Risk-Controlled Event-Driven Cascading Updates for Knowledge Graph Consistency Restoration

Anonymous ACL submission

Abstract

Knowledge Graphs (KGs) provide structured and interpretable representations of real-world entities and relations. While dynamic KGs attempt to capture real-time changes, they typically treat updates as independent facts. This overlooks a critical challenge: a factual, localized update can contradict and invalidate previously correct knowledge, requiring revisions beyond the localized update to maintain KG consistency. Many of these inconsistencies arise from events whose effects propagate through relational dependencies, necessitating coordinated multi-hop reasoning rather than isolated changes. To address this, we introduce a model-agnostic framework for cascading KG update identification that leverages conformal prediction to provide reliable uncertainty guarantees over the cascade as a whole, accounting for dependencies among multi-hop update candidates. Building on this foundation, we further develop a graph-based KG update scoring framework that integrates large language models (LLMs) to enrich event representations with world knowledge. Experiments on two newly constructed real-world datasets, designed to reflect scenarios where events necessitate coordinated multi-hop updates, demonstrate that our framework establishes a strong baseline while offering calibrated confidence estimates, providing an effective solution for event-driven KG consistency restoration.

1 Introduction

Knowledge Graphs (KGs) are widely used across many applications, e.g., question answering, recommendation, and information retrieval (Ji et al., 2022). Most existing KG systems typically assume that the underlying graph is factual, consistent, and reliable (Ni et al., 2025). Yet real-world knowledge is inherently dynamic (Cai et al., 2024): new facts emerges and may lead to changes in previously valid facts. Consequently, blindly incorporating updates can leave event-invalidated facts uncorrected,

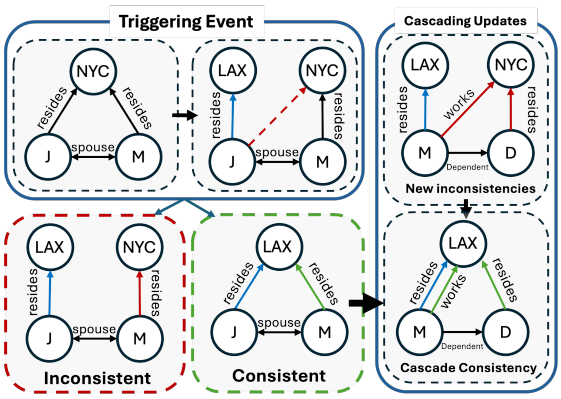


Figure 1: An illustration of event-driven cascading KG updates for consistency restoration. A triggering event, such as John moving to Los Angeles, invalidates an existing relation, and revising it reveals additional affected relations that require cascading updates.

and resolving one inconsistency may expose others via dependent relations, affecting downstream inferences. Ensuring the reliability and consistency of knowledge over time has therefore become an increasingly urgent challenge.

In practice, the effects of real-world events rarely remain confined to a single fact. As illustrated in Figure 1, events such as a change in residence can invalidate existing relations and require updates to restore local consistency. Importantly, revising one event-invalidated relation may expose additional dependent relations that also require revision. This dependency-driven behavior makes traditional KG completion and temporal forecasting models insufficient, as they assume missing but internally consistent facts. Simply adding new triplets without accounting for such dependencies can therefore leave the knowledge graph inconsistent, resulting in an inaccurate representation of the evolving world.

To accommodate the new information, prior work has primarily focused on synchronizing knowledge graphs with structured sources such as encyclopedias and external knowledge bases (Morsey et al., 2012; Liang et al., 2017).

For instance, Liang et al. (2017) relies on predefined rules and extractors tailored for Wikipedia to update the KG. While effective for integrating structured updates, such methods do not extend naturally to unstructured or event-driven inputs due to their reliance on rigid pipelines. More importantly, they lack mechanisms to assess whether updates restore consistency beyond the immediate change, making them ill-suited for scenarios where events require coordinated multi-hop revisions.

More recently, Tang et al. (2019) investigated knowledge graph updates from news snippets, leveraging a text-based attention mechanism to model both explicit and implicit updates from unstructured text inputs. Despite these advances, important limitations remain. First, the reliance on textual descriptions limits applicability in domains where rich textual coverage is unavailable. Second, the approach focuses primarily on local, one-hop changes and does not adequately capture multi-hop cascading updates induced by events through structural dependencies in the knowledge graph.

In this work, we propose a model-agnostic framework, CASCADEKG, to systematically address event-driven cascading updates in knowledge graphs. Our framework leverages the Learn-Then-Test (LTT) (Angelopoulos et al., 2022) calibration to provide statistical guarantees over multi-hop edge updates within the needed update cascade, ensuring that the propagated changes remain within a calibrated uncertainty bound. Rather than committing to individual updates in isolation, LTT supports uncertainty-aware identification of coordinated updates required to restore consistency. Additionally, ensuring consistency in real-world updates often requires external world knowledge to interpret event semantics and relational dependencies that are not explicitly encoded in the graph. Existing methods that rely solely on structural patterns therefore fall short in capturing these nuanced contextual cues. To this end, we develop a **T**ext-**au**gmented KG Update **S**coring Framework, TAUS, that integrates large language models (LLMs) to enrich event representations with contextual and world knowledge, enabling more faithful consistency restoration under real-world conditions.

To evaluate the proposed framework, we construct two new datasets derived from the Integrated Crisis Early Warning System (ICEWS) (Boschee et al., 2015) and Wiki knowledge graphs (Suchanek et al., 2007), designed to reflect scenarios where events necessitate coordinated multi-hop updates. Extensive experiments demonstrate that our approach consistently outperforms baselines, including rule-based methods, embedding-only models, and text-dependent GNNs, across multiple evaluation metrics. These results highlight the effectiveness of uncertainty-aware, event-conditioned graph reasoning for restoring consistency in knowledge graphs as real-world dynamics unfold.

Our key contributions can be summarized as:

- We identify and address the problem of event-driven cascading knowledge graph updates, where trigger events invalidate existing facts and require coordinated multi-hop revisions to restore consistency.
- We propose a model-agnostic risk control framework for multi-hop update identification that provides statistical guarantees over cascades of update candidates.
- We develop an event-conditioned, text-augmented graph reasoning framework for KG update scoring that captures relational effects triggered by events.
- We construct two new benchmark datasets from ICEWS and Wiki, designed to reflect event-driven cascading update scenarios, and conduct extensive experiments on these datasets to demonstrate the effectiveness of the proposed framework.

2 Problem Formulation

Before presenting our framework, we formally define the problem of event-driven cascading knowledge graph updates. We begin by introducing the necessary notations and the concept of consistency-aware updates, then present our proposed framework called CASCADEKG in Section 3.

2.1 Preliminaries

Let $\mathcal{G} = (\mathcal{E}, \mathcal{R}, \mathcal{T})$ denote a knowledge graph, where $\mathcal{E}$ and $\mathcal{R}$ are sets of entities and relations, respectively, and $\mathcal{T} \subseteq \mathcal{E} \times \mathcal{R} \times \mathcal{E}$ is the set of factual triplets. We define a *trigger event* e as a single KG update that necessitates a modification to $\mathcal{G}$ to reflect the current state of the world.

