mathbf{B}_n|\hat{\mathbf{B}}_n)}{p(\mathbf{B}_n)} + \log \frac{p(\mathbf{B}_n|\overline{\mathbf{B}}_n)}{p(\mathbf{B}_n)}\right) = max\left(\sum_{n \in [N]} \log \frac{p(\mathbf{B}_n|\hat{\mathbf{B}}_n)p(\mathbf{B}_n|\overline{\mathbf{B}}_n)}{p(\mathbf{B}_n)p(\mathbf{B}_n)}\right). \tag{17}$$

Instead of constructing a generative model $p(\mathbf{B}_n|\hat{\mathbf{B}}_n)p(\mathbf{B}_n|\overline{\mathbf{B}}_n)$, we leverage a log-bilinear function $\mathbb{L}$ to model the density ratio which preserves the mutual information:

$$\mathbb{L}(\mathbf{B}_n, \hat{\mathbf{B}}_n, \overline{\mathbf{B}}_n) = exp(\mathbf{B}_n^T \mathbf{W}_{\mathbb{L}} \hat{\mathbf{B}}_n) exp(\mathbf{B}_n^T \mathbf{V}_{\mathbb{L}} \overline{\mathbf{B}}_n) \tag{18}$$

$$= exp(\mathbf{B}_n^T \mathbf{W}_{\mathbb{L}} \hat{\mathbf{B}}_n + \mathbf{B}_n^T \mathbf{V}_{\mathbb{L}} \overline{\mathbf{B}}_n) \propto \frac{p(\mathbf{B}_n|\hat{\mathbf{B}}_n)p(\mathbf{B}_n|\overline{\mathbf{B}}_n)}{p(\mathbf{B}_n)p(\mathbf{B}_n)}, \tag{19}$$

Table 1: The results achieved by all competing methods on three datasets (i.e., COAD, LIHC, and BLCA). And the boldface denotes the best result.

	COAD		LIHC		BLCA		Overall	
	CI	AUC	CI	AUC	CI	AUC	CI	AUC
WSISA [43]	0.641±0.027	0.673±0.037	0.661±0.022	0.700±0.071	0.639±0.018	0.651±0.043	0.647	0.675
DeepGraphSurv [44]	0.629±0.054	0.639±0.038	0.613±0.027	0.633±0.047	0.620±0.015	0.687±0.046	0.620	0.653
MesoNet [6]	0.643±0.039	0.684±0.052	0.629±0.022	0.667±0.042	0.630±0.021	0.648±0.052	0.634	0.666
DeepAttnMISL [5]	0.683±0.025	0.654±0.045	0.672±0.027	0.676±0.019	0.642±0.020	0.661±0.076	0.666	0.663
Patch-GCN [10]	0.650±0.013	0.562±0.010	0.565±0.024	0.630±0.061	0.571±0.041	0.542±0.027	0.595	0.578
DC_MIL(our)	**0.717±0.012**	**0.754±0.031**	**0.705±0.015**	**0.745±0.012**	**0.672±0.029**	**0.720±0.039**	**0.698**	**0.740**

where $\mathbf{W}_{\mathbb{L}}$ and $\mathbf{V}_{\mathbb{L}}$ are trainable parameters. Motivated by [41], we design the TCL loss based on the InfoNCE function, which has the following definition:

$$\mathcal{L}_{tcl} = -\underset{\mathcal{B}}{\boldsymbol{E}} \left[\log \frac{\mathbb{L}(\mathbf{B}_n, \hat{\mathbf{B}}_n, \overline{\mathbf{B}}_n)}{\sum_{i \in [N], i \neq n} \mathbb{L}(\mathbf{B}_n, \hat{\mathbf{B}}_i, \overline{\mathbf{B}}_i)} \right], \tag{20}$$

where $\mathcal{B}$ denotes the collection of all bags. Additionally, we utilize the negative log partial likelihood of Cox proportional hazard regression model [42] to train the network, which is computed by

