Goal-Directed Planning via Hindsight Experience Replay

Abstract

We consider the problem of goal-directed planning under a deterministic transition model. Monte Carlo Tree Search has shown remarkable performance in solving deterministic control problems. It has been extended to complex continuous domains through function approximators to bias the search of the planning tree in AlphaZero. Nonetheless, these algorithms still struggle with control problems when sparse rewards are adopted such as goal-directed domains, where a positive reward is awarded only when reaching a goal state. In this work, we extend AlphaZero with Hindsight Experience Replay to tackle complex goal-directed planning tasks. We demonstrate the effectiveness of the proposed approach through an extensive empirical evaluation in several simulated domains, including a novel application to a quantum compiling domain.

1 Introduction

Monte Carlo Tree Search (MCTS) (Browne et al., 2012) algorithms have shown outstanding results in solving sequential decision-making problems, especially in deterministic transition tasks, such as games. MCTS planners use a forward environment model to build a search tree, estimate the value of each action in the current state, and execute the best-estimated one, respectively. Such a procedure allows finding a "local" solution to the decision problem in every decision step by sampling trajectories of possible future policies using the forward model. Although providing local solutions is advantageous in some contexts, it comes at a high computational cost since acting in the environment requires interleaved planning phases and possibly large search trees. These high computational costs have been a barrier in applying MCTS to larger problems, especially those with long planning horizons and huge tree branching factors (number of actions). However, MCTS does not require a training phase and can be deployed immediately.

Reinforcement Learning (RL) (Sutton et al., 1998), on the other hand, aims to find a global solution to the control problem by learning a policy that performs adequately in the whole state space. While this may seem a more desirable outcome, it can often be hard to produce a policy that generalizes satisfactorily across different state regions. For this reason, MCTS algorithms have achieved tremendous success in a wide range of tasks (Borsboom et al.; Enzenberger et al., 2010; Ikehata and Ito, 2011). The AlphaZero (Silver et al., 2016) family of algorithms made it possible to use sequential planners like MCTS in more challenging environments, such as the game of Go, where the AlphaGo agent defeated the world champion, achieving super-human performance. AlphaGo was in turn defeated by the AlphaZero, a version of the algorithm without any heuristic related to the game of Go. AlphaZero combines MCTS with the ability of RL algorithms to generalize across the state-action space by keeping a parametrized policy and value network. Specifically, the policy network biases the exploration during the tree search, and the value network estimates the value of the states corresponding to the search tree leaves, replacing the trajectory-based evaluation usually performed with an ad-hoc evaluation policy called *rollout* policy. On the other hand, the MCTS algorithm acts as a *policy improvement* step. It takes as input the current state, as well as the policy and value networks, therefore improving the parametrized policy and generating the samples used to train the networks in a supervised manner. Although a tree search is still required, the deployment is cheaper since it usually requires a humbler

planning budget, thanks to the policy and value networks which bias the search by making it more efficient. The algorithm has been successfully applied to different games such as Go, Chess, and Shogi (Silver et al., 2017a) without game-specific heuristics. However, despite its success, the algorithm suffers from a high sample complexity, especially prominent in tasks with sparse reward functions, such as goal-directed planning.

In goal-directed tasks, the agent aims to reach a goal state, and in general, the policies take both the current state of the environment and the goal state as input. Usually, the actual reward function in these problems is zero for any transition except the one to the goal state, which gives a positive reward. RL algorithms struggle to optimize sparse reward functions since it might be hard to reach goal states, or even practically impossible during exploration if the task is quite challenging. Therefore, there is not a reward signal to guide the exploration. While in practice, in specific tasks, it is possible to use more informative reward functions, such as a distance from the goal state, such a choice is not possible for every task. Furthermore, it might also lead to sub-optimal solutions since a reward function based on a state distance might generate local-optima in the policy space (Grzes and Kudenko, 2009). Hindsight Experience Replay (HER) (Andrychowicz et al., 2017) is a straightforward method to tackle the problem of sparse-reward functions in goal-directed tasks. HER can be used with any *off-policy* RL algorithm to extend the training dataset for the value networks. Practically, whenever the goal state is not reached during a training episode, the states visited during the episode are used as alternative goal states and are fed to the network during training. It allows reward signals to be given to the value networks and generalize them to reach the input goal state.

In this work, we consider the problem of applying HER to AlphaZero to tackle goal-directed tasks. We provide a scheme that does not involve computationally heavy tree re-weighting procedures or high additional computational costs. Finally, we benchmark the method with simulated environments, and we show a novel application to quantum compiling, where it is extremely hard to find unitary gate sequences from a set to approximate arbitrary single-qubit unitary operators.

