KEEP CALM AND CARRY OFFLINE:
POLICY REFINEMENT IN OFFLINE REINFORCEMENT LEARNING

ABSTRACT

The ability to discover optimal behaviour from fixed data sets has the potential to transfer the successes of reinforcement learning (RL) to domains where data collection is acutely problematic. In this offline setting a key challenge is overcoming overestimation bias for actions not present in data which, without the ability to correct for via interaction with the environment, can propagate and compound during training, thus leading to highly sub-optimal policies. One simple method to reduce this bias is to introduce a policy constraint via behavioural cloning (BC), which encourages agents to pick actions closer to the source data. By finding the right balance between RL and BC such approaches have been shown to be surprisingly effective while requiring minimal changes to the underlying algorithms they are based on. To date, this balance has been held constant but in this work we explore the idea of tipping this balance towards RL following initial training. Using TD3-BC we demonstrate that by continuing to train a policy offline while reducing the influence of the BC component we can produce refined policies that outperform the original baseline, as well as match or exceed the performance of more complex alternative approaches. Furthermore, we show these refined policies can be fine-tuned online while largely mitigating severe performance drops.

1 INTRODUCTION

In offline reinforcement learning (offline-RL) (Lange et al., 2012) an agent seeks to discover an optimal policy purely from a fixed data set. This is a challenging task as, unlike traditional reinforcement learning, an agent can no longer interact with the environment to assess the quality of exploratory actions and thus cannot correct for errors in value estimates. These errors can propagate and compound during training leading to highly sub-optimal policies or, in the worst case, a complete failure to learn (Levine et al., 2020).

A common approach to overcoming this problem is to perform some kind of regularisation during training, encouraging updates during policy evaluation and/or policy improvement to stay close to underlying data. One way to achieve this is to modify existing off-policy algorithms to directly incorporate behavioural cloning (BC), a technique that has been shown to be computationally efficient, easy to implement and able to produce policies that compete with more complex alternatives (Fujimoto & Gu, 2021). What's more, such approaches require minimal changes to the underlying algorithms they are based on, making performance gains easier to attribute and hyperparameter tuning less burdensome, both desirable properties where online interaction is limited.

Finding the optimal level of behavioural cloning is key; too little runs the risk of error propagation but too much limits the agent's ability to learn policies beyond those which generated the data. To date, such approaches have maintained a constant level throughout training, but in this work we explore the idea of reducing the influence of behavioural cloning following an initial period of learning.

Using TD3-BC as the foundation we show that by continuing to train offline in this way we are able to produce refined policies that improve over the baseline, particularly in cases where the data is sub-optimal. In addition, we show we are able to transition to online fine-tuning while maintaining a similar level of performance without having to make any additional implementation adjustments.

Despite the simplicity of our of approach we are able to match or exceed the performance of state-of-the-art alternatives.

2   BACKGROUND

We follow standard practice and define a Markov decision process (MDP) with state space S, action space A, transition dynamics $T(s'|s,a)$, reward function $R(s,a)$ and discount factor $\gamma \in [0,1]$ (Sutton & Barto, 2018). An agent interacts with this MDP by following a policy $\pi(a|s)$, which can be deterministic or stochastic. The goal of reinforcement learning is to discover an optimal policy $\pi^*(a|s)$ that maximises the expected discounted sum of rewards $\mathbb{E}_\pi(\sum_{t=0}^\infty \gamma^t r(s_t, a_t))$.

In Actor-Critic methods this is achieved by alternating between policy evaluation and policy improvement using Q-functions $Q^\pi(s,a)$, which estimate the value of taking action a in state s following policy π thereafter. Policy evaluation consists of updating Q-values based on the Bellman expectation equation $Q^\pi(s,a) = r(s,a) + \gamma \mathbb{E}_{s' \sim T, a' \sim \pi}(Q^\pi(s', a'))$ with improvement coming from updating policy parameters to maximise $Q^\pi(s,a)$.

In offline reinforcement learning the agent no longer has access to the environment and instead must learn solely from pre-existing interactions $D = (s_i, a_i, r_i, s_i')$. In this setting, agents struggle to learn effective policies due to overestimation bias for state-action pairs absent in D, which compounds and propagates during training leading to highly sub-optimal policies or a complete collapse of the learning process (Levine et al., 2020).

