ReaPER: Improving Sample Efficiency in Model-Based Latent Imagination

Abstract

Deep Reinforcement Learning (DRL) can distill behavioural policies from sensory input to solve complex tasks, however, the policies tend to be task-specific and sample inefficient, requiring a large number of interactions with the environment that may be costly or impractical for many real world applications. Model-based DRL (MBRL) can allow learned behaviours and dynamics from one task to be translated to a new task in a related environment, but still suffer from low sample efficiency. In this work we introduce ReaPER, an algorithm that addresses the sample efficiency challenge in model-based DRL, and illustrate the power of the proposed solution on the DeepMind Control benchmark. Our improvements are driven by incorporating sparse, self-supervised, contrastive model representations and efficient use of past experience. We empirically analyze each novel component of ReaPER and analyze how they contribute to overall sample efficiency. We also illustrate how other standard alternatives fail to improve upon previous methods. Code for the plug-and-play tools introduced here will be made available.

1 Introduction

Real world agents are able to efficiently achieve goals in complex, partially-controllable environments even in situations the agent has never experienced before. This capacity can be attributed to a robust model of how the agent's actions affect their surroundings, model that is distilled from past experience, allowing the agent to estimate the effect of their actions in the pursuit of a goal in a novel situation. In practice, learning an explicit world model as in Hafner et al. (2019a); Sekar et al. (2020) is challenging in terms of sample efficiency (number of environment interactions), since the agent needs to simultaneously learn good reward-seeking behaviours and refine a generalizeable model of the environment.

This sample-efficiency challenge has been empirically observed to be more pronounced on agents that act based on sensory input (e.g., raw pixels) instead of proprioception or latent states Lake et al. (2017); Kaiser et al. (2019); Tassa et al. (2018). Since the latter is often inferrable based on raw pixels, this indicates that pixel-based pipelines have room for improvement. This is an important issue since many real-world applications are more naturally solved and articulated in terms of pixels or sensory input.

In this work we investigate several potential sources of sample-inefficiency in model-based reinforcement learning (MBRL) methods, addressing each source separately using simple techniques. We propose ReaPER (**Re**gularized Contr**a**stive Model-Based DRL with **P**rioritized **E**pisodic **R**eplay), an MBRL algorithm built upon Dreamer Hafner et al. (2019a) that addresses the identified sources of sample-inefficiency and improves results over the DMControl suite Tassa et al. (2020). An efficient Pytorch implementation of this code will be made available.

Main Contributions. We introduce ReaPER, an MBRL agent for control tasks in visual environments that outperforms the previous state-of-the-art MBRL agent (Hafner et al. (2019a)) on the DMControl benchmark Tassa et al. (2020). We empirically study key sources of sample inefficiency in MBRL methods, and address each individually using simple approaches, the combination of all successful approaches is integrated onto ReaPER. This provides a self-contained ablation study of the effects of each component of the proposed ReaPER architecture.

We empirically show how ReaPER constructs a coarser but more robust world model, and how the sample efficiency improvement holds throughout model training. Ideas to improve sample efficiency that were ultimately unsuccessful in this setup are also shown and discussed due to their value to improve the understanding of MBRL. Code will be made available.

2 AGENT DESCRIPTION

We model the environment as a partially observable Markov decision process (POMDP) with discrete time steps $t \in [1 : T]$, high-dimensional observations and rewards produced by the environment $o_t, r_t \sim p(o_t, r_t \mid o_{1:t-1}, r_{1:t-1}, a_{1:t})$, and real-valued actions selected by the agent $a_t \sim p(a_t \mid o_{1:t}, r_{1:t}, a_{1:t-1})$. The goal of the agent is to maximize the expected discounted reward $E_p(\sum_{t=1}^{\infty} \gamma^{t-1} r_t)$, with discount factor $\gamma \in (0, 1]$.