2.2 Cascading KG Updates

Standard KG completion treats updates as isolated predictions (Chen et al., 2020). However, in dynamic environments, a single event often initiates a chain reaction of logical consequences. To capture this, we model the update process as an iterative cascade as follows:

Definition 1 (Event-Driven Cascading KG Update)**.** *Given an initial knowledge graph $\mathcal{G}_0$ and a trigger event e, let $\mathcal{G}_e \subseteq \mathcal{G}_0$ be an initial event-centered subgraph within L-hop of nodes in e. The cascading update process is defined as a sequence of state transitions $\mathcal{G}_0 \xrightarrow{\Delta_0} \mathcal{G}_1 \xrightarrow{\Delta_1} \dots \xrightarrow{\Delta_K} \mathcal{G}_K$, where:*

1. *Δ_0 represents the explicit update(s) directly specified by e.*

2. *For each subsequent step $k > 0$, the update Δ_k is the set of implicit cascading updates triggered by the changes in Δ_{k-1}. Crucially, Δ_k is derived by reasoning over the evolved local context $\mathcal{G}_e \cup \left(\bigcup_{i=0}^{k-1} \Delta_i\right)$. This formulation ensures that the prediction of the k-th stage integrates the cumulative relational dependencies introduced in all preceding stages.*

The objective is to identify the cumulative update set $\Delta_{total} = \bigcup_{k=0}^{K} \Delta_k$ such that the final graph $\mathcal{G}_K$ achieves global consistency and faithfulness to the real-world dynamics initiated by e.

Essentially, the *output* of step k serves as the *input trigger* for step $k+1$, propagating changes through the graph structure of the knowledge graph.

Remark 1 (Consistency vs. Forecasting). It is crucial to distinguish our setting from standard Dynamic Knowledge Graph forecasting (Jiang et al., 2025), which typically aims to predict *future* facts based on historical trends. In contrast, our objective is *maintaining consistency*. We aim to derive the logical ramifications of an event to ensure the KG remains non-contradictory and complete immediately following the trigger. For instance, if e is "John moves to LA," the update "John lives in LA" (Δ_0) logically implies "John's spouse lives in LA" (Δ_1). In other words, this is a synchronization of state, not a prediction of the future.

2.3 Error Accumulation in Cascading Knowledge Graph Updates

One of the biggest challenges in a cascading setting is error accumulation (He et al., 2025); a false positive at hop k can trigger a hallucinated cascade at $k+1$. Therefore, relying on deterministic predictions is insufficient for reliable system deployment.

Remark 2 (Risk Control with Prediction Sets). To resolve the issue of error propagation, instead of predicting a single deterministic graph state, we formulate the problem through the lens of uncertainty quantification (Angelopoulos and Bates, 2022). A trivial solution—predicting all possible relations between nodes—would guarantee perfect recall but renders the graph uselessly dense. Conversely, a highly selective model may miss critical cascading effects. To balance this, we seek to generate a *prediction set* $\mathcal{C}(e)$ of candidate updates that maximizes the retrieval of true updates while minimizing the size of the set $|\mathcal{C}(e)|$. Similar to uncertainty quantification tasks, formally, we aim to generate a prediction set $|\mathcal{C}(e)|$ that controls the expected recall risk:

$$\mathbb{E}\left[\frac{|\Delta_{\text{true}} \cap \mathcal{C}(e)|}{|\Delta_{\text{true}}|}\right] \geq 1 - \alpha \qquad (1)$$

where α is a user-specified error rate and Δ_{true} is ground truth update set.

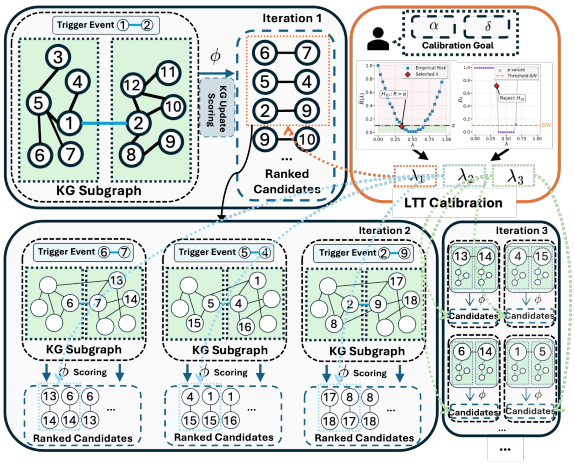


Figure 2: Overview of the proposed CASCADEKG.

3 CASCADEKG

We propose CASCADEKG, a unified framework designed to address the challenge of event-driven cascading updates in knowledge graphs. At a high level, CASCADEKG aims to tackle two fundamental challenges inherent to cascading knowledge graph updates. First, to address the issue of *error accumulation*, we propose a model-agnostic calibration framework based on Learn-then-Test (LTT) (Angelopoulos et al., 2022). This component provides rigorous statistical guarantees, ensuring that propagated updates remain within a confidence interval. Second, to effectively model *world state consistency* after an event, which necessitates reasoning beyond rigid graph structures, we introduce a text-augmented graph encoder-decoder framework that integrates LLMs to generate rich textual descriptions of triggering events, thereby enriching the structural and semantic node representations

with external world knowledge. In the remainder of this section, we first introduce the calibration framework for controlling cascading error accumulation, and subsequently detail the architecture of our text-augmented graph reasoning model.

3.1 Risk Control for Cascading KG Updates

The cascading nature of event-driven Knowledge Graph (KG) predictions poses significant challenges for standard uncertainty quantification methods, such as standard Conformal Prediction (Vovk et al., 2005; Angelopoulos and Bates, 2022), which typically assume single-step inference. In our setting, updates are multi-step and recursive; a decision made at iteration k determines the input for iteration $k+1$. To control the cumulative error risk across this dynamic process, we leverage the Learn-Then-Test (LTT) (Angelopoulos et al., 2022) framework. LTT treats the calibration task as a multiple-hypothesis testing problem over the hyperparameter space, allowing us to find a configuration that controls the overall risk of the cascade.

The Learn-Then-Test Framework. Formally, we consider a loss function $L_\lambda : \mathcal{Y} \times \hat{\mathcal{Y}} \to \mathbb{R}$ parameterized by a configuration λ drawn from a multi-dimensional search space Λ. Our objective is to ensure that the expected risk remains below a user-specified threshold α, such that $\mathbb{E}[L_\lambda] \leq \alpha$. Given a calibration dataset $\mathcal{D}_{\text{cal}}$, the LTT framework identifies a subset of valid hyperparameters, denoted as $\Lambda_{\text{valid}} \subseteq \Lambda$, which satisfies the probabilistic guarantee:

$$\mathbb{P}\left(\sup_{\lambda \in \Lambda_{\text{valid}}} \mathbb{E}[L_\lambda] \leq \alpha \right) \geq 1 - \delta \qquad (2)$$

where the probability $\mathbb{P}$ is taken over the randomness of the calibration set $\mathcal{D}_{\text{cal}}$, and the expectation $\mathbb{E}$ is taken over the underlying data distribution. Effectively, δ bounds the probability that the selected valid set fails to meet the risk constraint. To achieve this, we formulate a hypothesis test for each configuration $\lambda \in \Lambda$ with the null hypothesis $H_0^\lambda : \mathbb{E}[L_\lambda] > \alpha$. We derive super-uniform p-values p_λ via concentration inequalities (e.g., Hoeffding-Bentkus) and subsequently apply a Family-Wise Error Rate (FWER) controlling procedure to isolate the set of valid configurations Λ_{valid}.

