Information Directed Reward Learning for Reinforcement Learning

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Abstract

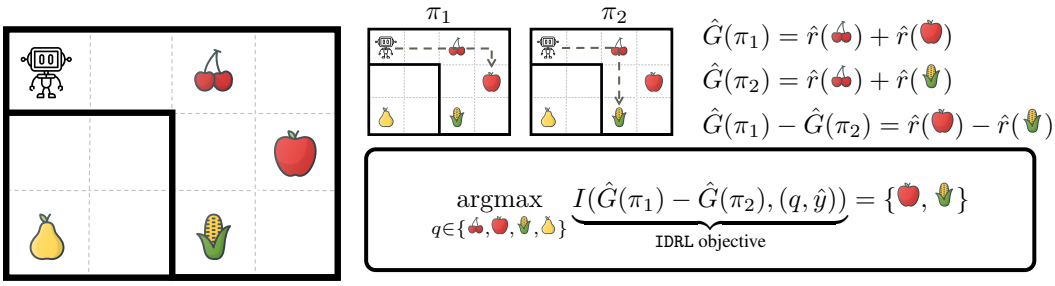
For many reinforcement learning (RL) applications, specifying a reward is difficult. This paper considers an RL setting where the agent obtains information about the reward only by querying an expert that can, for example, evaluate individual states or provide binary preferences over trajectories. From such expensive feedback, we aim to learn a model of the reward that allows standard RL algorithms to achieve high expected returns *with as few expert queries as possible*. To this end, we propose *Information Directed Reward Learning* (IDRL), which uses a Bayesian model of the reward and selects queries that maximize the information gain about the difference in return between plausibly optimal policies. In contrast to prior active reward learning methods designed for specific types of queries, IDRL naturally accommodates different query types. Moreover, it achieves similar or better performance with significantly fewer queries by shifting the focus from reducing the reward approximation error to improving the policy induced by the reward model. We support our findings with extensive evaluations in multiple environments and with different query types.

1 Introduction

Reinforcement learning (RL, Sutton and Barto, 2018) casts the problem of learning to perform complex tasks by interacting with an environment as an optimization problem where the learning agent aims to maximize its expected cumulative reward. Despite the remarkable successes of RL (e.g., Mnih et al., 2015; Silver et al., 2016), specifying reward functions that capture complex tasks is still an open problem. A promising approach is to *learn* a reward function from human feedback (e.g., Christiano et al., 2017). However, since human feedback is expensive, *active reward learning* aims to minimize the number of queries. Prior work often focuses on approximating the reward function uniformly well. However, this may not be aligned with the original goal of RL: *finding an optimal policy*, as Figure 1 shows. Moreover, prior work is often tailored to specific types of queries, such as comparisons of two trajectories (e.g., Sadigh et al., 2017) or numerical evaluations of trajectories (e.g., Daniel et al., 2015), limiting its applicability.

Contributions. We propose *Information Directed Reward Learning* (IDRL), a general *active reward learning* approach for learning a model of the reward function from expensive feedback with the goal of *finding a good policy* rather than uniformly reducing the model's error. IDRL can use arbitrary Bayesian reward models and arbitrary types of queries (Section 4), making it more general than existing methods. We describe an exact and efficient implementation of IDRL using Gaussian process (GP) reward models (Section 5) and different types of queries, and an approximation of IDRL that uses a deep neural network reward model and a state-of-the-art policy gradient algorithm to learn from comparison queries (Section 6). We evaluate IDRL extensively in simulated environments (Section 7), including a driving task and high-dimensional continuous control tasks in the MuJoCo simulator, and show that both implementations significantly outperform prior methods.

Submitted to 35th Conference on Neural Information Processing Systems (NeurIPS 2021). Do not distribute.



$T = 4$

Figure 1: The robot wants to collect food for a human. It can only move 4 timesteps in the gridworld, and collecting more food is always better. The robot does not know the human's preferences, but it can ask for food ratings. Common active learning methods aim to learn the reward uniformly well, and would query all items similarly often. In contrast, `IDRL` considers only the two plausibly optimal policies π_1 and π_2. Since both policies collect the cherry, and do not collect the pear, the robot only needs to learn about the apple and the corn. `IDRL` can solve the task with 2 queries instead of 4.

2 Related work

Reward Learning for RL. Several works aim to directly learn policies rather than reward functions from expert feedback in the form of numerical evaluations (Knox and Stone, 2009; MacGlashan et al., 2017) or comparisons (Regan and Boutilier, 2009; Fürnkranz et al., 2012), and some work also explores active query selection (Akrour et al., 2012; Wilson et al., 2012). However, learning policies directly from feedback has several downsides: it is difficult to combine different types of feedback, and policies tend to generalize poorly between environments. Ng and Russell (2000) argue that reward functions are a more robust representation of desired behavior than policies. *Inverse reinforcement learning* (IRL) aims to learn a reward model from expert demonstrations (Abbeel and Ng, 2004). Reward models can also be learned from comparisons of two or more different behaviors (Wirth et al., 2017), or other kinds of feedback (Jeon et al., 2020). While reward models can successfully learn hard-to-specify control and game-playing tasks (Christiano et al., 2017; Ibarz et al., 2018), most work uses simple heuristics to select queries to make. In contrast, *active reward learning* aims to select the most informative queries in a principled way.

Active reward learning. For linear reward functions, Sadigh et al. (2017) ask the expert to compare trajectories synthesized to maximize the volume removed from a hypothesis space. Bıyık et al. (2020b) argue that maximizing information gain leads to better sample efficiency and queries that are easier to answer than volume removal. Bıyık et al. (2020a) generalize maximizing information gain to non-linear reward functions using a GP model. We also use an information gain objective to select queries; however, our approach focuses on finding an optimal policy instead of uniformly reducing the error of the reward model. With a similar motivation, Wilde et al. (2020) aim to capture how informative a query is for distinguishing policies. However, their method is limited to comparisons between potentially optimal policies. Daniel et al. (2015) also introduce an acquisition function to measure how informative a query is for learning a good policy. However, their setting is restricted to observing the cumulative reward of a trajectory, and their acquisition function is computationally expensive. Table 1 gives an overview of how our method compares to this prior work.

