Blending Two Styles: Generating Inter-domain Images with MiddleGAN

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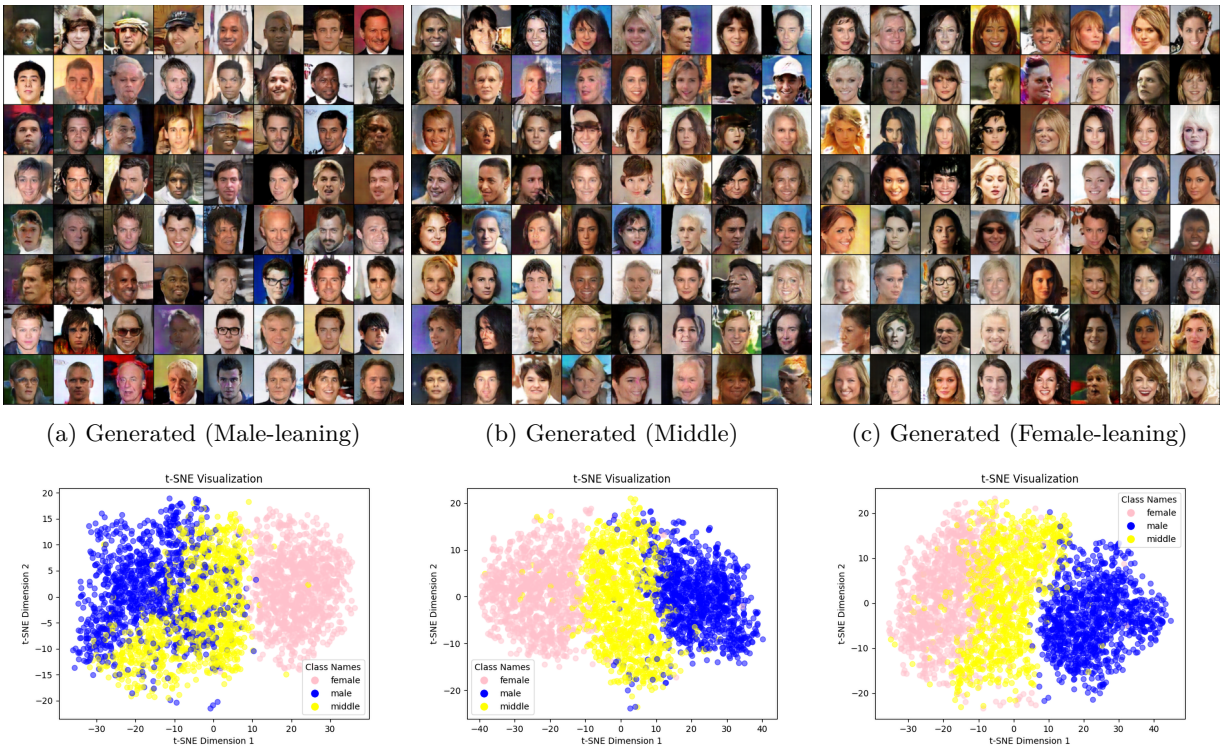


(a) Generated (Male-leaning) (b) Generated (Middle) (c) Generated (Female-leaning)

(d) t-SNE (Male-leaning) (e) t-SNE (Middle) (f) t-SNE (Female-leaning)

Figure 1: MiddleGAN can generate images which are blends of two domains. In this figure, we show the results of images generated with MiddleGAN at a resolution of 128px. The t-SNE visualizations support our claim that the blended images fall within the two input distributions (male and female).

Abstract

From celebrity faces to cats and dogs, humans enjoy pushing the boundaries of art by blending existing concepts together in new ways. With the rise of generative artificial intelligence, machines are increasingly capable of creating new images. Generative Adversarial Networks (GANs) generate images similar to their training data but struggle to blend images from distinct datasets. This paper introduces MiddleGAN, a novel GAN variant that blends inter-domain images from two distinct input sets. By incorporating a second discriminator, MiddleGAN forces the generator to create images that fool both discriminators, thus capturing the qualities of both input sets. We also introduce a blend ratio hyperparameter to control the weighting of the input sets and compensate for datasets of different complexities. Evaluating MiddleGAN on the CelebA dataset, we demonstrate that it successfully generates images that lie between the distributions of the input sets, both mathematically and visually. An additional experiment verifies the viability of MiddleGAN on handwritten

digit datasets (DIDA and MNIST). We provide a proof of optimal convergence for the neural networks in our architecture and show that MiddleGAN functions across various resolutions and blend ratios. We conclude with potential future research directions for MiddleGAN.

1 Introduction

Humans have always loved to create, especially visually. Using advanced photo manipulation tools such as Photoshop, digital artists have produced highly realistic blended faces of well-known celebrities (Emma Taggart). Simultaneously, with the rise of generative artificial intelligence (AI), computers are now "creating" images and other artistic works as well (Cetinic & She). One such method of image creation is Generative Adversarial Networks (GANs). GANs are machine learning models that are trained on a set of images and learn to create new images (from random noise) that are similar to the training images. More formally, GANs learn to generate images that are in distribution with the images of the input domain. The use of GANs to create images has been extensively explored over the last decade. However, traditional GANs are not designed to blend two distinct sets of images together.

In this paper, we present MiddleGAN, a novel variation of the traditional GAN, which takes as input two domains of images and learns to create images that lie between the input domains. In essence, MiddleGAN aims to create blended inter-domain images that contain features from both input domains. For example, given the input domains of male and female faces, MiddleGAN can produce images of human faces with both masculine and feminine qualities, as shown in Figure 1. Compared to existing state-of-the-art multi-discriminator GAN variations, such as FairGAN (Xu et al.) and D2GAN (Nguyen et al.), the dual-dataset input and blended-image objective of MiddleGAN is novel. Instead of manually blending the faces of celebrities, an artist could use a model such as MiddleGAN to create entirely new faces at the click of a button.

To achieve our goal of inter-domain image generation, we ask three overarching research questions:

- **RQ1:** How can we create inter-domain images that have qualities of both input domains, and validate this methodologically via t-SNE?
- **RQ2:** Is it feasible to generate images that lie in the middle of the feature space of the two domains, or can we extend our methodology to place unequal emphasis on each input domain?
- **RQ3:** Are the generated images consistently high quality across multiple image sizes and blend ratios?

In order to answer these research questions, we make three contributions:

- First, we propose a novel variation of a GAN, MiddleGAN, which leverages two discriminators and one generator to create blended inter-domain images from two input datasets.
- Second, we extend the initial functionality of MiddleGAN to introduce a Blend Ratio, which controls the amount of emphasis placed on each input domain's corresponding discriminator.
- Third, through extensive evaluation on the CelebA dataset, we show that images generated by MiddleGAN are within the expected distribution (via t-SNE) and have both masculine and feminine qualities when visually examined.

The remainder of this paper is organized as follows: Section 2 describes related work and the context of this project. Section 4 describes the theoretical basis of MiddleGAN and its model architecture. Section 5 discusses our implementation of MiddleGAN. Section 6 details our extensive evaluation of MiddleGAN. Section 7 discusses MiddleGAN and outlines opportunities for future work. Section 8 concludes our paper.

2 Related Work

In this section, we present an overview of the original generative adversarial network (GAN) as well as several subsequent GANs as they relate to our current work.