TD3-BC (Fujimoto & Gu, 2021) is an adaptation of TD3 (Fujimoto et al., 2018) to the offline setting, adding a behavioural cloning term to policy updates to encourage agents to stay close to actions in D. The updated policy objective is:

$$\pi = \arg\max_\pi \mathbb{E}_{(s,a) \sim D}\Big[\underbrace{Q(s, \pi(s))}_{\text{reinforcement learning}} - \alpha \underbrace{(\pi(s) - a)^2}_{\text{behavioural cloning}} \Big]$$

The hyperparamter α controls the balance between reinforcement learning and behavioural cloning. In order to keep this balance in check, Q-values (which scale with rewards and hence can vary across tasks) are normalised by dividing by the mean of the absolute values. States are also normalised to approximate an $N(0,1)$ distribution:

$$Q_{norm}(s_i, a_i) = \frac{Q(s_i, a_i)}{\frac{1}{N} \sum_{s_i, a_i} |Q(s_i, a_i)|} \qquad , \qquad s_i = \frac{s_i - \mu}{\sigma - \epsilon}$$

where $\epsilon = 10^{-3}$ is a small normalisation constant.

The only remaining task it to find a value of α that both prevents the propagation of overestimation bias and allows the agent to learn a policy that improves on the data.

3   RELATED WORK

While TD3-BC uses behavioural cloning explicitly in policy updates, other approaches such as BCQ (Fujimoto et al., 2019), PLAS (Wu et al., 2019), BRAC (Wu et al., 2019) and BEAR (Kumar et al., 2019) utilise it more implicitly, training a Conditional Variational AutoEncoder (CVAE) (Sohn et al., 2015) to mimic the data distribution and either optimise CVAE generated actions (BCQ, PLAS) or minimise divergence metrics between the CVAE and the policy (BRAC, BEAR). Such methods do successfully combat overestimation bias but tend to perform worse than simpler methods such as TD3-BC, particularly for multimodal distributions which are hard to model accurately.

Other examples of using behavioural cloning less directly include Implicit Q-learning (IQL) (Kostrikov et al., 2021b) which combines expectile regression and advantage weighted behavioural cloning to train agents without having to evaluate actions outside the dataset, and Fisher-BRC (Kostrikov et al., 2021a) which uses a cloned behaviour policy for critic regularisation via the Fisher divergence metric. Both methods perform comparably to TD3-BC but also suffer to the same degree when learning from sub-optimal data.

Conservative Q-learning (CQL) (Kumar et al., 2020) focuses specifically on critic regularisation by augmenting the Bellman expectation equation by "pushing down" on $Q(s, a)$ for actions outside the dataset and "pushing up" on $Q(s, a)$ for actions in the dataset. CQL performs well across a wide range of tasks but is computationally expensive and often relies on implementation tweaks to achieve such levels of performance (Fujimoto & Gu, 2021).

Finally, we note that behavioural cloning has also been used in the online setting with a focus on data efficiency, such as combining with DDPG (Nair et al., 2018) or SAC (Nair et al., 2020).

4 POLICY REFINEMENT

The relative simplicity and competitive performance of TD3-BC makes it an attractive proposition for offline-RL. There are however occasions where it falls short, particularly when the underlying data is sub-optimal. The BC component which is so crucial to preventing overestimation bias is the same component which limits the agent's potential. But is there a way to overcome this without increasing complexity?

We note that at the start of training too low a value of α fails to prevent overestimation bias. When α is sufficiently high this overestimation bias is mitigated leading to a more accurate critic, albeit more limited to the state-action region present in D. However, in learning to produce reasonable estimates in this region it may then be possible for the critic to improve its estimates outside this region, allowing the value of α to be reduced to a level which at the start was too small. In other words, the critic learns from actions close to the ground truth before generalising to actions further away: learning to walk before learning to run.

With this in mind we modify the training procedure of TD3-BC to include an additional period of policy refinement, reducing the value of α and carrying-on offline. To prevent overestimation bias reappearing we focus solely on the policy, performing no further updates to the critic. We illustrate this procedure in Figure 1 and provide full details in Appendix A.

