UMEC: UNIFIED MODEL AND EMBEDDING COMPRESSION FOR EFFICIENT RECOMMENDATION SYSTEMS

Anonymous authors
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ABSTRACT

The recommendation system (RS) plays an important role in the content recommendation and retrieval scenarios. The core part of the system is the ranking neural network, which is usually a bottleneck of whole system performance during online inference. Hammering an efficient neural network based recommendation system involves entangled challenges of compressing both the network parameters and the feature embedding inputs. We propose a unified model and embedding compression (**UMEC**) framework to jointly learn input feature selection and neural network compression together, which is formulated as a resource-constrained optimization problem using the alternating direction method of multipliers (ADMM) algorithm. Experimental results on public benchmarks show that our **UMEC** framework notably outperforms other non-integrated baseline methods.

1 INTRODUCTION

As the core component of a recommendation system (RS), recommendation models (RM) based on ranking neural networks are widely adopted in general content recommendation and retrieval applications. In general, an effective recommendation model consists of two components: a feature embedding sub-model and a prediction sub-model, as illustrated in Figure 1. Usually, RM adopts neural networks to serve for two sub-models. Formally, we denote a RM as $f(\cdot; \mathcal{W})$, where $\mathcal{W}$ is the learnable parameters of f. For the inference, the model f takes the input feature data $\boldsymbol{x}$ to predict the confidence of a content, serving the recommendation applications. Specifically, we further define the embedding and prediction sub-models as $f_e(\cdot; \mathcal{W}_e)$ and $f_p(\cdot; \mathcal{W}_p)$ respectively, where $\mathcal{W}_e$ and $\mathcal{W}_p$ are their own learnable parameters and $\mathcal{W} = \{\mathcal{W}_e, \mathcal{W}_p\}$. The embedding feature, $\boldsymbol{v} := f_e(\boldsymbol{x}; \mathcal{W}_e)$, is the input of f_p with the input data $\boldsymbol{x}$. Hence, we can express the RM as $f(\cdot; \mathcal{W}) \triangleq f_p(f_e(\cdot; \mathcal{W}_e); \mathcal{W}_p)$. Given a ranking training loss $\ell(\cdot)$ (i.e., binary cross entropy (BCE) loss), the ranking model learning goal can be written as

$$\min_{\mathcal{W}} \sum_{(\boldsymbol{x},\boldsymbol{y})\in\mathcal{D}} \ell(f(\boldsymbol{x}; \mathcal{W}), \boldsymbol{y}),$$

where $\boldsymbol{y}$ is a groud-truth label, and $\mathcal{D}$ is the training dataset.

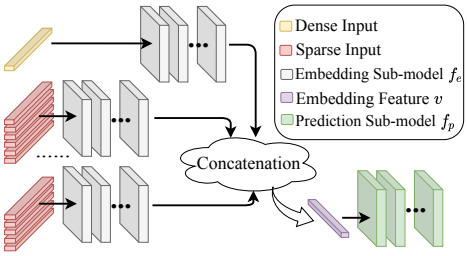

Figure 1: An example of the neural network based recommendation system, named the deep learning recommendation model (DLRM), proposed by Naumov et al. (2019).

Nowadays, extremely large scale datas are poured into the recommendation system to predict user behaviors in many applications. In the online inference procedure, the most heavy computation component is the layer-wise product between the hidden output vectors and the model parameters $\mathcal{W}$, for a neural network based RM. A slimmed neural network structure would save a great amount of power consumption during the inference. Hence, the main idea of a RM compression is to slim the structural complexity of $f(\mathcal{W})$ and reduce the dimension of hidden output vectors.

To obtain an efficient ranking model (for example, MLP based) for a RS, some existing model compression methods can be applied on MLP structure

directly. For example, Li et al. (2016) removes the entire filters in the network together with their connecting feature maps in terms of magnitudes, which can also be applied on MLP structure to remove a specific neuron as well as its connections. Molchanov et al. (2019) approximates the importance of a neuron (filter) to the final loss by using the first and second-order Taylor expansions, which can also be applied to prune the neurons without hassle. There are also some compression methods focusing on dimension reduction of embedding feature vectors. Ginart et al. (2019) proposes a mixed dimension embedding scheme by designing non-uniform embedding dimensions scaling with popularity of features. Joglekar et al. (2020) uses Neuron Input Search (NIS) method to learn the embedding dimensions for the sparse categorical features. However, the performance of these compression methods highly depends on the hyper-parameter tuning and the background knowledge of the specific recommendation model. For example, an embedding dimension compression method may require the user to search the best dimension with multiple training and search rounds.

We would like to solve the RM compression problem with a unified resource constrained optimization framework. It only relies on the resource consumption of the RM $f(\mathcal{W})$ to compress both the MLP and the embedding dimensions without expensive hyper-parameters tuning. Our novel unified model and embedding compression (**UMEC**) method directly satisfies both the requirement of resource consumption of the ranking neural network model and the prediction accuracy goal of the ranking model, with a unified gradient-based training strategy. We reformulate the optimization of training loss associated with hard constraints into a minimax optimization problem solved by ADMM method (Boyd et al., 2011).

To summarize our contributions, we present the merits of **UMEC** as the following:

- To the best of our knowledge, **UMEC** is the first unified optimization framework for the recommendation system scenarios. Unlike those existing works that treat selection of input feature and compression of model as two individual problems, **UMEC** jointly learns both together via unifying both original prediction learning goal and the model compression related hard constraints.
- We reformulate the joint input feature selection and model compression task as a constrained optimization problem. We convert resource constraints and L_0 sparsity constraints into soft optimization energy terms and solve the whole optimization using ADMM methods.
- Extensive experiments performed over an advertising dataset show that our method largely outperforms previous state-of-the-art input feature selection methods and model compression methods.

