DEEP ACTIVE LEARNING WITH NOISE STABILITY

ABSTRACT

Uncertainty estimation for unlabeled data is crucial to active learning. With a deep neural network employed as the backbone model, the data selection process is highly challenged due to the potential over-confidence of the model inference. Existing methods usually resort to multi-pass model training or adversarial training to handle this challenge. This tends to result in complex and inefficient pipelines, which would render the methods impractical. In this work, we propose a novel Single-Training Multi-Inference algorithm that leverages noise stability to estimate data uncertainty. A key idea behind is a magnitude measurement of output derivation from the original observation when the model parameters are randomly perturbed by noise. We provide analysis by using the small Gaussian noise theory and show that our method has a strong connection with the classical theory of variance reduction. That is, by labelling a data sample of higher uncertainty, as indicated by the inverse noise stability, our method contributes more to reducing the variance of existing training samples. Despite its simplicity, our method outperforms the state-of-the-art active learning baselines in image classification and semantic segmentation tasks.

1 INTRODUCTION

The success of training a deep neural network highly depends on a huge amount of labeled data. Nevertheless, in the era of big data, much data is unlabeled. This imposes a challenge on exploiting appropriate learning fashions. For instance, given a pool of unlabeled data, one can employ unsupervised manner to learn a model. However, the performance of unsupervised or semi-supervised learning is still bound to that of supervised learning (Yoo & Kweon, 2019). An ideal option could be annotating all the given data, so as to use the supervised way to learn a model. Nevertheless, the cost for data annotation could be extremely high, such as in medical area (Gorriz et al., 2017; Konyushkova et al., 2017). Due to the limited labeling budget, it may be more feasible to annotate a portion of the given data. This is also aligned with the prerequisite of semi-supervised learning. Then one can ask: which data is deserved for being annotated?

Active learning was proposed to solve this question. One of the main ideas, namely *uncertainty-based method*, aims to select a portion of the most uncertain or representative data from an unlabeled pool for annotation. The newly annotated data are then used to train a task model. Note that uncertainty estimation with deep neural networks (DNNs) remains challenging, due to the potential over-confidence of deep models. That is, the primitive softmax output[1] as a score does not necessarily reflect a reliable uncertainty or confidence for the prediction. Several methods have been proposed to address this challenge. For example, MC-Dropout (Gal & Ghahramani, 2016) implements a Single-Training Multi-Inference algorithm by aggregating multiple confidences sampled by Monte Carlo dropout. The algorithm has been shown to be equivalent to the approximate Bayesian inference. Another typical idea is query-by-committee (Freund et al., 1997; Gorriz et al., 2017), or QBC in short, which requires training multiple auxiliary models as a committee. Besides, many other efforts suggest to use specially designed auxiliary modules or training fashions, such as variational auto-encoder (Sinha et al., 2019), adversarial learning (Ducoffe & Precioso, 2018; Mayer & Timofte, 2020) and Graph Convolutional Network (Caramalau et al., 2021).

In this work, we study the problem of deep active learning from a different viewpoint, inspired by a relevant topic of *noise stability*. Noise stability, in terms of the output stability w.r.t. the input

---

[1]Considering classification problems

noise, is well studied in literature. For example, the authors in (Bishop, 1995) propose to train a model with perturbed input samples as a regularizer to improve the model performance. A recent theoretical work (Arora et al., 2018) shows that the interlayer cushion, evaluated by noise stability, acts as a good indicator of the generalization bounds for DNNs. Behind these achievements is an intuitive implication that, a model (or more exactly, its parameters) robust to perturbed input examples tends to be easy to recognize future examples. For the active learning problem, we give an analogous intuition by exchanging the role of the input and parameter that, an example robust to the perturbed current parameters tends to be easy to be recognized by a future model. In other words, *examples less robust to the parameter perturbation would be regarded as having higher uncertainty*.

Specifically, we introduce a simple algorithm of uncertainty estimation by computing the distance between outputs of the clean and perturbed input, when imposing a small noise on the parameters. The induced distance is used as a measurement of uncertainty used to select unlabeled examples in active learning. We provide a theoretical analysis under the condition that the noise magnitude is small. By imposing standard multivariate Gaussian noise to the parameter, we prove that the proposed noise stability is equivalent to the parameter-output Jacobian norm under the first order Taylor assumption. Furthermore, we show that, our algorithm has a close connection with variance reduction (Cohn et al., 1996). That is, selecting unlabeled samples with low noise stability would yield the same effect of reducing the prediction variance of existing training samples.

Our method is easy to implement and free of customized auxiliary models. Therefore, it can be exploited in various tasks, such as image classification and semantic segmentation, leading to its task-agnostic nature. We conduct extensive experiments to evaluate our method on various datasets including Cifar10 (Krizhevsky et al., 2009), Cifar100 (Krizhevsky et al., 2009), SVHN (Netzer et al., 2011), Caltech101 (Fei-Fei et al., 2006), Cityscapes (Cordts et al., 2016), and cryo-ET (Chen et al., 2017). The performance of our method significantly exceeds that of the state-of-the-art.

The contributions of this work are summarized as follows.

1. We propose a novel effective method of noise stability to select unlabeled data for active learning. The proposed method is free of any auxiliary models or special training fashions.

2. We provide a theoretical analysis to show that, selecting unlabeled data with higher noise stability is equivalent to selecting that with higher Jacobian norm w.r.t. the parameter. We also establish a connection between noise stability and variance reduction for the existing training set.

3. We conduct extensive experiments on benchmark datasets of image classification, semantic segmentation, and 3D cryo-ET subtomogram classification. The results demonstrate the effectiveness of the proposed method.

2 ACTIVE LEARNING WITH NOISE STABILITY

2.1 PROBLEM DEFINITION

Here we formulate the active learning problem. Given a pool of unlabeled data $\{X_U\}$, and a labeled pool $\{X_L, Y_L\}$ which is initially empty. Active learning aims to select a portion of data from $\{X_U\}$ depending on labeling budget (e.g. select 2500 samples out of 50000 at a time). The selected data X_N is then annotated by human oracles (or equivalent), and added to the labeled pool. That is, $\{X_L, Y_L\} \leftarrow \{X_L, Y_L\} + \{X_N, Y_N\}$, where Y_N is the new annotation for X_N. The unlabeled pool is then updated by removing the selected data: $\{X_U\} \leftarrow \{X_U\} - \{X_N\}$. $\{X_L, Y_L\}$ is then used to train a task model $f(.; \boldsymbol{\theta})$ in supervised fashion by minimizing an empirical loss L (e.g. cross-entropy loss for classification), where $f(.; \boldsymbol{\theta})$ denotes a neural network $f(.)$ parameterized with $\boldsymbol{\theta}$.

