PALU: KV-CACHE COMPRESSION WITH LOW-RANK PROJECTION

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ABSTRACT

Post-training KV-Cache compression methods typically either sample a subset of effectual tokens or quantize the data into lower numerical bit width. However, these methods cannot exploit redundancy in the hidden dimension of the KV tensors. This paper presents a hidden dimension compression approach called *Palu*, a KV-Cache compression framework that utilizes low-rank projection to reduce inference-time LLM memory usage. Palu decomposes the linear layers into low-rank matrices, caches compressed intermediate states, and reconstructs the full keys and values on the fly. To improve accuracy, compression rate, and efficiency, *Palu* further encompasses (1) a medium-grained low-rank decomposition scheme, (2) an efficient rank search algorithm, (3) low-rank-aware quantization compatibility enhancements, and (4) optimized GPU kernels with operators fusion. Extensive experiments with popular LLMs show that *Palu* compresses KV-Cache by 50%, while maintaining strong accuracy and delivering up to **1.89× speedup** on the RoPE-based attention module. When combined with quantization, *Palu*'s inherent quantization-friendly design yields small to negligible extra accuracy degradation, while saving additional memory than quantization-only methods and achieving up to **2.91× speedup** for the RoPE-based attention. Moreover, it maintains comparable or even **better accuracy (up to 1.19 lower perplexity)** compared to quantization-only methods. These results demonstrate *Palu*'s superior capability to effectively address the efficiency and memory challenges of LLM inference posed by KV-Cache.

1 INTRODUCTION

Large language models (LLMs) have propelled AI into new applications and capabilities, providing a high-level intelligence that previous machine learning (ML) models could not achieve. To speed up inference, caching the Key-Value states (KV-Cache) in memory is a simple yet effective technique. However, the size of the KV-Cache can grow rapidly, straining memory capacity and bandwidth especially with long context lengths (Fu, 2024); further, the memory-bounded nature of the decoding stage limits inference speed when loading KV-Cache data (Gholami et al., 2024). Therefore, KV-Cache compression has become a central research topic for running LLMs efficiently.

Although emerging attention mechanisms such as Multi-Query Attention (MQA) (Shazeer, 2019), Group-Query Attention (GQA) (Ainslie et al., 2023) and Multi-head Latent Attention (MLA) (DeepSeek-AI et al., 2024) can reduce KV-Cache size, it either requires model pre-training or has a significant impact on model's accuracy when converting from traditional Multi-Head Attention (MHA) (Chen et al., 2024). In contrast, post-training KV-Cache compression techniques offer an alternative approach to advance efficiency for existing models. Among various KV-Cache compression methods, quantization (Liu et al., 2024b; Hooper et al., 2024) and token eviction (Zhang et al., 2024; Xiao et al., 2024) stand out as effective strategies to reduce the memory footprint of KV-Cache.

Quantization methods aim to reduce the bit-width used to represent each piece of data, while token eviction techniques focus on retaining a partial set of KV-Cache. However, both methods neglect the hidden dimensions of the KV-Cache, where substantial redundancy often resides. To capitalize on this untapped potential, we introduce *Palu*, a post-training KV-Cache compression framework that leverages low-rank projection to reduce the hidden dimension of KV tensors, offering an additional and orthogonal compression dimension to existing quantization and token eviction methods.

A naive way to utilize low-rank projection for compressing the KV-Cache is by directly mapping cached matrices into low-rank space (Jolliffe & Cadima, 2016; Zhao et al., 2024). However, this approach imposes an unacceptably heavy overhead of computing the decomposition matrices during runtime. To avoid this, *Palu statically decomposes the Key and Value-projection weight matrices* and *caches the latent representations* of the low-rank decomposition (see Fig. 1). This innovative design enables *Palu* to reduce memory while mitigating the runtime overhead of KV-Cache low-rank decomposition.

In designing an effective decomposition strategy for attention modules with multiple attention heads, we observed a clear trade-off between accuracy and reconstruction overhead. Decomposing the projection matrices across all attention heads together improves accuracy by preserving global information, but this approach significantly increases reconstruction costs. On the other hand, decomposing each head separately reduces reconstruction overhead but leads to a higher loss in accuracy. To address this, *Palu* introduces a medium-grained, group-head low-rank decomposition that strikes a balance between accuracy and reconstruction efficiency.

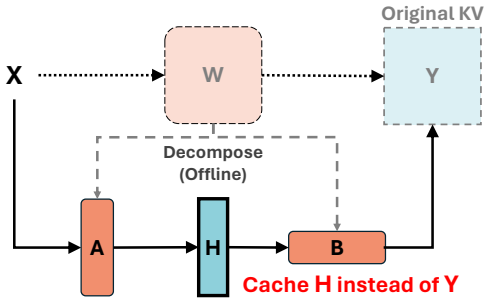


Figure 1: *Palu*'s *low-rank projection method* for KV-Cache reduction. A weight matrix **W** of linear projection is decomposed into two low-rank matrices. Input **X** is down-projected to latent representation **H**, which is cached. **Y** can be reconstructed from **H** using the up-projection matrix **B**.

For LLMs, each linear projection module has a different sensitivity to compression (Sharma et al., 2023; Yuan et al., 2023). To exploit the sensitivity and improve accuracy, we design an efficient *rank search algorithm* based on Fisher information (Ly et al., 2017; Liu et al., 2021). Our algorithm automatically assigns a higher rank for important matrices and lower ranks for less critical ones, boosting accuracy at the same overall KV-Cache compression rate.

In addition to its low-rank decomposition, *Palu* is compatible with quantization techniques. We found that low-rank decomposition can introduce severe outliers in the latent representation, which significantly hinders accurate low-bit quantization. Although the Hadamard transformation has been shown to be effective for outlier elimination in recent studies (Tseng et al., 2024; Ashkboos et al., 2024b; Liu et al., 2024a; Chiang et al., 2024), its integration often introduces computational overhead during runtime. However, *Palu*'s inherent matrix pair structure makes it highly compatible with this technique, allowing the transformation matrices to be seamlessly fused into the forward and backward matrices, effectively mitigating outliers without impacting runtime efficiency.

We evaluate *Palu* on widely used LLMs and benchmarks. Our experiments demonstrate that *Palu* maintains strong zero-shot accuracy and perplexity with up to 50% low-rank compression. Moreover, when combining low-rank compression with quantization, *Palu* achieves an impressive **over 91.25% compression (11.4× reduction)** and yields a *significantly lower perplexity of 1.19* than KVQuant (Hooper et al., 2024), a state-of-the-art KV-Cache quantization method, which only achieves an 87.5% compression rate.

For latency evaluation, under a 50% KV-Cache compression rate without quantization, *Palu* demonstrates up to *1.89× and 2.2× speedup* for RoPE-based and non-RoPE attention modules. When integrated with quantization, *Palu* achieves up to *2.91× and 6.17× acceleration* on RoPE-based and non-RoPE attention, respectively. These results underscore *Palu*'s ability to significantly reduce KV-Cache memory footprint while boosting inference efficiency for LLMs.

Our key contributions include:

- *Palu*, a new post-training KV-Cache compression framework that caches *low-rank latent representations* of Key and Value states.
- *Group-head low-rank decomposition (G-LRD)*, an optimization for balancing accuracy and reconstruction efficiency.
- An *automated rank search algorithm* for adaptively assigning ranks to each decomposed matrix, given a target compression rate.

- A co-designed *quantization compatibility optimization* that eliminates low-rank-induced outliers and imposes zero runtime overhead.

2 BACKGROUND

2.1 MULTI-HEAD ATTENTION MECHANISM

The multi-head attention (MHA) mechanism (Vaswani et al., 2017) is a core component of the transformer architecture. Given a new input token $\mathbf{x} \in \mathbb{R}^d$, an MHA with n heads projects the input into multiple queries, keys, and values using weight matrices $\mathbf{W}_i^q$, $\mathbf{W}_i^k$, and $\mathbf{W}_i^v$, respectively, for each head i, as shown by

$$\mathbf{q}_i = \mathbf{x}\mathbf{W}_i^q, \;\; \mathbf{k}_i = \mathbf{x}\mathbf{W}_i^k, \;\; \mathbf{v}_i = \mathbf{x}\mathbf{W}_i^v. \tag{1}$$

Here, $\mathbf{k}_i$ and $\mathbf{v}_i$ represent the key and value at time step t for head i. We can then compute the attention score for each head i and the corresponding attention output as

$$\mathbf{p}_{t,i} = \text{Softmax}\left(\frac{\mathbf{q}_i\mathbf{K}_i^T}{\sqrt{d_h}}\right), \;\; \mathbf{a}_i = \mathbf{p}_i\mathbf{V}_i, \tag{2}$$

where $\mathbf{K}_i$ and $\mathbf{V}_i$ denote the concatenation of current and all previous keys and values corresponding to the i-th head. The final MHA output is obtained by concatenating the outputs of all heads and then applying the out-projection layer $\mathbf{W}_o$, as shown by

$$\text{MHA}(\mathbf{x}) = \sum_{i=1}^{h} \mathbf{a}_i\mathbf{W}_i^o = \sum_{i=1}^{h} (\mathbf{p}_i\mathbf{V}_i)\mathbf{W}_i^o, \tag{3}$$

where $\mathbf{W}_i^o \in \mathbb{R}^{d_h \times d}$ represents the submatrices of the out-projection matrix for each head i.