KG Update Scoring. In the context of cascading KG updates, we define the configuration $\boldsymbol{\lambda}$ as a vector of decision thresholds, where λ_k corresponds to the cutoff threshold at cascade stage k. Let $\phi(\tau \mid e, \mathcal{G})$ be a scoring model (e.g., GNN based or embedding based) that assigns a likelihood score to a candidate triplet $\tau = (h, r, t)$ given the trigger event e and the current graph state $\mathcal{G}$.

For a given event e, the set of predicted updates $\mathcal{C}_{\boldsymbol{\lambda}}(e)$ is constructed recursively. At each stage k, the model evaluates all candidate triplets $\mathcal{E}_{cand}^{(k)}$ within the event-conditioned subgraph. The resulting state of the graph, $\mathcal{G}_k$, is formed by the set of all triplets that satisfy the stage-specific threshold λ_k. Formally, the updates at stage k are defined by the symmetric difference in graph states:

$$\Delta_k = \mathcal{G}_k \triangle \mathcal{G}_{k-1} = (\mathcal{G}_k \setminus \mathcal{G}_{k-1}) \cup (\mathcal{G}_{k-1} \setminus \mathcal{G}_k) \quad (3)$$

where $\mathcal{G}_k = \{\tau \in \mathcal{E}_{cand}^{(k)} \mid \phi(\tau \mid e, \mathcal{G}_{k-1}) \geq \lambda_k\}$.

To ensure the reliability of the update mechanism, we design our loss function to prioritize recall over precision. In the context of maintaining KG consistency, a missed update (false negative) leads to a corrupted graph state, whereas including extra candidate edges (false positives) is a tolerable cost that can be filtered by downstream verification (e.g. human verification in high-stakes applications). Therefore, we define the loss function based on the recall of the predicted set. We formulate $L_{\boldsymbol{\lambda}}$ as the *recall error*. For a ground truth update set Δ_{true}, the loss is defined as:

$$L_{\boldsymbol{\lambda}}(\Delta_{\text{true}}, \mathcal{C}_{\boldsymbol{\lambda}}(e)) = 1 - \frac{|\Delta_{\text{true}} \cap \mathcal{C}_{\boldsymbol{\lambda}}(e)|}{|\Delta_{\text{true}}|} \qquad (4)$$

In this formulation, a loss of 0 corresponds to perfect recall (all ground truth updates are successfully retrieved), while a loss of 1 indicates that no correct updates were identified. By controlling this risk, we effectively guarantee that the expected recall remains above $1 - \alpha$.

The LTT algorithm then processes the calibration set $\mathcal{D}_{\text{cal}}$ to identify Λ_{valid}, the set of all threshold vectors that statistically satisfy the risk control. We select the optimal configuration:

$$\boldsymbol{\lambda}^* = \operatorname*{argmin}_{\boldsymbol{\lambda} \in \Lambda_{\text{valid}}} \sum_{e \in \mathcal{D}_{\text{cal}}} |\mathcal{C}_{\boldsymbol{\lambda}}(e)| \qquad (5)$$

i.e., the most informative (smallest) prediction set.

Theorem 1 (Probabilistic Guarantee). Let $\mathcal{D}_{\text{cal}}$ be the calibration set and Λ_{valid} be the set of configurations identified by the LTT procedure satisfying Eq. 2. For any chosen configuration $\hat{\boldsymbol{\lambda}} \in \Lambda_{\text{valid}}$, the expected recall on the test distribution satisfies the guarantee defined in Eq. 1 with probability at least $1 - \delta$ over the randomness of the calibration data.

The proof of Theorem 1 is given in Appendix A.

3.2 Event-Conditioned Graph Reasoning for Knowledge Graph Update Scoring

Although the proposed Cascading Calibration in Section 3.1 provides a principled mechanism for controlling error propagation across update cascades, it does not address how candidate updates should be semantically prioritized at each stage. In practice, calibration alone cannot compensate for a fundamentally noisy or uninformed update scoring function. Without a way to distinguish event-consistent updates from spurious candidates, the number of scored edges can grow rapidly due to the combinatorial structure of KGs, rendering even calibrated prediction sets impractically large.

A critical bottleneck therefore lies in designing an *event-conditioned update scoring function* that assigns meaningful plausibility scores to candidate structural changes based on the semantic context of the triggering event, incorporating external world knowledge to better reason about relational consequences not explicitly encoded in the graph.

To this end, we propose a Text-Augmented Update Scoring framework, TAUS, which assigns event-conditioned plausibility scores to candidate structural changes in the localized KG. TAUS leverages natural language descriptions of event-induced updates generated from the trigger event to provide semantic context that grounds graph-based reasoning when evaluating candidate updates. Next, we provide the formal details of TAUS.

Event Context Generation. Encoding *world state consistency* directly into the model is challenging, as real-world events are heterogeneous and often governed by complex causal factors that are absent from the rigid KG structure. To address this, we leverage the extensive world knowledge of LLMs to bridge the gap between raw events and their relational consequences. The goal of this component is to provide a rich natural language context for the structural graph edits $\Delta\mathcal{T}$ that arise from an external trigger event e.

We adopt a *Teacher-Student* framework to capture this logic, which is visualized in Figure 3. First, we employ a powerful teacher LLM (M_t) to generate explanatory paragraphs for ground-truth event-update pairs $(e, \Delta\mathcal{T})$. In this step, the teacher explicitly articulates the underlying causal logic connecting the event to the corresponding topology changes. Second, we fine-tune a student model (M_s) on these generated rationales. This ensures the student learns to produce faithful text descriptions that reflect the necessary consistency updates, effectively internalizing the mapping from events to KG updates/modifications.

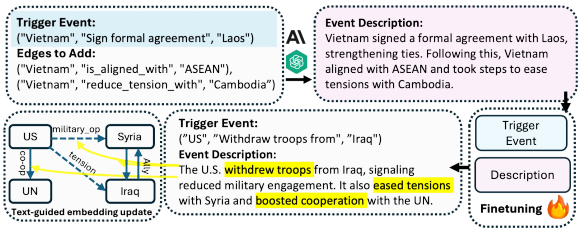


Figure 3: Overview of the proposed TAUS.