Train on actions close to data   Train on actions further from data   Deploy

Figure 1: Keep calm and carry offline. To begin with, an agent is trained on actions close to the data to avoid overestimation bias. Next, the agent is trained on actions further from the data to refine the policy prior to deployment. Following this procedure allows better generalisation to unseen state-action pairs that an agent may poorly estimate without prior training. Green area represents action space permitted by the value of α.

While there are many options available for reducing α, for the purpose of this work we simply scale by a constant $\lambda \geq 1$, giving rise to a new BC coefficient α' such that:

$$\alpha' = \frac{\alpha}{\lambda} \tag{1}$$

5 EXPERIMENTS

We evaluate our method using MuJoCo tasks from the D4RL benchmark (Todorov et al., 2012), (Fu et al., 2020) and compare to a number of state-of-the-art approaches mentioned in Section 3. This benchmark contains a variety of tasks aimed at testing an agent's ability to learn from sub-optimal or narrow data distributions as well as expert demonstrations. Each experiment is repeated across five random seeds with reported results the mean normalised score $\pm$ one standard deviation for

50 evaluations (10 from each seed). Scores of 0 and 100 represent equivalent random and expert policies, respectively. Further details, including network architecture and hyperparameters, can be found in Appendix B.

Offline policy refinement: Following the procedure in (Fujimoto & Gu, 2021) we train an agent for 1M gradient steps with $\alpha = 0.4$ to produce a baseline policy. We then perform policy refinement for a further 250k steps, setting $\lambda = 5$ for all tasks except hopper-medium-expert and halfcheetah-expert/medium-expert where $\lambda = 1$

We also conduct a number of ablation studies to highlight the importance of the design decisions outlined in Section 4. These results are presented in Appendix C.

Online fine-tuning: We assess each agent's ability to transition from offline to online learning. We initialise a new replay buffer and populate with 5k (s, a, r, s') samples collected using the offline trained policy. We then train both critic and policy for an additional 245k environment interactions (250k in total), decaying α exponentially from $\alpha_{start} = 0.4$ to $\alpha_{end} = 0.2$. While we acknowledge other TD3-BC based approaches such as REDQ+AdaptiveBC (Zhao et al., 2021), we find our simple procedure achieves a similar level of performance and stability without the need for domain knowledge or ensemble methods.

Results are summarised in Table 1. We denote the baseline policy as TD3-BC and refined policy as TD3-BC-PR. Corresponding online fine-tuned policies are suffixed -FT. Offline results for BC, CQL and IQL are taken from (Kostrikov et al., 2021b) with additional comparisons provided in Appendix D.

Dataset	BC	CQL	IQL	TD3-BC	TD3-BC PR	TD3-BC FT	TD3-BC PR-FT
halfcheetah-med	42.6	44.0	47.4	48.5 ±0.7	**55.3** ±0.8	74.5 ±2.1	74.4 ±2.4
hopper-med	52.9	58.5	66.3	56.6 ±9.4	**100.1** ±2.8	93.7 ±20.6	102.8 ±0.9
walker2d-med	75.3	72.5	78.3	83.3 ±7.0	**89.1** ±1.7	105.5 ±2.6	101.2 ±3.6
halfcheetah-med-rep	36.6	45.5	44.2	44.5 ±0.8	**48.7** ±1.2	68.0 ±2.6	69.8 ±1.7
hopper-med-rep	18.1	95.0	94.7	55.2 ±24.6	**100.5** ±1.2	102.8 ±1.8	103.4 ±1.7
walker2d-med-rep	26.0	77.2	73.9	82.5 ±13.6	**87.9** ±2.8	106.6 ±2.9	103.9 ±8.1
halfcheetah-med-exp	55.2	91.6	86.7	91.5 ±15.8	**91.9** ±11.1	96.2 ±1.3	96.6 ±1.1
hopper-med-exp	52.5	105.4	91.5	101.6 ±23.2	**103.9** ±15.9	110.8 ±6.4	111.2 ±5.6
walker2d-med-exp	107.5	108.8	109.6	110.4 ±0.4	**112.7** ±0.3	117.8 ±1.2	119.1 ±2.8
halfcheetah-exp	-	-	-	97.1 ±1.4	**97.5** ±1.1	96.7 ±2.1	97.7 ±1.8
hopper-exp	-	-	-	112 ±1.0	**112.4** ±0.8	111.8 ±0.8	111.9 ±0.7
walker2d-exp	-	-	-	110.2 ±0.2	**113.0** ±0.5	120.0 ±1.7	121.4 ±1.9