2 PRELIMINARIES

2.1 GOAL-DIRECTED REINFORCEMENT LEARNING

In this work, we focus on goal-directed Reinforcement Learning problems. In such setting, an autonomous agent interacts with an environment to maximize the sum of observed reward signals. Formally, in deterministic transition models, the environment consists of a state space $\mathcal{S}$, a set of goal states $\mathcal{G}$ (that can also be equal to $\mathcal{S}$), an action space $\mathcal{A}$, a goal-state dependent reward function $r : \mathcal{S} \times \mathcal{A} \times \mathcal{G} \rightarrow \mathbb{R}$, a transition model $\mathcal{P} : \mathcal{S} \times \mathcal{A} \rightarrow \mathcal{S}$, a probability distribution over $\mathcal{S}$ for the initial state $s_0 \sim \mu$, and a probability distribution over $\mathcal{G}$ for the goal state $s_g \sim \nu$.

The behavior of the agent is described by a Markovian stationary goal-dependent policy, $\pi : \mathcal{S} \times \mathcal{G} \rightarrow \Delta(\mathcal{A})$, which takes as input the current state s and the goal state s_g, and outputs a probability distribution over the actions in $\mathcal{A}$. At the beginning of each episode, an initial state $s_0 \sim \mu$ and a goal state $s_g \sim \nu$ are sampled. Then, at time step t, the agent observes the current state s_t, selects an action $a_t \sim \pi(s_t, s_g)$, observes the next state $s_{t+1} = \mathcal{P}(s_t, a_t)$ and it gets the reward signal $r_t = r(s_t, a_t, s_g)$.

The goal of the agent is to maximize the expected return $\mathbb{E}[R_t]$ defined as the expectation of the discounted sum of future rewards $R_t = \sum_{i=t}^{\infty} \gamma^{t-1} r_t$ taken over the initial state and goal state. Given a policy π, the value of each state is encoded by the value function $V^\pi(s, s_g) = \mathbb{E}_{a_t \sim \pi}[R_0 | s_0 = s]$. Similarly, the action-value function is defined for each state-action pair, conditioning on the first action of the trajectories, $Q^\pi(s, a, s_g) = \mathbb{E}_{a_t \sim \pi}[R_0 | s_0 = s, a_0 = a]$. The goal of maximizing the return can be expressed as finding an *optimal policy*, $\pi^* = \arg\max_\pi V^\pi(s, s_g), \quad \forall (s, s_g) \in \mathcal{S} \times \mathcal{G}$.

2.2 Monte Carlo Tree Search

We briefly introduce the Monte Carlo Tree Search (MCTS) family of algorithms, which combine tree-search algorithms with Monte Carlo sampling to build a search tree iteratively. We focus on the most popular algorithm in the MCTS family, i.e., the upper confidence bound for trees (UCT) (Kocsis and Szepesvári, 2006). More precisely the general MCTS algorithm consists of four stages (Browne et al., 2012):

Selection. In the selection stage, the selection policy is applied from the root of the search tree recursively until an unexpanded leaf node is reached.

Expansion. In the expansion stage, one or more successors to the previously-found unexpanded node are generated according to the actions available in the node.

Evaluation. The newly generated nodes are evaluated, generally through a simulation (*rollout*) using a default policy.

Backpropagation. In the last stage, the rewards collected during the selection and evaluation phase are backed up following the previously visited tree branch.

UCT performs the selection phase using the Upper Confidence Bound (UCB1) (Auer et al., 2002) bandit algorithm. Specifically, each node of the search tree maintains statistics related to the future value of each action, including the number of visits, the number of times an action is performed, and the total sum of the returns observed, used to estimate the mean return. Using such statistics UCB1 chooses the next action to perform, a_n, according to

$$a_n = \arg\max_{i=1..K} B(a_i) = \overline{R}_{i,T_i(n-1)} + C\sqrt{\frac{2\log n}{T_i(n-1)}}, \tag{1}$$

where K is the number of actions, C is a constant that regulates the exploration-exploitation trade-off, $T_i(n-1)$ is the number of times action i has been played up to time $n-1$ and $\overline{R}_{i,T_i(n-1)}$ is the average payoff observed from arm i. UCT recursively updates the values of the nodes from the leaf to the root of the tree, during the backup phase. The algorithm is proved to be *consistent*, i.e., it converges to the optimal policy in the limit, and *asymmetric*, which means that it iteratively builds the search tree by favoring the most promising regions of the tree while still giving a probability of selection to all branches. Such propriety is paramount in some applications where the search tree is extremely large.

2.3 AlphaZero

AlphaZero (Silver et al., 2017a) bridges the gap between RL and MCTS by maintaining a parametric policy, π_θ and value function v_ρ. The policy and value networks are provided as input to the MCTS algorithm to bias the tree search. In contrast, the visit counts in the tree's root are used to build the targets for the supervised training of the policy network.

