Class-Discriminative Attention Maps for Vision Transformers

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Paper under double-blind review

Abstract

Importance estimators are explainability methods that quantify feature importance for deep neural networks (DNN). In vision transformers (ViT), the self-attention mechanism naturally leads to attention maps, which are sometimes used as importance scores for which input features ViT models are focusing on. However, attention maps do not account for signals from downstream tasks. To generate explanations that are sensitive to downstream tasks, we have developed class-discriminative attention maps (CDAM), a gradient-based extension that estimates feature importance with respect to a known class or a latent concept. CDAM scales attention scores by how relevant the corresponding tokens are for the predictions of a classifier head. In addition to targeting the supervised classifier, CDAM can explain an arbitrary concept shared by selected samples by measuring similarity in the latent space of ViT. Additionally, we introduce Smooth CDAM and Integrated CDAM, which average a series of CDAMs with slightly altered tokens. Our quantitative benchmarks include correctness, compactness, and class sensitivity, in comparison to six other importance estimators. Vanilla, Smooth, and Integrated CDAM excel across all three benchmarks. In particular, our results suggest that existing importance estimators may not provide sufficient class-sensitivity. We demonstrate the utility of CDAM in medical images by training and explaining malignancy and biomarker prediction models based on lung Computed Tomography (CT) scans. Overall, CDAM is shown to be highly class-discriminative and semantically relevant, while providing compact explanations.

1 Introduction

Vision transformers (ViT) are a family of computer vision models based on the transformer architecture (Vaswani et al., 2017), that demonstrate comparable or even better performance than convolutional neural networks (CNN) on many object detection and classification tasks (Dosovitskiy et al., 2020; Wu et al., 2020a). A powerful feature of the transformers is that the attention mechanism provides a built-in explanation of the model's inner workings, if attention is understood as a weighing of the relevance of individual tokens (Mullenbach et al., 2018; Bahdanau et al., 2014; Serrano & Smith, 2019; Thorne et al., 2019). While *attention maps* provide intuitive and inherent interpretability, they fail to be discriminative with respect to a target class. Recognizing the potential of attention maps for explaining a ViT's inner workings, we have developed *class-discriminative attention maps* (CDAM), a gradient-based extension that makes them sensitive to class-specific signals based on a classifier or a concept derived from selected samples.

Attention maps are the visualization of the self-attention of the class token query `[CLS]` in the final attention layer. Attention heads can be visualized separately, and in certain instances, may be related to semantically meaningful concepts (e.g., in language (Clark et al., 2019)). Recently, ViT trained with self-supervised learning (SSL) methods such as DINO (Caron et al., 2021) have shown excellent performance leveraging a greater amount of unlabeled data. Attention maps from such self-supervised ViT models provide high-quality semantic segmentations of input images. These attention maps clearly distinguish regions of interest (ROI) from the background with very little noise, with different attention heads often focusing on semantically distinct regions (Caron et al., 2021). There have been many improvements to ViT including the introduction of convolution (Wu et al., 2021; Yuan et al., 2021) and spatial sparsity (Li et al., 2021). Attention maps, as well as our proposed CDAMs, are applicable to all ViT architectures with self-attention.

The major shortcoming of attention maps, when considering them as an explainable AI (XAI) method, is that they purely operate on the level of the last attention layer and therefore do not take into account any information coming from a downstream task, such as a classifier head. The proposed CDAM overcomes this shortcoming by calculating the gradients of the class score, i.e. the logit value of a target class, with respect to the token activations in the final transformer block (visualized in Fig. 2(a)). Essentially, CDAM scales the attention scores by how relevant the corresponding tokens are for the model's decision. CDAM therefore inherits the desirable properties of attention maps, but additionally indicates the evidence or counter-evidence for a target class that the ViT relies on for its predictions (examples in Fig. 1). We demonstrate that it is class-discriminative in the sense that the heat maps clearly distinguish the object representing the target class from the background and, importantly, from objects that belong to other classes. Therefore, CDAM is a useful tool for explaining the decision-making process of classifiers with a ViT backbone.

In addition to the classifier-based explanations, we present a concept-based approach that replaces the class score with the similarity measure in the latent space of the ViT, where a concept is defined through selected images. Averaging the latent representations of the example images yields a *concept embedding*, which is analogous to a concept vector in variational autoencoders (VAE) and related generative models (Brocki & Chung, 2019; Kim et al., 2018). This allows obtaining a heat map for the target concept the model has never been explicitly trained on, which is of particular interest for self-supervised models. We further demonstrate when computing gradients of a class (Section 3.1) or concept similarity (Section 3.2) score, with respect to the token activations in the final transformer block, smoothing or averaging could be applied to improve performance. Specifically, we introduce two additional variants of CDAM; (1) Smooth CDAM averages over multiple gradients that are computed with additional noise to tokens (inspired by SmoothGrad (Smilkov et al., 2017)) and (2) Integrated CDAM takes the intergral of the gradients along the path from the baseline to the token in the final transformer block (inspired by IntGrad (Sundararajan et al., 2017)).

We conduct several quantitative evaluations focusing on correctness, class sensitivity, and compactness. Correctness is measured by perturbing an increasing amount of input features and measuring the model output (Brocki & Chung, 2023c;b). By using the ImageNet samples (Deng et al., 2009) with multiple objects (Beyer et al., 2020) and applying importance estimators for different classes, we quantify the level of class-discrimination. Sparsity and shrinkage of explanations are measured by the number of near-zero importance scores. Besides vanilla, Smooth, and Integrated CDAM, we also employed attention maps, relevance propagation (RP) (Chefer et al., 2021a), partial Layer-wise Relevance Propagation (LRP) (Voita et al., 2019), Input $\times$ Gradients, SmoothGrad (Smilkov et al., 2017), and Integrated Gradient (Sundararajan et al., 2017) in comparison. Three variants of CDAM outperform other explainability methods on three benchmarks.

Lastly, we have applied CDAM on a ViT fine-tuned on the Lung Image Database Consortium image collection (LIDC) (Armato III et al., 2011). Two ViT-based models are built for predicting malignancy and biomarkers. CDAM, as well as attention maps, are obtained. CDAM is shown to be highly class-discriminative and semantically relevant, while providing implicit regularization of importance scores.

2 Related Works

Interpretability of ViT, and more broadly explainable artificial intelligence (XAI), is an active area of research, since understanding their decision-making process would help improve the model, identify weaknesses and biases, and ultimately increase human trust in them. The proposed class-discriminative attention map (CDAM) is related to both attention and gradient-based explanation methods for deep learning models.

Gradient-based methods operate by backpropagating gradients from the prediction score to the input features to produce feature attribution maps, which is also called saliency maps. Many variants have been proposed, see (Simonyan et al., 2013; Sundararajan et al., 2017; Selvaraju et al., 2017; Smilkov et al., 2017; Shrikumar et al., 2016) to just name a few. In particular, CDAM is similar to and inspired by the input$\times$gradient method (Shrikumar et al., 2016), because it involves calculating the gradients with respect to tokens multiplied by their activation (Eqs. (2) and (4)). The main difference to most gradient-based methods is that we don't backpropagate the gradients all the way to the input tokens. CDAM stops backpropagation at the tokens that enter the final attention layer. In that regard, our method is related to GradCam (Selvaraju et al.,

2017) which backpropagates the gradients to the final convolutional feature map in a CNN. GradCam and CDAM therefore share the property that they operate on high-level features which is presumably the reason why they are both sensitive to the targeted class, a feature that many explanation methods do not have (Rudin, 2019). Several methods have attempted to apply gradient-based methods or Layer-Wise Relevance Propagation (LRP) (Bach et al., 2015) to Transformer architectures (Atanasova et al., 2020; Ali et al., 2022; Voita et al., 2019; Abnar & Zuidema, 2020; Chefer et al., 2021b), mostly in the context of NLP tasks.

Attention has often been used to gain insight into a model's inner workings (Mullenbach et al., 2018; Bahdanau et al., 2014; Serrano & Smith, 2019; Thorne et al., 2019) since it seems intuitive that this weighing of individual tokens correlates with how important they are for the performed task. There is also an ongoing discussion about whether attention provides meaningful explanations (Serrano & Smith, 2019; Wiegreffe & Pinter, 2019; Jain & Wallace, 2019). Furthermore, methods such as "attention rollout" (Abnar & Zuidema, 2020) have been proposed that aim to quantify how the attention flows through the model to the input tokens. (Chefer et al., 2021a) defines the relevancy matrices, as the Hadamard product of the attention map and the gradient of f_c w.r.t. to the attention layer, accumulated at each layer. This relevance propagation (RP) method (Chefer et al., 2021a), to the best of our knowledge, shows the highest degree of class-discrimination in ViT models. This is used in our study as one of comparative importance estimators.

Many papers have been published on the problem of evaluating post-hoc explanation methods, leading even to the proposal of meta-evaluations (Hedström et al., 2023). In a recent overview of quantitative evaluation methods (Nauta et al., 2023b) 12 desirable properties have been identified. We primarily focus on three of them, namely correctness, contrastivity, and compactness. In particular, carefully designed occulusion/perturbation studies can help us calculate a fidelity statistics (Brocki & Chung, 2023c), which is also called the symmetric relevance gain (SRG) measure (Bluecher et al., 2024). (Adebayo et al., 2018) first demonstrated that many importance estimators, which purport to be sensitive to the internals of a classifier, produce similar importance scores regardless of the relation of inputs and classes in the training data, which they called "the data randomization test". Generally, if two importance scores with respect to two different classes produce very similar heat maps, the importance estimator is not class sensitive. We quantify this concept in our class sensitivity evaluation benchmark to measure whether an explanation is sensitive to the classes.

3 Methods

Adaptation of the transformer architecture to computer vision hinges on creating tokens from small patches of the input image (Dosovitskiy et al., 2020). In addition to those image patch tokens, the `[CLS]` token is added, which is utilized for downstream tasks such as classification. Attention maps are the two-dimensional visualization of the self-attention in the final attention layer with `[CLS]` as query token, where the attention scores are averaged over all heads.

By design, attention maps are not class-discriminative since they do not take into account any signal coming from a downstream task. Therefore, we have developed *class-discriminative attention maps (CDAM)* that can be computed based on a known class or latent concept. In order to estimate a token's relevance, CDAM computes gradients of a class score (Section 3.1) or concept similarity score(Section 3.2), obtained downstream using the `[CLS]`$'$ token, with respect to the token activations in the final transformer block (Fig. 2).

In the first scenario, the class score is obtained from the corresponding activation in the prediction vector of a classifier trained on top of the ViT in a supervised fashion. In the second scenario, we define a concept through a small set of examples (e.g. ten images of a dog) and obtain a *concept vector* by averaging their latent representations. Then, without training a classifier, a similarity measure between the concept vector and the latent representation of a targeted sample image is computed and used as the target for the gradients. We call the resulting maps of feature relevance "class-discriminative attention maps" because they scale the attention scores

$$A_i = \text{softmax}\left(\frac{Q_{\texttt{[CLS]}} K_i^\top}{\sqrt{d_k}}\right), \tag{1}$$

by how relevant the corresponding tokens T_i are for the class or similarity score. Q and K are the query and key matrices, consisting of a set of d_k dimensional vectors (Vaswani et al., 2017). We discuss the proportionality of CDAM to the attention scores in Appendix A.1.

Self-supervised learning (SSL) methods such as DINO can train ViT models whose attention maps are high-quality semantic segmentations of the input, without using labels (Caron et al., 2021). Therefore, we utilize a ViT model (Dosovitskiy et al., 2020) pre-trained with DINO as a backbone for our experiments and applications. We denote details about the ViT architecture, training schemes, and model performance in the Section 4. Note that the heat maps shown in this article are scaled independently.

3.1 CDAM for a known class

Consider a linear classifier $f : \mathbb{R}^{d_{\text{model}}} \to \mathbb{R}^C$ on top of the ViT that takes the `[CLS]`$'$ token as input and maps it to a prediction vector with C classes, where d_{model} is the embedding dimension of the ViT. The importance score $S_{i,c}$ with respect to the token T_i is defined as

$$S_{i,c} = \sum_j T_{ij} \frac{\partial f_c}{\partial T_{ij}}, \tag{2}$$

where T_{ij} is the j-th component of the i-th token that is fed to the last attention layer (Fig. 2). We found in our experiments that calculating the gradients with respect to the layer-normalized tokens yields far better results than using the unnormalized ones.

This definition is a first-order estimation of the contribution of T_i to f_c in the sense that it would be exact if f_c depended on T_{ij} only linearly. It is inspired by gradient-based explanation methods with the difference that we don't backpropagate the gradients all the way to the input layer but only to the input tokens to the final attention layer. This allows us to gain insight into the decision-making process of the combination of ViT and classifier based on high-level features. This approach leads to attention maps that are class-discriminative and well-aligned with the semantic relationships of the class and different parts of an image (Fig. 1).

3.2 CDAM for a latent concept

Another way of probing high-level features learned by the ViT is through the use of a similarity measure g in the latent space of the ViT. We compare the latent representation $l(X) = T_{\texttt{[CLS]}'}(X)$ of a sample image X and a *concept vector* l_c (Wu et al., 2020b; Brocki & Chung, 2019; Kim et al., 2018), i.e. the averaged latent representation of n images that are chosen to represent the concept of interest:

$$l_c = \frac{1}{n} \sum_{X \in c} l(X). \tag{3}$$

This approach is directly inspired by the concept saliency map (Brocki & Chung, 2019). The definition of the importance score in this setting is analogous to Eq. (2)

$$S_{i,c} = \sum_j T_{ij} \frac{\partial g(l, l_c)}{\partial T_{ij}}. \tag{4}$$

Possible choices for g are for example the L^2 distance, cosine similarity or dot product, where we use the latter in this article. The definition Eq. (4) estimates the contribution of T_i to g, such that it allows us to gauge how much each token is driving the similarity between l and l_c.