$$\mathcal{L}_{cox} = -\log(\prod_{n:\boldsymbol{\delta}_n=1} \frac{exp(\mathbf{B}_n \mathbf{W}_{\mathbb{S}})}{\sum_{j \in R(\mathbf{T}_n)} exp(\mathbf{B}_j \mathbf{W}_{\mathbb{S}})}) = -\sum_{n:\boldsymbol{\delta}_n=1} (\mathbf{B}_n \mathbf{W}_{\mathbb{S}} - \log(\sum_{j \in R(\mathbf{T}_n)} exp(\mathbf{B}_j \mathbf{W}_{\mathbb{S}}))),$$

where $\mathbf{W}_{\mathbb{S}}$ is the linear projection matrix in $\mathbb{S}$, and $R(\mathbf{T}_n) = \{i : \mathbf{T}_i \geq \mathbf{T}_n\}$ is the collection of all samples (including censored and uncensored samples) with survival time being longer than $\mathbf{T}_n$. Finally, the loss function $\mathcal{L}_{\mathrm{II}}$ for the second curriculum can be defined as

$$\mathcal{L}_{\mathrm{II}} = \mathcal{L}_{cox} + \mathcal{L}_{tcl} + \beta_s \mathcal{L}_s, \tag{21}$$

where β_s is the weight coefficient.

4 Experiments and Results

In this section, we briefly describe the datasets, preprocessing, and implementation details, followed by experimental results.

4.1 Datasets and Preprocessing

In this work, we evaluated the proposed method on three datasets from the Cancer Genome Atlas (TCGA) database, including colon adenocarcinoma (COAD)($N = 365$), hepatocellular carcinoma (LIHC)($N = 334$), and bladder urothelial carcinoma (BLCA)($N = 396$). Each dataset contains WSIs stained with hematoxylin and eosin (H&E) and clinical information of survival time and event status. After segmenting tissue areas by the Otsus method, a set of tiles under different magnifications ($20\times, 10\times, 5\times$) were non-overlappingly sampled from each segmented tissue area, and the window sizes were set to 512×512, 256×256, and 128×128, respectively.

4.2 Implementation Details

In our experiments, we adopted the 5-fold cross-validation strategy to comprehensively evaluate our proposed method and the ratio of training and validation sets was set to 4:1. Specifically, we divided the entire dataset into five folds, among which four folds for model training and fine-tuning while the remaining one for model evaluation. Notably, the cross-validation strategy was conducted on patient level to prevent data leakage, which means that the WSI of each patient only appears in one of these subsets. During training stage, we selected the best model in terms of two specific evaluation metrics for different curriculums. That is, the model with the highest accuracy was selected for Curriculum I, while the model with the highest C-index for Curriculum II. The concordance index (CI), the receiver operating characteristic (ROC) curve, the area under the ROC curve (AUC), and Kaplan-Meier (KM) curve were used to assess the performance of model. We chose three-year time as threshold for risk stratification status and AUC calculation, which lies on two reasons as follows: 1) Three-year survival time is an very important indicator for clinically evaluating the prognosis of patients, especially for these three cancer types studied in our work [45, 46, 47]. 2) For the used

Table 2: The results of ablation experiments on three datasets (i.e., COAD, LIHC, and BLCA). And the boldface denotes the best result.

