ENSEMW2S: CAN AN ENSEMBLE OF LLMS BE LEVERAGED TO OBTAIN A STRONGER LLM?

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ABSTRACT

How can we harness the collective capabilities of multiple Large Language Models (LLMs) to create an even more powerful model? This question forms the foundation of our research, where we propose an innovative approach to weak-to-strong (w2s) generalization—a critical problem in AI alignment. Our work introduces an easy-to-hard (e2h) framework for studying the feasibility of w2s generalization, where weak models trained on simpler tasks collaboratively supervise stronger models on more complex tasks. This setup mirrors real-world challenges, where direct human supervision is limited. To achieve this, we develop a novel AdaBoost-inspired ensemble method, demonstrating that an ensemble of weak supervisors can enhance the performance of stronger LLMs across classification and generative tasks on difficult QA datasets. In several cases, our ensemble approach matches the performance of models trained on ground-truth data, establishing a new benchmark for w2s generalization. We observe an improvement of up to 14% over existing baselines and average improvements of 5% and 4% for binary classification and generative tasks, respectively. This research points to a promising direction for enhancing AI through collective supervision, especially in scenarios where labeled data is sparse or insufficient.

1 INTRODUCTION

As AI models, particularly Large Language Models (LLMs), continue to surpass human performance in various domains, a pressing challenge arises: how do we effectively supervise models that exceed our capabilities? This problem, known as super-alignment, is exacerbated by the scarcity of high-quality labeled data, which limits direct human oversight. The key question driving our work is whether weak models, trained on simpler tasks, can be leveraged to instruct and improve stronger models in complex settings—a problem known as weak-to-strong (w2s) generalization.

The concept of w2s generalization was introduced by Burns et al. (2023), where weak models are used to align stronger models in the absence of sufficient ground-truth supervision. However, while this work laid the groundwork, it left several critical challenges unresolved. **(C1) Single Weak Supervisor Limitation.** Prior studies (Burns et al., 2023; Ji et al., 2024; Charikar et al., 2024; Lang et al., 2024) tend to rely on a single weak supervisor, limiting the diversity and robustness of the supervision. A single model's perspective often falls short when attempting to instruct stronger models in more complex tasks, highlighting the need for a more diversified supervisory approach. **(C2) Lack of Focus on Weak Model Enhancement.** Another limitation is that previous research (Burns et al., 2023; Ji et al., 2024; Charikar et al., 2024; Lang et al., 2024) has focused predominantly on improving knowledge transfer from weak to strong models without addressing how to enhance the weak models themselves. This oversight leaves weak models under-optimized, thereby restricting their utility in complex problem settings. **(C3) Overlooking Task Complexity.** Furthermore, while task complexity plays a crucial role in determining how well weak models can supervise stronger ones, most prior work (Sun et al., 2024) has not adequately addressed this issue. For instance, Burns et al. (2023) briefly explored the impact of task complexity using chess data, but a more structured and systematic approach is needed to differentiate between easy and hard tasks and study their effects on supervision.

To address these challenges, we propose a novel ensemble-based method designed to improve w2s generalization. Central to our approach is an easy-to-hard (e2h) framework, which extends w2s generalization by focusing on the progression from simpler tasks (easy) to more complex tasks (hard).

This mirrors practical scenarios, where human oversight is more feasible for simpler tasks, and weak models must step in to guide stronger models in tackling harder tasks. In this setting, weak models trained on easy data supervise stronger models working on more difficult problems, creating a more pragmatic approach to w2s generalization.

To further enhance the capabilities of weak models, we develop a novel AdaBoost-inspired ensemble method for generation tasks, in addition to classification tasks. By combining the supervision of multiple weak models, we create a more robust and effective supervisory system for stronger LLMs. This ensemble approach overcomes the limitations of single-supervisor systems and introduces a mechanism to refine the weak models themselves, ensuring they can provide meaningful guidance even in complex tasks. Our experiments demonstrate that this ensemble method not only improves the weak models' generalization capabilities but also enables stronger models to achieve performance on par with oracle models trained on high-quality data.

The **main contributions** of this paper are the following:
(1) We introduce an ensemble method inspired by AdaBoost, combining weak LLMs to provide stronger supervision for training stronger models. Our approach is validated through experiments on binary classification tasks, where we observe improvements of up to 14% over baselines and an average improvement of 7% across all model pairs, showcasing the feasibility of w2s generalization.
(2) We extend this framework to supervised fine-tuning tasks for autoregressive LLMs, where our novel algorithm combines weak LLMs via a voting mechanism that adjusts token probabilities. In several cases, we observe our strong model trained using weak labels to outperform the strong model trained on ground truth, thus enabling effective supervision, even on complex tasks.
(3) We propose a practical easy-to-hard (e2h) framework for w2s generalization, where models trained on easy data provide supervision for harder tasks. This setup emphasizes the importance of task complexity and demonstrates significant improvements when weak models guide strong LLMs. For our EnsemW2S method, along with observing w2s-trained student models outperforming the strong student oracle in several e2h generalization scenarios, we also observe accuracy improvements of up to 10% over baselines and an average improvement of 3.34% and 4.4% for Quartz and ARC data respectively.

2 Weak-to-Strong Generalization via Easy-to-Hard Framework

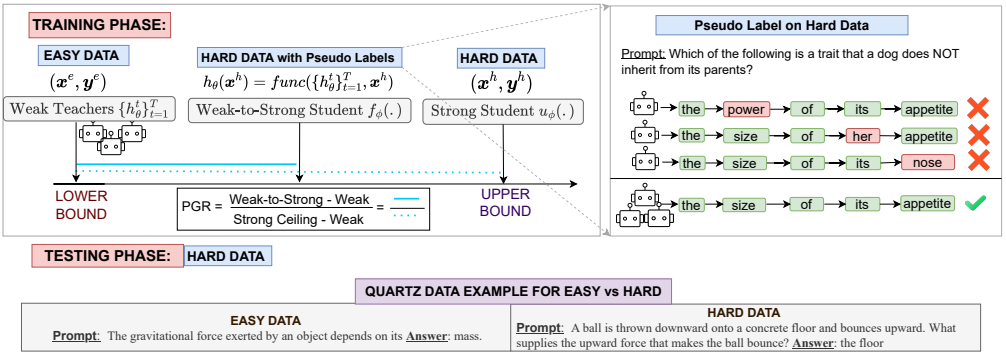

Figure 1: This figure illustrates the complete pipeline of our EnsemW2S method for easy-to-hard generalization using w2s generalization. In a realistic scenario, weak teachers are adept at answering easy questions but must supervise strong models to tackle hard problems. **In the leftmost portion**, we show that we train weak models on easy data, strong models on hard data, and transfer models on pseudo labels generated by the weak model on hard data. Ultimately, we aim to increase the Performance Gap Recovered (PGR). **On the right**, we depict how our EnsemW2S algorithm chooses the correct answer at the token level. **At the bottom**, we provide an example of easy and hard data for the Quartz dataset for e2h generalization, highlighting the importance of distinguishing between easy and hard data for realistic w2s generation.

The Overall Idea. We investigate the easy-to-hard framework as a more pragmatic setting to study the (im)possibility of w2s generalization. In this framework, weak models train on simpler tasks and subsequently instruct strong models to tackle more complex challenges, closely mirroring real-world conditions with limited human oversight. Figure 1 explains our idea and pipeline for easy-to-hard

generalization using w2s generalization. (Figure 7 in the Appendix provides the detailed algorithmic and data flow). In a realistic scenario, weak teachers are proficient in answering easy questions but must supervise strong models to tackle hard problems. We train weak models on easy data and strong models on hard data. A transfer model is trained using pseudo labels generated by the weak model on the hard data. Ultimately, we aim to improve the Performance Gap Recovered (PGR).

2.1 The Easy-to-Hard Framework

Weak Model h_θ as the Teacher. A state-of-the-art LLM h_θ is trained on a set of 'easy data' that we currently have access to labels, i.e., $(\boldsymbol{x}^e, \boldsymbol{y}^e)$. For example, this could be Go games, math problems, or common sense reasoning questions that we have solutions for. This 'weak teacher' is trained on the labeled easy data $(\boldsymbol{x}^e, \boldsymbol{y}^e)$. Although we refer to this model as a "weak teacher", it is only relatively weak compared to the strong model we aim to obtain. Moreover, the "easy data" is only relatively easy compared to the hard data for which we currently lack solutions. Thus, the easy data may not be simple but slightly easier than the hard data, which are currently unsolvable using existing models.

Strong Model u_ϕ as the Upper Bound. As an important part of our thought experiment, we establish an upper bound, which is not attainable in practice. Specifically, we assume access to the ground-truth labels of the hard data $(\boldsymbol{x}^h, \boldsymbol{y}^h)$, which is impractical but establishes an upper bound for this thought experiment. A model u_ϕ, larger than the weak teacher h_θ, is trained on the labeled hard data $(\boldsymbol{x}^h, \boldsymbol{y}^h)$. The reason why u_ϕ is larger than h_θ is that we believe a model strong enough to solve hard questions that no existing models can solve will require high capacity.