Compared to general MCTS, the selection and evaluation phases are modified. The former phase uses the policy π_θ, to bias the exploration according to the policy recommendations. Furthermore, AlphaZero replaces the classic UCT algorithm with PUCT (Rosin, 2011) and performs the selection according to:

$$a_n = \arg\max_{i=1..K} B(a_i) = \overline{R}_{i,T_i(n-1)} + C\pi_\theta(s,a_i)\sqrt{\frac{n}{1+T_i(n-1)}}. \tag{2}$$

By multiplying the PUCT confidence interval with the probability given to a_i by π_θ, AlphaZero initially prefers actions with high probability and a low visit count but asymptotically prefers actions with high values. In the latter phase, AlphaZero evaluates the leaf nodes using the estimate provided by the value network v_ρ, instead of performing expensive simulations with a default rollout policy. The training targets of the value network are the actual returns collected during acting. More formally, at each time step t, AlphaZero performs M search iterations of MCTS, starting from the current environment state s_t and using π_θ during the selection phase, and v_ρ during the evaluation of the leaves. After the search phase, the policy targets p_t are constructed using the visit counts at the root of the tree:

$$p_t(a_i) = \frac{N_{t,i}}{\sum_j N_{t,j}} \quad \forall i = 1, \dots, K, \tag{3}$$

where $N_{t,i}$ is the visit count of the i-th action in the search tree at step t, and K is the number of actions. Then a_t is sampled according to $\boldsymbol{p}_t$ and is executed observing the next state s_{t+1} and the reward signal r_t. In practice, $\boldsymbol{p}_t$ is often constructed as a greedy policy over the action counts, only executing the most explored one. At the end of each episode, the collected rewards are used to build the value network targets R_t. The triples $(s_t, \boldsymbol{p}_t, R_t)$ are added to a replay buffer $\mathbb{D}$ used during training of the networks. In the original AlphaZero paper, the policy and value networks share the parameter vector θ and AlphaZero minimizes:

$$\mathop{\mathbb{E}}_{(s,\boldsymbol{p},R)\sim\mathbb{D}} \left[(R - v_\theta(s))^2 - \boldsymbol{p}^T \log \pi_\theta(s) + c\|\theta\|^2 \right], \tag{4}$$

where c controls the amount of L_2 regularization.

2.4 HINDSIGHT EXPERIENCE REPLAY

Hindsight Experience Replay (Andrychowicz et al., 2017) is a method of extending off-policy RL algorithms to improve sample efficiency even in the presence of sparse reward functions. HER requires parameterizing the reward, policy, and value as a function of the current and the goal state. The basic idea behind HER is to extend the replay buffer $\mathbb{B}$ after each episode $\{s_0, s_1, \ldots, s_T\}$ with the returns calculated based on a set of subgoals. While the main goal influences the agent's actions during training, it does not influence the state transitions. Consequently, we can generate additional training samples by considering a subset of the states visited during the episode as subgoals. This is extremely beneficial in cases with sparse rewards, such as a reward function of the type $r(s_t, a_t, s_g) = \mathbb{1}(s_{t+1} = s_g)$, where reward signals would be null until the goal state is visited by chance. However, HER enables the reward signals to be generalized across the state space.

3 ALPHAZERO WITH HINDSIGHT EXPERIENCE REPLAY

This section describes the AlphaZeroHER algorithm. AlphaZero has been successfully applied to challenging games such as Go and Chess with outstanding results. The complexity of these games stands in the vast state-action spaces and the highly sparse reward function, since the agents will only know at the end of the game whether they have won (a reward of $+1$), lost (a reward of -1) or drawn (a reward of 0). Although in the context of Temporal Difference (TD) (Sutton et al., 1998) algorithms, Chess and Go fall under the definition of sparse reward, when considering returns observed at the end of the episode (Monte Carlo returns), such games have a clear reward function: the game's result is either a win, a loss or a draw. This reason may give the impression that AlphaZero doesn't suffer in sparse reward setting. However, in goal-directed planning, the Monte Carlo returns are often sparse, in the sense that the whole episode might finish without a reward signal. This problem was also mitigated in the original AlphaGo Zero paper (Silver et al., 2017b), where the authors employed ad-hoc board evaluators to compute the Monte Carlo returns when episodes of Go were interrupted because they were too long. Due to the criticality of sparse rewards, we extend AlphaZero with HER to tackle goal-directed tasks.

3.1 ALPHAZEROHER

The basic idea of AlphaZeroHER, is to extend AlphaZero by using a goal-directed policy and value network and injecting HER into such a setting. Exploiting a goal-directed policy and value network in AlphaZero is effortless since the experience samples also include the goal state s_g. However, AlphaZero is not an off-policy algorithm since the value network is trained with the returns collected while playing the MCTS augmented policy. Moreover, it is not straightforward how to evaluate the new policy when considering a new goal $s_t \neq s_g$ without introducing additional prohibitive computational costs and tree re-weighting procedures. Such problems represent the main obstacle toward introducing HER.

We propose a procedure that extends AlphaZero with HER without adding high computational costs. The basic idea is to neglect its on-policy nature generating additional training samples at the end of each episode by sampling additional subgoals from the visited states.

Figure 1: Performance of the AlphaZero agent in the BitFlip environment for different number of bits using 20 searches. Average over 10 runs, 95% c.i. The orange, blue and green lines report the performances achieved by the agent during the training for 10, 12 and 18 bits respectively.

In fact, even though the MCTS augmented policy of AlphaZero did not reach the goal state, it successfully reached all the states visited during the episode.

