Variational Automatic Curriculum Learning for Sparse-Reward Cooperative Multi-Agent Problems

Abstract

We introduce a curriculum learning algorithm, *Variational Automatic Curriculum Learning* (VACL), for solving challenging goal-conditioned cooperative multi-agent reinforcement learning problems. We motivate our paradigm through a variational perspective, where the learning objective can be decomposed into two terms: task learning on the current task distribution, and curriculum update to a new task distribution. Local optimization over the second term suggests that the curriculum should gradually expand the training tasks from easy to hard. Our VACL algorithm implements this variational paradigm with two practical components, task expansion and entity progression, which produces training curricula over both the task configurations as well as the number of entities in the task. Experiment results show that VACL solves a collection of sparse-reward problems with a large number of agents. Particularly, using a single desktop machine, VACL achieves 98% coverage rate with 100 agents in the simple-spread benchmark and reproduces the ramp-use behavior originally shown in OpenAI's hide-and-seek project.

1 Introduction

Building intelligent agents in complex multi-agent games remains a long-standing challenge in artificial intelligence [21]. Recently, it has been a trend to apply multi-agent reinforcement learning (MARL) to extremely challenging multi-agent games, such as Dota II [5], StarCraft [27] and Hanabi [3]. Despite these successes, learning intelligent multi-agent policies in general still remains a great RL challenge. Multi-agent games allow sophisticated interactions between agents and environment. Feasible solutions may require non-trivial intra-agent coordination, which leads to substantially more complex strategies than the single-agent setting. Moreover, as the number of agents increases, the joint action space grows at an exponential rate, which results in an exponentially large policy search space. Thus, most existing MARL applications typically require shaped rewards, or assume simplified environment dynamics, or only handle a limit number of agents.

We tackle goal-conditioned cooperative MARL problems with *sparse* rewards through a novel variational inference perspective. Assuming each task can be parameterized by a continuous representation, we introduce a variational proposal distribution over the task space and then decomposing the overall training objective into two separate terms, a policy improvement term and a task proposal update term. By treating the proposal distribution updates as the training curriculum, such a variational objective naturally suggests a curriculum learning framework by alternating between curriculum update and MARL training. In addition, we propose a continuous relaxation technique for discrete variables so that the variational curricula can be also applied over the number of agents and objects in the task, which leads to a generic and unified training paradigm for the MARL setting.

We implement our variational training paradigm through a computationally efficient algorithm, *Variational Automatic Curriculum Learning (VACL)*. VACL consists two components, *task expansion*

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and *entity progression*, which generate a series of effective training tasks in a hierarchical manner. Intuitively, *entity progression* leverages the inductive bias that tasks with more entities are usually more difficult MARL and progressively increases the entity size in the environment. *Task expansion* assumes a fixed number of entities and is motivated by Stein variational gradient descent (SVGD) [15] to expand the task distribution throughout the entire task space.

We provide thorough discussions on the differences between VACL and existing works (Sec. 3.4) and empirically validate VACL using a single desktop machine in 4 physical multi-agent cooperative games, i.e., 2 in the multi-agent particle-world environment (MPE) [17] and 2 in the MuJoCo-based hide-and-seek environment (HnS) [2] (Sec. 4). In the MPE games, VACL learns significantly faster and better than all baselines and achieves over **98% coverage rate** with **100 agents** in the *simple-spread* testbed even using **sparse rewards**. In the HnS scenarios, VACL achieves over 90% success rates on both two games, including reproducing the *ramp use* behavior discovered in [2], and a sparse-reward multi-agent *Lock-and-Return* challenge where none of the baselines can produce a success rate above 15% using the same amount of training timesteps.

2 A Variational Perspective on Curriculum Learning

2.1 Preliminary

We formulate each goal-conditioned cooperative multi-agent task as a multi-agent Markov decision process (MDP), $M(n, \phi) = <n, \phi, \mathcal{S}, \mathcal{A}, \mathcal{O}, O, P, R, s_\phi^0, g_\phi, \gamma>$, parameterized by a discrete variable n (e.g., number of agents[1]) and a continuous parameter $\phi \in \Phi$. $\mathcal{S}$ is the state space, $\mathcal{A}$ is the shared action space for each agent and $\mathcal{O}$ is the observation space. $o_i = O(s; i)$ denotes the observation for agent i under state S. s_ϕ^0 denotes the initial state and g_ϕ denotes the goal. $P(s'|s, A)$ and $R(s, A; g_\phi)$ are the transition probability and the goal-conditioned reward function given state s and joint actions $A = (a_1, \ldots, a_n)$. γ is the discounted factor.

