Simplifying Automated Pattern Selection for Planning with Symbolic Pattern Databases

Blind Review

Abstract

Pattern databases (PDBs) are memory-based abstraction heuristics that are constructed prior to the planning process, which if expressed symbolically yield a very efficient representation. Recent work in the automatically generation of symbolic PDBs has established it as one of the most successful approach for cost-optimal domain-independent planning. In this paper, we contribute two planners, both using *bin-packing* for its pattern selection. In the second one, we introduce a greedy selection algorithm called *Partial-Gamer*, which complements the heuristic given by bin-packing. We tested our approaches on the benchmarks of the last three International Planning Competitions, optimal track, getting very competitive results, with this simple and deterministic algorithm.

1 Introduction

The automated generation of search heuristics is one of the holy grails in AI, and goes back to early work of Gaschnik (1979), Pearl (1984), and Prieditis (1993). In most cases lower bound heuristics are problem relaxations: each plan in the original state space maps to a shorter one in some corresponding abstract one. In the worst case, searching the abstract state spaces at every given search nodes exceeds the time of blindly searching the concrete search space (Valtorta 1984). With pattern databases (PDBs), all efforts in searching the abstract state space are spent prior to the plan search, so that these computations amortize through multiple lookups.

Initial results of Culberson and Schaeffer (1998) in sliding-tile puzzles, where the concept of a pattern is a selection of tiles, quickly carried over to a number of combinatorial search domains, and helped to optimally solve random instances of the Rubik's cube, with non-pattern labels being removed (Korf 1997). When shifting from breadth-first to shortest-path search, the exploration of the abstract state-space can be extended to include action costs.

The combination of several databases into one, however, is tricky (Haslum et al. 2007a). While the maximum of two PDBs always yields a lower bound, the sum usually does not. Korf and Felner (2002) showed that with a certain selection of disjoint (or additive) patterns, the values in different PDBs can be added while preserving admissibility. Holte et al. (2004) indicated that several smaller PDBs may outperform one large PDB. The notion of a pattern has been generalized to production systems in vector notation (Holte and Hernádvölgyi 2001), while the automated pattern selection process for the construction of PDBs goes back to the work of Edelkamp (2007).

Many planning problems can be translated into state spaces of finite domain variables (Helmert 2004), where a selection of variables (pattern) influences both states and operators. For disjoint patterns, an operator must distribute its original cost, if present in several abstractions (Katz and Domshlak 2008; Yang et al. 2008).

During the PDB construction process, the memory demands of the abstract state space sizes may exceed the available resources. To handle large memory requirements, symbolic PDBs succinctly represent state sets as binary decision diagrams (Edelkamp 2002b). However, there are an exponential number of patterns, not counting alternative abstraction and cost partitioning methods. Hence, the automated construction of informative PDB heuristics remains a combinatorial challenge. Hill-climbing strategies have been proposed (Haslum et al. 2007a), as well as more general optimization schemes such as genetic algorithms (Edelkamp 2007; Franco et al. 2017). The biggest issue in this area remains assessing the quality of the PDBs (in terms of the heuristic values for the concrete state space) which can only be estimated. Usually, this involves generating the PDBs and evaluating them (Edelkamp 2001; Korf 1997).

This work contributes by improving the automated pattern selection process. We first define the settings of cost-optimal action planning and give a characterization of a pattern database. We stress spurious states, as they are inevitable to PDB generation. Next, we move to the encoding of the pattern selection problem and how to evaluate the heuristics resulted from them. The main contribution is a greedy partial PDB selection mechanism, which we show that complements well with bin packing, giving close to state of the art results on our benchmarks (bettering the results of the winner of the 2018 International Planning Competition).

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2 Background

There are a variety of planing formalisms. Fikes and Nilson (1971) invented the propositional specification language STRIPS, inspiring PDDL (McDermott 1998). Holte and Hernádvölgyi (1999) invented the production system vector notation (PSVN) for permutation games. Bäckström (1992) prefers the SAS$^+$ formalism, which is a notation of finite-domain state variables over partial states and operators with pre-, (prevail-,) and postconditions.