2 Related Work

Recommendation Models With the recent development of deep learning techniques, plenty of works have proposed learning-based recommendation systems to grapple with the personalized recommendation tasks. Hidasi et al. (2015) applies recurrent neural networks (RNN) on long session data to model the whole session and achieve better accuracy than the traditional matrix factorization approaches. Covington et al. (2016) proposes a high-level recommendation algorithm for YouTube videos by specifying a candidate generation model followed by a separate ranking model, which demonstrates a significant performance boost thanks to neural networks. Wu et al. (2019) proposes a recommendation algorithm based on graph neural network to better capture the complex transitions among items, achieving more accurate item embedding. Their method outperforms traditional sequential approaches. Naumov et al. (2019) exploits categorical features and designs a parallelism scheme for the embedding tables to alleviate the limited memory problem. Huang et al. (2020) proposes a multi-attention based model to mitigate the low efficiency problem in the group recommendation scenarios.

Input Feature Compression for Recommendation Models The enormous input features for practical recommendation scenarios necessitate the selection of useful ones to save memory resource and facilitate the computational efficiency during inference. In factorization machines(FM)-based and context-aware recommendation systems, for example, Mao et al. (2017) conducts input feature selection in an automatic manner by feature ranking and feature sub-sampling, while managing to improve the prediction quality. Ginart et al. (2019) designs a mixed dimension embedding layers

scheme and adjusts the dimension of a particular embedding feature according to the frequency of that item. Joglekar et al. (2020) performs Neural Input Search (NIS) method to search the embedding sizes for the sparse categorical features, and designs the multi-size embedding framework to leverage the model capacity more efficiently.

Model Compression Model compression aims to reduce the complexity of Deep Neural Network (DNN) models to achieving inference efficiency and resource saving. Generally, model compression techniques can be categorized into pruning (Han et al., 2015; Wen et al., 2016; Molchanov et al., 2019), quantization (Hubara et al., 2017; Ajanthan et al., 2019) and distillation (Hinton et al., 2015; Polino et al., 2018; Tung & Mori, 2019). Han et al. (2015) proposes a magnitude-based and element-wise pruning technique, which does not guarantee the reduction of computation efficiency, energy and memory costs. Structured pruning can solve this issue by removing whole certain type of structures from the network, such as filter pruning and channel pruning methods (Li et al., 2016; He et al., 2017; Molchanov et al., 2019). In the meanwhile, researchers also have great interest in investigating resource-constrained compression, which utilizes practical resource requirements(e.g., energy, latency, Flops) to guide the compression (He et al., 2018; Yang et al., 2019; Liu et al., 2019).

3 Unified Model and Embedding Compression on RS

For an arbitrary NN-based recommendation model $f(\cdot)$ in a RS, the terminology of "compression" refers to reduce the power consumption with respect to all the computation operations for the inference. The learning parameters of $f(\mathcal{W})$ can be expressed as $\mathcal{W} := \left\{\boldsymbol{W}^{(l)} | l \in [L]\right\}$, where there are L layers in the $f(\mathcal{W})$. For an arbitrary layer l, the layer's weight is denoted as $\boldsymbol{W}^{(l)} \in \mathbb{R}^{\mathrm{d_{out}} \times \mathrm{d_{in}}}$. The recommendation inference on the layer l is executed as

$$\boldsymbol{x}^{(l+1)} = \sigma\left(\boldsymbol{W}^{(l)}\boldsymbol{x}^{(l)} + \boldsymbol{b}^{(l)}\right),$$

where $\boldsymbol{x}^{(l)} \in \mathbb{R}^{\mathrm{d_{in}}}$ is the input of l-th layer, and $\boldsymbol{b}^{(l)}$ is the corresponding learning bias term. Since the RM consists of two components: feature embedding sub-model and neural network prediction sub-model, the "compression" can be interpreted as shrinking the dimension of embedding feature $\boldsymbol{v}$ and reducing the number of parameters in $\mathcal{W}$ and $\boldsymbol{b}$.

Perspective of model parameters $\mathcal{W}$ and $\boldsymbol{b}$ It is to reduce the input or output neurons for the specific layer l. For example, the i-th neuron of $\boldsymbol{x}^{(l+1)}$ and j-th neuron of $\boldsymbol{x}^{(l)}$ are chosen to remove, then the weight matrix $\boldsymbol{W}^{(l)}$ will be reshaped to $(\mathrm{d_{out}} - 1) \times (\mathrm{d_{in}} - 1)$.

Perspective of feature embedding vectors $\boldsymbol{v}$ The reduction of $\mathrm{d_{in}}$ would result in the elimination on the input features. For example, $\boldsymbol{v}^{(1)}$ is defined as the concatenation of a series of embedding vectors, $\boldsymbol{v}^{(1)} = [\boldsymbol{e}_1; \boldsymbol{e}_2; \cdots; \boldsymbol{e}_n]$, where $[\cdot;\cdot;\cdot]$ represents the concatenation operator, and n denotes the number of embedding feature vectors in the RS. Without loss of generality, for the first embedding vector $\boldsymbol{e}_1 \in \mathbb{R}^{\mathrm{d}_1}$, the zero-out of first d_1 columns in $\boldsymbol{W}^{(1)}$ will result in the elimination of the whole embedding vectors for $\boldsymbol{e}_1$. On the other hand, the compression on $f_e(\mathcal{W}_e)$ would reduce the feature embedding vectors' dimensions.