3.3 Smooth and Integrated CDAM

SmoothGrad (SG) (Smilkov et al., 2017) and Integrated Gradients (IG) (Sundararajan et al., 2017) extended saliency maps (Simonyan et al., 2013), which were introduced in the context of CNNs as visualizing gradients of the class with respect to the input features. Briefly, (Smilkov et al., 2017) adds a small Gaussian noise to

a sample image n times, resulting in n vanilla saliency maps. SG is an average of those n saliency maps. In IG, instead of adding random noise, (Sundararajan et al., 2017) uses multiple saliency maps obtained from interpolating between a given sample and a baseline (e.g., a black image).

We have adapted the analogous modifications to CDAM, resulting in two additional variants which we call Smooth and Integrated CDAM. Importantly, instead of modifying the input images, we vary the tokens that enter the final transformer block. In Integrated CDAM, we interpolate between a baseline and the tokens themselves, resulting in n maps. In Smooth CDAM, we repeatedly add a small Gaussian noise to the tokens and again obtain n maps.

Specifically, Smooth and Integrated CDAM are defined as follows:

$$S_{i,c}^{\text{SG}} = \frac{1}{n} \sum_{1}^{n} \sum_{j} T'_{ij} \frac{\partial f_c(T')}{\partial T'_{ij}} \tag{5}$$

$$S_{i,c}^{\text{IG}} = \sum_{j} (T_{ij} - \tilde{T}_{ij}) \times \frac{1}{n} \sum_{1}^{n} \frac{\partial f_c(\tilde{T} + k/n \times (T - \tilde{T}))}{\partial T_{ij}} \tag{6}$$

where $T_i = T_i + \mathcal{N}\left(0, \sigma^2\right)$ with $\mathcal{N}\left(0, \sigma^2\right)$ representing Gaussian noise with standard deviation σ. For the baseline $\tilde{T}_i$ we choose the null vector. We implement these two variants by first propagating an image through the ViT up to the final transformer block, where the activations of the tokens are obtained. Next, the activations are manipulated by either applying the noise or interpolation step and the manipulated tokens are then further propagated to obtain the final ViT output.

3.4 Quantitative Evaluation

We perform quantitative evaluations of the correctness, class sensitivity, and compactness of importance estimators. In addition to our proposed methods (vanilla, smooth, and integrated CDAM), we perform evaluations on the raw attention maps, relevance propagation (RP) (Chefer et al., 2021a), partial Layer-wise Relevance Propagation (LRP) (Voita et al., 2019), SmoothGrad (Smilkov et al., 2017), IntGrad (Sundararajan et al., 2017), and Input $\times$ Gradients. Note that based on classic LRP (Bach et al., 2015), partial LRP (Voita et al., 2019) provides improvement for multi-head self-attention mechanisms in modern transformer architecture (Voita et al., 2019). Relevance propagation is a state-of-the-art importance estimator for explaining a prediction (e.g., class discriminatory) based on ViT (Chefer et al., 2021a). We use 50 interpolation steps for IntGrad and Integrated CDAM and chose the standard deviation of the noise used in SmoothGrad and smooth CDAM based on the best performance on the fidelity benchmark (explained below) on a held-out validation set of 200 images.

To evaluate the correctness (also known as faithfulness) of importance scores, we employ two versions of input perturbation-based approaches (Samek et al., 2016; Petsiuk et al., 2018; Kindermans et al., 2017). Generally, an input feature (e.g., a pixel) is masked and a resulting model performance is observed. In all cases, input features are perturbed by being replaced with their blurred versions. A Gaussian blur with $\sigma = 14$ turns pixels uninformative while minimizing perturbation artifacts (Brocki & Chung, 2023c).

Fidelity. The first evaluation method uses accuracy curves obtained from the Most Important First (MIF) and the Least Important First (LIF) perturbations, which are abbreviated as MIF/LIF perturbation (Brocki & Chung, 2023c;b). Pixels are ranked by importance scores from a specific explainability method (e.g., CDAM) and are perturbed in the MIF or LIF order. In the MIF perturbation, an accurate importance score should lead to a relatively rapid decrease of the model output (logit) for the target class. For the LIF perturbation, we expect an inverse relationship. Note that some importance scores are unsigned (i.e., only non-negative values) and others are signed. For signed importance, with negative scores faithfully indicating counter-evidence, there may be an increase in the logits if pixels with negative scores are masked. For unsigned and correct importance scores, one expects initially constant logits in the LIF perturbation.

The model output $f_{\text{MIF}}(p)$ or $f_{\text{LIF}}(p)$ as a function of the fraction of perturbed pixels p gives the perturbation curve (Brocki & Chung, 2023c;b). We average these curves over all samples, providing an overview of fidelity for a given importance estimator. We further summarize the MIF and LIF perturbation evaluation by using the area $A_{\text{LIF-MIF}}$ (called the fidelity statistics) under the difference of perturbation curves $f_{\text{LIF}} - f_{\text{MIF}}$ to quantify the fidelity of the explanation methods (Brocki & Chung, 2023b). Generally speaking, a higher value of fidelity statistics $A_{\text{LIF-MIF}}$ indicates a better explanation (Brocki & Chung, 2023c). Similar ideas are developed into the symmetric relevance gain (SRG) measure (Bluecher et al., 2024).

Box sensitivity. For the second evaluation method, inspired by Sensitivity-n (Ancona et al., 2017), we measure how the model output (logit) changes as a group of pixels are perturbed. Pixels are selected by a randomly placed square box (of size $s \times s$); then, the sum of their importance scores and the change in the model output are measured. For accurate importance estimators, we expect to see a high correlation between the two measures.

For a given image, we sample these values 100 times and calculate the Pearson correlation between the sum of importance scores and the model output change. This is performed for a range of differently sized boxes to obtain $f_{\text{box}}(s)$, the correlation statistics as a function of the box size s. These sensitivity curves are averaged over all samples. Performance of importance estimators varies with s, and therefore we use the area A_{box} under the box sensitivity curve to quantify correctness. Generally, a larger box sensitivity statistics A_{box} implies greater correctness.

In contrast to *Sensitivity-n* which randomly selects and perturbs n pixels (Ancona et al., 2017), we use a random square of pixels. A box removes a certain region which mimics how image patches are processed by ViT. Box sensitivity may therefore remove larger parts or complete objects. In contrast, removing random pixels may leave enough neighboring pixels with sufficient semantic information such that perturbation may not have any impact of the model output. Indeed, we have observed that for Sensitivity-n, the correlation is very low (< 0.1) for all methods.

Class discrimination. We have designed an evaluation benchmark to measure class discrimination, which can be applied on images containing multiple objects (see X_{multi} dataset below). We obtain explanations for two distinct classes corresponding to the present objects. When performing the aforementioned evaluation benchmarks (fidelity and box sensitivity), we measure the change in the model output with respect to one of the classes. Evaluation metrics are thus obtained using importance scores based on either the correct target class (denoted by MIF/LIF or box) or a wrong class (denoted by MIF′/LIF′ or box′).

For important estimators that are not sensitive/discriminative to the target class, the importance scores are similar (or the same) regardless of which class is targeted. The change of the model output during perturbation would remain the same, irrespective of the class that was targeted to obtain the importance ranking of pixels. For highly class-discriminative importance estimators, importance scores would be different depending on which class is targeted. Furthermore, for accurate class-discriminative methods, the performances on fidelity and box sensitivity benchmarks can be expected to deteriorate substantially when perturbing according to the importance scores targeting the wrong class.

The areas under MIF/LIF perturbation or box sensitivity curves, when using a wrong class, are denoted by $A_{\text{LIF}'-\text{MIF}'}$ and $A_{\text{box}'}$, respectively. The areas $\Delta A_{\text{LIF-MIF}}$ and ΔA_{box} under the respective perturbation curves

$$\Delta f_{\text{LIF-MIF}} = (f_{\text{LIF}} - f_{\text{MIF}}) - (f_{\text{LIF}'} - f_{\text{MIF}'}), \tag{7}$$

$$\Delta f_{\text{box}} = f_{\text{box}} - f_{\text{box}'}. \tag{8}$$

measure the degree of class-discrimination. In particular, if an importance estimator is not sensitive to the target class at all, $\Delta f_{\text{LIF-MIF}} \approx \Delta f_{\text{box}} \approx 0$. An importance estimator that performs poorly in the data randomization test of (Adebayo et al., 2018) would have low $\Delta A_{\text{LIF-MIF}}$ and ΔA_{box}.

Compactness. We evaluate sparsity and shrinkage by counting the number of input pixels with importance scores smaller than 5% of the maximum value. A threshold is defined by $t \times S_c^{\max}$ with $t = 0.05$, where $S_c^{\max}$ is the maximum importance score for a given image and an importance estimator. Generally, a compact

explanation is considered desirable, where sparsity and shrinkage are quantitative approaches (Nauta et al., 2023a).

3.5 Data

We perform quantitative evaluations on two datasets. The first one, X_{val}, is a randomly selected subset of the ImageNet validation set consisting of 1000 images (Deng et al., 2009). The second one, X_{multi}, selects 1000 images from the validation set that contain multiple objects (Beyer et al., 2020). We filtered out instances in which the class labels provided by (Beyer et al., 2020) actually refer to the same object (e.g. notebook and laptop) by calculating and thresholding the cosine similarity of the embedded class names. Embeddings were obtained using OpenAI's *text-embedding-3-large* model.

The X_{multi} dataset is used to evaluate the degree of class-discrimination exhibited by the explanations. To this end, we obtain explanations w.r.t to two annotated classes, perform the MIF/LIF perturbation and box sensitivity, and record the model output for the chosen target class. For example, for the top right sample in Fig. 1, we would obtain the explanations for the classes *Tench* and *Golden Retriever* (not shown) and record the model output for the class *Golden Retriever*. For the right target (*Tench*), we obtain a fidelity statistics $A_{\text{LIF}-\text{MIF}}$. For the wrong target (*Golden Retriever*), $A_{\text{LIF}'-\text{MIF}'}$. In the worst case scenario, where explanations for those two distinct classes are the same, $A_{\text{LIF}'-\text{MIF}'} = A_{\text{LIF}-\text{MIF}}$ and the resulting $\Delta A_{\text{LIF-MIF}}$ is zero. Equivalent for ΔA_{box}.

For application in medical images, we use lung computed tomography (CT) scans that were collected from and validated by seven academic centers and eight medical imaging companies (Armato III et al., 2011). The Lung Image Database Consortium image collection (LIDC) (Armato III et al., 2011) contains 1018 records of CT scans. Presence of nodules (nodule $\leq$ 3 mm; nodule $<$ 3 mm; non-nodule $\geq$ 3 mm) is annotated by up to 4 human annotators. Segmentation of nodules (i.e., ROI) is the average contour given by annotators. Eight biomarkers that are informative in clinical practices are also collected in LIDC: subtlety, calcification, sphericity, margin, lobulation, spiculation, texture, and diameter. For clinical descriptions of biomarkers, refer to (Opulencia et al., 2011). After preprocessing, 854 nodule crops of size, corresponding biomarkers, and labels (benign or malignant) were saved and used for downstream procedures. Overall, the LIDC dataset used in this study contains 443 benign examples and 411 malignant examples.

4 Results

For our experiments using the ImageNet (Deng et al., 2009), we have been using the ViT-S/8 architecture trained with DINO as a backbone (Caron et al., 2021), which is available as a pre-trained model in their repository[1]. We first discuss the results of applying CDAM qualitatively and then perform a quantitative comparison with several baseline methods.

4.1 Qualitative Evaluation

4.1.1 CDAM for a known class

To demonstrate our method, we have trained a linear classifier on the ImageNet (Deng et al., 2009) that achieved an accuracy of 77.0%. We use random resized cropping and horizontal flipping with PyTorch default arguments as augmentation, Adam optimizer with learning rate 3×10^{-4}, batch size of 128, and train for 10 epochs. The parameters of the ViT backbone are frozen during training, so only the classifier head is trainable. The predictions of this classifier were then used to create the heat maps shown in Fig. 1 via Eq. (2).

CDAM clearly distinguishes the region of interest (ROI) semantically related to the targeted class with positive values (yellow) from the rest of the image. Most backgrounds and other objects are assigned either zero (irrelevant) or negative scores (counter-evidence). Note that CDAM does not assign non-zero $S_{i,c}$ to tokens that have zero attention in attention maps, see also the scatter plot between CDAM and attention

[1]https://github.com/facebookresearch/dino

map Fig. S1. CDAM therefore appears to compute $S_{i,c}$ by multiplying the attention with the relevance of the corresponding token for the targeted class (Appendix A.1). This is a nice feature since CDAM inherits the high-quality object segmentations present in attention maps. This qualitative evaluation of shrinkage and sparsity of CDAM is reflected in the quantitative measures for compactness (Section 4.2.1).

One of the most useful features of CDAM is that it is highly sensitive to the chosen class. In Fig. 4 (left), when either the *zuccini* or *bell pepper* class is chosen, CDAM clearly highlights that vegetable. Most of the other vegetables are assigned either near-zero or negative values (indicated in blue). Many other importance estimators do not distinguish the target class or only to a lesser degree. In Fig. 5, targeting the burger or the hotdog does not seem to change importance scores from partial LRP, Input $\times$ Grad, and IntGrad. Relevance propagation demonstrates some selective focus on the ROI, but is not as discriminative as CDAM (Fig. 5). This visual impression of class-sensitivity is supported by the quantitative evaluation in Section 4.2.2. Additional examples of CDAM and other interpretability methods are shown in the Appendix A.