Generative Adversarial Nets: Since the introduction of the first generative adversarial network over a decade ago, many novel variations of GANs have been introduced. However, at the start of them all is the work of Goodfellow et al. in the paper "Generative Adversarial Nets" (Goodfellow et al.). The original GAN contained one discriminator and one generator. These models are trained in parallel. The generator learns to take random noise as input and produce an image as output. The discriminator learns to distinguish between real images and those created by the generator. By engaging in a minimax game, the generator learns to produce better images while the discriminator learns to better differentiate between real and generated images. The goal of training is to create a generator model that can produce images, from uniform random noise, that are within the distribution of the original training images. In other words, "GANs are a framework for teaching a deep learning model to capture the training data distribution so we can generate new data from that same distribution" (Tutorials).

GANs have been used in a wide range of applications, ranging from image-to-image style transfer to domain transfer tasks. CycleGAN focuses on "unpaired image-to-image translation," while GP-GAN focuses on high-resolution composite image blending (Wu et al.; Zhu et al.). The work of Sankar et al. focuses on the use of GANs for domain adaptation, and the work of Rahman et al. focuses on how GANs can be leveraged for domain generalization.

DCGAN: While an important first step, the original GAN as proposed by Goodfellow et al. is notoriously hard to train and can often fail to converge (Nie & Patel). Due to these challenges, many improved GAN variations have been proposed over the course of the last decade. One such proposed improvement is the Deep Convolutional Generative Adversarial Network (DCGAN) (Radford et al.). Radford et al. modified the original GAN to use Convolutional Neural Networks (CNN), which at the time were gaining popularity in computer vision tasks. DCGAN forms the basis for our MiddleGAN model, with its use of "convolutional and convolutional-transpose layers in the discriminator and generator, respectively" (Tutorials). DCGAN helped to prove the viability of CNN-based GANs and improved the training stability of the model when compared to the original GAN (Radford et al.).

WGAN & WGAN-GP: The Wasserstein GAN (WGAN), introduced by Arjovsky et al. in 2017, builds upon the success of DCGAN, making use of a CNN-based architecture (Arjovsky et al.). The novelty of the WGAN is two-fold. First, WGAN trains the discriminator (termed "critic") at a higher rate than the generator. As such, "training WGANs does not require maintaining a careful balance in training of the discriminator and the generator, and does not require a careful design of the network architecture either" (Arjovsky et al.). Second, and more importantly, the loss function for the WGAN is based on the Earth Mover's (Wasserstein-1) distance, which differs from traditional GANs and provides "a meaningful loss metric that correlates with the generator's convergence and sample quality" (Arjovsky et al.).

Gulrajani et al. proposed WGAN-GP as a direct improvement of the traditional Wasserstein GAN (Gulrajani et al.). Instead of using weight clipping to enforce the Lipschitz constraint on the discriminator/critic, which is required by WGAN, WGAN-GP "penalizes the norm of the gradient of the critic with respect to its input" (Gulrajani et al.). We use the loss function of WGAN-GP as the basis for the loss function of MiddleGAN.

Multi-Discriminator GANs: Beyond the above works, several other proposed GAN variations make use of dual discriminators. In "Generative Multi-Adversarial Networks," Durugkar et al. propose the use of multiple discriminators for a variety of use cases, including serving as a "formidable adversary" and a "forgiving teacher" (Durugkar et al.). Nguyen et al. attempt to mitigate issues of mode collapse through the use of dual discriminators in "Dual Discriminator Generative Adversarial Nets" (Nguyen et al.). More concretely, Xu et al. make use of two discriminators to improve the fairness of generated images with FairGAN (Xu et al.). MD-GAN proposes the use of multiple discriminators as an approach to distributed learning (Hardy et al.). Lastly, PATE-GAN uses multiple discriminators as applied to the field of differential privacy (Jordon & Yoon).

Diffusion Models: Given the introduction of GANs in 2014, they are somewhat dated. One might be tempted to ask why we focused on a GAN-based architecture as opposed to a more modern architecture, such as Diffusion Models. Diffusion Models, introduced in 2015, leverage ideas from "nonequilibrium thermodynamics" to train a generative AI model (Sohl-Dickstein et al.). Unlike GANs, diffusion models are not adversarial. Instead, diffusion models work by "systematically and slowly destroying structure in a data distribution through an iterative forward diffusion process... [and] then learning a reverse diffusion process that restores structure in data, yielding a highly flexible and tractable generative model of the data" (Sohl-Dickstein et al.). In other words, a diffusion model first learns to convert an image to seemingly random noise, and then learns to reverse this process, taking random noise and converting it into an in-distribution image. This process cannot be easily extended to support multiple input datasets, which prevents traditional diffusion models from forming the basis for an inter-domain image generation model. While more recent work such as "Blended Latent Diffusion" has leveraged diffusion models to mask and blend individual images, this work does not overcome the inherent single-domain limitation of diffusion models (Avrahami et al.).

When compared to previous works, MiddleGAN is distinct in its goal. Unlike traditional GANs, MiddleGAN utilizes two discriminators and one generator. Even when compared to other multi-discriminator GANs such as MD-GAN and FairGAN, the objective of MiddleGAN is noticeably different, as MiddleGAN aims to generate images that are in between the distributions of the two input datasets. Despite the existence of more modern generative AI architectures such as diffusion models, MiddleGAN is still relevant as it leverages the adversarial nature of GANs to generate images in between two distributions, which diffusion models cannot do.

3 Theory

In Section 4, we are going to provide detailed information on exactly how we achieve to obtain the inter-domain. In this Section (Section 3), we explore what is the potential usage of the inter-domain. To wit, the inter-domain, whose similarity to the two original domains is showcased by being equally distant (measured via Wasserstein distance) to the two original domains, can be used as an intermediate domain shown to facilitate better domain adaptation and generalization: existing works Na et al. (2021); Wang et al. (2022) have already showcased that empirically, adapting from one original domain (source) to another (target) is useful. Here, we theoretically prove that the inter-domain generated by MiddleGAN can indeed lower the error difference over distribution and domain shift if we adapt from one original domain to the inter-domain then to the other original domain, compared with the strategy in which the domain adaptation/generalization happens directly from one original domain (that is used as the source) to the other original domain (that is used as the target). The purpose of this proof is to showcase a potential usage for the generated synthetic inter-domain.

3.1 Preliminaries

Let $\mathcal{X}$ and $\mathcal{Y}$ represent the input and output spaces, respectively. Let X and Y be random variables taken from the input and output spaces. For a given domain (e.g., female faces), the distribution is denoted as μ over $\mathcal{X} \times \mathcal{Y}$. When considering only the sample distribution and not the joint sample-label distribution, we denote the sample distribution of μ over the input space $\mathcal{X}$ as $\mu(X)$.

Assumption 1 (Bounded Input Space). A compact input space $\mathcal{X}$ is bounded in the d-dimensional unit ℓ_2 ball:

$$\mathcal{X} \subseteq \{x \in \mathbb{R}^d : \|x\|_2 \leq 1\}$$

Definition 1 (p-Wasserstein Distance). Consider μ and ν over $\mathcal{S} \subset \mathbb{R}^d$. For any $p \geq 1$, the p-Wasserstein distance is defined as:

$$W_p(\mu, \nu) := \left(\inf_{\gamma \in \Gamma(\mu,\nu)} \int_{\mathcal{S}\times\mathcal{S}} d(x,y)^p \, d\gamma(x,y) \right)^{1/p}$$

where $\Gamma(\mu, \nu)$ is the set of all measures over $\mathcal{S} \times \mathcal{S}$ with marginals equal to μ and ν respectively.