2.2 SINGULAR VALUE DECOMPOSITION (SVD)

SVD (Jolliffe & Cadima, 2016) is a commonly used technique for computing the low-rank approximation for a given matrix. We now introduce our specific use of SVD for *Palu*'s default low-rank decomposition method.

Given a weight matrix $\mathbf{W} \in \mathbb{R}^{m \times n}$, SVD decomposes $\mathbf{W}$ into three matrices: $\mathbf{W} = \mathbf{U}\mathbf{\Sigma}\mathbf{V}^T$. Here, $\mathbf{U}$ and $\mathbf{V}$ are orthogonal matrices containing the left and right singular vectors, respectively. The matrix $\mathbf{\Sigma}$ is a diagonal matrix that consists of singular values. We describe the decomposition as

$$\mathbf{W} \approx \mathbf{A}\mathbf{B}, \;\; \mathbf{A} = \mathbf{U}_r\sqrt{\mathbf{\Sigma}_r}, \;\; \mathbf{B} = \sqrt{\mathbf{\Sigma}_r}\mathbf{V}_r^T,$$

where $\mathbf{A} \in \mathbb{R}^{m \times r}$, $\mathbf{B} \in \mathbb{R}^{r \times n}$, $\mathbf{\Sigma}_r \in \mathbb{R}^{r \times r}$. $\mathbf{\Sigma}_r$ is a diagonal matrix containing the largest r singular values, and $\mathbf{U}_r$, $\mathbf{V}_r^T$ are corresponding singular vectors truncated from $\mathbf{U}$ and $\mathbf{V}^T$. This truncation and subsequent matrix formation let us approximate weight matrix $\mathbf{W}$ with two low-rank matrices $\mathbf{A}$ and $\mathbf{B}$, thereby reducing the storage by $\frac{mr+rn}{mn}$.

3 THE PALU FRAMEWORK

3.1 COMPRESSING THE KV-CACHE VIA LOW-RANK PROJECTION

A naïve approach to compress the KV-Cache with low-rank projection is to apply SVD directly on the KV-Cache and store the top-r singular vectors. However, this approach poses significant computational overhead during runtime that makes it impractical for deployments (see Appendix I).

To apply low-rank projection more efficiently than directly decomposing the KV-Cache during runtime, *Palu* uses SVD to decompose the Key and Value projection matrices. This approach is based on the observation that low-rank decomposition rewrites the linear projection layer from $\mathbf{y} = \mathbf{x}\mathbf{W}$ into $\mathbf{y} = \mathbf{x}\mathbf{A}\mathbf{B}$. Here, $\mathbf{A} \in \mathbb{R}^{d \times r}$ is the low-rank projection matrix, and $\mathbf{B} \in \mathbb{R}^{r \times d}$ is the reconstruction matrix derived by SVD. The forward process first *down-projects* the input token $\mathbf{x} \in \mathbb{R}^d$ into a low-dimensional latent space $\mathbf{h} \in \mathbb{R}^r$ and then *up-projects* it back to the original space:

$$\mathbf{h} = \mathbf{A}\mathbf{x}, \quad \mathbf{y} = \mathbf{B}\mathbf{h} \tag{4}$$

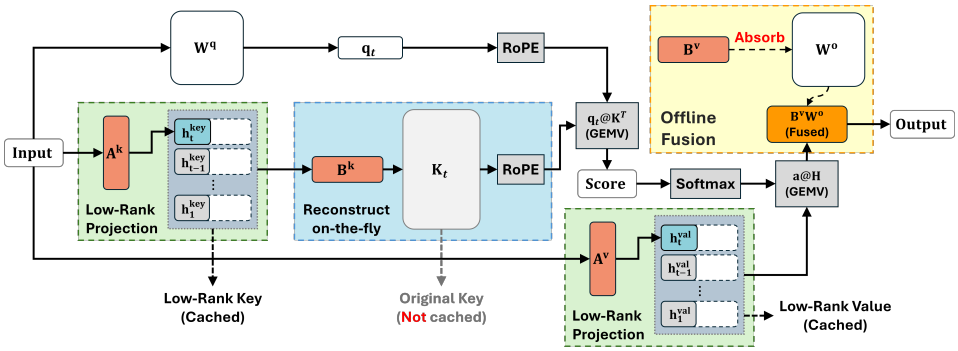


Figure 2: *Palu* uses low-rank decomposition ($\mathbf{W} \approx \mathbf{AB}$) to project the key (or value) to a lower-dimensional latent representation ($\mathbf{h}$), thereby reducing the size of the KV-Cache. The original key ($\mathbf{K}_t$) is reconstructed on-the-fly with $\mathbf{B}^k$, and $\mathbf{B}^v$ is fused into $\mathbf{W}^o$ to avoid reconstruction overhead. The fusion also reduces the computational burden for output projection.

This two-step process lets *Palu* (1) store the lower dimension latent representation instead of the origin key and value states, and (2) reconstruct them during decoding.

3.1.1 Integration with the Attention Mechanism and Offline Matrix Fusion

We now describe how *Palu* decomposes the key and value linear layers for the attention mechanism. For each attention head i, *Palu* applies SVD and maps the key-projection matrix $\mathbf{W}_i^k$ and value-projection matrix $\mathbf{W}_i^v$ into $\mathbf{A}_i^k\mathbf{B}_i^k$ and $\mathbf{A}_i^v\mathbf{B}_i^v$.

Based on the formula of attention output in Eq. 2, *Palu* absorbs the reconstruction matrix $\mathbf{B}_i^v$ into the output projection matrix $\mathbf{W}_i^o$ offline:

$$\mathbf{a}_i\mathbf{W}_i^o = (\mathbf{p}_i\mathbf{V}_i)\mathbf{W}_i^o = (\mathbf{p}_i\mathbf{H}_i^v\mathbf{B}_i^v)\mathbf{W}_i^o = \mathbf{p}_i\mathbf{H}_i^v(\mathbf{B}_i^v\mathbf{W}_i^o) \tag{5}$$

Such fusion lets *Palu* skip the explicit reconstruction of the full value vectors, reduce the number of matrix multiplications, and improve efficiency. A similar approach applies for calculating attention scores. Matrix $\mathbf{B}_i^k$ can be fused into the query projection matrix $\mathbf{W}_i^q$ offline, as shown by

$$\mathbf{q}_i\mathbf{K}_i^T = \mathbf{q}_i(\mathbf{H}_i^k\mathbf{B}_i^k)^T = \mathbf{x}_t\mathbf{W}_i^q(\mathbf{B}_i^k)^T(\mathbf{H}_i^k)^T = \mathbf{x}_t\Big(\mathbf{W}_i^q(\mathbf{B}_i^k)^T\Big)(\mathbf{H}_i^k)^T. \tag{6}$$

Here, $\mathbf{B}_i^k \in \mathbb{R}^{r\times d_h}$ and $\mathbf{W}_i^q \in \mathbb{R}^{d\times d_h}$, so the fused matrix $(\mathbf{W}_i^q(\mathbf{B}_i^k)^T)$ has size $\mathbb{R}^{d\times r}$. This fusion boosts computational efficiency by reducing the matrix dimension during attention score calculation.

3.1.2 Compability with Positional Embedding

Recent LLMs, such as the Llama family, apply Rotary Positional Embedding (*i.e.,* RoPE (Su et al., 2021)) onto the Query and Key states prior to their multiplication. The non-linear nature of these positional embeddings prevents the matrix fusion of attention scores, as outlined in Eq. 6. To address this, *Palu* dynamically reconstructs the keys from latent representations during decoding. We enhance reconstruction efficiency with a custom-designed GPU kernel, detailed in Sec. 4.1 and further described in Appendix B.