We consider homogeneous agents and learn a shared goal-conditioned policy $\pi_\theta(a_i|o_i, g)$ parameterized by θ for each agent i. The final objective is to maximize the expected accumulative reward over the entire task space, i.e.,

$$J(\theta) = \mathbb{E}_{n,\phi,a_i^t,s^t}\left[\sum_t \gamma^t R(s^t, A^t; g_\phi)\right] = \mathbb{E}_{n,\phi}[V(n, \phi, \pi_\theta)], \tag{1}$$

where $V(n, \phi, \pi_\theta)$ denotes the value function for π_θ over task $M(n, \phi)$. We remark that for problems with 0/1 sparse rewards, $V(n, \phi, \pi_\theta)$ can be also interpreted as the success rate of π_θ.

The main idea of curriculum learning is to construct a task sampler $q(n, \phi)$ that always generates training tasks $M(n, \phi)$ that yield the largest learning progress for π_θ to efficiently maximize $J(\theta)$.

2.2 Stein Variational Inference over a Continuous Task Space

For simplicity, we ignore the discrete variable n and only focus on the continuous variable ϕ in this subsection. Herein, our objective is to maximize the expectation $\mathcal{L} = \mathbb{E}_{\phi \sim p(\phi)}[V(\phi, \pi)]$, where $p(\phi)$ is a uniform distribution over feasible values of ϕ. The subscript θ of π is omitted for conciseness.

Given the objective $\mathcal{L}$, we motivate our automated curriculum learning procedure through the lens of variational inference. Let $q(\phi)$ denote the current distribution of training tasks, which will vary throughout learning; we can represent curriculum learning through an objective that optimizes $q(\phi)$. The following lower bound for the original objective $\mathcal{L}$ can be derived:

$$\mathcal{L} = \mathbb{E}_{\phi \sim p}[V(\phi, \pi)] = \mathbb{E}_{\phi \sim q}\left[\frac{p(\phi)}{q(\phi)}V(\phi, \pi)\right] = \mathbb{E}_{\phi \sim q}\left[V(\phi, \pi) + \left(\frac{p(\phi)}{q(\phi)} - 1\right)V(\phi, \pi)\right] \tag{2}$$

$$\geq \underbrace{\mathbb{E}_{\phi \sim q(\phi)}[V(\phi, \pi)]}_{\mathcal{L}_1: \text{policy update}} + \underbrace{\mathbb{E}_{\phi \sim q(\phi)}\left[V(\phi, \pi)\log\frac{p(\phi)}{q(\phi)}\right]}_{\mathcal{L}_2: \text{curriculum update}} \tag{3}$$

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[1]n can also be a discrete vector where each dimension represents the number of a particular type of objects. We now simply assume n is a single integer denoting the agent number for conciseness.

75 where the inequality is due to $x - 1 \geq \log x$, with equality achieved at $p(\phi) = q(\phi)$ for all ϕ.

76 Now, we have decomposed $\mathcal{L}(\pi, q)$ into a lower bound that contains two terms $\mathcal{L}_1$ and $\mathcal{L}_2$. $\mathcal{L}_1$ is
77 simply a policy update objective under the current task curriculum $q(\phi)$ while the second term $\mathcal{L}_2$ can
78 be interpreted as a curriculum update objective by maximizing $q(\phi)$ w.r.t. the policy π. Therefore,
79 the decomposed lower bound naturally yields a curriculum learning framework by performing an
80 iterative learning procedure, i.e., alternating between (1) maximizing $\mathcal{L}_1$ with π (policy update) and
81 (2) maximizing $\mathcal{L}_2$ with $q(\phi)$ (curriculum update). We remark that we only optimize π w.r.t. $\mathcal{L}_1$
82 instead of $\mathcal{L}_1 + \mathcal{L}_2$ for the purpose of stabilizing policy learning since q can be very different from p
83 in the early stage of training. This also aligns with the curriculum learning paradigm. In the following
84 proposition, we show that if we can perfectly optimize the RL procedure for $\mathcal{L}_1$ under the curriculum
85 $q(\phi)$, then the curriculum objective $\mathcal{L}_2$ will encourage $q(\phi)$ to converge to $p(\phi)$.

86 **Proposition 1.** *Assume that $V(\phi, \pi) \in [0, 1]$ and that there exists a unique policy $\pi^\star$ such that*
87 *$V(\phi, \pi^\star) = 1$ for all ϕ. For any $q \in \mathcal{P}(\Phi) \setminus \{p\}$ (i.e., any curriculum that is not the final*
88 *one) and $\pi \in \arg\max_\pi \mathcal{L}_1(\pi, q)$ (i.e., a policy that is optimal under the current curriculum),*
89 *$\mathcal{L}_2(\pi, q) < \mathcal{L}_2(\pi^\star, p) = 0$.*