2.2 UNCERTAINTY ESTIMATION WITH NOISE STABILITY

We use the noise stability to estimate uncertainty for unlabeled data. Specifically, for an input sample $\boldsymbol{x}$, we explore to what degree will the model's output deviate from the original observation $f(\boldsymbol{x}; \boldsymbol{\theta})$, when adding random noise to the model parameter $\boldsymbol{\theta}$. Let $\xi \Delta \boldsymbol{\theta}$ denote the added noise, where ξ controls the magnitude of the noise. If $\Delta \boldsymbol{\theta}$ conforms to the standard multivariate Gaussian

---

Algorithm 1: Active learning with noise stability as uncertainty estimation.

Input : $\mathcal{T}$: random initialized task model, $\mathcal{U}$: unlabeled pool of training data, $\mathcal{L}$: labeled pool of training data, $\mathcal{C}$: number of cycles in active learning;

Output: $\boldsymbol{\theta}$: Final learned parameter of $\mathcal{T}$;

1 **begin**
2   **for** $i \leftarrow 1$ **to** $\mathcal{C}$ **do**
3   train $\mathcal{T}$ with $\mathcal{L}$, obtaining the current parameter $\boldsymbol{\theta}$;
4   **for** $k \leftarrow 1$ **to** K **do**
5   sample $\Delta\boldsymbol{\theta} \sim \mathcal{N}(\mathbf{0}, \sigma^2 \mathbf{I})$;
6   create a perturbed model $\mathcal{T}'$ parameterized with $\boldsymbol{\theta} + \xi\Delta\boldsymbol{\theta}$;
7   **for** *every $\boldsymbol{x}$ in $\mathcal{U}$* **do**
8   calculate $R^{(k)}(\boldsymbol{x}) = \|\mathcal{T}(\boldsymbol{x}) - \mathcal{T}'(\boldsymbol{x})\|^2$;
9   compute every $R(\boldsymbol{x})$ by averaging all $R^{(k)}(\boldsymbol{x})$;
10   select samples in $\mathcal{U}$ with top N largest $R(\boldsymbol{x})$ as $\{X_N\}$, and obtain their labels $\{Y_N\}$;
11   update $\mathcal{L}$ with $\mathcal{L} = \mathcal{L} \bigcup \{X_N, Y_N\}$;
12   update $\mathcal{U}$ with $\mathcal{U} = \mathcal{U} \setminus \{X_N\}$;
13   return $\boldsymbol{\theta}$;

---

distribution[2] $\mathcal{N}(\mathbf{0}, \sigma^2 \mathbf{I})$, the criterion to quantify the degree of noise *instability* can be formulated as

$$R(\boldsymbol{x}) = \mathop{\mathbb{E}}_{\Delta\boldsymbol{\theta} \sim \mathcal{N}(\mathbf{0}, \sigma^2 \mathbf{I})} \|f(\boldsymbol{x}; \boldsymbol{\theta}) - f(\boldsymbol{x}; \boldsymbol{\theta} + \xi\Delta\boldsymbol{\theta})\|^2, \tag{1}$$

where $\|.\|^2$ is the L^2 norm of a vector. In active learning, we select samples with largest $R(\boldsymbol{x})$ for annotation. To approximate the expectation, we perform a Monto-carlo sampling from the multivariate Guassian distribution to generate multiple $\Delta\boldsymbol{\theta}^{(i)}$. Then we get the approximated noise stability by

$$R(\boldsymbol{x}) = \frac{1}{K} \sum_{i=1}^{K} \|f(\boldsymbol{x}; \boldsymbol{\theta}) - f(\boldsymbol{x}; \boldsymbol{\theta} + \xi^{(i)}\Delta\boldsymbol{\theta}^{(i)})\|^2. \tag{2}$$

The noise magnitude should be small relative to that of the original parameter (e.g. $\xi^{(i)} = 10^{-3} \frac{\|\boldsymbol{\theta}\|}{\|\Delta\boldsymbol{\theta}^{(i)}\|}$) in order to avoid catastrophic perturbation to the clean model. As for the the sampling number, we find the setting $K = 5$ or 10 works well in practice. A complete procedure of our method is presented in Algorithm 1.

3 THEORETICAL UNDERSTANDINGS

In this section, we provide theoretical understandings about our simple method for uncertainty estimation. Our main conclusions are summarized as follows.

- When the noise magnitude ξ is sufficiently small, selecting data according to $R(\boldsymbol{x})$ in Eq (1) is equivalent to selecting data by the Frobenius norm of parameter-output Jacobian w.r.t. f.

- Based on the above conclusion, selecting new samples with higher $R(\boldsymbol{x})$ are expected to contribute more in reducing the prediction variance of existing training samples.

3.1 NOISE STABILITY AS JACOBIAN NORM

Let $f(\boldsymbol{x}; \boldsymbol{\theta})$ be differentiable (w.r.t. $\boldsymbol{\theta}$) at the point $\boldsymbol{\theta}$ given $\boldsymbol{x}$ as the input. When the imposed noise $\xi\Delta\boldsymbol{\theta}$ in Eq (1) has a sufficiently small magnitude, we use the first-order Taylor expansion to estimate $f(\boldsymbol{x}; \boldsymbol{\theta} + \xi\Delta\boldsymbol{\theta})$ as

$$f(\boldsymbol{x}; \boldsymbol{\theta} + \xi\Delta\boldsymbol{\theta}) \approx f(\boldsymbol{x}; \boldsymbol{\theta}) + \mathrm{J}_{\boldsymbol{\theta}}(\boldsymbol{x}; \boldsymbol{\theta})\xi\Delta\boldsymbol{\theta}, \tag{3}$$

---

[2]See Appendix A.1 for preliminaries about the standard multivariate Gaussian distribution

where $J_{\boldsymbol{\theta}}(\boldsymbol{x}; \boldsymbol{\theta})$ is the Jacobian matrix of f with respect to the parameter $\boldsymbol{\theta}$ as $J_{\boldsymbol{\theta}}(\boldsymbol{x}; \boldsymbol{\theta})_{(i,j)} = \partial f(\boldsymbol{x}; \boldsymbol{\theta})_{(i)} / \partial \boldsymbol{\theta}_{(j)}$. By substituting the Taylor approximation into Eq (1), the uncertainty estimation can be reformulated as

$$R(\boldsymbol{x}) = \mathbb{E}_{\Delta\boldsymbol{\theta} \sim \mathcal{N}(\mathbf{0}, \sigma^2 \mathbf{I})} \|J_{\boldsymbol{\theta}}(\boldsymbol{x}; \boldsymbol{\theta})\xi\Delta\boldsymbol{\theta}\|^2. \tag{4}$$

