Modular Quantization-Aware Training for 6D Object Pose Estimation

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Paper under double-blind review

Abstract

Edge applications, such as collaborative robotics and spacecraft rendezvous, demand efficient 6D object pose estimation on resource-constrained embedded platforms. Existing 6D object pose estimation networks are often too large for such deployments, necessitating compression while maintaining reliable performance. To address this challenge, we introduce Modular Quantization-Aware Training (MQAT), an adaptive and mixed-precision quantization-aware training strategy that exploits the modular structure of modern 6D object pose estimation architectures. MQAT guides a systematic gradated modular quantization sequence and determines module-specific bit precisions, leading to quantized models that outperform those produced by state-of-the-art uniform and mixed-precision quantization techniques. Our experiments showcase the generality of MQAT across datasets, architectures, and quantization algorithms. Additionally, we observe that MQAT quantized models can achieve an accuracy boost ($>$ 7% ADI-0.1d) over the baseline full-precision network while reducing model size by a factor of 4$\times$ or more.

1 Introduction

Efficient and reliable 6D object pose estimation has emerged as a crucial component in numerous situations, particularly in robotics applications such as automated manufacturing Pérez et al. (2016), vision-based control Singh et al. (2022), collaborative robotics Vicentini (2021) and spacecraft rendezvous Song et al. (2022). However, such applications typically must run on embedded platforms with limited hardware resources.

These resource constraints often disqualify current state-of-the-art methods, such as ZebraPose Su et al. (2022), SO-Pose Di et al. (2021), and GDR-Net Wang et al. (2021), which employ a two stage approach (detection followed by pose estimation) and thus entail a large memory footprint. By contrast, single-stage methods Thalhammer et al. (2021); Peng et al. (2019); Song et al. (2020); Hu et al. (2021b); Wang et al. (2022); Chen et al. (2019); Rad & Lepetit (2017); Hodaň et al. (2020) offer a more pragmatic alternative, yielding models with a good accuracy-footprint tradeoff. Nevertheless, they remain too large for deployment on edge devices.

To address this challenge, CA-SpaceNet Wang et al. (2022) applies a *uniform* quantization approach to reduce the network memory footprint at the expense of a large accuracy loss; all network layers are quantized to the same bit width, except for the first and last layer.

In principle, *mixed-precision* quantization methods Cai & Vasconcelos (2020); Dong et al. (2020); Tang et al. (2022) could demonstrate similar compression with better performance, but they tend to require significant effort and GPU hours to determine the optimal bit precision for each layer. Furthermore, neither mixed-precision nor uniform quantization methods consider the importance of the order in which the network weights or layers are quantized, as searching for the optimal order is combinatorial in the number of, e.g., network layers.

In this work, we depart from such conventional Quantization-Aware Training (QAT) approaches and leverage the inherent modular structure of modern 6D object pose estimation architectures, which typically encompass components such as a backbone, a feature aggregation module, and prediction heads. Specifically, we

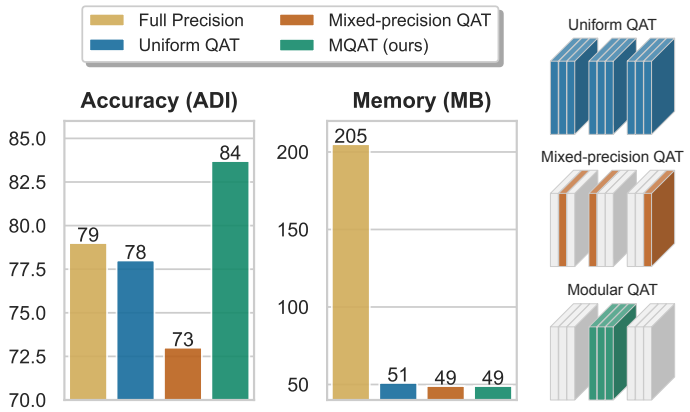

Figure 1: **Summary of this Work.** In contrast to uniform and mixed-precision quantization, MQAT accounts for the modularity of typical 6D object pose estimation frameworks. MQAT not only reduces the memory footprint of the network but can result in an accuracy boost that neither uniform nor mixed-precision quantization have demonstrated.

introduce a Modular Quantization-Aware Training (MQAT) paradigm that relies on a gradated quantization strategy, where the modules are quantized and fine-tuned in a mixed-precision way, following a sequential order based on their sensitivity to quantization. As the number of modules in an architecture is much lower than that of layers, our approach allows us to search for the optimal quantization order.

Our experiments evidence that MQAT is particularly well-suited to 6D object pose estimation, consistently outperforming the state-of-the-art quantization techniques in terms of accuracy for a given memory consumption budget, as shown in fig. 1. We demonstrate the generality of our approach by applying it to different single-stage architectures, WDR Hu et al. (2021b), CA-SpaceNet Wang et al. (2022); different datasets, SwissCube Hu et al. (2021b), Linemod Hinterstoisser et al. (2012), and Occlusion Linemod Brachmann et al. (2014); and using different quantization strategies, INQ Zhou et al. (2017) and LSQ Esser et al. (2020), within our modular strategy. We further show that our method also applies to two-stage networks, such as ZebraPose Su et al. (2022), on which it outperforms both uniform and mixed-precision quantization. Furthermore, we extend MQAT to the task of object detection, further validating its efficacy in the computer vision domain. The results of applying MQAT to object detection are presented in appendix A.2, demonstrating its potential for broader applicability and performance improvement.

To summarize, our main contributions are as follows:

- We develop Modular Quantization-Aware Training (MQAT), a novel adaptive, mixed-precision quantization-aware training method tailored for modular neural network architectures.

- We demonstrate substantial accuracy gains over other quantization-aware training (QAT) methods and even surpass full-precision counterparts in case of single-stage networks Hu et al. (2021b); Wang et al. (2022), while significantly reducing the computational cost and model size, showcasing the effectiveness of MQAT in balancing precision and performance.