3.1 A compression example: Group Lasso for Weight Pruning

We first consider a simple example with a RS model consists of $f_e(\mathcal{W}_e)$ and $f_p(\mathcal{W}_p)$. For this RS, to reduce the computation consumption, we present a straightforward model compression method with group lasso. The method considers both the feature embedding selection and network slimming. We only need to apply the sparse regularization terms on the weight matrices. The optimization problem can be expressed as

$$\min_{\mathcal{W}} \ell(\mathcal{W}) + \lambda_1 \sum_i \left\|\boldsymbol{W}^{(1)}_{\cdot,g_i}\right\|_1 + \sum_{l=2}^{L} \lambda_l \sum_i \left\|\boldsymbol{W}^{(l)}_{\cdot,i}\right\|_1, \tag{1}$$

where $\ell(\mathcal{W})$ is the original objective function . The λs are hyper-parameters to control the importance of these regularization terms. $g_\cdot$ denotes the feature groups for the input layer. $\|\cdot\|_1$ indicates the

$\mathcal{L}_1$ norm. The optimization problem (1) restricts the group-wise sparsity for the input layer and the neuron-wise sparsity (or group size = 1) for the rest model layers while training with the original objective function $\ell(\mathcal{W})$. The optimization problem can be solved with the projected gradient descent method. However, the optimization problem (1) has its own limitation. The hyper-parameters λs only have the latent impact on the model size and we could not directly affect the model size. It is not friendly where the users would like to restrict the model size to a specific number. On the other hand, the hyper-parameters also make the optimization problem hard to tune, requiring multiple arguments searching rounds. To avoid these shortages, we are supposed to have new approaches to handle the compression of RS.

3.2 Resource Constrained Model Compression

In this section, we propose a novel unified model and embedding compression method on RS and treat it as a constrained optimization problem. We discuss how to solve the problem using a gradient-based optimization algorithm.

Computation Resource Function for RS Model To avoid the hyper-parameter tuning in the optimization of problem (1), we define the resource function to measure the resource consumption for a specific RS model structure, which can be used to guide the compression of structure. For example, if considering the computation Flops, the resource of an MLP can be defined as

$$R_{\text{Flops}} = \sum_{l=1}^{L} \left(2 \times \mathrm{d}_{\text{in}}^{(l)} \times \mathrm{d}_{\text{out}}^{(l)} + \mathrm{d}_{\text{out}}^{(l)} \right),$$

where $\mathrm{d}_{\text{in}}^{(l)}$ and $\mathrm{d}_{\text{out}}^{(l)}$ indicate the number of input and output neurons. For a pruned layer l, the input and output dimension are restricted by the number of pruned neurons, annotated as $s^{(l)}$ and $s^{(l+1)}$. Therefore, we can define a resource consumption function in terms of s from each layer as

$$R_{\text{Flops}}(\boldsymbol{s}) \triangleq \sum_{l=1}^{L} \left(2 \times \left(\mathrm{d}_{\text{in}}^{(l)} - s^{(l)} \right) \times \left(\mathrm{d}_{\text{out}}^{(l)} - s^{(l+1)} \right) + \left(\mathrm{d}_{\text{out}}^{(l)} - s^{(l+1)} \right) \right).$$

For simplicity, the resource function R_{Flops} only takes the s as the number of neurons. In a more general case, s can be substituted with the product between the number of pruned groups and the size of each pruned group.

Resource Constrained RS Model Compression With the definition of the resource function, we can formulate the following optimization problem,

$$\min_{\mathcal{W}} \ell(\mathcal{W}), \quad \text{s.t. } R_{\text{Flops}}(\mathcal{W}) \leq R_{\text{budget}}, \tag{2}$$

where R_{budget} denotes the upper bound of the overall model computation Flops setted by users. Since we consider the group-wise sparsity for each layer, we utilize the set of variables $\boldsymbol{s} := \{s^{(1)}, s^{(2)}, \ldots, s^{(L)}\}$ to control the model's Flops. The $s^{(l)}$ defines the lower bound of the l-th layer's zero group number for the pruned model. Therefore, we reformulate the optimization problem (2) to be

$$\min_{\mathcal{W}, \boldsymbol{s}} \ell(\mathcal{W}) \tag{3a}$$

$$\text{s.t. } R_{\text{Flops}}(\boldsymbol{s}) \leq R_{\text{budget}} \tag{3b}$$

$$\sum_i \mathbb{I}\left(\left\| \boldsymbol{W}_{.,i}^{(l)} \right\|_2^2 = 0 \right) \geq s^{(l)}, \forall\, l = 2, \ldots, L, \tag{3c}$$

$$\sum_i \mathbb{I}\left(\left\| \boldsymbol{W}_{.,g_i}^{(1)} \right\|_2^2 = 0 \right) \geq s^{(1)}, \tag{3d}$$

where $\mathbb{I}(\cdot)$ is an indicator function with the output $\{0, 1\}$. When the condition is satisfied, the indicator function results in 1, otherwise, it would be 0. $\sum_i \mathbb{I}\left(\left\| W_{.,i}^{(l)} \right\|_2^2 = 0 \right)$ denote the zero group number for the l-th layer. The resource constraint (3b) bounds the resource consumption of the recommendation model. The inequalities in both (3c) and (3d) regularize the Flops consumption for each layer.

3.3 OPTIMIZATION

To address the optimization problem (3), we adopts the alternating direction method of multipliers (ADMM) for the reformulation. In details, the optimization problem contains non-continuous indicator function in constraint (3c, 3d), and non-convex constraint (3b), which make the problem difficult to solve. Therefore, we first reformulate the inequality constraints as soft regularizations and introduce Minimax optimization with dual variables. Then we tackle the non-differentiable objective function using self-defined numerical differentiation. At last, we summarize all the optimization details into a gradient-based optimization formulation.