Table 1: Comparison of results for D4RL benchmark using -v2 data sets. Offline learning: refined policies (PR) match or exceed the performance of TD3-BC baseline and competing methods, particularly for medium/medium-replay tasks. Online learning: Fine-tuning policies (FT) continues to improve performance. Figures are mean normalised scores ± one standard deviation across 50 evaluations (10 evaluations across 5 random seeds). Bold indicates the highest mean for offline learning.

For offline learning we see the simple act of policy refinement produces policies that outperform the original baseline. This is particularly the case when data is sub-optimal, i.e. medium/medium-replay or where TD3-BC performs poorly, i.e. hopper-medium/medium-replay. For data sets where TD3-BC already achieves expert or near-expert performance, refined policies match or exceed this. TD3-BC is now able to compete with or surpass other leading methods across all tasks, despite being the simplest to implement.

In terms of online learning we see from Table 1 that both baseline and refined policies benefit from fine-tuning. In Figure 2 we plot the corresponding learning curves and (un-normalised) scores across the 5 random seeds, where evaluation takes place every 5k environment interactions. The solid line represents the mean, shaded area ± one standard deviation and dashed line performance prior to fine tuning. We see in general that learning is relatively stable with very few catastrophic performance drops, comparable to results presented in (Zhao et al., 2021) despite being much more straightforward. The only exception to this is hopper-medium-expert which takes nearly the entire training period to stabilise.

Figure 2: Learning curves for online fine-tuning. For all but hopper-medium-expert fine-tuning is reasonably stable with very few sudden performance drops. This is the case for both baseline policies (blue) and refined policies (green).

6 DISCUSSION, LIMITATIONS AND FUTURE WORK

In our experiments we have shown that simple approaches to offline learning and online fine-tuning can produce policies that match or exceed more complex alternatives. The policy improvement procedure set out in Section 4 allows TD3-BC to overcome some of its shortcoming relating to sub-optimal data, while still adhering to the core principles of minimalism. Resulting policies can, for the most part, be fine-tuned online with little or no detrimental impact on performance.

There are however several limitations to our work. First, our policy refinement process is sensitive to the value of λ, particularly for the medium-expert data sets (see Appendix E). While we note much published research in offline-RL reports results for optimised hyperparameters across tasks, such a procedure is unrealistic for real-world applications where online fine-tuning is limited or prohibited. Second, our fine-tuning procedure isn't completely immune to performance drops, which may be considered unacceptable for high-risk environments. Finally, we have only applied our method to dense-reward environments, but equally important are those where rewards are sparse.

In future work we look to address these shortcomings, devising methods to tune and/or set the value of λ offline and provide more stability during online fine-tuning, as well as evaluate both procedures in sprase-reward/goal-conditioned settings. We also hope to provide a theoretical analysis to complement our empirical results. In addition, we plan to incorporate policy refinement into online reinforcement learning as a means to improve data efficiency.

7 CONCLUSION

In this work we have highlighted the potential of simple approaches for offline reinforcement learning and subsequent online fine-tuning. We have shown how deficiencies with TD3-BC can be overcome using a policy refinement procedure and how policies can be fine-tuned online in a relatively stable manner. We have discussed limitations of our work and directions for future research.

ACKNOWLEDGEMENTS

We would like to acknowledge Weights & Biases (Biewald, 2020) as the online platform we used for experiment tracking and visualizations to develop insights for this paper.

REFERENCES

Arthur Argenson and Gabriel Dulac-Arnold. Model-based offline planning. *arXiv preprint arXiv:2008.05556*, 2020.

Lukas Biewald. Experiment tracking with weights and biases, 2020. URL `https://www.wandb.com/`. Software available from wandb.com.