Bayesian optimization. *Bayesian optimization* (BO) aims to maximize an expensive-to-evaluate function by learning a Bayesian model of the function and selecting informative queries (Mockus et al., 1978). We face a related but significantly harder problem: we aim to find an optimal policy in RL but only *indirectly* obtain information about the value of policies. Our problem has striking connections to variants of the *multi-armed bandit problem* (Bubeck and Cesa-Bianchi, 2012), in particular *partial monitoring problems* (Rustichini, 1999) and *transductive linear bandits* (Fiez et al., 2019). We explore this connection in detail in Appendix C.

3 Background and problem setting

Markov decision process. Markov decision processes (MDPs, Puterman, 2014) model sequential decision-making problems in dynamical systems. An MDP $(\mathcal{S}, \mathcal{A}, P, r, q, \gamma)$ consists of a state space $\mathcal{S}$, an action space $\mathcal{A}$, a transition function P, a reward function r, an initial state distribution q, and a discount factor $\gamma \in [0, 1)$. In an MDP, the

	Non-linear Rewards	Single-state Queries	Trajectory Queries	Numerical Queries	Comparison Queries	Considers Env. Dynamics
Sadigh et al. (2017)	✗	✗	✓	✗	✓	✗
Bıyık et al. (2020b)	✗	✗[1]	✓	✗[1]	✓	✗
Bıyık et al. (2020a)	✓	✗[1]	✓	✗[1]	✓	✗
Daniel et al. (2015)	✓	✗[1]	✓	✓	✗[1]	✓
Wilde et al. (2020)	✗	✗	✓	✗	✓	✓
IDRL (ours)	✓	✓	✓	✓	✓	✓

[1] The original authors do not consider this setting, but we provide an extension to their method in Section 7 and Appendix D.

Table 1: In contrast to most prior work on active reward learning for RL, IDRL can handle non-linear reward functions and different query types, in particular numerical evaluations and comparisons of individual states and (partial) trajectories. Further, IDRL takes the environment dynamics into account to achieve better sample efficiency (cf. Figure 1).

agent starts in state $s_0 \sim q(s)$ and, when taking action a_t, transitions from state s_t to state s_{t+1} with probability $P(s_{t+1}|s_t, a_t)$. The agent affects the environment through actions determined by a policy $\pi(a_t|s_t)$, indicating the probability of taking action a_t in state s_t. The agent's goal is to find a policy π that maximizes the *expected discounted return* $G(\pi) = \mathbb{E}_{P,\pi,q}\left[\sum_{t=0}^{\infty} \gamma^t r_t\right]$.

Problem setting. We focus on MDPs where the reward function is not readily available. Instead, the agent can query an expert for information about the reward. In iteration i, the agent makes a query q_i to the expert, and receives a response y_i. For example, q_i could ask the expert to compare two trajectories or judge a single trajectory, and y_i could indicate which of the two trajectories is better or provide the return of a single trajectory. However, queries to the expert are *expensive*, and the agent has to find a policy π that *maximizes the expected return* $G(\pi)$ using *as few queries as possible*.

Our reward learning approach. We approach this problem by learning a model of the reward function, i.e., a model that predicts the reward of a given state,[1] and computing a policy that maximizes the return induced by the model. Importantly, we want to learn a reward model such that the induced optimal policy achieves a high return under the true reward function. Note that any RL algorithm can be used to find the policy. Hence, the problem reduces to selecting a model for the reward function and deciding which queries to make. Our key insight is that queries that help most to find a good policy might differ from those that uniformly reduce the model's uncertainty.

4 The Information Directed Reward Learning acquisition function

This section introduces Information Directed Reward Learning (IDRL) for a general Bayesian model of the reward and discusses how to select queries q_i, making no assumptions on their form nor on the responses y_i.

Reward model. To select informative queries, we need to quantify uncertainty; hence, we use a Bayesian model of the reward function. From a Bayesian perspective, it is important to distinguish between the agent's belief about a quantity and its "actual" value that is unknown to us. We denote the belief about the reward in state s with $\hat{r}(s)$ and its actual value with $r(s)$.

Query selection. To select informative queries, we have to consider that the responses might only give *indirect* information about the set of optimal policies. For example, assume the agent can ask the expert to quantify the reward of individual states. These rewards provide information about the expected return of a policy but may yield no information about the set of optimal policies. For example, if a state is visited similarly often by every plausibly optimal policy, knowing its reward does not help decide between the policies (e.g., the cherry in Figure 1). Therefore, any approach that only aims to reduce the uncertainty of the reward model may waste expensive queries that do not help find an optimal policy.

Intuitively, we want to instead select queries that *help identify the optimal policy*. In the language of information theory, we want to maximize the *information gain* of a query about *the identity of the optimal policy*. More formally, let us denote with $P(\hat{\pi}^*|\mathcal{D})$ our belief about the optimal policy, induced by our belief about the reward function $\hat{r}$, and let $\mathcal{Q}_c$ be a set of candidate queries the agent can make. Then, one way to formalize this intuition is to select queries

[1] Our approach is also applicable to reward functions that depend on state-action pairs or transitions. We focus on state-dependent reward functions for simplicity of exposition.

Algorithm 1 *Information Directed Reward Learning* (`IDRL`). The algorithm requires a set of candidate queries $\mathcal{Q}_c$, a Bayesian model of the reward function, and an RL algorithm that returns a policy given a reward function. $\hat{G}(\pi)$ is the belief about the expected return of policy π, induced by the reward model $P(\hat{r}|\mathcal{D})$, and $\hat{r}$ is the belief about the reward function.