Specifically, let $\mathcal{D} = \{(e_i, \Delta\mathcal{T}_i)\}$ be the training set of events and their corresponding KG updates. We first use the teacher M_t to generate a descriptive rationale x_i for each pair, such that $x_i \sim M_t(e_i, \Delta\mathcal{T}_i)$. This yields an augmented dataset $\mathcal{D}_{\text{aug}} = \{(e_i, x_i)\}$. We then fine-tune the student model M_s, parameterized by θ, to minimize the negative log-likelihood of generating the rationale given the event:

$$\mathcal{L}_{\text{gen}}(\theta) = -\mathbb{E}_{(e,x)\sim\mathcal{D}_{\text{aug}}}\left[\log P_{M_s}(x \mid e; \theta)\right] \quad (6)$$

During inference, the smaller (and faster) M_s is used to generate the context $\hat{x}$ for a new event e, guiding the downstream graph reasoning.

Text-Conditioned Graph Encoding. To incorporate the generated event context into the update scoring, we condition graph-based reasoning on semantic representations derived from text. Specifically, we use a pre-trained sentence encoder (e.g., Sentence-Transformers (Reimers and Gurevych, 2019)) to embed the textual rationale $\hat{x}$ produced by the student model M_s into a vector $\mathbf{z}_{\text{txt}} \in \mathbb{R}^{d_t}$. This embedding serves as the semantic conditioning signal that captures event-specific context.

To propagate this semantic signal through the knowledge graph, we instantiate the scoring function using a Relational Graph Convolutional Network (R-GCN) (Schlichtkrull et al., 2018) as the backbone encoder. The text embedding is projected into the graph feature space via a learnable transformation $W_t \in \mathbb{R}^{d \times d_t}$ and injected into the initial node representations, effectively shifting the initial feature distribution based on the event context. For each node v, the conditioned initialization is given by $\mathbf{h}_v^{(0)} = \mathbf{h}_v^{\text{raw}} + W_t \mathbf{z}_{\text{txt}}$, where $\mathbf{h}_v^{\text{raw}}$ denotes the static pre-trained KG embedding. These conditioned embeddings are then updated through the R-GCN message passing to capture relational dependencies, enabling relation-aware graph reasoning that integrates both local KG structural dependencies and event semantics for KG update scoring.

4 Experiments

In this section, we evaluate CASCADEKG in the context of event-driven cascading updates. Our experimental design follows a two-stage logic to address our core research questions.

First, regarding **RQ1 (Reasoning Capability)**, we evaluate the raw predictive performance of our proposed TAUS against existing KG embedding methods as scoring functions to determine if event-conditioning aids in identifying structural updates. Second, we study the effectiveness of our LTT-based framework for cascading KG updates as **RQ2 (Error Accumulation Control)**. We demonstrate the effectiveness of our plug-and-play calibration component by evaluating it across multiple scoring backbones and comparing it against post-hoc strategies. To rigorously address these questions, we construct two new benchmarks, ICEWS14-Event and YAGO-Event, which explicitly model the cascading changes introduced by external events in the knowledge graph.

4.1 Datasets

Evaluating performance on event-driven cascading KG updates requires a benchmark that captures both event-driven evolution and logical consistency constraints. However, most KG benchmarks are focused on KG completion that predicts missing edges in a fixed structure rather than modeling the causal ripple effects of external events. To bridge this gap and evaluate CASCADEKG, we thus curate two new datasets derived from real-world KGs. Additional dataset details are in Appendix B.

ICEWS14-Event. We construct the ICEWS14-Event dataset from The Integrated Crisis Early Warning System (ICEWS) (Boschee et al., 2015) dataset, which consists of structured geopolitical events between entities over time. To construct the knowledge graphs with corresponding updates, we incrementally build the KG based on the chronological order of incoming events.

YAGO-Event. The YAGO-Event dataset is constructed from the YAGO (Suchanek et al., 2007) knowledge base, which is a large semantic graph constructed from Wikipedia, WordNet, and GeoNames, containing rich entity-type and relation-type annotations. Because the YAGO3-10 dataset does not contain naturally occurring changes, we synthetically simulate event-triggered updates by applying a set of inference rules to its static triples.

4.2 Comparison Methods

To comprehensively evaluate the performance of CASCADEKG and KG update scoring module TAUS, we include two distinct families of baselines: established post-hoc calibration strategies and KG embedding models for scoring.

4.2.1 Cascade Calibration Baselines

Aggregate (Agg). This strategy serves as a naive baseline that ignores the hierarchical structure of the graph data. Instead of distinguishing between hops, we collapse the calibration sets from both the one-hop and two-hop neighbors into a single pool. We then apply standard split conformal prediction on this aggregated set.

Bonferroni Conformal (Con). This baseline acknowledges the multi-hop structure but avoids the complexity of the Learn-then-Test framework. Instead of dynamically selecting hypotheses, we treat the one-hop and two-hop neighborhoods as fixed, independent calibration tasks. We then apply a standard Bonferroni correction to control the global risk by calibrating each hop independently at a stricter error rate of $\alpha/2$.

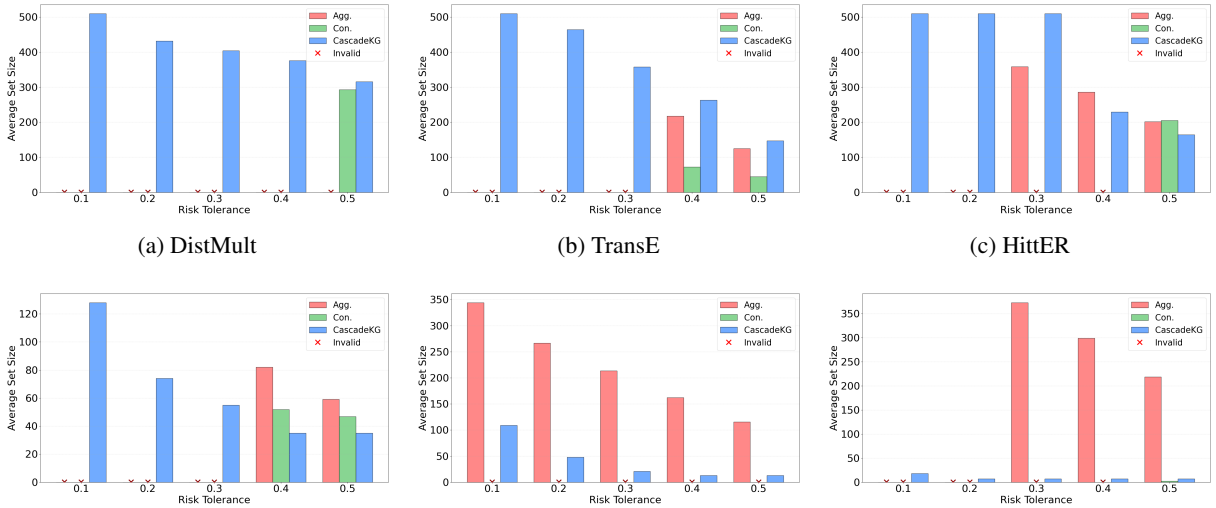
4.2.2 KG Update Scoring Baselines

To evaluate the effectiveness of our proposed text-augmented graph reasoning module TAUS for KG update scoring, we compare against the following representative KG update scoring methods: DistMult (Yang et al., 2015), R-GAT (Busbridge et al., 2019), TransE (Bordes et al., 2013), HittER (Chen et al., 2021), CompGCN (Vashishth et al., 2019). More details are presented in Appendix C.