We introduce **Re**gularized Cont**r**astive Model Based DRL with **P**rioritized **E**pisodic **R**eplay (ReaPER), a latent dynamics arquitecture extending the work of Dreamer Hafner et al. (2019a), with the following key components, which will be detailed and exploited in the coming sections:

$$
\begin{aligned}
\text{Sequence Augmentation} \quad & \{o_t^q, o_t^k\}_{t=T}^{T+L} = \mathcal{SA}(\{o_t\}_{t=T}^{T+L}), \\
\text{Image encoders} \quad & h_t^k = f_\theta(o_t^k),\ h_t^q = f_{\theta'}(o_t^q), \\
\text{Representation} \quad & p_\theta(s_t \mid s_{t-1}, a_{t-1}, h_t^q), \\
\text{Transition} \quad & q_\theta(s_t \mid s_{t-1}, a_{t-1}), \\
\text{Image Decoder} \quad & q_\theta(o_t^q \mid s_t), \\
\text{Reward predictor} \quad & q_\theta(r_t \mid s_t), \\
\text{Policy} \quad & \pi_\phi(a_t \mid s_t), \\
\text{Value} \quad & v_\psi(s_t).
\end{aligned}
\tag{1}
$$

We use the letters p, q to denote true and estimated distributions respectively. To interact with the environment, observations o_t are perturbed and then passed through the image encoder $h_t = f_\theta(o_t)$, the current model state is sampled from the representation $p_\theta(s_t \mid s_{t-1}, a_{t-1}, h_t)$, and the action is selected from policy $a_t \sim \pi_\phi(a_t \mid s_t)$. The full algorithm is presented next, an explanation of each component and the reasoning behind its inclusion is provided in the following sections.

2.1 MODEL LEARNING

The model is trained on batches of sequential, observable past experience $\{\{(o_t, r_t, a_t)\}_t^{t+L}\}_{b=1}^B$, where t indicates time from start of episode, L is sequence length, b is a batch indicator, and B is the total number of batches. The model's parameters, denoted by θ, are trained on a variety of complimentary objectives, some of these objectives are computed independently for each time sequence (i.e., one per batch element), while others include comparisons against elements in different batches. To simplify the notation, we denote each model loss by a super-index t or t, b to indicate if these losses are computed across time or across time and batch respectively. The losses are described next.

Reconstruction loss. We follow the derivation in Hafner et al. (2019a) to increase the variational lower bound of the model (ELBO, Jordan et al. (1999)). The resulting reconstruction loss is

$$
\begin{aligned}
& \mathcal{L}_O^t = \ln q_\theta(o_t \mid s_t),\ \mathcal{L}_R^t = \ln q_\theta(r_t \mid s_t), \\
& \mathcal{L}_{KL}^t = -\text{KL}(p_\theta(s_t \mid s_{t-1}, a_{t-1}, h_t) \,\|\, q_\theta(s_t \mid s_{t-1}, a_{t-1})), \\
& \mathcal{L}_{REC}^t = \mathcal{L}_O^t + \mathcal{L}_R^t + \mathcal{L}_{KL}^t.
\end{aligned}
\tag{2}
$$

The reconstruction loss $\mathcal{L}_{REC}$ is intuitively interpretable, the state s_t needs to encode sufficient information about the environment to reconstruct the current observation and reward o_t, r_t ($\mathcal{L}_O^t, \mathcal{L}_R^t$), it also needs to be compact enough to be *predictable* given the past state and action ($\mathcal{L}_{KL}^t$). The state then should capture the minimum amount of information of the past trajectory needed to reconstruct current and future observations and rewards.