Note that for some positional embedding methods, such as ALiBi (Press et al., 2022), or new attention mechanisms, such as MLA (DeepSeek-AI et al., 2024), positional embedding is not directly applied to the Key states. Consequently, the fusion described in Eq. 6 remains valid. For these non-RoPE attention modules, *Palu* achieves greater speedup compared to RoPE-based attention, as their reconstruction can be avoided with matrix fusion. A detailed workflow of *Palu* in the context of Llama's RoPE-based attention is illustrated in Fig. 2.

3.2 Decomposition Granularity

3.2.1 Multi-Head Low-Rank Decomposition

We name the per-head decomposition scheme in Sec. 3.1.1 as *multi-head low-rank decomposition (M-LRD)*. We found M-LRD often causes a non-negligible accuracy degradation (discussed further in Sec. 4.2), possibly because SVD fails to capture the common information shared across heads. Therefore, alternative approaches are needed to preserve model accuracy.

3.2.2 Joint-Head Low-Rank Decomposition

An alternative approach is to jointly decompose weight matrices for all heads. By considering the combined weight matrix $\mathbf{W}_{\text{joint}} = [\mathbf{W}_1, \mathbf{W}_2, \ldots, \mathbf{W}_n] \in \mathbb{R}^{d\times(d_h\cdot n_h)}$, we can perform a single low-rank decomposition $\mathbf{W}_{\text{joint}} \approx \mathbf{A}_{\text{joint}}\mathbf{B}_{\text{joint}}$, where $\mathbf{A}_{\text{joint}} \in \mathbb{R}^{d\times r_{\text{joint}}}$ and $\mathbf{B}_{\text{joint}} \in \mathbb{R}^{r_{\text{joint}}\times(d_h\cdot n_h)}$. We call this scheme *joint-head low-rank decomposition (J-LRD)*.

J-LRD has the advantage of preserving the common principal components shared among different heads. This occurs because SVD is particularly effective at capturing the dominant components when applied to a larger, combined matrix, resulting in a more accurate approximation.

For J-LRD, the joint latent representation shared among all heads can be computed with $\mathbf{h}_{\text{joint}} = \mathbf{x}\mathbf{A}_{\text{joint}}$. During decoding, the original states for each head can be reconstructed via

$$[\mathbf{y}_1, \ldots, \mathbf{y}_n] = \mathbf{h}_{\text{joint}}\mathbf{B}_{\text{joint}}.$$

High Inference Overhead. Despite better preserving model accuracy, J-LRD introduces *significant computational and memory overhead* during decoding. Specifically, the total number of floating point operations (FLOPs) to reconstruct the Key or Value state of all heads now becomes $L \cdot r_{\text{joint}} \cdot d_h \cdot n$. Assuming the same size as the total low-rank latent representations (*i.e.*, $r_{\text{joint}} = \sum_{i=1}^{n} r_i$), the total reconstruction cost is n times higher than M-LRD, whose total FLOPs is $L \cdot r_i \cdot d_h \cdot n$. When considering the matrix fusion in Sec. 3.1.1, the fused matrix of J-LRD has a size of $r_{joint} \cdot d \cdot n$, which is also n times larger than M-LRD, leading to substantial higher memory consumption.

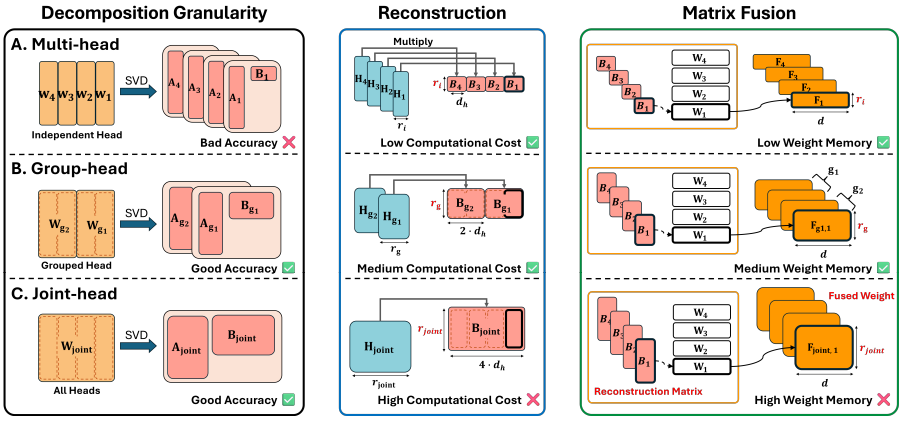


Figure 3: Performing decomposition at different granularities. Jointly decomposing multiple heads can achieve higher accuracy. Assuming the same total size of the latent representations (*i.e.*, $4 \cdot r_i = 2 \cdot r_g = r_{\text{joint}}$), the FLOPs for reconstruction overhead in joint-head decomposition schemes are 4 times larger than those in multi-head ones.

3.2.3 Group-Head Low-Rank Decomposition

To balance the trade-off between accuracy and reconstruction cost, we propose *group-head low-rank decomposition* (G-LRD). G-LRD decomposes the matrices for a group of heads together. With combined weight matrices, it captures shared information within each group while limiting computational overhead and preserving accuracy.

To illustrate the G-LRD process, consider the weight matrices for a group of s heads, $\mathbf{W}_{g_j} = \left[\mathbf{W}_{j,1} \dots \mathbf{W}_{j,s}\right]$, where $\mathbf{W}_{g_j} \in \mathbb{R}^{d \times (d_h \cdot s)}$. We low-rank decompose $\mathbf{W}_{g_j} \approx \mathbf{A}_{g_j}\mathbf{B}_{g_j}$, where $\mathbf{A}_{g_j} \in \mathbb{R}^{d \times r_g}$ and $\mathbf{B}_{g_j} \in \mathbb{R}^{r_g \times (d_h \cdot s)}$. The latent representation shared among attention heads in the same group can be computed as $\mathbf{h}_{\mathrm{g}_j} = \mathbf{x}\mathbf{U}_{\mathrm{g}_j}$. During decoding, the original key or value for each head can be reconstructed via

$$[\mathbf{y}_{j,1} \dots \mathbf{y}_{j,s}] = \mathbf{h}_{\mathrm{g}_j}\mathbf{B}_{\mathrm{g}_j}.$$

The FLOPs for reconstructing the keys and values for all heads in G-LRD is $L \cdot r_g \cdot d_h \cdot n$. Comparing the cost to J-LRD and assuming the same total rank size ($r_g \cdot n_g = r_{\text{joint}}$), G-LRD reduces the reconstruction cost by n_g. Similarly, G-LRD also reduces the fused matrix size by n_g. To sum up, G-LRD offers a middle ground between computation overhead and approximation accuracy. We illustrate M-LRD, J-LRD and G-LRD in Fig. 3. Please refer to Appendix C for further discussions on the costs of different decomposition granularities.

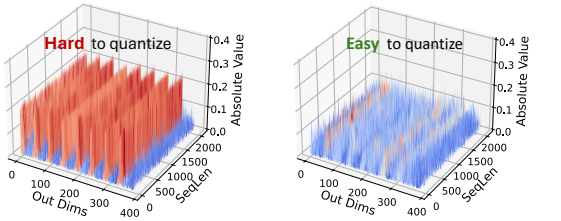
3.3 Automatic Rank Allocation

To allocate an ideal rank size to the decomposition target, it is crucial to accurately estimate the importance of the target matrix (*e.g.,* grouped weights). In *Palu*, we identify **Fisher information** (Ly et al., 2017; Liu et al., 2021) as an accurate approximator since it can quantify the amount of information for each parameter. We then employ the sum of Fisher information to estimate the importance of the weight matrix of each linear layer (Abdelfattah et al., 2021).

Assuming that the compression sensitivity is proportional to Fisher information, we determine the rank for each weight matrix by computing the ratio of its Fisher information to the total Fisher information across all decomposition targets. We use this ratio to allocate the compression rate (*i.e.,* rank level r), ensuring that more important layers retain higher rank levels. For a detailed ablation study on our Automatic Rank Allocation, please refer to Appendix G.3.

3.4 Quantization Compatibility

We integrate quantization into *Palu* to compress the KV-Cache further. We observe that low-rank compressed latent representations have severe outliers, which limit quantization applicability in *Palu*. Unlike natural outliers described in previous KV-Cache quantization literature (Liu et al., 2024b; Hooper et al., 2024), these outliers are induced by SVD-based low-rank factorization.



(a) Low-Rank Key Cache (b) Low-Rank Key Cache (with Hadamard)

Figure 4: Activation distribution of the low-rank key caches at the 4th Llama-2 attention layer.