Weak-to-Strong Model f_ϕ Obtained in Practice. To test the weak-to-strong generalization, we will train a weak-to-strong transfer model f_ϕ that has the same capacity as the strong model, i.e., the same model size as u_ϕ, but is not trained under the unrealistic assumption of oracle access to hard labels. Rather, it is trained using weak teacher's feedback. Specifically, we consider using the pseudo-labeled $(\boldsymbol{x}^h, h_\theta(\boldsymbol{x}^h)$ as training data for training the weak-to-strong transfer model f_ϕ.

2.2 Easy and Hard Data

Dataset and Setup. We use the SciQ dataset (Welbl et al., 2017) for the binary classification task. It is a multiple-choice science question-answer dataset and is also used as one of the NLP classification datasets by Burns et al. (2023). We convert it into binary labels following (Burns et al., 2023). For the supervised fine-tuning (SFT) task on the Q/A dataset, we use ARC (Clark et al., 2018) and Quartz (Tafjord et al., 2019) datasets, which are also multiple-choice question-answer datasets, allowing us to generate multiple-choice pseudo labels. Ding et al. (2024) provide difficulty levels for some common mathematics and programming problems, chess puzzles, and reasoning question datasets, which can be further utilized to expand this work.

Easy $(\boldsymbol{x}^e, \boldsymbol{y}^e)$ and Hard $(\boldsymbol{x}^h, \boldsymbol{y}^h)$ Data Split. To generate difficulty ratings for our datasets, we employ the n-fold cross-validation method. We train the model on the $(n-1)$ out of n splits of the data and test on the remaining split. We repeat the process n times with different splits for testing each time and aggregate the errors. We use this error value for each sample as its difficulty rating. We split the low difficulty-rated data for weak model training and use the high difficulty-rated data to generate strong model training data and testing data randomly. We follow the same cross-validation method, with different training protocols, for generating difficulty for both binary classification and generation tasks. More details and our difficulty rating plots can be seen in Figures 8, 9, and 10 in the Appendix.

2.3 An Ensemble of Teachers

In a practical situation, we may face a dearth of strong supervisors but have an abundance of weak supervisors. Previous works (Burns et al., 2023; Ji et al., 2024) have used only one weak supervisor. Our work aims to combine the power of multiple weak supervisors to provide stronger supervision for better weak-to-strong (w2s) generalization. However, combining multiple weak supervisors to improve w2s generalization is challenging. In the following section, we detail how to combine a collection of weak teachers with diverse skill sets to obtain a competitive weak-to-strong model that is better than the weak model and ideally reaches or even surpasses the strong model, i.e., the upper bound of performance.

3 W2S GENERALIZATION VIA ENSEMW2S OF EXISTING DIVERSE TEACHERS

In this section, we introduce our ensemble based method to boost teachers. We first show how simple ensemble method (Adaboost) can be applied to a binary classification task for NLP datasets. Then we introduce EnsemW2S for more complex supervised fine-tuning task for multiple-choice Q/A datasets. A list of important notations is mentioned in Appendix C.2 for reference.

3.1 ADABOOST OF WEAK LLM TEACHERS FOR CLASSIFICATION TASKS

This simple thought experiment tests w2s generalization and is the first task evaluated by Burns et al. (2023). We utilize the vanilla AdaBoost (Algorithm 2, detailed in the Appendix C.3) to generate answer to hard questions, $\boldsymbol{x}^h$, from each weak LLM teacher, i.e., generate $h_\theta^t(\boldsymbol{x}^h)$ for $t \in \{1, \ldots, T\}$, where T is max Adaboost round. It works iteratively by focusing on the samples that are hardest to classify, assigning them higher weights in each subsequent iteration. The weak teachers are trained one at a time on the re-weighted training examples, as detailed in Line 5 of Algorithm 2. The only requirement is that they perform better than random, thus satisfying the well-known weak learning condition.

A weighted "majority vote/aggregation" is implemented to generate a consensus as the answer, $\mathbb{1}(\sum_{t=1}^{T} \alpha_t h_\theta^t(\boldsymbol{x}^h) > 0) \in \{0, 1\}$, also known as the pseudo-label, to the hard question $\boldsymbol{x}^h$. Here, the coefficients $\{\alpha_t \mid t \in \{1, \ldots, T\}\}$ are hyperparameters that weigh the weak learner's contributions based on their accuracy. A detailed mathematical summary of Adaboost is provided in Appendix section C.3.

AdaBoost leverages the "wisdom of the crowd" to obtain a stronger learner. Inspired by this philosophy, we use an ensemble of weak LLM teachers as "weak learners" to obtain a "stronger learner," i.e., a stronger model that improves binary classification tasks, eventually enabling better w2s generalization. These weak teachers represent a practical scenario where, although individually weak, they possess complementary knowledge like different human experts. Thus, when combined, they have the potential to form a stronger teacher.

3.2 ENSEMW2S: ADABOOST INSPIRED ALGORITHM FOR COMPLEX GENERATION TASKS

Challenges of Applying AdaBoost. The canonical AdaBoost algorithm assumes a sophisticated ensemble of feedback in the form of scores. However, LLMs are generative AI models known for their remarkable ability to generate coherent, free-form text. Applying the vanilla AdaBoost algorithm directly to generation tasks is challenging because (1) the output is not just a single class label but a sequence of text with no fixed length, and (2) different teachers may generate answers in various formats, making it non-trivial to combine their responses.

EnsemW2S: Our AdaBoost inspired Algorithm for Multiple-Choice Q/A Task. To address these challenges, we propose a modified multi-class generation based AdaBoost algorithm where the number of classes corresponds to the vocabulary size. We treat each token as an independent sample, as shown in Algorithm 1, and apply multi-class AdaBoost (Hastie et al., 2009) with major modifications described below, calling our algorithm EnsemW2S.

Token-Level Weighting. The first modification involves generating weights for each token within a sentence sample. We define the initial token-sample weights vector $D_1(i, j) \leftarrow \frac{1}{n}$ for all $i \in [m], j \in [k_i]$, where $n = \sum_{i=1}^{m} k_i$, k_i is the number of tokens in the answer part of each sample i, m is the total number of training data samples and j is the jth token in a particular chosen i^{th} sample. We update these weights, $D_t(i, j)$, for each iteration t of EnsemW2S.

Token-Level Data Sampling. We sample $S' = \{(\boldsymbol{x}_i'^e, \boldsymbol{y}_i'^e)\}_{i=1}^{m}$ from S using token-sample weights $D_t(i, j)$. By sampling with respect to probability masses $D_t(i, j)$ with repetition, we obtain a set of $n = \sum_{i=1}^{m} k_i$ tokens to train on. However, treating these n sampled tokens as independent training samples is very inefficient. Instead, we "assemble" the sampled tokens back into the sentences they belong to and implement label masking to only train on the sampled tokens in each sentence. Following this method, we can train on sampled tokens with minimal overheads.

Training and Generating New Weak Teachers. For each iteration, t, of EnsemW2S algorithm we train a new weak teacher model h_θ^t on the sampled data, S'.

Incorporating Prior Term. Following Hastie et al. (2009), multi-class boosting uses an additional $\log(c-1)$ term, where c is the number of classes, in the calculation of the AdaBoost parameter α. This term serves two purposes: (1) It enables the generation of weak models with accuracy above $\frac{1}{c}$ %, where $\frac{1}{c}$ % is random selection accuracy. This is crucial for smaller models and challenging tasks that cannot achieve 50% accuracy. (2) It ensures that α remains positive. Bayesian inference is used to provide proof of the benefits of this prior term. Given the large vocabulary size in our case, using $\log(c-1)$ will make all the α practically similar. Therefore, we introduce a different prior term $\log(\frac{1}{1-\epsilon_{pre}}-1)$, where ϵ_{pre} is the pre-trained model error of the chosen LLM. This term is sensible because it represents the error before fine-tuning the LLM, effectively replacing the random error baseline. Thus, the final α equation is: $\alpha_t \leftarrow \log(\frac{1-\epsilon_t}{\epsilon_t}) + \log(\frac{1}{1-\epsilon_{pre}}-1)$. Please refer to Appendix section C.4 for intuition behind the prior term.