State-space compression. The state-space representation of the model may attempt to capture irrelevant or non-generalizeable details of the environment. These details may still be consistent

---

Algorithm 1 ReaPER

Require: Hyper-parameters: Seed Episodes S, Collect interval C, Batch size B, Sequence length L,
  Imagination horizon H, learning rate lr, Contrastive and Sparsity bonuses $\lambda_C, \lambda_{\ell_1}$, Contrastive
  momentum α
  Initialize Priority Episodic replay buffer D with S random episodes
  Initialize network parameters θ, ϕ, ψ
  while *training* **do**
    for step $= 1, \ldots, C$ **do**
          Model Learning
      Draw B sequential samples $\{(o_t, r_t, a_t)\}_t^{t+L} \sim D$
      Do sequence-consistent contrastive image augmentation $\{(o_t^k, o_t^q)\}_t^{t+L} = \mathcal{SA}(\{o_t\}_t^{t+L})$
      Compute model states $s_t \sim p(s_t \mid o_t^q, a_{t-1}, s_{t-1})$
      Compute model component $\mathcal{L}_{REC}, \mathcal{L}_{\ell_1}, \mathcal{L}_C$ as in equations 2,3,4.
      Compute model loss $\mathcal{L}_M = \mathcal{L}_{REC} + \lambda_{\ell_1} \mathcal{L}_{\ell_1} + \lambda_C \mathcal{L}_C$
      Update buffer sample priorities according to $\mathcal{L}_M$
      Update model parameters on model loss $\theta \leftarrow \theta - lr\nabla_\theta(\mathcal{L}_M)$
      Update key encoder parameters $\theta' \leftarrow \alpha\theta' + (1 - \alpha)\theta$
          Policy Learning
      Imagine latent trajectories $\{(s_\tau, a_\tau)\}_{\tau=t}^{t+H}$ for each state s_t
      Compute value targets $V_\lambda(s_\tau)$ as in Eq 8
      Compute policy and value losses $\mathcal{L}_\pi; \mathcal{L}_V$ as in Eq 7
      Update $\phi \leftarrow \phi - lr\nabla_\phi(\mathcal{L}_\pi); \ \psi \leftarrow \psi - lr\nabla_\psi(\mathcal{L}_V);$
    end for
          Data Collection
    $o_1 \leftarrow$ env.reset()
    for $t = 1, \ldots, T$ **do**
      Sample $s_t, a_t \sim p_\theta(s_t \mid o_t, a_{t-1}, s_{t-1})\pi_\phi(a_t \mid s_t)$
      Add exploration noise $a_t \leftarrow$ clamp$(a_t + \epsilon z_t; -1, 1), \ z_t \sim \mathcal{N}(0, 1)$
      Observe $o_t, r_t \leftarrow$ env.step(a_t)
    end for
    Add to buffer $D \leftarrow D \oplus \{(o_t, a_t, r_t)\}_{t=1}^T$
  end while

---

across the training dataset, and thus are not eliminated by the state prediction loss $\mathcal{L}_{KL}^t$. We therefore add a sparsity prior to the model state to alleviate this issue,

$$\mathcal{L}_{\ell_1}^t = ||s_t||_1^1; \ \mathcal{L}_{\ell_1} = \mathbb{E}_p[\sum_t \mathcal{L}_{\ell_1}^t]. \tag{3}$$

This prior is directly applied to the state-space representations, and not to the model weights as in standard ℓ_1 regularization.

Robustness to visual perturbations. Contrastive learning has proven an effective technique to learn robust representations from visual input Oord et al. (2018); He et al. (2020); Chen et al. (2020a,b); Srinivas et al. (2020). We follow Srinivas et al. (2020), where a batch of sequential observations $\{\{o_t\}_t^{t+L}\}_{b=1}^B$ drawn from the dataset are augmented independently into query and key observations $\{\{(o_t^q, o_t^k)\}_t^{t+L}\}_{b=1}^B$ (denoted by the superscript q[1] and k respectively), these augmented pairs are fed through their corresponding encoders $f_\theta(\cdot), f_{\theta'}(\cdot)$ to produce paired encodings $\{\{(h_t^q, h_t^k)\}_t^{t+L}\}_{b=1}^B$. The objective of the contrastive loss is to match the encoded query $h_{t,b}^q$ (where we index the query both by time and sequence indicator) to its corresponding encoded key through a bilinear log-loss classifier,

$$\mathcal{L}_C^{t,b} = \log \frac{\exp\left((h_{t,b}^q)^T W h_{t,b}^k\right)}{\sum_{t',b'} \exp\left((h_{t,b}^q)^T W h_{t',b'}^k\right)}. \tag{4}$$

Here $W \in \mathbb{R}^{H \times H}$ is a learned bi-linear matrix, $(\cdot)^T$ denotes transposition, and key parameters θ' are updated via exponential moving average $\theta' \leftarrow \alpha\theta' + (1-\alpha)\theta$.