Since the elements of $\Delta\boldsymbol{\theta}$ are independent with each other, it's easy to derive that the expected uncertainty in Eq (4) is in proportion with the Frobenius norm of Jacobian as

$$R(\boldsymbol{x}) = \xi^2 \sigma^2 \|J_{\boldsymbol{\theta}}(\boldsymbol{x}; \boldsymbol{\theta})\|_F^2. \tag{5}$$

In fact, Eq (5) stands for any appropriate noise distribution with the above mentioned independence prerequisite and zero mean. *We put a detailed proof of Eq (5) in Appendix A.2.*

3.2 CONNECTIONS WITH PREDICTION VARIANCE REDUCTION

We next show an interesting connection between uncertainty estimation with noise stability and existing theoretical literature of variance reduction. For convenience, we assume that $\hat{y} = f(.; \boldsymbol{\theta})$ is a real-valued function parameterized with $\boldsymbol{\theta}$ that results in $\hat{y} : \mathbb{R}^d \to \mathbb{R}$, and the results are easy to generalize to vector-valued functions. Given a labeled training set $\mathcal{L} = \{\boldsymbol{x}_i, y_i\}_{i=1}^m$, we aim at minimizing the Mean Squared Error as

$$S^2 = \frac{1}{m} \sum_{i=1}^m (f(\boldsymbol{x}_i; \boldsymbol{\theta}) - y_i)^2. \tag{6}$$

Then, we define by $\mathbf{J}_{\hat{y}}(\boldsymbol{x})$ the Jacobian w.r.t. the parameter $\boldsymbol{\theta}$ at $\boldsymbol{x}$, i.e. $\partial\hat{y}(\boldsymbol{x}) / \partial\boldsymbol{\theta}$. Let $\mathbf{A}_{S^2}$ denote the Fisher Information Matrix that $\mathbf{A}_{S^2} = \frac{1}{S^2} \partial^2 S^2 / \partial\boldsymbol{\theta}^2$. Note that we omit the notation of $\boldsymbol{\theta}$ in $\mathbf{J}$ and $\mathbf{A}$ to avoid ambiguity. According to the well-established theory of variance estimation (Thisted, 1988), the output variance at the input point $\boldsymbol{x}$ can be represented as

$$\sigma_{\hat{y}}^2(\boldsymbol{x}) \approx \mathbf{J}_{\hat{y}}(\boldsymbol{x})^T \mathbf{A}_{S^2}^{-1} \mathbf{J}_{\hat{y}}(\boldsymbol{x}). \tag{7}$$

With the normality and local linearity assumptions, the authors in (MacKay, 1992; Cohn, 1996) further quantify the change of output variance. Specifically, when a new sample $\tilde{\boldsymbol{x}}$ is labeled and added to the training set, the expected new output variance at $\boldsymbol{x}$ is

$$\tilde{\sigma}_{\hat{y}}^2(\boldsymbol{x}) \approx \sigma_{\hat{y}}^2(\boldsymbol{x}) - \frac{\sigma_{\hat{y}}^2(\boldsymbol{x}, \tilde{\boldsymbol{x}})}{S^2 + \sigma_{\hat{y}}^2(\tilde{\boldsymbol{x}})}, \tag{8}$$

where $\sigma_{\hat{y}}^2(\boldsymbol{x}, \tilde{\boldsymbol{x}})$ is defined as

$$\sigma_{\hat{y}}(\boldsymbol{x}, \tilde{\boldsymbol{x}}) \equiv \mathbf{J}_{\hat{y}}(\boldsymbol{x})^T \mathbf{A}_{S^2}^{-1} \mathbf{J}_{\hat{y}}(\tilde{\boldsymbol{x}}). \tag{9}$$

Therefore, by adding a new sample $\tilde{\boldsymbol{x}}$, the reduction of output variance $\sigma_{\hat{y}}^2(\boldsymbol{x})$ is:

$$\begin{aligned}
\underset{\tilde{\boldsymbol{x}}}{\Delta}\sigma_{\hat{y}}^2(\boldsymbol{x}) &= \frac{\sigma_{\hat{y}}^2(\boldsymbol{x}, \tilde{\boldsymbol{x}})}{S^2 + \sigma_{\hat{y}}^2(\tilde{\boldsymbol{x}})} \\
&= \frac{\|\mathbf{J}_{\hat{y}}(\boldsymbol{x})^T \mathbf{A}_{S^2}^{-1} \mathbf{J}_{\hat{y}}(\tilde{\boldsymbol{x}})\|^2}{S^2 + \mathbf{J}_{\hat{y}}(\tilde{\boldsymbol{x}})^T \mathbf{A}_{S^2}^{-1} \mathbf{J}_{\hat{y}}(\tilde{\boldsymbol{x}})} \\
&= \frac{\|\mathbf{J}_{\hat{y}}(\boldsymbol{x})^T \mathbf{A}_{S^2}^{-1} \boldsymbol{u}(\tilde{\boldsymbol{x}})\|^2 \cdot \|\mathbf{J}_{\hat{y}}(\tilde{\boldsymbol{x}})\|^2}{S^2 + \|\boldsymbol{u}(\tilde{\boldsymbol{x}})^T \mathbf{A}_{S^2}^{-1} \boldsymbol{u}(\tilde{\boldsymbol{x}})\| \cdot \|\mathbf{J}_{\hat{y}}(\tilde{\boldsymbol{x}})\|^2},
\end{aligned} \tag{10}$$

where we use $\boldsymbol{u}(\tilde{\boldsymbol{x}})$ with the unit length to denote the direction of $\mathbf{J}_{\hat{y}}(\tilde{\boldsymbol{x}})$ as $\boldsymbol{u}(\tilde{\boldsymbol{x}}) = \frac{\mathbf{J}_{\hat{y}}(\tilde{\boldsymbol{x}})}{\|\mathbf{J}_{\hat{y}}(\tilde{\boldsymbol{x}})\|^2}$. Eq (10) implies that, for any direction $\boldsymbol{u}(\tilde{\boldsymbol{x}})$ the optimal choice for maximizing $\underset{\tilde{\boldsymbol{x}}}{\Delta}\sigma_{\hat{y}}^2(\boldsymbol{x})$ is the ones with the largest $\|\mathbf{J}_{\hat{y}}(\tilde{\boldsymbol{x}})\|^2$. Though the objective is also affected by the direction $\boldsymbol{u}(\tilde{\boldsymbol{x}})$, searching for an optimal direction is usually inefficient due to the characteristic of almost orthogonality of high-dimensional independent vectors (Vershynin, 2018).