Definition 1 (SAS$^+$ Planning Task) *is a quadruple $\mathcal{P} = \langle \mathcal{V}, \mathcal{O}, s_0, s_* \rangle$, where $\mathcal{V} = \{v_1, \ldots, v_n\}$ is the set of finite-domain variable; $\mathcal{O}$ are the operators which consist of preconditions and effects. The remaining two, $s_0 and s_*$ are states. A (complete) state $s = (a_1, \ldots, a_n) \in \mathcal{S}$ assigns a value a_i to every $v_i \in \mathcal{V}$, with a_i in a finite domain D_i, $i = 1, \ldots, n$. For partial states $s^+ \in \mathcal{S}^+$, each $v_i \in \mathcal{V}$ is given an extended domain $D_i^+ = D_i \cup \{\sqcup\}$. We have $s_0 \in \mathcal{S}$ and $s_* \in \mathcal{S}^+$.*

Let an abstract operator $o' = \phi(o)$ be defined as $pre' = \phi(pre)$, and $post' = \phi(post)$. For planning task described above, the corresponding abstract task is $\langle \mathcal{V}, \mathcal{O}', s'_0, s'_* \rangle$ with $s'_0 \in \mathcal{A}$, $s'_* \in \mathcal{A}^+$, The result of applying operator $o' = (pre', post')$ to an abstract state $a = s'$ satisfying pre', sets $s'_i = post'_i \neq \sqcup$, for all $i = 1, \ldots, n$.

A cost is assigned to each operator. In the context of cost-optimal planning, the aim is to minimize the total cost over all plans that lead from the initial state to one of the goals.

The set of reachable states is generated on-the-fly, starting with the initial state by applying the operators. In most state-of-the-art planners, lifted planning tasks are grounded to SAS$^+$. A STRIPS domain with states being subsets of propositional atoms can be seen as a SAS$^+$ instance with a vector of Boolean variables. The core aspect of grounding is to establish invariances, which minimizes the SAS$^+$ encoding.

Definition 2 (State-Space Homomorphism) *A homomorphic abstraction ϕ imposes that if s' is the successor of s in the concrete state space we have $\phi(s')$ is the successor of $\phi(s)$ in abstract one. This suggests abstract operators $\phi(o)$ leading from $\phi(s)$ to $\phi(s')$ for each $o \in \mathcal{O}$ from s of s'.*

As the planning problem spans a graph by applying a selection of set of rules, the planning task abstraction is generated by abstracting the initial state, the partial goal state *and* the operators. Plans in the original space have counterparts in the abstract space, but not vice verse. Usually, the planning task of finding a plan from $\phi(s_0)$ to $\phi(s_*)$ in $\mathcal{A}$ is computationally easier than finding one from s_0 to s_* in $\mathcal{P}$.

The main issue encountered when working with abstractions are *spurious* paths in the abstract state space that have no corresponding path in the original (concrete) space. An intuitive example of two disconnected paths $s_0 \rightarrow s_1 \rightarrow s_2 \rightarrow s_3 \rightarrow \ldots \rightarrow s_l$ and $s_{l+1} \rightarrow s_{l+2} \rightarrow s_{l+3} \rightarrow \ldots \rightarrow s_m = s_*$, is shown in Figure 1 with $l = 3$. As we map s_l and s_{l+1} to the same abstract state, we have an abstract plan which has no preimage in the original one.

Homomorphic abstractions preserve the property that every path (plan) present in the original space is also present

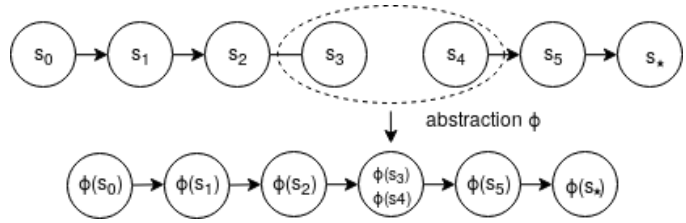

Figure 1: Example of the spurious path problem.

(and shorter) in the abstract state space. Still, abstract operators may yield spurious states.