More precisely, we employ HER after finishing an episode of length T and having generated the sequence of states, reward and policies, $\{s_t, \boldsymbol{p}_t, r_t\}_{t=1}^T$. The episode is retraced so that at each state s_t, M subgoals are sampled from future visited states, $\{s_i\}_{i=t+1}^T$. After selecting the subgoals states for state s_t, we need to compute these states' policy and value targets. This task is not straightforward since AlphaZero is an on-policy algorithm. If we computed, in some way, a different policy target from the actual policy played $\boldsymbol{p}_t$, these would generate a different sequence of state and rewards after timestep t, which are not available. We could use the built tree-s to evaluate these returns related to the subgoals, but these would come with heavy tree-reweighting schemes for an already computationally heavy algorithm as AlphaZero. For this reason, we select as additional policy targets the policies played during the episode $\boldsymbol{p}_t$ since, although these are not the optimal policies that the MCTS agent would have played if the subgoal states were the goal during the search, they successfully reached the alternative goal states. Therefore, these samples still represent an improvement over the current policy $\boldsymbol{p}_\theta$, which can be used as policy improvement steps. Finally, we compute the new returns based on the states visited only by computing the new reward signals for each new subgoal. Such procedure is done once for each episode and involves negligible additional computation. We call this method AlphaZeroHER.

3.2 Motivating Example

To highlight the AlphaZero criticality in sparse reward environments, we consider a simple BitFlip domain from (Andrychowicz et al., 2017), described in detail in Section 5. In this domain, the goal is to modify a long series of n bits to reach the desired bit configuration. While it might be easy to achieve the goal configuration by applying a random policy when considering few bits only, it is practically impossible reaching the goal state if the bit length is increased.

Figure 1 shows the performance of plain AlphaZero in the bit-flip environment, where we have plotted the expected return and the percentage of solved episodes as a function of the training epochs for three different scenarios. While AlphaZero can consistently solve an "easy" scenario of 10 bits achieving almost perfect performance, it struggles with a modest increase in the number of bits, dramatically failing to solve the task with 18 bits.

4 Related Works

Goal-Directed Reinforcement Learning has been extensively studied over the years. The optimization of multiple goals has been largely investigated in multi-goal policy optimization, curriculum learning, goal-directed planning, and multiple-task off-policy learning.

In the context of universal value function approximators, in Schaul et al. (2015) the authors consider the problem of approximating multiple value functions in a single architecture. In this line of work, various works study the problem of compact representations of multiple tasks (Dhiman et al., 2018; Ghosh et al., 2018). In such context, the use of sub-goals (intermediate states between the current state and the goal state) have been studied to accelerate learning and generalize over the state-space (Nasiriany et al., 2019; Jurgenson et al., 2020). In Parascandolo et al. (2020), the authors move the problem of goal-directed planning from the space of possible policies to the problem of finding suitable sub-goals. While this has some advantages in certain situations, it cannot be applied in large state spaces since the complexity of the algorithm scales linearly with the number of states.

In the context of policy search, Pinto and Gupta (2016) and Caruana (1997) aim to learn policies to solve multiple tasks simultaneously. Meta-learning has also been extensively studied in recent years and can be seen as closely related to multi-task learning. In meta-learning, a meta-learner is trained to learn swiftly in ever-changing tasks to adapt to learning in new untested tasks quickly. While meta-learning has been investigated early in the literature (Schmidhuber, 1987; 2007), recent work has shown impressive results in the context of Deep RL (Finn et al., 2017; 2018). Hierarchical Reinforcement Learning is also closely related to meta-learning (and our work). Here the goal is to (automatically) learn to perform multiple tasks by splitting the main problem into sub-tasks (Schmidhuber, 2002; Fruit et al., 2017). This is also closely related to the options framework.

5 Experiments

In this section, we provide an experimental evaluation of AlphaZeroHER on simulated domains, including a novel application on a quantum compiling task, modeled as a deterministic goal-directed MDP. We ran each experiment in a single multi-core machine, with no GPUs. Details on the hyperparameters employed are given in Appendix A.1.

5.1 BitFlip

We consider a BitFlip environment where the individual bits of a long series of n bits are changed to reach a desired final configuration. More precisely, the state space is $\mathcal{S} = \{0, 1\}^n$, as well as the goal space $\mathcal{G}$. The action space $\mathcal{A} = \{0, 1, \ldots, n-1\}$ specifies which bit of the current state changes from 0 to 1 or vice-versa. At the beginning of each episode, the starting bits and goal state are set randomly with uniform measures over the state space. We use a "sparse" reward of -1 for each transition, unless the goal state is reached.