4.1.2 CDAM for a latent concept

Concept embeddings l_c have been obtained by averaging 30 latent representations of images depicting the concept of interest. These 30 images were randomly selected from the corresponding classes in the ImageNet validation set (Deng et al., 2009) and the CDAM in Fig. 3 were obtained using Eq. (4). We observe that CDAM reveals that the model clearly distinguishes the parts of the images that are relevant for the chosen concept from the rest of the image. For example, for the concept *hammer* (bottom right), CDAM primarily highlights the hammer. CDAM also provides positive importance scores for the wooden handles of the screwdrivers and the top of the ratchet, which are indeed relevant for this concept. Unrelated tools or parts appear in blue indicating that the model deems them to be unrelated to the concept *hammer*.

Just as CDAM is sensitive to the chosen class, it also produces attention maps that are sensitive to the chosen concept (Fig. 4, right). This makes the proposed method particularly valuable for understanding the representations the ViT has learned, since the explanations for different concepts can give a complementary view. For instance, CDAM distinguishes *african elephant* and *zebra*. However, CDAM also shows that parts of the elephant's trunk are counter-evidence for the concept *african elephant* (Fig. 4, right) which is initially counter-intuitive. However, when targeting the concept *zebra*, the model deems this part of the trunk to be similar to a zebra. Speculatively, the trunk may be too similar to the zebra's muzzle or the trunk's wrinkles may be mistaken for the zebra's stripes.

4.2 Quantitative evaluation

We have performed quantitative evaluations of the correctness and compactness of our proposed methods, in comparison to multiple well-known importance estimators. We further investigated class sensitivity by using importance scores from multiple classes.

4.2.1 Evaluation of correctness

CDAM performs favorably in terms of the correctness of estimated feature importance compared to other methods. For the dataset containing multiple objects (Table 2), the Smooth CDAM outperforms all other methods on the fidelity evaluation using MIF/LIF perturbation (Fig. 7), with $A_{\text{LIF-MIF}} = 827$ (Table 2). On the box sensitivity benchmark, Integrated CDAM ($A_{\text{box}} = 13.0$) performs the best, closely followed by Smooth CDAM ($A_{\text{box}} = 12.4$) (Fig. 6). Some methods, such as IntGrad, perform very well on the MIF benchmark but poorly for LIF (Table 2). We consider the difference (LIF-MIF) to be more meaningful and intuitive as ideally, one would want a large area under the LIF perturbation curve and a small area under the MIF perturbation curve. Thus, larger $A_{\text{LIF-MIF}} \uparrow$ indicates higher correctness. Particularly, a good score in MIF could stem from simply triggering perturbation artifacts of the model (Brocki & Chung, 2023b; Hooker et al., 2019).

For the random subset of ImageNet, the Integrated CDAM demonstrates the best performance ($A_{\text{box}} = 12.9$), closely followed by Relevance Propagation ($A_{\text{box}} = 12.7$) on the box sensitivity benchmark (Fig. S4,

Table S1). Relevance Propagation outperforms all other methods on the MIF/LIF perturbation, followed by the Smooth CDAM (Fig. S5).

4.2.2 Evaluation of class discrimination

Class discrimination (or sensitivity) is measured by the difference in fidelity statistics $A_{\Delta(\text{LIF-MIF})}$ when perturbing according to importance scores obtained for the correct or wrong target class. Larger $A_{\Delta(\text{LIF-MIF})}$ is considered to indicate better performance.

CDAM ($A_{\Delta(\text{LIF-MIF})}$=739), Smooth CDAM ($A_{\Delta(\text{LIF-MIF})}$=823), and Integrated CDAM ($A_{\Delta(\text{LIF-MIF})}$=708) clearly outperform other methods in terms of class discrimination (Table 2). IntGrad (540), Input $\times$ Grad (433), and Relevance Propagation (293) follow. Surprisingly, Partial LRP and SmoothGrad perform deficiently. Whereas SmoothGrad has low class-discrimination because its importance scores have low accuracy to begin with, Partial LRP's scores have mediocre accuracy but it appears to be insensitive to the choice of the target class (Fig. 5). By design, attention maps do not consider the target class and therefore, $A_{\Delta(\text{LIF-MIF})}$=0.

The importance scores for CDAM become anti-correlated with the model output when the *wrong* importance scores are used for the perturbation (Fig. S3). This anti-correlation probably results from the fact that pixels that are evidence for the correct target class are counter-evidence for the wrong class. This result corroborates the visual impression that CDAM correctly assigns importance scores with opposite signs to the objects corresponding to the targeted class and other objects that are present (Fig. 5). This is also reflected in the negative values of $f_{\text{LIF}'} - f_{\text{MIF}'}$ for CDAM (Fig. S2), indicating that the ranking from least to most important has been, at least partially, reversed.

4.2.3 Evaluation of compactness

Sparsity and shrinkage are evaluated by our compactness evaluation, which is one of the major desired properties in explainability of deep learning (Nauta et al., 2023a). While sparsity may not always imply the most accurate estimation at a single data point, a bias-variance trade-off is well-known in machine learning (Lahlou Kitane, 2022). Ideally, compact explanations (e.g., sparse and shrunken importance estimators) are preferred, when other properties such as correctness and class sensitivity are constant.

CDAM and Integrated CDAM resulted in the highest degree of compactness, together with Input $\times$ Grad. For those three importance estimators, on average, 88% of importance scores were less than 5% of the maximum score Table 2. IntGrad and SmoothGrad show relatively high sparsity 0.84 and 80%, respectively. But both are lacking in correctness (Section 4.2.1) and class-discrimination (Section 4.2.2). Relevance Propagation shows the lowest sparsity of all considered methods 48%, but a high level of correctness. These results suggest that these correctness and compactness metrics are orthogonal.

5 Application to Medical Images

To demonstrate CDAM for another use case we apply it to lung nodule malignancy and biomarker prediction using the LIDC dataset (Armato III et al., 2011).

5.1 Malignancy Prediction

After preprocessing, the LIDC data consists of 443 benign and 411 malignant lung CT scans. Training, validation, and test sets (in the ratios of 0.7225, 0.1275, 0.15) were stratified by and balanced according to these labels, e.g., benign and malignant. We fine-tuned a ViT model, with a DINO backbone pre-trained on the ImageNet, for 50 epochs. In a parameter sweep, we varied the number of trainable layers $(10 - 50)$ and dropout rates $(0.0 - 0.09)$, where the learning rate was exponentially decaying ($\alpha = 0.0003$ and $\beta = 0.95$). The best accuracy on the test set of 0.85 was obtained with 50 trainable layers and dropout rate of 0.003[2]. Attention maps and CDAM are obtained based on this model.

[2]It might be possible to increase the model performance via further investigation. Here, we use a straightforward model and training scheme to demonstrate the application of CDAM on medical images.

The obtained attention maps suggest that the model focuses on patches with nodule fragments (Fig. S9(b)). However, we note that attention maps almost always focus on pulmonary nodules without taking into account the downstream classification into benign and malignant samples. CDAM provides detailed structures where positive and negative values are indicated by orange and blue, respectively. In this binary classification where 0 is for benign and 1 for malignancy, input pixels with positive values in CDAMs are driving the classification towards malignancy.

5.2 Biomarker prediction

We turn our attention to clinical biomarkers in LIDC that are routinely used by medical practitioners. Inspired by the concept bottleneck model (CBM) (Koh et al., 2020), we fine-tuned a ViT model pre-trained with DINO on 8 biomarkers (subtlety, calcification, sphericity, margin, lobulation, spiculation, texture, and diameter). Essentially, a regression model was built on a pre-trained ViT model with the mean squared error (MSE) as loss function. For investigation of LIDC and incorporation of CBM, see (Brocki & Chung, 2023a).

CDAMs were obtained for 8 biomarkers (Fig. 8). In the context of the margin, patches including the edge of a nodule get positive CDAM scores, whereas patches corresponding to the nodule body get negative CDAM scores. For the diameter, patches corresponding to the nodule body get a positive score, whereas the background pixels exhibit neutral (near zero) or slightly negative scores. When it comes to sphericity, patches including fragments of nodule curvature get a positive CDAM score. Spiculation refers to the presence of needle and spike-like structures, on the margin. High spiculation often is an indication of malignancy. In a majority of cases, CDAM highlights spicules with positive values, whereas the inner bodies of nodules (i.e., not spicules) tend to get low importance scores.

6 Discussion

Class-Discriminative Attention Map (CDAM) is a gradient-based extension of attention maps, that provides strong discrimination with respect to a chosen class or concept, while exhibiting excellent fidelity and compactness. We introduce additional variants of CDAM, inspired by SmoothGrad ((Smilkov et al., 2017)) and IntGrad (Sundararajan et al., 2017)), which improve the performance on the quantitative benchmarks. Our proposed methods retain appealing characteristics of attention maps, namely high-quality semantic segmentation in self-supervised ViTs. The proposed importance estimation for CDAM scales the attention scores by how relevant they are for a target class or concept (Appendix A.1). Therefore, zero attention scores remain zero in CDAM and it produces compact explanations with high sparsity and shrinkage.

Post-hoc explanation methods for DNNs aim to make the full decision-making process of the model more transparent by providing an approximation with certain desirable properties, such as correctness, sensitivity, and compactness. Particularly, many explanation methods that estimate feature importance are not very useful because they give almost identical results when targeting different classes in the model output (Rudin, 2019; Adebayo et al., 2018). Even randomization in the model weights is often shown to have minimal impact on explanations (i.e., saliency maps (Adebayo et al., 2018)). We find, both qualitatively and quantitatively, that CDAM is highly sensitive to the targeted class, assigning positive importance scores to objects corresponding to the target class and negative ones to other (semantically distinct) objects in the image.

Besides explaining predictions of the classifier on the top of ViT, we introduce several variants. Firstly, by probing the latent space of the ViT (Fig. 4), self-supervised CDAM provides importance scores specific to the user-defined concept. In the context of SSL, where class labels are absent, this makes it a valuable technique to investigate the representations learned by the model, as shared by user-selected samples. To some degree, this can alternatively be done by looking at the attention maps of the different heads, which tend to specialize in different categories of objects or parts thereof (Caron et al., 2021). This approach is, however, limited to the categories that the attention heads happened to have learned. Secondly, we introduce Smooth and Integrated CDAM, which essentially average a series of (vanilla) CDAMs. Notably, instead of adding noise to or modifying the input images as in SmoothGrad (Smilkov et al., 2017)) or IntGrad (Sundararajan et al., 2017), respectively, our methods act on tokens in the final transformer block.

Our application on medical images exemplifies the need for fine-grained class-sensitive explanations offered by CDAM. Other explainability methods including attention maps are often highlighting whole nodules and tumors. But they are uninformative about the inner workings of the ViT model predicting malignancy or biomarkers. As the methods of explainable AI (XAI) are considered for practical implementations, investigation of human interactions with different explainability methods represents a promising direction for future studies. Last but not least, while this paper focuses on a ViT model, CDAM is applicable more broadly to all transformer models with self-attention, including large language models (LLMs).

References

Samira Abnar and Willem Zuidema. Quantifying attention flow in transformers. In *Proceedings of the 58th Annual Meeting of the Association for Computational Linguistics*, pp. 4190–4197. Association for Computational Linguistics, 2020.

Julius Adebayo, Justin Gilmer, Michael Muelly, Ian Goodfellow, Moritz Hardt, and Been Kim. Sanity checks for saliency maps. *Advances in neural information processing systems*, 31, 2018.

Ameen Ali, Thomas Schnake, Oliver Eberle, Grégoire Montavon, Klaus-Robert Müller, and Lior Wolf. Xai for transformers: Better explanations through conservative propagation. In *International Conference on Machine Learning*, pp. 435–451. PMLR, 2022.

Marco Ancona, Enea Ceolini, Cengiz Öztireli, and Markus Gross. Towards better understanding of gradient-based attribution methods for deep neural networks. *arXiv preprint arXiv:1711.06104*, 2017.

Samuel G Armato III, Geoffrey McLennan, Luc Bidaut, Michael F McNitt-Gray, Charles R Meyer, Anthony P Reeves, Binsheng Zhao, Denise R Aberle, Claudia I Henschke, Eric A Hoffman, et al. The lung image database consortium (lidc) and image database resource initiative (idri): a completed reference database of lung nodules on ct scans. *Medical physics*, 38(2):915–931, 2011.

Pepa Atanasova, Jakob Grue Simonsen, Christina Lioma, and Isabelle Augenstein. A diagnostic study of explainability techniques for text classification. *arXiv preprint arXiv:2009.13295*, 2020.

Sebastian Bach, Alexander Binder, Grégoire Montavon, Frederick Klauschen, Klaus-Robert Müller, and Wojciech Samek. On pixel-wise explanations for non-linear classifier decisions by layer-wise relevance propagation. *PloS one*, 10(7):e0130140, 2015.

Dzmitry Bahdanau, Kyunghyun Cho, and Yoshua Bengio. Neural machine translation by jointly learning to align and translate. *arXiv preprint arXiv:1409.0473*, 2014.

Lucas Beyer, Olivier J Hénaff, Alexander Kolesnikov, Xiaohua Zhai, and Aäron van den Oord. Are we done with imagenet? *arXiv preprint arXiv:2006.07159*, 2020.

Stefan Bluecher, Johanna Vielhaben, and Nils Strodthoff. Decoupling pixel flipping and occlusion strategy for consistent XAI benchmarks. *Transactions on Machine Learning Research*, 2024. ISSN 2835-8856. URL `https://openreview.net/forum?id=bIiLXdtUVM`.

Lennart Brocki and Neo Christopher Chung. Concept saliency maps to visualize relevant features in deep generative models. In *2019 18th IEEE International Conference On Machine Learning And Applications (ICMLA)*, pp. 1771–1778. IEEE, 2019.