This problem also pops up in unabstracted search spaces. One cause for this is the nature of PDB construction, namely regression search. To illustrate this, consider the (1×3) sliding-tile puzzle with two tiles 1 and 2 and one empty position, the blank. In one SAS$^+$ encoding we have three state variables: two for the position of the tile $t_i \in \{1, 2, 3\}$, $i \in \{1, 2\}$, and one for the position of the blank $b \in \{1, 2, 3\}$. Let $s_0 = (t_1, t_2, b) = (2, 3, 1)$ and $s_* = (1, 2, \sqcup)$. The operators have preconditions $t_i = x$, $b = x + 1$, and effects $t_i = x + 1$, $b = x$, or preconditions $t_i = x$, $b = x - 1$, and effects $t_i = x - 1$, $b = x$, for $i = \{1, 2\}$ and $x \in \{1, 2, 3\}$ (whenever possible). Going backwards from s_*, the planner does not know the location of the blank and beside the reachable state $t_1 = 2$, $t_2 = 3$, $b = 3$ it generates two additional states $t_1 = t_2 = 1$, $b = 2$ and $t_1 = t_2 = 2$, $b = 1$.

How to mitigate the problem? We cannot expect to remove all spurious states, but there is hope to reduce their number. In the case of the sliding-tile puzzle, there is a dual SAS$^+$ encoding with three variables denoting which tile (or blank) is present at a given position p_1, p_2, or p_3. This *exactly-one-of* state invariance is inferred by the static analyzer, but not used in the state encoding. The information, however, can help to eliminate spurious states.

Either spurious paths through abstraction or though regression, they do not affect the lower bound property of the resulting abstraction heuristic. However, they can blow up the PDBs considerably, given that there are abstract states and paths for which no corresponding preimage in the forward space exist. As a result, refined state invariants (including mutex detection of contradicting facts) greatly improve backward search and, thus, reduce the size of pattern databases.

3 Pattern Databases

As planning is a PSPACE-complete problem (Bylander 1994), heuristic search has proven to be one of the best ways to find solutions in a timely manner.

Definition 3 (Heuristic) *A heuristic h is a mapping of the set of states in $\mathcal{P}$ to positive reals $R_{\geq 0}$. A heuristic is called* admissible*, if $h(s)$ is a lower bound of the cost of all goal-reaching plans starting at s. Two heuristics h_1 and h_2 are* additive*, if h defined by $h(s) = h_1(s) + h_2(s)$ for all $s \in \mathcal{S}$, is admissible. A heuristic is* consistent *if for all operators o from s to s' we have $h(s') - h(s) + c(o) \geq 0$.*

For admissible heuristics, search algorithms like A*

(Hart, Nilsson, and Raphael 1968) will return optimal plans. If h is also consistent, no states will be reopened during search. This is the usual case for PDBs.

Definition 4 (Pattern Database) *is an abstraction mapping for states and operators* and *a lookup table that for each abstract state a provides the (minimal) cost value from a to the goal state.*

The minimal cost value is a lower bound for reaching the goal of the state that is mapped to a in the original state space. PDBs are generated in a backwards enumeration of the abstract state space, starting with the abstract goal. They are stored in a (perfect) hash table for explicit search, and in the form of a BDD with all abstract states of a certain h value while in symbolic symbolic.

Showing that PDBs yield consistent heuristics is trivial (Edelkamp 2001; Haslum et al. 2005), as shortest path distances satisfy the triangular inequality. It has also been shown that for PDBs the sum of heuristic values obtained via *projection* to a disjoint variable set is admissible (Edelkamp 2001). The projection of state variables induces a projection of operators and requires *0/1 cost partitioning*, where operators in abstract space are mapped to either 0 or $c(o)$, so that an operator cannot contribute to more than once. There are extended forms of cost partitioning, that distribute the cost $c(o)$ of operators o to the abstract state spaces (Pommerening et al. 2015).

Definition 5 (Pattern Selection Problem) *is to find a collection of PDBs that fit into main memory, and maximize the average heuristic.*

Definition 6 (Perimeter PDB) *is the result of an unabstracted (blind) backward shortest path search until memory resources are exhausted, setting the value of all yet unreached abstract space to the maximum cost value found in the perimeter, while adding the minimum cost of an operator.*

In several planning tasks, generating the perimeter PDB already solved the problem (Franco et al. 2017).

Symbolic Pattern Databases

In symbolic plan search, we encode each variable domain D_j of the SAS$^+$ encoding, $j = 1, \ldots, n$, in binary. Then we assign a Boolean variable x_i to each i, $0 \leq i < \lceil \log_2 |D_1| \rceil + \ldots + \lceil \log_2 |D_n| \rceil$. This eventually results in a characteristic function $\chi_S(x)$ for any set of states S. The ordering of the variables is important for a concise representation, so that we keep finite domain variables as blocks and move inter-depending variables together. The optimization problem of finding such best linear variable arrangement among them is NP-hard. It is also possible to encode operators as Boolean functions $\chi_o(x, x')$ and to progress (and regress) a set of states to accelerate this (pre)image, the disjunction of the individual operators images could be optimized. For action costs, always expanding the set attached to the minimum cost value yields optimal results (Edelkamp 2002b). As symbolic search is available for partial states (which denote sets of states), both the forward and the backward symbolic exploration in plan space become similar.