90 *Proof.* First, we have that $\mathcal{L}_1(\pi^\star, p) = 1$ (definition of $\pi^\star$) and $\mathcal{L}_2(\pi^\star, p) = 0$. Suppose that $\exists \pi, q$
91 such that $q \neq p$ and $\mathcal{L}_1(\pi, q) = 1$; then it must be the case that whenever $V(\phi, \pi) \neq 1$, $q(\phi) = 0$, *i.e.*,
92 $\forall \phi \in \text{supp}(q)$, $V(\phi, \pi) = 1$. Then $\mathcal{L}_2(\phi, \pi) = -D_{\text{KL}}(q \| p) < 0$, which completes the proof. $\square$

93 In other words, if our policy π already performs well under the current curriculum $q(\phi)$, then $\mathcal{L}_2$ will
94 encourage $q(\phi)$ to become "closer" to $p(\phi)$, aligning with our eventual target of learning all tasks.

2.2.1   Stein Variational Gradient Descent for Curriculum Update

96 The most straightforward approach for optimizing $\mathcal{L}_2$ is to learn a generative model w.r.t. the
97 current π, which can be particularly sample-inefficient. Instead, we consider updates to our current
98 curriculum via smooth updates, which is much more efficient than learning generative models.

99 Let us represent the task distribution under the current curriculum $q(\phi)$ with a set of particles Q.
100 To update the particles, we consider an incremental transform $T(\phi) = \phi + \epsilon f(\phi)$, where $f(\phi)$ is a
101 smooth function and ϵ is a magnitude scalar. Our goal is then to derive suitable updates to q that
102 maximizes $\mathcal{L}_2(q, \pi)$ based on the transform T. Following [9] and [25], we introduce an assumption
103 over the generalization ability of the task space.

104 **Assumption 1.** *An optimal policy π that is trained over a specific task ϕ has some generalization*
105 *ability to another goal ϕ' close to ϕ. Specifically, if $V(\phi, \pi) = c$ for any $\phi \in \text{supp}(q)$, then*
106 *$V(\phi', \pi) = c$ for all $\phi' \in \mathcal{B}(\phi)$, where $\mathcal{B}(\phi)$ is a small open ball around ϕ.*

107 In the context of curriculum learning, this assumption suggests that for any policy that is trained
108 on a set of tasks, the performance (e.g., success rate) does not change if we only change the task
109 parameters by an infinitesimal amount. In the following theorem, we derive the functional gradient of
110 the curriculum update objective $\mathcal{L}_2$ in a reproducing kernel Hilbert space (RKHS).

111 **Theorem 1.** *Let $T(\phi) = \phi + \epsilon f(\phi)$ where f is an element of some vector-valued RKHS of a positive*
112 *definite kernel $k(\phi, \phi') : \Phi \times \Phi \to \mathbb{R}$, and $q_{[T]}$ the density of $\psi = T(\phi)$ when $\phi \sim q$, then*

$$\nabla_f \mathcal{L}_2(q_{[T]}, \pi)|_{f=0} = f^*(\phi), \tag{4}$$

113 *where $f^*(\cdot) = \mathbb{E}_{\phi' \in \mathcal{Q}}[V(\phi', \pi)(k(\phi', \cdot)\nabla_{\phi'} \log p(\phi') + \nabla_{\phi'} k(\phi', \cdot))]$.*

114 Proof is in App. A. While the above statement is very similar to that used for Stein variational gradient
115 descent [15], the update for our case also directly depends on the values $V(\phi', \pi)$, and thus indirectly
116 depends on the current policy. Intuitively, if $V(\phi', \pi)$ is large, then ϕ' will contribute more to the
117 curriculum update, whereas if $V(\phi', \pi) = 0$, then ϕ' will not contribute to the update.

118 Since we assume that $p(\phi)$ is uniform over the task space, $\nabla_{\phi'} \log p(\phi') = 0$ for the interior of Φ,
119 and the task update becomes

$$f^*(\cdot) = \mathbb{E}_{\phi' \in \mathcal{Q}}[V(\phi', \pi) \cdot \nabla_{\phi'} k(\phi', \cdot)]. \tag{5}$$

120 For example, we take the RBF kernel $k(\phi, \phi') = \exp(-\frac{1}{h}\|\phi - \phi'\|_2^2)$, and then Eq. (5) will drive ϕ
121 away from neighbouring points that have large $k(\phi, \phi')$, and the repelling force scales with $V(\phi', \pi)$.

122 If $V(\phi', \pi) = 0$, *i.e.*, ϕ' has not been solved at all, then there is no repelling force from ϕ' to ϕ.
123 Intuitively, this process encourages the curriculum update to prioritize tasks that have not been fully
124 solved yet, by exploring in the vicinity of existing tasks with high values.