Active learning with the objective of maximizing variance reduction has been successfully validated for shallow models such as mixture of Gaussians and kernel regression (Cohn et al., 1996). However, computing the inversion of $\mathbf{A}$ for each new sample is too cumbersome for deep neural networks. Our work establishes a strong connection between variance reduction and noise stability, and renders the algorithm implementable easily.

Figure 1: Classification performance due to different active learning methods on Cifar10 (**top left**), Cifar100 (**top right**), SVHN (**bottom left**), and Caltech101 (**bottom right**).

4 EXPERIMENTAL RESULTS

We compare our method with the state-of-the-art active learning methods. Furthermore, since random selection is the most straightforward strategy for data selection, we also include it as a baseline in this paper. We first validate our method on classical image classification and semantic segmentation tasks. Then we investigate its performance on simulated cryo-ET data (see Appendix A.3), demonstrating its competency for domain tasks. For all the tasks, the labeling budget varies from 10% to 40% corresponding to 7 active learning cycles. In each cycle, 5% of all the training data will be selected for annotation. For the first cycle, we randomly select and annotate 10% of the data from the unlabeled pool and use the selected data as initial training data for all the compared methods. Each reported result is based on three trials to obtain a reliable evaluation. We conduct all the experiments using Pytorch (Paszke et al., 2017) and the source code will be publicly available.

4.1 IMAGE CLASSIFICATION

Datasets. We adopt four benchmark classification datasets for evaluations, including Cifar10 (Krizhevsky et al., 2009), Cifar100 (Krizhevsky et al., 2009), SVHN (Netzer et al., 2011), and Caltech101 (Fei-Fei et al., 2006). Each Cifar dataset contains 50000 training and 10000 testing samples, uniformly distributed across 10 and 100 classes, respectively. SVHN includes 73257 training and 26032 testing samples, and we do not use the additional training data in SVHN following the standard settings. There are 8677 images of higher resolution (e.g. 300×200 pixels) in the Caltech101 dataset. We follow the common practice to resize the images to 256×256, and center-crop the images within a 224×224 region. Both SVHN and Caltech101 are typical imbalanced datasets. In the latter, for example, the number of samples in a class varies from 40 to 800.

Model and Training We use ResNet-18 He et al. (2016) as the task model all the classification experiments. Specifically, we follow the practice in Caramalau et al. (2021); Zhang et al. (2020) to

adopt a special version[3] of ResNet-18 He et al. (2016) as the task model to make the model compatible with the smaller image resolution (i.e. 32×32) in Cifar10/100 and SVHN. For Caltech101, we use the original ResNet-18. Since an active learning algorithm is generally independent of network architectures, we use the same task model for all the compared methods in each experiment. For instance, on Cifar10, the original CoreSet Sener & Savarese (2018) and VAAL Sinha et al. (2019) employ VGG-16 as the task model which will be replaced by ResNet-18 in our reproduction.

In each cycle of the Cifar and SVHN experiments, we use a batch size of 128 samples to train the task model with an initial learning rate of 0.1. The training continues for 200 epochs and we decay the learning rate with 0.1 at the 160th epoch. In Caltech101, the training will continue for 50 epochs and we choose 0.01 as the initial learning rate, which will be decayed by 0.1 at the 40th epoch. Due to the higher image resolution, a smaller batch size of 64 is used to avoid GPU memory issues. In order to make the evaluations not impacted by different optimization routines, we employ the same optimizer (i.e. SGD (Bottou, 2010)) for all the experiments of image classification. A momentum of 0.9 and a weight decay rate of 5×10^{-4} are used with the optimizer.

Observations. We compare our method with the state-of-the-art baselines and illustrate the results in Figure 1. The baseline methods include random selection, MC-Dropout (Gal & Ghahramani, 2016), QBC (Kuo et al., 2018), CoreSet (Sener & Savarese, 2018), VAAL (Sinha et al., 2019), LL4AL (Yoo & Kweon, 2019), SRAAL (Zhang et al., 2020) and GCN (Caramalau et al., 2021). For all these algorithms, we use the recommended hyper-parameters as suggested in their original papers. For the proposed noise stability, we use default hyper-parameters in all experiments: $\sigma^2 = 1$, $K = 10$ and $\xi = 10^{-3} \frac{\|\theta\|}{\|\Delta\theta\|}$ to ensure the relative noise magnitude constrained.

As can be seen in Figure 1, the proposed method (*NoiseStability*) consistently outperforms the baselines (in terms of accuracy) in each active learning cycle. In particular, for harder datasets such as Cifar10, Cifar100 and Caltech, our method achieves remarkably higher final accuracy against the others. For the easier task SVHN, our method yields a more rapid and stable increase of accuracy at the first several cycles, more competitive than the baselines. In addition to the general comparison, we present a detailed analysis below to demonstrate more merits of our method.

- In the later cycles (e.g. 35% and 40%), our method usually exceeds the others by a larger margin (e.g. in Cifar10 and Caltech101). This indicates that when the task model remembers more samples (i.e. the trained model is more likely to behave over-confident), estimating uncertainty by our noise stability is much more accurate than other competitors.

- The superior performance in the Caltech101 experiment suggests that our method is more suitable for imbalanced datasets than the existing baselines. We conjecture this is due to the simplicity of our method, since training helper models (Kuo et al., 2018; Sinha et al., 2019; Zhang et al., 2020; Caramalau et al., 2021) with imbalanced data could be adverse to these helpers themselves, thus leading to an inferior performance of the task model.

- Lastly, we observe that in the Cifar10 experiment, the performance of our method (94.25%) exceeds that (93.6%) of the same model which is trained on the entire dataset without considering active learning. This counter-intuitive observation indicates that training only with a subset of *hard* samples may make DNNs generalize better than training with an entire set.

4.2 SEMANTIC SEGMENTATION

Semantic segmentation is more complex than image classification due to the requirement of high classification accuracy at pixel level. As a consequence, in several baseline methods, such as VAAL Sinha et al. (2019), SRAAL Zhang et al. (2020) and GCN Caramalau et al. (2021), the auxiliary models need careful design in order to achieve an satisfactory performance. This increases the burden of deploying AI algorithms in practice. In contrast, our method is free of extra design and can be easily adopted for this problem, demonstrating its task-agnostic advantage.

Dataset. We use the Cityscapes Cordts et al. (2016), a large-scale street scene dataset. It includes images taken under various weather conditions in different seasons from 50 cities, making the task on it more challenging. We consider the standard training and validation data of this set. We crop

---

[3]https://github.com/kuangliu/pytorch-cifar

Figure 2: Classification performance due to different active learning methods on the semantic segmentation task Cityscapes.

the images to a dimension of 688×688, and there are 19 categories (classes) in total for each pixel. It is worth noting that the cropping size also depends on the task model, discussed in next section.