Minimax Optimization Reformulation Let $\|\boldsymbol{W}_{\cdot,g_i}\|_{s,2}$ be the bottom-$(s,2)$ "norm", which denotes the Frobenius-norm of the sub-matrix (group) composed of bottom-s groups, by sorting from top to bottom in terms of norm of each group. The equivalent formulation of the sparsity constraint (3c, 3d) can be

$$\|\boldsymbol{W}_{\cdot,g_i}\|_{s,2}^2 = 0 \Leftrightarrow \sum_i \mathbb{I}\left(\|\boldsymbol{W}_{\cdot,g_i}\|_2^2 = 0\right) \geq s. \tag{4}$$

The above equivalence (4) is proved by Tono et al. (2017), where the LHS is called DC (difference of convex functions) representation of the $\mathcal{L}_0$-constraint. With the transformation, we can reformulate the problem in Eq. (3), into this minimax optimization problem:

$$\min_{\mathcal{W},\boldsymbol{s}} \max_{\boldsymbol{y},z\geq 0} \ell(\mathcal{W}) + \underbrace{y^{(1)} \left\|\boldsymbol{W}_{\cdot,g}^{(1)}\right\|_{\lceil s^{(1)}\rceil,2}^2 + \sum_{l=2}^{L} y^{(l)} \left\|\boldsymbol{W}_{\cdot,\cdot}^{(l)}\right\|_{\lceil s^{(l)}\rceil,2}^2}_{\text{sparsity loss: } \mathcal{S}(\boldsymbol{y},\boldsymbol{s},\mathcal{W})} + \underbrace{z\left(R_{\text{Flops}}(\boldsymbol{s}) - R_{\text{budget}}\right)}_{\text{resource loss}}, \tag{5}$$

where y and z are dual variables. The operator $\lceil\cdot\rceil$ indicates the ceiling function. In the problem (5), the importance of regularization terms are tuned automatically based on the minimax optimization. The sparsity loss $\mathcal{S}(\boldsymbol{y},\boldsymbol{s},\mathcal{W}) := y^{(1)} \left\|\boldsymbol{W}_{\cdot,g}^{(1)}\right\|_{\lceil s^{(1)}\rceil,2}^2 + \sum_{l=2}^{L} y^{(l)} \left\|\boldsymbol{W}_{\cdot,\cdot}^{(l)}\right\|_{\lceil s^{(l)}\rceil,2}^2$ and the resource loss $z\left(R_{\text{Flops}}(\boldsymbol{s}) - R_{\text{budget}}\right)$ are introduced to substitute the original constraints (3c, 3d). Therefore, the optimal solution to the new problem (5) can serve as the optimal for the original problem (3). To solve it, we present the details of updating rules for all learnable variables in the appendix.

We wrap up all the updating rules together to be a unified optimization algorithm, as described in Algorithm 1. In this algorithm, we only show an example that the input layer is column-wise grouped. For a more general case, the column-wise group sparsity can be applied to an arbitrary layer in the RS model.

Prune and Finetune Solving the minimax optimization problem (5) will make some channel weights extremely close but not exactly equal to zeros. In order to extract the slimmed network, for each $\boldsymbol{W}^{(l)}$, we discard the $s^{(l)}$ groups with smallest $\mathcal{L}_2$ norms $\|\boldsymbol{W}_{\cdot,g_i}^{(l)}\|_2$ (extremely close to 0) after we have solved problem (5). Then we finetune the explicitly pruned network to further improve the performance.

4 EXPERIMENTS

To demonstrate the effectiveness of **UMEC**, we run experiments on a standard public RM over the real-world recommendation dataset. And we'd like to answer the following questions: *Whether our unified optimization framework that jointly considers input feature selection and prediction model compression has superiority over previous state-of-the-art RS compression methods which solve the problem from only one aspect? If yes, why?*

4.1 EXPERIMENTAL SETUP

Dataset and Model We conduct all our experiments on the state-of-the-art ads CTR prediction model named DLRM (Naumov et al., 2019), as illustrated in Figure 1. Following Naumov et al.

Algorithm 1: Gradient-based algorithm to solve problem (5) for **UMEC**.

Input: Resource budget R_{budget}, learning rates $\eta_1, \eta_2, \eta_3, \eta_4$, number of total iterations τ.
Result: DNN pruned weights $\mathcal{W}^*$.

Initialize $t = 1, \mathcal{W}^1$; `// random or a pre-trained dense model`
for $t \leftarrow 1$ **to** τ **do**
  $\mathcal{W}^{t+1} = \text{Prox}_{\eta_1 \mathcal{S}(\boldsymbol{y}^t, \boldsymbol{s}^t, \mathcal{W}^t)} \left(\mathcal{W}^t - \eta_1 \hat{\nabla}_{\mathcal{W}} \ell \left(\mathcal{W}^t \right) \right)$; `// Proximal-SGD`
  $\boldsymbol{s}^{t+1} = \boldsymbol{s}^t - \eta_2 \left(\tilde{\nabla}_{\boldsymbol{s}} \mathcal{S} \left(\boldsymbol{y}^t, \boldsymbol{s}^t, \mathcal{W}^{t+1} \right) + \tilde{\nabla}_{\boldsymbol{s}} z^t \left(R_{\text{Flops}} \left(\boldsymbol{s}^t \right) - R_{\text{budget}} \right) \right)$; `// Gradient (STE) Descent`
  $y^{(1)^{t+1}} = y^{(1)^t} + \eta_3 \left(\left\| \boldsymbol{W}_{\cdot,g}^{(1)^{t+1}} \right\|^2_{\lceil \boldsymbol{s}^{(1)^{t+1}} \rceil, 2} \right)$; `// Gradient Ascent`
  $y^{(l)^{t+1}} = y^{(l)^t} + \eta_3 \left(\left\| \boldsymbol{W}^{(l)^{t+1}} \right\|^2_{\lceil \boldsymbol{s}^{(l)^{t+1}} \rceil, 2} \right), \forall\, l = 2, \cdots, L$
  $z^{t+1} = z^t + \eta_4 \left(R_{\text{Flops}} \left(\boldsymbol{s}^t \right) - R_{\text{budget}} \right)$; `// Gradient Ascent`
$\mathcal{W}^* = \mathcal{W}$

(2019), we use the Criteo AI Labs Ad Kaggle dataset[1] for all experiments. The Criteo AI Labs Ad Kaggle dataset contains approximately 45 million click log samples collected over seven days. Each sample contains 13 continuous and 26 categorical input features. Following the official setting, we split the data of the last day into validation and testing sets, and use data from the rest six days as training set.