- We validate the MQAT method across multiple datasets and neural network architectures, proving its adaptability and effectiveness in different settings and its potential for broad application in the field of 6D object pose estimation.

- We provide comprehensive studies offering insights into the impact of module-specific order and bit precision on network performance. This includes detailed ablation studies that establish the superiority of MQAT over existing QAT methods.

2 Related Work

In this section, we survey recent advances in RGB-based 6D object pose estimation, outlining key architectures and their contributions to the field. We then explore the developments in quantization-aware training (QAT), particularly in relation to modular neural network designs. This review sets the groundwork for our proposed Modular Quantization-Aware Training framework, which is inspired by these advances and addresses their limitations.

2.1 6D Object Pose Estimation

Single-Stage Direct Estimation. PoseCNN Xiang et al. (2018) was one of the first methods to estimate 6D object pose using a deep neural network. The network comprised a backbone feature extractor which fed into three heads: a labeller, a segmenter and a fully-connected head to regress the pose directly. Unfortunately, representing the $SO(3)$ group rotations in a manner suitable for direct regression proved to be challenging. SSD6D Liu et al. (2016); Kehl et al. (2017) instead proposed a discretization of the rotation space to form a classification problem instead of a regression one. URSONet Proença & Gao (2020), and more recently Mobile-URSONet Posso et al. (2022), demonstrated competitive results via a backbone–bottleneck–head structure to estimate the weights of a set of *classification* quaternions corresponding to Euler angle rotations.

Single-Stage with PnP. In general, a better performing strategy consists of training a network to predict 2D-to-3D correspondences instead of the pose. The pose is then obtained via a RANdom SAmple Consensus (RANSAC) / Perspective-n-Point (PnP) 2D–to–3D correspondence fitting process. These methods typically employ a backbone, a feature aggregation module, and one or multiple heads Hu et al. (2021b); Chen et al. (2019); Rad & Lepetit (2017); Wang et al. (2022); Peng et al. (2019); Tekin et al. (2018); Thalhammer et al. (2021); Iwase et al. (2021); Zakharov et al. (2019); Oberweger et al. (2018); Jafari et al. (2018); Hu et al. (2019). Rad & Lepetit (2017); Tekin et al. (2018) estimate these correspondences in a single global fashion, whereas Peng et al. (2019); Jafari et al. (2018); Hu et al. (2019); Zakharov et al. (2019); Oberweger et al. (2018) aggregate multiple local predictions to improve robustness. To improve performance in the presence of large depth variations, a number of works Thalhammer et al. (2021); Hu et al. (2021b); Wang et al. (2022) use an FPN Lin et al. (2016) to exploit features at different scales.

Multi-Stage with PnP. The current state-of-the-art pose estimation frameworks incorporate a pipeline of networks that perform different tasks Su et al. (2022); Di et al. (2021); Wang et al. (2021); Li et al. (2019b); Labbé et al. (2020). In the first stage network, the target is localized and a Region of Interest (RoI) is cropped and forwarded to the second stage network. This isolates the position estimation task from the orientation estimation one and further provides the orientation estimation network with an RoI containing only object features. The second stage orientation estimation network can then more easily fit to the target object. Therefore, these multi-stage frameworks tend to yield more accurate results. However, they also have much larger memory footprints as they may include one object classifier network; one object position/RoI network; and N object pose networks. For hardware-restricted scenarios, a multi-stage framework may thus not be practical. Even for single-stage networks, additional compression is required Blalock et al. (2020).

2.2 Quantization-Aware Training

Neural network quantization reduces the precision of parameters such as weights and activations. Existing techniques fall into two broad categories: Post-training quantization (PTQ) Nagel et al. (2020); Li et al. (2021); Frantar & Alistarh (2022); Zhao et al. (2019); Cai et al. (2020); Nagel et al. (2019) and quantization-aware training (QAT). The latter further divides into uniform QAT Esser et al. (2020); Zhou et al. (2017); Bhalgat et al. (2020); Yamamoto (2021) and mixed-precision QAT Cai & Vasconcelos (2020); Dong et al. (2020); Tang et al. (2022); Dong et al. (2019); Chen et al. (2021); Yao et al. (2020). While PTQ avoids the laborious training step, QAT exploits the training and thus better preserves the model's full-precision accuracy. As accuracy can be critical in robotics applications relying on 6D object pose estimation, we focus on QAT.

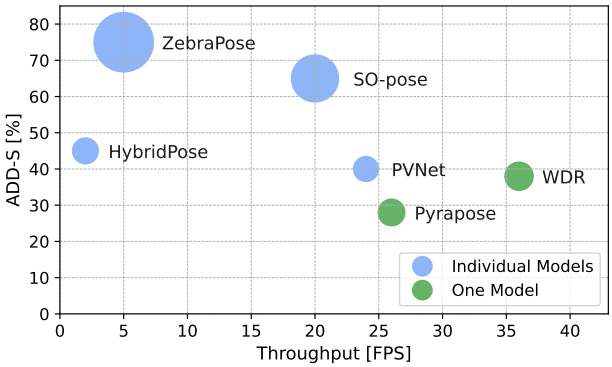

Figure 2: **Performance Comparison on O-LINEMOD.** The marker size is proportional to the memory footprint. *Individual Models* refers to methods training one model for each object. *One Model* refers to methods training a single model for all objects.

Uniform QAT methods quantize every layer of the network to the same precision. In Incremental Network Quantization (INQ) Zhou et al. (2017), this is achieved by quantizing a uniform fraction of each layers' weights at a time and continuing training until the next quantization step. Quantization can be achieved in a structured manner, where entire kernels are quantized at once, or in an unstructured manner. In contrast to INQ, Learned Step-size Quantization (LSQ) Esser et al. (2020) quantizes the entire network in a single action. To this end, LSQ treats the quantization step-size as a learnable parameter. The method then alternates between updating the weights and the step-size parameter.