3.2 Error Difference over Distribution & Domain Shift

Assumption 2 (R-Lipschitz Classifier). Let $h \in \mathcal{H}$ be R-Lipschitz in ℓ_2 norm, i.e.:

$$\forall x, x \in \mathcal{X} : |h(x) - h(x')| \leq R\|x - x'\|_2$$

Assumption 3 (ρ-Lipschitz Loss). ℓ is ρ-Lipschitz, i.e., $\forall y, y' \in \mathcal{Y}$:

$$|\ell(y, \cdot) - \ell(y', \cdot)| \leq \rho\|y - y'\|_2$$

$$|\ell(\cdot, y) - y(\cdot, y)| \leq \rho\|y - y'\|_2$$

In the settings of MiddleGAN, consider μ, ν and the measures for the middle domain m.

Lemma 1 (Error difference over shifted domains):

Population loss $|\epsilon_\mu(h) - \epsilon_m(h)| + |\epsilon_m(h) - \epsilon_\nu(h)| \leq \sqrt{\rho R^2 + 1} W_p(\mu, \nu)$

Proof:

$$\begin{aligned}
|\epsilon_\mu(h) - \epsilon_m(h)| &= |\mathbb{E}_{x,y\sim\mu}[\ell(h(x), y)] - \mathbb{E}_{x',y'\sim m}[\ell(h(x'), y')]| \\
&= \left| \int \ell(h(x), y)\, d\mu - \int \ell(h(x'), y')\, dm \right| \\
|\mathbb{E}_m(h) - \mu_\nu(h)| &= |\mathbb{E}_{x',y'\sim m}[\ell(h(x'), y')] - \mathbb{E}_{x'',y''\sim\nu}[\ell(h(x''), y'')]| \\
&= \left| \int \ell(h(x'), y')\, dm - \int \ell(h(x''), y'')\, d\nu \right|
\end{aligned}$$

$$|\epsilon_\mu(h) - \epsilon_m(h)| + |\epsilon_m(h) - \epsilon_\nu(h)| = \left| \int \ell(h(x), y)\, d\mu - \int \ell(h(x'), y')\, dm \right| + \left| \int \ell(h(x'), y')\, dm - \int \ell(h(x''), y'')\, d\nu \right|$$

Let γ be an arbitrary coupling of μ and m (i.e., a joint distribution of μ, m). Similarly, we define $\gamma_{m,\nu}$.

$$|\epsilon_\mu \ell(h) - \epsilon_\nu \ell(h)| = \left| \int \ell(h(x), y) - \ell(h(x'), y')\, d\gamma_{\mu,m} \right|$$

Triangle inequality $\leq \int \left| \ell(h(x), y) - \int \ell(h(x'), y') \right| d\gamma_{\mu,m}$

(ℓ is ρ-Lipschitz)

$$\left| \int \ell(h(x), y) - \ell(h(x'), y')\, d\gamma_{\mu,m} \right| \leq \int \rho(||h(x) - h(x')||) + \rho||y - y'||)\, d\gamma_{\mu,m}$$

(h is R-Lipschitz)

$$\int \rho(||h(x) - h(x')||) + \rho||y - y'||)\, d\gamma_{\mu,m} \leq \int \rho R||x - x'|| + \rho||y - y'||\, d\gamma_{\mu,m}$$

(R > 0)

$$\leq \int \rho\sqrt{R^2+1}(||x-x'||+||y-y'||)\, d\gamma_{\mu,m}$$

$$\leq \inf_{\gamma_{\mu,m}} \int \rho\sqrt{R^2+1}(||x-x'||+||y-y'||)\, d\gamma_{\mu,m}$$

$$= \rho\sqrt{R^2+1}W_1(\mu,m) \leq \rho\sqrt{R^2+1}W_p(\mu,m)$$

Similarly:

$$|\epsilon_m(h) - \epsilon\mu_\nu(h)| \leq \ell\sqrt{R^2+1}W_p(m,\nu)$$

$$|\epsilon_\mu(h) - \epsilon_m(h)| + |\epsilon_m(h) - \epsilon_\nu(h)| \leq \rho\sqrt{R^2+1}W_p(\mu,m) + \rho\sqrt{R^2+1}W_p(m,\nu)$$

Since $W_p(\mu,m) = W_p(m,\nu) = \frac{1}{2}W_p(\mu,\nu) \leq 2\rho\sqrt{R^2+1}W_p(\mu,m) \leq \rho\sqrt{R^2+1}W_p(\mu,\nu)$

4 Model Architecture & Design

In this section, we provide an overview of the model architecture as well as the design of MiddleGAN. Additionally, we provide a theoretical basis for MiddleGAN, building on top of the original GAN. We show show that there exists optimal parameters for both discriminators as well as an optimal solution for the parameters of the generator.

Before we discuss MiddleGAN, we need to discuss the original GAN on which MiddleGAN is based. In the original GAN (Goodfellow et al.), the generator G and the discriminator D engage in a minimax game in which G tries to minimize a value objective $V(G,D)$ whereas D tries to maximize it. $V(G,D)$ is defined in Equation 1, in which p is the distribution of the real samples and q is the distribution of the noise. A key observation obtained from Equation 1 is that G's effort is to generate $G(z)$ whereas z is an input noise such that $G(z)$ will be in-distribution with the distribution of the real samples p.

$$\begin{aligned}\min_G \max_D V(G,D) = \mathbb{E}_{x\sim p(x)}[\log(D(x))] \\ + \mathbb{E}_{z\sim q(z)}[\log(1-D(G(z)))]\end{aligned} \tag{1}$$

Based on the key observation that we obtain from Equation 1, in MiddleGAN we propose to employ two discriminators, D_a and D_b. Each discriminator is only aware of one domain of images. The first discriminator, termed D_a, only knows of the images in Domain A. Similarly, the second discriminator, termed D_b, only knows of the images in Domain B. Neither discriminator knows of the existence of the other domain of images, and is solely responsible for determining if an image came from its corresponding domain or not. The generator G engages in a two-way minimax game with the two discriminators. The samples it generates will be in the middle of the feature space of both input domains. Below, we empirically prove that the generated samples in p_m are represented by the features that are invariant across the input domains.

Formally, the objective function of D_a, D_b, and G is described by Equation 2.

$$\begin{aligned}&\min_G \max_{D_a,\, D_b} V(G,D_a,D_b) \\ &= \mathbb{E}_{x_a\sim p_a(x_a)}[\log(D(x_a))] + \mathbb{E}_{z\sim q(z)}[\log(1-D_a(G(z)))] \\ &+ \mathbb{E}_{x_b\sim p_b(x_b)}[\log(D(x_b))] + \mathbb{E}_{z\sim q(z)}[\log(1-D_b(G(z)))]\end{aligned} \tag{2}$$

In the previous paragraphs we have described how to generate samples that are similar to samples from both input domains. Figure 2 outlines the duel-discriminator architecture of MiddleGAN and how it is used to generate domain agnostic samples.