Baseline methods Latency of an ads CTR prediction model mainly comes from two sources: feature embedding and prediction model inference. Feature embedding layers map input categorical values into a vector space. Both the number of input categorical values and the output feature space dimension can affect the latency of feature embedding stage. The inference latency of predication model mainly depends on the prediction model size. Following the above analyses, methods to accelerate ads CTR prediction models mainly fall into three categories:

- Prediction model compression: compressing the prediction model with traditional model compression methods, such as Li et al. (2016); Molchanov et al. (2019); Yang et al. (2019).
- Input feature selection: reducing the number of input categorical features by filtering out non-essential ones.
- Embedding dimension reduction: shrinking the dimension of embedding layers' output space. Two recent works (Ginart et al., 2019; Joglekar et al., 2020) fall into this category.

Our unified optimization framework jointly considers input feature selection and model compression. We will further show that our method can be generalized to also consider input feature dimension-reduction. So we compare our method with baselines from all three categories to show the superiority of our method over those baselines tackling RS compression problem from only one aspect.

General Training and Evaluation Details For the general training and evaluation settings in our experiments, please see the appendix A for more details.

Evaluation Metrics We evaluate the performance with the following two terminologies: *Accuracy* and *Compression Ratio (CR)*. **Accuracy:** CTR prediction accuracy on the validation set. **Compression ratio (CR):** the ratio between the pruned Flops and original model Flops. More formally, $\text{CR} = 1 - p_f(\mathcal{W})/p_f(\mathcal{W}_0)$, where $p_f(\cdot)$ calculates the Flops of a (sub-)model. $\mathcal{W}$ and $\mathcal{W}_0$ are the pruned and original dense prediction models, respectively. The larger CR, the more compact and efficient model we have obtained.

[1] https://www.kaggle.com/c/criteo-display-ad-challenge

4.2 PREDICTION MODEL COMPRESSION FOR RS MODEL

We design and conduct extensive experiments to examine the compression performance among our method and several state-of-the-arts model compression methods. The baseline methods include handcrafted structures, one-shot magnitude pruning (MP) (Li et al., 2016), and two recent state-of-the-art methods, namely Taylor pruning (TP) (Molchanov et al., 2019) and energy-constrained model compression (ECC) (Yang et al., 2019).

In Figure 2, we demonstrate the best accuracy on validation set under different compression ratios (CRs) on the Criteo AI Labs Ad Kaggle dataset. For more results on the the Criteo Ad Terabyte dataset, please see the appendix A.

Several observations can be drawn from this comparison figure. First, our method continuously outperforms all other methods with a margin of at least 0.01%. Second, only our method can successfully compress the original dense model to the ideal budget while still manages to maintain the performance without any degradation, within a certain CR scope.

These results show that our joint model compression and input selection method can achieve much better balance of efficiency vs accuracy than traditional model compression methods.

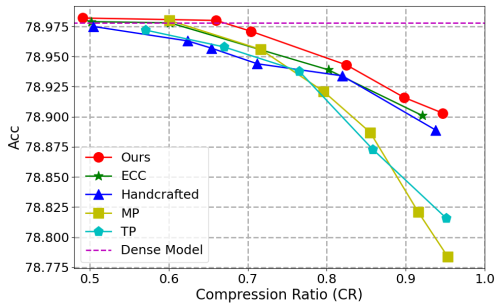

Figure 2: Results on RS prediction model compression by different methods on the Criteo AI Labs Ad Kaggle dataset. Each curve shows the CR-Accuracy trade-off of one compression method. The doted magenta line represents the accuracy achieved by the original dense DLRM model.

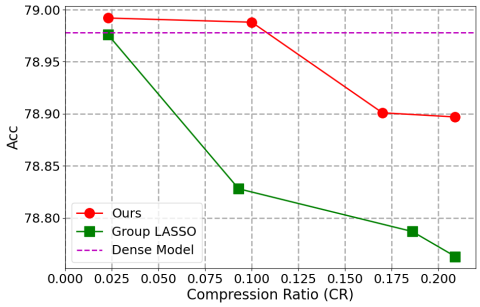

Figure 3: Results on RS input feature selection by different methods on the Criteo AI Labs Ad Kaggle dataset. Each curve shows the CR-Accuracy trade-off of one input feature selection method. The doted magenta line represents the accuracy achieved by the original dense DLRM model.