Mixed-precision QAT methods, conversely, treat each network layer uniquely, aiming to determine the appropriate bit precision for each one. In HAWQ Dong et al. (2019; 2020); Yao et al. (2020), the network weights' Hessian is leveraged to assign bit precisions proportional to the gradients. In Cai & Vasconcelos (2020), the mixed precision is taken even further by applying a different precision to different kernels within a single channel. Mixed-precision QAT is a challenging task; existing methods remain computationally expensive for modern deep network architectures.

2.3 Quantization and Modular Deep Learning

In recent years, deep network architectures have increasingly followed a modular paradigm, owing to its advantages in model design and training efficiency Jacobs et al. (1991); Pfeiffer et al. (2023); Ansell et al. (2021); Hu et al. (2021a); Pfeiffer et al. (2020). This approach leverages reusable modules, amplifying the flexibility and adaptability of neural networks and fostering parameter-efficient fine-tuning.

In the quantization domain, several studies have underscored the importance of selecting the appropriate granularity to bolster model generalization Li et al. (2021) and enhance training stability Zhang et al. (2023). To our knowledge, no existing research has advocated a systematic methodology for executing modular quantization-aware training (QAT), let alone studied the impact of quantization order on modular architectures. Furthermore, in the 6D object pose estimation domain, the application of quantization remains limited Wang et al. (2022), with none of the aforementioned quantization techniques addressing the specific task or underlying network architecture. Thus, in this work, we aim to bridge this gap by introducing a comprehensive methodology for modular QAT, tailored but not limited to 6D object pose estimation.

3 Method

In this section, we first describe the general type of network architecture we consider for compact 6D object pose estimation and then introduce our Modular Quantization-Aware Training (MQAT) method.

3.1 Network Architecture

As discussed in section 2, multi-stage networks Su et al. (2022); Di et al. (2021); Wang et al. (2021); Labbé et al. (2020); Li et al. (2019b) tend to induce large memory footprints and large latencies, thus making poor candidates for hardware-restricted applications. This is further evidenced in fig. 2, where we compare a number of 6D object pose estimation architectures' memory footprint, throughput and accuracy on the O-LINEMOD dataset. While demonstrating admirable accuracy, the size and latency of ZebraPose Su et al. (2022) and SO-pose Di et al. (2021) preclude their inclusion in hardware-restricted platforms.

On this basis, we therefore focus on single-stage[1] 6D object pose estimation networks Thalhammer et al. (2021); Wang et al. (2022); Tekin et al. (2018); Peng et al. (2019); Hu et al. (2021b). In general, such networks consist of multiple modules, exhibiting an encoder-decoder structure followed by prediction heads. Examples include PyraPose Thalhammer et al. (2021), WDRHu et al. (2021b), and CA-SpaceNet Wang et al. (2022); a representative generic architecture is illustrated in fig. 3.

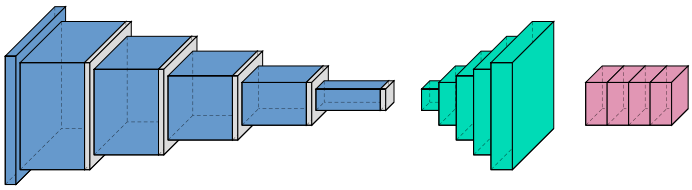

Figure 3: **Representative 6D Object Pose Estimation Network** with $K = 3$ modules. From left to right, we denote them as *backbone*, *feature aggregation*, and *heads*.

3.2 MQAT Overview

Conventional Quantization Aware Training (QAT) methods Esser et al. (2020); Zhou et al. (2017); Bhalgat et al. (2020); Yamamoto (2021) approaches uniformly apply quantization across network layers, efficiently reducing memory usage but often impairing performance, particularly with aggressive techniques like ternary weights {-1,0,1}. In contrast, our Modular Quantization Aware Training (MQAT) method leverages the inherent modular architecture of 6D object pose estimation networks, allowing for differentiated quantization strategies across modules to minimize performance degradation.

MQAT starts with the aggressive quantization (i.e ternary weights) of individual modules using established QAT methods (e.g., INQ Zhou et al. (2017), LSQ Esser et al. (2020)), this process is repeated for all K modules, where only the kth module is quantized while the remaining $K-1$ modules retain full precision. The quantization of only a selected module B_k provides flexibility for the other $K-1$ full precision modules to compensate for any accuracy loss; in some cases accuracy may even improves as will be shown in section 4.

Given the aggressive quantization sensitivity results for each individual module, B_k, we define an optimal quantization order — termed the *quantization flow*. We then sequentially quantize the modules in the optimal order, with the optimal bit precision, determined using constrained optimization. The resulting MQAT strategy is provided in algorithm 1 and described in more detail below. The results of MQAT in conjunction with LSQ and INQ will be demonstrated in section 4. Note that any traditional QAT algorithm can be applied as the quantization method Q, in lieu of INQ or LSQ.

3.3 Algorithmic Details

We introduce MQAT algorithm in algorithm 1 where we also defined the notations. We begin by introducing the critical components for our approach.

Quantization Flow (*Lines 1:15*). For a modular network with K modules, we conduct K independent 2 bit quantizations for each module. A module B_k^q (B_k quantized to bit-precision q) is retained if it results

[1]For completeness, we also demonstrate that our quantization approach applies to two-stage networks (e.g., ZebraPose).