We tested such an environment as a motivating example for the application of HER in AlphaZero and a benchmark test since increasing the number of bits can vary the task's difficulty sensibly. In all the runs, we use the same network architecture, consisting of a simple MLP with one hidden layer shared with the policy and value network heads with an additional layer nodes each. In the BitFlip environment, we use 20 neurons for the shared layer, 8 neurons for the policy layer and 4 for the value layer. The network hyper-parameters were not optimized. Figure 2 reports the performance of AlphaZeroHER in the scenario of 70 bits for different number of subgoals sampled (0 subgoals refers to plain AlphaZero). While AlphaZero struggles with 12 bits and fails with 18 bits, AlphaZeroHER manages to achieve great results in the case of 70 bits. Moreover, the agent achieves better performance by increasing the number of additional goals, getting perfect performance by using 4 subgoals only.

5.2 2D Navigation Task

In this section, we consider a 2D navigation task built on top of the Mujoco (Todorov et al., 2012) robotics simulator, called Point. The purpose of this experiment is to observe the performance of AlphaZero and AlphaZeroHER in a more challenging task, that requires a fair amount of exploration. More precisely, the agent's goal (orange ball) has to reach the goal state highlighted by the green rectangle as shown in Figure 4. The task is made more challenging by the presence of a wall in the center of the environment. At the beginning of

Figure 2: Comparison between the AlphaZero (red line) and the AlphaZeroHER agents (green, blue, and orange lines) in the BitFlip environment for different numbers of additional sampled subgoals, using 20 searches and 70 bits. Average over 10 runs, 95% c.i.

Figure 3: Comparison between AlphaZero (orange line) and AlphaZeroHER (blue line) in the 2D Navigation task using 70 searches. AlphaZeroHER outperforms AlphaZero by sampling two additional subgoals at each episode. Average over 5 runs, 95% c.i.

each episode, the starting state and the goal state are sampled on the left and right sides of the wall, respectively. The agent observes its current position and its current velocities in both directions and the coordinates of the goal state, while the action space is represented as control over two actuators of the agent. Although the original action space is continuous over the domain $[-1, 1]^2$, we restricted the space to 9 discrete actions, representing the center (no action) and 8 points on the circle centered at action $(0, 0)$ with radius 1. The reward function is -1 at each step, making the optimal policy the shortest path that reaches the green rectangle while circumventing the wall.

We use a simple MLP with one initial layers of 20 hidden nodes. The policy and value network heads have an additional layer of 10 and 4 hidden nodes respectively. Figure 3 shows the results of the experiments in this domain. We use a large horizon of 200 steps, after which we interrupt if the goal state was not reached. While AlphaZero fails to solve the environment, only reaching the goal state in 10% of the episodes, by applying HER we manage to solve most of the episodes, with only sampling 2 additional goals each episode of experience.

5.3 2D MAZE

This section considers an environment of 2D procedurally generated mazes whose structure changes at each episode, as shown in Figure 4. This experiment aims to test the algorithm's performance in a challenging image task, where Convolutional Neural Networks represent the policy and value space. At each episode, the agent is spawned on a free cell (shown in red) and moves to reach the goal cell (shown in green). The action space consists of four directional movements, which move the agent to one of the adjacent cells. However, if the action points towards a wall, the agent does not move. The reward function employed in

Figure 4: Visual representation of the Point (left) and Maze (right) environments.

Figure 5: Comparison between AlphaZero (orange line) and AlphaZeroHER (blue line) in the 2D Maze task using 120 searches. AlphaZeroHER outperforms AlphaZero by sampling two additional subgoals at each episode. Average over 5 runs, 95% c.i.

this environment is a constant reward of -1, prompting the agent to find the shortest path to the goal. The state-space corresponds to a 2D image of the complete maze.

We employ the same network architecture in all the experiments, consisting of a 3-Layer CNN, with a kernel size of 3, a Layer Normalization after each convolutional layer, and strides of [1,1,2]. The policy and value network heads have two additional fully connected layers of 128 and 64 units each. We run experiments in 10x10 mazes, using an horizon of 60 steps, after which we interrupt if the goal state was not reached. Figure 5 shows the results of the experiments in this domain. We can see that AlphaZeroHER clearly outperforms plain AlphaZero in this environment, although it does not itself achieve a perfect score. We attribute this low general performance to the fact that the hyperparameters of the training process were not optimized, and in an image based task, with CNNs as policy and value space, the architecture and training procedure is crucial. Nonetheless, AlphaZeroHER manages to substantially clearly improve over plain AlphaZero with only 2 additional goals.

5.4 QUANTUM COMPILER ENVIRONMENT

Gate-model quantum computers achieve quantum computation by applying quantum transformations on quantum physical systems called qubits (Nielsen and Chuang, 2002). Due to hardware constraints and quantum disturbances (Linke et al., 2017; Maslov, 2017; Leibfried et al., 2007; Debnath et al., 2016), quantum computers require compilers to approximate any quantum transformations as ordered sequences of quantum gates that can be applied on the hardware. In this work, we employ AlphaZeroHER to address the problem of quantum compilation. We consider a Quantum Compiler (QC) environment consisting of a sequence $U_n = \prod_{j=1}^{n} A_j$ of quantum gates A_j that starts empty at the beginning of each episode, as fully described in Moro et al. (2021). Such sequence is built incrementally at each time-step by the agent, choosing from a finite set of quantum gates $\mathcal{B}$ corresponding to

Figure 6: Comparison between AlphaZero (orange line) and AlphaZeroHER (blue line) in the quantum compiling environment with 20 searches. At each episode, AlphaZeroHER sampled 4 additional subgoals. Average over 10 runs, 95% c.i.

the action space. More specifically, we chose the base composed of six finite rotations, i.e $\mathcal{B} = \left(R_{\hat{x}}(\pm\frac{\pi}{128}), R_{\hat{y}}(\pm\frac{\pi}{128}), R_{\hat{z}}(\pm\frac{\pi}{128}) \right)$.