Algorithm 1 Main Algorithm: EnsemW2S

Input: An "easy" Q/A training dataset with m examples: $S^e = \{(\boldsymbol{x}_i^e, \boldsymbol{y}_i^e)\}_{i=1}^m$; a pre-trained weak teacher model h_θ^0 parameterized by θ; total number of EnsemW2S iterations T; a "hard" unlabeled (questions only) dataset with O examples: $S^h = \{\boldsymbol{x}_o^h\}_{o=1}^O$

Output: Weak-to-Strong Student Model $f_\phi(\cdot)$

1: Initialize Token-Sample Weights: $D_1(i,j) \leftarrow \frac{1}{n}$ for all $i \in [m], j \in [k_i]$, where k_i is the token length in the ith easy example (i.e., $\boldsymbol{y}_i^e = (\boldsymbol{y}_i^{e,1}, \boldsymbol{y}_i^{e,2} ... \boldsymbol{y}_i^{e,k_i})$) and $n = \sum_{i=1}^m k_i$

2: Calculate pre-training error of h_θ^0: $\epsilon_{pre} \leftarrow \sum_{i=1}^m \sum_{j=1}^{k_i} \mathbb{1}\{h_\theta^0(\boldsymbol{x}_i^e, \boldsymbol{y}_i^{e,j-1}) \neq \boldsymbol{y}_i^{e,j}\} D_1(i,j)$

3: **for** $t \leftarrow 1$ to T **do**

4: Sample $S' = \{(\boldsymbol{x}_i'^e, \boldsymbol{y}_i'^e)\}_{i=1}^m$ from S using token-sample weights $D_t(i,j)$

5: **Train** a new weak teacher h_θ^t on S'

6: Calculate $\epsilon_t = \sum_{i=1}^m \sum_{j=1}^{k_i} \mathbb{1}\{h_\theta^t(\boldsymbol{x}_i^e, \boldsymbol{y}_i^{e,j-1}) \neq \boldsymbol{y}_i^{e,j}\} D_t(i,j)$

7: **if** $\epsilon_t \geq \epsilon_{pre}$ **then**

8: **break**

9: **Calculate** $\alpha_t \leftarrow \log \frac{1-\epsilon_t}{\epsilon_t} + \log(\frac{1}{1-\epsilon_{pre}} - 1)$

10: Update $D_{t+1}(i,j) \leftarrow \frac{1}{Z_t} D_t(i,j) e^{\alpha_t \mathbb{1}\{h_\theta^t(\boldsymbol{x}_i^e, \boldsymbol{y}_i^{e,j-1}) \neq \boldsymbol{y}_i^{e,j}\}}$ for all $i \in [m], j \in [k_i]$, where Z_t is a normalization factor such that $\sum_{i=1}^m \sum_{j=1}^{k_i} D_{t+1}(i,j) = 1$

11: **for** $o \leftarrow 1$ to O **do**

12: **for** $j \leftarrow 1$ to k_o **do**

13: Autoregressively generate the jth token of the "pseudo-answer" $\widehat{\boldsymbol{y}}_o^{h,j} \sim \Delta^{\text{vocab}}(\sum_{t=1}^T \alpha_t \cdot \text{softmax}(h_\theta^t([\boldsymbol{x}_o^h, \widehat{\boldsymbol{y}}_o^{h,1:j-1}])))$, where Δ^{vocab} denotes the simplex on the vocabulary

14: **Train** weak-to-strong student model $f_\phi(\cdot)$ on $\{(\boldsymbol{x}_o^h, \widehat{\boldsymbol{y}}_o^h)\}_{o=1}^O$

Weighted Error Calculation. Our weighted error equation ϵ_t also undergoes minor changes. The strict condition for each round of AdaBoost-inspired EnsemW2S training is that the weighted model error (calculated by comparing each token of each sample) must be less than the pre-training error, i.e., $\epsilon_t < \epsilon_{pre}$. The weighted model error ϵ_t is defined as, $\epsilon_t = \sum_{i=1}^m \sum_{j=1}^{k_i} \mathbb{1}\{h_\theta^t(\boldsymbol{x}_i^e, \boldsymbol{y}_i^{e,j-1}) \neq \boldsymbol{y}_i^{e,j}\} D_t(i,j) < \epsilon_{pre}$. Here, $\boldsymbol{y}_i^{e,j-1}$ is the $(j-1)^{\text{th}}$ ground-truth token in the answer part. The model $h_\theta^t(\boldsymbol{x}_i^e, \boldsymbol{y}_i^{e,j-1})$ predicts the next token and compares it with the ground-truth token $\boldsymbol{y}_i^j$.

Weight Update Equation. Our sample-weight update equation for each token is $D_{t+1}(i,j) \leftarrow \frac{1}{Z_t} D_t(i,j) e^{\alpha_t \mathbb{1}\{h_\theta^t(\boldsymbol{x}_i^e, \boldsymbol{y}_i^{e,j-1}) \neq \boldsymbol{y}_i^{e,j}\}}$ where Z_t is a normalization factor ensuring that the updated weights satisfy $\sum_{i=1}^m \sum_{j=1}^{k_i} D_{t+1}(i,j) = 1$. The main idea is to adjust the sample weights to emphasize misclassified examples, thereby guiding the sampling process for training the next weak learner.

Combining Teachers to Generate Pseudo Answers for Hard Questions: To combine the outputs of different teachers trained during the various EnsemW2S rounds, we scale the probability distribution for each token generated by the model h_θ^t in round t by its corresponding weight α_t. Specifically, we multiply α_t by the probability distribution vector of each token. We then aggregate these weighted distributions across all rounds, normalizing the resulting vector to form a new probability distribution for each token.

Using this aggregated distribution, we sample the final predicted token. The process is autoregressive, where the jth token of the "pseudo-answer" is generated as

$$\widehat{\boldsymbol{y}}_o^{h,j} \sim \Delta^{\text{vocab}} \left(\sum_{t=1}^{T} \alpha_t \cdot \text{softmax} \left(h_\theta^t \left([\boldsymbol{x}_o^h, \widehat{\boldsymbol{y}}_o^{h,1:j-1}] \right) \right) \right) \tag{1}$$

where Δ^{vocab} represents the simplex over the vocabulary.

By combining the outputs of multiple teachers, each trained in different EnsemW2S rounds, the ensemble approach leverages diverse perspectives from the weak models. Each teacher contributes its learned strengths, and through weighted aggregation, we diminish the influence of models that are less confident or less effective on certain tokens. This helps reduce variance in the generation process, ensuring that errors from individual weak models are mitigated. The result is a more robust pseudo-labeling system that is better aligned with the true distribution of the hard data, often yielding a performance improvement over any single weak model.

Unlike classification, where scores are combined over a fixed set of classes, generation tasks involve predicting sequences of tokens, where each prediction affects future ones. This makes combining generation probabilities more complex, as errors in early token predictions can propagate throughout the sequence. Additionally, we are aggregating probability distributions over large vocabularies, which introduces computational overhead and potential numerical instability.

Our method addresses these challenges by using a weighted combination of teacher models' token probabilities, ensuring that weaker predictions from individual rounds are minimized. By normalizing the aggregated distribution for each token, we maintain valid probability distributions across the vocabulary, effectively reducing the risk of cascading errors during autoregressive generation. This ensemble approach results in a more stable and accurate generation process, mitigating the issues inherent in sequence modeling.

Pseudo answer generation on multiple-choice datasets: On multiple-choice Q/A datasets, instead of using generated tokens $\widehat{\boldsymbol{y}}^h$ as pseudo answers, we can select one of the choices in the MCQ dataset using negative log-likelihood (NLL). Specifically, we calculate the NLL between the choices and $\widehat{\boldsymbol{y}}^h$ and select the choice with the lowest NLL. For datasets without multiple choices, we can directly use $\widehat{\boldsymbol{y}}^h$.

Train W2S Model: The strong student model, $f_\phi(\cdot)$, is trained using pseudo answers generated for the hard data $\{(\boldsymbol{x}_o^h, \widehat{\boldsymbol{y}}_o^h)\}_{o=1}^O$. While it might be beneficial to include the labeled easy data in the training process, we adhere to the pipeline established by Burns et al. (2023) by focusing exclusively on the hard examples to maintain consistency.

Ablation Studies. We experimented with combining the logits directly instead of probabilities but did not observe any improvement (refer to Appendix Figure 11). We conducted ablation studies where, instead of treating each token as independent, we used a sliding window of length L while calculating weights and aggregating errors (see Appendix Figure 12 and 13). Different window lengths did not cause significant changes in values, so we ultimately chose a window of $L = 1$. We also explored treating each sample as independent instead of each token as independent in the sample-answer part, finding better results with the latter. This is reasonable since the error calculated using independent-sample weights is less accurate.

Evaluation Metric. We used two metrics to evaluate this Q/A dataset. One is **(1) Token-wise comparison**, where we compare each predicted token and average the total error, and **(2) Option-wise comparison**, where we compare the negative log-likelihood (NLL) of the correct answer completion with the NLLs of the incorrect answer completions. Accuracy represents the number of entries where the correct answer completion has the lowest NLL among all choices.

4 Related Work

Weak-to-Strong (Burns et al., 2023) was the first to introduce the problem of weak-to-strong generalization for the super-alignment problem, where the ultimate aim is to elicit the full capabilities of the strong model using supervision only from weak models. (Charikar et al., 2024) provides a theoretical framework for the same with insights on how much w2s improvement can occur, though their work is limited to a few layer neural networks. Similarly, (Lang et al., 2024) provides bounds

on expansion properties using finite data distributions for when w2s generalization will happen, but only for simple binary classification tasks. (Zhang et al., 2024) proves that transcendence (exceeding the capability of the model that generates the training data) is possible for low-temperature sampling. Although this setting is not exactly w2s, it sheds light on this direction.