The augmentations used to generate the key-query pairs define the invariance class we induce into our image encodings. Since ReaPER is a model-based architecture that predicts future states based on current model state, it is imperative for these augmentations to be temporally consistent, otherwise the augmentation procedure is in direct conflict to the observation reconstruction loss $\mathcal{L}_O^t$ and the prediction loss $\mathcal{L}_{KL}^t$, since it introduces an unpredictable perturbation in successive observations that makes pixel-wise prediction impossible. We follow Srinivas et al. (2020) and chose time-consistent random cropping as our augmentation class, where all observations of the same sequence are cropped using the same mask. Randomized temporally-consistent cropping has the added benefit of having a low computational budget, since it can be computed as a tensorized view of the observation matrix, and requires no extra post-processing. An example is shown on Figure 1.

Figure 1: Random crop augmentation. Top row shows original observations from a single episode on the walker run environment, middle and bottom row show corresponding key and query observations. Note that the crop is consistent across time on both key and query. Original image is 80×80, cropped images are 64×64.

---

[1]To be consistent with the literature, q is used both for the estimated distributions and for the query, the context making the distinction clear.

Per-sample model loss. The resulting per-sample model loss is a linear combination of the previous objectives,

$$\mathcal{L}_M^{t,b} = \mathcal{L}_{REC}^{t,b} + \lambda_{\ell_1} \mathcal{L}_{\ell_1}^{t,b} + \lambda_C \mathcal{L}_C^{t,b}. \tag{5}$$

Since this model loss contains both a state sparsity term and a contrastive robustness term, we expect the model to produce coarser and more robust reconstructions of its environment, this simplified and robust reconstruction yields faster policy improvement than the baseline, improving sample efficienct. Figure 2 shows a comparison between Dreamer and ReaPER reconstructions on 4 environments.

(a) Dreamer   (b) ReaPER

Figure 2: Comparison of observation versus reconstructed observation in Dreamer vs ReaPER for the walker run, hopper hop, finger spin, and cartpole two poles environments. ReaPER builds coarse and robust reconstructions compared to Dreamer, where irrelevant background details are blurred but important elements in the environment are well modeled.

2.2 PRIORITIZED EPISODIC REPLAY

Prioritized experience replay Schaul et al. (2015) has been extensively used in off-policy, model-free learning (Schaul et al. (2015); Wang et al. (2016); Hessel et al. (2017)), as a way to enable the learning agent to focus on high error samples from the replay buffer, and thus converge faster to a good quality agent. We extend this notion to episodic (temporally-sequential) sampling, where a sequence $\{(o_t, a_t, r_t)\}_{t=t_0}^{t_0+L}$ is sampled from the buffer with probability

$$p_{t_0} \propto \sum_{t=t_0}^{t_0+L} \mathcal{L}_M^t. \tag{6}$$

Standard prioritized replay utilizes a sum-tree for efficient sampling. We extend this algorithm to temporally-sequential sampling via a tuple-valued sum-tree, where each leaf in the tree (sample) contains both its own sample loss $\mathcal{L}_M^t$ and the episodic sample loss ($\sum_{t'=t}^{t+L} \mathcal{L}_M^{t'}$); whenever a sample is fed through the model, we register δ_t, the change in the sample loss, and add this sample to an update queue. Before sampling from the prioritized replay buffer, all samples in the update queue update their own $\mathcal{L}_M^t$ value and the cumulative $\sum_{t'=\tau}^{\tau+L} \mathcal{L}_M^{t'}$ values of all leaves up to distance M with change δ_t, the non-leaf nodes are then updated based on the cumulative loss as usual. This update is computationally efficient and only introduces a small $\mathcal{O}(L)$ linear overhead w.r.t the standard sum-tree algorithm. To our understanding, this is the first application of prioritized replay in MBRL.