4.3 Evaluation Metrics

To comprehensively evaluate CASCADEKG, we utilize two distinct categories of metrics. First, to assess the raw predictive power of the scoring backbones (**RQ1**), we report standard classification metrics including Accuracy, F1-score, and Recall. These metrics measure the model's ability to distinguish valid additions and deletions from noise before calibration is applied.

Second, to evaluate the statistical reliability and efficiency of our calibration framework (**RQ2**), we follow the uncertainty quantification literature (Angelopoulos and Bates, 2022) and adopt two specialized metrics. **ECR (Empirical Coverage Rate)** measures the reliability of the system by calculating the frequency with which the ground-truth update



(a) DistMult (b) TransE (c) HittER

(d) CompGCN (e) R-GAT (f) TAUS

Figure 4: Efficiency comparison of the calibration baselines on the six backbone models for YAGO-Event. Red cross is marked if the calibration method cannot achieve the desired risk tolerance. For each risk tolerance level, the lower the bar the better.

Model	F1	Acc.	Rec.	MRR	AUROC
DistMult	0.804	0.769	0.950	0.331	0.769
R-GAT	0.798	0.788	0.836	0.339	0.788
TransE	0.787	0.784	0.800	0.237	0.784
HittER	0.737	0.667	0.931	0.114	0.667
CompGCN	0.765	0.713	0.932	0.293	0.713
TAUS	**0.880**	**0.866**	**0.985**	**0.435**	**0.866**

Table 1: KG Update Scoring Methods Performance in ICEWS14-Event.

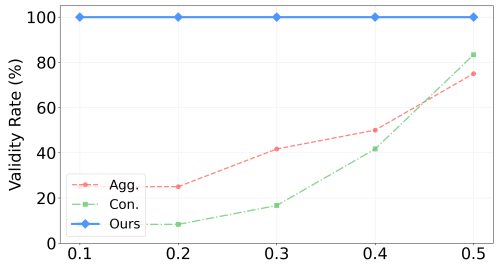


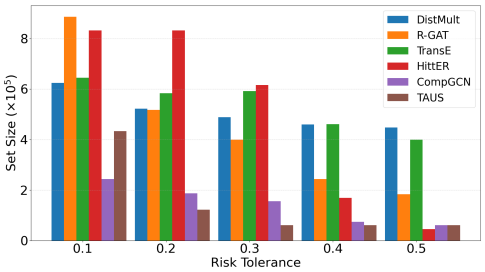
Figure 5: Calibration Methods Valid Coverage Rate.

set is fully contained within the predicted set; a system is considered valid if its ECR remains above the $1-\alpha$ threshold. Conversely, **APSS (Average Prediction Set Size)** evaluates the efficiency of the model. While high ECR can be trivially achieved with large sets, a practical update mechanism must be informative. APSS measures the average cardinality of the predicted sets, where a smaller value indicates a more precise model that filters out irrelevant candidates while maintaining the required statistical guarantees.

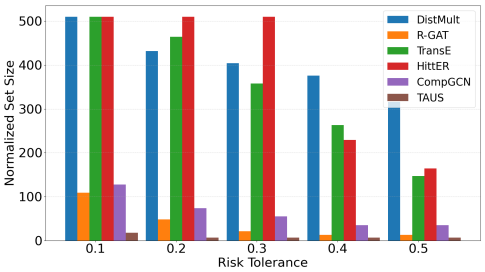
4.4 Experimental Results Results

Predictive Performance of the Scoring Module (RQ1). We first evaluate the fundamental ability of the underlying scoring models to correctly identify valid structural updates. We report the performance of various KG scoring backbones on the ICEWS14-Event datasets in Table 1. As shown in the table, our proposed TAUS backbone consistently demonstrates superior performance across all evaluation metrics on both datasets. Specifically, TAUS achieves an F1-score of 0.880 and an accuracy of 0.866, significantly outperforming traditional embedding methods like TransE and structural GNNs like R-GAT. Additional case study in Appendix D.1 further reveals that by integrating LLM-generated rationales, TAUS effectively grounds its reasoning in external world knowledge, capturing the semantic dependencies required to maintain global KG coherence in real-world.

Error Control (RQ2). To answer RQ2, we evaluate the effectiveness of the proposed CASCADEKG calibration framework by specifying varying risk levels α for the KG update scoring backbones. We report the relationship between coverage and prediction set size for the YAGO-Event dataset in Figure 4. For ECR that does not satisfy the risk tolerance, red crosses are used to mark the method. The detailed numerical results (ECR, etc.) are supplied in Appendix D. As observed across all model backbones, our calibration framework consistently achieves the smallest prediction set size while sat-



(a) Results for ICEWS14-Event.



(b) Results for YAGO-Event.

Figure 6: Experimental results scoring backbones coupled with CASCADEKG.

isfying the target coverage. Notably, as visualized in Figure 5, CASCADEKG succeeds in maintaining valid coverage across all specified risk levels. This reliability is a direct result of the Learn-Then-Test procedure, which explicitly manages the risk budget across successive cascading stages to prevent error amplification. Results for ICEWS14-Event exhibit similar trend and are included in Appendix D.

Furthermore, in Figure 6, we plot the scoring backbones calibrated with CASCADEKG. our result demonstrates that the effectiveness of the calibration framework is significantly enhanced when paired with stronger underlying reasoning models such as TAUS, which integrate LLM-enriched event representations, producing the smallest prediction sets. This highlights CASCADEKG's ability to manage error propagation in cascading updates. By adaptively calibrating thresholds across different stages of the cascade, our framework avoids the "explosion" of predicted edges that typically renders uncalibrated KG update systems impractical.

5 Related Work

KG Predictions and Updating Most KG embedding and temporal KG work studies link prediction or forecasting under the assumption that each KG snapshot is internally coherent (Wang et al., 2017; Ji et al., 2022; Trivedi et al., 2017; Dasgupta et al., 2018; Liu et al., 2020). In contrast, our setting is triggered by external events that can invalidate previously correct facts and require consistency restoration via a sequence of iterative updates that cascade through relational dependencies.

Early KG update systems primarily synchronized KGs with structured sources (e.g., Wikipedia/encyclopedias) via curated extraction pipelines (Morsey et al., 2012; Liang et al., 2017). More recent work explores updating KGs from unstructured streams such as news (Tang et al., 2019), and related lines study KG consistency control (Wang et al., 2021; Padia et al., 2024).