There has been considerable effort to show that PDB heuristics can be generated symbolically and used in a symbolic version of A* (Edelkamp 2002a). The concise representation of the Boolean formula for these characteristic functions in a binary decision diagram (BDD) is a technique to reduce the memory requirement during the search. Frequently, the running time for the exploration often reduces as well.

4 Pattern Selection and Cost Partitioning

Using multiple abstraction heuristics can lead to solving more complex problems, but to maintain optimality, we need to distribute the cost of an operator among the abstractions. One way of doing this is present in (Seipp and Helmert 2018). Saturated Cost Partitioning (SCP) has shown benefits to simpler cost partitioning methods. Given an ordered set of heuristics, in our case PDBs, SCP relies on only using those costs which each heuristic uses to create an abstract plan. The remaining costs are left free to be used by any subsequent heuristic. However, considering the limited time budget, this approach is time consuming compared to other cost partitioning methods (Pommerening, Helmert, and Bonet 2017).

One such method is 0/1 cost partition, which zeroes any cost for subsequent heuristics if the previous heuristic has any variables affected by that operator. Both SCP and 0/1 allow heuristics values to be added admissibly. SCP dominates 0/1 cost partitioning (given a set of patterns and enough time, SCP would produce better heuristic values), but it is much more computationally expensive than 0/1 cost partitioning.

Franco et al., (2017) shows that, in order to find good complementary patterns, it is beneficial to try as many pattern collections as possible (Franco et al. 2017). As such, we implemented 0/1 cost partitioning in our work. We tested using the canonical cost partitioning (Haslum et al. 2007b) method as well whenever we added a new PDB, but this resulted in a very pronounced slow down which increased the more PDBs have already been selected. This was the reason we adopted a hybrid combination approach, where 0/1 cost partition is used on-the-fly to generate new pattern collections, and, only after all interesting pattern collections have been selected, we run the canonical combination method, slightly extended to take into account that each pattern has its own 0/1 cost partition.

Given a number of PDBs in the form of pattern collections (sets of individual patterns, each associated with a cost partitioning function), *canonical pattern databases* will select the best admissible combination of PDB maximization and addition. The computation of the canonical PDB is still expensive, so we execute it only once, right before search starts.

There are many alternatives for automated pattern selection based on bin packing such as random bin packing (PBP), causual dependency bin packing (CBP), which could be refined by a genetic algorithm (Franco et al. 2017).

Greedy Selection

Franco et al. (2017) compared the pattern selection method to the one of Gamer (Kissmann and Edelkamp 2011), which tries to construct one single best PDB for a problem. Its pattern selection method is an iterative process, starting with all the goal variables in one pattern, where the causally connected variables who would most increase the average h value of the associated PDB are added to the pattern.

Following this work, we devised a new *Gamer-style* pattern generation method, which behaves similarly, but which adds the option of *partial pattern database* generation to it. By partial we mean that we have a time and memory limit for building each PDB. If the PDB building goes past this limit, we truncate it in the same way we would do with a perimeter PDB, i.e., any unmapped real state has the biggest h value the PDB building was at when it was interrupted.

An important difference with the Gamer method is that we do not try every possible pattern resulting of adding a single causally connected variable to the latest pattern.

Genetic Algorithm Selection

A *genetic algorithm* (GA) is a general optimization method in the class of *evolutionary strategies* (Holland 1975). It refers to the recombination, selection, and mutation of *genes* (states in a state-space) to optimize the *fitness* (objective) function. In a GA, a population of candidate solutions is sequentially evolved to generate a better performing population of solutions, by mimicking the process of evolution. Each candidate solution has a set of properties which can be mutated and recombined. Traditionally, candidate solutions are bitvectors, but there are strategies that work on real-valued state vectors.

An early approach for the automated selection of PDB variables by Edelkamp (2007) employed a GA with genes representing state-space variable patterns in the form of a 0/1 matrix G, where $G_{i,j}$ denotes that state variable i is chosen in PDB j. Besides flipping and setting bits, mutations may also add and delete PDBs in the set.