4.3 INPUT FEATURE SELECTION FOR RS MODEL

We evaluate the effectiveness of our proposed method on input feature selection task. The input feature selection task can be easily realized using our proposed framework, by keeping the resource constraint for the features groups in input layer (*i.e.*, Eq. (3c)) and ignoring constraint for weights of hidden layers(*i.e.*, Eq. (3d)). We use group Lasso as self-designed baseline. The loss function of group Lasso is shown in Eq. (1). Since we are only considering input feature selection in this sub-section, the sparsity regularization on hidden layers *(e.g.*, the second term in $\mathcal{S}(\boldsymbol{y}, \boldsymbol{s}, \mathcal{W})$) is ignored. We tune hyper-parameter λ_1 among 0.0005, 0.001, 0.005, 0.01 in order to get different compression ratios. After group Lasso training, all input features whose $\mathcal{L}_2$ norms are below a threshold th will be removed, and the Flops for the new model are calculated accordingly. We empirically find that setting th to 0.01 can achieve good performance for group Lasso and thus using it as the default value. For both our method and group Lasso, we train and fine-tune for 1 epoch and 2 epochs, respectively.

In Figure 3, the performance on the holdout validation set at the end of the compressing process is reported. We demonstrate the effectiveness of our method in input feature selection task, by showing its superior performance under all the compress ratios. Another observation is that the pruned model of both methods will fail to recover the performance of the original dense model if too many input features are removed. For example, at 0.21 compression ratio, which corresponds to removing 9 out of the total 27 input features, both methods have considerable drop of accuracy. This indicates that reducing number of input features will cause considerable harm to the model's performance.

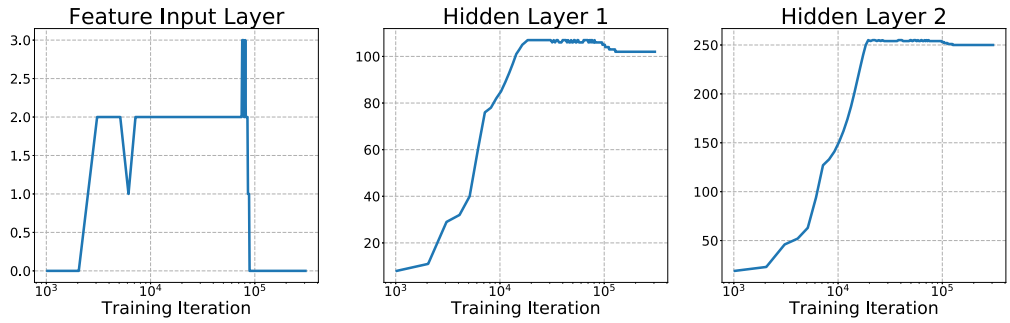

Figure 4: The number of pruned features/neurons for each layer during the training process using **UMEC** with $R_{\text{budget}} = 0.5 \times p_f(\mathcal{W}_0)$, where $p_f(\mathcal{W}_0)$ denotes the Flops of the original dense model. For the input layer, the mentioned dense model has 27 features in total. For the two hidden layers, it has 512 and 256 neurons respectively. The convergency of the binary cross entropy (BCE) loss during training is shown in Figure 5 in the appendix.

4.4 Embedding Dimension Reduction for RS Model

We show that our method can also be applied on embedding dimension reduction. In this new scenario, $\mathcal{W}$ in Eq. (3) is embedding layer weights, instead of previous prediction model weights. Eq. (3d) is removed (*i.e.*, no longer to prune the input dimension). The rest parts of the objective function remain the same.

We compare our method with the state-of-the-art embedding dimension reduction method named mixed dimension embedding layers (MDEL) (Ginart et al., 2019). Following Ginart et al. (2019), we use size of the embedding layers to help define compression ratio. More specifically, in this setting, $\text{CR} = 1 - p_s(\mathcal{W})/p_s(\mathcal{W}_0)$, where $p_s(\cdot)$ calculates the number of parameters in a (sub-)model. $\mathcal{W}$ and $\mathcal{W}_0$ are the pruned and original dense embedding sub-models, respectively. To evaluate performance change after pruning, we define $\Delta_{acc} = \text{Acc}_{\mathcal{W}} - \text{Acc}_{\mathcal{W}_0}$, where $\text{Acc}_{\mathcal{W}}$ and $\text{Acc}_{\mathcal{W}_0}$ are CTR prediction accuracy of a pruned and original dense model, respectively.

Experiment results are shown in Table 1. As we can see, both methods have slightly improvement on accuracy at around 50% CR, while the accuracy improvement of our method is larger than that of MDEL. Also, our method can still achieve better accuracy improvements than MDEL with even 10% larger CR. These results show that our ADMM based compression algorithm is better than MDEL.

Table 1: Results on embedding dimension reduction.

Method	CR	Δ_{acc}
MDEL	0.5	0.10%
Ours	0.5	0.24%
	0.6	0.16%

4.5 Sparsity Analyses of **UMEC**

Below we present how the sparsity of the prediction model evolves during the pruning phase in Section 4.2. As a recall, the aforementioned prediction model consists of one input layer and two hidden layers, with 27 input features, 512 and 256 neurons respectively. As shown in Figure 4, when $R_{\text{budget}} = 0.5 \times p_f(\mathcal{W}_0)$, the pruned input features/neurons converges to 0, 102 and 250 respectively. During training, last hidden layer getting the most percentage of neurons removed and the input layer getting the least percentage. We can come to several conclusions from this result. First, such phenomenon aligns with the observation in Section 4.3 and serves as an evidence that we need enough number of input features to adequately represent the raw input information and contribute to the downstream classification task. Second, to perform the relatively easier task, i.e., binary classification, the requirement of neurons from last hidden layer falls far below the original design, thus considerable resource consumption can be saved here. Third, it demonstrates that our resource-constrained unified optimization plays a smart role in globally finding the optimal resource allocations across all layers.

5 CONCLUSION

The goal of this paper is to tackle with the new problem that jointly compressing input features and neural network structures in the recommendation models. We propose **UMEC** framework by integrating these two objectives into one unified constrained optimization problem, solved by ADMM method. We conduct extensive experiments and demonstrate the effectiveness of our proposed **UMEC** method by observing its superior performance than other state-of-the-art baseline methods.