$\mathcal{D} \leftarrow \{\}$; $\Pi_c \leftarrow$ initialize candidate policies; initialize reward model with prior distribution $P(\hat{r})$
while not converged **do**
  Select a query:
    $\pi_1, \pi_2 \in \text{argmax}_{\pi,\pi' \in \Pi_c} H(\hat{G}(\pi) - \hat{G}(\pi')|\mathcal{D})$
    $q^* \in \text{argmax}_{q \in \mathcal{Q}_c} I(\hat{G}(\pi_1) - \hat{G}(\pi_2); (q, \hat{y})|\mathcal{D})$
  Query q^* and update reward model:
    $y^* \leftarrow$ Response to query q^*
    $P(\hat{r}|\mathcal{D} \cup \{(q^*, y^*)\}) \propto P(y^*|\hat{r}, \mathcal{D}, q^*)P(\hat{r}|\mathcal{D})$
    $\mathcal{D} \leftarrow \mathcal{D} \cup \{(q^*, y^*)\}$
  Optionally update candidate policies Π_c
end while
$\bar{r} \leftarrow$ mean estimate of the reward model; $\bar{\pi}^* \leftarrow \texttt{RL}(\bar{r})$
return $\bar{\pi}^*$

$q^* \in \text{argmax}_{q \in \mathcal{Q}_c} I(\hat{p}^*; (q, \hat{y})|\mathcal{D})$, where $\hat{y}$ is the agent's belief about the response it will get to query q, and $\mathcal{D} = \{(q_1, y_1), \ldots, (q_{t-1}, y_{t-1})\}$ is a set of past queries and responses. Unfortunately, this objective has two undesirable properties. First, the agent has to keep track of a distribution over all possible policies to compute it, which is intractable in general. Second, reducing uncertainty about the optimal policy only matters as long as there are significant differences in the return of plausibly optimal policies. For example, if the agent identifies a set of plausibly optimal policies with similar returns, we care less about identifying exactly which policy is optimal, compared to when such policies have very different returns.

To address the first challenge, we obtain a finite set of *candidate policies* Π_c that are *plausibly optimal* according to our Bayesian reward model. To address the second challenge, we select the most informative query for distinguishing policies in terms of their value.

Let us first discuss how to select queries, assuming a set of plausibly optimal policies Π_c to be available. We can exploit the fact that the belief about the reward function $\hat{r}$ induces a belief about the expected return of policy $\pi \in \Pi_c$, denoted as $\hat{G}(\pi)$. Concretely, the expected return of a policy is given by $G(\pi) = \langle \mathbf{f}^\pi, \mathbf{r} \rangle$, where $\mathbf{f}^\pi$ is a vector of the (discounted) expected state-visitation frequencies of policy π and $\mathbf{r}$ is a vector of rewards of the corresponding states. We can estimate $\mathbf{f}^\pi$ from trajectories sampled using policy π, and then determine $\hat{G}(\pi)$ from $\hat{r}$.

Given $\hat{G}(\pi)$, `IDRL` proceeds in two steps. It first selects two policies that maximize the model's uncertainty about the difference in their expected returns:

$$\pi_1, \pi_2 \in \underset{\pi,\pi' \in \Pi_c}{\text{argmax}}\, H(\hat{G}(\pi) - \hat{G}(\pi')|\mathcal{D}), \tag{1}$$

where H is the entropy of the belief conditioned on past queries. To gather information about the distinction between π_1 and π_2, `IDRL` then selects queries that maximize the information gain about the difference in expected return between π_1 and π_2:

$$q^* \in \underset{q \in \mathcal{Q}_c}{\text{argmax}}\, I(\hat{G}(\pi_1) - \hat{G}(\pi_2); (q, \hat{y})|\mathcal{D}). \tag{2}$$

Note that this is not the same as jointly maximizing the information gain about $\hat{G}(\pi_1)$ and $\hat{G}(\pi_2)$. Equation (2) prefers queries that help to distinguish π_1 and π_2 over queries that help to determine the exact value of $\hat{G}(\pi_1)$ and $\hat{G}(\pi_2)$. Assuming a set of optimal policies is contained in Π_c, reducing the uncertainty about the difference in returns within Π_c will help to identify an optimal policy quickly. In particular, if there is no remaining uncertainty about the differences in return, we can clearly identify an optimal policy.

Let us now discuss how to obtain a set of candidate policies Π_c. For `IDRL` to select informative queries, Π_c has to reflect the agent's current belief about optimal policies. `IDRL` uses Thompson sampling (TS, Thompson, 1933) as a flexible way to create Π_c. We implement TS by repeatedly sampling a reward function from the posterior reward model and finding an approximately optimal policy

for this sampled reward function. This approximates sampling from the posterior distribution over optimal policies. Since TS is demanding, in our experiments, we investigate two effective alternatives to alleviate its computational burden: (1) we update Π_c in regular intervals, rather than at every step, and (2) we start from the candidates computed in previous steps rather than starting the policy optimization from scratch.

Algorithm 1 shows the full IDRL algorithm. In each iteration, IDRL identifies two plausibly optimal policies with high uncertainty about their difference in return and then aims to reduce this uncertainty. We can stop the algorithm after a fixed number of queries, or by checking a convergence criterion, and return a policy $\bar{\pi}^*$ that is optimized for the current reward model.

Note that IDRL is agnostic to how the candidate queries $\mathcal{Q}_c$ are generated. Different applications might require different approaches to generating $\mathcal{Q}_c$. In our experiments, for example, we consider: using all possible queries in small environments, choosing states or trajectories to query from rollouts of the currently optimal policy $\bar{\pi}^*$, selecting queries from rollouts of the candidate policies, and selecting queries from trajectories of a pre-defined explorations policy. Importantly, all of these, and others, are compatible with IDRL.

5 An exact and efficient implementation of IDRL for GP reward models

Here, we describe one concrete implementation of IDRL using a Gaussian process (GP, Rasmussen and Williams, 2006) reward model and linear query types. These choices allow us to compute equations (1) and (2) exactly and efficiently.

Reward model. We model the reward function as a GP with (w.l.o.g.) a zero-mean prior distribution $\hat{r}(s) \sim \mathcal{GP}(0, k(s, s'))$ using a kernel k which measures the similarity of states.

Query selection. We first show how to compute equations (1) and (2) if the posterior belief about the reward function is Gaussian. Then, we discuss a family of practically relevant query types that satisfy this assumption. We provide proofs for all results in Appendix A.

Proposition 5.1. If $\hat{r}(s)|\mathcal{D}$ is a GP, then $P(\hat{G}(\pi) - \hat{G}(\pi')|\mathcal{D})$ is Gaussian and:

$$\operatorname*{argmax}_{\pi,\pi' \in \Pi_c} H(\hat{G}(\pi) - \hat{G}(\pi')|\mathcal{D}) = \operatorname*{argmax}_{\pi,\pi' \in \Pi_c} \mathrm{Var}[\hat{G}(\pi) - \hat{G}(\pi')|\mathcal{D}]$$

$$\operatorname*{argmax}_{q \in \mathcal{Q}_c} I(\hat{G}(\pi_1) - \hat{G}(\pi_2); (q, \hat{y})|\mathcal{D}) = \operatorname*{argmin}_{q \in \mathcal{Q}_c} \mathrm{Var}[\hat{G}(\pi_1) - \hat{G}(\pi_2)|\mathcal{D} \cup \{(q, \hat{y})\}]$$

We can compute both variances analytically, enabling exact implementation of equations (1) and (2).