2.3 POLICY LEARNING

Imagined trajectories. The latent dynamic components $q_\theta(s_t \mid s_{t-1}, a_{t-1}), q_\theta(r_t \mid s_t)$ define a fully observable Markov decision process (MDP, Sutton & Barto (2018)); we denote the time indices drawn from these imaginary trajectories by τ. Imaginary trajectories start at true model states s_t and then follow the MDP defined below, the policy and value functions are trained jointly on imagined trajectories on the objectives

$$\max_\phi \mathbb{E}_{q_\theta, \pi_\phi}[\textstyle\sum_{\tau=1}^H V_\lambda(s_t)], \quad \min_\psi \mathbb{E}_{q_\theta, \pi_\phi}[\textstyle\sum_{\tau=1}^H \frac{1}{2}||v_\psi(s_t) - V_\lambda(s_t)||_2^2], \tag{7}$$

where $V_\lambda(s_t)$ is an exponentially-weighted average of the bootstrapped value target as defined in Hafner et al. (2019a),

$$
\begin{aligned}
V_N^k(s_\tau) &= \mathbb{E}_{q_\theta, \pi_\phi}[\textstyle\sum_{n=\tau}^{h-1} \gamma^{n-\tau} r_n + \gamma^{h-\tau} v_\psi(s_h), \; h = \min(\tau + k, t + H), \\
V_\lambda^k(s_\tau) &= (1 - \lambda) \textstyle\sum_{n=1}^{H-1} \lambda^{n-1} V_N^k(s_\tau) + \lambda^{H-1} V_H^k(s_\tau).
\end{aligned}
\tag{8}
$$

Note that we can differentiate through model transitions and through the reward function, so the policy can propagate gradients throughout the transitions and learn directly via gradient descent, rather than relying on policy gradients. Likewise for the value function.

2.4 ARCHITECTURE

We emulate the architecture of Hafner et al. (2019a), our observation encoder and decoder f_θ and $q_\theta(o_t \mid s_t)$ are implemented with a CNN and a transposed CNN respectively, the representation and transition functions $p_\theta(s_t \mid s_{t-1}, a_{t-1}, h_t^q)$, $q_\theta(s_t \mid s_{t-1}, a_{t-1})$ are jointly implemented with an RSSM Hafner et al. (2019b), which splits the state s_t into a deterministic component and a stochastic component, the deterministic component is shared for the representation and transition function, and does not depend on the current image embedding h_t. All other components are implemented as MLPs. All parameters used throughout the experiment are presented in the Appendix.

3 RELATED WORK

In this work we combine and extend ideas from diverse sources to address sample efficiency in MBRL. The works of Sekar et al. (2020); Hafner et al. (2019a) propose the use of analytic gradients through latent dynamics to train the policy, making efficient use of the world model to reduce the number of environment interactions needed to recover good behaviours from the available environment interactions.

Schaul et al. (2015) proposed the use of prioritized memory replay to enable the agent to focus on high loss samples in the experience buffer. This ensures that examples from rare or novel transitions are adequately explored by the model, reducing the need to collect a large number of transitions before these peculiarities of the environment can be learnt. While their work focused on Q-learning, here we extend their work to episodic sampling.

The use of sparse priors and data augmentation to improve performance in machine learning algorithms is well documented. Recent works in contrastive learning in particular He et al. (2020); Hénaff et al. (2019); Chen et al. (2020a) have yielded impressive results in other areas of machine learning, and recently Srinivas et al. (2020) applied these notions to augment a SAC-like agent with contrastive learning. The use of data augmentation in RL has also proven effective in Laskin et al. (2020), who also identify temporally-consistent random cropping as a particularly effective type of data augmentation for image-based pipelines in RL.