Lennart Brocki and Neo Christopher Chung. Integration of radiomics and tumor biomarkers in interpretable machine learning models. *Cancers*, 15(9), 2023a. ISSN 2072-6694. doi: 10.3390/cancers15092459. URL `https://www.mdpi.com/2072-6694/15/9/2459`.

Lennart Brocki and Neo Christopher Chung. Feature perturbation augmentation for reliable evaluation of importance estimators in neural networks. *Pattern Recognition Letters*, 176:131–139, 2023b.

Lennart Brocki and Neo Christopher Chung. Fidelity of interpretability methods and perturbation artifacts in neural networks. In Krystal Maughan, Rosanne Liu, and Thomas F. Burns (eds.), *The First Tiny Papers Track at ICLR 2023, Tiny Papers @ ICLR 2023, Kigali, Rwanda, May 5, 2023*. OpenReview.net, 2023c. URL https://openreview.net/pdf?id=nbqO93YTz-.

Mathilde Caron, Hugo Touvron, Ishan Misra, Hervé Jégou, Julien Mairal, Piotr Bojanowski, and Armand Joulin. Emerging properties in self-supervised vision transformers. In *Proceedings of the IEEE/CVF international conference on computer vision*, pp. 9650–9660, 2021.

Hila Chefer, Shir Gur, and Lior Wolf. Generic attention-model explainability for interpreting bi-modal and encoder-decoder transformers. In *Proceedings of the IEEE/CVF International Conference on Computer Vision*, pp. 397–406, 2021a.

Hila Chefer, Shir Gur, and Lior Wolf. Transformer interpretability beyond attention visualization. In *Proceedings of the IEEE/CVF conference on computer vision and pattern recognition*, pp. 782–791, 2021b.

Kevin Clark, Urvashi Khandelwal, Omer Levy, and Christopher D. Manning. What does BERT look at? an analysis of BERT's attention. In Tal Linzen, Grzegorz Chrupała, Yonatan Belinkov, and Dieuwke Hupkes (eds.), *Proceedings of the 2019 ACL Workshop BlackboxNLP: Analyzing and Interpreting Neural Networks for NLP*, pp. 276–286, Florence, Italy, August 2019. Association for Computational Linguistics. doi: 10.18653/v1/W19-4828. URL https://aclanthology.org/W19-4828.

Jia Deng, Wei Dong, Richard Socher, Li-Jia Li, Kai Li, and Li Fei-Fei. Imagenet: A large-scale hierarchical image database. In *2009 IEEE conference on computer vision and pattern recognition*, pp. 248–255. Ieee, 2009.

Alexey Dosovitskiy, Lucas Beyer, Alexander Kolesnikov, Dirk Weissenborn, Xiaohua Zhai, Thomas Unterthiner, Mostafa Dehghani, Matthias Minderer, Georg Heigold, Sylvain Gelly, et al. An image is worth 16x16 words: Transformers for image recognition at scale. *arXiv preprint arXiv:2010.11929*, 2020.

Anna Hedström, Philine Bommer, Kristoffer K Wickstrøm, Wojciech Samek, Sebastian Lapuschkin, and Marina M-C Höhne. The meta-evaluation problem in explainable ai: Identifying reliable estimators with metaquantus. *arXiv preprint arXiv:2302.07265*, 2023.

Sara Hooker, Dumitru Erhan, Pieter-Jan Kindermans, and Been Kim. A benchmark for interpretability methods in deep neural networks. *Advances in neural information processing systems*, 32, 2019.

Sarthak Jain and Byron C Wallace. Attention is not explanation. *arXiv preprint arXiv:1902.10186*, 2019.

Been Kim, Martin Wattenberg, Justin Gilmer, Carrie Cai, James Wexler, Fernanda Viegas, et al. Interpretability beyond feature attribution: Quantitative testing with concept activation vectors (tcav). In *International conference on machine learning*, pp. 2668–2677. PMLR, 2018.

Pieter-Jan Kindermans, Kristof T Schütt, Maximilian Alber, Klaus-Robert Müller, Dumitru Erhan, Been Kim, and Sven Dähne. Learning how to explain neural networks: Patternnet and patternattribution. *arXiv preprint arXiv:1705.05598*, 2017.

Pang Wei Koh, Thao Nguyen, Yew Siang Tang, Stephen Mussmann, Emma Pierson, Been Kim, and Percy Liang. Concept bottleneck models. In *International conference on machine learning*, pp. 5338–5348. PMLR, 2020.

Driss Lahlou Kitane. *Sparsity in Machine Learning: Theory and Applications*. PhD thesis, Massachusetts Institute of Technology, 2022.

Yawei Li, Kai Zhang, Jiezhang Cao, Radu Timofte, and Luc Van Gool. LocalViT: Bringing Locality to Vision Transformers. *CoRR*, abs/2104.05707, 2021. URL https://arxiv.org/abs/2104.05707. arXiv: 2104.05707.

James Mullenbach, Sarah Wiegreffe, Jon Duke, Jimeng Sun, and Jacob Eisenstein. Explainable prediction of medical codes from clinical text. *arXiv preprint arXiv:1802.05695*, 2018.

Meike Nauta, Jan Trienes, Shreyasi Pathak, Elisa Nguyen, Michelle Peters, Yasmin Schmitt, Jörg Schlötterer, Maurice van Keulen, and Christin Seifert. From anecdotal evidence to quantitative evaluation methods: A systematic review on evaluating explainable ai. *ACM Computing Surveys*, 55(13s):1–42, 2023a.

Meike Nauta, Jan Trienes, Shreyasi Pathak, Elisa Nguyen, Michelle Peters, Yasmin Schmitt, Jörg Schlötterer, Maurice van Keulen, and Christin Seifert. From anecdotal evidence to quantitative evaluation methods: A systematic review on evaluating explainable ai. *ACM Computing Surveys*, 55(13s):1–42, 2023b.

Pia Opulencia, David S Channin, Daniela S Raicu, and Jacob D Furst. Mapping lidc, radlex™, and lung nodule image features. *Journal of digital imaging*, 24:256–270, 2011.

Vitali Petsiuk, Abir Das, and Kate Saenko. Rise: Randomized input sampling for explanation of black-box models. *arXiv preprint arXiv:1806.07421*, 2018.

Cynthia Rudin. Stop explaining black box machine learning models for high stakes decisions and use interpretable models instead. *Nature machine intelligence*, 1(5):206–215, 2019.

Wojciech Samek, Alexander Binder, Grégoire Montavon, Sebastian Lapuschkin, and Klaus-Robert Müller. Evaluating the visualization of what a deep neural network has learned. *IEEE transactions on neural networks and learning systems*, 28(11):2660–2673, 2016.

Ramprasaath R Selvaraju, Michael Cogswell, Abhishek Das, Ramakrishna Vedantam, Devi Parikh, and Dhruv Batra. Grad-cam: Visual explanations from deep networks via gradient-based localization. In *Proceedings of the IEEE international conference on computer vision*, pp. 618–626, 2017.

Sofia Serrano and Noah A Smith. Is attention interpretable? *arXiv preprint arXiv:1906.03731*, 2019.

Avanti Shrikumar, Peyton Greenside, Anna Shcherbina, and Anshul Kundaje. Not just a black box: Learning important features through propagating activation differences. *arXiv preprint arXiv:1605.01713*, 2016.

Karen Simonyan, Andrea Vedaldi, and Andrew Zisserman. Deep inside convolutional networks: Visualising image classification models and saliency maps. *arXiv preprint arXiv:1312.6034*, 2013.

Daniel Smilkov, Nikhil Thorat, Been Kim, Fernanda Viégas, and Martin Wattenberg. Smoothgrad: removing noise by adding noise. *arXiv preprint arXiv:1706.03825*, 2017.

Mukund Sundararajan, Ankur Taly, and Qiqi Yan. Axiomatic attribution for deep networks. In *International conference on machine learning*, pp. 3319–3328. PMLR, 2017.

James Thorne, Andreas Vlachos, Christos Christodoulopoulos, and Arpit Mittal. Generating token-level explanations for natural language inference. *arXiv preprint arXiv:1904.10717*, 2019.

Ashish Vaswani, Noam Shazeer, Niki Parmar, Jakob Uszkoreit, Llion Jones, Aidan N Gomez, Łukasz Kaiser, and Illia Polosukhin. Attention is all you need. *Advances in neural information processing systems*, 30, 2017.

Elena Voita, David Talbot, Fedor Moiseev, Rico Sennrich, and Ivan Titov. Analyzing multi-head self-attention: Specialized heads do the heavy lifting, the rest can be pruned. *arXiv preprint arXiv:1905.09418*, 2019.

Sarah Wiegreffe and Yuval Pinter. Attention is not not explanation. *arXiv preprint arXiv:1908.04626*, 2019.

Bichen Wu, Chenfeng Xu, Xiaoliang Dai, Alvin Wan, Peizhao Zhang, Zhicheng Yan, Masayoshi Tomizuka, Joseph Gonzalez, Kurt Keutzer, and Peter Vajda. Visual Transformers: Token-based Image Representation and Processing for Computer Vision. *arXiv e-prints*, June 2020a. doi: 10.48550/arXiv.2006.03677. URL `https://ui.adsabs.harvard.edu/abs/2020arXiv200603677W`.

Haiping Wu, Bin Xiao, Noel Codella, Mengchen Liu, Xiyang Dai, Lu Yuan, and Lei Zhang. CvT: Introducing Convolutions to Vision Transformers. In *Proceedings of the IEEE/CVF International Conference on Computer Vision (ICCV)*, pp. 22–31. IEEE Computer Society, October 2021. ISBN 9781665428125. doi: 10.1109/ICCV48922.2021.00009. URL `https://www.computer.org/csdl/proceedings-article/iccv/2021/281200a022/1BmEM0WJfTW`.

Weibin Wu, Yuxin Su, Xixian Chen, Shenglin Zhao, Irwin King, Michael R Lyu, and Yu-Wing Tai. Towards global explanations of convolutional neural networks with concept attribution. In *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*, pp. 8652–8661, 2020b.

Kun Yuan, Shaopeng Guo, Ziwei Liu, Aojun Zhou, Fengwei Yu, and Wei Wu. Incorporating convolution designs into visual transformers. In *Proceedings of the IEEE/CVF international conference on computer vision*, pp. 579–588, 2021.

7 Figures

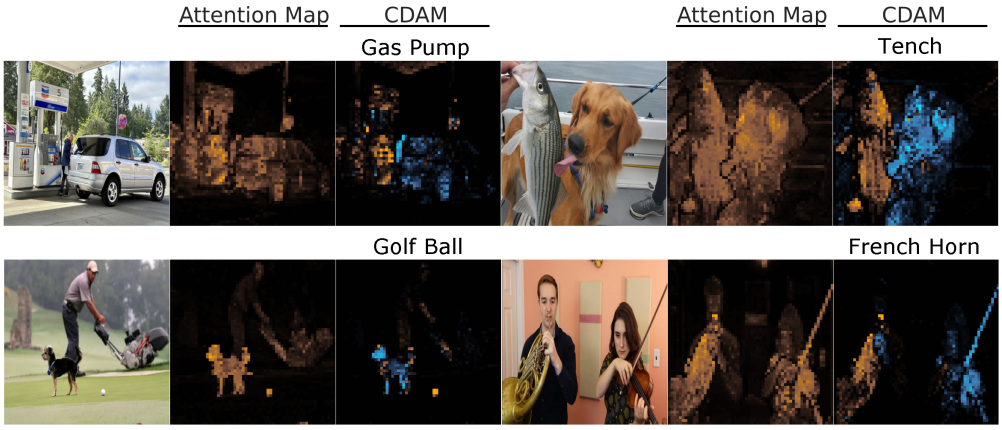

Figure 1: Extending attention maps (AM), the proposed class-discriminative attention maps (CDAM) quantify and visualize input features that are relevant for the target class in Vision Transformers (ViT). We visualize importance scores obtained with CDAM for a linear classifier with ViT-S/8, trained with DINO, as a backbone (Caron et al., 2021). For details, refer to Section 3.1. Orange and blue colors correspond to positive and negative values, respectively.

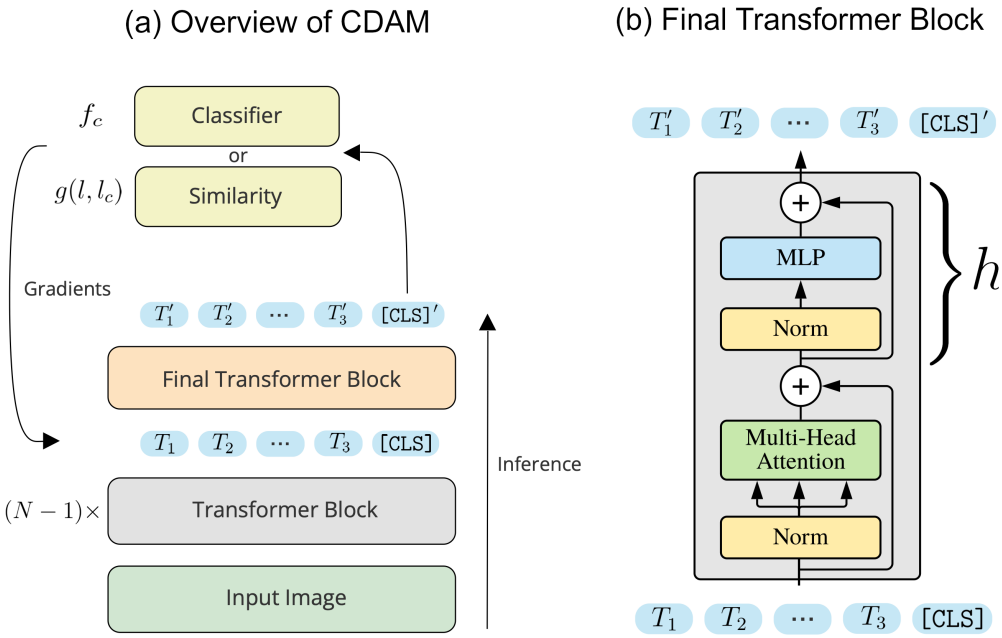

Figure 2: Graphical scheme of *class-discriminative attention maps* (CDAM). **(a)** CDAMs are obtained by first propagating an image through the transformer blocks and using its latent representation $l = \texttt{[CLS]}'$ to infer a class score f_c or similarity score $g(l, l_c)$. The gradients wrt the *layer-normalized* input tokens T_i of the final attention layer and their activations are then used to calculate the importance score $S_{i,c}$ according to Eq. (2) or Eq. (4). **(b)** Detailed view of the final transformer block, adapted from (Dosovitskiy et al., 2020).