Query types. To apply this result, we need $\hat{r}(s)|\mathcal{D}$ to be a GP, which is not the case for general observations (q_i, y_i). If the queries are individual states, i.e., $q_i = s_i$ and $y_i = r(s_i)$, the problem is standard GP regression, and $\hat{r}(s)|\mathcal{D}$ is a GP (Rasmussen and Williams, 2006). More generally, a similar statement holds if the observations are *linear* combinations of rewards.

Definition 5.1. We call $q = (S, C)$ a *linear reward query*, if it consists of states $S = \{s_1, \ldots, s_N\}$ and linear weights $C = \{c_1, \ldots, c_N\}$, and the response to query q is a linear combination of rewards $y = \sum_{j=1}^{N} c_j r(s_j) + \varepsilon$, with Gaussian noise $\varepsilon \sim \mathcal{N}(0, \sigma_n^2)$.

Proposition 5.2. Let q be a linear reward query. If the prior belief about the reward $\hat{r}(s)$ is a GP, then the posterior belief about the reward $\hat{r}(s)|(q, y)$ is also a GP.

Linear reward queries result in a particularly efficient implementation of IDRL. Of course, IDRL with a GP model could be extended to non-linear observations using approximate inference. However, it turns out that many commonly used query types can be modeled as linear reward queries, including the return of trajectories or comparisons of trajectories (see Appendix B).

6 A scalable Deep RL approximation of IDRL

GP models provide a convenient way to implement IDRL exactly. But, can IDRL also be used if we can not model the reward function as a GP? Moreover, can we scale it to large environments on the scale of typical Deep RL applications?

To address these questions, we propose a second implementation of IDRL using a deep neural network (DNN) reward model. To scale IDRL to large Deep RL scenarios, we integrate it into a

policy gradient algorithm, similar to Christiano et al. (2017).[2] Here, we focus on comparison queries, but the algorithm can easily be extended to other query types.

Reward model. To model the reward function, we use adaptive basis function regression with DNNs, similar to Snoek et al. (2015). Concretely, we train a DNN from comparisons of short clips of the agents behavior using the Bradley-Terry model and ℓ_2-regularization. We then treat the learned representation as a basis function and the final layer of the DNN as a maximum *a posteriori* (MAP) estimate of the parameters of a Bayesian logistic regression model. Finally, we approximate the full posterior using a Laplace approximation.

Query selection. The approximate posterior distribution of $\hat{r}(s)|\mathcal{D}$ is Gaussian, and we can compute equations (1) and (2) the same way we did for a GP reward model.

Query types. Similar to Christiano et al. (2017), we consider queries $q_i = (\sigma_i^1, \sigma_i^2)$ that compare two segments of trajectories σ_i^1 and σ_i^2, where the user responds with their preference $y_i \in \{-1, 1\}$.

Candidate policies. In large environments, it is infeasible to train new policies from scratch during the TS step. To avoid this, we maintain a fixed set of policies that we update regularly, instead of training new policies from scratch whenever we receive new samples.

Candidate queries. We generate candidate queries by rolling out the current policy optimized for the mean estimate of the reward model, and the candidate policies and uniformly sampling pairs of segments from the resulting trajectories.

Full algorithm. We use a policy gradient algorithm to train a policy for the current reward model, and the candidate policies. Similar to Christiano et al. (2017), the agent queries comparisons following a fixed schedule in which the number of samples is proportional to $\frac{1}{T}$, where T is the number of policy training steps, i.e., we provide more samples early during training and less later on. For more details, see Appendix E.3.

7 Experiments

We empirically test IDRL in several environments, ranging from gridworlds to complex continuous control tasks, and for several different query types, including numerical evaluations and comparisons of trajectories. Our evaluation covers most scenarios existing in the literature and shows that IDRL attains comparable or superior performance to methods designed for specific scenarios.

In all experiments, the agent's queries are answered with simulated feedback based on an underlying true reward function unknown to the agent. We usually evaluate the *regret* of a policy π trained using the reward model, i.e., $G(\pi^*) - G(\pi)$ for an optimal policy π^*. If we do not know π^*, we approximate it with a policy trained on the true reward function.

We first validate that GP-based IDRL improves sample efficiency in simple gridworld environments for numerical and comparison queries (Section 7.2). Next, we consider the most common setup in the literature, that is, learning from comparisons of trajectories, and compare GP-based IDRL against alternative approaches in a driving simulator, proposed in prior work (Section 7.3). Then, we study another natural feedback type: ratings of clips of the agent's behavior. In this setting, we demonstrate how GP-based IDRL can be scaled up to bigger environments in the MuJoCo simulator (Section 7.4). Finally, we further demonstrate scalability by considering the Deep RL implementation of IDRL to learn standard MuJoCo tasks from comparisons of clips of trajectories, similar to Christiano et al. (2017) (Section 7.5).

For each environment, we choose our setup to be close to prior work to promote a fair comparison. This leads to some design choices, such as the RL solver or the query types, to differ between environments. As a side effect, this highlights IDRL's generality. Appendices D and E describe the experimental setup in more detail, and we provide code to reproduce all experiments.