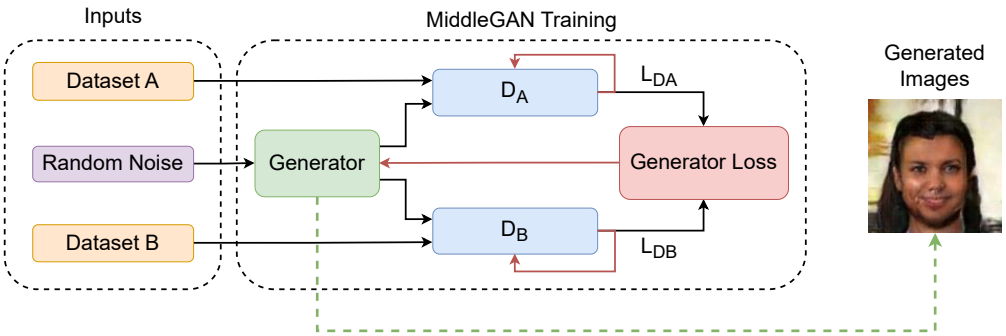


Figure 2: In this figure we describe how to use the MiddleGAN to generate fake, domain agnostic samples. As shown in the diagram, neither discriminator is directly aware of the others existence or the existence of a second dataset. This is importance, as it allows each discriminator to focus solely on differentiating between images in it's own dataset and any other images, regardless of source. Black arrows indicate the forward flow of information, while red arrows indicate backwards propagation. The dashed green line indicates that the generated images come from the trained generator.

4.1 Optima for the Discriminators and Generator

We first discuss the two discriminators D_a and D_b given a fixed G. We propose Theorem 4.1 regarding the optimal values for D_a and D_b, represented as D_a^* and D_b^*

Given p_m, the distribution of samples generated by a fixed generator G, the optimal values for the parameters of D_a and D_b are $D_a^* = \frac{p_a}{p_a+p_m}$ and $D_b^* = \frac{p_b}{p_b+p_m}$.

Proof. The value objective $V(G, D_a, D_b)$ can be expanded.

$$\begin{aligned} V(G, D_a, D_b) &= \int_{x_a} p_a(x_a) \log(D_a(x_a)) dx_a + \int_{x_b} p_b(x_b) \log(D_b(x_b)) dx_b \\ &+ \int_z q(z) \log(1 - D_a(G(z))) dz + \int_z q(z) \log(1 - D_b(G(z))) dz \\ &= \int_{x_a} p_a(x_a) \log(D_a(x_a)) dx_a + p_m(x_a) \log(1 - D_a(x_a)) dx_a \\ &+ \int_{x_b} p_b(x_b) \log(D_b(x_b)) + p_m(x_b) \log(1 - D_a(x_b)) dx_b \end{aligned} \tag{3}$$

We observe that p_a, p_b and p_m belong in $\mathbb{R}$. For the domain A discriminator D_a, any pair of p_a and p_m in the form of $p_a \log(y) + p_m (1 - \log(y))$, $p_a \log(y) + p_m (1 - \log(y))$ achieves its maximum value at $\frac{p_a}{p_a+p_m}$ (Goodfellow et al.). Similarly, for the domain B discriminator D_b, any pair of p_b and p_m in the form of $p_b \log(y) + p_m (1 - \log(y))$, $p_b \log(y) + p_m (1 - \log(y))$ achieves its maximum value at $\frac{p_b}{p_b+p_m}$. □

Now we bring forth Theorem 4.1 which proposes that there exists an optimal solution for the parameters of not only D_a and D_b, but also G. There exists a global minimum for the virtual training criterion $C(G)$ defined as

$$C(G) = \max_{D_a,\, D_b} V(G, D_a, D_b). \tag{4}$$

In other words, there exists an optimal solution for the parameters of the generator G.

Proof. Goodfellow et al. proved that, in the original GAN where there is only one discriminator D and one generator G, the virtual training criterion can be written as the following:

$$
\begin{aligned}
C_{original}(G) &= \max_{D} V(G, D) \\
&= -log(4) + KL(p \parallel \frac{p + p_m}{2}) + KL(p_m \parallel \frac{p + p_m}{2})
\end{aligned} \tag{5}
$$

in which p is the distribution of the real samples and p_m is the distribution of generated fake samples, and KL is the Kullback–Leibler divergence. With two discriminators, our virtual training criterion $C(G)$ can be rewritten as:

$$
\begin{aligned}
C(G) = &- log(4) + KL(p_a \parallel \frac{p_a + p_m}{2}) + KL(p_m \parallel \frac{p_a + p_m}{2}) \\
&- log(4) + KL(p_b \parallel \frac{p_b + p_m}{2}) + KL(p_m \parallel \frac{p_b + p_m}{2}) \\
= &- 2log(4) + 2JSD(p_a \parallel p_m) + 2JSD(p_b \parallel p_m)
\end{aligned} \tag{6}
$$

In Equation 6, JSD is the Jensen–Shannon divergence. To find the global minimum, $M(G)$, we want to obtain

$$
M(G) = \underset{p_m}{argmin} - 2log(4) + 2JSD(p_a \parallel p_m) + 2JSD(p_b \parallel p_m) \tag{7}
$$

We observe in Equation 7 that we are looking for the optimal value of the JSD centroid defined as $Centroid^* = arg \min_{Q} \sum_{i=1}^{n} JSD(P_i \parallel Q)$ in which P_i and Q are distributions. We can see that the generator is essentially looking for the JSD controid of the source domain distribution p_a and the target domain distribution p_b. The convexity of the problem has been proved in (Nielsen, 2020). □

4.2 Beyond the "Middle" Feature Space

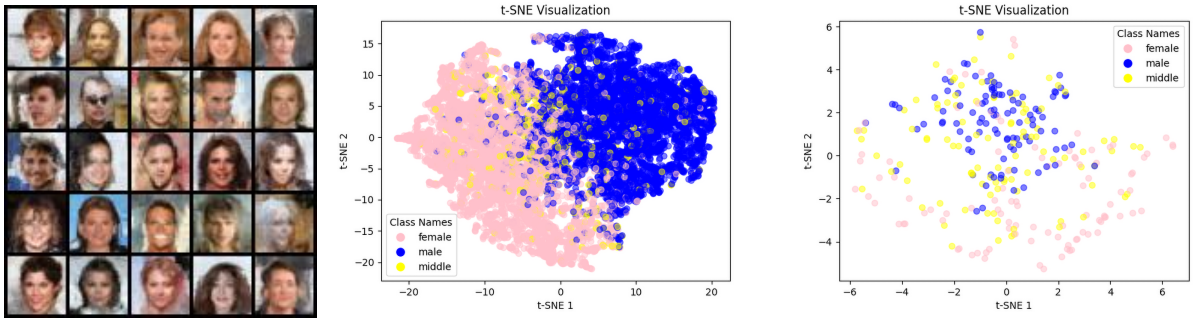
With two discriminators, the generator G faces an additional challenge, as its success is determined by its ability to fool both discriminators. In order to do this, the generator must learn to produce images that have features of both input domains. Simply put, the loss of the generator is the averaged loss from both discriminators, as shown in Equation 8.

$$
\mathcal{L}_G = \frac{(\mathcal{L}_{D_A} + \mathcal{L}_{D_B})}{2} \tag{8}
$$

In Equation 8, the losses of both discriminators are weighed equally. This aims to ensure that the generator G learns to produce images that are in the middle of both input domains. However, this is an artificial limitation, as the weights for the losses from each discriminator do not have to be evenly weighted. To expand the flexibility of MiddleGAN, we introduced a new blending hyperparameter, the blend ratio, into our model architecture.

$$
\mathcal{L}_G = \mathcal{L}_{D_A} * (BR) + \mathcal{L}_{D_B} * (1 - BR) \tag{9}
$$

The updated loss for the generator is shown in Equation 9. The blend ratio can range from 0 to 1, and directly controls the percent of weight placed on the loss of D_A. A blend ratio of 0.5 equally weighs the losses from both discriminators and replicates our initial implementation of MiddleGAN. A blend ratio of 0 would completely ignore Domain A and cause MiddleGAN to act like a traditional GAN, using only Domain B as input. A blend ratio of 0.75 would result in the loss of discriminator A carrying three times the weight of the loss of discriminator B. The blend ratio vastly increases the range of images that MiddleGAN can learn to produce.