2.3 Continuous Relaxation for Discrete Parameter

126 Now we switch to the discrete parameter n in our task representation, which results in a non-
127 continuous task space and can be difficult to directly combine with continuous optimization tech-
128 niques. Therefore, we propose to utilize a continuous variable alternative z to represent the discrete
129 variable n so that the same variational inference technique for ϕ can be applied here. Specifi-
130 cally, assuming n denotes the number of agents, we represent n with a categorical distribution
131 $p(n; z) = \text{Cat}(z_1, z_2, \ldots, z_N)$ parametrized by a continuous vector $z = [z_1, \ldots, z_N]$ assuming the
132 maximum possible of agents[2] is N. $p(n; z)$ denotes the distribution which generates n agents with
133 probability z_n. In this case, we can similarly introduce a target distribution $p(z)$ over the space of z
134 and derive the corresponding variational updates with $V(z, \pi)$. Since we typically wish to learn a
135 policy that can generalizes across different number of agents, so such a representation over multiple
136 n's naturally satisfies this practical requirement. We also remark that this formulation can be directly
137 extended to the problems with multiple discrete variables (e.g., number of both agents and objects)
138 via a categorical distribution over all possible discrete combinations.

3 Variational Automatic Curriculum Learning

140 In this section, we implement the variational inference paradigm with computation-efficient approxi-
141 mations as our VACL algorithm in the context of sparse-reward cooperative MARL problems.

3.1 Task Expansion as Approximated Stein Variational Inference

143 We present *Task Expansion*, a computation-efficient curriculum update method, which assumes a
144 continuous task representation ϕ and optimizes the variational lower bound $\mathcal{L}_2$ w.r.t. $q(\phi)$.

3.1.1 An Ever-Expanding Particle Set

146 In the standard Stein variational inference framework, we typically maintain a fixed-size particle set
147 $\mathcal{Q}$ and gradually update the distribution of these particles using Stein variational gradient descent.
148 Since the policy is constantly changing throughout training, we need to repeatedly update the entire
149 set of particles to match the corresponding proposal distribution under $\mathcal{L}_2$, which is computationally
150 expensive. Note that in the cooperative MARL setting, assuming a fixed amount of agents and an
151 ever-improving policy, if we initialize $q(\phi)$ to the proper sub-space of easiest tasks, $q(\phi)$ would
152 monotonically expand towards the entire task space. Hence, we can simply maintain an ever-
153 expanding particle set by repeatedly adding novel tasks with sufficiently high values (i.e., success
154 rates) under the current policy without the need of modifying those existing particles in $\mathcal{Q}$.

3.1.2 Value Quantization

156 Another issue for optimizing $\mathcal{L}_2$ is that whenever π updates,
157 $V(\phi, \pi)$ changes accordingly but evaluating the value function
158 can be particularly expensive in MARL problems. As a practi-
159 cal approximation, we roughly categorize all the tasks into 3 cate-
160 gories w.r.t. their values, i.e., a solved subspace of highest values,
161 $\mathcal{Q}_{\text{sol}} = \{\phi | V(\phi, \pi) > \sigma_{\max}\}$, an active subspace of moderate values,
162 $\mathcal{Q}_{\text{act}} = \{\phi | \sigma_{\min} \le V(\phi, \pi) \le \sigma_{\max}\}$, and the remaining unsolved
163 subspace. Here $\sigma_{\min}$ and $\sigma_{\max}$ are quantization thresholds. Since
164 the value function would monotonically increase as training pro-

Figure 1: Task space partition.

165 ceeds, we only need to verify whether an active task becomes solved or whether an unsolved task
166 becomes active, and maintain $\mathcal{Q}_{\text{act}}$ and $\mathcal{Q}_{\text{sol}}$ accordingly. Once a task becomes solved, future value

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[2]If N is unbounded, we may consider parametrized discrete random processes such as the Chinese restaurant
process. For all practical purposes here, this is unnecessary.

167 estimation becomes no longer necessary. In addition, w.r.t. the curriculum learning principle, when
168 optimizing π under $\mathcal{L}_1$, we can also sample more training tasks from $\mathcal{Q}_{\text{act}}$ for more effective training.

3.1.3 Sampling-Based Particle Exploration

170 With an ever-expanding particle set $\mathcal{Q}$, we need to explore novel task
171 samples in the task space and add those tasks with sufficiently high
172 values (i.e., $V \geq \sigma_{\min}$) to $\mathcal{Q}$. The update equation for $q(\phi)$ in Eq.(5)
173 naturally suggests a diversity-based task expansion scheme, namely
174 exploring sufficiently novel tasks in the vicinity of $\mathcal{G}$. Due to the
175 difficulty in value estimation, we again follow the value quantization
176 framework and simplify Eq.(5) as follows:

$$\tilde{f}^*(\cdot) \propto \mathbb{E}_{\phi' \in \mathcal{Q}_{\text{sol}}}[\nabla_{\phi'} k(\phi', \cdot)]. \qquad (6)$$