DC_MIL: C-I + C-II				COAD		LIHC		BLCA	
MM	SG	HT	C-II	CI	AUC	CI	AUC	CI	AUC
✗	✗	✗	✓	0.676±0.031	0.696±0.055	0.662±0.021	0.659±0.032	0.640±0.038	0.680±0.046
✓	✗	✓	✓	0.692±0.049	0.705±0.091	0.671±0.045	0.720±0.050	0.647±0.019	0.678±0.037
✓	✓	✗	✓	0.707±0.033	0.714±0.061	0.699±0.019	0.721±0.018	0.654±0.016	0.700±0.043
PT w/o MM			✓	0.642±0.030	0.643±0.022	0.644±0.030	0.640±0.018	0.618±0.013	0.635±0.028
PT w/ MM			✓	0.660±0.017	0.683±0.025	0.662±0.021	0.691±0.036	0.633±0.015	0.639±0.020
C-I	SB	CSA	TCL	CI	AUC	CI	AUC	CI	AUC
✓	✗	✗	✗	0.651±0.020	0.697±0.040	0.653±0.028	0.680±0.022	0.621±0.023	0.630±0.029
✓	✓	✗	✗	0.670±0.034	0.715±0.066	0.673±0.031	0.717±0.063	0.655±0.024	0.668±0.033
✓	✓	✗	✓	0.709±0.025	0.729±0.063	0.693±0.033	0.736±0.029	0.669±0.017	0.696±0.030
✓	✓	✓	✗	0.678±0.031	0.721±0.047	0.680±0.046	0.731±0.044	0.659±0.031	0.680±0.063
✓	✓	✓	✓	**0.717±0.012**	**0.754±0.031**	**0.705±0.015**	**0.745±0.012**	**0.672±0.029**	**0.720±0.039**

[1] C-I, Curriculum I; MM, multi-magnification strategy; SG, saliency-guided method; HT, hierarchical transfer strategy; PT, pre-trained strategy; C-II, Curriculum II; SB, soft-bag learning; CSA, constrained self-attention module; TCL, two-tier contrastive learning.

datasets, using three-year survival time as threshold can make the distribution of positive and negative samples relatively balanced, which is beneficial to network training. We implemented all competing methods using Pytorch1.9 library on Python3.6. All intensive calculations were offloaded to a 12 GB NVIDIA Pascal Titan X GPU.

Curriculum I. We adopted Adam optimizer with the weight decay of 0.2 for network training. For different magnifications $s \in \{1, 2, 3\}$, the learning rate, batch size and epoch number were set to $\{10^{-5}, 3 \times 10^{-6}, 3 \times 10^{-6}\}$, $\{32, 16, 16\}$ and $\{50, 50, 50\}$, respectively. The weight coefficient β_{Ω} was set to 10^{-5}.

Curriculum II. We adopted SGD optimizer with the momentum of 0.9. The learning rate, batch size and epoch number were set to 10^{-4}, 16 and 1000, respectively. The soft-bag size was set to 3 and the weight coefficient β_s was set to 10^{-3}.

4.3 Comparison with State-of-the-Art Methods

We compared our method with other weakly-supervised methods in cancer prognosis analysis, including clustering approaches [43], graph networks [10, 44], and multi-instance learning methods [5, 6]. Table 1 presents the 5-fold cross-validation results (in terms of CI and AUC) of all competing methods. The KM curves as well as p-values are provided in Figure S1. We can observe that the proposed method outperforms others in head-to-head comparisons, achieving overall CI of 0.698 and AUC of 0.74. It may benefit from several potential advantages in DC_MIL: 1) Unlike some methods that leverage the dimension reduction technique [43] or pre-trained model [5, 6, 10, 44], it encodes instances in a weakly-supervised manner so as to reduce label noises and maintain prognosis-related guidance. 2) It utilizes the low-magnification saliency map to guide the encoding of high-magnification instances for exploring fine-grained information across multi-magnification WSIs. 3) It introduces a soft-bag learning method and a constrained self-attention strategy to help reduce intra-bag redundancy in both instance and feature levels, respectively. 4) It equips the Cox loss with two-tier contrastive learning for enhancing intra-bag and inter-bag discrimination. Additionally, it also can be observed that WSISA [43], MesoNet [6], and DeepAttnMISL [5] outperform DeepGraphSurv [44] and Patch-GCN [10], which may owe the selection of discriminant tiles. More results can refer to Appendix.

4.4 Ablation Study

Abaltion on Curriculum I. We validated the efficacy of each crucial component in Curriculum I. From Table 2, we can observe several key points: 1) Compared with pre-trained ResNet-34 (regardless with MM or not), the proposed model shows significant performance improvement, which demonstrates the effectiveness of Curriculum I. 2) The model with MM outperforms the one without MM and gets CI gain of 0.039 and AUC gain of 0.061, which benefits from the utilization of multi-magnification information. 3) The model without SG or FT suffers from performance reduction

Figure 3: Visualization of salient maps output by the proposed method. The first column shows the original WSIs, and the second and third columns exhibit the salient maps under $10\times$ and $20\times$ magnifications, respectively.