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A Appendix

A.1 Update Rule for all learnable variables

To solve the optimization problem (5), we utilize the ADMM strategy to solve a series of sub-problems as follows.

Update $\mathcal{W}$ The optimization problem on $\mathcal{W}$ can be solved with proximal-SGD (Nitanda, 2014). The definition of proximal operator is as follows:

$$\mathrm{Prox}_{\eta\mathcal{S}(\boldsymbol{y},\boldsymbol{s},\mathcal{W})}(\bar{\mathcal{W}}) = \arg\min_{\mathcal{W}} \frac{1}{2}\left\|\mathcal{W}-\bar{\mathcal{W}}\right\|^2 + \eta\mathcal{S}\left(\boldsymbol{y},\boldsymbol{s},\mathcal{W}\right)$$

where $\bar{\mathcal{W}}$ is the direct stochastic gradient descent update of $\mathcal{W}$. The sub-problem above has the closed form solution for $\mathcal{W}^* := \{\boldsymbol{W}^{(1)*}, \boldsymbol{W}^{(2)*}, \ldots, \boldsymbol{W}^{(L)*}\}$:

$$\boldsymbol{W}_i^* = \begin{cases} \bar{\boldsymbol{W}}_i, & \text{if } \left\|\bar{\boldsymbol{W}}_i\right\| >= \left\|\bar{\boldsymbol{W}}_{\text{least-}\lceil s \rceil}\right\|, \\ \frac{1}{1+2\eta y}\bar{\boldsymbol{W}}_i, & \text{otherwise,} \end{cases}$$

where $\boldsymbol{W}_i$ denotes the i-th sub-matrix, and $\boldsymbol{W}$ is the weight for an arbitrary layer.

Update dual variables z and $\boldsymbol{y}$ For the sub-optimization problem, we have

$$\max_{\boldsymbol{y}, z \geq 0} \; y^{(1)} \left\|\boldsymbol{W}_{\cdot,g}^{(1)}\right\|^2_{\lceil s^{(1)} \rceil, 2} + \sum_{l=2}^{L} y^{(l)} \left\|\boldsymbol{W}_{\cdot,\cdot}^{(l)}\right\|^2_{\lceil s^{(l)} \rceil, 2} + z\left(R_{\text{Flops}}(\boldsymbol{s}) - R_{\text{budget}}\right),$$

and we can adopt the gradient ascent method as the update rule.

Update $\boldsymbol{s}$ The optimization on $\boldsymbol{s}$ relies on both sparsity and resource loss. However, both of them are non-differentiable due to the ceiling function $\lceil s \rceil$. Straight-through estimator (STE) (Bengio et al., 2013) is an effective approach for optimization through the non-differentiable functions. The main idea is to adopt some simple proxy to be the derivative of the non-differentiable formulation. Thus, the back-propagation can be applied as what happened in the differentiable case. For $\|\boldsymbol{W}\|^2_{s,2}$, we can apply the numerical differentiation $\|\boldsymbol{W}\|^2_{s+1,2} - \|\boldsymbol{W}\|^2_{s,2}$ as the proxy derivative of $\|\boldsymbol{W}\|^2_{s,2}$ with respect to s:

$$\frac{\tilde{\partial} \|\boldsymbol{W}\|^2_{s,2}}{\tilde{\partial} s} = \boldsymbol{W}^2{}_{\text{least-min}(\text{Dim}(\boldsymbol{W}),\, s+1)},$$

where $\boldsymbol{W}^2$ is the column-group wise $\mathcal{L}_2$ format of $\boldsymbol{W}$, $\text{Dim}(\boldsymbol{W})$ is the total number of column groups of $\boldsymbol{W}$, and $\boldsymbol{W}^2_{\text{least}-j}$ is the j-th least column group in $\boldsymbol{W}^2$.

For a general resource consumption function (e.g., Flops), the non-differentiable part of R is the ceiling function $\lceil s \rceil$, for which we can use a common STE (Bengio et al., 2013): $\frac{\tilde{\partial}\lceil s \rceil}{\tilde{\partial} s} = 1$.

$$\frac{\tilde{\partial}\lceil s \rceil}{\tilde{\partial} s} = 1.$$

Now we can wrap up all the update rules together to be a unified optimization algorithm 1. In this algorithm, we only show an example for the input layer to be column grouped. For a more general case, the column-group wise sparsity can be applied to an arbitrary layer in the RS model.

A.2 General Training and Evaluation Details

We follow the general settings in Naumov et al. (2019) in all our experiments: we use SGD optimizer with learning rate 0.1 to optimize the BCE loss ($\ell(\mathcal{W})$ in our method); we set training batch size to 128, initial feature embedding dimension to 16, and use the default three-layer MLP prediction model with hidden dimensions 512 and 256.

For our method, we use Adam optimizer (Kingma & Ba, 2014) for $\boldsymbol{s}$ and SGD optimizer for $\mathcal{W}$, $\boldsymbol{y}$, and z. We set learning rates $\eta_1, \eta_2, \eta_3, \eta_4$ in Algorithm 1 to be $[0.1, 0.05, 0.1, 2.0]$ respectively, and set τ to be 306,969 which equals to 1 epoch. After the training process in Algorithm 1, we zero out the redundant neurons (as described in the last paragraph in Section 3) and keep the model weights of the exacted sub-network as initialization values for the following fine-tune process. We then perform fine-tuning for 2 epochs. For fair comparison, we also fine-tune 2 epochs for all baseline methods. Following Naumov et al. (2019), the best accuracy on validation set is reported.