Fig. 4 (a) shows the distribution of low-rank compressed key states from a layer of Llama-2 with G-LRD. Repeating outlier patterns appear at the beginning of each decomposed group because SVD arranges larger eigenvalues in the initial rows or columns, resulting in rapidly descending values in the latent representation. This pattern stretches the data distribution and hurts quantization accuracy.

Inspired by recent LLM quantization literature (Ashkboos et al., 2024b; Tseng et al., 2024), we apply the Walsh-Hadamard transform (WHT, Fino & Algazi) to eliminate outliers (Fig. 4 (b)), enabling a high quantization accuracy. However, this transformation introduces an extra matrix multiplication with associated runtime overhead. Unlike earlier methods (Ashkboos et al., 2024b) that must apply online WHT when quantizing KV-Cache, we optimize this process by integrating the Hadamard matrix into low-rank decomposed weights with no additional compute overhead, as described by

$$\mathbf{W} \approx \mathbf{A}\mathbf{B} = (\mathbf{A}\mathbf{R})(\mathbf{R}^T\mathbf{B}) = \hat{\mathbf{A}}\hat{\mathbf{B}}, \tag{7}$$

where $\mathbf{R}$ is the Hadamard matrix. This optimization allows *Palu* to integrate the proposed low-rank compression technique with low-bit quantization. Our experiments show that, on top of the low-rank compression, our quantization method only *negligibly increases perplexity*, even at extreme levels such as *3-bit or 2-bit* with a simple per-token quantization scheme (see Sec. 4.3).

4 EXPERIMENTS

4.1 EXPERIMENTS SETUP

Models and Tasks. We evaluate *Palu* on four LLM families, Llama-2 (Touvron et al., 2023), Llama-3 (Dubey et al., 2024), Mistral (Jiang et al., 2023) and LongChat (Li et al., 2023). For accuracy evaluation, we measure perplexity on the WikiText-2 (Merity et al., 2016) and C4 (Raffel et al., 2020) datasets and use LM-Evaluation-Harness (Gao et al., 2023) to measure zero-shot accuracy on six common sense tasks. We also evaluate long context accuracy on 16 tasks in LongBench (Bai et al., 2023). Unless specification, we refer to baseline as a model with non-compressed KV-Cache. See Appendix H for further details on the dataset and settings.

Compression Settings. We implemented *Palu* based on the Huggingface library (Wolf et al., 2020). Decomposition of the Key and Value projection layers was performed using the truncation-aware SVD method proposed by SVD-LLM (Wang et al., 2024). Unless otherwise specified, *Palu*'s results are G-LRD with a group size of 4 (gs-4), with equal rank size for each group. To calculate Fisher information in rank searching, we used 2048 random samples from Wikitext-2, each with a sequence length of 1024. For quantization integration in *Palu*, we use a simple per-token, asymmetric integer quantization. For evaluation on quantization results, we compare *Palu* to advanced KV-Cache quantization methods, including Atom (Zhao et al., 2023), KVQaunt (Hooper et al., 2024), and KIVI (Liu et al., 2024b). Refer to Sec. 5 for a brief summary of these methods.

GPU Kernels Implementation. To efficiently compute the attention score with RoPE in *Palu*, we implemented a customized kernel in Triton (Tillet et al., 2019). Our kernel fuses the key reconstruction, applying RoPE, and the final multiplication with query in a single kernel call, minimizing data movement (See Appendix B). For quantization integration, we implemented kernels in CUDA for attention output and non-RoPE attention score, where matrix fusion can be applied (refer to Sec. 3.1.1 and Fig. 2). Our low-precision kernel fuses the dequantization process and the follow-up multiplication with low-rank compressed keys or values, enabling efficient processing on quantized latent KV-Cache. When evaluating speedup with quantization, we compare to the non-compressed baseline and KIVI (Liu et al., 2024b), which we use their official code[1] in our experiments.

4.2 RESULTS WITH DIFFERENT DECOMPOSITION GRANULARITY

We evaluate perplexity and zero-shot accuracy of *Palu* with a **50% low-rank compression rate** using M-LRD, G-LRD, and J-LRD on Llama2-7B and Llama3-8B-Instruct, and present the results in Table 1.

Table 1: Perplexity and zero-shot accuracy of *Palu* at 50% compression rate.

Model	Method	Perplexity ↓		Zero-Shot Accuracy (%) ↑						
		Wiki2	C4	OBQA	Hella	PIQA	ARC-e	ARC-c	Wino	Avg.
Llama2-7B	Baseline	5.47	7.26	44.20	76.00	78.07	76.30	46.42	69.30	65.05
	J-LRD	5.62	7.75	45.40	75.57	77.48	75.97	45.31	69.22	64.82
	G-LRD	6.01	9.82	43.60	73.39	76.33	73.02	42.57	66.77	62.61
	M-LRD	6.75	12.01	39.60	65.35	74.76	67.17	35.24	64.64	57.79
Llama3-8B-Inst	Baseline	8.28	13.01	43.20	75.80	78.62	81.61	56.83	71.90	67.99
	J-LRD	9.12	15.90	43.40	73.20	76.50	79.63	51.96	72.45	66.19
	G-LRD	10.11	17.87	42.60	70.36	76.06	76.30	48.99	72.38	64.45
	M-LRD	12.38	23.02	38.80	63.04	73.67	69.78	42.58	62.51	58.40

Perplexity Evaluation. As Table 1 shows, for the Llama2-7B model, *Palu*'s M-LRD method fails to maintain a low perplexity at a 50% compression rate. In contrast, despite having a high recomputation cost, J-LRD significantly outperforms M-LRD and achieves a 5.62 perplexity on WikiText-2.

For G-LRD, which still maintains a low computation cost, yields a 6.01 perplexity on Wikitext-2, showing a great balance between model accuracy and compression overheads. The same trend is observed in the Llama-3-8B model as well. More results Llama-2-13B can be found in Appendix F.

[1]https://github.com/jy-yuan/KIVI

Zero-shot Evaluation Results. Similar to the perplexity evaluation, the J-LRD method demonstrates the best performance for the zero-shot accuracy on Llama-2-7B, with only a 0.23% average accuracy degradation. M-LRD method results in the lowest average performance, with a 7.26% drop in accuracy compared to the baseline. In comparison, G-LRD only has a 2.4% average accuracy decline, offering a sweet spot between model accuracy and compression overheads again.

4.3 Results of Quantization Integration

Table 2 showcases the impact of quantization on perplexity and KV-Cache size when combined with *Palu*. With 3-bit quantization, *Palu* incurs only a **slight 0.08 and 0.23 perplexity increase** at 30% and 50% low-rank compression rate. These demonstrate a minimal accuracy trade-off for significant compression gains compared to the 16-bit baseline.

Notably, at 2-bit quantization, *Palu* decisively outperforms the state-of-the-art KVQuant method, **reducing perplexity by 1.19 and 0.54**, while further slashing memory usage by 30% and 50%. These results establish *Palu* with quantization as a superior KV-Cache compression method.

Table 2: Quantization perplexity and KV-Cache size for Llama2-7B on WikiText-2. For perplexity, sequence length is 4096. KV-Cache size is demonstrated for 128K sequence length.

Method	Bit	PPL	KV-Cache Size (GB)	Comp. Rate
Baseline	16	5.12	64.0	-
Palu-30%	16	5.25	44.8	30%
Palu-50%	16	5.63	32.0	50%
Atom	3	6.15	12.6	80.32%
KVQuant	3	5.35	12.0	81.25%
Palu-30%	3	**5.33**	**8.4**	**86.87%**
Palu-50%	3	5.77	6.0	90.63%
Atom	2	117.88	8.6	86.56%
KVQuant	2	6.95	8.0	87.50%
Palu-30%	2	**5.76**	**5.6**	**91.25%**
Palu-50%	2	**6.41**	**4.0**	**93.75%**

4.4 Evaluation on Long Context Datasets

To access *Palu*'s ability for long-context scenarios, we evaluate baseline, KIVI and *Palu*'s accuracy on LongBench (Bai et al., 2023) Here, we evaluate the Mistral-7B and LongChat-7B models, which have up to 32K context length. We report the average score for each task type separately, as well as the overall average across all 16 tasks. The results are shown in Table 3. We report the accuracy of KIVI using the configuration with a group size of 32 and 128-element fp16 residual (Liu et al., 2024b).