Model and Training. As a common practice Zhang et al. (2020), we choose a dilated residual network (DRN-D-22) (Yu et al., 2017) as the task model. It includes 8 layer modules and each module is composed of 1 or 2 *BasicBlock* of layers. One can refer to the original paper (Yu et al., 2017) for the network details .

Similar to the classification evaluations, we train the model for 7 cycles and 50 epochs for each cycle. Following the suggestion in (Yu et al., 2017), we use the Adam optimizer (Kingma & Ba, 2014). We choose a learning rate of 1×10^{-4}, remained unchanged in the entire training. For the proposed noise stability, we set $K = 3$ and keep the remaining hyper-parameters the same as specified in the classification experiments.

Observations. We compare our method with MC-Dropout (Gal & Ghahramani, 2016), QBC (Kuo et al., 2018), CoreSet (Sener & Savarese, 2018), VAAL (Sinha et al., 2019), SRAAL (Zhang et al., 2020) in this experiment. We illustrate the results in Figure 2. We observe that the improvement of the proposed method is solid. Given Cityscapes is highy imbalanced, this experiment once again demonstrates the superiority of our method on imbalanced datasets. More importantly, from classification to segmentation, our method can easily adapt to the new task by simply sampling and adding noise to the output (without being affected by the change of the output format).

5 DISCUSSIONS

In this section, we provide further analysis on the effect of the proposed method. First in Section 5.1, we discuss the choice of hyper-parameters used in noise stability. Then we evaluate our algorithm with fewer cycles and larger selection size in Section 5.2. Moreover, in Appendix A.4, we provide an empirical validation for the theoretical hypothesis that selecting samples by noise stability is conducive to reducing the output variance for the training set.

5.1 SENSITIVITY TO HYPER-PARAMETERS

We first investigate how our algorithm is sensitive to the hyper-parameters (i.e. the noise magnitude, the noise distribution and the sampling times). We conduct experiments on Cifar10 and Cifar100 for this analysis.

Noise magnitude. The criterion of noise stability in Eq (1) is sensitive to the noise magnitude. Specifically, noise with too large magnitudes tends to destroy the learned knowledge in DNNs. For simplicity, we denote by λ the relative (to the clean parameter) magnitude, i.e. $\xi = \lambda \frac{\|\boldsymbol{\theta}\|}{\|\Delta \boldsymbol{\theta}^{(i)}\|}$. We evaluate the choices of $\{10^{-5}, 10^{-4}, 10^{-3}, 10^{-2}, 10^{-1}, 1\}$ for λ. Results in Figure 3 (left) show that

Figure 3: Evaluations of different hyper-parameters on Cifar100: noise magnitude λ (**left**), sampling times K (**middle**) and noise distribution (**right**). In the left and middle plots, we use dots with different colors to denote different cycles, e.g. the blue dots at the bottom refer to cycle 1 and the pink dots at the top refer to cycle 7.

using λ between 10^{-4} and 10^{-2} is likely to yield good performance. From the various experiments of this work, we observe that a default choice of 10^{-3} would be suitable in general.

Sampling times. Accurate approximations such as that for Eq (1) usually require a considerable sampling times. However, we surprisingly find that the noise stability scheme used in our algorithm is very insensitive to the sampling times K. We evaluate K with choices of $\{1, 3, 10, 30, 50\}$ and observe very similar results, as shown in Figure 3 (middle). We conjecture this might be because the uncertainty estimation in active learning does not require an accurate approximation of the exact value, even nor the exact order. The main factor that impacts the final results is only the selected subset of data.

Noise distribution. Note that our method is not limited to the multivariate Gaussian distribution. Any distribution with all the elements independent of each other satisfies the theoretical properties. Here we evaluate two alternative noise distributions, which are the Uniform distribution $\Delta\boldsymbol{\theta}_i \sim \mathrm{U}(-1, 1)$ and the zero-mean Laplace distribution $\Delta\boldsymbol{\theta}_i \sim \mathrm{Laplace}(0, b)$ with $b = 1$. Results in Figure 3 (right) show that both of them achieve similar good performance as the normal distribution.

5.2 Performance on Larger Selection Size

It remains a long-term open problem that whether data uncertainty and diversity are empirically consistent or in a trade-off relationship. Instead of directly addressing this dilemma, we design an experiment to investigate how our algorithm performs with an increased selection size[4]. As the training pool is enlarged by adding a large amount of samples, both uncertainty and diversity tend to be crucial to further training, e.g. highly imbalanced (lack of diversity) data is definitely harmful to learning. For efficiency, we perform a single cycle of sample selection after cycle 1. We use different algorithms to select unlabeled samples with the labeling budgets of 10%, 15%, 20%, 25%, 35% and 40% respectively. Note that it is different from the standard experiments presented in Figure 1, since the sample selection here is one-off rather than iterative. Results in Figure 4 demonstrate that our method still consistently outperforms the SOTA baseline GCN Caramalau et al. (2021).

6 Related Work

Active learning has been a long-term open research topic in the community. Most of the methods can be categorized into three types including uncertainty-based, diversity-based and synthesis-based methods. In this section we provide a brief review of these typical studies.

Uncertainty-based. Traditional methods solve the problem mainly via estimating uncertainty for unlabeled data. Some typical works (Joshi et al., 2009; Lewis & Catlett, 1994; Lewis & Gale, 1994; Roth & Small, 2006; Tong & Koller, 2001; Vijayanarasimhan & Grauman, 2014; Li & Guo, 2014) have been proposed for shallow or statistical models. Nevertheless, as the rapid development of deep learning, a new challenge has emerged. That is, how to estimate data uncertainty with deep neural

---

[4]Selection size in this section refers to the number of the unlabeled samples selected in a cycle.

Figure 4: Evaluation of using larger selection size, denoted by *non-iterative* as it only performs an one-off selection. Results with the standard setting (denoted as *iterative*), copied from Figure 1, are also shown for comparison. Experiments are conducted on Cifar10 (**left**) and Cifar100 (**right**).

networks (DNNs). Several methods (Sinha et al., 2019; Yoo & Kweon, 2019; Zhang et al., 2020; Mackowiak et al., 2018) have been proposed to address this challenge with the aid of specialized DNNs and training fashions, such as VAE (variational auto-encoder) (Kingma & Welling, 2013) and adversarial learning. Sener & Savarese (2018); Kuo et al. (2018) attempt to combine a classical algorithm (e.g. K-center or 0-1 Knapsack problem) with DNNs to select the most uncertain data for annotation. Note that our method belongs to this category.