The use of alternative metrics to improve representation learning has been extensively studied Oord et al. (2018); Lee et al. (2019); Hafner et al. (2019b); one approach to avoid pixel reconstruction relies on the use of bisimulation distance Ferns et al. (2011); Ferns & Precup (2014), where two states are taken to be similar if for any action sequence effected on these states, the rewards are similar. The work of Zhang et al. (2020) addressed the use of bisimulation in DRL, and their experiments show that their agent is robust to large nuisance perturbations in the visual input. In section 6.2 we adapt this idea to latent bisimulation distance, but we observe no improvement in terms of sample-efficiency.

The work of Sekar et al. (2020) utilizes an ensemble of embedding predictors to estimate model uncertainty, this uncertainty is used as an unsupervised reward to learn a robust world model without extrinsic rewards. In section 6.3 we utilize latent disagreement to train an auxiliary exploration policy for data collection. Our results indicate that this did not improve sample efficiency in the low sample regime, further motivating our approach.

4 EXPERIMENTS AND RESULTS

We experimentally show the improvement in sample efficiency over a range of tasks from the Deep-mind control suite. All environments feature an articulated robot that the agent controls, with continuous actions in the range $[-1, 1]$, instantaneous rewards line in the range $r_t \in [0, 1]$, the maximum episode length is 1000, so all environments can accrue at most 1000 reward per episode. To isolate the contribution of each novel component of ReaPER, we first conduct an ablation study over a smaller subset of tasks. The results, shown in Table 1, indicate that contrastive augmentation and sparse priors can both improve sample efficiency over the benchmark, achieving higher rewards for the same number of environment interactions. Surprisingly, prioritized episodic replay by itself seemed to reduce the performance when compared against the baseline. Prioritized experience replay was, however, effective at improving sample efficiency when paired with the contrastive and sparsity auxiliary losses

Table 1: Episodic reward average for Dreamer, ReaPER, and the individual components of ReaPER, as a function of environment steps. Rewards are averaged across the cartpole balance, cartpole swingup, reacher easy, cup catch, finger spin, walker walk, walker run, and cheetah run environments in DMControl. ReaPER consistently outperforms the other options. Prioritized episodic replay by itself does not improve upon the Dreamer baseline, but is effective in conjunction with the rest of the ReaPER pipeline.

Steps	Dreamer	Contrast	L1	L1Contrast	PER	ReaPER
$100K$	309	349	358	262	263	**374**
$200K$	549	663	563	619	452	**670**
$300K$	636	714	693	691	562	**756**
$400K$	682	732	752	758	595	**780**
$500K$	707	760	774	741	611	**787**

We further validate these observations on a significantly larger set of experiments. We compare results across 18 environments and observe that, in general, ReaPER is able to obtain the same or greater rewards than Dreamer asymptotically, but it achieves these results in a smaller number of environment interactions. Figure 3a shows how the average reward over the benchmark increases as a function of environment interactions, and how this metric is improved by the addition of the regularization proposed in ReaPER. Figure 3b highlights these results by showing the average number of interactions required to achieve or surpass a given reward target for the first time over the baseline. Table 2 shows the number of steps required to reach a reward target for Dreamer and ReaPER over the same environments. We observe that ReaPER achieves better results on the benchmark across the training procedure, it also requires less samples to achieve these targets; this is especially pronounced for higher values of target rewards, since a good model is required for consistently high rewards.

(a) Average reward across environment steps   (b) Average time-to-reward

Figure 3: Performance comparison across 18 environments of the DMControl benchmark. Left figure shows average agent reward as a function of environment steps. Right figure shows the average number of steps needed to meet or exceed a reward target on the benchmark.

Figure 4 shows the reward vs environment step curves for the best 8 environments. These environments show a marked improvement by the proposed ReaPER from the Dreamer baseline, having overall better results at each timestep. Some of the environments can continue improving with additional training time, but the results here highlight that the auxiliary objectives in ReaPER can provide a marked improvement on environments of varying complexity, especially when training budget is limited.