177 In the simplified Eq.(6), we simply ignore tasks with moderate values
178 (i.e., active tasks in $\mathcal{Q}_{\text{act}}$) and only evaluate the expectation w.r.t.
179 tasks with the highest values (i.e., solved tasks in $\mathcal{Q}_{\text{sol}}$) as a practical
180 approximation. Moreover, since $\mathcal{Q}_{\text{sol}}$ is ever-expanding, Eq.(6) also
181 suggests that we should explore novel tasks in the boundary region

Figure 2: We explore novel tasks in the boundary region between $\mathcal{Q}_{\text{sol}}$ and $\mathcal{Q}_{\text{act}}$

182 between $\mathcal{Q}_{\text{sol}}$ and $\mathcal{Q}_{\text{act}}$ (Fig. 2). Hence, in practice, whenever an active task from $\mathcal{Q}_{\text{act}}$ becomes solved
183 after policy update, we select them as seed tasks to derive novel exploration task samples.

184 Eq.(6) suggests purely gradient-based exploration, which may cause practical issues in curriculum
185 learning since the feasible task parameterization space is often highly constrained. Fig. 6 illustrates a
186 maze scenario where agents need to navigate towards the landmarks and avoid the black obstacles. A
187 valid task parameterization ϕ includes the positions of agents and landmarks. The feasible subspace
188 of ϕ is constrained by the obstacles while these feasibility constraints are only accessible as a black
189 box in the curriculum learning setting. Therefore, directly computing a constraint-free gradient
190 can easily lead to an exploration direction towards infeasible regions. Here we suggest a sampling-
191 based enhancement, which promotes task-space exploration and can be viewed as a zero-th order
192 approximation of the projected gradient.

193 **Rejection-Sampling Exploration:** We explore novel tasks ϕ_{exp} by adding small uniform noise to
194 the gradient of seed tasks, namely $\phi_{\text{exp}} \leftarrow \phi_{\text{seed}} + \epsilon \tilde{f}^*(\phi_{\text{seed}}) + \text{Unif}(-\delta, \delta)$. Then we reject those
195 infeasible tasks by querying the environment for configuration feasibility.

3.2 Entity Progression for Massive Multi-Agent Learning

197 Directly applying the Stein variational update (Eq.(5)) over the relaxation z of the discrete variable n
198 results in a uniform expansion over the entire N-dimensional space of z, which can be computational
199 challenging when N is particularly large. We leverage an important inductive bias in cooperative
200 MARL that problems with more agents are generally harder than fewer agents, which implies a
201 monotonic update scheme over the z space by starting with $z_{n_0} = 1$, where n_0 is the smallest possible
202 number of agents, and gradually increasing the probability mass of z_k for larger k.

203 *Entity Progression* simplifies this procedure further by restricting z to only have two non-zero entries,
204 i.e., $z_k + z_{k'} = 1$ with $k' > k$, which suggests a smooth and progressive transition from a simpler
205 problem with k agents (i.e., $z_k = 1$) to a harder problem with k' agents (i.e., $z_{k'} = 1$). Note that we
206 can increase the agent number incrementally (i.e., $k' = k + 1$) or at an exponential rate (i.e., $k' = 2k$),
207 the latter of which is typically more preferred in practice. We remark that entity progression can
208 directly apply to problems with multiple discrete parameters by viewing k as a discrete vector.

3.3 VACL: A Hierarchical Automatic Curriculum Learning Algorithm

210 Since the change of discrete variable n may cause a drastic distribution shift of value functions,
211 instead of using a joint continuous representation unifying both n and ϕ, VACL combines *Entity*
212 *Progression* and *Task Expansion* in a hierarchical manner: at the low level, task expansion maintains
213 a separate curriculum $q^n(\phi)$ for each n and performs particle-based curriculum update under a fixed
214 n; at the high level, entity progression progressively increases n to n' by smoothly switching training
215 distribution from $q^n(\phi)$ to $q^{n'}(\phi)$. The full procedure is summarized in Algo. 1.

Algorithm 1: The VACL Algorithm

Input: $\theta, n_0, N, B, B_{\text{exp}}$; // B : training batch size; B_{exp} : exploration size
Output: final policy π_θ;
$k \leftarrow 0, \mathcal{Q}_{\text{sol}}^0 \leftarrow \{\}, \mathcal{Q}_{\text{act}}^0 \leftarrow$ **GetEasy**(n_0); // use easy tasks to initialize $q(\phi)$
repeat

    $z \leftarrow 1, n_{k+1} \leftarrow$ **Inc**$(n_k), \mathcal{Q}_{\text{sol}}^{k+1} \leftarrow \{\}, \mathcal{Q}_{\text{act}}^{k+1} \leftarrow$ **GetEasy**(n_{k+1});
    while *not converge with n_k* **do**