David Brandfonbrener, Will Whitney, Rajesh Ranganath, and Joan Bruna. Offline rl without off-policy evaluation. *Advances in Neural Information Processing Systems*, 34:4933–4946, 2021.

Lili Chen, Kevin Lu, Aravind Rajeswaran, Kimin Lee, Aditya Grover, Misha Laskin, Pieter Abbeel, Aravind Srinivas, and Igor Mordatch. Decision transformer: Reinforcement learning via sequence modeling. *Advances in neural information processing systems*, 34:15084–15097, 2021.

Justin Fu, Aviral Kumar, Ofir Nachum, George Tucker, and Sergey Levine. D4rl: Datasets for deep data-driven reinforcement learning. *arXiv preprint arXiv:2004.07219*, 2020.

Scott Fujimoto and Shixiang Shane Gu. A minimalist approach to offline reinforcement learning. *arXiv preprint arXiv:2106.06860*, 2021.

Scott Fujimoto, Herke Hoof, and David Meger. Addressing function approximation error in actor-critic methods. In *International Conference on Machine Learning*, pp. 1587–1596. PMLR, 2018.

Scott Fujimoto, David Meger, and Doina Precup. Off-policy deep reinforcement learning without exploration. In *International Conference on Machine Learning*, pp. 2052–2062. PMLR, 2019.

Michael Janner, Yilun Du, Joshua B Tenenbaum, and Sergey Levine. Planning with diffusion for flexible behavior synthesis. *arXiv preprint arXiv:2205.09991*, 2022.

Rahul Kidambi, Aravind Rajeswaran, Praneeth Netrapalli, and Thorsten Joachims. Morel: Model-based offline reinforcement learning. *arXiv preprint arXiv:2005.05951*, 2020.

Ilya Kostrikov, Rob Fergus, Jonathan Tompson, and Ofir Nachum. Offline reinforcement learning with fisher divergence critic regularization. In *International Conference on Machine Learning*, pp. 5774–5783. PMLR, 2021a.

Ilya Kostrikov, Ashvin Nair, and Sergey Levine. Offline reinforcement learning with implicit q-learning. *arXiv preprint arXiv:2110.06169*, 2021b.

Aviral Kumar, Justin Fu, George Tucker, and Sergey Levine. Stabilizing off-policy q-learning via bootstrapping error reduction. *arXiv preprint arXiv:1906.00949*, 2019.

Aviral Kumar, Aurick Zhou, George Tucker, and Sergey Levine. Conservative q-learning for offline reinforcement learning. *arXiv preprint arXiv:2006.04779*, 2020.

Sascha Lange, Thomas Gabel, and Martin Riedmiller. Batch reinforcement learning. In *Reinforcement learning*, pp. 45–73. Springer, 2012.

Sergey Levine, Aviral Kumar, George Tucker, and Justin Fu. Offline reinforcement learning: Tutorial, review, and perspectives on open problems. *arXiv preprint arXiv:2005.01643*, 2020.

Ashvin Nair, Bob McGrew, Marcin Andrychowicz, Wojciech Zaremba, and Pieter Abbeel. Overcoming exploration in reinforcement learning with demonstrations. In *2018 IEEE international conference on robotics and automation (ICRA)*, pp. 6292–6299. IEEE, 2018.

Ashvin Nair, Abhishek Gupta, Murtaza Dalal, and Sergey Levine. Awac: Accelerating online reinforcement learning with offline datasets. *arXiv preprint arXiv:2006.09359*, 2020.

Kihyuk Sohn, Honglak Lee, and Xinchen Yan. Learning structured output representation using deep conditional generative models. *Advances in neural information processing systems*, 28: 3483–3491, 2015.

Richard S Sutton and Andrew G Barto. *Reinforcement learning: An introduction*. MIT press, 2018.

Emanuel Todorov, Tom Erez, and Yuval Tassa. Mujoco: A physics engine for model-based control. In *2012 IEEE/RSJ International Conference on Intelligent Robots and Systems*, pp. 5026–5033. IEEE, 2012.

Yifan Wu, George Tucker, and Ofir Nachum. Behavior regularized offline reinforcement learning. *arXiv preprint arXiv:1911.11361*, 2019.