(a) Generated Images (b) t-SNE Visualization (c) t-SNE Visualization

Figure 3: A sample of images generated with our transformer-based MiddleGAN implementation as well as associated tSNE visualizations. The images were generated at a resolution of 32px by 32px with a blend ratio of of 0.50. **As shown by the t-SNE visualizations, the generated images fell within the distribution of both input domains (as opposed to between it).**

5 Implementation

Our implementation of MiddleGAN builds upon PyTorch's official implementation of DCGAN (Tutorials). This implementation was designed for use with the CelebA dataset, which sped up our initial development time. However, this implementation had several limitations, most notably a fixed input image size of 64px. By dynamically computing the number of layers required by both the generator and discriminator models based on the requested image size, we enabled our implementation of DCGAN to support any power-of-two image size.

Next, we modified our implementation of DCGAN to add an additional discriminator and support two input domains. These changes formed the basis for MiddleGAN. We modified the model architecture so that in each training epoch, images from both domain A and domain B were seen by the model. To account for differences in the sizes of the input domains, we leveraged the itertools library's Cycle method to ensure that the length of the smaller dataset would appear to match that of the larger dataset (pyt, a). With the addition of the second discriminator, we simply adjusted the loss function for the generator to take into account the losses of both discriminators when evaluated on generated images. At this stage, our implementation of MiddleGAN could generate images, albeit with low quality.

With the basic MiddleGAN implementation complete, we began preliminary testing and evaluation of the model. We observed high training instability of the GAN and poor quality of generated images. After making these observations, we began to look into ways to stabilize the training of the GAN.

In parallel, we were exploring the idea of a transformer-based implementation of MiddleGAN, based on TransGAN (Jiang et al.). While the paper authors provided a PyTorch implementation of TransGAN (git, b) (which itself was based on their earlier work, AutoGAN (git, a)), we opted for a cleaner re-implementation of TransGAN (Sarıgün). Using TransGAN as our base model, we developed a low resolution (32px) transformer-based version of MiddleGAN. This implementation utilized the loss function from WGAN-GP (Gulrajani et al.) to stabilize the training process. A sample of the images produced with our transformer-based implementation of MiddleGAN is shown in Figure 3a. Figure 3c and Figure 3b were very intermixed, showing that generated samples were not clearly between the input distributions. Given these results, along with significantly longer training times we observed, we ultimately declined to pursue development of a transformer-based MiddleGAN for this project. We leave it to future research to better evaluate the viability and effectiveness of a transformer-based MiddleGAN.

While we ultimately declined to pursue a Transformer-based implementation of MiddleGAN, that work was not in vain, as we did observe that the loss function being used in TransGAN was leading to more stable model training. The loss function, WGAN-GP loss, is based on the work of Gulrajani et al. in "Improved

Table 1: MiddleGAN Hyperparameters

Hyperparameter	Description	Values	Source
Batch Size	Batch size during training.	128	DCGAN
NZ	Latent space for generator.	128	-
Epochs	Epochs during training.	200	-
LR_D	Learning rate of discriminators.	0.0001	TransGAN
LR_G	Learning rate of generator.	0.0001	TransGAN
B_1	Beta 1 for Adam optimizers.	0.0	TransGAN
B_2	Beta 2 for Adam optimizers.	0.999	DCGAN
N Critic	Discriminator to generator training ratio.	5	WGAN
GP Weight	Gradient penalty weight (used in loss function).	100	-
Blend Ratio	The blend ratio between input domains.	0.25, 0.50, 0.75	-
Image Size	The size of the generated images.	32px, 64px, 128px	-

Training of Wasserstein GANs" (Gulrajani et al.). When we implemented WGAN-GP loss on our DCGAN-based MiddleGAN, we observed more stable training performance. Taking inspiration from the original WGAN paper (Arjovsky et al.), we also modified our model to train the discriminators at a higher frequency then the generator, which also led to improved quality in the output images.

6 Evaluation

In this section we describe our dataset, experimental setup, and results for MiddleGAN across multiple datasets.

6.1 Experimental Setup

Dataset: We primarily evaluated MiddleGAN using the CelebA dataset (Liu et al., 2015), which was proposed by Liu et al. in 2015. The CelebA dataset contains over 200,000 annotated images of celebrity faces. We selected this dataset due to its large size, extensive use in prior works, and separability into two domains ("Male" and "Female"). To create the two domains we used the boolean "Male" identifier present in the original dataset annotations[1]. By splitting on the "Male" identifier we created two smaller datasets, which we designated 'Male' (with approx. 84,000 images) and "Female" (with approx. 118,000 images). In all experiments, the "Female" dataset was assigned domain A, and the 'Male' dataset was assigned domain B. These dataset-domain assignments were based on alphabetical ordering, but given the order-agnostic structure of MiddleGAN with regards to input domains, we would anticipate identical results if the dataset-domain assignments were reversed.

Image Generation: To evaluate MiddleGAN, we used the "Male" and "Female" datasets to train nine different MiddleGAN models using a combination of three blend ratios (0.25, 0.50, and 0.75) and three image sizes (32px, 64px, and 128px). Aside from the blend ratio and Image Size, all models used the same hyperparameters as shown in Table 1. If our selection of a hyperparameter was heavily influenced by one or more prior works, those works are noted in the "Source Paper" column. All models were trained on a NVIDIA A100 GPU, with an average per-model training time of around 12 hours. We generated 1000 images per model for use in our experiments.

Feature Extraction & t-SNE: We elected to use the pre-trained ResNet101 model provided by PyTorch as the basis of our feature extractor (pyt, c; He et al.). We then fine-tuned the model to provide a binary classification for male and female faces from the original CelebA dataset. This resulted in 3 fine-tuned

[1]All annotations in the CelebA dataset are booleans. As such, we made the assumption that any image that had a value of "1" for the "Male" identifier was male, and a value of "-1" was female. While this may not be 100% accurate, as a "-1" value is technically "Not Male" as opposed to "Female", we do not expect that this assumption significantly impacted our results.

(a) Domain A Images (F) (b) Domain B Images (M) (c) Generated Images

Figure 4: This figure shows the results of images from both input domains as well as images generated by MiddleGAN. We used an image size of 128px and a blend ratio of 0.5. The generated images have both masculine and feminine qualities.