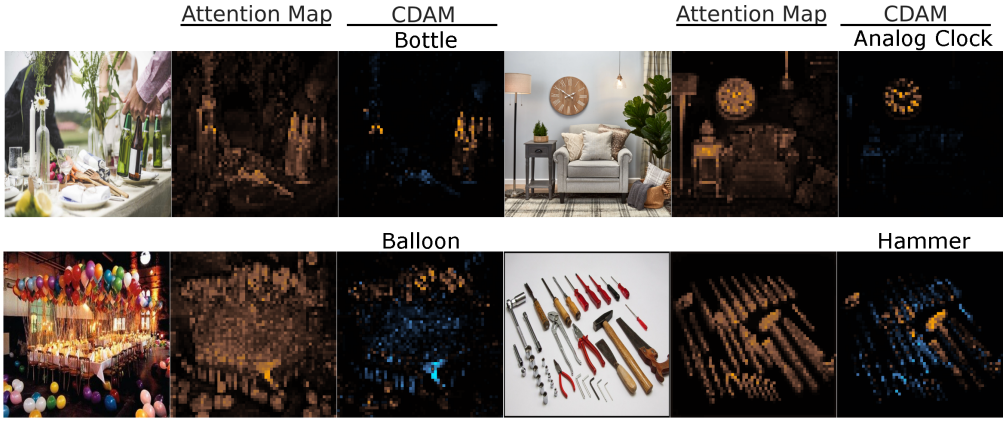

Figure 3: Class-Discriminative Attention Maps (CDAM) for user-defined concepts (Section 3.2). The concept embedding l_c has been obtained by averaging the latent representations of 30 images that include the common concept. In each instance, from left to right: Sample image, AM, and CDAM. Orange and blue correspond to positive and negative values, respectively.

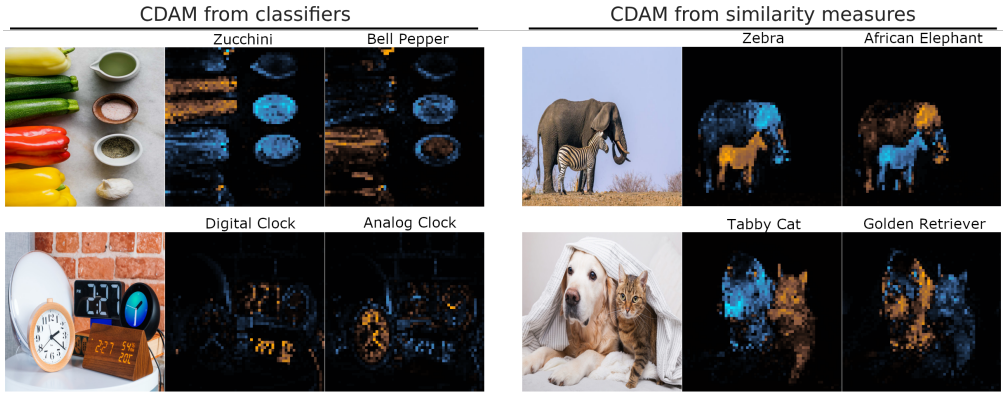

Figure 4: When targeting different classes (left) or concepts (right), the resulting CDAMs are distinct and align with the corresponding objects. Note that green parts of vegetables are shown to activate the *zuccini* class (left). The wrinkles in the elephant's trunk appear to be related to the *zebra* concept, semantically mistaken by the model as zebra stripes.

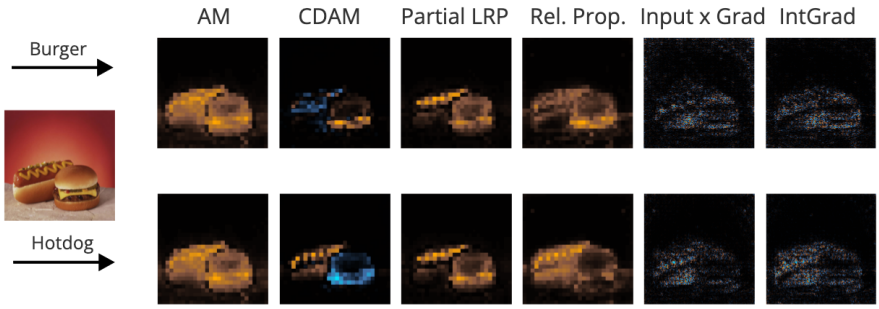

Figure 5: Visual comparison of different importance estimators which obtain explanations w.r.t. different output classes. Similar heat maps regardless of target classes imply that importance estimators are not class discriminative. Attention maps (AM) are, by design, not class discriminative. Orange and blue colors correspond to positive and negative values, respectively.

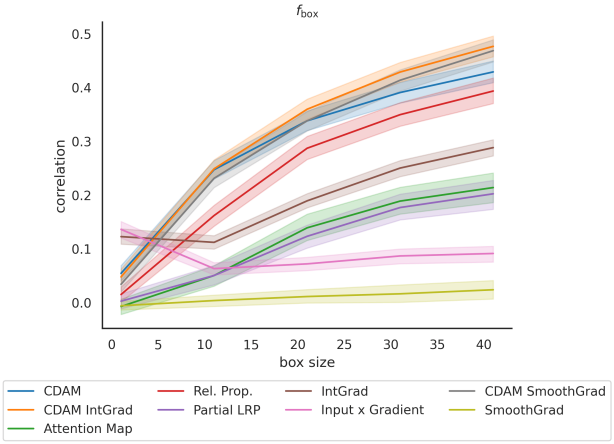

Figure 6: Correctness of importance estimators as measured by box sensitivity evaluation. The change in the model output (logit) is measured as pixels within a $s \times s$ box are perturbed. The sum of their importance scores would correlate with the change in the model output, if importance estimators are accurate. This is repeated 100 times per sample and the Pearson correlation between the sum of importance scores and the change in the model output is calculated, based on the X_{multi} dataset.

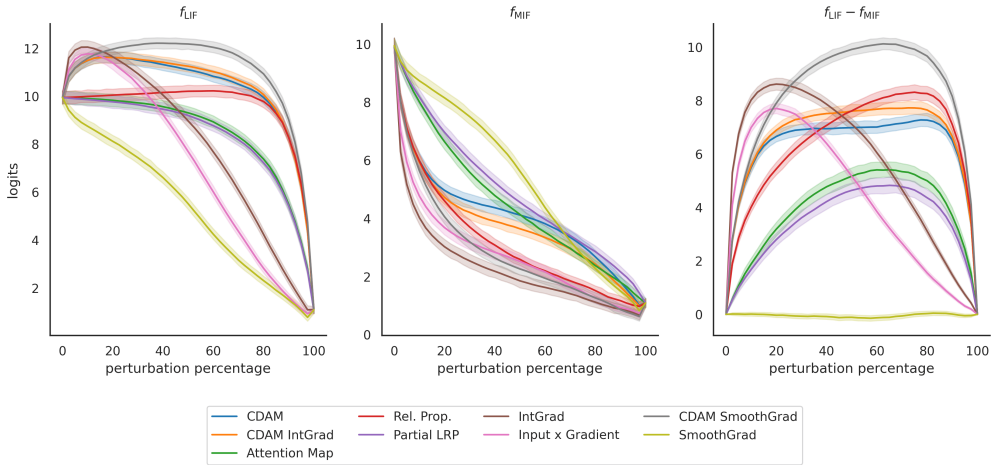

Figure 7: Fidelity of importance estimators based on MIF/LIF perturbation curves obtained from the X_{multi} dataset. The change in the model output is measured as a proportion of input features are perturbed according to the Least Important First (LIF) or the Most Important First (MIF) orders. Importance estimators are evaluated by the area between LIF and MIF perturbation curves, which is equivalent to the area underneath f_{LIF}-f_{MIF} (right). See Table 2.

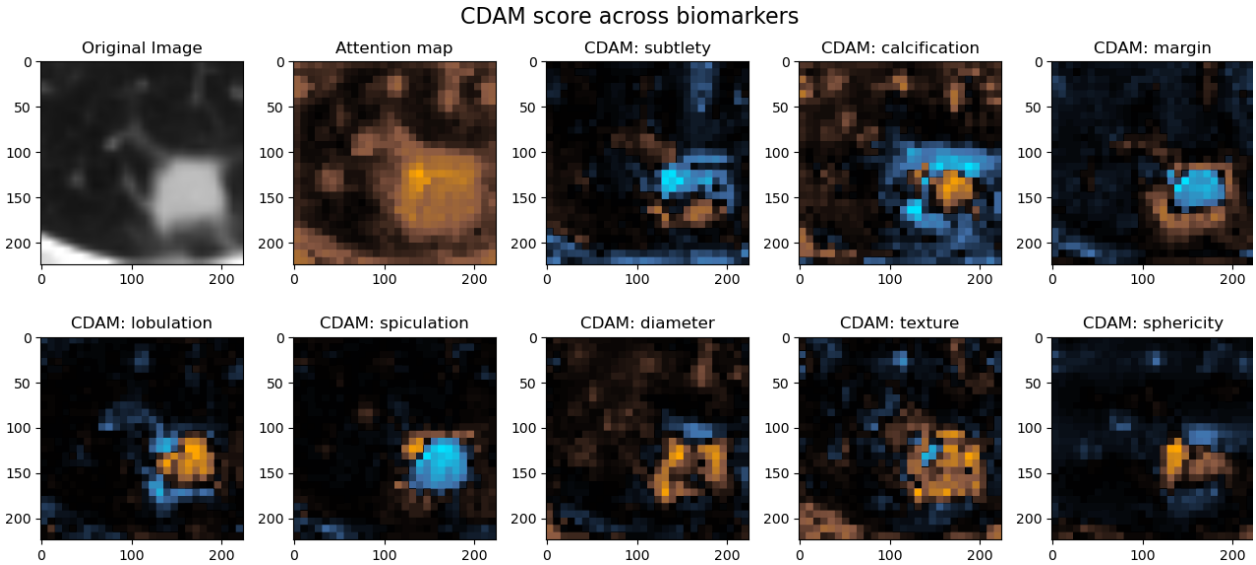

Figure 8: Explanations for the biomarker prediction model. Eight biomarkers available in the LIDC dataset are used to fine-tune a ViT regression model with a DINO backbone. CDAMs provide distinct and relevant explanations for different biomarkers. For more examples, see Appendix A.4.

8 Tables

	Compactness↑
CDAM	**0.88**
CDAM Integrated	**0.88**
CDAM Smooth	0.75
Relevance Propagation	0.48
Partial LRP	0.74
Attention map	0.56
SmoothGrad	0.8
IntGrad	0.84
Input × Grad	**0.88**

Table 1: Compactness, measuring sparsity and shrinkage, is defined by the fraction of pixels with importance score lower or equal to 5% of the maximum score, evaluated on the X_{multi} dataset.

			Fidelity	Box Sensitivity
	$\text{A}_{\text{MIF}}\downarrow$	$\text{A}_{\text{LIF}}\uparrow$	$\text{A}_{\text{LIF-MIF}}\uparrow$	$\text{A}_{\text{box}}\uparrow$
CDAM	404	1038	632	12.2
CDAM Integrated	375	1045	669	**13.0**
CDAM Smooth	282	**1110**	**827**	12.4
Relevance Propagation	315	957	643	10.0
Partial LRP	489	837	348	4.5
Attention map	452	846	393	4.8
SmoothGrad	534	529	-4	0.4
IntGrad	**226**	802	574	7.6
Input × Grad	273	713	439	3.5

Table 2: Evaluation of correctness by fidelity and box sensitivity. In X_{multi}, importance scores for the target class were used to perturb pixels. The changes in the model output w.r.t. the perturbation percentage ($f_{\text{LIF-MIF}}$; Fig. 7) or the box size (f_{box}; Fig. 6) are quantified by the area under the curves.

	Fidelity	Box Sensitivity
	$\text{A}_{\Delta(\text{LIF-MIF})}\uparrow$	$\text{A}_{\Delta\text{box}}\uparrow$
CDAM	739	14.6
CDAM Integrated	708	**14.8**
CDAM Smooth	**823**	13.4
Relevance Propagation	293	6.6
Partial LRP	3	0.0
Attention map	0	-0.2
SmoothGrad	-11	-0.1
IntGrad	540	7.6
Input × Grad	433	3.4

Table 3: Evaluation of class discrimination by differences in fidelity and box sensitivity metrics. By using the X_{multi} dataset, sensitivity of estimated importance scores w.r.t. a target class or a wrong class is measured (Details in Section 3.5). Area under the $\Delta f_{\text{LIF-MIF}}$ (Fig. S2) and Δf_{box} curves (Fig. S3).