Several works have attempted to solve w2s generalization in LLMs. (Sang et al., 2024) tries to improve this supervision using ensemble learning and scalable oversight for binary classification NLP tasks but cannot observe significant improvement. (Ji et al., 2024) introduces a model that enhances the alignment of LLMs with human intentions by correcting the residual differences between aligned and unaligned answers by training on a query-answer correction dataset. This method boosts w2s generalization using supervisory signal from smaller models to improve the performance of complex systems. In (Sun et al., 2024), the authors propose a scalable approach for e2h generalization which involves training reward models on easier tasks and using them to evaluate performance on harder tasks. (Liu & Alahi, 2024) introduces a method similar to the classical hierarchical mixture of experts, where multiple specialized weak supervisors are used for weak-to-strong generalization instead of a single generalist model. (Bansal et al., 2024) compares large LLM training from data generated using weak (cheap) vs strong (expensive) model in a compute matching way and finds larger data from weaker model to provide better w2s.

Ensemble Learning Binary Classification Boosting (Freund & Schapire, 1997) and multi-classfication boosting (Hastie et al., 2009) are common ensemble learning algorithms. In (Verga et al., 2024), they use a voting mechanism to combine multiple small LLMs instead of a single large LLM to evaluate another LLM and show it performs better than large LLMs. An extended related work section is present in Appendix A.

5 Experimental Setup

We test two different strategies for each task. One aligns with Burns et al. (2023), where we split the training data randomly into train-weak and train-strong. Train-weak is used to train the weak model. Train-strong is used to train the strong and transfer models using pseudo labels generated using the weak model. The second strategy involves splitting the training data into easy and hard splits, where the easy data is now train-weak, and the hard data is now train-strong with the same training pipeline. This is also a more realistic setup for weak-to-strong generalization, as discussed in Section 1. For both strategies, we aim to recover the performance gap (PGR) and elicit the full capability of the strong model using an ensemble of weak models. The baseline in all experiments uses a single model for w2s generalization, following the principle of Burns et al. (2023).

We run AdaBoost/EnsemW2S algorithm 10 times for the binary classification tasks and 5 times for the generation tasks. We pick the best w2s performing round for our plots. However, we observe that all rounds ($n >= 2$) are better than the baseline ($n = 1$). Additionally, we chose single model performance ($n = 1$) for weak model performance.

5.1 Binary Classification Task

W2S Results with Random Training Data Splits. The baseline of this method is a replication of Burns et al. (2023). From Figure 2, by applying AdaBoost, we observe a significant improvement in the weak model accuracy, significantly improving the PGR values. In the case of the GPT-2-medium to GPT-2-large pair, we even see the PGR exceeding 100%, meaning that the transfer model has outperformed the strong model's performance. This is the ambitious aim of the w2s generalization problem, and our results show that w2s generalization is achievable.

W2S Results with Easy and Hard Training Data Splits. From Figure 2, we see that applying AdaBoost significantly improves weak model accuracy, thereby enhancing the PGR values. However, for this holistic e2h generalization problem, we are far from reaching the full capability of a strong model. For very small (GPT-2) and large model pairs (GPT-2-xl and above), we do not see improvement in w2s generalization despite the weak models' accuracy improvements. Overall, we observe an improvement of up to 14% in accuracy compared to the baseline and an average improvement of 6.52% and 3% for random and easy-hard splits, respectively.

Scaling Law: In Figure 2 (line plot), we see less PGR recovery for the Qwen-1.8B model even though it is similar in size to GPT-2-xl. Similarly, in the bar plot, we see a drastic difference between the oracle performance of GPT2xl and Qwen-1.8B. This is because the Qwen models series are more

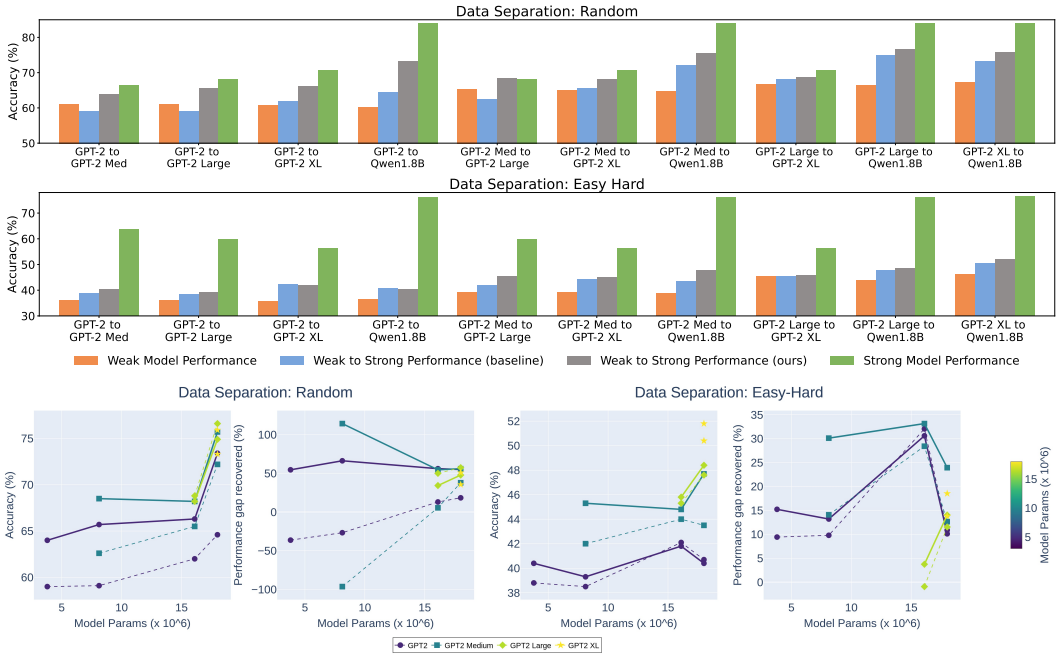

Figure 2: **Binary Classification Task: Top figure** shows a bar plot comparing w2s generalization of our method (grey) with a baseline (blue) from Burns et al. (2023) using accuracy values(%) for different combinations of weak and strong model pairs for random data split (top bar-plot) and easy-hard split(bottom bar-plot). **Bottom figure** shows a line plot comparing the accuracy and performance gap recovered values (PGR). The left two figures are for random data split, while the right two figures are for the easy-hard split to show e2h generalization.

capable even after being the same size. Thus, model size is not a good metric, but model capability is a better metric for differentiating between weak and strong models.

Better metric: Figure 2 shows the accuracy and PGR plots for both random and easy-hard split. We observe that PGR is not very informative, as it can produce extremely large or even negative values. In the w2s experiments, large values occur because the ensemble of weak models becomes strong enough to match or exceed a strong model, improving w2s generalization. Negative values, seen in baseline experiments, indicate the transfer model performed worse than the weak model, often when the strong model fails to learn and its inductive bias becomes random with pseudo-label training. Similar patterns are seen in Figure 5 and 4. (Refer to Appendix Table 1 and 2 for more details.)

5.2 Generation Task for Multiple Choice Dataset

5.2.1 Comparing Weak model's performance

In Figure 3, we compare the performance of a single weak model (dark color) with combined weak models after 5 rounds of EnsemW2S algorithm. Smaller models show greater improvement, which is expected since boosting works best when weak models are diverse. Using EnsemW2S, smaller models can diversify through the data sampling step; however, larger models tend to learn all possible information and cannot learn something different with each round. Also, we use token error in Figure 3 since it is a more precise metric to measure improvement in weak models.

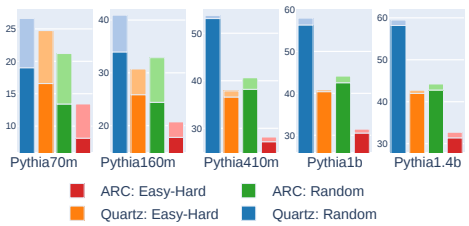

Figure 3: Performance comparison of a single weak model (dark color) with the combined weak models (Lighter hue shows improvement).

5.2.2 Comparing Strong model's performance

Here, we use the multiple-choice classification accuracies to calculate the accuracy of all our plots. We show the accuracy values of token-wise metrics in the Appendix tables.

W2S Results with Random Training Data Splits. From Figure 4 and 5, we see that w2s training using an ensemble of teachers almost consistently outperforms the baseline (single teacher). Thus, ensemble learning is beneficial. We can see the trend of accuracy and performance gap recovered for the different model pairs in Figure 4 and 5 for Quartz and ARC datasets, respectively. For Quartz data, we see that our PGR percentage (Figure 4) improves as the model scales up except when the weak model is the smallest sized model (pythia-70m). This could be because the increasing capability difference between the small and large models makes it difficult for the strong model to learn anything from the weak. This trend is the same in the baseline as well as our EnsemW2S. But an important thing to note is that for some cases for both ARC and Quartz data, our method generates a large PGR percentage of >=100%, showing the ability of our w2s method to recover the performance gap.

W2S Results with Easy-Hard Training Data Splits. From Figure 4 and 5, we see that w2s training using an ensemble of teachers almost consistently outperforms the baseline (single teacher). Thus showing that ensemble learning is beneficial. Our method shows more improvement over baseline for easy-hard data split as compared to random split. This is because of two reasons. Firstly, the power of combining weak models using our modified AdaBoost is more useful when all of them are weak but slightly different from each other. Secondly, by easy and hard splitting, the margin between weak and strong increases more, giving more room for improvement.