7.1 Baselines

We consider five baselines: (*i*) *Uniform sampling* selects queries from $\mathcal{Q}_c$ with equal probability. (*ii*) *Information gain on the reward* (IGR) selects queries that maximize information gain about the reward $I((q, \hat{y}); \hat{r}|\mathcal{D})$. For a GP model, this is equivalent to maximizing $\mathrm{Var}[\hat{y}|\mathcal{D}, q]$. Bıyık et al. (2020b) use IGR to learn rewards from comparisons of trajectories; however, it can be extended to other

[2] We provide a detailed comparison between our setup and Christiano et al. (2017) in Appendix E.3.

query types. (*iii*) *Expected improvement on the reward* (EIR) maximizes the improvement in the value of a query compared to the best observation so far, in *expectation*, and is a common acquisition function in BO (Mockus et al., 1978). EIR can not be applied to comparison queries. (*iv*) *Expected policy divergence* (EPD) is an active reward learning method introduced by Daniel et al. (2015), which makes queries that maximally change the current policy. Since EPD updates the policy for each potential observation, it is prohibitively expensive for large $\mathcal{Q}_c$. While EPD was introduced to query the return of trajectories, we extend it to other query types (cf. Appendix D). (*v*) *Maximum regret* (MR) is an acquisition function proposed by Wilde et al. (2020). It assumes access to a set of potential reward functions and corresponding optimal policies. MR compares policies that perform well according to one reward function but poorly according to a different one. It can only be used with comparisons of full trajectories. We also tested *expected volume removal* (EVR, Sadigh et al., 2017) for comparison queries; however, we found it to get stuck often, which confirms the findings of Bıyık et al. (2020b). Note that IGR and EIR reduce uncertainty uniformly over the state space, while EPD and MR consider the environment dynamics.

7.2 Can IDRL improve sample efficiency by considering the environment dynamics?

We first validate our hypothesis that IDRL improves sample efficiency in small toy environments. Here, we highlight experiments in a set of *Gridworlds* similar to Figure 1. Appendix F presents two additional toy environments that isolate specific reasons why IDRL outperforms the baselines.

Setup. We consider 10×10 *Gridworlds* with randomly placed walls and objects with different rewards. The agent has to find the object with the largest reward. We consider queries about the reward of individual states, i.e., $q_i = s_i \in \mathcal{S}$ and $y_i = r(s_i)$, and comparison queries with $q_i = (s_{i1}, s_{i2})$ and $y_i \in \{-1, 1\}$. The candidate queries $\mathcal{Q}_c$ either consist of all states or all pairs of states. We use GP-based IDRL, with a kernel that encodes which objects are the same, and which are different. All experiments run for less than 1 hour on a single CPU.

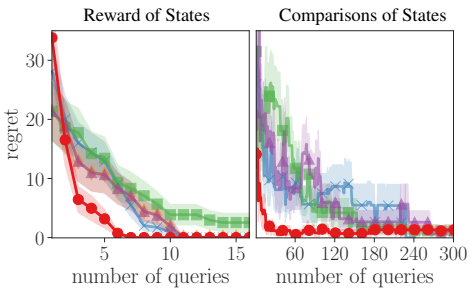


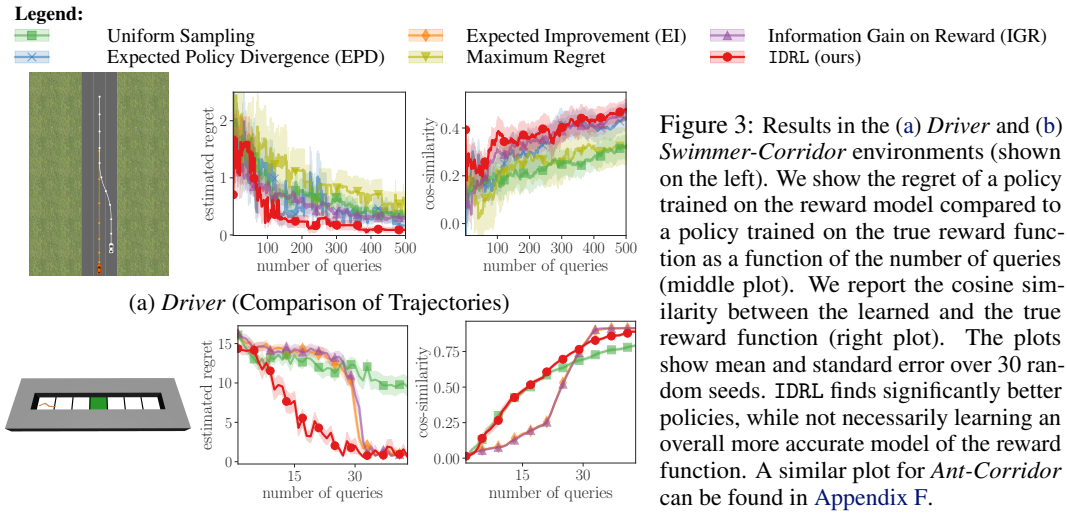
Figure 2: Regret of a policy trained in randomly generated gridworlds as a function of the number of queries. The queries are either asking about the reward of individual states, or comparisons between two states. The plot compares IDRL (●) to EPD (×), IGR (▲) and uniform sampling (■). For numerical queries, we also compare to EIR (◆), which is not applicable to comparisons. MR is not applicable to single-state queries.

Results. Figure 2 shows the regret of a policy trained on the reward model after different numbers of queries. IDRL finds better policies than the baselines with a limited number of queries because it focuses on regions of the state space relevant for finding the optimal policy. As shown in Figure 1, this improves sample efficiency over methods that uniformly reduce uncertainty, such as IGR and EIR. IDRL also outperforms EPD, because EPD's goal of selecting queries that maximally change the current policy is also misaligned with the goal of finding an optimal policy. We investigate EPD's specific failure modes in Appendix F.

7.3 Can IDRL learn from comparisons of trajectories using a GP reward model?

Most prior work studies reward learning from comparisons of trajectories. To evaluate IDRL in this setting, we consider the 2-dimensional, continuous *Driver* environment by Sadigh et al. (2017).

Setup. In *Driver*, the agent controls a car on a highway with another car driving on a fixed trajectory (cf. Figure 3a). For each experiment, we randomly sample an underlying (linear) reward function to describe the desired driving behavior. We use code by Sadigh et al. (2017) to simulate and solve the environment, but we adapt it to our setting. In contrast to Sadigh et al. (2017), we do not synthesize queries. Instead, we sample a fixed set of 200 reward functions from a Gaussian prior distribution. We then optimize a policy for each of these reward functions, and, similarly to Wilde et al. (2020), consider all pairs of policies as potential queries. Moreover, we assume a linear observation model (see Appendix B), whereas Sadigh et al. (2017) and Wilde et al. (2020) choose different non-linear observation models. Each experiment runs for less than 24 hours on a single CPU.