Tianhe Yu, Aviral Kumar, Rafael Rafailov, Aravind Rajeswaran, Sergey Levine, and Chelsea Finn. Combo: Conservative offline model-based policy optimization. *arXiv preprint arXiv:2102.08363*, 2021.

Yi Zhao, Rinu Boney, Alexander Ilin, Juho Kannala, and Joni Pajarinen. Adaptive behavior cloning regularization for stable offline-to-online reinforcement learning. 2021.

A POLICY REFINEMENT AND ONLINE-TUNING PROCEDURES

Let θ_i and $\theta_i^{'}$ represent parameters for i Q-networks and target Q-networks, respectively. Let ϕ and ϕ' represent parameters for a policy network and target policy network, respectively. Let B be a sample of transitions from a replay buffer, α a BC regulariser and τ a target network update rate

Define Q-networks update via gradient descent:

$$\nabla_{\theta_i} \frac{1}{|B|} \sum_{(s,a,r,s') \in B} \left(Q_{\theta_i} - r - \gamma \min_{i=1,2} Q_{\theta_i}(s', a') \right)^2 \tag{2}$$

where $a' = \text{clip}(\pi_{\phi'}(s') + \text{noise}, \text{-0.5}, \text{0.5})$ and noise is sampled from an $N(0, \epsilon)$ distribution.

Define policy network update via gradient ascent:

$$\nabla_{\phi} \frac{1}{|B|} \sum_{(s,a) \in B} Q_{\theta_1}\left(s, \pi_\phi(s)\right) - \left(\pi_\phi(s) - a\right)^2 \tag{3}$$

Define target network updates via polyak averaging:

$$\begin{aligned} \theta_i^{'} &\leftarrow \tau\theta_i + (1 - \tau)\theta_i^{'} \\ \phi^{'} &\leftarrow \tau\phi + (1 - \tau)\phi^{'} \end{aligned} \tag{4}$$

With these updates defined we outline TD3-BC, policy improvement and online fine-tuning in Algorithm 1:

Algorithm 1 TD3-BC with policy refinement and/or online fine-tuning

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Require: Dataset D, discount factor γ, target update rate τ, policy noise ϵ and BC regulariser α
Initialise critic parameters θ_i, policy parameters ϕ and corresponding target parameters θ_i', ϕ'.

TD3-BC
for $j = 0$ to J **do**
    Sample minibatch of transitions (s, a, r, s') from D
    Update critic parameters θ_i using equation (2)
    Update policy parameters ϕ using equation (3)
    Update target network parameters θ_i', ϕ' using equations (4)
end for

Policy refinement
Set scaling factor λ and replace α with α' as per equation 1
for $k = 0$ to K **do**
    Sample minibatch of transitions (s, a, r, s') from D
    Update policy parameters ϕ using equation (3)
    Update target network parameters ϕ' using equations (4)
end for

Online fine-tuning
Initialise environment and replay buffer R. Set exploration noise σ and decay parameters $\alpha_{start}, \alpha_{end}$
Set decay rate $\kappa_\alpha = \exp\left[\frac{1}{N}\log\left(\frac{\alpha_{end}}{\alpha_{start}}\right)\right]$
for $m = 0$ to M **do**
    Act in environment with exploration, $a \sim \pi_\phi(s) + N(0, \sigma)$
    Store resulting transitions (s, a, r, s') in R
end for
for $n = 0$ to N **do**
    Act in environment with exploration, $a \sim \pi_\phi(s) + N(0, \sigma)$
    Sample minibatch of transitions (s, a, r, s') from R
    Update critic parameters θ_i using equation (2)
    Update policy parameters ϕ using equation (3)
    Update target network parameters θ_i', ϕ' using equations (4)
    Update decay rate $\alpha \leftarrow \kappa_\alpha \alpha$
end for

B EXPERIMENTAL DETAILS

TD3-BC hyperparameters and network architecture
In the original TD3-BC (Fujimoto & Gu, 2021) the hyperparamater α is attached to Q-values but since our focus in the BC component we attach to the MSE. This is an equivalent set-up if $\alpha = 0.4$, the inverse of the original value $\alpha = 2.5$. All other details are the same, as per Table 2

Policy refinement hyperparameter
Table 3 reiterates the value of the scaling parameter λ used in our experiments.