In terms of methodology, the most similar existing work to ours is MC-Dropout (Gal & Ghahramani, 2016). However, the motivation is quite different in that we adopt noise stability to estimate uncertainty, whereas MC-Dropout resorts to Bayesian inference to approximate the uncertainty (measured in the output entropy). Another essential difference lies in that, noise stability only needs a local sampling that generates parameter noise around a specific solution, whereas Bayesian inference requires global sampling over the entire hypothesis space. As a consequence, the necessary sampling times of MC-Dropout (e.g. ~ 100 or ~ 1000) is orders of magnitude larger than noise stability.

Diversity-based. In addition to the uncertainty-based methods, several works attempt to select unlabeled data that can diversify the labeled pool. This category of methods are also known as distribution-based (Bilgic & Getoor, 2009; Elhamifar et al., 2013; Freytag et al., 2014; Hasan & Roy-Chowdhury, 2015; Mac Aodha et al., 2014; Nguyen & Smeulders, 2004; Roy & McCallum, 2001; Yang et al., 2015; Settles et al., 2008). Although the diversity-based methods were traditionally treated as essentially different from the uncertainty-based methods, it is worth noting that a recent study (Loquercio et al., 2020) argues that data diversity is correlated to data uncertainty.

Synthesis-based. Another typical category of methods aim to diversify the labeled pool by synthesizing new data that can benefit the task model training. Typical methods (Zhu & Bento, 2017; Mahapatra et al., 2018; Mayer & Timofte, 2020) resort to generative models, such as GAN (Goodfellow et al., 2014) or VAE (Kingma & Welling, 2013) to synthesize diverse data samples to train the task model.

7 CONCLUSION

This paper proposes a simple method that utilizes noise stability for uncertainty estimation in active learning. For an input sample, noise stability measures how stable can the output be when a random perturbation is added on the model parameters. Our theoretical analysis prove that the noise stability approximates Jacobian norm w.r.t. the parameters assuming the noise magnitude is small. Theoretical and empirical analysis also demonstrate that, selecting those samples mostly unstable to parameter noise has the effect of reducing the prediction variance of the training samples. Experiments on image classification, semantic segmentation, and 3D cryo-ET subtomogram classification demonstrate the efficacy of the proposed method.

REFERENCES

Sanjeev Arora, R. Ge, Behnam Neyshabur, and Yi Zhang. Stronger generalization bounds for deep nets via a compression approach. *ArXiv*, abs/1802.05296, 2018.

Mustafa Bilgic and Lise Getoor. Link-based active learning. In *NIPS Workshop on Analyzing Networks and Learning with Graphs*, 2009.

Chris M Bishop. Training with noise is equivalent to tikhonov regularization. *Neural computation*, 7(1):108–116, 1995.

Léon Bottou. Large-scale machine learning with stochastic gradient descent. In *Proceedings of the COMPSTAT*, pp. 177–186. Springer, 2010.

Razvan Caramalau, Binod Bhattarai, and Tae-Kyun Kim. Sequential graph convolutional network for active learning. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition (CVPR)*, pp. 9583–9592, June 2021.

Muyuan Chen, Wei Dai, Stella Y Sun, Darius Jonasch, Cynthia Y He, Michael F Schmid, Wah Chiu, and Steven J Ludtke. Convolutional neural networks for automated annotation of cellular cryo-electron tomograms. *Nature Methods*, 14(10):983, 2017.

D. A Cohn, Z Ghahramani, and M. I Jordan. Active learning with statistical models. *The Journal of artificial intelligence research*, 4:129–145, 1996. ISSN 1076-9757.

David A Cohn. Neural network exploration using optimal experiment design. *Neural networks*, 9 (6):1071–1083, 1996. ISSN 0893-6080.

Marius Cordts, Mohamed Omran, Sebastian Ramos, Timo Rehfeld, Markus Enzweiler, Rodrigo Benenson, Uwe Franke, Stefan Roth, and Bernt Schiele. The cityscapes dataset for semantic urban scene understanding. In *IEEE Conference on Computer Vision and Pattern Recognition*, 2016.

Melanie Ducoffe and Frederic Precioso. Adversarial active learning for deep networks: a margin based approach. *arXiv Preprint arXiv:1802.09841*, 2018.

Ehsan Elhamifar, Guillermo Sapiro, Allen Yang, and S Shankar Sasrty. A convex optimization framework for active learning. In *Proceedings of the IEEE International Conference on Computer Vision*, pp. 209–216, 2013.

Li Fei-Fei, Rob Fergus, and Pietro Perona. One-shot learning of object categories. *IEEE TPAMI*, 28 (4):594–611, 2006.

Yoav Freund, H. Sebastian Seung, Eli Shamir, and Naftali Tishby. Selective sampling using the query by committee algorithm. *Machine Learning*, 28(2-3):133–168, 1997.

Alexander Freytag, Erik Rodner, and Joachim Denzler. Selecting influential examples: Active learning with expected model output changes. In *Proceedings of the European Conference on Computer Vision*, pp. 562–577, 2014.

Yarin Gal and Zoubin Ghahramani. Dropout as a bayesian approximation: Representing model uncertainty in deep learning. In *International Conference on Machine Learning*, 2016.

Ian Goodfellow, Jean Pouget-Abadie, Mehdi Mirza, Bing Xu, David Warde-Farley, Sherjil Ozair, Aaron Courville, and Yoshua Bengio. Generative adversarial nets. In *Proceedings of the Advances in Neural Information Processing Systems*, pp. 2672–2680, 2014.

Marc Gorriz, Axel Carlier, Emmanuel Faure, and Xavier Giro-i Nieto. Cost-effective active learning for melanoma segmentation. *arXiv Preprint arXiv:1711.09168*, 2017.

I Gubins, G van der Shot, RC Veltkamp, F Foerster, X Du, X Zeng, et al. SHREC'19 track: Classification in cryo-electron tomograms. In *Eurographics Workshop on 3D Object Retrieval*, 2019.

Mahmudul Hasan and Amit K Roy-Chowdhury. Context aware active learning of activity recognition models. In *Proceedings of the IEEE International Conference on Computer Vision*, pp. 4543–4551, 2015.

Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pp. 770–778, 2016.

Ajay J Joshi, Fatih Porikli, and Nikolaos Papanikolopoulos. Multi-class active learning for image classification. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pp. 2372–2379, 2009.

Diederik P Kingma and Jimmy Ba. Adam: A method for stochastic optimization. *arXiv Preprint arXiv:1412.6980*, 2014.

Diederik P Kingma and Max Welling. Auto-encoding variational bayes. *arXiv Preprint arXiv:1312.6114*, 2013.