We also observe that PGR for e2h generalization is significantly lower, highlighting the complexity of the e2h generalization problem. We hope this work could motivate researchers to build more sophisticated methods for this more complex e2h generalization problem. Another simple observation is as the models become more capable, both the performances (baseline and ours) increase.

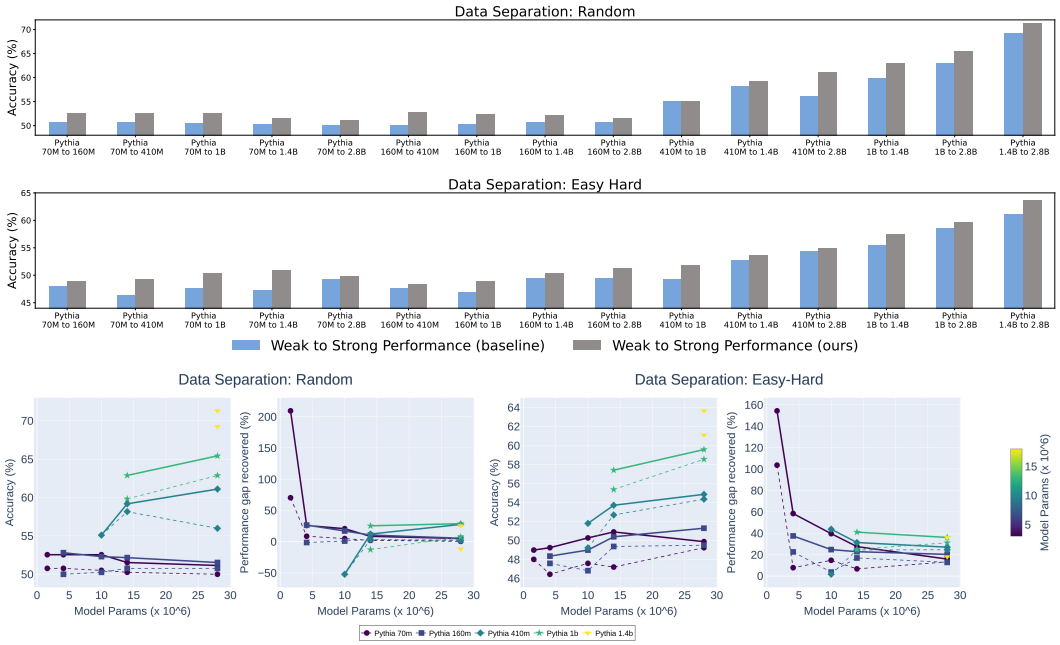

Figure 4: **Generation Task (Quartz Data): Top figure** shows a bar plot comparing the w2s generalization of our method (grey) with a baseline (blue) for various combinations of weak and strong model pairs for the SFT task on Q/A data for random data split (top bar-plot) and easy-hard split (bottom bar-plot). **Bottom figure** shows a line plot comparing accuracy and PGR. The left two figures are for random data split, while the right two are for the easy-hard split to show e2h generalization.

Note: Refer to Appendix Table 3 and 6 for detailed values of our experiments for Quartz and ARC datasets, respectively, for random data split. Appendix Figure 14 and Fig. 16 show bar plots with weak and strong (oracle) model performance for the Quartz and ARC datasets, respectively, for the random split. For easy-hard data split, the same details can be found in Appendix Tables 4, 7 and Figure 15 and 17.

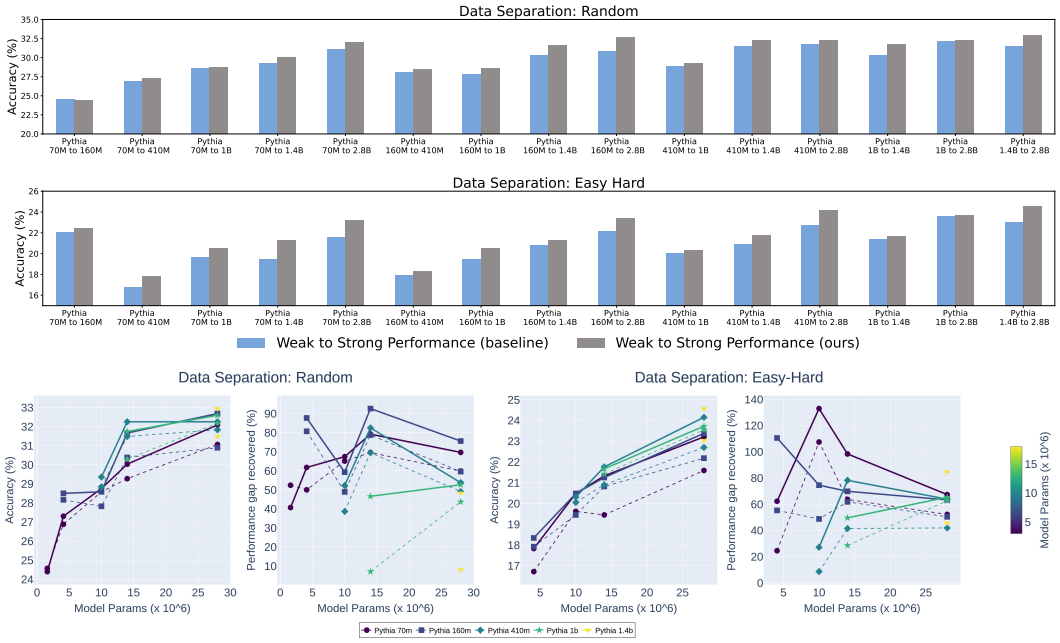

Figure 5: **Generation Task (ARC Data): Top figure** shows a bar plot comparing the w2s generalization of our method (grey) with a baseline (blue) for various combinations of weak and strong model pairs for the SFT task on Q/A data for random data split (top bar-plot) and easy-hard split (bottom bar-plot). **Bottom figure** shows a line plot comparing accuracy and PGR. The left two figures are for random data split, while the right two are for the easy-hard split to show e2h generalization.

5.2.3 PERFORMANCE ON HARD DATA AFTER TRAINING ON WEAK VS STRONG DATA

We conduct this experiment to motivate the importance of e2h with w2s generalization. For the Quartz dataset in Table 6, we see a significant margin of improvement when trained on hard data for the larger models, showing larger models are more capable of understanding complicated data. With ARC, we see improvement in all models but with a lesser margin, implying that ARC data has a lesser disparity between easy and hard samples.

	Quartz		ARC	
Model Size	**Easy Split**	**Hard Split**	**Easy Split**	**Hard Split**
pythia-70m	49.11	**50.13**	21.42	**25.26**
pythia-160m	**48.47**	46.43	21.85	**22.10**
pythia-410m	51.50	**51.50**	18.01	**18.95**
pythia-1b	53.32	**56.77**	19.80	**22.10**
pythia-1.4b	60.34	**63.78**	21.42	**21.42**
pythia-2.8b	66.84	**70.41**	25.09	**26.71**

Figure 6: Accuracy (%) values for LLMs trained on easy vs hard data and evaluated on hard data.

6 CONCLUSION, LIMITATION AND FUTURE WORK

Conclusion: This paper aims to stimulate discussion on the more holistic problem of weak-to-strong generalization by emphasizing easy-to-hard generalization. We develop a new AdaBoost-inspired algorithm and conduct a thought experiment on how to combine the "wisdom of the crowd" to improve w2s generalization. We are first to focus on the idea of making the weaks less weak using an ensemble, and test our method for binary classification and Q/A-based SFT task. Our method in some cases recovers full strong model capability.

Limitation and Future Work: This work only explores the supervised fine-tuning phase. While SFT is an important part of the LLM learning pipeline, our future work will focus on developing weak supervision in the reward modeling phase. Another interesting future direction would be to improve the combination of tokens in the decoding phase by replacing the classical AdaBoost algorithm with more adaptive ensemble learning methods. We hope this work sparks discussion on combining multiple LLMs to improve weak-to-strong generalization.

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A RELATED WORKS

Weak-to-Strong Generalisation: (Continue from the main manuscript) Guo et al. (2024) introduces an dynamic adjustable loss function for weak-to-strong supervision. Hase et al. (2024) demonstrates that current language models can achieve high performance on difficult tasks by training on simpler, cleanly labeled data, thus avoiding the high costs and noise associated with hard data labeling. None of these works focused on making the weak teachers, less weak but only focus on improving transfer learning and correction of weak labels. Thus, our method can be combined with all ideas focused on improving transfer learning.