The PDBs corresponding to the bitvectors in the GA have to fit into main memory, so we have to restrict the generation of offsprings to the ones that represent a set of PDB that respect the memory limitation. If time becomes an issue, we stop evolving patterns and invoke the overall search (in our case progressing explicit states) eventually. An alternative, which sometimes is applied as a subroutine to generate the initial population for the GA, is to use bin packing.

Bin Packing

The bin packing problem (BPP) is one of the first problems shown to be NP-hard (Garey and Johnson 1979). Given objects of integer size $a_1, \ldots, a_n$ and maximum bin size C, the problem is to find the minimum number of bins k so that the established mapping $f : \{1, \ldots, n\} \rightarrow \{1, \ldots, k\}$ of objects to bins maintains $\sum_{f(a)=i} a \leq C$ for all $i \leq k$. The problem is NP-hard in general, but there are good approximation strategies such as first-fit and best-fit decreasing (being at most 11/9 off the optimal solution (Dósa 2007)).

Algorithm 1 Greedy PDBs Creation

function GREEDYPDBS(M,T,S_{min},S_{max},EM) :
Require: time and memory limits T and M, min and max PDB size S_{min} ad S_{max}, evaluation method EM.
  $SelPDBs \leftarrow \emptyset$
  $\mathcal{P}_{sel} \leftarrow \mathcal{P}_{sel} \cup Packer(FFD, S_{min}, M, T, EM)$
  $\mathcal{P}_{sel} \leftarrow \mathcal{P}_{sel} \cup Packer(FFI, S_{min}, M, T, EM)$
  $\mathcal{P}_{sel} \leftarrow \mathcal{P}_{sel} \cup PartialGamer(M, T, EM)$
  Return $\mathcal{P}_{sel}$
end function

function PACKER($Method$,S_{min}, M, T,EM) :
  $SizeLim \leftarrow S_{min}$
  while $(t < T)$ **and** $(m < M)$ **do**
    GENERATE_$\mathcal{P}$($Method$,$SizeLim$)
    if $EM(\mathcal{P})$ **then**
      $\mathcal{P}_{sel} \leftarrow \mathcal{P}$
    end if
    $Size \leftarrow Size * 10$
  end while
  Return $\mathcal{P}_{sel}$
end function

function PARTIALGAMER(M, T,$EvalMethod$) :
  $InitialPDB \leftarrow$ all goal variables
  $SelPDBs \leftarrow InitialPDB$
  while $(t < T)$ **and** $(m < M)$ **do**
    generate all $CandidatePatterns$ resulting of adding one casually connected variable to latest $P \in \mathcal{P}_{sel}$
    for all $P \in CandidatePatterns$ **do**
      if $EM(\mathcal{P})$ **then**
        $\mathcal{P}_{sel} \leftarrow P$
        break
      end if
    end for
  end while
  Return $\mathcal{P}_{sel}$
end function

In the PDBs selection process, however, the definition of the BPP is slightly different. We estimate the size of the PDB by computing the product (not the sum) of the variable domain sizes, aiming for a maximum bin capacity M imposed by the available memory, and we find the minimum number of bins k, so that the established mapping f of objects to bins maintains $\prod_{f(a)=i} a \leq M$ for all $i \leq k$. By taking the logs on both sides, we are back to sums, but the sizes become fractional. In this case, $\prod_{f(a)=i}$ is an upper bound on the number of abstract states needed.

Taking the product of variable domain sizes is a coarse upper bound. In some domains, the abstract state spaces are much smaller. Bin packing chooses the memory bound on each individual PDB, instead of limiting their sum. Moreover, for symbolic search, the correlation between the cross product of the domains and the memory needs is rather weak. However, because of its simplicity and effectiveness,

this form of bin packing currently is chosen for PDB construction.

By limiting the amount of optimization time for each BPP, we do not insist on optimal solutions, but we want fast approximations that are close-to-optimal. Recall, that suboptimal solutions to the BPP do not imply suboptimal solutions to the planning problem. In fact, *all* solutions to the BPP lead to admissible heuristics and therefore optimal plans.

For the sake of generality, we strive for solutions to the problem that do not include problem-specific knowledge but still work efficiently. Using a general framework also enables us to participate in future solver developments. Therefore, in both of the approaches we present in this paper, we focus on the first-fit algorithm.