        // Policy Update
        $\mathcal{M}_{\text{train}} \leftarrow$ **Sample**$(B \times z, \mathcal{Q}^k) +$ **Sample**$(B \times (1 - z), \mathcal{Q}^{k+1})$;
        Train and evaluate π_θ on $\mathcal{M}_{\text{train}}$ via MARL;
        // Task Expansion
        expand $\mathcal{Q}_{\text{sol}}^{\{k,k+1\}}$ and $\mathcal{Q}_{\text{act}}^{\{k,k+1\}}$ using the value estimates on $\mathcal{M}_{\text{train}}$;
        // generate novel exploration tasks
        $\mathcal{M}_{\text{seed}} \leftarrow$ active tasks from $\mathcal{M}_{\text{train}}$ that just become solved under π_θ ;
        $\mathcal{M}_{\text{exp}} \leftarrow$ generate B_{exp} exploration task samples from seeding tasks in $\mathcal{M}_{\text{seed}}$;
        Add exploration tasks $\mathcal{M}_{\text{exp}}$ to $\mathcal{Q}_{\text{act}}^{\{k,k+1\}}$;
        // Entity Progression
        Decay z;

    $k \leftarrow k + 1$;
until $n_k = N$;

3.4 Connection to Existing Works

We focus on goal-conditioned multi-agent cooperative problems and assume a paramterized task space. This is a common setting in the recent Automatic Curriculum Learning (ACL) literature [4, 23]. Some works also consider a fixed set of tasks [18], which are typically referred to as multi-task learning [31]. The core idea of ACL is to train the policy using tasks with moderate difficulty, i.e., neither too hard nor too easy, which naturally emerges as a consequence of our variational paradigm.

A popular class of ACL methods learn a generative model over the task space with density concentrated on tasks with desired difficulties, such as VAE [24], GAN [9, 7] and Gaussian mixture models [22, 12, 20]. These methods can be viewed as a generic solution under our variational objective (Eq. 3) by representing $q(\phi)$ as a generative model and directly optimizing $\mathcal{L}_2$ whenever the policy is updated. However, it can be extremely sample-inefficient to repeatedly learn $q(\phi)$ from scratch without leveraging the fact that $q(\phi)$ is ever-expanding in cooperative MARL problems.

Another type of ACL methods is particle-based, which maintains a set of solvable task samples and gradually expands the set towards the entire space. [10, 11] assume a fixed goal and generate tasks with starting states increasingly far away from the goal; [1, 19] consider a task space over simulator configurations and train from the easiest settings to the hardest for sim-to-real adaptation. These methods are conceptually similar to the *Task Expansion* component in VACL for its particle-based nature and can be viewed as a random search procedure for optimizing $\mathcal{L}_2$ in a gradient-free manner. our method provides a principled interpretation to curriculum updates, and achieves superior performance in practice. Besides, [28] learn an individual policy paired with each task for discovering diverse behaviors while our work learns a single goal-conditioned policy for the entire task space; [30] propose to meta-learn $f^*(\phi)$ to more effectively expand the curriculum distribution, which is complementary to our work.

[16, 29] propose *population curriculum*, which trains entity-invariant policies over training tasks with a growing number of agents. [8] adopt a similar curriculum learning method for Sokoban with an increasing number of boxes. These methods can be viewed as a special case as our *Entity Progression* component by applying a hard transfer from $z_k = 1$ to $z_{k'} = 1$ while our method smoothly switches between different number of entities and also yields better empirically performances.

4 Experiment

We consider four tasks over two environments, *Simple-Spread* and *Push-Ball* in the multi-agent particle-world environment (MPE) [17], and *Ramp-Use* and *Lock-and-Return* in the hide-and-seek

Figure 3: MPE tasks.

Figure 4: Comparison of VACL and baselines on MPE.

environment (HnS) [2]. Every experiment is repeated over 3 seeds and performed on a desktop machine with one 64-core CPU, and one 2080-Ti GPU, which is used for forward action computation and training updates. More details are in Appendix.

4.1 The Multi-Agent Particle-World Environment

The two tasks are illustrated in Fig. 3. In *Simple-Spread*, there are n agents and n landmarks and the agents need to occupy all the landmarks. The agents are penalized for collisions and only receive a positive reward when all the landmarks are covered. In *Push-Ball*, there are n agents, n balls and n landmarks. The agents need to physically push the balls to get every landmark covered. A success reward is given after all landmarks are covered. We scale n at an exponential rate following [16].