Multi-LLM learning: There are numerous works involving the collaboration of multiple LLMs. Chang et al. (2023) proposes Reinforcement Learning with Guided Feedback (RLGF), where a dynamic black-box guide like GPT-3 is used to fine-tune large language models. Rosset et al. (2024) introduces Direct Nash Optimization (DNO), a scalable algorithm that combines contrastive learning with general preference optimization. Cai et al. (2024) presents MEDUSA, an innovative framework designed to accelerate inference in large language models by introducing multiple decoding heads, enabling simultaneous prediction of several tokens, and enhancing efficiency through reduced decoding steps and parallel processing capabilities. Shen et al. (2024) proposes Co-LLM, a collaborative decoding framework that interleaves token-level generations from multiple models. This method optimizes the latent variable model for marginal likelihood, allowing a base model to decide when to generate tokens itself or utilize an assistant model, thereby improving performance across various specialized tasks without direct supervision. Jin et al. (2024) introduces a novel collaborative decoding framework aimed at improving the factuality of large language models by employing a critical token classifier. This approach strategically uses both pre-trained and aligned models to selectively generate critical tokens, significantly enhancing the model's ability to maintain factual accuracy without compromising the diversity of the generated content.

Additionally, Mudgal et al. (2023) introduces Controlled Decoding (CD), a method for aligning language model outputs with desired outcomes using a separate prefix scorer module. This approach allows multi-objective RL without additional training and performs well on benchmarks, bridging the gap between token-level control and sequence-level best-of sampling strategies.

B LIMITATION AND FUTURE WORK

(Continue from main manuscript)

Computational Overhead: For fully generative tasks, multiple forward passes are required in an autoregressive manner. At each step, the final voted token is input to all LLMs to predict the next token. This increases generation time, which can be mitigated using efficient decoding algorithms like speculative decoding. Addressing this also forms part of our future work. *Smaller Models:* Another limitation is of all w2s work is they attempt to mimic the weak and strong setting as an analogy to the realistic problem and cannot test on a real human with super-human model.

C Details on the Methodology

C.1 Detailed Flowchart

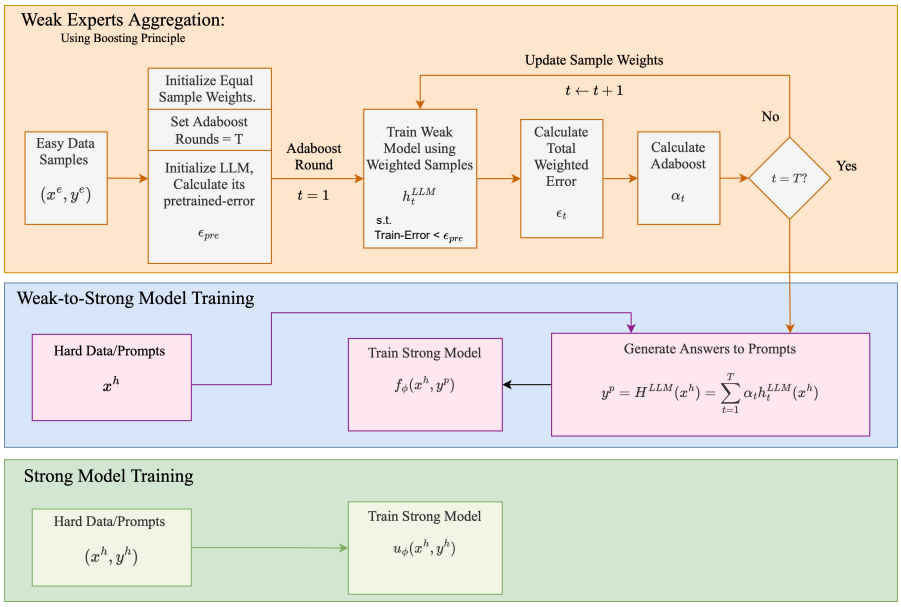

Figure 7: This figure explains our pipeline for easy-to-hard generalization using w2s generalization in complete detail including the algorithm and data flow. We train weak models on easy data and strong models on hard data. A transfer model is trained using pseudo labels generated by the weak model on the hard data. Ultimately, we aim to improve the Performance Gap Recovered (PGR).

C.2 Important Notations

Easy Data: $\{(\boldsymbol{x}_i^e, \boldsymbol{y}_i^e)\}_{i=1}^m$

Hard Data: $\{(\boldsymbol{x}_o^h, \boldsymbol{y}_o^h)\}_{o=1}^O$

Total number of Easy Data points: m

Total number of Hard Data points: O

Total EnsemW2S-AdaBoost Rounds: T Weak Teachers: $\{h_\theta^t\}_{t=1}^T$

Strong Student (Oracle): u_ϕ

Weak-to-Strong model: f_ϕ

Total number of tokens in the answer part of each sample i: k_i

AdaBoost voting parameter: $\{\alpha_t\}_{t=1}^T$

EnsemW2S-AdaBoost token-sample weights for i^{th} sample and j^{th} token: $\{D_t(i,j)\}_{t=1}^T$

Pre-trained Model error: ϵ_{pre}

EnsemW2S-AdaBoost's weighted model error for round t: ϵ_t

C.3 Adaboost

AdaBoost is an ensemble learning algorithm that combines multiple weak classifiers, such as decision stumps, to create a strong classifier. It works iteratively by focusing on the samples that are hardest to classify, assigning them higher weights in each subsequent iteration. Weak classifiers are trained

one at a time, and their contributions are weighted based on their accuracy. The final prediction is made by taking a weighted majority vote of all weak classifiers. AdaBoost is known for its ability to improve generalization by focusing on difficult cases and is often resistant to overfitting with simple weak learners. However, it can struggle with noisy data if overemphasis is placed on misclassified samples. Its also presented as Algorithm 2.

Let the training dataset consist of m samples:

$$\{(x_i, y_i) \mid i = 1, 2, \ldots, m\}, \quad x_i \in \mathbb{R}^d, \quad y_i \in \{-1, +1\}.$$

Each weak learner $h_t(x)$ outputs a prediction $h_t(x_i) \in \{-1, +1\}$. The goal is to sequentially train weak learners such that the combined model minimizes the classification error. A weight distribution $D_t(i)$ is maintained over the training samples at each iteration t, where:

$$D_t(i) \geq 0, \quad \sum_{i=1}^{m} D_t(i) = 1.$$

Initially, all samples are equally weighted: $D_1(i) = \frac{1}{m}, \quad \forall i$

Training the Weak Learners: For each iteration $t = 1, 2, \ldots, T$, train a weak learner $h_t(x)$ using the current weight distribution D_t. Compute the weighted error:

$$\epsilon_t = \sum_{i=1}^{m} D_t(i) \cdot \mathbb{I}(h_t(x_i) \neq y_i),$$

where $\mathbb{I}(\cdot)$ is the indicator function.

Weak Learner Weight Assign a weight α_t to the weak learner based on its performance:

$$\alpha_t = \frac{1}{2} \ln \left(\frac{1 - \epsilon_t}{\epsilon_t} \right)$$

Intuition behind it is that if ϵ_t is small, α_t is large, giving more importance to the weak learner. If $\epsilon_t = 0.5$, $\alpha_t = 0$, indicating no contribution to the ensemble. $\epsilon_t > 0.5$ is undesirable, as the weak learner performs worse than random guessing.

Update the weights of the training samples to focus on misclassified samples:

$$D_{t+1}(i) = \frac{D_t(i) \exp(-\alpha_t y_i h_t(x_i))}{Z_t},$$

where Z_t is a normalization factor ensuring $\sum_{i=1}^{m} D_{t+1}(i) = 1$:

$$Z_t = \sum_{i=1}^{N} D_t(i) \exp(-\alpha_t y_i h_t(x_i)).$$

Misclassified samples ($y_i \neq h_t(x_i)$) receive higher weights, making them more influential in the next iteration. The **final strong classifier** $H(x)$ is a weighted majority vote of the weak learners:

$$H(x) = \text{sign} \left(\sum_{t=1}^{T} \alpha_t h_t(x) \right).$$

Generalization Abilities: AdaBoost improves generalization by maximizing the margins on the training set. The margin for a sample (x_i, y_i) is defined as:

$$\text{Margin}(x_i) = y_i \sum_{t=1}^{T} \alpha_t h_t(x_i).$$

AdaBoost aims to increase the margin for all samples, reducing the chance of misclassification.

Summary of Key Properties

a) **Sequential Training:** Weak learners are trained iteratively, with weights updated to focus on difficult samples.

b) **Weighting Scheme:** Misclassified samples are emphasized in subsequent iterations.

c) **Generalization:** AdaBoost achieves strong generalization by maximizing margins and minimizing exponential loss.

d) **Flexibility:** It can work with any weak learner as long as the learner achieves performance slightly better than random guessing.

Algorithm 2 AdaBoost Freund & Schapire (1997)

Input: Training Dataset $S = \{(x_i, y_i)\}_{i=1}^{m} \sim D^m$
$T =$ AdaBoost iterations
$\vec{D}_1(i) \leftarrow \frac{1}{m} \forall i \in [m]$
for $t \leftarrow 1$ to T **do**
  h_t such that $\epsilon_t = \sum_{i=0}^{m} \mathbb{1}\{h_t(x_i) \neq y_i\} \vec{D}_t(i) < \frac{1}{2}$
  $\alpha_t \leftarrow \frac{1}{2} \log \frac{1-\epsilon_t}{\epsilon_t}$
  $Z_t \leftarrow 2\sqrt{\epsilon_t(1-\epsilon_t)}$
  $\vec{D}_{t+1} \leftarrow \frac{1}{Z_t} \vec{D}_t e^{-\alpha_t y_i h_t(x_i)}$
  $g \leftarrow \sum_{t=1}^{T} \alpha_t h_t$
Return $h(x) = \text{sign}(g)$

C.4 Intuition Behind Prior Term in EmsemW2S

The calculation of α cannot rely solely on error, ϵ, as the traditional Adaboost method is valid only when $\epsilon < 0.5$. Applying the same equation in our context could yield negative α values. We introduce a prior term, $\log(\frac{1}{1-\epsilon_{pre}} - 1)$, inspired from multi-class classification Adaboost works Hastie et al. (2009), to address this issue.