Figure 4: Performance comparison between Dreamer and the proposed ReaPER across 8 of the best performing environments in the benchmark, mean and standard deviations are computed across 3 seeds. These environments show a marked contrast in sample efficiency between the two methods, highlighting the benefit of selecting the appropriate auxiliary objectives during training.

Table 2: Time-to-reward comparison between Dreamer and ReaPER on 8 environments in DMControl benchmark. Times indicate the average number of steps required to reach reward target (expressed as percentage of maximum reward achieved by the ReaPER agent). Average is computed over the seeds that reached the target, so the estimate is optimistic.

Reward%	Cartpole Two-poles	Reacher easy	Finger spin	Walker walk	Walker run	Pendulum swingup	Quadruped walk	Hopper hop
10%	24/24	24/34	135/61	77/89	35/13	49/59	44/40	57/38
30%	113/102	53/70	163/97	97/108	396/292	169/100	118/104	102/74
50%	378/153	151/131	196/144	122/128	540/362	226/129	255/165	141/103
70%	493/229	−/203	260/183	159/157	573/401	301/164	444/251	231/141
90%	−/494	−/305	404/249	357/240	−/485	402/229	−/459	379/209

5 DISCUSSION

We study sample efficiency in the context of model based RL and propose ReaPER, an agent that learns behaviours on latent imagination and improves upon Dreamer by explicitly introducing auxiliary objectives that enable the agent to only encode and learn the parts of the environment which are relevant for behaviour learning. We ablate each novel component of ReaPER to show how each contributes to the overall agent, and experimentally validate our findings on visual control tasks in the DMControl environment suite. We also investigate the use of latent disagreement for exploration and bisimulation, which have been successfully used for other purposes in RL, and show that these alternatives were not effective at addressing sample efficiency in this context. A potential direction of future research is to extend this analysis to curricular and continual learning in RL, and to environments where reward sparsity is in itself a major hurdle to overcome. We also wish to evaluate this approach on the Atari benchmark for discrete control.

REFERENCES

Ting Chen, Simon Kornblith, Mohammad Norouzi, and Geoffrey Hinton. A simple framework for contrastive learning of visual representations. *arXiv preprint arXiv:2002.05709*, 2020a.

Xinlei Chen, Haoqi Fan, Ross Girshick, and Kaiming He. Improved baselines with momentum contrastive learning. *arXiv preprint arXiv:2003.04297*, 2020b.

Djork-Arné Clevert, Thomas Unterthiner, and Sepp Hochreiter. Fast and accurate deep network learning by exponential linear units (elus). *arXiv preprint arXiv:1511.07289*, 2015.

Norm Ferns, Prakash Panangaden, and Doina Precup. Bisimulation metrics for continuous markov decision processes. *SIAM Journal on Computing*, 40(6):1662–1714, 2011.

Norman Ferns and Doina Precup. Bisimulation metrics are optimal value functions. In *UAI*, pp. 210–219. Citeseer, 2014.

David Ha and Jürgen Schmidhuber. World models. *arXiv preprint arXiv:1803.10122*, 2018.

Danijar Hafner, Timothy Lillicrap, Jimmy Ba, and Mohammad Norouzi. Dream to control: Learning behaviors by latent imagination. *arXiv preprint arXiv:1912.01603*, 2019a.

Danijar Hafner, Timothy Lillicrap, Ian Fischer, Ruben Villegas, David Ha, Honglak Lee, and James Davidson. Learning latent dynamics for planning from pixels. In *International Conference on Machine Learning*, pp. 2555–2565. PMLR, 2019b.

Kaiming He, Haoqi Fan, Yuxin Wu, Saining Xie, and Ross Girshick. Momentum contrast for unsupervised visual representation learning. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pp. 9729–9738, 2020.

Olivier J Hénaff, Aravind Srinivas, Jeffrey De Fauw, Ali Razavi, Carl Doersch, SM Eslami, and Aaron van den Oord. Data-efficient image recognition with contrastive predictive coding. *arXiv preprint arXiv:1905.09272*, 2019.