Offline policy evaluation procedure
Policy evaluation takes place online in the simulated MuJoCo environment. The reported results are mean normalised scores $\pm$ one standard deviation across evaluations and seeds, where scores of 0 and 100 represent random and expert policies, respectively. Further details can be found in the D4RL paper (Fu et al., 2020).

Online policy evaluation procedure
Policy evaluation takes place online in the simulated MuJoCo environment. The reported results are mean un-normalised scores $\pm$ one standard deviation across seeds

	Hyperparameter	Value
	Optimizer	Adam
	Actor learning rate	3e-4
	Critic learning rate	3e-4
	Batch size	256
	Discount factor γ	0.99
TD3-BC	Target network update rate τ	0.005
	Policy noise ϵ	0.2
	Policy noise clipping	(-0.5, 0.5)
	Critic-to-Actor update ratio	2:1
	BC regulariser α	0.4
	Exploration noise σ	0.1
TD3-BC online	α_{start}	0.4
	α_{end}	0.2
	Critic hidden nodes	256
	Critic hidden layers	2
	Critic hidden activation	ReLU
	Critic input	State + Action
	Critic output	Q-value
Architecture	Actor hidden nodes	256
	Actor hidden layers	2
	Actor hidden activation	ReLU
	Actor input	State
	Actor outputs	Action (tanh transformed)

Table 2: TD3-BC hyperparameters and network architecture

Dataset	Scaling factor λ
halfcheetah-medium	5
hopper-medium	5
walker2d-medium	5
halfcheetah-medium-replay	5
hopper-medium-replay	5
walker2d-medium-replay	5
halfcheetah-medium-expert	1
hopper-medium-expert	1
walker2d-medium-expert	5
halfcheetah-expert	1
hopper-expert	5
walker2d-expert	5

Table 3: Policy refinement scaling factor λ

Hardware All experiments were conducted on a single machine with the following hardware specification: Intel Core i9 9900K CPU, 64GB RAM, 1TB SSD, 2x NVIDIA GeForce RTX 2080Ti 11GB TURBO GPU.

C ABLATIONS

In Section 4 we note two key designs decisions as part of policy refinement. The first is reducing the value of α after initial training, allowing us to choose values that at the start would be too low. The second is only training the policy while keep the critic fixed in efforts to prevent overestimation bias reappearing. To check the relative importance of each of these we carry out the following ablations:

- Ablation 1: Run baseline TD3-BC with the value of α' from Section 5
- Ablation 2: During policy refinement train both the policy and critic. Note, to reach an equivalent 250k policy updates the total additional gradient steps is 500k as the critic-actor update ratio is 2:1.

For completeness we also run the baseline TD3-BC with $\alpha = 0.4$ for 1.5M gradient steps (1.5M critic, 750k policy) to show additional training alone isn't the cause of policy improvements. We denote this Ablation 3.

Results are summarised in Table 4. Ablation 1 results show that while setting $\alpha = \alpha'$ works for a few data sets, for most this leads to a collapse in learning and highly sub-optimal policies. Ablation 2 results show that training the policy and critic leads to collapse for certain data sets, and even when it doesn't the results aren't as strong as training the policy alone. Ablation 3 results show additional training alone can't match the performance of policy refinement when data sets are sub-optimal (medium/medium-replay).