Algorithm 1 MQAT Algorithm

Input: Training data, Quantization Q, Model M with modules $\mathbf{B} = [B_1, B_2, ..., B_K]$, Bit-width search $q = [2, 4, 8...]$, Accuracy metric $ac(M)$

1: **for** $k = 1, 2, ..K$ **do**
2: $\quad M_k^2 \leftarrow Q_k^2(M)$
3: $\quad$ **if** $ac(M_k^2) > ac(M) \wedge ac(M_k^2) > ac(M_{best})$ **then**
4: $\quad\quad M_{best} \leftarrow M_k^2$
5: $\quad\quad k_{best} \leftarrow k$
6: $\quad$ **end if**
7: **end for**
8: $flow = [\,]$
9: **if** M_{best} **then**
10: $\quad M \leftarrow M_{best}$
11: $\quad flow \leftarrow index(SORT_SIZE(\mathbf{B}))$
12: $\quad flow.pop(k_{best})$
13: **else**
14: $\quad flow \leftarrow index(SORT_SIZE(\mathbf{B}))$
15: **end if**
16: $\rho \leftarrow ILP(M, q)$
17: $i \leftarrow 0$
18: **while** $i < len(flow)$ **do**
19: $\quad M^Q \leftarrow Q_{flow(i)}^{\rho(i)}(M)$
20: $\quad$ retrain(M^Q)
21: **end while**

Output: Modular quantized model (M^Q).

Variables:

$flow$	Sequence of quantization order of modules.
k_{best}	Index of the quantized module which increased performance.
K	Number of modules.
M_{best}	Highest accuracy model containing a quantized module.
M_k^q	Model with only module k quantized to q bits.
M^Q	Model with modules quantized to different bit precisions.
ρ	List of bit precisions for each module.
Q_c^j	Quantization applied to module B_c with j-bits.

in an improved accuracy for M_k^q (Model with only B_k quantized to bit-precision q), providing a baseline for the appropriate bit precision optimization. The sequence of module quantization is critical since quantizing the modules of a network is not commutative; we prioritize starting with modules that do not compromise accuracy, as errors introduced early on are typically not mitigated by later steps. Moreover, we also observe that quantization-related noise can lead to weight instability Défossez et al. (2021); Shin et al. (2023); Peters et al. (2023), hindering the performance of the quantized network.

If no quantized module yields an improved accuracy, we proceed with quantizing the module with the lowest number of parameters first; the modules with higher parameter numbers will have more flexibility to adapt to aggressive quantization. The resulting optimal *quantization flow* is then passed to the next algorithmic step.

Optimal Bit Precision (*Lines 16:21*). In MQAT, the optimal bit precision for each module (except k_{best}) is ascertained through a process of constrained optimization, *Integer Linear Programming* (ILP), drawing inspiration from Yao et al. (2020). However, our methodology distinguishes itself by offering a lower degree of granularity. Central to our strategy is the uniform quantization of all layers within a given module to an identical bit-width. This design choice not only simplifies the computational complexity but also significantly enhances the hardware compatibility of the system, an essential consideration for efficient real-world deployment.

To achieve this, we introduce the *importance metric* for modular quantization. This metric is conceptualized as the product of two factors: the sensitivity metric, λ, for each layer in a module which is computed by a similar approach to that in Dong et al. (2020), and the quantization weight error. The latter is calculated as the squared 2-norm difference between the quantized and full precision weights. Therefore, the importance metric is given by

$$\Omega_k = \frac{1}{L_k} \sum_{i=1}^{L_k} \frac{\lambda_i}{N_i} \left| Q\left(W_i\right) - W_i \right|_2^2, \tag{1}$$

with

k the k-th module in the modular network;

i the i-th layer within module k;

L_k the total number of layers in module k;

N_i the number of parameters in the i-th layer of module k;

λ_i the sensitivity of the i-th layer in module k;

Q the quantization operation;

W_i the weights of the i-th layer in module k.

Finding optimal bit precisions using ILP is formulated as

$$\begin{aligned} &\min_{\{\rho_k\}_{k=1}^{K}} \sum_{k=1}^{K} \Omega_k^{(\rho_k)}, \\ &\text{subject to} \quad \sum_{k=1}^{K} S_k^{(\rho_k)} \leq \frac{\text{Full Precision Model Size}}{\text{Compression factor}} \ . \end{aligned} \tag{2}$$

In this formulation, ρ_k denotes the bit-width for the kth module; S_k denotes the model size of module k; and K represents the total number of layers.

4 Experiments

Historically, quantization and other compression methods have been used to exercise a trade-off between inference accuracy and deployment feasibility, particularly in resource-constrained circumstances. In the following sections, we will show that our approach may yield a significant inference accuracy improvement during compression.

We first introduce the datasets and metrics used for evaluation. Then, we present ablation studies to explore the properties of MQAT; this result is directly compared to uniform and mixed QAT methods. Finally, we demonstrate the generality of our method applied to different datasets, architectures, and QAT methods.

4.1 Datasets and Metrics

The LINEMOD and O-LINEMOD datasets are standard benchmarks for evaluating 6D object pose estimation methods, where the LINEMOD dataset contains 13 different sequences consisting of ground-truth poses for a single object. Similar to GDR-Net Wang et al. (2021), we utilize 15% of the images for training. O-LINEMOD extends LINEMOD by including occlusions. For both datasets, additional rendered images are used during training Wang et al. (2021); Peng et al. (2019). Similarly to previous works, we use the ADD and ADI error metrics Hodaň et al. (2016) expressed as

$$e_{ADD}(P^{est}, P^{gt}) = \frac{1}{V} \sum_{i=1}^{V} \| P_i^{est} - P_i^{gt} \|_2 \ , \tag{3}$$

$$e_{ADI}(P^{est}, P^{gt}) = \frac{1}{V} \sum_{i=1}^{V} \min_{j \in [1,V]} \| P_i^{est} - P_j^{gt} \|_2 \ , \tag{4}$$

where P_i^{est} and P_i^{gt} denote the ith vertex of the 3D mesh after transformation with the predicted and ground-truth pose, respectively. We then report the accuracy using the *ADD-0.1d* and *ADD-0.5d* metrics, which encode the proportion of samples for which e_{ADD} is less than 10% and 50% of the object diameter.

While LINEMOD and O-LINEMOD present their own set of challenges, their scope is restricted to household objects, consistently illuminated without significant depth variations. Conversely, the SwissCube dataset Hu et al. (2021b) embodies a challenging scenario for 6D object pose estimation in space, incorporating large scale variations, diverse lighting conditions, and variable backgrounds. To remain consistent with previous works, we use the same training setup and metric as Wang et al. (2022).