As Table 3 indicates, we find that at a 50% low-rank compression level, *Palu* is relatively difficult to fully preserve accuracy. However, at a 30% compression level, *Palu* achieves only a minor average accuracy drop ($< 1\%$) compared to the baseline for both models.

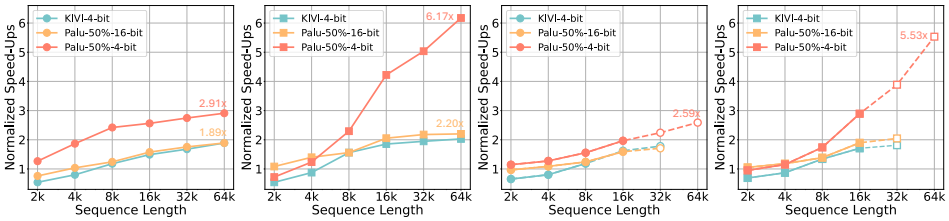
Furthermore, *Palu* can quantize the low-rank latent KV-Cache down to 3 bits, with less than 1% further accuracy degradation. Overall, *Palu* maintains a strong 40.77% and 34.33% average accuracy for Mistral-7B and LongChat-7B, with an impressive 7.59x compression ratio. Compared to KIVI (Liu et al., 2024b), *Palu* achieves a similar accuracy, while having an additional 30% compression rate from low-rank. Notably, *Palu* does not require the complex grouped quantization and mixed-precision techniques employed by KIVI, resulting in a high inference efficiency (see Sec. 4.5 for details).

Table 3: Experiment Results on LongBench: The average bit widths represent the total storage cost per element in the compressed KV-Cache, including the overhead of quantization parameters. These values are calculated for each approach, assuming a context length of 10K.

Model	Method	Avg. Bits	Comp. Ratio	Multi-QA	Single-QA	Summarization	Few-Shot	Code	Synthetic	Avg.
Mistral-7B-v0.2	Baseline	16	1.00x	29.63	36.43	28.10	66.71	54.16	44.87	42.54
	Palu-30%	16	1.43x	29.83	36.52	27.48	65.70	55.16	37.92	41.55
	Palu-50%	16	2.00x	26.92	35.33	26.01	64.04	44.54	16.88	36.23
	KIVI-2	3.16	5.05x	28.81	35.07	27.60	66.45	54.47	40.28	41.45
	Palu-30% (3 bits)	3	7.59x	29.48	36.40	27.20	65.73	53.19	34.74	40.77
	Palu-50% (3 bits)	3	10.6x	26.73	32.72	25.73	63.25	44.43	18.57	35.71
LongChat-7B-v1.5	Baseline	16	1.00x	23.95	31.12	26.74	63.80	56.91	15.25	36.32
	Palu-30%	16	1.43x	22.42	29.43	25.52	62.87	58.99	14.25	35.45
	Palu-50%	16	2.00x	22.61	25.33	22.73	60.12	43.52	6.84	30.82
	KIVI-2	3.16	5.06x	23.24	30.19	26.47	63.54	53.51	16.13	35.60
	Palu-30% (3 bits)	3	7.59x	23.12	29.21	25.04	61.99	54.38	11.25	34.33
	Palu-50% (3 bits)	3	10.6x	18.56	24.14	22.35	58.76	40.50	6.02	29.03

4.5 LATENCY EVALUATION

In this section, we provide latency and speedup evaluation, using Llama-2-7b as the base model. We measure decode latency on a single RTX 4090 GPU and compare *Palu* to the FP16 and KIVI-4-bit baselines. We evaluate *Palu*'s latency at a 50% compression rate, where we set compression rates for key and value to 75% and 25%, respectively. This allocation is based on our observations from the rank allocation results (see Appendix G.3 for details). For the FP16 baseline, we use the default implementation from HuggingFace. For KIVI, we use the CUDA kernels from its official repository. Due to the small memory capacity of RTX 4090 GPU, we adopt a 4-bit quantization (Frantar et al., 2024) for the weights of all linear layers. Our results are the average of 100 runs.



(a) Attention Module (w/ RoPE) (b) Attention Module (w/o RoPE) (c) End-to-End Model (w/ RoPE) (d) End-to-End Model (w/o RoPE)

Figure 5: Normalized speedup for both the attention module and end-to-end model decoding. Solid lines represent exact measurements, while dashed lines indicate the FP16 baselines are out of memory, and the speedups are compared to the estimated baseline's latency.

4.5.1 SPEEDUPS OF ATTENTION MODULE AND END-TO-END DECODING.

Attention module speedup. We compare latency against standard attention without compression or quantization and show the speedups of *Palu* and KIVI-4-bit in Fig. 5 (a) and (b) for RoPE-based and non-RoPE attention. For RoPE-based attention, we applied our online reconstruction kernel for key and employed offline fusion for value as described in Sec 3.1.2.

As shown in Fig. 5 (a), *Palu* has minimal to no speedup when the sequence length is short, e.g. 4K. However, as sequence length increases, *Palu* delivers substantial performance gains. At 64K input length, *Palu* achieves a **1.89× speedup** over the FP16 baseline when using low-rank projection alone. By further applying 4-bit quantization to the Value states, the **speedup rises to 2.91**× for the same 64K context length, owing to our optimized low-precision kernel and reduced memory loading times. This performance notably surpasses KIVI-4-bit, which only achieves a 1.89× speedup at 64K, hindered by the overheads of its fined-grained group quantization. Notably, for RoPE-based attention, *Palu*-4-bit does not quantize key, as our online reconstruction kernel only supports FP16 precision for now.

For non-RoPE attention, we apply matrix fusion to both the Key and Value states (Eq. 6), effectively eliminating all reconstruction overhead. At a 64K sequence length with a 50% compression rate, *Palu* achieves a **2.20× speedup over the FP16 baseline**. By further applying 4-bit quantization to both the Key and Value states, *Palu* boosts the speedup to **6.17×** for 64K input length. These results demonstrate that combining low-rank compression and quantization significantly enhances inference efficiency, particularly in long-context scenarios.

End-to-end speedup. We present the end-to-end speedups in Fig. 5 (c) and (d), measuring the decoding latency of generating the next token at various input lengths. Similar to the attention performance results, *Palu* shows minimal or no speedup for short sequences but delivers significant acceleration for longer sequences. Without quantization, *Palu* achieves up to **1.71× and 2.05× speedups** for RoPE-based and non-RoPE models, respectively. With a 50% compression rate, *Palu* runs up to 32K input length on an RTX 4090 GPU. By incorporating 4-bit quantization, *Palu* handles even longer sequences and delivers **2.59× and 5.53× end-to-end speedups** at a 64K sequence length. *Palu* integrated with quantization provides a substantial speed advantage over KIVI-4-bit, which only reaches 1.78× and 1.81× speedups at 32K sequence length for RoPE and non-RoPE scenarios, respectively, and is out-of-memory for longer sequences.

4.5.2 Kernel for RoPE-Based Attention Score

In this section, we evaluate the performance of our online reconstruction kernel for RoPE-based attention scores. We measure latency from the **pre-RoPE query vector** to **post-GEMV attention score**, and compare it with PyTorch's GEMV, which is used in the baseline attention (see Fig. 2).

We present speedups for group size 1, 4, and 32 at different sequence lengths in Fig. 6. For gs-32 (J-LRD), the highest accuracy decomposition, the high reconstruction cost causes a significant slowdown across all sequence lengths. For gs-1 (M-LRD), our kernel achieves up to a 3.56× speedup at sequence length 16K, showing strong performance when moderate accuracy loss is acceptable. For gs-4 (G-LRD), our kernel reaches up to 1.95× speedup. These results emphasize the need to explore various decomposition granularities for better accuracy and speed tradeoffs.

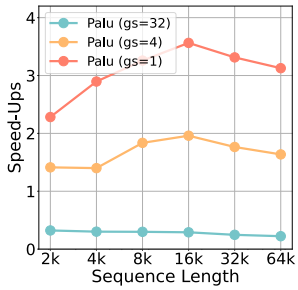


Figure 6: Speedup of *Palu*'s attention score kernel with online reconstruction.

We also observe that speedup decreases for sequence lengths beyond 16K due to rising reconstruction costs, shifting the online reconstruction from memory- to compute-bound. A potential optimization is to quantize the decomposed weight matrices further and leverage high-throughput, low-precision hardware (*e.g.,* INT4 Tensor Cores) for online reconstruction, which we leave for future work. Despite the speedup drop at longer lengths, *Palu*'s overall attention speedup increases with longer input, thanks to matrix fusion on the Value state and the reduced memory footprint.