Matteo Hessel, Joseph Modayil, Hado Van Hasselt, Tom Schaul, Georg Ostrovski, Will Dabney, Dan Horgan, Bilal Piot, Mohammad Azar, and David Silver. Rainbow: Combining improvements in deep reinforcement learning. *arXiv preprint arXiv:1710.02298*, 2017.

Zhimin Hou, Kuangen Zhang, Yi Wan, Dongyu Li, Chenglong Fu, and Haoyong Yu. Off-policy maximum entropy reinforcement learning: Soft actor-critic with advantage weighted mixture policy (sac-awmp). *arXiv preprint arXiv:2002.02829*, 2020.

Michael I Jordan, Zoubin Ghahramani, Tommi S Jaakkola, and Lawrence K Saul. An introduction to variational methods for graphical models. *Machine learning*, 37(2):183–233, 1999.

Lukasz Kaiser, Mohammad Babaeizadeh, Piotr Milos, Blazej Osinski, Roy H Campbell, Konrad Czechowski, Dumitru Erhan, Chelsea Finn, Piotr Kozakowski, Sergey Levine, et al. Model-based reinforcement learning for atari. *arXiv preprint arXiv:1903.00374*, 2019.

Diederik P Kingma and Jimmy Ba. Adam: A method for stochastic optimization. *arXiv preprint arXiv:1412.6980*, 2014.

Brenden M Lake, Tomer D Ullman, Joshua B Tenenbaum, and Samuel J Gershman. Building machines that learn and think like people. *Behavioral and brain sciences*, 40, 2017.

Michael Laskin, Kimin Lee, Adam Stooke, Lerrel Pinto, Pieter Abbeel, and Aravind Srinivas. Reinforcement learning with augmented data. *arXiv preprint arXiv:2004.14990*, 2020.

Alex X Lee, Anusha Nagabandi, Pieter Abbeel, and Sergey Levine. Stochastic latent actor-critic: Deep reinforcement learning with a latent variable model. *arXiv preprint arXiv:1907.00953*, 2019.

Aaron van den Oord, Yazhe Li, and Oriol Vinyals. Representation learning with contrastive predictive coding. *arXiv preprint arXiv:1807.03748*, 2018.

Tom Schaul, John Quan, Ioannis Antonoglou, and David Silver. Prioritized experience replay. *arXiv preprint arXiv:1511.05952*, 2015.

Ramanan Sekar, Oleh Rybkin, Kostas Daniilidis, Pieter Abbeel, Danijar Hafner, and Deepak Pathak. Planning to explore via self-supervised world models. *arXiv preprint arXiv:2005.05960*, 2020.

Aravind Srinivas, Michael Laskin, and Pieter Abbeel. Curl: Contrastive unsupervised representations for reinforcement learning. *arXiv preprint arXiv:2004.04136*, 2020.

Richard S Sutton and Andrew G Barto. *Reinforcement learning: An introduction*. MIT press, 2018.

Yuval Tassa, Yotam Doron, Alistair Muldal, Tom Erez, Yazhe Li, Diego de Las Casas, David Budden, Abbas Abdolmaleki, Josh Merel, Andrew Lefrancq, et al. Deepmind control suite. *arXiv preprint arXiv:1801.00690*, 2018.

Yuval Tassa, Saran Tunyasuvunakool, Alistair Muldal, Yotam Doron, Siqi Liu, Steven Bohez, Josh Merel, Tom Erez, Timothy Lillicrap, and Nicolas Heess. dm_control: Software and tasks for continuous control, 2020.

Ziyu Wang, Tom Schaul, Matteo Hessel, Hado Hasselt, Marc Lanctot, and Nando Freitas. Dueling network architectures for deep reinforcement learning. In *International conference on machine learning*, pp. 1995–2003, 2016.

Amy Zhang, Rowan McAllister, Roberto Calandra, Yarin Gal, and Sergey Levine. Learning invariant representations for reinforcement learning without reconstruction. *arXiv preprint arXiv:2006.10742*, 2020.