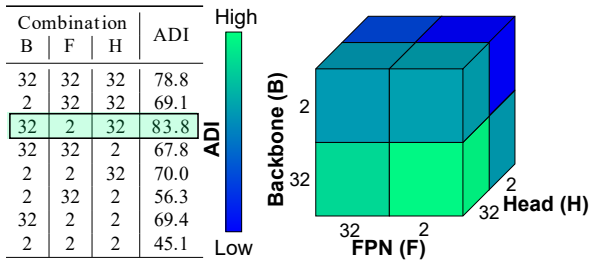

Figure 4: **Aggressive Quantization for Order Optimality.** This corresponds to line 1-7 in Algo.1.

Table 1: Effect of Starting MQAT with Different Modules.

MQAT First Quantized Module	**ADI** 0.1d	0.5d
Full Precision	78.79	98.98
Backbone	69.08	96.79
Head	67.84	98.12
Feature Pyramid Network (FPN)	**83.8**	**99.4**

4.2 Implementation Details

We use PyTorch to implement our method. For the retraining of our partially quantized pretrained network, we employ an SGD optimizer with a base learning rate of `1e-2`. For all experiments, we use a batch size of 8, train for 30 epochs, and employ a hand-crafted learning scheduler which decreases the learning rate at regular intervals by a factor of 10 and increases it again when we quantize a module with INQ[2]. However, when we quantize our modules using LSQ, the learning rate factor is not increased, only decreased by factors of 10. We use a 512×512 resolution input for the SwissCube dataset and 640×480 for LINEMOD and O-LINEMOD as in Peng et al. (2019).

4.3 MQAT Paradigm Studies

In this section, we conduct comprehensive studies using SwissCube and demonstrate the superior performance of our approach over conventional QAT ones.

4.3.1 MQAT Order.

We first perform an ablation study to validate the optimal order for quantizing the network modules. As discussed in section 3.3, the module quantization order is not commutative. Using WDR, we perform aggressive quantization to every combination of modules in the network. This is an $O(2^K)$ search; this results in eight module quantization combinations for a network with $K = 3$ modules. The results are visualized in fig. 4. The backbone and head modules exhibit greater sensitivity to aggressive quantization. Conversely, the accuracy of the network is enhanced when using 2 bit quantization on the Feature Pyramid Network (FPN) module only. No other combination of module quantizations yields an accuracy increase. This further emphasizes the importance of carefully selecting a module quantization flow.

We additionally perform ablation studies on the optimal order (i.e., flow) of module quantization. We begin by quantizing different modules first, instead of the FPN. table 1 shows the results of both the head and backbone modules when they are the first module quantized. We observe that the inference accuracy decreases dramatically for both cases. No combination of module flow or bit precision schedule is able to recover the inference accuracy after it was lost. The 2 bit aggressive FPN quantization yields improved accuracy only when the FPN is quantized first.

4.3.2 Quantized FPN Sensitivity Study.

To expand upon the 2 bit FPN accuracy enhancement, we perform a higher granularity bit-precision search on the FPN module. Again, the FPN module was quantized, but to five different bit-widths for comparison; the results are presented in fig. 5. The accuracy of two full-precision networks, WDR Hu et al. (2021b) and CA-SpaceNet Wang et al. (2022), are shown with dashed lines. The highest accuracy is achieved with a 2 bit

[2]The learning rate and quantization schedulers are provided in the appendix.

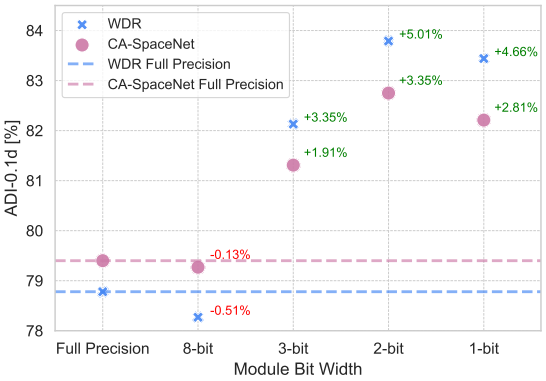

Figure 5: **Ablation study on the FPN bit-width**. We compare the performance by varying the bit-width of the feature aggregation module in each model.

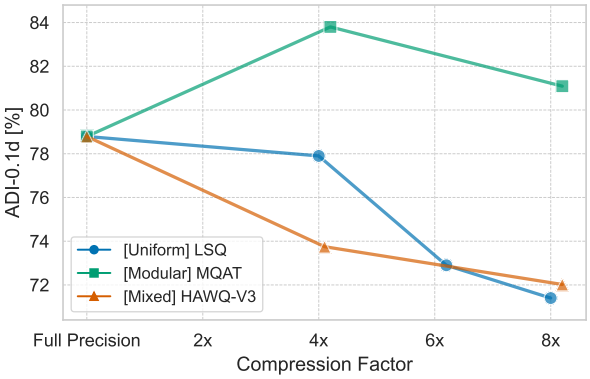

Figure 6: Comparison between our proposed paradigm MQAT, uniform QAT (LSQ), and layer-wise mixed-precision QAT (HAWQ-V3).

or ternary $\{-1, 0, 1\}$ FPN. Further pushing the FPN to binary weights $\{-1, 1\}$ slightly reduces the accuracy, but maintains a significant improvement over both baselines[3].

In the context of our study, as depicted in fig. 5, our findings support the premise that varying bit-precisions across different modules within QAT, such as the FPN, can significantly influence overall performance. This can be attributed to a redistribution of computes or inherent regularization effects on the modules. The improvements in performance reinforce the potential of MQAT in enhancing model generalizability.