(a) *Driver* (Comparison of Trajectories)

(b) *Swimmer-Corridor* (Evaluation of Trajectory Clips)

Figure 3: Results in the (a) *Driver* and (b) *Swimmer-Corridor* environments (shown on the left). We show the regret of a policy trained on the reward model compared to a policy trained on the true reward function as a function of the number of queries (middle plot). We report the cosine similarity between the learned and the true reward function (right plot). The plots show mean and standard error over 30 random seeds. IDRL finds significantly better policies, while not necessarily learning an overall more accurate model of the reward function. A similar plot for *Ant-Corridor* can be found in Appendix F.

Results. Figure 3a shows the regret curves for the learned policy and the cosine similarity for the learned reward function weights. IDRL outperforms the baselines and finds a better policy with fewer queries. However, the difference to pure information gain is small in this simple environment.

7.4 Can IDRL with a GP model be scaled to bigger environments?

To demonstrate that GP-based IDRL scales to larger environments, we use the MuJoCo simulator (Todorov et al., 2012), which provides challenging environments commonly used as benchmarks for RL. However, its standard locomotion tasks are very easy to learn for a GP model because the reward is directly proportional to the agent's velocity in x-direction. Instead, we propose a task where the reward function is harder to learn.

	Swimmer-Corridor	*Ant-Corridor*
Uniform Sampling	11.8 ± 0.9	15 ± 1
IGR	13.3 ± 0.6	17.2 ± 0.5
EIR	12.0 ± 0.8	17.5 ± 0.8
IDRL (20 updates)	$\mathbf{2.4 \pm 0.8}$	$\mathbf{2.2 \pm 0.8}$
IDRL (4 updates)	2.8 ± 0.7	5 ± 1
IDRL (2 updates)	5.1 ± 0.6	8 ± 1
IDRL (1 update)	7.6 ± 0.8	12 ± 1

Table 2: Results comparing IDRL for different update frequencies of the candidate policies in the *Corridor* environments. The table shows the estimated regret of a policy trained using 20 queries about the reward function.

Setup. In our *Corridor* environments (Figure 3b), a robot (*Swimmer*, or *Ant*) has to move forward and stop at a goal position. A simulated expert rates trajectory clips according to a reward function defined over a one dimensional grid, where the reward is proportional to the velocity in the direction of the goal. This reward function is still linear in the robot's velocity, but is different across the grid. We use *augmented random search* (Mania et al., 2018) as RL algorithm. For the *Swimmer-Corridor* we learn a linear policy, and for the *Ant-Corridor* we learn a hierarchical policy on top of pre-trained policies moving in four different directions. To generate candidate queries, we use a fixed, noisy exploration policy that moves along the whole corridor. Unfortunately, EPD is too expensive to evaluate in this environment and MR is not suited to this kind of queries.

Results. Figure 3b shows that IDRL needs significantly fewer queries to find a good policy than any of the baselines. IDRL adapts its queries to the policies that the current reward model induces: it initially samples clips in which the robot moves close to its starting position and shifts its focus to other regions as the reward model improves, and the learned policy starts to move. In contrast, the baselines make queries in the whole reachable space similarly often, and, therefore, waste queries in regions that are not directly relevant for improving the policy.

The computationally most expensive part of this implementation of IDRL is updating the candidate policies in each iteration. Updating them less often reduces the computational cost at the expense of potentially reducing the sample efficiency. Table 2 studies this trade-off and shows that IDRL outperforms the baselines even when the policies are updated only once at the beginning of training. In this extreme case, we reduce IDRL's runtime from about 40 hours to about 20 hours in *Swimmer-Corridor*, and from about 40 hours to about 10 hours in *Ant-Corridor*. This shows the benefits are larger when solving the RL problem is

more expensive. Nonetheless, the baseline algorithms are still faster, and run for only $2-3$ hours. This is because they do not require the additional inference steps necessary to optimize Equation (2). These results indicate that IDRL using full Thompson sampling to generate candidate policies can trade-off computational cost and sample efficiency, which allows it to be applied to large environments.

7.5 Can IDRL be scaled to a Deep RL setting?

Finally, we consider the Deep RL implementation of IDRL from Section 6, using the Soft Actor-Critic algorithm (SAC; Haarnoja et al., 2018). We test it on standard MuJoCo locomotion tasks, which are harder to learn with a DNN than with a GP model because the former encodes less prior information.

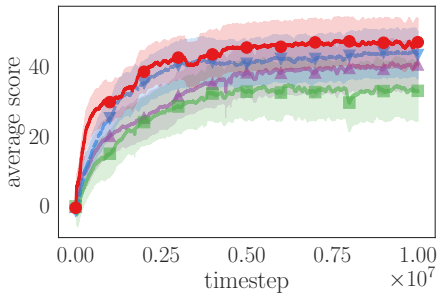


Figure 4: Normalized score of policies learned from 1400 (synthetic) comparisons of clips of the agent's behavior, averaged over all MuJoCo environments (higher is better). We show the mean and standard error of the score averaged over 5 random seeds per environment. The plot compares IDRL (—●—) to IGR (—▲—) and uniform sampling (—■—), as well as an ablation of IDRL that does not use the candidate policies to generate additional candidate queries (—▼—). EPD is too expensive and MR is not suited to this kind of queries.

Setup. We consider a suite of standard tasks in MuJoCo implemented in OpenAI Gym (Brockman et al., 2016): *HalfCheetah-v3*, *Walker2d-v3*, *Hopper-v3*, *Ant-v3*, *Swimmer-v3*, *InvertedPendulum-v2*, *InvertedDoublePendulum-v2*, *Reacher-v2*. Similar to Christiano et al. (2017), we modify some environments to remove the termination conditions. Our environments differ slightly from Christiano et al., for the details see Appendix E.3. Our evaluation metric is a normalized score, averaged over all environments. A score of 0 corresponds to a random policy and a score of 100 is the performance of a policy trained on the true reward function. We provide results for the individual environments in Appendix F. Since IDRL tracks the candidate policies, it generates the candidate queries rolling out the currently optimal policy *and* the candidate policies. However, the baselines do not have access to the candidate policies, and therefore consider a smaller set of potential queries. For a fair comparison, we perform an ablation where IDRL does not consider the candidate policies to generate candidate queries. Since IDRL maintains 3 (additional) candidate policies, it is roughly 4 times slower (about 80 hours on a single GPU) than the baselines (about 20 hours on a single GPU).