KG Embedding Methods. Knowledge graph embedding methods are mainly developed for KG completion by scoring candidate triplets. In our experiments, we compare representative backbones spanning major modeling families: bilinear (DistMult) (Yang et al., 2015), translational (TransE) (Bordes et al., 2013), relational GNN encoders (R-GAT, CompGCN) (Busbridge et al., 2019; Vashishth et al., 2019), and Transformer-based KGE (HittER) (Chen et al., 2021). We note that a further discussion on these is provided in Appendix C. Recent KG completion models continue to build on these directions by adding stronger path reasoning or language-model-based formulations (e.g., NBFNet (Zhu et al., 2021), SimKGC (Wang et al., 2022) KGT5 (Saxena et al., 2022), KGT5-context (Kochsiek et al., 2023)), which are largely complementary to our cascade-level risk control and event-conditioned update scoring.

6 Conclusion

In this paper, we addressed the challenge of Knowledge Graph consistency through event-driven cascading updates. Our proposed framework, CASCADEKG, utilizes the Learn-Then-Test calibration framework to provide rigorous statistical guarantees on multi-hop update reliability, effectively managing error propagation. Furthermore, we introduced a text-augmented GNN module TAUS that leverages LLMs to enrich event representations with world knowledge. Experimental results on the newly curated ICEWS14-Event and YAGO-Event datasets demonstrate that CASCADEKG significantly outperforms baseline scoring and calibration methods. By integrating structural reasoning with textual context, our approach offers an effective solution for maintaining global KG consistencies in real-world event-driven environments.

7 Limitations

While CASCADEKG provides rigorous statistical guarantees, a primary limitation lies in the assumption that calibration and test data share the same distribution; in volatile real-world scenarios, frequent re-calibration may be necessary to maintain reliability under distribution shift. Furthermore, although our theoretical symmetric difference formulation $\Delta_k = \mathcal{G}_k \triangle \mathcal{G}_{k-1}$ accounts for both additions and deletions, our current empirical evaluation on the ICEWS14-Event and YAGO-Event benchmarks focuses primarily on edge additions due to the growth-oriented nature of these historical datasets. Future work should explicitly investigate CASCADEKG's performance in high-deletion environments and develop adaptive calibration techniques to ensure long-term reliability under evolving world dynamics.

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A Probabilistic Guarantee Proof of our Cascading Calibration Framework

Here we provide the detailed proof of Theorem 1.

Proof. Recall that our loss function is defined as the recall error:

$$L_{\boldsymbol{\lambda}} = 1 - \text{Recall}_{\boldsymbol{\lambda}} = 1 - \frac{|\Delta_{\text{true}} \cap \mathcal{C}_{\boldsymbol{\lambda}}(e)|}{|\Delta_{\text{true}}|} \quad (7)$$

The Learn-Then-Test condition (Eq. 2) guarantees that:

$$\mathbb{P}\left(\sup_{\lambda \in \Lambda_{\text{valid}}} \mathbb{E}[L_\lambda] \leq \alpha\right) \geq 1 - \delta \quad (8)$$

Let E be the event that the calibration succeeds, i.e., $\forall \lambda \in \Lambda_{\text{valid}}, \mathbb{E}[L_\lambda] \leq \alpha$. The algorithm ensures $\mathbb{P}(E) \geq 1 - \delta$. Conditioned on event E, for any selected $\hat{\boldsymbol{\lambda}} \in \Lambda_{\text{valid}}$, we have:

$$\mathbb{E}[L_{\hat{\boldsymbol{\lambda}}}] \leq \alpha \quad (9)$$

$$\mathbb{E}[1 - \text{Recall}_{\hat{\boldsymbol{\lambda}}}] \leq \alpha \quad (10)$$

$$\mathbb{E}[\text{Recall}_{\hat{\boldsymbol{\lambda}}}] \geq 1 - \alpha \quad (11)$$

Thus, the expected recall is lower-bounded by $1-\alpha$ with probability at least $1-\delta$. When δ is sufficiently small, we can approximate this probabilistic bound as Eq. 1, effectively guaranteeing that the system satisfies the target recall. □

B Dataset Details: Construction and Characteristics

In this section, we provide additional details regarding the construction and characteristics of the two newly constructed benchmarks used in our evaluation: ICEWS14-Event and YAGO-Event.

For both datasets, ground-truth cascading updates are obtained by recursively applying predefined consistency rules to an initial trigger event until the graph reaches a stable, consistent state. This iterative process mimics the "ripple effect" of real-world event consequences. We summarize the key statistics for both datasets in Table 2 and provide the exhaustive set of logical consistency rules in Tables 3 and 4.

Table 2: Statistics of the constructed ICEWS14-Event and YAGO-Event datasets. We report the number of event samples, unique entities, and unique relations active in each split. The **Avg. Subgraph Nodes** column reports the mean number of entities in the event-conditioned subgraph (local L-hop neighborhood) $\pm$ the standard deviation.

Dataset	Split	# Samples	# Entities	# Relations	Avg. Subgraph Nodes
ICEWS14-Event	Train	7,605	1,230	160	41.90 ± 28.81
	Valid	108	114	36	12.93 ± 8.95
	Test	107	147	50	14.60 ± 10.46
	Overall	*7,820*	*1,252*	*161*	–
YAGO-Event	Train	20,152	22,320	43	96.88 ± 12.81
	Valid	1,963	9,545	43	95.69 ± 15.56
	Test	2,034	9,597	41	95.15 ± 16.09
	Overall	*24,149*	*26,851*	*43*	–

B.1 ICEWS14-Event

The ICEWS14-Event dataset is derived from the Integrated Crisis Early Warning System (ICEWS) (Boschee et al., 2015) repository, which records geopolitical interactions between international actors. For each time step t, we define the knowledge graph $\mathcal{G}_t$ as the aggregation of all historical facts observed up to day t. Changes introduced by new events on day $t+1$ are denoted as $\Delta\mathcal{T}_{t+1}$.

To model logical dependencies, we apply a set of hand-crafted consistency rules that propagate relational changes beyond the explicitly stated event facts. For example, if *Country A* signs a formal agreement with *Country B*, and *Country B* already maintains a military cooperation with *Country C*, our framework infers a new cooperative link between *Country A* and *Country C*. We note that for the ICEWS14-Event benchmark, the graph grows monotonically over time; i.e., updates in our current experiments consist solely of edge additions.

B.2 YAGO-Event

The YAGO-Event dataset is built upon the YAGO3-10 knowledge base (Suchanek et al., 2007). Unlike ICEWS, which is inherently temporal, YAGO is a large-scale semantic graph. To evaluate cascading updates, we synthetically simulate event-triggered changes by selecting initial event triples and applying two-hop rule patterns that reflect plausible downstream relational inconsistencies.

For each trigger event, we generate additional updates based on these patterns to evaluate the model's capacity for multi-hop reasoning in a dense, semantically rich environment. For example, as shown in Table 4, an academic trigger event such as *Person A* `hasAcademicAdvisor` *Person B*—where *Person B* previously `graduatedFrom` *University C*—would recursively infer the update *Person A* `academicLineageFrom` *University C*. Similarly, in professional contexts, if a person `playsFor` a team that `isLocatedIn` a specific city, our rules infer a corresponding `livesIn` relation.