First-Fit Increasing (FFI), or Decreasing (FFD), is a fast on-line approximation algorithm that first sorts the objects according to their sizes and, then, starts placing the objects into the bins, putting an object to the first bin it fits into. In terms of planning, the variables are sorted by the size of their domains in increasing/decreasing order. Next, the *first* variable is chosen and packed at the same bin with the rest of the variables which are related to it if there is space enough in the bin. This process is repeated until all variables are processed.

5 Symbolic PDB Planners

Based on the results from (Franco et al. 2017), we decided to work only with Symbolic PDBs. Further experiments suggested that PDBs heuristic performs well when it is complemented with other methods. One good combination was using our method to complement a symbolic perimeter PDB, method that we used in the first of the planners we present. The selected method to be complemented first generates a symbolic PDB up to a fixed time limit and memory limit. One advantage of seeding our algorithm with such a perimeter search is that if there is an easy solution to be found in what is basically a brute force backwards search, we are finished before even creating a PDB. Secondly, we combined the Partial-Gamer with bin packing and saw very good results in how they complemented each other. In Figure 2 we see that each method gives good results on their own, Bin-Packing solving 434 and Partial-Gamer 457, but when used toghether they increase to 475.

In our work, however, we decided to use a hybrid, keeping the forward exploration explicit-state, and the PDBs generated in the backward exploration symbolic. Lookups are slightly slower than in hash tables, but they are still in time linear to the bitvector length.

In this section, we will present two symbolic planners, BP-PDB and GreedyPDB, based on the Fast-Downward [Helmert, 2006] planning framework. The two differ in the pattern selection methods that we use in each of them.

BP-PDB

In *BP-PDBs*, we start with the construction of the perimeter PDB, and continue by using two bin-packing methods to create a collection of PDBs. The first method uses first-fit increasing, while the second being first-fit decreasing. Bin-packing for PDBs creates a small number of PDBs which

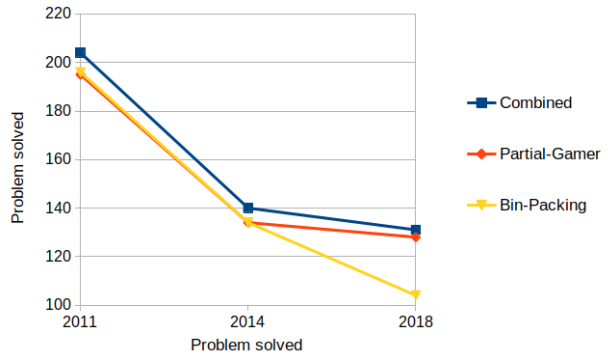

Figure 2: Coverage of Bin Packing, Partial Gamer and of both combined on three latest cost-optimal IPC benchmark problems.

use all available variables. Even though reducing the number of PDBs used to group all possible variables does not guarantee a better PDB, by having a smaller PDB collections, it is less likely to miss interactions between variables due to them being placed on different PDBs. The bin packing algorithms used ensures that each PDB has a least one goal variable.

If no solution is found after the perimeter PDB has been finished, the method will start generating pattern collections stochastically until either the generation time limit or the overall PDB memory limit are reached. We then decide whether to add a pattern collection to the list of selected patterns if it is estimated that adding such PDB will speed up search. We optimize the results given by the bin-packing algorithm giving it to a GA. It then resolve operator overlaps in a 0/1 cost partitioning. To evaluate the fitness function, the corresponding PDBs is built —a time-consuming operation, which nevertheless payed off in most cases. Once all patterns have been selected, the resulting canonical PDB combination is used as an admissible heuristic to do A* search.

GreedyPDB

We encountered that greedily constructed PDBs outperform the perimeter PDB, which we decided not to use. The two construction methods do not complement well, on the extreme case greedy PDBs will build a perimeter PDB after adding all the variables. There is a significant amount of overlapping between both methods. The collection of patterns received from bin packing, however, complements well the greedily constructed PDBs. One reason for this is that in domains amenable to cost-partitioning strategies, i.e. alternative goals are easily parallelized into a complementary collection of PDBs, bin packing can do significantly better than the single PDB approach. Evaluation is based on the definition of sample fitness. The sample is redrawn each time an improvement was found.