Ksenia Konyushkova, Raphael Sznitman, and Pascal Fua. Learning active learning from data. In *Proceedings of the Advances in Neural Information Processing Systems*, pp. 4225–4235, 2017.

Alex Krizhevsky, Geoffrey Hinton, et al. Learning multiple layers of features from tiny images. 2009.

Weicheng Kuo, Christian Häne, Esther Yuh, Pratik Mukherjee, and Jitendra Malik. Cost-sensitive active learning for intracranial hemorrhage detection. In *International Conference on Medical Image Computing and Computer-Assisted Intervention*, 2018.

David D Lewis and Jason Catlett. Heterogeneous uncertainty sampling for supervised learning. In *Machine learning proceedings*, pp. 148–156. Elsevier, 1994.

David D Lewis and William A Gale. A sequential algorithm for training text classifiers. In *SIGIR*, 1994.

Xin Li and Yuhong Guo. Multi-level adaptive active learning for scene classification. In *Proceedings of the European Conference on Computer Vision*, pp. 234–249, 2014.

Antonio Loquercio, Mattia Segu, and Davide Scaramuzza. A general framework for uncertainty estimation in deep learning. *IEEE Robotics and Automation Letters*, 5(2):3153–3160, 2020.

Oisin Mac Aodha, Neill DF Campbell, Jan Kautz, and Gabriel J Brostow. Hierarchical subquery evaluation for active learning on a graph. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pp. 564–571, 2014.

David J. C MacKay. Information-based objective functions for active data selection. *Neural computation*, 4(4):590–604, 1992. ISSN 0899-7667.

Radek Mackowiak, Philip Lenz, Omair Ghori, Ferran Diego, Oliver Lange, and Carsten Rother. Cereals-cost-effective region-based active learning for semantic segmentation. *arXiv Preprint arXiv:1810.09726*, 2018.

Dwarikanath Mahapatra, Behzad Bozorgtabar, Jean-Philippe Thiran, and Mauricio Reyes. Efficient active learning for image classification and segmentation using a sample selection and conditional generative adversarial network. In *International Conference on Medical Image Computing and Computer-Assisted Intervention*, 2018.

Christoph Mayer and Radu Timofte. Adversarial sampling for active learning. In *Proceedings of the IEEE Winter Conference on Applications of Computer Vision*, pp. 3071–3079, 2020.

Yuval Netzer, Tao Wang, Adam Coates, Alessandro Bissacco, Bo Wu, and Andrew Y Ng. Reading digits in natural images with unsupervised feature learning. In *NIPS Workshop on Deep Learning and Unsupervised Feature Learning*, 2011.

Hieu T Nguyen and Arnold Smeulders. Active learning using pre-clustering. In *International Conference on Machine Learning*, 2004.

Adam Paszke, Sam Gross, Soumith Chintala, Gregory Chanan, Edward Yang, Zachary DeVito, Zeming Lin, Alban Desmaison, Luca Antiga, and Adam Lerer. Automatic differentiation in pytorch. 2017.

Dan Roth and Kevin Small. Margin-based active learning for structured output spaces. In *Proceedings of the European Conference on Machine Learning*, pp. 413–424, 2006.

Nicholas Roy and Andrew McCallum. Toward optimal active learning through monte carlo estimation of error reduction. *International Conference on Machine Learning*, 2001.

Ozan Sener and Silvio Savarese. Active learning for convolutional neural networks: A core-set approach. In *International Conference on Learning Representations*, 2018.

Burr Settles, Mark Craven, and Soumya Ray. Multiple-instance active learning. In *Proceedings of the Advances in Neural Information Processing Systems*, pp. 1289–1296, 2008.

Samarth Sinha, Sayna Ebrahimi, and Trevor Darrell. Variational adversarial active learning. In *Proceedings of the IEEE International Conference on Computer Vision*, pp. 5972–5981, 2019.

Ronald A. (Ronald Aaron) Thisted. *Elements of statistical computing*. Chapman and Hall, New York, 1988. ISBN 0412013711.

Simon Tong and Daphne Koller. Support vector machine active learning with applications to text classification. *Journal of Machine Learning Research*, 2(Nov):45–66, 2001.

Roman Vershynin. *High-dimensional probability: An introduction with applications in data science*, volume 47. Cambridge university press, 2018.

Sudheendra Vijayanarasimhan and Kristen Grauman. Large-scale live active learning: Training object detectors with crawled data and crowds. *International Journal of Computer Vision*, 108 (1-2):97–114, 2014.

Yi Yang, Zhigang Ma, Feiping Nie, Xiaojun Chang, and Alexander G Hauptmann. Multi-class active learning by uncertainty sampling with diversity maximization. *International Journal of Computer Vision*, 113(2):113–127, 2015.

Donggeun Yoo and In So Kweon. Learning loss for active learning. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pp. 93–102, 2019.

Fisher Yu, Vladlen Koltun, and Thomas Funkhouser. Dilated residual networks. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pp. 472–480, 2017.

Beichen Zhang, Liang Li, Shijie Yang, Shuhui Wang, Zheng-Jun Zha, and Qingming Huang. State-relabeling adversarial active learning. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pp. 8756–8765, 2020.

Jia-Jie Zhu and José Bento. Generative adversarial active learning. *arXiv Preprint arXiv:1702.07956*, 2017.

A APPENDIX

A.1 STANDARD MULTIVARIATE GUASSIAN DISTRIBUTION

The univariate Gaussian distribution is often referred to as $\mathcal{N}(\mu, \sigma^2)$, where μ denotes the expectation of the distribution and σ is the standard deviation. $\mathcal{N}(\mu, \sigma^2)$ can be described by its probability density function as $p(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$. Multivariate Gaussian distribution $\boldsymbol{x} \sim \mathcal{N}(\boldsymbol{\mu}, \boldsymbol{\Sigma})$, is a generalized form for the vector variable, where $\boldsymbol{\mu}$ is the mean vector and $\boldsymbol{\Sigma}$ is the covariance matrix. In this work, we shall focus on the standard case, in which $\boldsymbol{\mu}$ is the zero vector $\boldsymbol{0}$ and $\boldsymbol{\Sigma}$ is a diagonal matrix with all diagonal elements being σ^2, i.e. $\boldsymbol{\Sigma} = \sigma^2 \mathbf{I}$. Note that if $\boldsymbol{x} \sim \mathcal{N}(\boldsymbol{0}, \sigma^2 \mathbf{I})$, all the samplings $\{\boldsymbol{x}_i\}$ are independent of each other, and each conforms to the standard univariate Gaussian distribution as $x_i \sim \mathcal{N}(0, \sigma^2)$.