4.3.3 MQAT Compared to Uniform and Mixed QAT.

For direct comparison, we apply three different quantization paradigms. Starting from a full precision WDR network, we apply a uniform QAT method, LSQ Esser et al. (2020), a mixed-precision QAT method, HAWQ-V3 Yao et al. (2020), and finally our proposed MQAT method with increasing compression factors. The results are provided in fig. 6. Again, MQAT demonstrates a significant accuracy improvement comparing to other methods while sustaining the requested compression factor; it is the only quantization approach to show an increase in inference accuracy during compression.

4.4 MQAT Generality

Finally, we demonstrate the generality of MQAT to different datasets, QAT methods, and network architectures.

Table 2: **Quantized FPN in WDR network on different datasets.** Following common practice, we report ADI for Swisscube and ADD for LINEMOD / O-LINEMOD, for MQAT methods, we use the quantization flow F→H→B.

MQAT Mode	Bit-Precisions	SwissCube		LINEMOD		O-LINEMOD	
		0.1d	0.5d	0.1d	0.5d	0.1d	0.5d
Full precision	Full precision	78.8	98.9	56.1	99.1	37.8	85.2
MQAT_{LSQ}	8-2-8	83.4	99.3	63.5	99.2	39.8	86.4
MQAT_{INQ}	8-2-8	**83.7**	**99.4**	**63.9**	**99.5**	**40.2**	**86.7**

[3]For the interested reader, the FPN layer-wise ADI-0.1d accuracies are provided in the appendix.

Table 3: **Comparison with the state-of-the-art on SwissCube.** We report ADI-0.1d scores for three different depth ranges. A * indicates applying MQAT with 2-bit precision FPN to the model.

Network	Near	Medium	Far	All
SegDriven-Z Hu et al. (2019)	41.1	22.9	7.1	21.8
DLR Chen et al. (2019)	52.6	45.4	29.4	43.2
CA-SpaceNet	91.0	86.3	61.7	79.4
CA-SpaceNet*	95.5	90.7	66.2	82.7
WDR	92.4	84.2	61.3	78.8
WDR*	**96.1**	**91.5**	**68.2**	**83.8**

Table 4: **CA-SpaceNet Published Quantization vs MQAT.** We report ADI scores on the SwissCube dataset sorted by the compression factor of the network, for MQAT methods, we use quantization flow F→H→B.

Quantization Method	ADI-0.1d	Compression	Bit-Precisions (B-F-H)
LSQ	79.4	1×	32-32-32
LSQ B	76.2	2.2×	8-32-32
LSQ BF	75.0	3.2×	8-8-32
LSQ BFH	74.7	4.0×	8-8-8
MQAT (Ours)	**82.7**	4.7×	8-2-8
LSQ B	75.1	2.9×	3-32-32
LSQ BF	74.5	5.9×	3-3-32
MQAT (Ours)	**80.2**	8.2×	4-2-4
LSQ BFH	68.7	10.6×	3-3-3

4.4.1 Dataset and QAT Generality

As discussed in section 4.1, the image domains of LINEMOD, O-LINEMOD and SwissCube are vastly different. The full precision and MQAT quantized models results for all three datasets are shown in table 2. MQAT demonstrates an accuracy improvement in all datasets. We use the ADI metric for evaluation on the SwissCube dataset as in Hu et al. (2021b); Wang et al. (2022), while we use the ADD metric for LINEMOD and O-LINEMOD as used by Wang et al. (2021); Su et al. (2022); Thalhammer et al. (2021); Labbé et al. (2020); Peng et al. (2019).

Accuracy improvements of 5.0%, 7.8% and 2.4% are demonstrated on SwissCube, LINEMOD and O-LINEMOD, respectively, when MQAT with INQ is utilized. Replacing INQ with LSQ yields accuracy improvements of 4.6%, 7.5% and 2.0%, respectively. This evidences that the performance enhancement is independent of the dataset domain and the applied QAT method.

As discussed in section 3.3 and section 4.3.1, it is difficult to recover accuracy once it is lost during quantization. To this end, since INQ Zhou et al. (2017) quantizes only a fraction of the network at once, it follows that the remaining unquantized portion of the network is left flexible to adapt to aggressive quantization. Conversely, LSQ Esser et al. (2020) quantizes the entire network in a single step; no fraction of the network is left unperturbed. Consequently, INQ demonstrates superior results in table 2. While any QAT method may be used, we recommend partnering MQAT with INQ for optimal aggressive quantization results.

4.4.2 Architecture Generality

In table 3, we compare several single-stage PnP architectures on the SwissCube dataset. To demonstrate the generality of our performance enhancement, we aggressively quantize the FPN of apply MQAT to both CA-SpaceNet Wang et al. (2022) and WDR Hu et al. (2021b). We demonstrate an accuracy improvement of 4.5%, 4.4% and 4.5% for Near, Medium and Far images, respectively, on CA-SpaceNet, resulting in a total testing set accuracy improvement of 3.3%. Recall the already presented total testing set accuracy improvement of 5.0% for WDR. Previously, the full precision CA-SpaceNet had shown a performance improvement over the full precision WDR, but WDR sees greater gains from the application of MQAT.

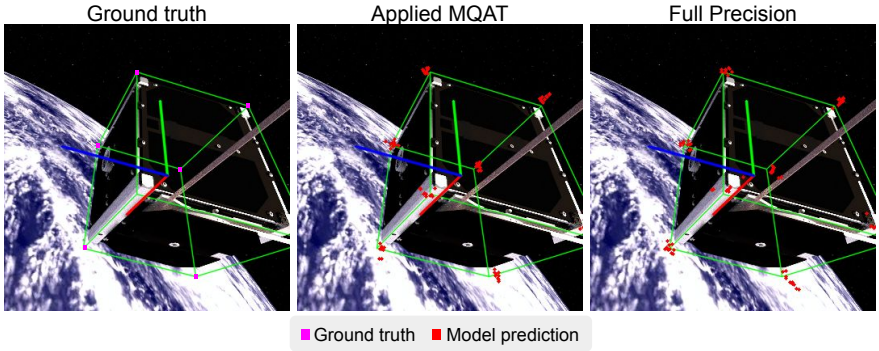

Figure 7: **Visualization of predictions.** Comparison between our proposed MQAT paradigm, and full-precision network. The model applying MQAT yields predictions that are on par with, or more concentrated than its full-precision counterpart.