Results. Figure 4 shows that IDRL on average learns better policies than the baselines. The results per environment (in Appendix F) show that IDRL clearly outperforms the baselines in some environments (e.g., *Hopper-v3*), and performs comparably in others (e.g., *HalfCheetah-v3*). Crucially, these experiments demonstrate that IDRL is scalable to high-dimensional, complex tasks, and that it improves sample efficiency over existing methods for such tasks.

8 Conclusion

We studied the problem of actively learning reward function models using as few expert queries as possible. We introduced *Information Directed Reward Learning* (IDRL), a novel information-theoretic algorithm that focuses on learning a good policy rather than attaining a low approximation error of the reward and that, differently from most prior methods, works with multiple types of feedback. We show it needs significantly fewer queries than prior methods and that it scales to complex environments.

Limitations. The main limitation of IDRL is its computational cost. We demonstrated how to scale IDRL to complex environments, increasing the runtime by only a constant factor. While IDRL is still more demanding than most existing algorithms, it is preferable in situations where better sample efficiency is more important than low computational cost. Consequently, we consider IDRL an addition to the set of existing active reward learning algorithms rather than a replacement of existing methods.

Broader impact. IDRL improves the sample efficiency of learning reward models, which is a step towards making RL a viable solution for real-world problems. RL systems can be used in various ways, and they could cause risks from malicious actors (Brundage et al., 2018). However, overall, learning reward models is likely to help in making RL more robust and safe (Leike et al., 2018).

References

Pieter Abbeel and Andrew Y Ng. Apprenticeship learning via inverse reinforcement learning. In *Proceedings of International Conference on Machine Learning (ICML)*, 2004.

Riad Akrour, Marc Schoenauer, and Michèle Sebag. April: Active preference learning-based reinforcement learning. In *Joint European Conference on Machine Learning and Knowledge Discovery in Databases*, 2012.

Christopher M Bishop. *Pattern recognition and machine learning*. Springer, 2006.

Erdem Bıyık, Nicolas Huynh, Mykel J. Kochenderfer, and Dorsa Sadigh. Active preference-based Gaussian process regression for reward learning. In *Proceedings of Robotics: Science and Systems (RSS)*, July 2020a.

Erdem Bıyık, Malayandi Palan, Nicholas C Landolfi, Dylan P Losey, and Dorsa Sadigh. Asking easy questions: A user-friendly approach to active reward learning. In *Conference on Robot Learning (CoRL)*, 2020b.

Greg Brockman, Vicki Cheung, Ludwig Pettersson, Jonas Schneider, John Schulman, Jie Tang, and Wojciech Zaremba. Openai gym. *arXiv arXiv:1606.01540*, 2016.

Miles Brundage, Shahar Avin, Jack Clark, Helen Toner, Peter Eckersley, Ben Garfinkel, Allan Dafoe, Paul Scharre, Thomas Zeitzoff, Bobby Filar, et al. The malicious use of artificial intelligence: Forecasting, prevention, and mitigation. *arXiv:1802.07228*, 2018.

Sébastien Bubeck and Nicolo Cesa-Bianchi. Regret analysis of stochastic and nonstochastic multi-armed bandit problems. *Foundations and Trends® in Machine Learning*, 5(1):1–122, 2012.

Sébastien Bubeck, Rémi Munos, and Gilles Stoltz. Pure exploration in multi-armed bandits problems. In *International Conference on Algorithmic Learning Theory*, pages 23–37. Springer, 2009.

Paul F Christiano, Jan Leike, Tom Brown, Miljan Martic, Shane Legg, and Dario Amodei. Deep reinforcement learning from human preferences. In *Advances in Neural Information Processing Systems*, 2017.

Thomas M Cover and Joy A Thomas. *Elements of information theory*. John Wiley & Sons, 2006.

Christian Daniel, Oliver Kroemer, Malte Viering, Jan Metz, and Jan Peters. Active reward learning with a novel acquisition function. *Autonomous Robots*, 39(3):389–405, 2015.

Yan Duan, Xi Chen, Rein Houthooft, John Schulman, and Pieter Abbeel. Benchmarking deep reinforcement learning for continuous control. In *Proceedings of International Conference on Machine Learning (ICML)*, 2016.

Tanner Fiez, Lalit Jain, Kevin G Jamieson, and Lillian Ratliff. Sequential experimental design for transductive linear bandits. In *Advances in Neural Information Processing Systems*, 2019.

Johannes Fürnkranz, Eyke Hüllermeier, Weiwei Cheng, and Sang-Hyeun Park. Preference-based reinforcement learning: a formal framework and a policy iteration algorithm. *Machine learning*, 89 (1-2):123–156, 2012.

Tuomas Haarnoja, Aurick Zhou, Pieter Abbeel, and Sergey Levine. Soft actor-critic: Off-policy maximum entropy deep reinforcement learning with a stochastic actor. In *Proceedings of International Conference on Machine Learning (ICML)*, 2018.

Borja Ibarz, Jan Leike, Tobias Pohlen, Geoffrey Irving, Shane Legg, and Dario Amodei. Reward learning from human preferences and demonstrations in atari. In *Advances in Neural Information Processing Systems*, 2018.

Hong Jun Jeon, Smitha Milli, and Anca D Dragan. Reward-rational (implicit) choice: A unifying formalism for reward learning. In *Advances in Neural Information Processing Systems*, 2020.

Johannes Kirschner, Tor Lattimore, and Andreas Krause. Information directed sampling for linear partial monitoring. In *Conference on Learning Theory*, 2020.

W Bradley Knox and Peter Stone. Interactively shaping agents via human reinforcement: The TAMER framework. In *International Conference on Knowledge Capture*, 2009.

Jan Leike, David Krueger, Tom Everitt, Miljan Martic, Vishal Maini, and Shane Legg. Scalable agent alignment via reward modeling: a research direction. *arXiv:1811.07871*, 2018.

James MacGlashan, Mark K Ho, Robert Loftin, Bei Peng, Guan Wang, David L Roberts, Matthew E Taylor, and Michael L Littman. Interactive learning from policy-dependent human feedback. In *Proceedings of International Conference on Machine Learning (ICML)*, 2017.

Horia Mania, Aurelia Guy, and Benjamin Recht. Simple random search of static linear policies is competitive for reinforcement learning. In *Advances in Neural Information Processing Systems*, 2018.