The goal of the agent consists to approximate a single-qubit unitary transformation $\mathcal{U}$ that is chosen at each episode from Haar matrices. Pictorially, sampling Haar unitary matrices can be seen as choosing a number from a uniform distribution (Russell et al., 2017). The observation used as input at time-step t corresponds to the vector of the real and imaginary parts of the elements of the matrix O_n, where $\mathcal{U} = U_n \cdot O_n$. Such representation encodes all the useful information required to achieve the task, i.e the unitary transformation to approximate $\mathcal{U}$ and the current sequence of gates. We exploited average gate fidelity (AGF) (Nielsen, 2002) as a metric to evaluate the distance between the target gate $\mathcal{U}$ and the current sequence of gates U_n. The task is solved whenever the agent reaches a distance equal to or greater than 0.99 AGF. The base of gates $\mathcal{B}$ allows defining a distance-based reward, which allows solving the problem with relative ease, although it leads to sub-optimal solutions as shown in Moro et al. (2021). However, in this work, we employ a sparse reward equal to -1 regardless of the action performed by the agent. For such reason, the task is very challenging since a high number of steps are required to approximate Haar unitary targets on average.

In all the experiments, we use the same network architecture, consisting of a simple MLP with one initial layers of 16 hidden nodes. The policy and value network heads have an additional layer of 8 and 4 hidden nodes respectively. Figure 6 shows the results of the experiments in the QC task. In this task, the planning horizon is substantially longer than in previous environments. We interrupted the episodes at 300 steps since a perfect policy achieves an average episode length of 180 steps, and 95% of the solution can be achieved using less than 200 steps (Moro et al., 2021). AlphaZero shows a slow performance improvement, but after 100 training epochs it fails to learn the optimal policy. On the other hand, AlphaZeroHER consistently improves the performance and achieves almost perfect resolution of the problem.

6 Conclusions

We introduced a novel algorithm for goal-oriented planning, consisting of the extension of AlphaZero with the Hindsight Experience Replay (HER) method to overcome the issues caused by sparse reward functions typical of goal-oriented planning. We provide a straightforward procedure that does not involve high computational costs by sampling other goals from the visited states and addressing the intrinsic on-policy nature of AlphaZero. The proposed approach outperforms AlphaZero in several test domains, including a novel application to quantum compiling, with negligible additional computation compared to plain AlphaZero. In the future, we aim to apply the proposed method to more challenging goal-directed tasks, including tasks with stochastic transition models, which were not considered in this work.

REFERENCES

Marcin Andrychowicz, Filip Wolski, Alex Ray, Jonas Schneider, Rachel Fong, Peter Welinder, Bob McGrew, Josh Tobin, OpenAI Pieter Abbeel, and Wojciech Zaremba. Hindsight experience replay. In I. Guyon, U. V. Luxburg, S. Bengio, H. Wallach, R. Fergus, S. Vishwanathan, and R. Garnett, editors, *Advances in Neural Information Processing Systems*, volume 30. Curran Associates, Inc., 2017. URL `https://proceedings.neurips.cc/paper/2017/file/453fadbd8a1a3af50a9df4df899537b5-Paper.pdf`.

Peter Auer, Nicolò Cesa-Bianchi, and Paul Fischer. Finite-time analysis of the multiarmed bandit problem. *Mach. Learn.*, 47(2–3):235–256, May 2002. ISSN 0885-6125. doi: 10.1023/A:1013689704352. URL `https://doi.org/10.1023/A:1013689704352`.

Joris Borsboom, Jahn takeshi Saito, Guillaume Chaslot, and Jos W. H. M. Uiterwijk. A comparison of monte-carlo methods for phantom go.

C. B. Browne, E. Powley, D. Whitehouse, S. M. Lucas, P. I. Cowling, P. Rohlfshagen, S. Tavener, D. Perez, S. Samothrakis, and S. Colton. A survey of monte carlo tree search methods. *IEEE Transactions on Computational Intelligence and AI in Games*, 4(1):1–43, 2012. doi: 10.1109/TCIAIG.2012.2186810.

Rich Caruana. Multitask learning. *Mach. Learn.*, 28(1):41–75, July 1997. ISSN 0885-6125. doi: 10.1023/A:1007379606734. URL `https://doi.org/10.1023/A:1007379606734`.

Shantanu Debnath, Norbert M Linke, Caroline Figgatt, Kevin A Landsman, Kevin Wright, and Christopher Monroe. Demonstration of a small programmable quantum computer with atomic qubits. *Nature*, 536(7614):63, 2016.