Algorithm 1 shows how Greedy PDBs combines two bin packing algorithms with a greedy selection method called Partial Gamer. The two bin packing algorithms use First Fit Decreasing (*FFD*) and First Fit Increasing (*FFI*), same used

Domain/Method	Agr	Cal	DN	Nur	OSS	PNA	Set	Sna	Spi	Ter	Total
GreedyPDB	13	**12**	**14**	**15**	**13**	16	8	13	11	16	**131**
BP-PDB	6	12	14	12	**13**	**19**	8	11	12	16	123
Scorpion	1	**12**	**14**	12	**13**	0	**10**	13	**15**	14	104
SymBiDir	**14**	9	12	11	**13**	**19**	8	4	6	**18**	114
Complementary1	10	11	14	12	12	18	8	11	11	16	123
Complementary2	6	**12**	13	12	**13**	18	8	**14**	12	16	124
Oracle	14	12	14	15	13	19	10	14	15	18	142

Table 1: Coverage of PDB-type planners on the 2018 International Planning Competition for cost-optimal planning

in BP-PDB. For FFD we set a limit of 50 seconds, while for FFI we used a limit of 75 seconds (both limits were found empirically to give the best results). To evaluate (EM) if the generated pattern collections should be added to our selection ($\mathcal{P}_{sel}$), we used as an evaluation method a random walk. If enough of the sampled states heuristic values are improved, the pattern is selected. Partial Gamer greedily grows the largest possible PDB by adding causally connected variables to the latest added pattern. If a pattern is found to improve, as defined by the evaluation method, then we add it to the list of selected pattern collections as a pattern collection with a single PDB. Note that we are using symbolic PDBs with time limits on PDB construction, hence a PDB which includes all variables of a smaller PDB does not necesarily dominate it since the smaller PDB might reach a further depth.

An important difference with the Gamer method is that we do not try every possible pattern resulting of adding a single causally connected variable to the latest pattern. As soon as a variable is shown to improve the pattern, we add it and restart the search for an even larger improving pattern. We found this to work better with the tight time limits required by combining several approaches. All the resulting pattern database collections are combined by simply maximizing their individual heuristic values. The PDBs inside each collection were combined using zero-one cost partitioning. The rationale behing the algorithm is that some domains are more amenable to using several patterns where costs are distributed between each patterns, while other domains seem to favour looking for the best possible single pattern.

6 Experiments

Following is an ablation-type study were we analyze which components worked best. We run different configurations on the competition benchmarks on our cluster that utilized Intel Xeon E5-2660 V4 with 2.00GHz processors. We compare GreedyPDB Planner and BP-PDB with other pattern database and symbolic planners that competed in the 2018 International Planning Competition in the most prestigious and attended deterministic cost-optimal track.

Table 2: Overall coverage of PDB-type planners across different International Planning Competitions for cost-optimal planning.

Year/Method	2011	2014	2018	Total
GreedyPDB	**204**	140	**131**	475
BP-PDB	190	131	123	444
Scorpion	190	118	104	412
SymBiDir	174	129	114	417
Comp1	185	111	123	419
Comp2	**204**	**155**	124	**483**
Oracle	227	171	143	541

Looking at the results of various cost-optimal planners across all domains from the IPC competitions from 2011 to 2018 in Table 2, we get a good overall picture on the PDB planner performance. Symbolic bidirectional search (417 problems being solved) is almost on par with Scorpion (412) and Complementary1 (419), while BP-PDB performs slightly better (444). The overall top two planning systems are GreedyPDB (475) and Complementary2 (483). We deduce that with GreedyPDB we have a simple automated pattern selection strategy in a PDB planning system that is competitive with the state-of-the-art.

On the 2018 benchmark, likely the most challenging one featuring a wide range of expressive application domain models, GreedyPDB would have actually won the competition (Table 1). This indicates that for several planning problems, the best option is to keep growing one PDB with the greedy pattern selector, and compare and merge the results with a PDB collection based on bin packing [1].

7 Conclusion and Discussion

The 2018 International Planning Competition in cost-optimal planning revealed that symbolic PDB planning probably is the best non-portfolio approach. In fact, five of the top six IPC planners were based on heuristic search with PDB and/or symbolic search, while the winning portfolio used such a planner (namely SymBA*, the winner of IPC 2014) for more than half of its successful runs.