Table 5: **Quantization of ZebraPose Su et al. (2022).** We report ADI scores on the O-LINEMOD dataset and compare MQAT to mix-precision quantization (HAWQ-V3).

Quantization Method	**ADI 0.1d**	**Compression**	**Bit-Precisions**	**Quantization Flow**
Full precision	76.90	1×	Full precision	N/A
HAWQ-V3 Yao et al. (2020)	71.11	4×	Mixed (layer-wise)	N/A
HAWQ-V3 Yao et al. (2020)	69.87	4.60×	Mixed (layer-wise)	N/A
MQAT $K = 2$ (ours)	**72.54**	**4.62×**	8-4 (B-D)	D → B

In addition, Wang et al. (2022) published accuracy results for a uniform QAT quantized CA-Space network, shared in table 4. Specifically, CA-SpaceNet explored three quantization modes (B, BF and BFH). These correspond to quantizing the backbone, quantizing the backbone and FPN (paired), and quantizing the whole network (uniformly), respectively.

Finally, we evaluate MQAT on a multi-stage network architecture. Specifically, in Table 5, we demonstrate the performance of our method on the state-of-the-art 6D object pose estimation network, the two-stage ZebraPose network Su et al. (2022). Note that, when quantized using MQAT, the model's performance comes close to that of its full-precision counterpart while being more than four times smaller. Furthermore, MQAT outperforms the state-of-the-art HAWQ-V3 Yao et al. (2020) by ∼2.6%, with the added advantage of further network compression. To further demonstrate the efficacy, we quantize another two stage network i.e GDR-Net with existing uniform and mixed-precision methods, and MQAT. We employed ADD-0.1d metric for 6D object pose evaluation for O-Linemod dataset as Wang et al. (2021). It is evident from table 6 that MQAT outperforms both LSQ Esser et al. (2020) and HAWQv3 Yao et al. (2020) even with slightly more compressed network.

Quantization Method	**ADI 0.1d**	**Compression**	**Bit-Precisions**	**Quantization Flow**
Full precision	56.1	1×	Full precision	N/A
LSQ Esser et al. (2020)	50.7	4.57×	Uniform(7-bit)	N/A
HAWQ-V3 Yao et al. (2020)	50.3	4.9×	Mixed (layer-wise)	N/A
MQAT (ours)	**51.8**	**4.97×**	8-4-4 (B-R-P)	R → P → B

Table 6: **Quantization of GDR-Net Wang et al. (2021).** We report ADI scores on the O-Linemod dataset and compare MQAT to uniform (LSQ) and mix-precision quantization (HAWQ-V3). B, R and P indicates *Backbone*, *Rotation Head* and *PnP-Patch* modules.

As we demonstrated in section 4.3.1, quantizing network modules all together greatly reduces inference accuracy as the smaller unquantized fraction of the network is not able to adapt to the quantization. Additionally, quantizing from backbone to head does not consider the sensitivity of the network modules to quantization. As a final note, CA-SpaceNet does not quantize the first and last layer in any quantization mode. In contrast, MQAT quantizes the entire network.

5 Limitations and Discussion

Module Granularity. As conclusively demonstrated in section 4.3.1, MQAT exploits the modular structure of a network. Therefore, if the network does not contain distinct modules, MQAT simply converges to a uniform QAT methodology. In principle, MQAT can apply to any architectures with $K \geq 2$.

Latency. Directly reporting latency measurements involves hardware deployment, which goes beyond the scope of this work. However, as shown in Yao et al. (2020), latency is directly related to the bit operations per second (BOPs). With lower-precision networks, both the model size and the BOPs are reduced by the same compression factor, which we provide in our experiments. Therefore, it is expected that MQAT would demonstrate a latency improvement proportional to the network compression factor.

Quantization Order Optimality. A major contribution of this paper is the identification of the existance of an asynchronous optimal quantization order. In section 3.3 we recommend a method to obtain a defined quantization order and exhaustively demonstrate its optimality for $K = 3$ in fig. 4. However, the optimality for our method's quantization order has yet to be proven for all combinations of networks and number of modules, K.

6 Conclusion

We have introduced Modular Quantization-Aware Training (MQAT) for networks that exhibit a modular structure, such as 6D object pose estimation architectures. Our approach builds on the intuition that the individual modules of such networks are unique, and thus should be quantized uniquely while heeding an optimal quantization order. Our extensive experiments on different datasets and network architectures, and in conjunction with different quantization methods, conclusively demonstrate that MQAT outperforms uniform and mixed-precision quantization methods at various compression factors. Moreover, we have shown that it can even enhance network performance. In particular, aggressive quantization of the network FPN resulted in 7.8% and 2.4% test set accuracy improvements over the full-precision network on LINEMOD and O-LINEMOD, respectively. In the future, we will investigate the applicability of MQAT to tasks other than 6D object pose estimation.

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A Appendix

A.1 Multi-scale Fusion Analysis of MQAT Applied to WDR Hu et al. (2021b)

In this section we study the inference performance of our MQAT when applied to WDR, our primary focus is to understand the impact of MQAT on the multi-scale fusion inference of WDR, particularly examining changes in performance across individual layers of FPN module in WDR. To this end, we applied MQAT to the WDR architecture and conducted a layer-by-layer performance analysis of FPN module similar to the original WDR paper. The results are presented in Table 7. A notable observation from this analysis is the overall enhancement in performance across most layers and the improvement is consistent across various scales and depth ranges. Particularly, Layer 1 exhibits a significant performance boost, especially for objects classified as *Far*. This layer-specific insight underscores the effectiveness of MQAT in optimizing the WDR network at a granular level.