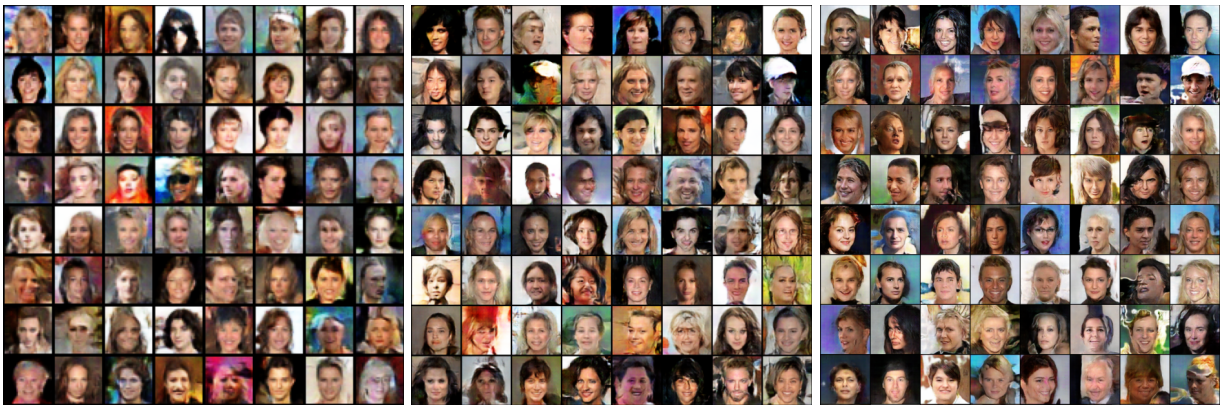
(a) Epoch 50 (b) Epoch 100 (c) Epoch 150 (d) Epoch 200

Figure 5: Generated images on fixed noise across 200 epochs. We used an image size of 128px and a blend ratio of 0.50. Image quality continues to improve until at least the 200th epoch.

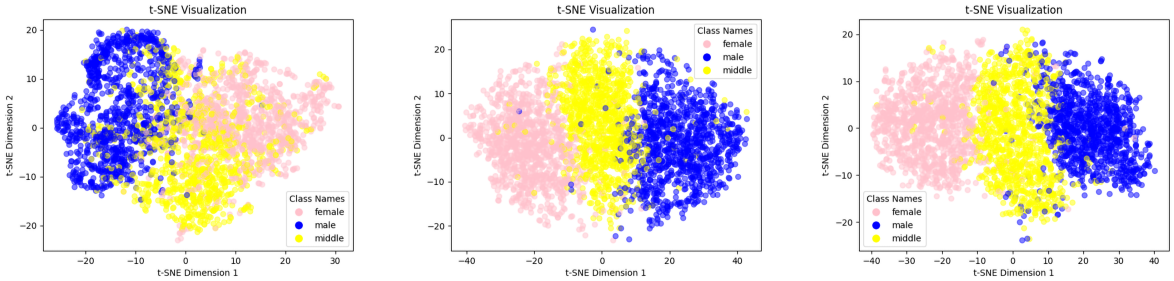
ResNet101 models, one per Image Size. From there, we were able to extract feature vectors (length=2048) from the second-to-last layer of the ResNet101 model. We extracted feature vectors for each of the nine sets of images generated by MiddleGAN, as well as matching-size sets of images from both input domains. Roughly speaking, this means we extracted 3000 feature vectors for each of the nine models, which were evenly split between domain A images, domain B images, and generated images. Leveraging principal component analysis (PCA), we reduced the length of each extracted vector to 50 (skl, b). After performing PCA, we input the feature vectors into t-SNE in order to better understand the relationship between the input images and generated images.

6.2 Experimental Results

We achieved positive results on all nine trained versions of MiddleGAN, across a variety of blend ratios and image sizes. Figure 4 shows a sample of images from both input domains as well as images generated by MiddleGAN. An informal evaluation by the authors of the paper found the generated images to have both masculine and feminine qualities, which one would expect given the input domains of male and female faces. Beyond the mix of masculine and feminine qualities, we noted a diverse range of skintones and ethnicities present in both the input images and generated images, which further shows the diversity of images that MiddleGAN can generate. This is also an indicator that MiddleGAN did not suffer from mode collapse, which is when "the generator starts producing the same output (or a small set of outputs) over and over again" (pro).



(a) Generated Images (32px) (b) Generated Images (64px) (c) Generated Images (128px)



(d) t-SNE Visualization (32px) (e) t-SNE Visualization (64px) (f) t-SNE Visualization (128px)

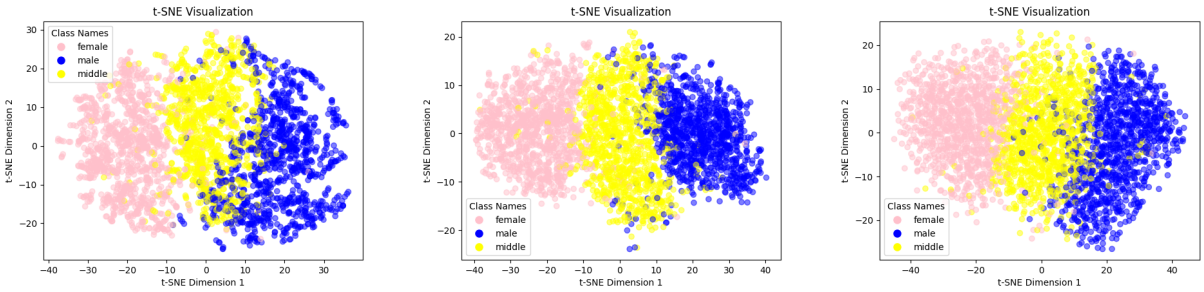
Figure 6: The impact of different image sizes on the images generated by MiddleGAN, with a blend ratio of 0.5. While the generated images contain masculine and feminine qualities at all resolutions, the t-SNE visualizations are noticeably different at lower resolutions. This is expected, as at low resolutions, there are not enough pixels to clearly differentiate between masculine and feminine qualities.

While the training loss for the generator slowly increases over the course of the training, we continued to see improvements in the resulting imagery, as shown in Figure 5, which shows samples generated by MiddleGAN on fixed noise across training epochs. For this project, all training stopped after 200 epochs. We leave it to future work to evaluate if the quality of images generated by MiddleGAN could continue to improve after 200 epochs.

6.3 Image Size Experiments

The impact of different blend ratios on the images generated by MiddleGAN, with an image size of 128px. With a blend ratio of 0.25, the generated images were more masculine. When visualized with t-SNE, a blend-ratio of 0.25 caused the generated images to largely overlap with the images from the Male domain. A similar yet reversed pattern was visible with a blend ratio of 0.75, which resulted in more feminine images.

As previously discussed in Section 5, we modified the traditional DCGAN architecture to support any power-of-two image size by scaling the number of layers in the generator and discriminators. To assess the success of this modification, we evaluated MiddleGAN on three image sizes - 32px, 64px, and 128px. Figure 6 shows our results. Our results show that MiddleGAN can produce high quality images across a wide range of image sizes. Additionally, despite having different image resolutions (and thus layers), all three models had similar training losses and all had strong alignment when visualized with t-SNE. One key observation is that the generated samples fell *within* the distributions of the input domains at lower resolutions, while the generated samples fell *between* the distributions of the input domains at higher resolutions. We hypothesize that this is because at lower resolutions, there are not enough pixels to distinguish between masculine and feminine faces.



(a) Perplexity = 5 (b) Perplexity = 30 (c) Perplexity = 90

Figure 7: This figure shows the results of our t-SNE perplexity experiments. We used an image size of 128px and a blend ratio of 0.5. We varied the perplexity from 5 to 90. In all cases, the generated images fell within or between the input domain images, as expected.