5 Related Work

SVD for LLM Compression. Several works have explored using SVD to compress LLMs. An early approach (Noach & Goldberg, 2020) applied standard SVD to weight matrices, resulting in significant compression errors. FWSVD (Hsu et al., 2022) addressed this by using Fisher information to prioritize parameters, while ASVD (Yuan et al., 2023) considered activation outliers. SVD-LLM (Wang et al., 2024) further minimized compression loss for each singular value. Unlike these methods, which compress model weights, *Palu* focuses on reducing KV-Cache size.

KV-Cache Quantization. Quantization is a widely used technique for compressing KV-Cache. Atom (Zhao et al., 2023) applies simple per-token quantization, while WKVQuant (Yue et al., 2024) introduces a two-level scheme to enhance accuracy. KIVI (Liu et al., 2024b) uses per-channel and per-token quantization for Keys and Values, combined with fine-grained group quantization. KVQuant (Hooper et al., 2024) employs a similar setup but incorporates non-uniform quantization and sparse matrices to handle outliers. On top of these approaches, GEAR adds a low-rank matrix to compensate for quantization errors. In *Palu*, we leverage low-rank techniques to exploit hidden dimension redundancy and achieve outstanding compression through simple per-token quantization.

MLA. The recently released DeepSeek-V2 model (DeepSeek-AI et al., 2024) introduces the MLA mechanism, which reduces KV-Cache size by down-projecting Key and Value to a low-rank space and reconstructing them to full rank at runtime. Although MLA may seem similar to *Palu* at a high level, particularly with J-LRD, our design and derivation processes are fundamentally different. Unlike MLA, a new attention mechanism requiring pre-training, *Palu* is specifically designed for post-training integration. *Palu* focuses on converting existing models with MHA or GQA to support low-rank compressed KV-Cache, preserving high accuracy while enhancing inference efficiency.

6 Conclusion

We introduce *Palu*, a novel KV-Cache compression framework that decomposes linear projection weight matrices and caches the compressed latent representations. We propose various optimizations, including group-head low-rank decomposition, automatic rank allocation algorithm, quantization compatibility enhancement, and customized kernels with operator fusion. With these optimizations, *Palu* can maintain accuracy while achieving significant memory reduction and high inference speedup. Experiments show that, with 50% low-rank compression and 4-bit quantization, *Palu* accelerates RoPE-based attention module by up to 2.91× and delivers up to 2.59× end-to-end speedup for the same RoPE-based model, while preserving strong accuracy on various benchmarks.

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APPENDIX

A QUANTIZATION BASICS

Quantization techniques use discrete low-bit values to approximate high-precision floating points. The general asymmetric uniform quantization function is defined as:

$$\overline{\mathbf{X}} = \text{clamp}\left(\left\lfloor \frac{\mathbf{X}}{s} \right\rceil + z, 0, 2^B - 1\right), \tag{8}$$

where $\overline{\mathbf{X}}$ denotes the approximated tensor with low-bit representations (i.e., 4-bit integers), $\mathbf{X}$ is the floating-point tensor, $s = \frac{\mathbf{X}_{\text{max}} - \mathbf{X}_{\text{min}}}{2^B - 1}$ is the scaling factor, and $z = \left\lfloor \frac{-\mathbf{X}_{\text{min}}}{s} \right\rceil$ is a zero-point. The $\lfloor \cdot \rceil$ is the rounding operation.

B KERNEL IMPLEMENTATION DETAILS

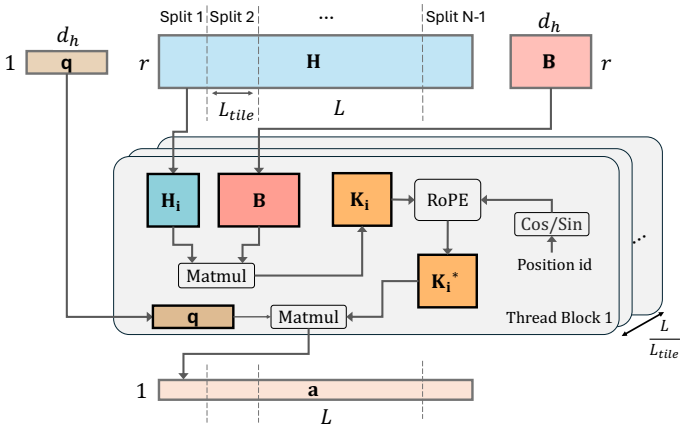


Figure 7: Illustration of our fused GPU kernel for computing attention scores with online reconstruction. In this figure, $\mathbf{q}$ represents the query vector, $\mathbf{H}$ denotes the low-rank compressed key states, and $\mathbf{B}$ stands for the reconstruction matrices.

Kernel for attention score calculation with reconstruction. The central idea of *Palu* is to leverage low-rank latent representations to accelerate the attention mechanism by reducing data transfer overhead. Instead of working directly with the full-sized key matrix, we store and transfer a compressed low-rank latent representation, denoted as $\mathbf{H} \in \mathbb{R}^{L \times r}$. During computation, our custom GPU kernel performs an on-the-fly reconstruction using a reconstruction matrix $\mathbf{B} \in \mathbb{R}^{r \times d_h}$, producing a restored key matrix $\mathbf{K} \in \mathbb{R}^{L \times d_h}$, where L is the sequence length, d_h is the hidden dimension, and r denote the remaining rank after performing low-rank projection. The query vector, represented as $\mathbf{q} \in \mathbb{R}^{1 \times d_h}$, then multiplies with the reconstructed keys to obtain the attention scores.

To efficiently leverage parallelism, we perform tiling along the sequence length dimension L. Specifically, we split the sequence into smaller tiles of size L_{tile}, assigning each tile to a dedicated thread block. Each thread block independently reconstructs a submatrix $\mathbf{H}_i \in \mathbb{R}^{L_{\text{tile}} \times d_h}$ from the low-rank latent representation $\mathbf{H}$, then applies the positional embedding using RoPE, and finally performs the matrix-vector multiplication between $\mathbf{q}$ and $\mathbf{H}_i$ to produce partial attention scores. This design ensures that all intermediate computations, from reconstruction to embedding and final multiplication, remain entirely in on-chip memory (*i.e.,* share memory), thus minimizing high-latency memory access and taking full advantage of the GPU's parallel processing capabilities to achieve significant speedups.

C DISCUSSION REGARDING MEMORY USAGE

In this work, the experimental results focus on the compression rate of the KV-Cache as a key metric. However, it is crucial to consider overall memory savings as a more significant factor. For instance, as demonstrated in Sec. 2.2, a typical compression rate of 30% can lead to an increase in weight size by approximately 40%. This increase is calculated under the assumption that $m = n$ and $r = 0.7n$, resulting in the equation $\frac{mr+nr}{mn} = 1.4$. Such an increase indicates substantial extra memory usage.

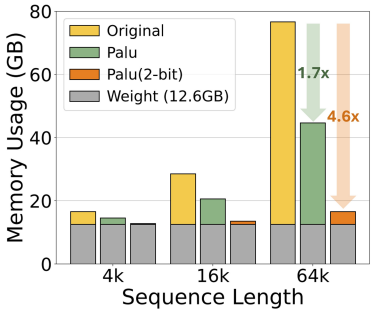
This issue primarily arises in J-LRD decomposition schemes, where the projections of all heads are decomposed jointly. In contrast, our M-LRD decomposition schemes and optimized G-LRD schemes involve non-square target matrices. For example, in the G-LRD scheme with a group size of 4, the target matrix is formed by concatenating the original projection matrices of each attention head in the group. In the Llama-2-7b model, with an embedding dimension of 4096 and head dimensions of 128, each projection matrix is 4096x128, resulting in a concatenated matrix of size 4096x512. In this case, the dimensions should be considered as $m = 8n$. Applying the referenced equation $\frac{mr+nr}{mn}$ with $r = 0.7n$, we find that $\frac{mr+nr}{mn} = 0.7875$, indicating no additional storage cost and, in fact, achieving an additional 21.25% memory savings.

Furthermore, it is important to highlight that the weights associated with the K and V projections account for only 2 out of 7 linear layers within transformer blocks, comprising merely 16% of the parameters in Llama-2-7b models. This limits the overall impact on memory usage. Thus, while J-LRD may incur overhead, the M-LRD and G-LRD schemes provide efficient alternatives that do not lead to increased memory usage, making them viable options for practical applications.