A Appendix

A.1 Proportionality of CDAM to attention maps

The proposed class-discriminative attention scores scale the attention scores. Empirically, in all of our evaluation tasks and applications (e.g., Fig. S1), we observe that features with attention scores $A_i = \text{softmax}\left(\frac{Q_{\texttt{[CLS]}} K_i^\top}{\sqrt{d_k}}\right)$ of 0 have class-discriminative attention scores of 0:

$$A_i = 0 \Rightarrow S_{i,c} = 0. \tag{9}$$

This operating characteristic is highly favorable, as besides introducing class discrimination, CDAM provides implicit regularization resulting in sparser heat maps. Based on a combination of empirical observations and mathematical derivations, we argue that the attention score $A_i = \text{softmax}\left(\frac{Q_{\texttt{[CLS]}} K_i^\top}{\sqrt{d_k}}\right)$ is scaled by the relevance of the corresponding token T_i for a concept or a class.

To better understand this observation, we first consider a concept-based CDAM with a single attention head. Eq. (4) is expanded:

$$\begin{aligned}
S_{i,c} &= \sum_j T_{ij} \frac{\partial g(l, l_c)}{\partial T_{ij}} \\
&= \sum_j T_{ij} \frac{\partial}{\partial T_{ij}} \sum_k l_k l_{c,k} \\
&= \sum_j T_{ij} \frac{\partial}{\partial T_{ij}} \sum_k h_k \left(\sum_m A_m V_m + \texttt{[CLS]} \right) l_{c,k} \\
&= \sum_j T_{ij} \sum_{k,m,n} \nabla_n h_k \times \left(\frac{\partial A_m}{\partial T_{ij}} V_{mn} + A_m \frac{\partial V_{mn}}{\partial T_{ij}} \right) l_{c,k} \\
&= \sum_{j,k,m,n} T_{ij} \nabla_n h_k \frac{\partial A_m}{\partial T_{ij}} V_{mn} l_{c,k} + \sum_{k,n} A_i V_{in} \nabla_n h_k l_{c,k},
\end{aligned} \tag{10}$$

where we assume the architecture of (Dosovitskiy et al., 2020) and use the projection of the tokens onto the key vector $V_i = T_i W^V$ with $W^V \in \mathbb{R}^{d_{\text{model}} \times d_v}$. We have also used the fact that the latent representation l (i.e. $\texttt{[CLS]}'$) is the sum of value vectors weighted by the corresponding attention, $l = \sum_i A_i V_i$ with $A_i = \text{softmax}\left(\frac{Q_{\texttt{[CLS]}} K_i^\top}{\sqrt{d_k}}\right)$ plus `[CLS]` due to the residual connection, see Fig. 2(b). The function $h : \mathbb{R}^{d_v} \to \mathbb{R}^{d_{\text{model}}}$ consists of the layer normalization, MLP, and residual connection and performs the final processing of the `[CLS]` token before it enters the classifier (Fig. 2(b)). ∇_n is the n-th component of the gradient and $Q_{\texttt{[CLS]}}$, V_i and K_i are the rows of matrices Q, V and K that correspond to the `[CLS]` and the i-th tokens.

Eq. (9) implies that in Eq. (10), all terms that are not proportional to A_i are zero or cancelled out and we are left with

$$S_{i,c} = A_i V_i \cdot \nabla(h \cdot l_c). \tag{11}$$

We thus find that $S_{i,c}$ is obtained by multiplying A_i with the directional derivative of $h \cdot l_c$ in the direction of V_i. In other words, CDAM scales A_i by the rate at which the dot product (similarity) between h and c changes in the direction of V_i.

In the special case that h is the identity function, we obtain an even simpler interpretation of CDAM due to $\nabla_n h_k(f) = \partial_{f_n} f_k = \delta_{nk}$. Assuming $\frac{\partial A_m}{\partial T_{ij}} = 0$, Eq. (10) simplifies to $S_{i,c} = A_i V_i \cdot l_c$, which means that A_i is scaled by the similarity of V_i and l_c.

We note that introducing h attention heads does not change the above derivations qualitatively. Instead of the sum $Z = \sum_m A_m V_m$, there will be a term $\text{Concat}(Z^1, Z^2, .., Z^h) W^O, W^O \in \mathbb{R}^{h d_v \times d_{\text{model}}}$ so that in the

case of multi-head attention the equivalent of Eq. (10) reads

$$S_{i,c} = \text{Concat}\left(Y^1, Y^2, .., Y^h\right) W^O \nabla(h \cdot l_c),\ Y^n = T_i \sum_m \frac{\partial A_m^n}{\partial T_i} V_m^n + A_i^n V_i^n \tag{12}$$

and since $A_i^n > 0, A_i = \sum_n \frac{A_i^n}{h}$ implies that $A^i = 0 \Rightarrow A_i^n = 0, \forall n$ we can again conclude that in order for Eq. (9) to hold all terms that are not proportional to A_i either vanish or cancel out. For multi-head attention we thus arrive at

$$S_{i,c} = \text{Concat}\left(Y'^1, Y'^2, .., Y'^h\right) W^O \nabla(h \cdot l_c),\ Y'^n = A_i^n V_i^n, \tag{13}$$

which does not have such a straightforward interpretation as the single-headed case due to the mixing of the attention heads.

If we think of W^O as acting first on $\nabla(h \cdot l_c)$, creating a column vector of dimension hd_v, we can understand Eq. (13) as the sum of h directional derivatives of the d_v-long segments of this columns vector in the directions of Y'^1 to Y'^h. Each of the summands is proportional to the corresponding A^n, and the interpretation of CDAM from the single-head case therefore extends to the multi-head one.

Although our observation $A_i = 0 \Rightarrow S_{i,c} = 0$ implies that all terms that are not proportional to A_i in Eq. (10) should vanish, we don't have a theoretical argument why that would be the case. It seems unlikely that the various terms in the first sum cancel out, which leaves $\frac{\partial A_m}{\partial T_{ij}} = 0$ as an explanation. However, in general, A_i depends on T_i through K_i and one would therefore expect the derivative to be non-zero.

We can also show that CDAM scales the attention by the relevance of the corresponding token for a chosen class (instead of concept), in the case that a classifier with weights W^C has been trained on top of the ViT. Analogously to the above single-head discussion we have

$$\begin{aligned} S_{i,c} &= \sum_j T_{ij} \frac{\partial f_c}{\partial T_{ij}} \\ &= \sum_j T_{ij} \frac{\partial}{\partial T_{ij}} \sum_k l_k W_{kc}^C \\ &= \sum_{j,k,m,n} T_{ij} \nabla_n h_k \frac{\partial A_m}{\partial T_{ij}} V_{mn} W_{kc}^C + \sum_{k,n} A_i V_{in} \nabla_n h_k W_{kc}^C, \end{aligned} \tag{14}$$

and the only difference is that the directional derivative now acts on $\sum_k h_k W_{kc}$, i.e. the contribution of h to the activation of class c in the prediction vector, instead of $\sum_k h_k l_{c,k}$. All the intuitions we have gained from the concept-based CDAM therefore extend to the class-based one.

A.2 Quantitative Evaluations

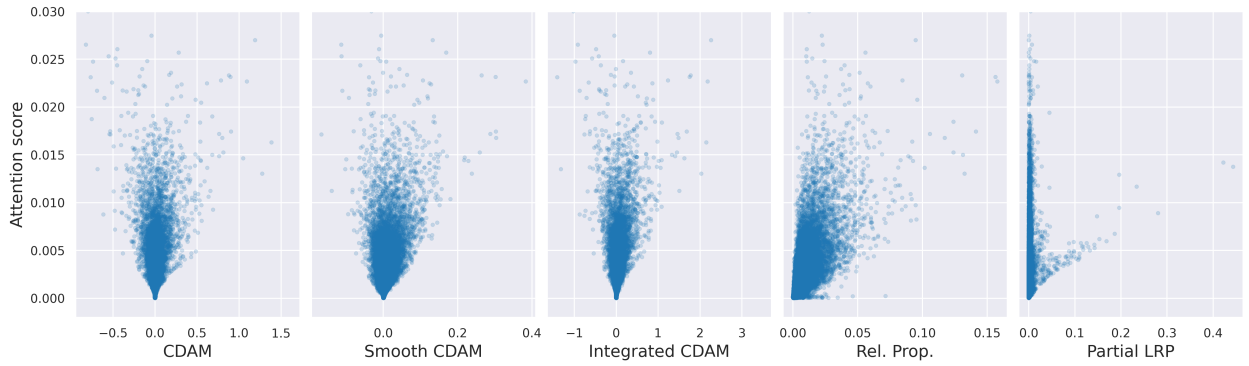

Figure S1: Scatter plot of raw attention scores and token importance scores obtained from 200 randomly selected samples of the ImageNet validation set X_{val}.

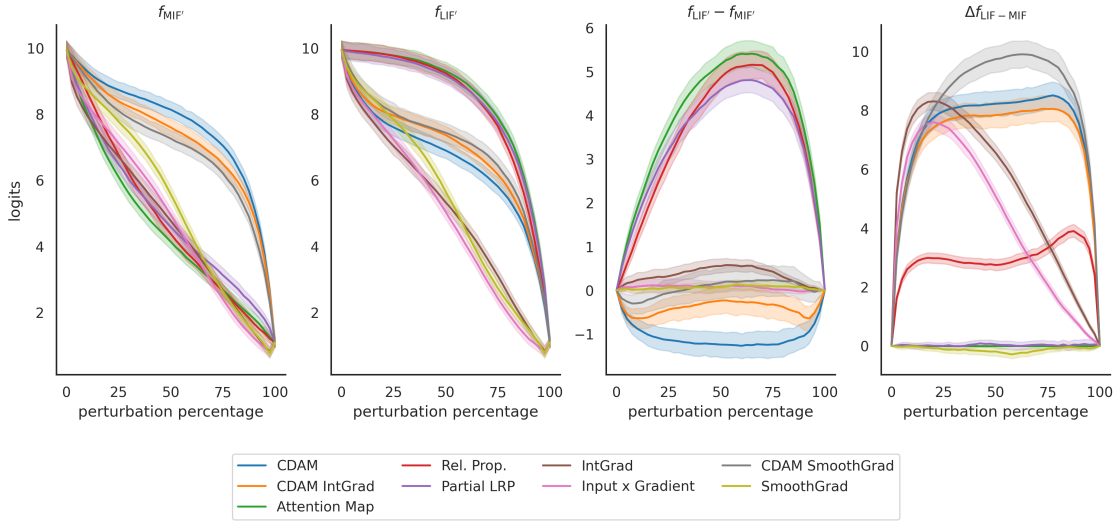

Figure S2: MIF/LIF perturbation curves for the evaluation of class-discrimination. Different classes are targeted for obtaining importance scores and measuring model output (Section 3.5), a large ΔA_{box}, therefore, indicates importance scores that are class-discriminative. See Table 3

	$A_{\text{MIF}}\downarrow$	$A_{\text{LIF}}\uparrow$	$A_{\text{LIF-MIF}}\uparrow$	$A_{\text{box}}\uparrow$
CDAM	801	1423	623	11.3
Integrated CDAM	696	1459	753	**12.9**
Smooth CDAM	591	**1482**	890	11.9
Rel. Prop.	**475**	1432	**957**	12.7
Partial LRP	654	1329	674	8.4
Att. map	580	1352	771	9.1
SmoothGrad	796	786	-10	0.2
IntGrad	411	1055	644	8.3
Input x Grad	470	935	465	3.1

Table S1: Area under the curve for MIF, LIF and LIF-MIF curves (Fig. S5) and box sensitivity curves (Fig. S4) obtained from the random ImageNet subset.