Volodymyr Mnih, Koray Kavukcuoglu, David Silver, Andrei A Rusu, Joel Veness, Marc G Bellemare, Alex Graves, Martin Riedmiller, Andreas K Fidjeland, Georg Ostrovski, Stig Petersen, Charles Beattie, Amir Sadik, Ioannis Antonoglou, Helen King, Dharshan Kumaran, Daan Wierstra, Shane Legg, and Demis Hassabis. Human-level control through deep reinforcement learning. *Nature*, 518, 2015.

Jonas Mockus, Vytautas Tiesis, and Antanas Zilinskas. The application of Bayesian methods for seeking the extremum. *Towards Global Optimization*, 2, 1978.

Andrew Y Ng and Stuart J Russell. Algorithms for inverse reinforcement learning. In *Proceedings of International Conference on Machine Learning (ICML)*, 2000.

Martin L Puterman. *Markov decision processes: discrete stochastic dynamic programming*. John Wiley & Sons, 2014.

Antonin Raffin, Ashley Hill, Maximilian Ernestus, Adam Gleave, Anssi Kanervisto, and Noah Dormann. Stable baselines3. https://github.com/DLR-RM/stable-baselines3, 2019.

Carl Edward Rasmussen and Christopher K. I. Williams. *Gaussian Processes for Machine Learning*. The MIT Press, 2006.

Kevin Regan and Craig Boutilier. Regret-based reward elicitation for Markov decision processes. In *Uncertainty in Artificial Intelligence*, 2009.

Daniel Russo and Benjamin Van Roy. Learning to optimize via information-directed sampling. In *Advances in Neural Information Processing Systems*, 2014.

Aldo Rustichini. Minimizing regret: The general case. *Games and Economic Behavior*, 29(1-2): 224–243, 1999.

Dorsa Sadigh, Anca D Dragan, Shankar Sastry, and Sanjit A Seshia. Active preference-based learning of reward functions. In *Proceedings of Robotics: Science and Systems (RSS)*, 2017.

David Silver, Aja Huang, Chris J. Maddison, Arthur Guez, Laurent Sifre, George van den Driessche, Julian Schrittwieser, Ioannis Antonoglou, Veda Panneershelvam, Marc Lanctot, Sander Dieleman, Dominik Grewe, John Nham, Nal Kalchbrenner, Ilya Sutskever, Timothy Lillicrap, Madeleine Leach, Koray Kavukcuoglu, Thore Graepel, and Demis Hassabis. Mastering the game of Go with deep neural networks and tree search. *Nature*, 529(7587):484–489, 2016.

Jasper Snoek, Oren Rippel, Kevin Swersky, Ryan Kiros, Nadathur Satish, Narayanan Sundaram, Mostofa Patwary, Mr Prabhat, and Ryan Adams. Scalable Bayesian optimization using deep neural networks. In *Proceedings of International Conference on Machine Learning (ICML)*, 2015.

Richard S Sutton and Andrew G Barto. *Reinforcement learning: An introduction*. MIT press, 2018.

William R Thompson. On the likelihood that one unknown probability exceeds another in view of the evidence of two samples. *Biometrika*, 25(3/4):285–294, 1933.

Emanuel Todorov, Tom Erez, and Yuval Tassa. Mujoco: A physics engine for model-based control. In *2012 IEEE/RSJ International Conference on Intelligent Robots and Systems*, pages 5026–5033. IEEE, 2012.

Larry Wasserman. *All of statistics: a concise course in statistical inference*. Springer Science & Business Media, 2004.

Nils Wilde, Dana Kulic, and Stephen L Smith. Active preference learning using maximum regret. In *International Conference on Intelligent Robots and Systems (IROS)*, 2020.

Aaron Wilson, Alan Fern, and Prasad Tadepalli. A Bayesian approach for policy learning from trajectory preference queries. *Advances in Neural Information Processing Systems*, 2012.

Christian Wirth, Riad Akrour, Gerhard Neumann, and Johannes Fürnkranz. A survey of preference-based reinforcement learning methods. *The Journal of Machine Learning Research*, 18(1):4945–4990, 2017.

Checklist

1. For all authors...
   (a) Do the main claims made in the abstract and introduction accurately reflect the paper's contributions and scope? [Yes]
   (b) Did you describe the limitations of your work? [Yes] In Section 8.
   (c) Did you discuss any potential negative societal impacts of your work? [Yes] In Section 8.
   (d) Have you read the ethics review guidelines and ensured that your paper conforms to them? [Yes]
2. If you are including theoretical results...
   (a) Did you state the full set of assumptions of all theoretical results? [Yes]
   (b) Did you include complete proofs of all theoretical results? [Yes] See Appendix A.
3. If you ran experiments...
   (a) Did you include the code, data, and instructions needed to reproduce the main experimental results (either in the supplemental material or as a URL)? [Yes] In the supplementary material
   (b) Did you specify all the training details (e.g., data splits, hyperparameters, how they were chosen)? [Yes] See Appendices D and E.
   (c) Did you report error bars (e.g., with respect to the random seed after running experiments multiple times)? [Yes]
   (d) Did you include the total amount of compute and the type of resources used (e.g., type of GPUs, internal cluster, or cloud provider)? [No] We do provide approximate run times for each experiment and the number of CPUs/GPUs used. Experiments were run on a university cluster; unfortunately, we are unable to provide the exact type of hardware each experiment was run on because of how jobs are scheduled.
4. If you are using existing assets (e.g., code, data, models) or curating/releasing new assets...
   (a) If your work uses existing assets, did you cite the creators? [Yes]
   (b) Did you mention the license of the assets? [N/A] The only assets we used was code published under permissible open source licenses.
   (c) Did you include any new assets either in the supplemental material or as a URL? [Yes] We include code in the supplementary material.
   (d) Did you discuss whether and how consent was obtained from people whose data you're using/curating? [N/A]
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5. If you used crowdsourcing or conducted research with human subjects...
   (a) Did you include the full text of instructions given to participants and screenshots, if applicable? [N/A]
   (b) Did you describe any potential participant risks, with links to Institutional Review Board (IRB) approvals, if applicable? [N/A]
   (c) Did you include the estimated hourly wage paid to participants and the total amount spent on participant compensation? [N/A]