Layer	Near	Medium	Far	All
1	13.6 (+0.8)	83.8 (+1.0)	55.1 (+6.2)	52.9(+3.0)
2	13.6 (+2.6)	83.8 (+1.3)	55.1 (+0.3)	54.1 (+1.3)
3	16.3 (-0.5)	77.8 (+1.6)	17.1 (-1.2)	37.2 (-0.1)
4	13.0 (+0.7)	0.41 (+0.7)	0 (0)	3.8 (+0.4)

Table 7: **Layer-wise 6D Pose Validation Results with MQAT on WDR's FPN.** ADI-0.1d are reported for each layer. Notable performance enhancements, particularly in Layer 1 for *Far* objects, illustrate the effective quantization of WDR by MQAT.

A.2 Generality of MQAT in Object Detection Problem

In our study, while the primary focus is on 6D pose estimation, where our method's efficacy is already demonstrated, we further extend our evaluation to object detection tasks. This extension is aimed at underscoring the generality of our approach.

To this end, we applied our quantization technique to the Faster R-CNN network, which utilizes a ResNet-50 backbone, a widely recognized model in object detection tasks. Our evaluation was conducted on the comprehensive COCO dataset, a benchmark for object detection.

Network	QAT Method	mAP	Compression
FasterRCNN	Full Precision	37.9	1x
	FQN	32.4	8x
	INQ	33.4	8x
	LSQ	33.8	8x
	MQAT (ours)	**35.1**	**8x**
EfficientDet-D0	Full Precision	33.16	1x
	N2UQ	20.11	10x
	MQAT (ours)	**21.67**	**10x**

Table 8: **Quantization for Object Detection.** We evaluate the given networks on COCO dataset and report mAP.

The results of this experiment are summarized in Table 8. Here, our method, denoted as MQAT, is compared against other quantization approaches: INQ Zhou et al. (2017), LSQ Esser et al. (2020), and the FQN Li et al. (2019a) method, which has been specifically tailored for object detection tasks. The comparison reveals

Figure 8: **Visualization of the Difference in Object Detection Performance** on MSCOCO Lin et al. (2014) between N2UQ and MQAT at the same compression ratio.

that MQAT not only adapts well to a different task domain but also achieves superior performance over these established Quantization-Aware Training techniques. This underlines the adaptability and robustness of our approach, extending its potential applications beyond 6D pose estimation to broader areas within computer vision.

Moreover, we also created a baseline for the network, EfficientDet Tan et al. (2020) by quantizing it with a recent quantization method: Non-Uniform to Uniform Quantization (N2UQ) Liu et al. (2022)). This comparison is crucial to validate the effectiveness of MQAT across various modular architectures and quantization methods. Remarkably, our MQAT approach demonstrated a performance improvement of approximately 1.6% over N2UQ as shown in both Table 8. and fig. 8. This enhancement was observed under comparable compression ratios and identical training durations, further substantiating the superiority of MQAT in terms of efficiency and effectiveness.

A.3 More Results on Speed+ Dataset Park et al. (2021)

A.3.1 Overview of Speed+ Dataset

The Next Generation Spacecraft Pose Estimation Dataset (Speed+) addresses the the domain gap challenge in spacecraft pose estimation. it encompasses 60,000 synthetic images, divided into an 80:20 train-to-validation ratio. The test set comprises of 9,531 Hardware-In-the-Loop images of the half-scale mockup model of the Tango spacecraft.

A.3.2 Results on Speed+ Dataset

Our method was further tested on the Speed+ dataset. The WDR network was quantized with our proposed MQAT and the results are shown in Table 9, where we exclusively assess the model on the validation dataset.

Network	ADI-0.1d
Full precision	96.2
$\text{MQAT}_{(8-2-8)}$	**99.1**

Table 9: **Evaluation of MQAT on Speed+ dataset.**

A.4 More Implementation Details

A.4.1 Training Time

It is common practice for quantization algorithms to start with a pre-trained model Esser et al. (2020); Dong et al. (2019); Zhou et al. (2017). For a comparison of MQAT to other quantization methods, let us consider the training time for WDR. We employed 30 epochs to identify the starting module at 2bits (Alg. 1 Lines 1-7) and then 30 epochs per module (Alg. 1 Lines 18-21), for a total of 120 epochs. Note that vanilla LSQ Esser et al. (2020) employs 90 epochs and vanilla HAWQv3 Yao et al. (2020) also employs 90 epochs (plus preprocessing), but we trained them to 120 epochs for fair comparison.

A.4.2 LR Schedule for INQ Zhou et al. (2017)

As mentioned in our experiments section, we employ a SGD optimizer with a base learning rate (lr_b) of $1e^{-2}$. We trained for 30 epochs with a batch size of 8. We created a hand-crafted learning scheduler which decreases the learning rate at regular intervals by a factor of 10 and increases it again when we quantize a module. The gamma (γ) and quantization fraction scheduler are shown in Table 10. The quantization fraction corresponds to the percentage of weights quantized at each epoch. At each epoch, the learning rate (lr) is computed as:

$$lr = lr_b * \gamma$$

A.4.3 LR Schedule for LSQ Esser et al. (2020) and HAWQ-V3 Yao et al. (2020)

As mentioned in our experiments section, we employ a SGD optimizer with a base learning rate (lr_b) of *1e-2*. However, we used a multi-step decay scheduler here. Learning rate was decreased by factors of 10 at epochs $\{10, 20, 25\}$ of the training. We trained for 30 epochs with a batch size of 8.

A.5 Reproducibility

The source code will be provided publicly along with the details of the environments and dependencies. Moreover, we will provide instructions to reproduce the main results in the manuscript.

Epoch	**Schedule**	
	γ	fraction
0	1	0.2
3	0.1	-
5	1	0.4
7	0.1	-
9	1	0.6
11	0.1	-
13	1	0.8
15	0.1	-
17	1	0.9
19	0.1	-
21	1	0.95
23	0.1	-
25	1	0.975
27	0.1	-
29	1	1
30	0.1	-

Table 10: **Learning Rate Schedule**.