Vikas Dhiman, Shurjo Banerjee, Jeffrey Mark Siskind, and Jason J. Corso. Floyd-warshall reinforcement learning learning from past experiences to reach new goals. *CoRR*, abs/1809.09318, 2018. URL `http://arxiv.org/abs/1809.09318`.

M. Enzenberger, M. Müller, B. Arneson, and R. Segal. Fuego—an open-source framework for board games and go engine based on monte carlo tree search. *IEEE Transactions on Computational Intelligence and AI in Games*, 2:259–270, 2010.

Chelsea Finn, Pieter Abbeel, and Sergey Levine. Model-agnostic meta-learning for fast adaptation of deep networks. In Doina Precup and Yee Whye Teh, editors, *Proceedings of the 34th International Conference on Machine Learning*, volume 70 of *Proceedings of Machine Learning Research*, pages 1126–1135. PMLR, 06–11 Aug 2017. URL `http://proceedings.mlr.press/v70/finn17a.html`.

Chelsea Finn, Kelvin Xu, and Sergey Levine. Probabilistic model-agnostic meta-learning. *CoRR*, abs/1806.02817, 2018. URL `http://arxiv.org/abs/1806.02817`.

Ronan Fruit, Matteo Pirotta, Alessandro Lazaric, and Emma Brunskill. Regret minimization in mdps with options without prior knowledge. In I. Guyon, U. V. Luxburg, S. Bengio, H. Wallach, R. Fergus, S. Vishwanathan, and R. Garnett, editors, *Advances in Neural Information Processing Systems*, volume 30. Curran Associates, Inc., 2017. URL `https://proceedings.neurips.cc/paper/2017/file/90599c8fdd2f6e7a03ad173e2f535751-Paper.pdf`.

Dibya Ghosh, Abhishek Gupta, and Sergey Levine. Learning actionable representations with goal-conditioned policies. *CoRR*, abs/1811.07819, 2018. URL `http://arxiv.org/abs/1811.07819`.

Marek Grzes and Daniel Kudenko. Theoretical and empirical analysis of reward shaping in reinforcement learning. In *2009 International Conference on Machine Learning and Applications*, pages 337–344, 2009. doi: 10.1109/ICMLA.2009.33.

Nozomu Ikehata and Takeshi Ito. Monte-carlo tree search in ms. pac-man. In *2011 IEEE Conference on Computational Intelligence and Games (CIG'11)*, pages 39–46, 2011. doi: 10.1109/CIG.2011.6031987.

Tom Jurgenson, Or Avner, Edward Groshev, and Aviv Tamar. Sub-goal trees - a framework for goal-based reinforcement learning. *CoRR*, abs/2002.12361, 2020. URL https://arxiv.org/abs/2002.12361.

Levente Kocsis and Csaba Szepesvári. Bandit based monte-carlo planning. In *In: ECML-06. Number 4212 in LNCS*, pages 282–293. Springer, 2006.

D Leibfried, E Knill, Christian Ospelkaus, and David J Wineland. Transport quantum logic gates for trapped ions. *Physical Review A*, 76(3):032324, 2007.

Norbert M Linke, Dmitri Maslov, Martin Roetteler, Shantanu Debnath, Caroline Figgatt, Kevin A Landsman, Kenneth Wright, and Christopher Monroe. Experimental comparison of two quantum computing architectures. *Proceedings of the National Academy of Sciences*, 114(13):3305–3310, 2017.

Dmitri Maslov. Basic circuit compilation techniques for an ion-trap quantum machine. *New Journal of Physics*, 19(2):023035, 2017.

Lorenzo Moro, Matteo G. A. Paris, Marcello Restelli, and Enrico Prati. Quantum compiling by deep reinforcement learning. *Communications Physics*, 4(1):178, Aug 2021. ISSN 2399-3650. doi: 10.1038/s42005-021-00684-3. URL https://doi.org/10.1038/s42005-021-00684-3.

Soroush Nasiriany, Vitchyr Pong, Steven Lin, and Sergey Levine. Planning with goal-conditioned policies. In H. Wallach, H. Larochelle, A. Beygelzimer, F. d'Alché-Buc, E. Fox, and R. Garnett, editors, *Advances in Neural Information Processing Systems*, volume 32. Curran Associates, Inc., 2019. URL https://proceedings.neurips.cc/paper/2019/file/c8cc6e90ccbff44c9cee23611711cdc4-Paper.pdf.

Michael A Nielsen. A simple formula for the average gate fidelity of a quantum dynamical operation. *Physics Letters A*, 303(4):249–252, 2002.

Michael A Nielsen and Isaac Chuang. Quantum computation and quantum information, 2002.

Giambattista Parascandolo, Lars Buesing, Josh Merel, Leonard Hasenclever, John Aslanides, Jessica B. Hamrick, Nicolas Heess, Alexander Neitz, and Theophane Weber. Divide-and-conquer monte carlo tree search for goal-directed planning. *CoRR*, abs/2004.11410, 2020. URL https://arxiv.org/abs/2004.11410.