(average CI drops of 0.028 and 0.011 and AUC drops of 0.039 and 0.028). It indicates that fine-gained information across multi-scale tiles and hierarchical transfer strategy can help significantly improve the performance of model. More results can refer to Appendix.

Abaltion on Curriculum II. We also validated the efficacy of each key component in Curriculum II. From Table 2, we have the following observations: 1) The baseline method performed prognosis prediction with the Cox model, which achieves average CI of 0.642 and AUC of 0.669. Compared to the baseline method, the model with soft-bag strategy achieves average CI gain of 0.024 and AUC gain of 0.031, which mainly profits by adaptively identifying and integrating the representative instances within a bag. 2) The models with CSA, TCL, and both of them show better performance with average CI gains of 0.006, 0.024, and 0.032 and AUC gains of 0.011, 0.02, and 0.04, respectively, which benefits from the reduction of intra-bag redundancy and the enhancement of intra-bag and inter-bag discrimination. More results can refer to Appendix.

4.5 Visualization

In this section, we show the salient maps output by the proposed method for some samples. As shown in Figure 3, the model mainly focuses on the fine-grained regions (under $20\times$ WSIs) that is wrapped by the salient regions under $10\times$ WSIs, which indicates that the proposed method can effectively guide the encoding of high-magnification instances so as to encourage the network to focus on more fine-grained information. We have provided more intuitive results and analyses in Appendix.

5 Conclusion

In this paper, we propose a dual-curriculum contrastive MIL method for cancer prognosis analysis with WSIs, which contains two easy-to-hard curriculums, i.e., saliency-guided weakly-supervised instance encoding with cross-scale tiles and contrastive-enhanced soft-bag prognosis inference. The proposed network is easy to train in each curriculum, and can be applied to gigapixel WSI analysis with good visualization. Besides, the proposed method outperforms the state-of-the-art methods in cancer prognosis analysis over three public datasets.

References

[1] Ole-Johan Skrede et al. Deep learning for prediction of colorectal cancer outcome: a discovery and validation study. *The Lancet*, 395(10221):350–360, 2020.

[2] Richard Colling et al. Artificial intelligence in digital pathology: a roadmap to routine use in clinical practice. *The Journal of pathology*, 249(2):143–150, 2019.

[3] Chetan L Srinidhi, Ozan Ciga, and Anne L Martel. Deep neural network models for computational histopathology: a survey. *Medical Image Analysis*, 67:101813, 2021.

[4] Jana Lipkova et al. Deep learning-enabled assessment of cardiac allograft rejection from endomyocardial biopsies. *Nature medicine*, 28(3):575–582, 2022.

[5] Jiawen Yao, Xinliang Zhu, Jitendra Jonnagaddala, Nicholas Hawkins, and Junzhou Huang. Whole slide images based cancer survival prediction using attention guided deep multiple instance learning networks. *Medical Image Analysis*, 65:101789, 2020.

[6] Pierre Courtiol et al. Deep learning-based classification of mesothelioma improves prediction of patient outcome. *Nature Medicine*, 25(10):1519–1525, 2019.

[7] Hassan Muhammad et al. Epic-survival: end-to-end part inferred clustering for survival analysis, with prognostic stratification boosting. In *Medical Imaging with Deep Learning*, 2021.

[8] Bin Li, Yin Li, and Kevin W Eliceiri. Dual-stream multiple instance learning network for whole slide image classification with self-supervised contrastive learning. In *in Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 14318–14328, 2021.

[9] Gabriele Campanella et al. Clinical-grade computational pathology using weakly supervised deep learning on whole slide images. *Nature Medicine*, 25(8):1301–1309, 2019.