Existing works on multi-class classification Adaboost Hastie et al. (2009) suggest using $\frac{1}{c}$ (where c is the number of classes) in the prior term, $\log(c-1)$, as $\frac{1}{c}$ represents the random performance of the model. However, when c (the number of classes) becomes very large, the $\log(c-1)$ term also grows significantly, causing the α parameters of Adaboost to become nearly identical and, consequently, less useful. To address this, we introduce a pre-training error term, ϵ_{pre}, which represents an upper bound on the sample error. We then use $1 - \epsilon_{pre}$ (a lower bound on accuracy) as a replacement for the $\frac{1}{c}$ term, as our model's lowest possible accuracy is $1 - \epsilon_{pre}$, not $\frac{1}{c}$.

D Binary Classification Task

D.1 Detailed Results for Binary Classification Task with α and Err_t^{Train} in Table 1 and Table 2

Table 1: This table shows weak to strong generalization using random data-splits for sciq dataset. We also study the impact of using ensemble learning methods like AdaBoost, which combines weak learners, for weak to strong training. Each model is trained for 3 epochs and uses an optimized learning rate.

AdaBoost	Weak Model	Strong Model	Weak-to-Strong Model	α	Err_i^{train}
Model Name	GPT-2	GPT-2 Medium			
Baseline	0.610	0.665	0.590	0.455	0.287
With AdaBoost (T:02)	0.613	0.665	0.619	0.488	0.274
With AdaBoost (T:03)	0.614	0.665	0.609	0.463	0.284
With AdaBoost (T:04)	0.611	0.665	0.622	0.467	0.282
With AdaBoost (T:05)	**0.623**	**0.665**	**0.640**	0.448	0.290
With AdaBoost (T:06)	0.621	0.665	0.641	0.333	0.340
With AdaBoost (T:07)	0.646	0.665	0.638	0.433	0.300
With AdaBoost (T:08)	0.610	0.665	0.626	0.471	0.281
With AdaBoost (T:09)	0.634	0.665	0.619	0.463	0.284
With AdaBoost (T:10)	0.618	0.665	0.622	0.503	0.268
Model Name	GPT-2	GPT-2 Large			
Baseline	0.610	0.681	0.591	0.455	0.287
With AdaBoost (T:02)	**0.613**	**0.681**	**0.657**	0.488	0.274
With AdaBoost (T:03)	0.614	0.681	0.620	0.463	0.284
With AdaBoost (T:04)	0.611	0.681	0.629	0.467	0.282
With AdaBoost (T:05)	0.623	0.681	0.656	0.448	0.290
With AdaBoost (T:06)	0.621	0.681	0.650	0.333	0.340
With AdaBoost (T:07)	0.646	0.681	0.654	0.433	0.300
With AdaBoost (T:08)	0.610	0.681	0.633	0.471	0.281
With AdaBoost (T:09)	0.634	0.681	0.648	0.463	0.284
With AdaBoost (T:10)	0.618	0.681	0.652	0.503	0.268
Model Name	GPT-2	GPT-2 XL			
Baseline	0.607	0.707	0.620	0.455	0.287
With AdaBoost (T:02)	0.613	0.707	0.654	0.488	0.274
With AdaBoost (T:03)	0.614	0.707	0.628	0.463	0.284
With AdaBoost (T:04)	**0.611**	**0.707**	**0.663**	0.467	0.282
With AdaBoost (T:05)	0.623	0.707	0.645	0.448	0.290
With AdaBoost (T:06)	0.621	0.707	0.648	0.333	0.340
With AdaBoost (T:07)	0.646	0.707	0.649	0.433	0.300
With AdaBoost (T:08)	0.610	0.707	0.653	0.471	0.281
With AdaBoost (T:09)	0.634	0.707	0.657	0.463	0.284
With AdaBoost (T:10)	0.618	0.707	0.654	0.503	0.268
Model Name	GPT-2	Qwen1.5-1.8B			
Baseline	0.602	0.842	0.646	0.445	0.291
With AdaBoost (T:02)	0.599	0.842	0.683	0.500	0.269
With AdaBoost (T:03)	0.626	0.842	0.702	0.444	0.292
With AdaBoost (T:04)	0.611	0.842	0.723	0.400	0.310
With AdaBoost (T:05)	0.613	0.842	0.704	0.461	0.285
With AdaBoost (T:06)	**0.613**	**0.842**	**0.734**	0.417	0.303
With AdaBoost (T:07)	0.603	0.842	0.712	0.422	0.301
With AdaBoost (T:08)	0.608	0.842	0.717	0.319	0.346
With AdaBoost (T:09)	0.614	0.842	0.712	0.405	0.308
With AdaBoost (T:10)	0.606	0.842	0.712	0.360	0.328
Model Name	GPT-2 Medium	GPT-2 Large			
Baseline	0.653	0.681	0.626	0.705	0.196
With AdaBoost (T:02)	0.656	0.681	0.643	0.624	0.223
With AdaBoost (T:03)	0.646	0.681	0.639	0.674	0.206
With AdaBoost (T:04)	0.663	0.681	0.664	0.645	0.216
With AdaBoost (T:05)	0.645	0.681	0.654	0.690	0.201
With AdaBoost (T:06)	0.652	0.681	0.667	0.619	0.225
With AdaBoost (T:07)	0.650	0.681	0.665	0.722	0.191
With AdaBoost (T:08)	**0.657**	**0.681**	**0.685**	0.733	0.187
With AdaBoost (T:09)	0.651	0.681	0.684	0.601	0.231
With AdaBoost (T:10)	0.648	0.681	0.666	0.682	0.203
Model Name	GPT-2 Medium	GPT-2 XL			
Baseline	0.653	0.707	0.655	0.705	0.196
With AdaBoost (T:02)	0.656	0.707	0.651	0.624	0.223
With AdaBoost (T:03)	0.646	0.707	0.648	0.674	0.206
With AdaBoost (T:04)	0.663	0.707	0.675	0.645	0.216
With AdaBoost (T:05)	0.645	0.707	0.663	0.690	0.201
With AdaBoost (T:06)	**0.652**	**0.707**	**0.682**	0.619	0.225
With AdaBoost (T:07)	0.650	0.707	0.657	0.722	0.191
With AdaBoost (T:08)	0.657	0.707	0.673	0.733	0.187
With AdaBoost (T:09)	0.651	0.707	0.665	0.601	0.231
With AdaBoost (T:10)	0.648	0.707	0.687	0.682	0.203
Model Name	GPT-2 Medium	Qwen1.5-1.8B			
Baseline	0.649	0.842	0.722	0.658	0.211
With AdaBoost (T:02)	0.649	0.842	0.742	0.626	0.222
With AdaBoost (T:03)	0.669	0.842	0.732	0.673	0.206
With AdaBoost (T:04)	**0.649**	**0.842**	**0.757**	0.662	0.210
With AdaBoost (T:05)	0.661	0.842	0.745	0.688	0.202
With AdaBoost (T:06)	0.655	0.842	0.735	0.722	0.191
With AdaBoost (T:07)	0.664	0.842	0.732	0.717	0.192
With AdaBoost (T:08)	0.664	0.842	0.741	0.718	0.192
With AdaBoost (T:09)	0.657	0.842	0.748	0.791	0.171
With AdaBoost (T:10)	0.667	0.842	0.737	0.671	0.207
Model Name	GPT-2 Large	GPT-2 XL			
Baseline	0.673	0.707	0.682	1.675	0.034
With AdaBoost (T:02)	0.658	0.707	0.675	0.974	0.125
With AdaBoost (T:03)	0.671	0.707	0.687	1.091	0.101
With AdaBoost (T:04)	0.671	0.707	0.684	1.080	0.103
With AdaBoost (T:05)	0.668	0.707	0.687	1.033	0.112
With AdaBoost (T:06)	0.675	0.707	0.683	1.133	0.094
With AdaBoost (T:07)	**0.669**	**0.707**	**0.688**	1.083	0.103
With AdaBoost (T:08)	0.676	0.707	0.683	1.047	0.110
With AdaBoost (T:09)	0.678	0.707	0.682	1.085	0.103
With AdaBoost (T:10)	0.669	0.707	0.681	1.132	0.094
Model Name	GPT-2 Large	Qwen1.5-1.8B			
Baseline	0.664	0.842	0.749	1.454	0.052
With AdaBoost (T:02)	0.670	0.842	0.717	0.971	0.126
With AdaBoost (T:03)	0.670	0.842	0.728	0.037	0.481
With AdaBoost (T:04)	0.677	0.842	0.727	1.128	0.095
With AdaBoost (T:05)	0.675	0.842	0.740	1.107	0.098
With AdaBoost (T:06)	0.677	0.842	0.737	0.979	0.124
With AdaBoost (T:07)	**0.676**	**0.842**	**0.766**	1.136	0.093
With AdaBoost (T:08)	0.680	0.842	0.741	1.103	0.099
With AdaBoost (T:09)	0.691	0.842	0.762	1.075	0.104
With AdaBoost (T:10)	0.683	0.842	0.755	1.052	0.109
Model Name	GPT-2 XL	Qwen1.5-1.8B			
Baseline	0.673	0.842	0.733	0.564	0.244
With AdaBoost (T:02)	0.701	0.842	0.740	0.428	0.298
With AdaBoost (T:03)	0.702	0.842	0.753	0.383	0.317
With AdaBoost (T:04)	0.694	0.842	0.756	0.316	0.347
With AdaBoost (T:05)	**0.704**	**0.842**	**0.759**	0.260	0.373
With AdaBoost (T:06)	0.693	0.842	0.757	0.288	0.360
With AdaBoost (T:07)	0.708	0.842	0.755	0.277	0.365
With AdaBoost (T:08)	0.706	0.842	0.761	0.223	0.391
With AdaBoost (T:09)	0.700	0.842	0.748	0.252	0.377
With AdaBoost (T:10)	0.703	0.842	0.747	0.258	0.374