D OVERALL MEMORY REDUCTION

In Fig. 8, we show the total memory usage, including model weights and KV-Cache under different sequence lengths. We observe that KV-Cache quickly becomes the memory bottleneck as sequence length grows. At a sequence length of 64k, the KV-Cache constitutes 78% of the total memory consumption. With 50% low-rank compression, *Palu* effectively reduces memory usage by 1.7×, and when combined with 2-bit quantization, it further decreases total memory usage by 4.6×.

Figure 8: Total memory usage for various sequence lengths in Llama-2-7B. low-rank compression is at 50% for *Palu*.



E INTEGRATING *Palu* WITH LORA FINETUNE

LoRA (Hu et al., 2022) has become one of the most widely used efficient fine-tuning techniques for adapting models to particular tasks or domains with limited data. It has also been applied with LLM compression approaches (Wang et al., 2024; Ma et al., 2023) as a post-compression recovery technique to recover information loss after compression. In *Palu*, LoRA is also applicable to boost the accuracy further.

Table 4: Evaluation integrating LoRA with Palu on Llama2-7B.

Comp. Rate	Method	Zero-Shot Accuracy (%) ↑							
		OBQA	HellaSwag	PIQA	ARC-e	ARC-c	WinoGrande	Avg.	Diff.
Rate = 0%	baseline	44.20	76.00	78.07	76.30	46.42	69.30	65.05	-
Rate = 50% w/o LoRA	J-LRD	45.40	75.57	77.48	75.97	45.31	69.22	64.83	-0.22
	G-LRD	43.60	73.39	76.33	73.02	42.57	66.77	62.61	-2.44
	M-LRD	39.60	65.35	74.76	67.17	35.24	64.64	57.79	-7.26
Rate = 50% w/ LoRA	J-LRD	44.20	74.09	78.51	77.27	48.81	71.03	65.65	+0.60
	G-LRD	43.40	73.08	78.56	75.72	47.10	69.85	64.62	-0.43
	M-LRD	41.80	70.78	78.02	73.86	43.86	69.22	62.92	-2.12

Table 5: Perplexity and zero-shot accuracy of *Palu*, with different decomposition strategies at 50%

Model	Method	Perplexity ↓		Zero-Shot Accuracy (%) ↑						
		Wiki2	C4	OBQA	Hella	PIQA	ARC-e	ARC-c	Wino	Avg.
Llama2-13B	Baseline	4.88	6.70	45.20	79.39	79.11	79.42	49.06	72.38	67.43
	J-LRD	4.97	6.92	46.40	79.48	78.62	79.29	49.91	70.56	67.38
	G-LRD	5.31	7.76	45.60	77.29	77.42	76.05	45.99	72.45	65.80
	M-LRD	5.65	8.34	43.20	74.34	77.53	75.76	45.39	68.98	64.20

To integrate LoRA with *Palu*, we introduce additional low-rank matrices $\mathbf{A}'_r \in \mathbb{R}^{d\times r'}$ and $\mathbf{B}'_r \in \mathbb{R}^{r'\times d}$ to refine the original low-rank projection as below:

$$\mathbf{h} = \mathbf{A}\mathbf{x} + \mathbf{A}_{\mathbf{r}'}\mathbf{B}_{\mathbf{r}'}\mathbf{x} \tag{9}$$

Here, $\mathbf{A}$ will be fixed parameters derived from low-rank decomposition from pre-trained weights of linear layers, while $\mathbf{A}'_r$ and $\mathbf{B}'_r$ are trainable parameters to capture the task-specific nuances and recovers the information lost during the compression.

Setup. Following Ashkboos et al. 2024a, we sample 8k samples from the Alpaca training dataset as a fine-tuning dataset and apply LoRA with rank $r' = 32$ and $\alpha = 32$. All other hyper-parameters are aligned with Ashkboos et al. (2024a), except for the learning rate $2e-4$, and the use of a cosine learning rate scheduler.

Experiment Results. We present the experiment results with LoRA in Table 4. Following Ashkboos et al. 2024a With LoRA incorporated, J-LRD continues to show minimal performance degradation with an average drop of 1.00%. G-LRD (gs=4) and M-LRD show improved results compared to their non-LoRA counterparts, with average drops of 2.01% and 5.14%, respectively. Notably, with LoRA integration, G-LRD shows only a 1.03% accuracy difference compared to J-LRD.

F More Results on Zero-shot Accuracy

Following up Sec. 4.2, we further report the perplexity and zero-shot evaluation results of *Palu* on the Llama-2-13B at 50% compression rate. As shown in Table. 5, we observe that *Palu* achieve competitive accuracy drops around 3% or less across different using either J-LRD, G-LRD, or M-LRD. Thus, the users may adopt M-LRD first to optimize the efficiency further.

G Ablation Study

G.1 Influence of Different Group Size

Since our proposed G-LRD method allows for balancing performance and efficiency by adjusting the group size, we conducted an ablation study on group size. As seen in Table 6, as the group size increases, the amount of shared information also increases, leading to improved performance.

Table 6: Ablation study of low-rank decomposition group size on perplexity for the Llama2-7B model at a 50% compression rate using Wikitext-2.

Method	Group Size	Perplexity
Baseline	-	5.47
J-LRD	32	5.62
G-LRD	16	5.74
	8	5.88
	4	6.01
	2	6.42
M-LRD	1	6.81

G.2 Influence of Walsh-Hadamard Transform

We conduct the ablation study to profile the benefits of applying the Walsh-Hadamard Transform (WHT). Experiment results are reported at Table 7. On the 3-bit quantization level, we observe that the Hadamard Transform only brings a slight amount of perplexity. However, when we quantize the low-rank representation more extremely (*i.e.,* 2-bit), we can observe a notable 4.17 perplexity enhancements. It's worth re-emphasizing that Hadamard Transform will not bring extra overhead during inference, as *Palu* optimizes the WHT process via offline preprocessing. The reader may refer to Sec. 3.4 for more details.

G.3 Automatic Rank Allocation vs. Uniform Rank Allocation

Table 8 presents the ablation study on the impact of different rank allocation schemes on the model's accuracy. Applying rank searching results in a notable performance improvement. For instance, at a compression rate of 50%, there is a significant reduction in perplexity by 2.18. Fig. 9 visualizes the rank allocation across different transformer blocks for key and value projection layers. The results clearly demonstrate a non-uniform allocation result. Specifically, we observe that the value is generally allocated a higher rank than the key. Additionally, the first half of the layers are assigned higher ranks, indicating their greater importance in preserving model performance. This visualization underscores the effectiveness of our rank search algorithm in identifying and allocating appropriate ranks to different components, thereby optimizing the balance between compression and accuracy.

Table 7: Ablation Study on different quantization settings for quantizing low-rank latent representations. Same as Sec. 4.3, we use the WikiText-2 with sequence length set to 4096 as the evaluation benchmark.

Method	Wikitext-2 PPL ↓
Llama2-7B	5.12
Palu-30% (FP16)	5.25
+ 3-bits w/o Hadamard	5.52
+ 3-bits w Hadamard	5.33 (0.19↓)
+ 2-bits w/o Hadamard	9.48
+ 2-bits w Hadamard	5.77 (3.71↓)
Palu-50% (FP16)	5.63
+ 3-bits w/o Hadamard	5.99
+ 3-bits w Hadamard	5.77 (0.22↓)
+ 2-bits w/o Hadamard	10.58
+ 2-bits w Hadamard	6.41 (4.17↓)

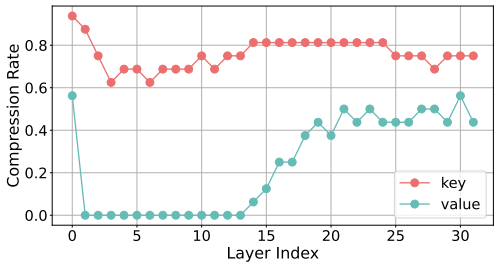


Figure 9: Visualization of layer-wise low-rank compression rate on Llama-2-7B with 50% of overall compression rate. Here, compression rates (*i.e.,* rank) are allocated using the proposed Fisher Information-based automated rank allocation algorithm.

Table 8: Ablation study on w/ and w/o rank search. We use Llama2-7b and Wikitext-2 with sequence length 2048 as the benchmark.