Dataset	TD3-BC Refined	Ablation 1	Ablation 2	Ablation 3
halfcheetah-med	55.3 ±0.8	55.9 ±1.0	55.7 ±1.2	48.2 ±0.7
hopper-med	100.1 ±2.8	14.8 ±9.8	100.8 ±0.6	62.5 ±13.4
walker2d-med	89.1 ±1.7	5.0 ±7.9	48.8 ±38.6	82.9 ±10.1
halfcheetah-med-rep	48.7 ±1.2	50.2 ±1.1	49.4 ±1.0	44.6 ±0.7
hopper-med-rep	100.5 ±1.2	90.6 ±9.4	88.0 ±23.6	55.9 ±25.2
walker2d-med-rep	87.9 ±2.8	41.9 ±34.6	70.6 ±35.1	77.1 ±21.3
halfcheetah-med-exp	91.9 ±11.1	91.5 ±15.8*	95.5 ±2.2**	95.5 ±2.2
hopper-med-exp	103.9 ±15.9*	101.6 ±23.2	91.6 ±27.8**	91.6 ±27.8
walker2d-med-exp	112.7 ±0.3	22.6 ±44.4	3.9 ±4.7	109.8 ±0.9
halfcheetah-exp	97.5 ±1.1	97.1 ±1.4*	97.6 ±1.4**	97.6 ±1.4
hopper-exp	112.4 ±0.8	2.9 ±2.3	111.1 ±8.5	111.7 ±0.7
walker2d-exp	113.0 ±0.5	4.5 ±5.1	112.7 ±0.3	110.5 ±0.1

Table 4: Ablation studies investigating the importance of design decisions in policy refinement. While some data sets are agnostic to these choices, in general they are required to attain the performance levels reported in the main paper. Note results marked with a single asterisk are the same as baseline TD3-BC and results marked with a double asterisk are the same as Ablation 3 (as $\lambda = 1$ for these data sets).

D ADDITIONAL COMPARISONS FOR OFFLINE-RL

In Table 5 we provide additional comparisons for a range of offline approaches, including some model-based methods not covered in Section 3. Specifically we compare to:

- Advantage weighted actor-critic (AWAC) (Nair et al., 2020)
- One-step Exp. Weight (OnestepRL) (Brandfonbrener et al., 2021)
- Decision Transformer (DT) (Chen et al., 2021)
- Diffuser (Janner et al., 2022)
- CQL + Model Based Policy Optimization (COMBO) (Yu et al., 2021)
- Model-based Offline Reinforcement Learning (MOReL) (Kidambi et al., 2020)
- Model-based Offline Planning (MBOP) (Argenson & Dulac-Arnold, 2020)

We note some comparisons aren't directly equivalent due to differences in data sets, using -v0 instead of -v2. Since we use the latest -v2 we mark -v0 approaches with an asterisk. AWAC, OnestepRL and DT are taken from (Kostrikov et al., 2021b) with Diffuser, COMBO, MOReL and MBOP taken from their respective papers. As can be seen, TD3-BC-PR remains competitive despite its minimalist approach.

Dataset	TD3-BC-PR	AWAC	OnestepRL	DT	Diffuser	COMBO*	MOReL*	MBOP*
halfcheetah-med	55.3 ±0.8	43.5	48.4	42.6	44.2	54.2	42.1	44.6
hopper-med	100.1 ±2.8	57.0	59.6	67.6	58.5	97.2	95.4	48.8
walker2d-med	89.1 ±1.7	72.4	81.8	74.0	79.7	81.9	77.8	41.0
halfcheetah-med-rep	48.7 ±1.2	40.5	38.1	36.6	42.2	55.1	40.2	42.3
hopper-med-rep	100.5 ±1.2	37.2	97.5	82.7	96.8	89.5	93.6	12.4
walker2d-med-rep	87.9 ±2.8	27.0	49.5	66.6	61.2	56.0	49.8	9.7
halfcheetah-med-exp	91.9 ±11.1	42.8	93.4	86.8	79.8	90.0	53.3	105.9
hopper-med-exp	103.9 ±15.9	55.8	103.3	107.6	107.2	111.1	108.7	55.1
walker2d-med-exp	112.7 ±0.3	74.5	113.0	108.1	108.4	103.3	95.6	70.2

Table 5: Additional comparisons for offline D4RL tasks. Despite many of these methods being more complex and computationally expensive, TD3-BC-PR remains competitive across all tasks. Note results for -expert data sets are not reported for these alternative methods

E MEDIUM-EXPERT PERFORMANCE FOR $\lambda = 5$

Dataset	TD3-BC-PR
halfcheetah-medium-expert	63.0 ±27.1
hopper-medium-expert	69.3 ±39.7

Table 6: Policy refinement for hopper and halfcheetah medium-expert dataset when $\lambda = 5$. Performance is significantly worse than TD3-BC baseline