Unlike ICEWS14-Event, the rule set for YAGO-Event is specifically designed to test structural dependencies within a localized context. This provides a controlled environment for measuring calibration efficiency, as it requires the model to ground its predictions in both the initial event and the surrounding static topology to maintain world-state consistency.

C Baseline KG Embedding Descriptions

In the below we provide some additional details on the KG embedding baselines we compare our proposed CASCADEKG against in this work.

DistMult (Yang et al., 2015): As a widely-used knowledge graph embedding model, DistMult scores triplets using a bilinear function, capturing the semantic relationships between entities.

R-GAT (Busbridge et al., 2019): Relational Graph Attention Networks (R-GAT) extends GAT to handle multi-relational data, allowing the model to weigh the importance of different neighbors.

TransE (Bordes et al., 2013): TransE is a translation-based embedding model that represents relations as translations between embeddings.

HittER (Chen et al., 2021): Hierarchical Transformers for Knowledge Graph Embeddings (HittER) is a Transformer-based model that jointly learns entity-relation composition and relational contextualization.

CompGCN (Vashishth et al., 2019): Composition-based Multi-Relational Graph Convolutional Networks (CompGCN) integrate multi-relational GCNs with KG embedding techniques.

Table 3: Selected logical consistency rules for **ICEWS14-Event**. The rules define how a trigger event (A, r_{trig}, B) interacts with precondition (B, r_{cond}, C) to infer (A, r_{new}, C).

Trigger Event	Precondition	Inferred Update	Op
Positive Cascades (Additions)			
Sign formal agreement	Engage in diplomatic coop.	Engage in diplomatic coop.	+
Provide military aid	Cooperate militarily	Cooperate militarily	+
Declare truce, ceasefire	Engage in diplomatic coop.	De-escalate intent	+
Occupy territory	Engage in diplomatic coop.	Complain officially	+
Sign formal agreement	Grant diplo. recognition	Engage in diplomatic coop.	+
Negative Cascades (Deletions)			
Break diplomatic rel.	Engage in diplomatic coop.	Break diplomatic rel.	–
Impose embargo	Cooperate economically	Cooperate economically	–
Threaten with mil. force	Engage in diplomatic coop.	Increase armed forces	–
Multi-hop / Complex Rules			
Sign formal agreement	Diplo. Coop → Mil. Coop	Cooperate militarily	+
Impose sanctions	Trade → Trade	Impose sanctions	+

Table 4: Selected horn-clause rules for **YAGO-Event**. These rules infer a new relation from a 2-hop path in the static graph.

Path Step 1 (r_1)	Path Step 2 (r_2)	Inferred Relation	Mode
Social & Family			
hasChild	hasChild	hasGrandchild	Fwd
isLeaderOf	isLocatedIn	livesIn	Fwd
playsFor	isLocatedIn	livesIn	Fwd
Academic & Professional			
graduatedFrom	isLocatedIn	wasEducatedIn	Fwd
hasAcademicAdvisor	graduatedFrom	academicLineageFrom	Fwd
owns	isLocatedIn	hasBusinessIn	Fwd
Creative Collaborations			
actedIn	directed	collaboratedWith	Cross
actedIn	wroteMusicFor	sharedCreativeWork	Cross
directed	edited	coDirectedOrEdited	Cross

D Case Study and Additional Experiments

D.1 Case Study

To demonstrate how the inclusion of additional world context can enhance the effectiveness of event-based KG update prediction, we conduct a qualitative case study on an instance where TextGCN significantly outperforms the DistMult baseline, as shown in Table 5. In this scenario, the model is tasked with predicting a missing link involving South Korea and a combatant group following a trigger event between Vietnam and Iran. As shown in the example, *TextGCN* was able to correctly rank the ground truth triplet atw1.0 for both head and tail predictions. In contrast, *DistMult*, which relies solely on existing static graph structures and lacks access to the dynamic narrative of the event, produces much lower rankings.

The world context generated by the fine-tuned LLM explicitly mentions Vietnam expanding its outreach to South Korea. By encoding this textual information, TextGCN can capture the transitive diplomatic shift that a purely structural model misses. This valuable insight thus allows the model to reason that the recent formal agreement between Vietnam and Iran has downstream effects on South Korea's diplomatic and security positioning.

D.2 Additional Experiment Details

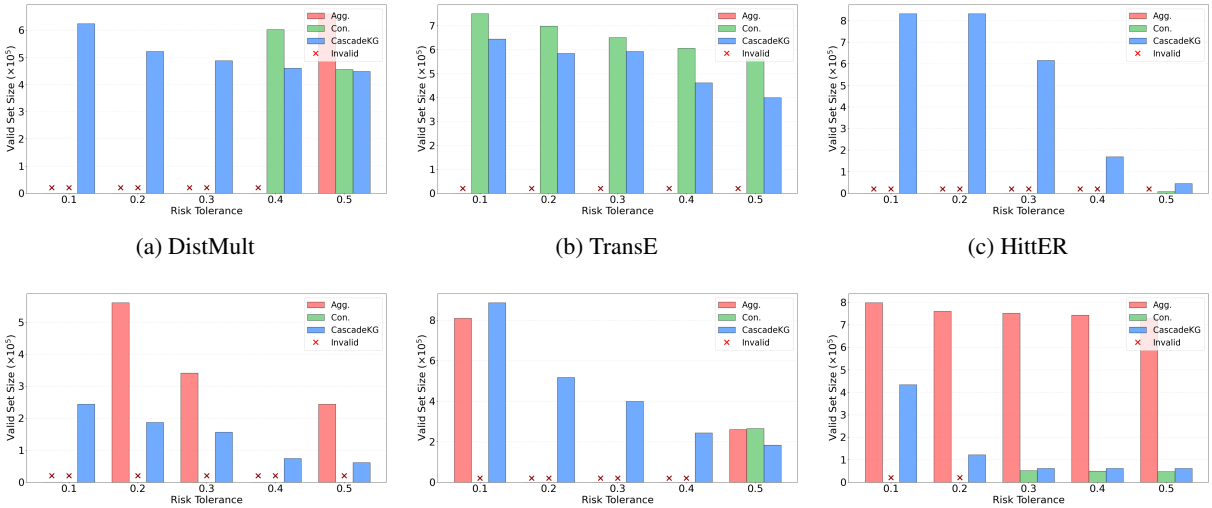
In this section, we provide the complete empirical results for all tested models. Detailed efficiency comparisons for the ICEWS14-Event dataset are presented in Figure 7, while the comprehensive numerical performance for both benchmarks is summarized in Table 6 and Table 7.

As visualized in Figure 7, the calibration trends on ICEWS14-Event mirror those observed on YAGO-Event (Figure 4). Across all scoring calibration methods, our proposed CASCADEKG consistently produces the most compact (smallest) prediction sets while strictly adhering to the user-specified risk tolerance α. These results further validate the robustness of our Learn-Then-Test framework across different graph topologies and relational distributions.