4.1.1 Main Result

We compare *VACL* with 5 baselines, including (1) multi-agent PPO with uniform task sampling (*Uniform*), (2) population curriculum only (*PC-Unif*), (3) reverse curriculum generation (*RCG*) [10], (4) automatic goal generation (*GoalGAN*) [9], which uses a GAN to generate training tasks, (5) adversarially motivated intrinsic goals (*AMIGo*) [6], which learns a teacher to generate increasingly challenging goals. We test all methods in *Simple-Spread* with $n = 8$ and *Push-Ball* with $n = 4$. For *PC-Unif* and *VACL*, we start with $n_0 = 4$ in *Simple-Spread* and $n_0 = 2$ in *Push-Ball* and then switch to the desired agent

Table 1: The best coverage rate ever reported on *Simple-Spread*.

n	EPC	ATOC	VACL
24	56.8%	/	**97.6%**
50	/	92%	**98.5%**
100	/	89%	**98%**

number. Evaluation is always performed on the final N. Results are shown in Fig. 4, where VACL outperforms all baselines with a clear margin. In *Simple-Spread*, all baselines fail to solve the task: Uniform and PC-Unif fail to gain sufficient progress due to sparse rewards; RCG quickly runs out of active tasks; GoalGAN and AMIGo takes an extremely long time to train a good neural goal-generator. In *Push-Ball*, Uniform and PC-Unif learn much slower, RCG quickly converges to a local minimum without further policy improvements, GoalGAN and AMIGo[3] again consumes a large number of samples to make training progress.

In addition to the baselines above, we also consider the setting of **massive agents** on *Simple-Spread* and compare our VACL method with other coverage numbers in the existing literature. We consider two existing works. The *attentional communication* (ATOC) method [13], which adopts intra-agent communication channels and trains $n = 50$ and $n = 100$ agents with *dense* rewards. ATOC is not open-sourced[4]. We re-train VACL on the same environment configuration (i.e., same agent/landmark size and room size) as ATOC for a fair comparison with the number reported in [13]. The other work is evolutionary population curriculum (EPC) [16], which reports the coverage rate on the standard *Simple-Spread* task with $n = 24$ agents. EPC adopts dense rewards and separate policies for each agent while VACL trains a shared policy with *sparse 0/1 rewards*. The results are reported in Tab. 1. VACL achieves a 98% coverage rate with $n = 100$ agents, which outperforms the highest number ever reported to the best of our knowledge.

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[3]We do not finish the training of AMIGo in *Push-Ball* before the deadline, but the current results show that AMIGo is converging much slower than our VACL method.

[4]We contacted the authors but did not get a response.

(a) Choice of seed tasks   (b) Exploration strategies   (c) Effectiveness of entity progression

Figure 5: Ablation studies. (a) We evaluate difference choices of seed tasks in *Simple-Spread*; (b) We compare our SVGD-principled exploration strategy with random exploration from seed tasks in the *Hard-Spread* scenario (Fig. 6), which has a highly constrained task space; (c) We compare entity progression with direct transfer in standard *Simple-Spread* and *Push-Ball*.

4.1.2 Ablation Study

Choice of seed task: As implied by Eq. (5) and Eq. (6), VACL explores from the boundary between $\mathcal{Q}_{\text{act}}$ and $\mathcal{Q}_{\text{sol}}$ by taking newly solved tasks as seeds to generate exploration tasks. A naive alternative is to simply take active tasks from $\mathcal{Q}_{\text{act}}$ as seeds (*Exp.Act.*), which is similar to the exploration scheme in the RCG algorithm [10]. Note that exploration from active tasks may possibly produce unsolvable tasks, we consider an additional enhanced variant (*Exp.Act w. eval*), which take active tasks as seeds but also perform value estimates (and training) on those exploration tasks to filter out unsolvable tasks before adding them to $\mathcal{Q}_{\text{act}}$. Results of these variants are shown in Fig. 5(a). Using active tasks as seeds (*Exp.Act.*) leads to a clear failure since the aggressive exploration brings too many unsolvable tasks to $\mathcal{Q}_{\text{act}}$. Although additional evaluation on exploration tasks (*Exp.Act.w.eval*) significantly stabilizes training, it still yields much worse training progress than the standard VACL. This suggests that it is critical to explore from the vicinity of solved subspace.

SVGD-Principled Update: Our Stein Variational paradigm suggests a gradient-based update rule to explore novel tasks in Sec. 3.1.3. However, most existing particle-based algorithms adopts a much simplified gradient-free alternative via uniform random noise, i.e., $\phi_{\text{exp}} \leftarrow \phi_{\text{seed}} + \text{Unif}(-\delta, \delta)$. To illustrate the effectiveness of our SVGD-principled update rule, we consider a challenging *Hard-Spread* scenario in Fig. 6 with 4 agents and 4 landmarks. Obstacles are in black and landmarks can only be placed in the right side. We initialize $\mathcal{Q}_{\text{act}}$ with easy tasks where each landmark has an agent nearby and evaluate the performance of the learning policy on those hardest tasks in Fig. 6. We remark that due to the highly constrained task space, it becomes particularly challenging for the ACL method to gradually guide the agents to learn to go through the narrow doors between obstacles. We evaluate the test performances of VACL and the simplified gradient-free version (*Unif. noise*) in Fig. 5(b). Our principled rule produces a stable learning curve with fast convergence while the gradient-free version fails to solve the task.