Figure 5: The convergency of the binary cross entropy (BCE) loss during training using **UMEC** with $R_{\text{budget}} = 0.5 \times p_f(\mathcal{W}_0)$, where $p_f(\mathcal{W}_0)$ denotes the Flops of the original dense model.

Table 2: Real-device energy consumption and latency of different methods. Best values among all compression methods are shown in bold.

Method	Acc (%)	Energy (10^{-3}J)	Latency (ms)
Ours	**78.971**	**8.81**	**0.123**
ECC	78.939	9.05	0.132
Handcrafted	78.963	9.32	0.140
MP	78.956	9.16	0.136
TP	78.958	9.23	0.137
Dense Model	78.978	9.49	0.144

A.3 Energy Consumption and Inference Latency of Network

We evaluate the energy cost and latency of all models on a GTX 2080 Ti GPU. Following Yang et al. (2019), we use the `nvidia-smi` utility[2] to monitor the energy consumption. We follow the settings in Fu et al. (2020) to measure inference latency on the aforementioned real-device. All experiments are implemented with PyTorch. As shown in Table 2, our method achieves best accuracy with least energy consumption and latency among all compared compression methods.

A.4 Experimental Results on Terabyte Dataset

We also provide the experimental results for the Criteo Ad Terabyte dataset[3]. The full dataset consists of approximately 4.4 billion click log samples collected over 24 days. For quick demonstration purpose, we perform uniform sampling with 12.5% sampling rate from the data among first 6 days, where the first 5 days are used as the training data and the 6th day is split into validating and testing data. The general training settings all follow those in appendix A.2 except with batch size equal to 2048 and τ equal to 69,281. The experimental results over the full dataset following the same sampling scheme in Naumov et al. (2019) will be included in the camera ready version once the paper gets accepted.

As shown in Figure 6 and Figure 7, our proposed method consistently outperforms all other baseline methods.

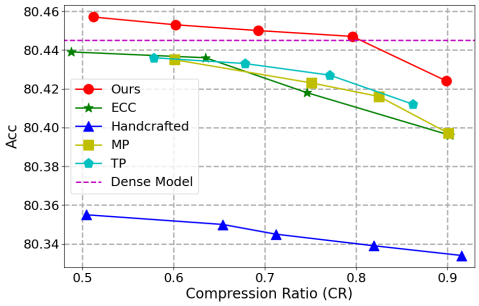

Figure 6: Results on RS prediction model compression by different methods on the Criteo Ad Terabyte dataset. Each curve shows the CR-Accuracy trade-off of one compression method. The doted magenta line represents the accuracy achieved by the original dense DLRM model.

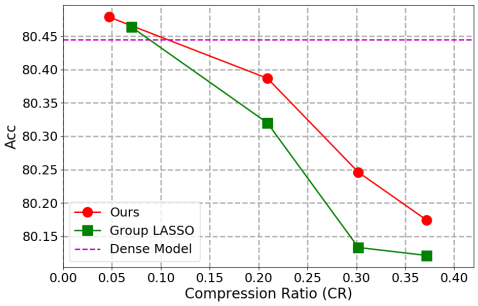

Figure 7: Results on RS input feature selection by different methods on the Criteo Ad Terabyte dataset. Each curve shows the CR-Accuracy trade-off of one input feature selection method. The doted magenta line represents the accuracy achieved by the original dense DLRM model.

[2]https://developer.download.nvidia.com/compute/DCGM/docs/nvidia-smi-367.38.pdf
[3]https://labs.criteo.com/2013/12/download-terabyte-click-logs/

A.5 CASCADED PIPELINE AS A BASELINE

We provide experimental results under cascaded pipeline using **UMEC**, where the compression processes for the input feature and the prediction model are carried out sequentially. Two scenarios are demonstrated: a) Conducting input feature selection first, then prediction model compression, of which the results are shown in Figure 8; b) Conducting embedding dimension reduction first, then prediction model compression, of which the results are shown in Figure 9. We set CR values of first stage in cascaded pipeline as 0.116, 0.116, 0.302, 0.302, 0.302 respectively for a), and 0.1, 0.1, 0.1 for b). Then we try our best to set the final CR values of whole cascaded pipeline to be similar to the CR values used in our joint framework respectively for fair comparisons in both figures. For demonstration purpose, we choose to conduct the experimental comparisons on the Criteo AI Labs Ad Kaggle dataset.

Each curve shows the CR-Accuracy trade-off of one compression method. Comparing the results of the cascaded pipeline with the joint framework, Figure 8 and Figuire 9 both support the superiority of the joint framework.

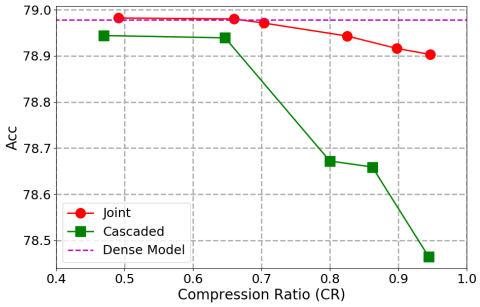

Figure 8: Results on the pipeline with a cascade of input feature selection and prediction model compression, and comparison with the corresponding jointly optimized framework.

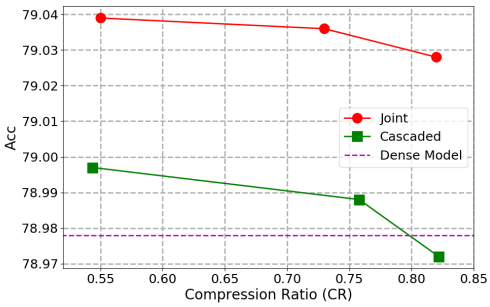

Figure 9: Results on the pipeline with a cascade of embedding dimension reduction and prediction model compression, and comparison with the corresponding jointly optimized framework.