[10] Richard J Chen et al. Whole slide images are 2d point clouds: context-aware survival prediction using patch-based graph convolutional networks. In *International Conference on Medical Image Computing and Computer-Assisted Intervention*, pages 339–349. Springer, 2021.

[11] Ming Y Lu, Drew FK Williamson, Tiffany Y Chen, Richard J Chen, Matteo Barbieri, and Faisal Mahmood. Data-efficient and weakly supervised computational pathology on whole-slide images. *Nature Biomedical Engineering*, 5(6):555–570, 2021.

[12] Zhuchen Shao et al. Transmil: transformer based correlated multiple instance learning for whole slide image classification. *Advances in Neural Information Processing Systems*, 34, 2021.

[13] Chetan L Srinidhi and Anne L Martel. Improving self-supervised learning with hardness-aware dynamic curriculum learning: An application to digital pathology. In *in Proceedings of the IEEE/CVF International Conference on Computer Vision*, pages 562–571, 2021.

[14] Chetan L Srinidhi, Seung Wook Kim, Fu-Der Chen, and Anne L Martel. Self-supervised driven consistency training for annotation efficient histopathology image analysis. *Medical Image Analysis*, 75:102256, 2022.

[15] Xueting Yan, Ishan Misra, Abhinav Gupta, Deepti Ghadiyaram, and Dhruv Mahajan. Clusterfit: improving generalization of visual representations. In *in Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 6509–6518, 2020.

[16] Noriaki Hashimoto et al. Multi-scale domain-adversarial multiple-instance cnn for cancer subtype classification with unannotated histopathological images. In *in Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 3852–3861, 2020.

[17] Hongrun Zhang et al. Dtfd-mil: double-tier feature distillation multiple instance learning for histopathology whole slide image classification. In *in Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 18802–18812, 2022.

[18] Trung Vu, Phung Lai, Raviv Raich, Anh Pham, Xiaoli Z Fern, and UK Arvind Rao. A novel attribute-based symmetric multiple instance learning for histopathological image analysis. *IEEE Transactions on Medical Imaging*, 39(10):3125–3136, 2020.

[19] Pierre Courtiol, Eric W Tramel, Marc Sanselme, and Gilles Wainrib. Classification and disease localization in histopathology using only global labels: A weakly-supervised approach. *arXiv preprint arXiv:1802.02212*, 2018.

[20] Weixin Li and Nuno Vasconcelos. Multiple instance learning for soft bags via top instances. In *in Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 4277–4285, 2015.

[21] Wei Shao, Tongxin Wang, Zhi Huang, Zhi Han, Jie Zhang, and Kun Huang. Weakly supervised deep ordinal cox model for survival prediction from whole-slide pathological images. *IEEE Transactions on Medical Imaging*, 40(12):3739–3747, 2021.

[22] Nima Hatami, Mohsin Bilal, and Nasir Rajpoot. Deep multi-resolution dictionary learning for histopathology image analysis. *arXiv preprint arXiv:2104.00669*, 2021.

[23] Hiroki Tokunaga, Yuki Teramoto, Akihiko Yoshizawa, and Ryoma Bise. Adaptive weighting multi-field-of-view cnn for semantic segmentation in pathology. In *in Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pages 12597–12606, 2019.

[24] Naofumi Tomita, Behnaz Abdollahi, Jason Wei, Bing Ren, Arief Suriawinata, and Saeed Hassanpour. Attention-based deep neural networks for detection of cancerous and precancerous esophagus tissue on histopathological slides. *JAMA Network Open*, 2(11):e1914645–e1914645, 2019.

[25] Nikhil Naik et al. Deep learning-enabled breast cancer hormonal receptor status determination from base-level h&e stains. *Nature Communications*, 11(1):1–8, 2020.

[26] Shujun Wang et al. Rmdl: recalibrated multi-instance deep learning for whole slide gastric image classification. *Medical Image Analysis*, 58:101549, 2019.

[27] Dmitrii Bychkov et al. Deep learning based tissue analysis predicts outcome in colorectal cancer. *Scientific Reports*, 8(1):1–11, 2018.