6.3.1 Blend Ratio Experiments

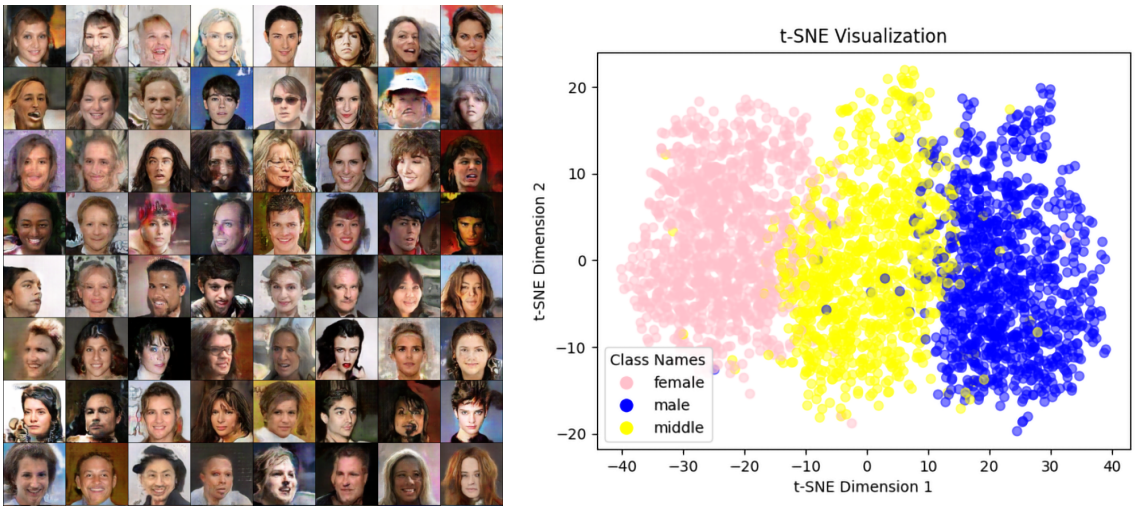
The inclusion of a blend ratio in our model architecture enabled greater flexibility and variety in the range of images that MiddleGAN could produce. In this section we explore the impact that the blend ratio had on generated images as well as the corresponding visualizations. We evaluated MiddleGAN on three blend ratios - 0.25, 0.50, and 0.75. Figure 1 shows our results along with samples of the original input images as reference.

When compared to a blend ratio of 0.50, the results shown for the other blend ratios are noticeably different. A blend ratio of 0.25 weighs the loss of discriminator A (which trains on Domain A, female images) at 25% and weighs the loss of discriminator B (which trains on Domain B, male images) at 75%. As such, the resulting images (shown in Figure 1a) are noticeably more male than images generated with a blend ratio of 0.5, while still being more feminine than the original all-male images. The training loss is also different, as discriminator B shows much lower losses than discriminator A. This intuitively makes sense, as the loss of discriminator B is more heavily penalized during training, and thus a priority for the model to minimize. Lastly, the t-SNE visualization shows a shift in distribution, with the generated images falling both within and between the male and female images, as shown in Figure 1d. A blend ratio of 0.75 shows similar but inverse changes, with the images, training losses, and t-SNE visualizations all being biased towards female images (shown in Figures 1c, and 1f).

6.4 t-SNE & Perplexity Results

Given our reliance on t-SNE as an indicator for the quality of the images generated by MiddleGAN, we wanted to ensure that any results that we observed were not due to chance in terms of hyperparameter selection. Of specific concern to us was the "Perplexity" hyperparameter, which past research has established can have a dramatic effect on the visualizations that t-SNE generates (Wattenberg et al., 2016; skl, a).

Figure 7 shows the results of three different perplexity experiments we performed, with perplexity values ranging from 5 to 90. We selected this range of values based on the guidance provided in the scikit-learn implementation of t-SNE, which recommends "a value between 5 and 50" (skl, c). For these experiments, all input images were 128px resolution images, with the generated images created with a blend ratio of 0.5. Our results show that perplexity did not have a major impact on the t-SNE visualizations we generated, which is a positive result. We ultimately selected a perplexity value of 30 for all of our other t-SNE visualizations presented in this paper, as we found it generated consistently good results. Coincidentally, the default Perplexity value in scikit-learn's t-SNE implementation is 30, which supports our selection (skl, c).



(a) Sample Images

(b) t-SNE Visualization

Figure 8: The preliminary results from our high resolution (256px) implementation of MiddleGAN. The generated images have both masculine and feminine qualities when using a blend ratio of 0.50. Additionally, the generated images fall within the input domains when visualized with t-SNE.

6.5 High Resolution Results

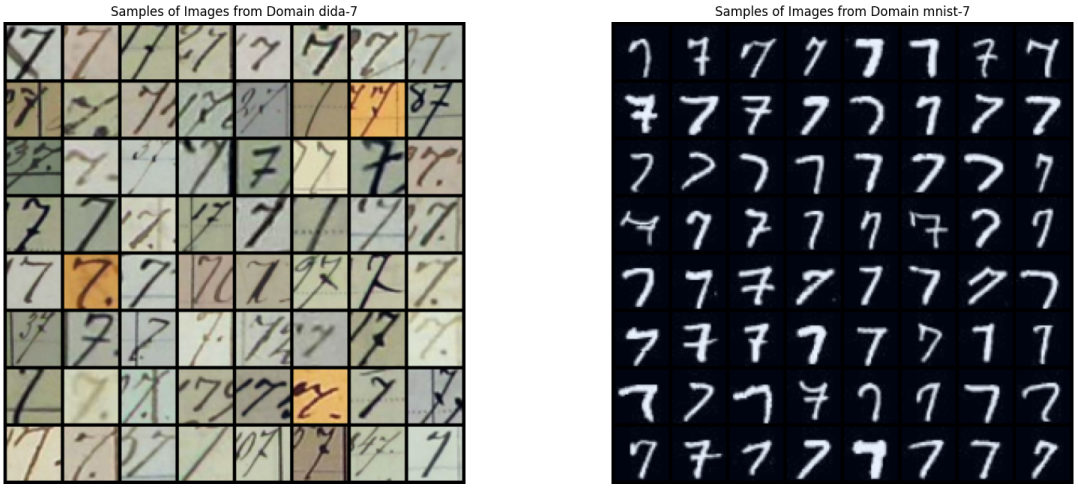
While our evaluation of MiddleGAN's ability to scale to different images sizes presented in Section 6.3 is thorough, we were eager to see if MiddleGAN could produce high quality images beyond 128px resolution. The push to go beyond 128px resolution images was prompted by our observation that the original WGAN-GP paper appeared to only test image generation up to 128px resolution (Gulrajani et al.). Given our model's requirement for power-of-two image sizes, the next possible image size for us to generate was 256px resolution. Our initial 256px resolution results are shown in Figure 8. We believe these results, while preliminary, show a positive outcome with both the generated samples and the t-SNE visualization appearing as expected, even with the higher resolution.

6.6 Handwritten Digits Experiments

Our evaluation of MiddleGAN for handwritten digit datasets followed a very similar process to that of the CelebA dataset. We first identified our datasets, trained MiddleGAN to generate images, and then visualized the results using t-SNE. We discuss our process and results below.

Datasets: While our earlier experiments split a single dataset into two domains, our handwritten digit experiments leverage two different datasets - each one serving as input ton one domain. We selected the MNIST dataset (LeCun et al., 2010), published in 2010, and the DIDA dataset (Kusetogullari et al., 2020b;a), published in 2020. The MNIST dataset contains over 70,000 black and white cropped and centered images of the digits 0 through 9. The DIDA dataset contains over 250,000 color images of the digits 0 through 9, sourced from Swedish historical documents from 1800 to 1940 - DIDA is claimed to be the "largest historical handwritten digit dataset" (Kusetogullari et al., 2020b;a). Unlike the CelebA experiments, in which the domains were both relatively similar (human faces), the DIDA and MNIST datasets are visually distinct and have different levels of complexity (the images in MNIST are at least 3 times less complex then DIDA due to having a single channel of black and white color information).