Using different pattern generators to complement the two seeding heuristics was extremely successful. It improved our overall results for all the methods we tested compared to simply using the seeding heuristics. One of the best performing method is the combination of an incremental pattern se-

[1] We include all the results of our experiments in Table 3

Planner/ Domain	Greedy PDB	Greedy PDB-BinPack	Greedy PDB-PartGamer	BP-PDB	Scorpion	SymBiDir	Comp1	Comp2	Oracle
Agr	13	4	8	6	1	**14**	10	6	14
Cal	**12**	**12**	**12**	**12**	**12**	9	11	**12**	12
DN	**14**	**14**	12	**14**	**14**	12	**14**	13	14
Nur	14	12	**16**	12	12	11	12	12	16
OSS	**13**	**13**	**13**	**13**	**13**	**13**	12	**13**	13
PNA	18	6	17	**19**	0	**19**	18	18	19
Set	9	9	9	8	**10**	8	8	8	10
Sna	12	11	**14**	11	13	4	11	**14**	14
Spi	11	11	11	12	**15**	6	11	12	15
Ter	15	12	16	16	14	**18**	16	16	18
Bar14	3	3	4	3	3	**6**	3	3	6
Cave14	**7**	**7**	**7**	6	**7**	**7**	**7**	**7**	7
Child14	0	0	0	**5**	0	4	0	1	5
City14	10	10	10	11	14	**18**	10	13	18
Fl14	**20**	**20**	**20**	**20**	8	**20**	14	**20**	20
GED	**20**	**20**	**20**	**20**	**20**	**20**	**20**	**20**	20
Hike	17	17	16	12	10	10	10	**19**	19
Mai	**5**	**5**	**5**	**5**	**5**	**5**	**5**	**5**	5
OS14	8	3	8	5	2	8	5	**13**	13
Pa	4	4	4	3	**6**	2	3	4	6
Tet14	11	11	12	**14**	13	10	11	13	14
TB14	**13**	11	12	5	7	3	7	**13**	13
Tr14	9	9	9	9	**10**	9	9	9	10
Va14	13	14	10	14	13	7	7	**15**	15
Bar11	7	8	8	8	7	**9**	8	8	9
Elev	19	19	19	19	19	**20**	19	19	20
Floor	**12**	**12**	**12**	**12**	6	**12**	**12**	**12**	12
Mys	**20**	**20**	**20**	14	14	11	14	14	20
OS	19	16	16	13	14	14	18	**20**	20
PP	16	16	16	18	**20**	14	18	18	20
Pa	1	1	1	4	**7**	1	1	1	7
Peg	**20**	**20**	**20**	16	17	17	16	19	20
Scan	9	9	9	8	**12**	8	7	9	12
Sok	**20**	**20**	**20**	**20**	**20**	**20**	**20**	**20**	20
TB	**17**	15	15	12	13	9	13	**17**	17
Tr	11	11	11	**13**	**13**	10	10	11	13
Vis	15	16	16	14	8	9	10	**17**	17
Wo	18	13	13	19	**20**	**20**	19	19	20

Table 3: Complete coverage (total number of problems solved) on all of the domains from the previous 3 IPC, cost-optimal track (2011, 2014 and 2018). Domain names have been abbreviated. The planners tested are: three versions of GreedyPDB (one only using Bin Packing, one only using Partial Gamer, and one with both approaches combined); BP-PDB planner; Scorpion and both versions of Complementary planners from IPC 2018; SymBiDir (benchmark planner from IPC 2018).

lection with advanced bin packing. When combining both pattern selection methods, the results are greatly improved, and GreedyPDB would have won the last IPC even ahead of the best portfolio planners (solving 5 more problems), thus contributing a new state-of-the-art in cost-optimal planning.

It is probable that using SCP instead of canonical would improve results. It is also likely that if we used SCP online, i.e., for evaluating whether to add a PDB to the current selected set, instead of the current 0/1 approach a PDB is evaluated, would significantly reduce the total number of patterns we can try given the IPC time limit. How to navigate the trade-off between SCP's better heuristic values vs 0/1's faster computational time is future research.

However, as seen with the impressive results of Complementary2 in the 2011 and 2014 competition benchmark, there is no free lunch. Which pattern generator method is best depends on the benchmark domain it is applied to. By the obtained diversity in the individual solutions, an oracle deciding which pattern selector to take would have solved more problems, so that a portfolio planner could exploit this.

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