Figure 6: The *Hard-Spread* scenario.

Entity Progression: We compare *entity progression* with naive population curriculum, i.e., directly transfer the trained policy on n_{k-1} to the next entity size n_k (*transfer*). We train with the two methods on *Simple-Spread* from $n_0 = 4$ to $N = 8$ and on *Push-Ball* from $n_0 = 2$ to $N = 4$. The results are shown in Fig. 5(c). In both two tasks, direct transfer yields a significant performance drop, which we believe due to the drastic training distribution shift. For *entity progression*, due to its smooth transition between the continuous relaxation of $z_k = 1$ and $z_k' = 1$, it produces a much stable training curves. *Entity progression* also yields the much better final performances particularly on the more challenging *Push-Ball* scenario.

Table 2: Results of VACL and baselines in HnS tasks.

		Uniform	RCG	GoalGAN	AMIGo	VACL
Ramp-Use	$n = 1$	$42.8\% \pm 35.4\%$	$31.5\% \pm 33.7\%$	$1.0\% \pm 0.8\%$	$47.2\% \pm 10.3\%$	$93.3\% \pm 5.4\%$
Lock-and-Return	$n = (2, 2)$	$<1\%$	$5.0\% \pm 5.1\%$	$<1\%$	$< 2\%$	$97.3\% \pm 0.1\%$
	$n = (4, 4)$	/	/	/	/	$97.0\% \pm 1.6\%$

4.2 The Hide-and-Seek Environment

We consider two tasks in the hide-and-seek environment (HnS) as shown in Fig. 7, i.e., a simplified hide-and-seek game called *Ramp-Use* and a multi-agent and sparse-reward variant of the *Lock-and-Return* task from the transfer task suite in [2]. *Ramp-Use* is a single-agent scenario for the ramp use strategy, with 1 ramps, 1 movable seeker and 1 fixed hider in the quadrant room. We need to train a seeker policy to use the ramp to get into the quadrant room for positive rewards. In *Lock-and-Return*, the discrete parameter n becomes a 2-dimensional vector and each dimension represents the number of agents and boxes respective. Agents need to lock all the boxes and return to their birthplaces. Agents get a reward of 1 when *all* boxes are locked and another success reward when the task is finished, i.e., all boxes locked and all agents back to the birthplaces.

Figure 7: Tasks in the hide-and-seek environment (HnS).

The results of different methods are shown in Tab. 2. We train each algorithm on *Ramp-Use* for 80M timesteps and on *Lock-and-Return* with $n = (2, 2)$ for 180M timesteps. For *Lock-and-Return* with $n = (4, 4)$, we train VACL for a total number of 230M timesteps. We report the average success rate over 3 seeds. VACL is the only algorithm able to solve both two tasks.

In *Lock-and-Return*, we start with the easy setting of $n_0 = (2, 2)$ and proceed towards $N = (4, 4)$. Note that n is a 2-dimensional discrete vector in this task, there are multiple paths to transition from the continuous relaxation $z_{(2,2)} = 1$ to $z_{(4,4)} = 1$. One is to double the number of agents first and keep the box number unchanged, and then double the number of boxes, i.e., $z_{n_0} = 1 \rightarrow z_{(4,2)} = 1 \rightarrow z_N = 1$ (*agent-first*). The other is to first double the number of boxes and then increase the agent number, i.e., $z_{n_0} = 1 \rightarrow z_{(2,4)} = 1 \rightarrow z_N = 1$ (*box-first*). Although both two paths are feasible transitions, they lead to different practical performances. The results are shown in Fig. 8, where we clearly observe that the strategy of increasing agent number first substantially outperforms the box-first strategy. Therefore, we generally suggest to increase the number of agents before objects in entity progression. We remark that since no baseline achieves a success rate above 15% even in the easy case of $n = (2, 2)$, we do not evaluate them in the hard setting.

Figure 8: Results of different entity switching strategies.

5 Conclusion

In this paper, we propose a novel curriculum learning paradigm following the principle of Stein variational inference and developed a effective algorithm, Varitional Automatic Curriculum Learning (VACL), which solves a collection of sparse-reward multi-agent cooperative problems. In this work, we consider cooperative tasks for the clear measurement of training progress. We also remark that VACL assumes a monotonic expansion of $q(\phi)$, which only holds in the fully cooperative setting. There are also existing works also study ACL for competitive games [26, 14, 2], which we leave as future work. Our framework tackles an important research problem in the literature while experiments are conducted on open-source environments with student licences, so we believe our work does not produce any negative impact to the society.

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