A.2 PROOF OF EQ (5)

We first assume $f(.; \boldsymbol{\theta})$ is a real-valued function and the Jacobian is a vector. If $\Delta\boldsymbol{\theta} \in \mathbb{R}^d$ conforms to the standard multivariate Gaussian distribution that $\Delta\boldsymbol{\theta} \sim \mathcal{N}(\mathbf{0}, \sigma^2\mathbf{I})$, each of its elements are independent with each other. That is, for any $1 \leq i, j \leq d$, the following is true:

$$\mathbb{E}_{\Delta\boldsymbol{\theta} \sim \mathcal{N}(\mathbf{0}, \sigma^2\mathbf{I})} \Delta\boldsymbol{\theta}_i \Delta\boldsymbol{\theta}_j = \sigma^2 \delta_{ij}, \tag{11}$$

where $\delta_{ij} = \mathbf{1}_{i=j}$. Without ambiguity, here we use J as a shorthand for $\mathrm{J}_{\boldsymbol{\theta}}(\boldsymbol{x}; \boldsymbol{\theta})$. The notation of Gaussian distribution under the expectation is also omitted for simplicity.

Proof. Based on Eq (11), we can expand the inner product between J and $\Delta\boldsymbol{\theta}$ in Eq (4) as

$$
\begin{aligned}
R(\boldsymbol{x}) &= \xi^2 \mathbb{E}_{\Delta\boldsymbol{\theta}} \| \sum_{i=1}^{d} \mathrm{J}_i \Delta\boldsymbol{\theta}_i \|^2 \\
&= \xi^2 \mathbb{E}_{\Delta\boldsymbol{\theta}} \sum_{i=1}^{d} \mathrm{J}_i^2 \Delta\boldsymbol{\theta}_i^2 + \xi^2 \mathbb{E}_{\Delta\boldsymbol{\theta}} \sum_{\substack{i,j=1 \\ i \neq j}}^{d} \mathrm{J}_i \Delta\boldsymbol{\theta}_i \mathrm{J}_j \Delta\boldsymbol{\theta}_j \\
&= \xi^2 \sum_{i=1}^{d} \mathrm{J}_i^2 \mathbb{E}_{\Delta\boldsymbol{\theta}} \Delta\boldsymbol{\theta}_i^2 + \xi^2 \sum_{\substack{i,j=1 \\ i \neq j}}^{d} \mathrm{J}_i \mathrm{J}_j \mathbb{E}_{\Delta\boldsymbol{\theta}} \Delta\boldsymbol{\theta}_i \Delta\boldsymbol{\theta}_j \\
&= \xi^2 \sum_{i=1}^{d} \mathrm{J}_i^2 \sigma^2 \\
&= \xi^2 \sigma^2 \|\mathrm{J}\|^2.
\end{aligned} \tag{12}
$$

When $f(.; \boldsymbol{\theta})$ is vector-valued, we can straightforwardly put each row of the Jacobian matrix into Eq (12) and finally get

$$R(\boldsymbol{x}) = \xi^2 \sigma^2 \|\mathrm{J}\|_F^2. \tag{13}$$

$\square$

Note that, the conclusion is true for any other zero-mean distribution as long as it satisfies the independence prerequisite and has a definite variance. The multivariate Gaussian distribution is used only as a typical example.

A.3 CRYO-ET CHALLENGES

Cryo-Electron Tomography (cryo-ET) is an important imaging technique to study biological macro-molecules and cells, used to produce their high-resolution 3D tomograms of cellular landscapes and structures. Active learning is of great interest for such kind of tasks since the annotation cost is extremely high. We evaluate our active learning algorithm on cryo-ET subtomogram classification (Chen et al., 2017), demonstrating the capability of our method in various domains.

Dataset. We compare our noise stability against the baseline methods on one simulated cryo-ET dataset consisting of subtomogram images contaminated by noise with a SNR (signal-noise-ratio) of 0.03. Given different conformational states, all the samples in this dataset are categorized into 50 classes, namely *50c-snr003*. There are 24000 training and 1000 test samples, uniformly distributed across all the classes. One can refer to Gubins et al. (2019) for how to generate the data.

Model and Training. The dimension of the subtomogram data (i.e. $32 \times 32 \times 32$) is different with that of RGB images, making the classification task more challenging. To adapt to this particular data dimension, we employ a customized ResNet-18 with 3D convolutional layers as the task model. In addition to the task model, in the baseline methods one also needs to customize the auxiliary models (e.g. VAE in VAAL (Sinha et al., 2019) and SRAAL (Zhang et al., 2020), and the loss prediction module in LL4AL (Yoo & Kweon, 2019)), whereas our method is free of this extra implementation.

The SGD optimizer (Bottou, 2010) is employed to train the task model. The training will continue for 100 epochs and the initial learning rate is set as 0.1, and we decay it by 0.1 at the 80th epoch. We

choose a momentum of 0.9 and a weight decay rate of 5×10^{-4}, respectively. For the proposed noise stability, we set $K = 5$ and remain the hyper-parameters the same as specified in the classification experiments.

Figure 5: Classification performance due to different active learning methods on the cryo-ET task: 50c-snr003.

Observations. We present the comparisons of the different methods in Figure 5. At each cycle, our method demonstrates solid improvement over the others. Moreover, in the later cycles, our method outperforms the others by a significant margin, demonstrating its consistent superiority. Moreover, due to the noise in the data, some other methods show reduced accuracy as cycle increases (e.g. CoreSet (Sener & Savarese, 2018), whereas our method keeps climbing towards a higher accuracy.

A.4 EMPIRICAL VALIDATION OF VARIANCE REDUCTION

Theoretical analysis in Section 3.2 reveals the connection between noise stability and variance reduction. Here we validate this connection, by quantifying the variance reduction for the training samples used in cycle 1, using the model trained in the subsequent cycle. As the original form of output variance is intractable for DNNs (Thisted, 1988), we choose MC-Dropout (Gal & Ghahramani, 2016) as the criterion of variance estimation to evaluate our method and other competitors. Specifically, we approximate the uncertainty with 1) the confidence represented by Bayesian posterior probability for the true label and 2) the prediction entropy. Results are shown in Table 1. While training with more samples always reduce the output variance for training samples, selecting samples with noise stability exhibits the most significant effect.

Table 1: Evaluation of variance reduction for different active learning methods at cycle 2 on Cifar10. The confidence of the true label (higher is better) and Entropy (lower is better) are used to approximate the variance. We use the same random seed in the all experiments. The Confidence and Entropy at cycle 1 for training samples are 0.64 and 0.69, respectively.

Criterion	Random	CoreSet	VAAL	GCN	NoiseStability
Confidence	0.77	0.79	0.74	0.78	**0.80**
Entropy	0.45	0.44	0.51	0.44	**0.42**