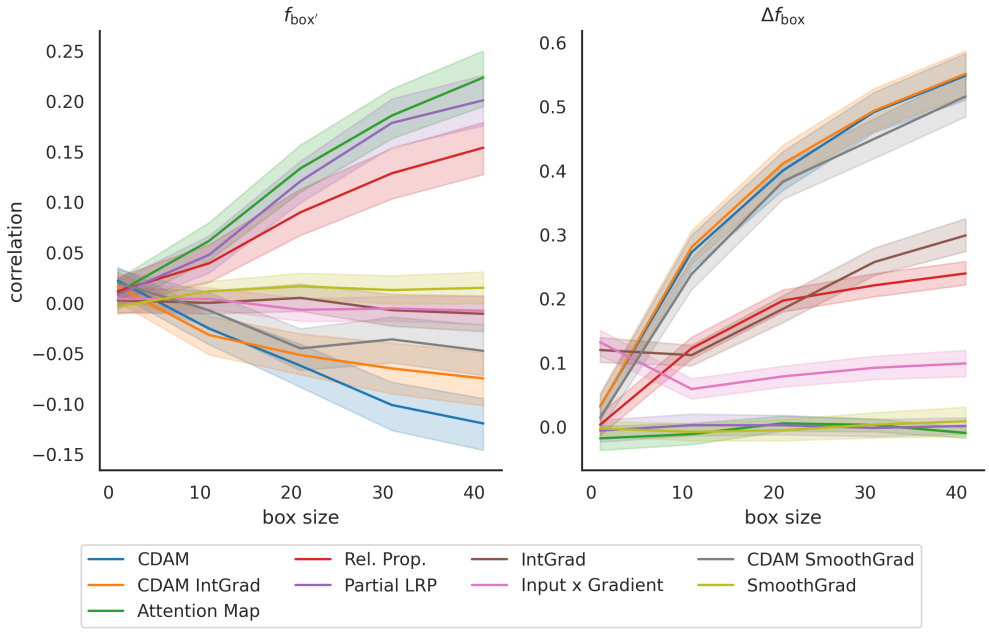

Figure S3: Box sensitivity curves for the evaluation of class-sensitivity

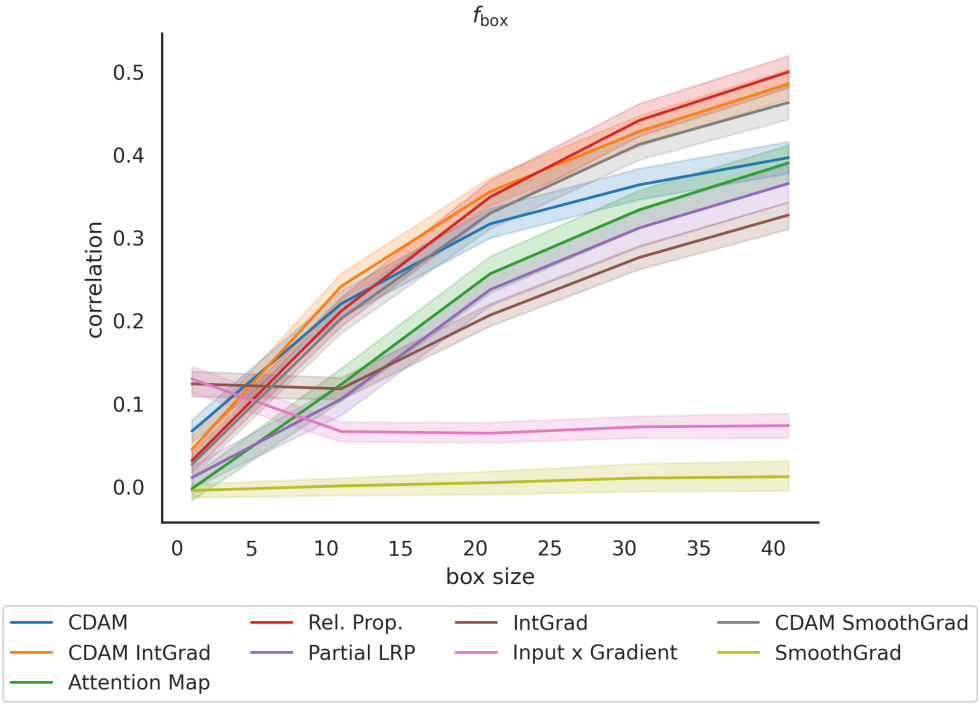

Figure S4: Box sensitivity curves obtained from the random ImageNet subset X_{val}. Refer to Section 3.5 for data description.

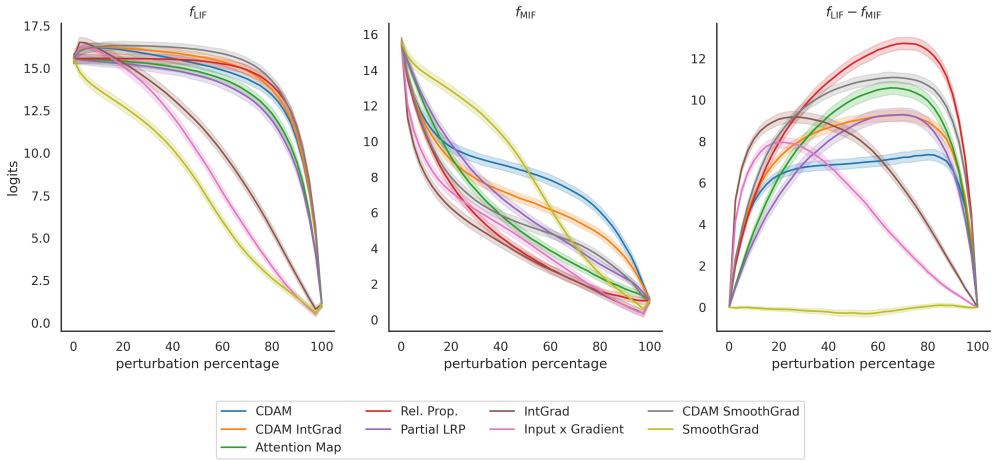

Figure S5: MIF/LIF perturbation curves obtained from the random ImageNet subset X_{val}. Refer to Section 3.5 for data description.

A.3 Examples of CDAMs from the ImageNet

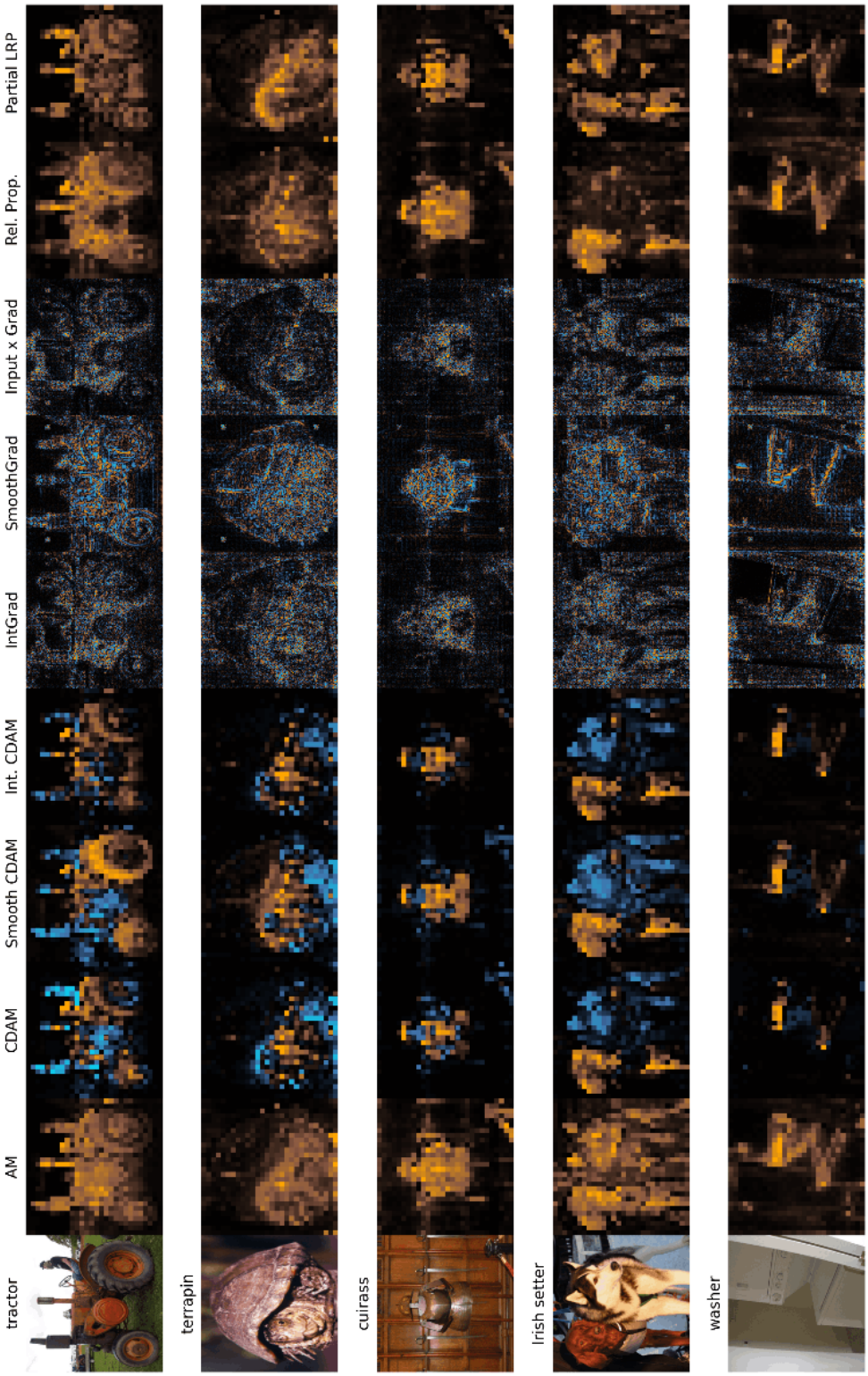

Figure S6: Examples for CDAM and other explanation methods on the ImageNet. The indicated class is the one predicted by the model and is the target for the explanation methods.

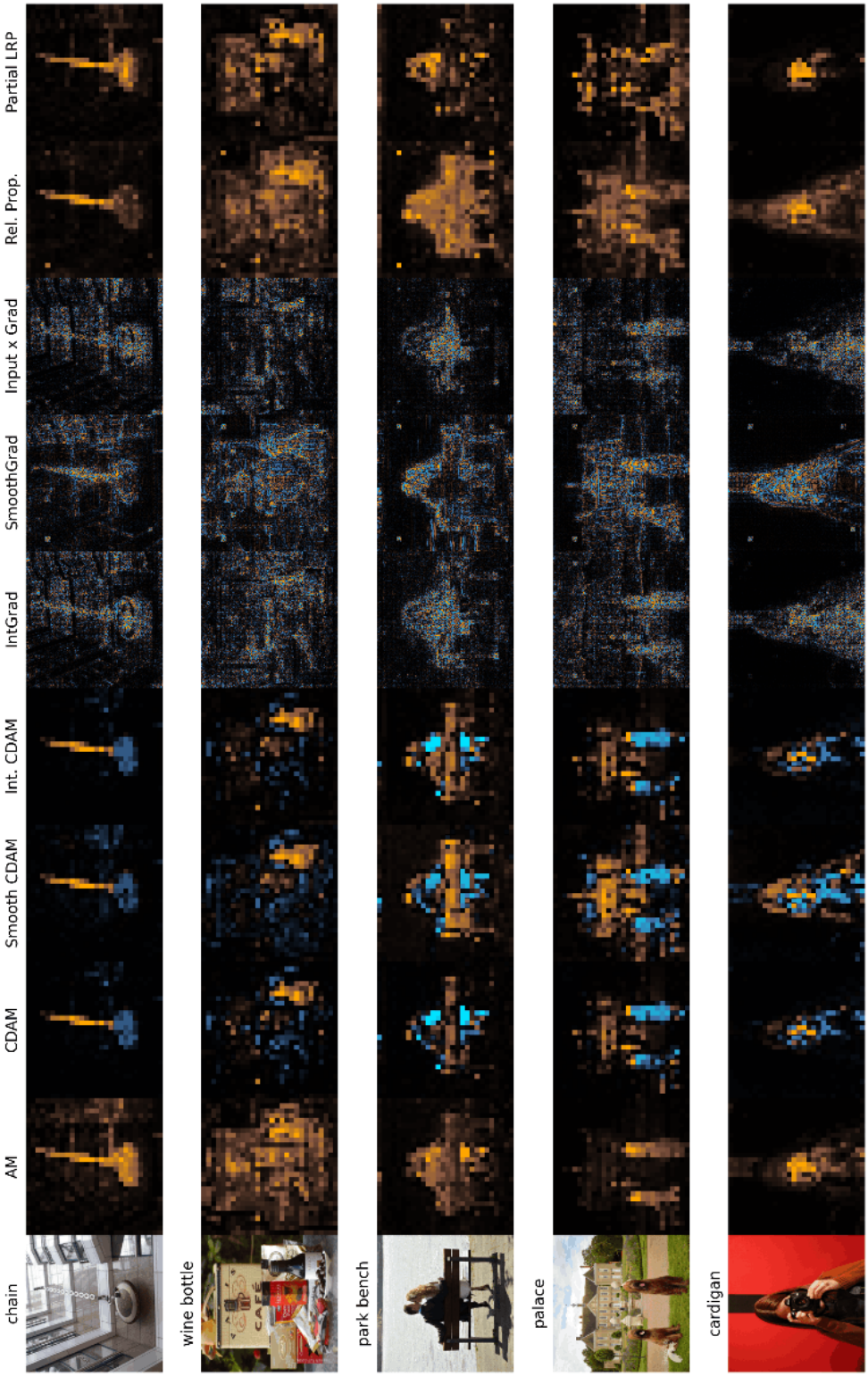

Figure S7: Examples for CDAM and other explanation methods on the ImageNet. The indicated class is the one predicted by the model and is the target for the explanation methods.