Image Generation: We trained MiddleGAN using the DIDA and MNIST datasets, specifically images from the class of "7" for both datasets. Samples of both input datasets are shown in Figure 9. We utilized a image size of 32px and a blend ratio of 0.60. Given that handwritten digits are significantly simpler then human faces, we modified many of the hyperparameters shown in Table 1 to better work for handwritten



(a) Domain A Images (DIDA)

(b) Domain B Images (MNIST)

Figure 9: This figure shows images from both DIDA and MNIST input domains.

digits. We selected a blend ratio of 0.60 after observing that a blend ratio of 0.50 caused MiddleGAN to only produce MNIST-like images. By adjusting the blend ratio to 0.60 (with DIDA as domain A), we placed more weight on the more complex dataset, which ensured a diverse quality of images were produced when MiddleGAN was trained. This observation is important, as it means that the blend ratio can be used to compensate for cases when two domains of dataset have radically different complexities.

Feature Extraction & t-SNE: We elected to use the pre-trained GoogleLeNet model provided by PyTorch as the basis of our feature extractor (pyt, b; Szegedy et al., 2014). We opted for GoogleLeNet over ResNet101 as we felt GoogleLeNet was better suited for the simpler task of handwritten digit recognition. We fine-tuned the model to provide a binary classification for DIDA vs MNIST digits. From there, we were able to extract feature vectors from the second-to-last layer of the GoogleLeNet model. We extracted feature vectors for the images generated by MiddleGAN, as well as both input domains. After performing PCA, we input the feature vectors into t-SNE in order to better understand the relationship between the input images and generated images.

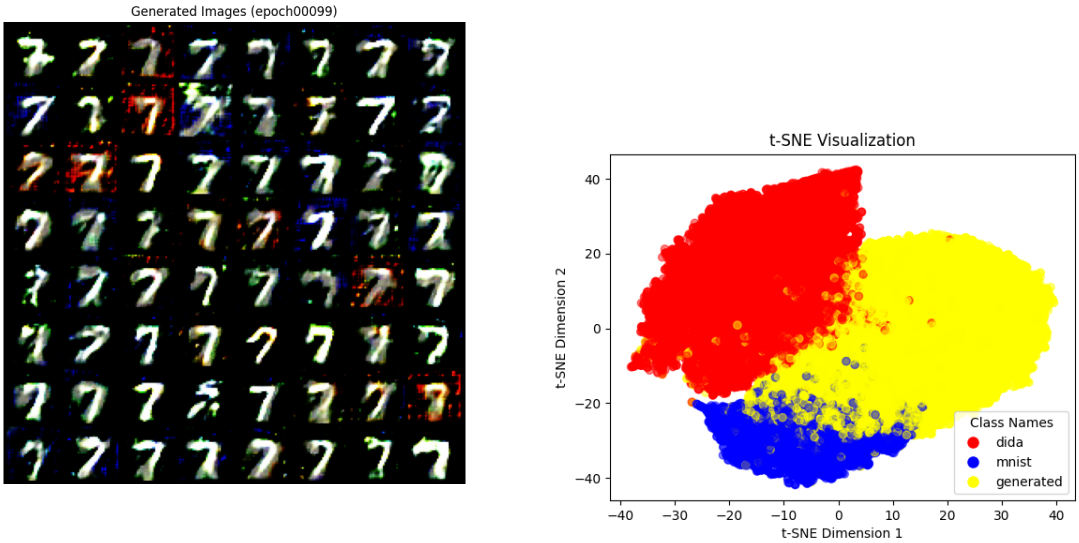
Results:

THe images generated by MiddleGAN during our handwritten digit experiments, as well as associated t-SNE visualization, are shown in Figure 10. While it is difficult to say if the generated images are truly in the "middle" visually from a human perspective, the t-SNE visualization reveals that algorithmically the generated images fall between the DIDA and MNIST datasets. The results of this experiment emphasis the ability of MiddleGAN to blend sharply different domains together in a way that will still result in "middle" images when visualized with t-SNE.

7 Discussion & Future Work

In this paper we demonstrated both the theoretical and empirical results of images generated with MiddleGAN. However, we think there are many opportunities to build upon MiddleGAN. We discuss our existing work and opportunities for future work below.

Limitation of CelebA Dataset:



(a) Generated Images

(b) t-SNE Visualization

Figure 10: This figure shows the generated images for the blended DIDA-MNIST dataset as well as the associated t-SNE visualization.

Throughout this work, we have primarily used the CelebA dataset with a split on the "male" attribute to create the "male" and "female" input domains. Although we achieved strong results using these domains, there are some inherent limitations of our approach and we caution against similar blending being blindly applied to future applications. Firstly, the CelebA dataset comprises images of celebrities, meaning our MiddleGAN model learns to generate faces resembling celebrities rather than everyday people. While we expect that MiddleGAN would perform equally well with photos of non-celebrities, it currently generates new celebrity-like faces. Secondly, and perhaps more importantly, MiddleGAN is learning stereotypical masculine and feminine traits rather than the true essence of being "male" or "female". This could potentially reinforce gender stereotypes if misused in the future, despite the model's ability to demonstrate the blending capabilities of MiddleGAN. We emphasize that MiddleGAN, like any tool, has the potential for artistic and other applications. However, it is crucial to remain mindful that certain blending combinations (e.g., different races) may produce uncomfortable or inappropriate results.

Expanding to N-Domains: While MiddleGAN currently supports the blending of two-domains, this is not a hard limitation. In fact, MiddleGAN could be modified to support N-domains by modifying the training code to support one discriminator per input domain. However, while this is theoretically possible, we anticipate larger losses for, and the eventual collapse of, MiddeleGAN's generator if too many different domains were included. We anticipate this happening as the generator would be unable to create a single image that would satisfy all discriminators. Despite this anticipated challenge, we still believe that this area of research would be worth future exploration.

Domain Diversity: Moving beyond images of faces (CelebA) and handwritten digits (DIDA and MNIST), we would like to further explore the limits of MiddleGAN. In our evaluation of MiddleGAN, we primarily focused on two domains of images from the CelebA dataset (male and female faces) that, while different, were both of humans, and thus relatively similar in a broader sense. In the future, we would like to evaluate MiddleGAN on domains with larger differences such as plants and cars or similarly outlandish combinations. We expect that given input domains with extreme enough differences, MiddleGAN would fail to output high quality images. However, our results with the handwritten digit based experiments indicate that algorithmically (via t-SNE) the images generated by MiddleGAN might still be in the "middle" - more research is needed to evaluate if this holds true for other data sets.

8 Conclusion

In this work, we introduced MiddleGAN, a novel variation of the traditional GAN capable of generating images in between two distinct input domains. MiddleGAN leverages two discriminators and one generator to create images that appear to be in both domains, resulting in blended images. The theoretical basis for MiddleGAN was covered in detail, in additional to the empirical evaluation. We extensively evaluated the capabilities of MiddleGAN on the CelebA dataset across three Blend Ratios (0.25, 0.50, and 0.75) and three Image Sizes (32px, 64px, and 128px). Our evaluation with the CelebA dataset showed the blended nature of the generated images, which contained both masculine and feminine features. In our handwritten digit based experiments, we revealed that with some adjustments of the Blend Ratio hyperparameter, MiddleGAN could handle datasets with radically different complexities (MNIST being "low" complexity and DIDA being "high" complexity). We concluded our work by outlining future opportunities for MiddleGAN as well as the limitations and caveats of MiddleGAN.

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