[28] Richard J Chen et al. Multimodal co-attention transformer for survival prediction in gigapixel whole slide images. In *in Proceedings of the IEEE/CVF International Conference on Computer Vision*, pages 4015–4025, 2021.

[29] Charlie Saillard et al. Predicting survival after hepatocellular carcinoma resection using deep learning on histological slides. *Hepatology*, 72(6):2000–2013, 2020.

[30] Pooya Mobadersany et al. Predicting cancer outcomes from histology and genomics using convolutional networks. *in Proceedings of the National Academy of Sciences*, 115(13):E2970–E2979, 2018.

[31] Richard J Chen et al. Pathomic fusion: an integrated framework for fusing histopathology and genomic features for cancer diagnosis and prognosis. *IEEE Transactions on Medical Imaging*, 2020.

[32] Shuai Jiang, George J Zanazzi, and Saeed Hassanpour. Predicting prognosis and idh mutation status for patients with lower-grade gliomas using whole slide images. *Scientific Reports*, 11(1):1–9, 2021.

[33] David Tellez, Geert Litjens, Jeroen van der Laak, and Francesco Ciompi. Neural image compression for gigapixel histopathology image analysis. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 43(2):567–578, 2019.

[34] Gang Xu et al. Camel: a weakly supervised learning framework for histopathology image segmentation. In *in Proceedings of the IEEE/CVF International Conference on Computer Vision*, pages 10682–10691, 2019.

[35] Fahdi Kanavati et al. Weakly-supervised learning for lung carcinoma classification using deep learning. *Scientific Reports*, 10(1):1–11, 2020.

[36] Chensu Xie et al. Beyond classification: whole slide tissue histopathology analysis by end-to-end part learning. In *Medical Imaging with Deep Learning*, pages 843–856. PMLR, 2020.

[37] Yash Sharma, Aman Shrivastava, Lubaina Ehsan, Christopher A Moskaluk, Sana Syed, and Donald Brown. Cluster-to-conquer: a framework for end-to-end multi-instance learning for whole slide image classification. In *Medical Imaging with Deep Learning*, pages 682–698. PMLR, 2021.

[38] Bolei Zhou, Aditya Khosla, Agata Lapedriza, Aude Oliva, and Antonio Torralba. Learning deep features for discriminative localization. In *in Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pages 2921–2929, 2016.

[39] Ashish Vaswani et al. Attention is all you need. *Advances in Neural Information Processing Systems*, 30, 2017.

[40] Aaron Van den Oord, Yazhe Li, and Oriol Vinyals. Representation learning with contrastive predictive coding. *arXiv e-prints*, pages arXiv–1807, 2018.

[41] Ting Chen, Simon Kornblith, Mohammad Norouzi, and Geoffrey Hinton. A simple framework for contrastive learning of visual representations. In *International Conference on Machine Learning*, pages 1597–1607. PMLR, 2020.

[42] John Fox and Sanford Weisberg. Cox proportional-hazards regression for survival data. *An R and S-PLUS Companion to Applied Regression*, 2002, 2002.

[43] Xinliang Zhu, Jiawen Yao, Feiyun Zhu, and Junzhou Huang. Wsisa: making survival prediction from whole slide histopathological images. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pages 7234–7242, 2017.

[44] Ruoyu Li, Jiawen Yao, Xinliang Zhu, Yeqing Li, and Junzhou Huang. Graph cnn for survival analysis on whole slide pathological images. In *International Conference on Medical Image Computing and Computer-Assisted Intervention*, pages 174–182. Springer, 2018.

[45] Daniel J Sargent et al. Disease-free survival versus overall survival as a primary end point for adjuvant colon cancer studies: individual patient data from 20,898 patients on 18 randomized trials. *Journal of Clinical Oncology*, 23(34):8664–8670, 2005.

[46] Josep M Llovet, Andrew Burroughs, and Jordi Bruix. Hepatocellular carcinoma. *The Lancet*, 362(9399):1907–1917, 2003.

[47] Ashish M Kamat et al. Bladder cancer. *The Lancet*, 388(10061):2796–2810, 2016.