	Rate=30%	Rate=50%	Rate=70%
Uniform	6.34	7.36	10.77
Automatic (ours)	5.62 (0.72↓)	6.02 (1.36↓)	8.59 (2.18↓)

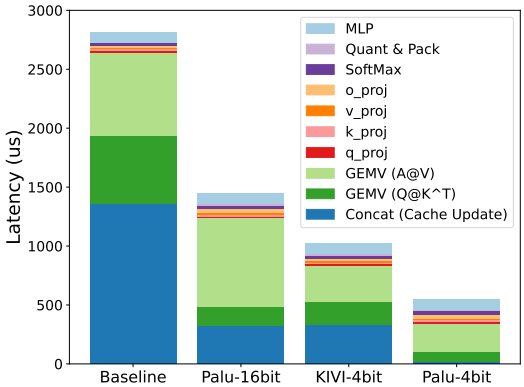


Figure 10: Transformer block w/o RoPE latency breakdown. Latency is measured on an RTX 4090 GPU for 64k sequence length, and the averaged results over 100 runs are reported.

G.4 Attention Module Latency Profiling

The performance analysis of the attention module across four configurations—Baseline, Palu-16bit, KIVI-4bit, and Palu-4bit—reveals significant variations in latency distribution. The Baseline configuration incurs the highest total latency, with substantial contributions from the concatenation operation (**1360 µs**) and the matrix multiplications for attention output ($\mathbf{aV}$: **700 µs**) and attention score calculation ($\mathbf{qK^T}$: **580 µs**).

In the Palu-16bit configuration, there are notable reductions in the concatenation latency, down to **325 µs**, and in the attention score calculation ($\mathbf{q}(\mathbf{H}^k\mathbf{B}^k) \approx \mathbf{qK^T}$) to **160 µs**. However, this configuration introduces a slight increase in the output projection latency ($\mathbf{o}_{\text{proj}}$, **35 µs** vs. **15 µs** in Baseline).

The KIVI-4bit implementation offers a balanced improvement, reducing the matrix multiplication latency for attention output ($\mathbf{aV}$) to **305 µs** and the concatenation operation to **330 µs**, while slightly increasing the time for attention score calculation ($\mathbf{qK^T}$) to **195 µs** compared to Palu-16bit.

The Palu-4bit configuration delivers the most dramatic efficiency gains, especially in the concatenation step (down to **20 µs**), attention score calculation ($\mathbf{qK^T}$: **80 µs**), and attention output ($\mathbf{aV}$: **240 µs**).

Overall, Palu-4bit exhibits the greatest latency reductions, particularly in key attention operations. Compared to the Baseline, the total latency across the concatenation, attention score calculation, and attention output steps drops from **2640 µs** to just **340 µs**, representing an approximate **87%** reduction. This underscores Palu-4bit's potential for optimizing attention mechanisms, particularly in scenarios involving long sequence lengths.

H EXPERIMENT DETAILS

H.1 ZERO-SHOT EVALUATION DETAILS

We selected six zero-shot tasks from the LM-eval benchmark to evaluate *Palu*:

- OpenBookQA (accuracy, Mihaylov et al.)
- HellaSwag (acc_norm, Zellers et al.)
- PIQA (accuracy, Bisk et al.)
- ARC-Easy (accuracy, Clark et al.)
- ARC-Challenge (acc_norm, Clark et al.)
- WinoGrande (accuracy, Sakaguchi et al.)

We report accuracy for WinoGrande, PIQA, and ARC-Easy, and accuracy normalized by sequence length (acc_norm) for HellaSwag and ARC-Challenge.

H.2 LONGBENCH EVALUATION DETAILS

For the LongBench evaluation in this manuscript, we conducted tests on all available English tasks. These comprise sixteen tasks categorized into six subgroups, ensuring a comprehensive evaluation of *Palu*. The tasks and their corresponding metrics are detailed below:

- Single-Document QA:
  - Qasper (F1 score, Dasigi et al.)
  - NarrativeQA (F1 score)
  - MultiFieldQA-en (F1 score)
- Multi-Document QA:
  - HotpotQA (F1 score, Dasigi et al.)
  - 2WikiMultihopQA (F1 score)
  - MuSiQue (F1 score)
- Summarization:
  - QMSum (ROUGE score, Zhong et al.)
  - MultiNews (ROUGE score, Fabbri et al.)
  - GovReport (ROUGE score)
- Few-shot Learning:
  - TREC (classification score, Li & Roth)
  - TriviaQA (F1 score, Joshi et al.)
  - SAMSum (ROUGE score, Gliwa et al.)
- Code Completion:
  - LCC (similarity score, Guo et al.)
  - RepoBench-P (similarity score, Liu et al.)
- Synthetic:
  - PassageCount (Accuracy)
  - PassageRetrevial (Accuracy)

During the evaluation, we set the maximum sequence length to 31500 for both the Mistral and LongChat model.

I Discussion of Directly Performing SVD on KV-Cache During Runtime

Seqlen	32k	64k	128k
Decoder Block (fp16)	0.231s	0.65s	1.93s
SVD	9.24s	9.90s	11.44s

Table 9: Latency comparison between performing SVD on the KV-Cache and a single forward pass through the transformer decoder block, using the model configuration of Llama-2-7B

As discussed at the beginning of Sec. 3.1, a straightforward approach to compress the KV-Cache with low-rank projections is to apply Singular Value Decomposition (SVD) directly to the KV-Cache. To evaluate its feasibility, we compare the latency required for performing SVD to the time taken for a forward pass through a decoder block, as illustrated in Tab.9. The results clearly demonstrate that performing SVD on the fly introduces significant computational overhead. Specifically, runtime SVD is approximately 5–10$\times$ slower than a single forward pass of the decoder block.

Given these findings, we adopt static weight decomposition techniques and modify the caching mechanism to store the lower-dimensional latent representations, thereby reducing the memory footprint while avoiding the runtime costs associated with on-the-fly SVD.

J More Related Work

Token Eviction. One prominent direction for reducing the memory footprint of KV-Cache is KV-Cache eviction Adnan et al. (2024); Ge et al. (2024); Xiao et al. (2024); Zhang et al. (2024). KV-Cache eviction techniques selectively retain parts of the KV-Cache and discard less important tokens to maintain the use of a fixed-size KV-Cache to control memory usage. Representative works, such as AttentionSink (Xiao et al., 2024), employ a fixed eviction policy by preserving the tokens in the very beginning, which is also called attention sink, together with recent KV pairs. H2O (Zhang et al., 2024) selected the tokens based on accumulative attention scores. SnapKV (Li et al., 2024) evicts non-important tokens of each head based on the local observation window of prompts. While these methods reduce the memory footprint of KV-Cache and data to be transferred, they permanently discard KV pairs deemed less important, leading to accuracy degradation in some complex tasks that may require information from those eviction parts of the sequence.

Token Selection. To address the limitations of token eviction methods, another line of research focuses on retaining the entire KV-Cache while employing sparse attention mechanisms to process only selected parts of the KV-Cache, thereby reducing latency. Notable examples include SparQ (Ribar et al., 2024) and Quest (Tang et al., 2024). These methods achieve significant improvements in latency and accuracy preservation. However, since the full KV-Cache is retained, memory requirements remain unaddressed. As a result, techniques like CPU offloading are often necessary to execute inference requests.

In *Palu*, we take an orthogonal approach by compressing the hidden dimensions of the KV-Cache via low-rank projections. A potential direction for future work could be combining *Palu* with token selection methods to reduce memory usage further. This approach could involve compressing non-salient or infrequently accessed tokens to enhance memory efficiency and overall system performance further.

K Discussion of Alternative Strategies for Deriving Low-Rank Projection Matrices

In Palu, low-rank matrices $\mathbf{W} \approx \mathbf{AB}$ are derived by applying Singular Value Decomposition (SVD) to the weight matrices. Aside from this approach, alternative strategies for obtaining low-rank projection matrices in an offline manner, such as those proposed in Chen et al. (2021); Sakr & Khailany (2024), also exist. For instance, ESPACE Sakr & Khailany (2024) performs calibration on the input $\mathbf{x}$ and subsequently applies eigenvector decomposition to compute the low-rank projection matrix $\mathbf{P}$. During inference, ESPACE operates as $\mathbf{h} = \mathbf{xA}'$ and $\mathbf{y} = \mathbf{hB}'$, where $\mathbf{A}' = \mathbf{P}$ and $\mathbf{B}' = \mathbf{WP}$ are pre-computed. This approach ultimately achieves the same down-projection and reconstruction mechanism in the forward pass as the weight decomposition method used in Palu.

Future research could investigate accuracy differences between deriving low-rank projection matrices through direct weight decomposition, as implemented in Palu, and alternative techniques like ESPACE. Additionally, Palu's GPU kernel optimizations and quantization-friendly enhancements—such as the fusion of the Hadamard Transform—are agnostic to the method used to derive low-rank projection matrices. This adaptability provides a robust framework for integrating ESPACE or other approaches in future work.