Lerrel Pinto and Abhinav Gupta. Learning to push by grasping: Using multiple tasks for effective learning. *CoRR*, abs/1609.09025, 2016. URL http://arxiv.org/abs/1609.09025.

Christopher D. Rosin. Multi-armed bandits with episode context. *Annals of Mathematics and Artificial Intelligence*, 61(3):203–230, Mar 2011. ISSN 1573-7470. doi: 10.1007/s10472-011-9258-6. URL https://doi.org/10.1007/s10472-011-9258-6.

Nicholas J Russell, Levon Chakhmakhchyan, Jeremy L O'Brien, and Anthony Laing. Direct dialling of haar random unitary matrices. *New Journal of Physics*, 19(3):033007, 2017.

Tom Schaul, Daniel Horgan, Karol Gregor, and David Silver. Universal value function approximators. In Francis Bach and David Blei, editors, *Proceedings of the 32nd International Conference on Machine Learning*, volume 37 of *Proceedings of Machine Learning Research*, pages 1312–1320, Lille, France, 07–09 Jul 2015. PMLR. URL http://proceedings.mlr.press/v37/schaul15.html.

Jurgen Schmidhuber. Evolutionary principles in self-referential learning. on learning now to learn: The meta-meta-meta...-hook. Diploma thesis, Technische Universitat Munchen, Germany, 14 May 1987. URL http://www.idsia.ch/~juergen/diploma.html.

Jürgen Schmidhuber. Optimal ordered problem solver. *CoRR*, cs.AI/0207097, 2002. URL https://arxiv.org/abs/cs/0207097.

Jürgen Schmidhuber. *Gödel Machines: Fully Self-referential Optimal Universal Self-improvers*, pages 199–226. Springer Berlin Heidelberg, Berlin, Heidelberg, 2007. ISBN 978-3-540-68677-4. doi: 10.1007/978-3-540-68677-4_7. URL `https://doi.org/10.1007/978-3-540-68677-4_7`.

David Silver, Aja Huang, Chris J. Maddison, Arthur Guez, Laurent Sifre, George van den Driessche, Julian Schrittwieser, Ioannis Antonoglou, Veda Panneershelvam, Marc Lanctot, Sander Dieleman, Dominik Grewe, John Nham, Nal Kalchbrenner, Ilya Sutskever, Timothy Lillicrap, Madeleine Leach, Koray Kavukcuoglu, Thore Graepel, and Demis Hassabis. Mastering the game of Go with deep neural networks and tree search. *Nature*, 529(7587): 484–489, January 2016. doi: 10.1038/nature16961.

David Silver, Thomas Hubert, Julian Schrittwieser, Ioannis Antonoglou, Matthew Lai, Arthur Guez, Marc Lanctot, Laurent Sifre, Dharshan Kumaran, Thore Graepel, Timothy P. Lillicrap, Karen Simonyan, and Demis Hassabis. Mastering chess and shogi by self-play with a general reinforcement learning algorithm. *CoRR*, abs/1712.01815, 2017a. URL `http://arxiv.org/abs/1712.01815`.

David Silver, Julian Schrittwieser, Karen Simonyan, Ioannis Antonoglou, Aja Huang, Arthur Guez, Thomas Hubert, Lucas Baker, Matthew Lai, Adrian Bolton, Yutian Chen, Timothy Lillicrap, Fan Hui, Laurent Sifre, George van den Driessche, Thore Graepel, and Demis Hassabis. Mastering the game of go without human knowledge. *Nature*, 550(7676):354–359, Oct 2017b. ISSN 1476-4687. doi: 10.1038/nature24270. URL `https://doi.org/10.1038/nature24270`.

Richard S Sutton, Andrew G Barto, et al. *Reinforcement learning: An introduction*. MIT press, 1998.

Emanuel Todorov, Tom Erez, and Yuval Tassa. Mujoco: A physics engine for model-based control. In *2012 IEEE/RSJ International Conference on Intelligent Robots and Systems*, pages 5026–5033, 2012. doi: 10.1109/IROS.2012.6386109.

Table 1: List of the hyperparameters and their values used in all environments.

Hyperparameter	Value
Optimizer	Adam
c_{uct}	2.0
Discount factor	0.999
Episodes per epoch	50

Table 2: List of the hyperparameters and their values used in each environment.

Hyperparameter	Environment	Value
Learning rate	BitFlip	0.0005
	2D Navigation	0.001
	2D Maze	0.0005
	Quantum Compiling	0.00005
Batch size	BitFlip	256
	2D Navigation	512
	2D Maze	512
	Quantum Compiling	512
Search Iterations	BitFlip	20
	2D Navigation	70
	2D Maze	120
	Quantum Compiling	20

A   APPENDIX

A.1   REPRODUCIBILITY DETAILS

In this section, we provide the hyper-parameters employed in the experiments presented in this work. Table 1 and Table 2 provide a list of hyperparameters employed for both AlphaZero and AlphaZeroHER, without being optimized.