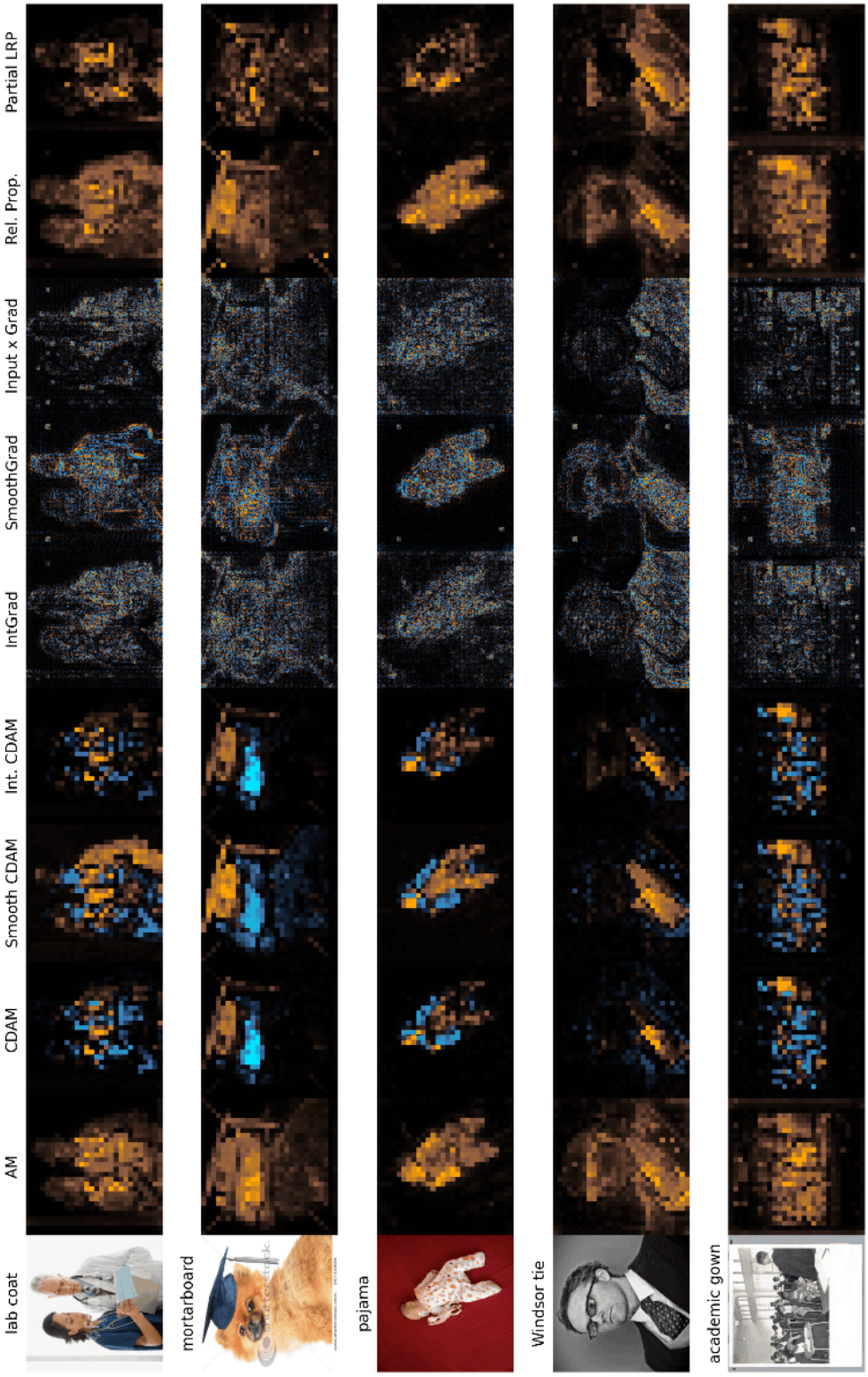

Figure S8: Examples for CDAM and other explanation methods on the ImageNet. The indicated class is the one predicted by the model and is the target for the explanation methods.

A.4 Examples for CDAMs from lung CT scans

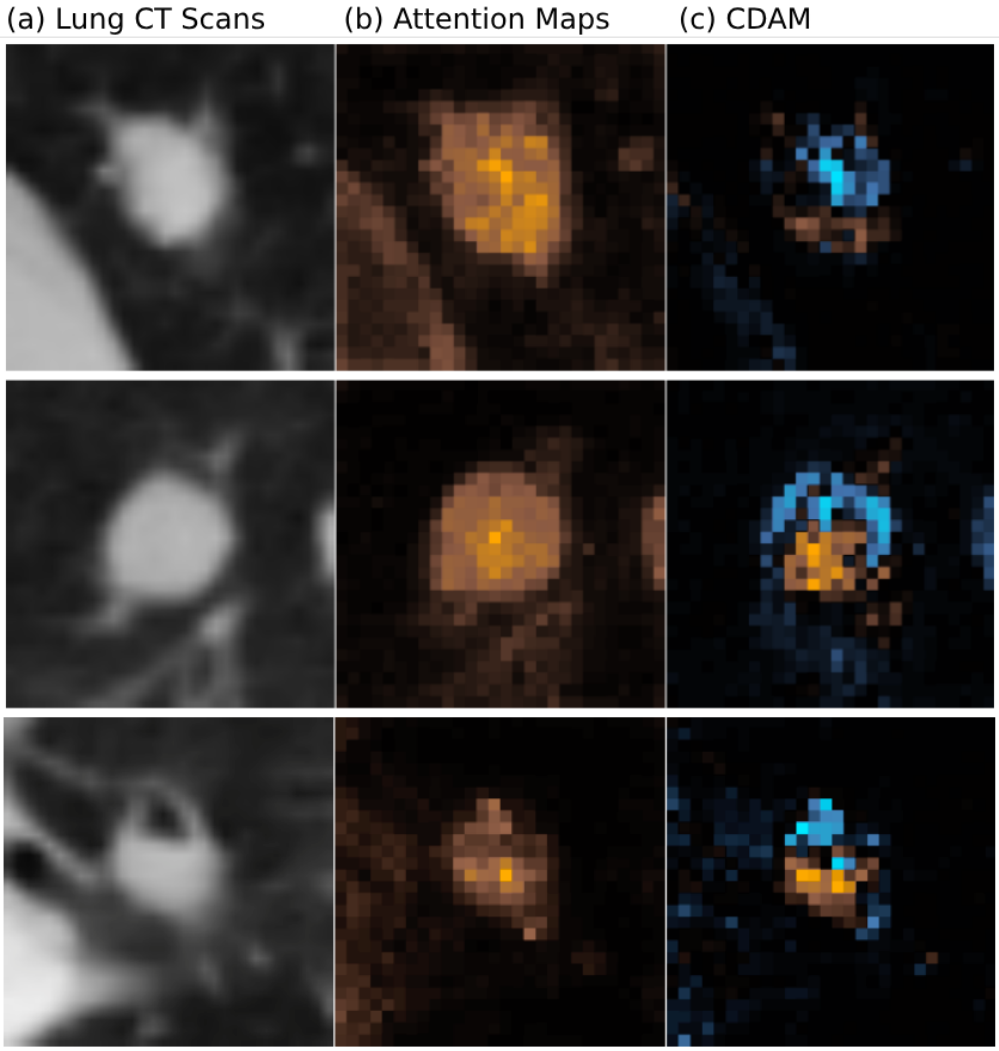

Figure S9: Explanations for the malignancy prediction model. A ViT-based classifier fine-tuned on the lung CT scans (LIDC) was used to predict benign vs. malignant lung nodules, followed by obtaining their attention maps and CDAMs. Orange and blue correspond to positive and negative values, respectively.

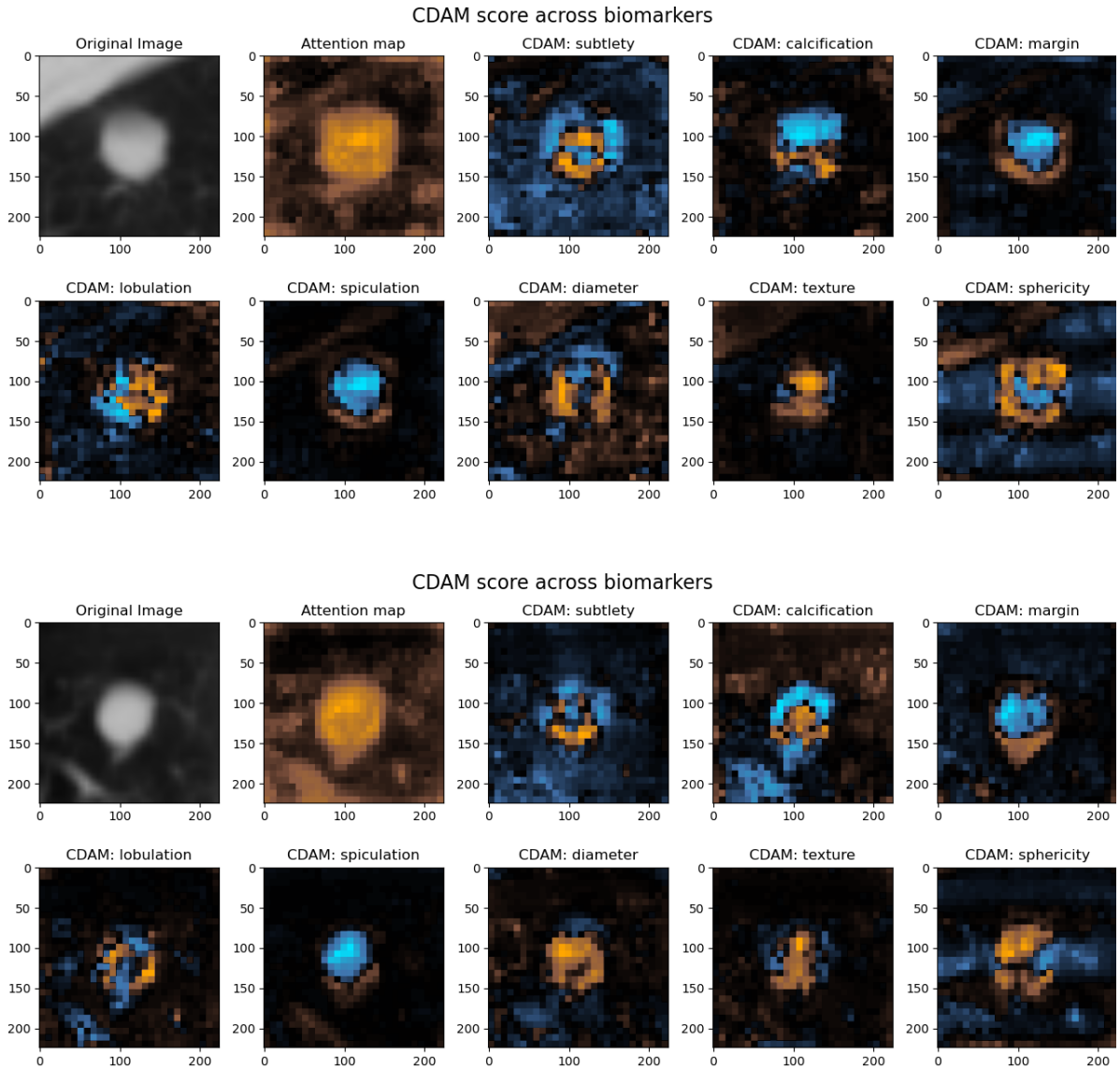

Figure S10: Examples for the Attention Map and CDAM based on a ViT biomarker model trained on the lung nodule data from LIDC.

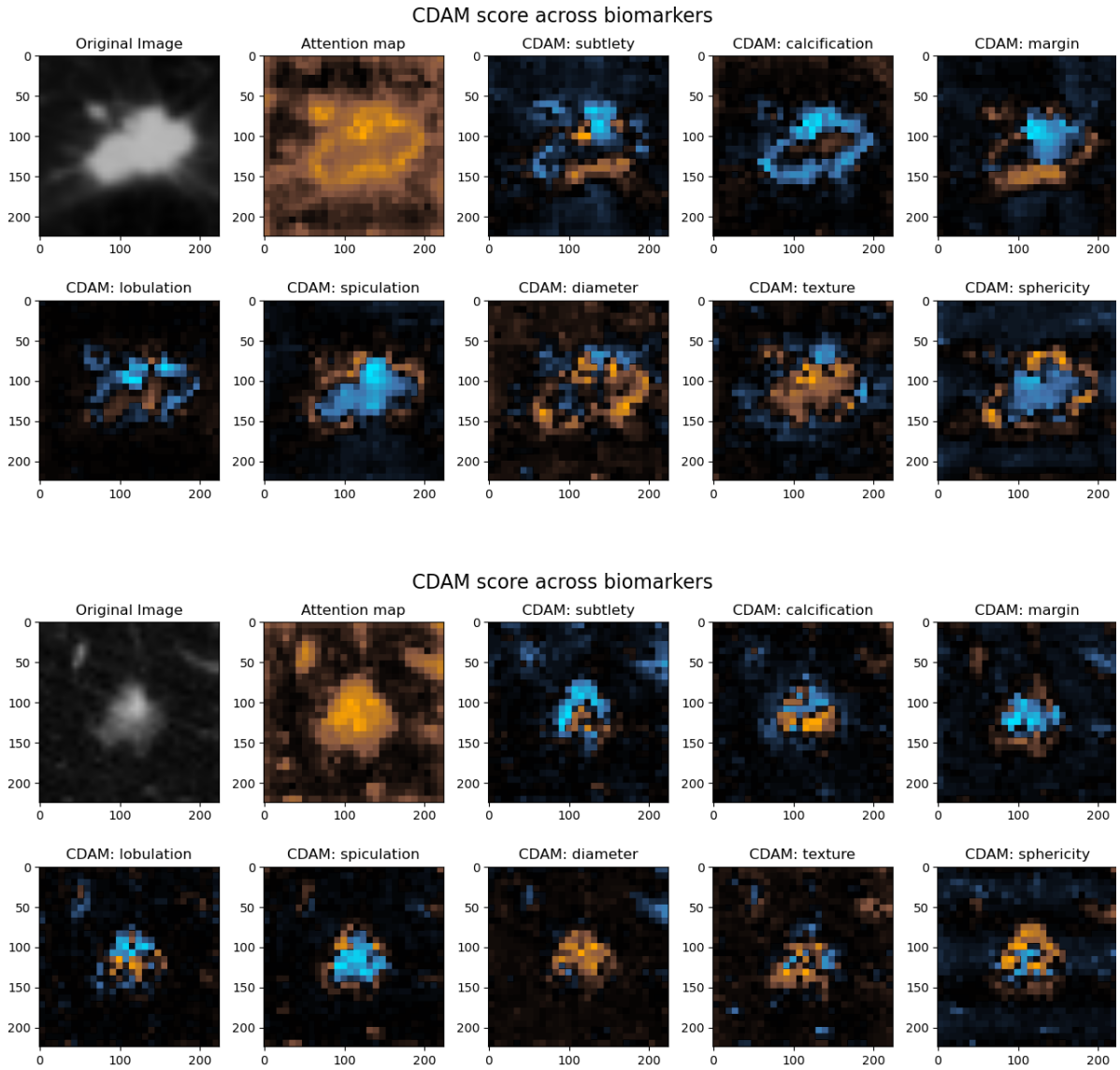

Figure S11: Examples for the Attention Map and CDAM based on a ViT biomarker model trained on the lung nodule data from LIDC.