The raw numerical data in Table 6 and Table 7 provides a granular view of the Empirical Coverage Rate (ECR) and Average Prediction Set Size (APSS). These tables demonstrate that CASCADEKG significantly reduces the APSS compared to the *Aggregate* and *Conformal* baselines.

Table 5: Case Study. We list the ranking of the ground truth triplet under the method names.

Property	**Value**	**TextGCN**	**DistMult**
Context (TextGCN)	Vietnam signs agreement with Iran; expands to South Korea, Mexico, etc.	–	–
Trigger Event	(Vietnam, Sign formal agreement, Iran, 2014-10-19)	–	–
Triplet	(**South Korea**, Sign formal agreement, **Combatant (Al Qaeda)**)	1.0 / 1.0	22.0 / 16.0



(a) DistMult (b) TransE (c) HittER

(d) CompGCN (e) R-GAT (f) TAUS

Figure 7: Efficiency comparison of the calibration baselines on the six backbone models for ICEWS14-Event. Red cross is marked if the calibration method cannot achieve the desired risk tolerance. For each risk tolerance level, the lower the bar the better.

Model	Set Size (SS) / Empirical Coverage Rate (ECR)				
	α=0.1	α=0.2	α=0.3	α=0.4	α=0.5
DistMult + Agg.	800624 / 0.15	775182 / 0.32	761812 / 0.37	715362 / 0.49	660914 / 0.39
DistMult + Con.	703757 / 0.36	668810 / 0.36	636175 / 0.38	602700 / 0.39	456026 / 0.44
DistMult + Ours	**623806** / 0.07	**522011** / 0.18	**488106** / 0.23	**460345** / 0.43	**448201** / 0.44
R-GAT + Agg.	809140 / 0.00	301022 / 0.36	275660 / 0.45	265590 / 0.46	260080 / 0.46
R-GAT + Con.	422049 / 0.43	304502 / 0.45	292531 / 0.45	281099 / 0.45	265083 / 0.46
R-GAT + Ours	**886443** / 0.00	**517983** / 0.05	**399970** / 0.19	**243539** / 0.24	**182992** / 0.37
TransE + Agg.	414932 / 0.14	223511 / 0.21	160232 / 0.53	99342 / 0.56	71755 / 0.52
TransE + Con.	750339 / 0.04	698616 / 0.08	650705 / 0.13	606146 / 0.18	561997 / 0.22
TransE + Ours	**644920** / 0.02	**583993** / 0.03	**592330** / 0.10	**461069** / 0.11	**399659** / 0.15
HittER + Agg.	799278 / 0.28	797914 / 0.31	613198 / 0.37	789465 / 0.41	756304 / 0.52
HittER + Con.	693003 / 0.36	15998 / 0.42	10277 / 0.43	8345 / 0.44	7076 / 0.44
HittER + Ours	**832363** / 0.01	**832363** / 0.01	**615598** / 0.22	**168502** / 0.30	**45011** / 0.31
CompGCN + Agg.	702483 / 0.12	560816 / 0.16	341105 / 0.26	268027 / 0.44	243903 / 0.50
CompGCN + Con.	353033 / 0.38	74216 / 0.36	48989 / 0.40	46873 / 0.44	16862 / 0.58
CompGCN + Ours	**243984**/ 0.00	**186690** / 0.06	**156290** / 0.05	**74086** / 0.05	**61015**/ 0.05
TAUS + Agg.	798554 / 0.02	760599 / 0.06	752152 / 0.06	743308 / 0.06	728563 / 0.08
TAUS + Con.	73811 / 0.25	62118 /0.25	51877 / 0.26	48968 / 0.28	46903 / 0.34
TAUS + Ours	**433251** / 0.00	**121994** / 0.00	**61006** / 0.06	**61006** / 0.06	**61006**/ 0.06

Table 6: Set Size (SS) and Empirical Coverage Rate (ECR) under varying risks α on the ICEWS14-Event dataset. We note that our overall proposed framework CASCADEKG is represented as the TAUS+ Ours setting.

Model	Set Size (SS) / Empirical Coverage Rate (ECR)				
	α=0.1	α=0.2	α=0.3	α=0.4	α=0.5
DistMult + Agg.	204.49 / 0.14	181.25 / 0.23	163.71 / 0.33	150.49 / 0.42	137.63 / 0.52
DistMult + Con.	374.96 / 0.30	341.56 / 0.34	323.63 / 0.37	307.17 / 0.41	**293.21** / 0.44
DistMult + Ours	**510** / 0.00	**432** / 0.09	**404** / 0.09	**376** / 0.19	316 / 0.35
R-GAT + Agg.	344.21 / 0.09	266.61 / 0.15	213.60 / 0.22	162.29 / 0.31	115.39 / 0.41
R-GAT + Con.	64.87 / 0.29	33.74 / 0.33	20.47 / 0.37	15.40 /0.41	12.61 / 0.44
R-GAT + Ours	**109** / 0.02	**48** / 0.09	**21** / 0.17	**13** / 0.24	**13** / 0.24
TransE + Agg.	411.81 / 0.10	349.06 / 0.23	290.44 / 0.31	217.21 / 0.39	124.71 / 0.46
TransE + Con.	320.38 / 0.28	238.07 / 0.31	137.96 / 0.35	**72.52** / 0.39	**44.61** / 0.44
TransE + Ours	**510** / 0.00	**464** / 0.04	**358** / 0.15	263 / 0.27	147 / 0.42
HittER + Agg.	443.96 / 0.19	404.64 / 0.23	358.27 / 0.29	285.80 / 0.38	201.55 / 0.46
HittER + Con.	439.03 / 0.32	433.50 / 0.34	431.53 / 0.38	418.59 / 0.42	205.32 / 0.47
HittER + Ours	**510** / 0.00	**510** / 0.00	**510** / 0.00	**229** / 0.30	**164** / 0.32
CompGCN + Agg.	156.49 / 0.16	126.63 / 0.25	103.45 / 0.36	82.02 / 0.40	59.17 / 0.48
CompGCN + Con.	88.62 / 0.29	67.73 / 0.33	58.12 / 0.36	51.80 / 0.40	46.85 / 0.43
CompGCN + Ours	**128** / 0.01	**74** / 0.06	**55** / 0.11	**35** / 0.24	**35** / 0.24
TAUS + Agg.	472.98 / 0.14	430.27 / 0.22	372.79 / 0.30	299.16 / 0.37	218.87 / 0.43
TAUS + Con.	4.28 / 0.29	3.49 /0.33	3.10 / 0.37	2.79 / 0.41	**2.52** / 0.45
TAUS + Ours	**18**/ 0.02	**7** / 0.05	**7** / 0.05	**7** / 0.05	**7** / 0.05

Table 7: Normalized Set Size (SS) and Empirical Coverage Rate (ECR) under varying risks α on the YAGO-Event dataset. We note that our overall proposed framework CASCADEKG is represented as the TAUS+ Ours setting.