Table 2: This table shows weak to strong generalization using easy and hard data-splits for sciq dataset. We also study the impact of using ensemble learning methods like AdaBoost, which combines weak learners, for weak to strong training. Each model is trained for 3 epochs and uses an optimized learning rate.

AdaBoost	Weak Model	Strong Model	Weak-to-Strong	α	Err_i^{train}
Model Name	GPT-2	GPT-2 Medium			
Baseline	0.362	0.638	0.388	2.178	0.013
With AdaBoost (T:02)	0.356	0.638	0.382	1.790	0.027
With AdaBoost (T:03)	0.343	0.638	0.386	1.953	0.020
With AdaBoost (T:04)	0.361	0.638	0.385	2.014	0.018
With AdaBoost (T:05)	0.361	0.638	0.382	1.534	0.044
With AdaBoost (T:06)	0.365	0.638	0.393	1.588	0.040
With AdaBoost (T:07)	0.365	0.638	0.402	1.474	0.050
With AdaBoost (T:08)	**0.369**	**0.638**	**0.404**	1.478	0.049
With AdaBoost (T:09)	0.362	0.638	0.394	1.865	0.023
With AdaBoost (T:10)	0.364	0.638	0.394	1.267	0.074
Model Name	GPT-2	GPT-2 Large			
Baseline	0.362	0.597	0.385	2.178	0.013
With AdaBoost (T:02)	0.356	0.597	0.367	1.790	0.027
With AdaBoost (T:03)	0.343	0.597	0.383	1.953	0.020
With AdaBoost (T:04)	0.361	0.597	0.379	2.014	0.018
With AdaBoost (T:05)	0.361	0.597	0.387	1.534	0.044
With AdaBoost (T:06)	0.365	0.597	0.382	1.588	0.040
With AdaBoost (T:07)	0.365	0.597	0.388	1.474	0.050
With AdaBoost (T:08)	0.369	0.597	0.389	1.478	0.049
With AdaBoost (T:09)	**0.362**	**0.597**	**0.393**	1.865	0.023
With AdaBoost (T:10)	0.364	0.597	0.395	1.267	0.074
Model Name	GPT-2	GPT-2 XL			
Baseline	0.355	0.561	0.421	2.178	0.013
With AdaBoost (T:02)	0.356	0.561	0.409	1.791	0.027
With AdaBoost (T:03)	0.343	0.561	0.409	1.953	0.020
With AdaBoost (T:04)	0.361	0.561	0.407	2.014	0.018
With AdaBoost (T:05)	**0.361**	**0.561**	**0.418**	1.534	0.044
With AdaBoost (T:06)	0.365	0.561	0.409	1.588	0.040
With AdaBoost (T:07)	0.365	0.561	0.407	1.474	0.050
With AdaBoost (T:08)	0.369	0.561	0.413	1.478	0.049
With AdaBoost (T:09)	0.362	0.561	0.410	1.865	0.023
With AdaBoost (T:10)	0.364	0.561	0.409	1.267	0.074
Model Name	GPT-2	Qwen1.5-1.8B			
Baseline	0.364	0.760	0.407	2.178	0.013
With AdaBoost (T:02)	0.356	0.760	0.397	1.791	0.027
With AdaBoost (T:03)	0.343	0.760	0.393	1.953	0.020
With AdaBoost (T:04)	0.361	0.760	0.381	2.014	0.018
With AdaBoost (T:05)	0.361	0.760	0.390	1.534	0.044
With AdaBoost (T:06)	0.365	0.760	0.394	1.588	0.040
With AdaBoost (T:07)	0.365	0.760	0.390	1.474	0.050
With AdaBoost (T:08)	0.369	0.760	0.387	1.478	0.049
With AdaBoost (T:09)	0.362	0.760	0.402	1.865	0.023
With AdaBoost (T:10)	**0.364**	**0.760**	**0.404**	1.267	0.074
Model Name	GPT-2 Medium	GPT-2 Large			
Baseline	0.391	0.597	0.420	1.511	0.046
With AdaBoost (T:02)	0.448	0.597	0.438	1.571	0.041
With AdaBoost (T:03)	0.426	0.597	0.405	1.483	0.049
With AdaBoost (T:04)	0.454	0.597	0.437	1.601	0.039
With AdaBoost (T:05)	0.448	0.597	0.428	1.334	0.065
With AdaBoost (T:06)	0.465	0.597	0.444	1.249	0.076
With AdaBoost (T:07)	**0.449**	**0.597**	**0.453**	1.460	0.051
With AdaBoost (T:08)	0.461	0.597	0.444	1.646	0.036
With AdaBoost (T:09)	0.449	0.597	0.433	1.453	0.052
With AdaBoost (T:10)	0.447	0.597	0.424	1.154	0.090
Model Name	GPT-2 Medium	GPT-2 XL			
Baseline	0.392	0.561	0.440	1.510	0.047
With AdaBoost (T:02)	0.459	0.561	0.442	1.589	0.040
With AdaBoost (T:03)	0.420	0.561	0.435	1.669	0.034
With AdaBoost (T:04)	0.458	0.561	0.441	1.460	0.051
With AdaBoost (T:05)	0.424	0.561	0.431	1.393	0.058
With AdaBoost (T:06)	**0.444**	**0.561**	**0.448**	1.286	0.071
With AdaBoost (T:07)	0.419	0.561	0.436	1.429	0.054
With AdaBoost (T:08)	0.454	0.561	0.443	1.596	0.039
With AdaBoost (T:09)	0.437	0.561	0.439	1.577	0.041
With AdaBoost (T:10)	0.432	0.561	0.439	1.289	0.071
Model Name	GPT-2 Medium	Qwen1.5-1.8B			
Baseline	0.388	0.760	0.435	1.511	0.046
With AdaBoost (T:02)	**0.448**	**0.760**	**0.477**	1.571	0.041
With AdaBoost (T:03)	0.426	0.760	0.462	1.483	0.049
With AdaBoost (T:04)	0.454	0.760	0.473	1.601	0.039
With AdaBoost (T:05)	0.448	0.760	0.471	1.334	0.065
With AdaBoost (T:06)	0.465	0.760	0.470	1.249	0.076
With AdaBoost (T:07)	0.449	0.760	0.469	1.460	0.051
With AdaBoost (T:08)	0.461	0.760	0.480	1.646	0.036
With AdaBoost (T:09)	0.449	0.760	0.476	1.453	0.052
With AdaBoost (T:10)	0.447	0.760	0.483	1.154	0.090
Model Name	GPT-2 Large	GPT-2 XL			
Baseline	0.454	0.561	0.453	2.981	0.003
With AdaBoost (T:02)	0.451	0.561	0.455	1.791	0.027
With AdaBoost (T:03)	0.458	0.561	0.451	1.954	0.020
With AdaBoost (T:04)	0.463	0.561	0.447	2.220	0.012
With AdaBoost (T:05)	0.471	0.561	0.452	2.145	0.014
With AdaBoost (T:06)	**0.465**	**0.561**	**0.458**	1.745	0.030
With AdaBoost (T:07)	0.459	0.561	0.453	1.729	0.031
With AdaBoost (T:08)	0.469	0.561	0.455	1.726	0.031
With AdaBoost (T:09)	0.471	0.561	0.445	1.915	0.021
With AdaBoost (T:10)	0.466	0.561	0.447	2.179	0.013
Model Name	GPT-2 Large	Qwen1.5-1.8B			
Baseline	0.439	0.760	0.476	2.745	0.004
With AdaBoost (T:02)	0.437	0.760	0.467	1.747	0.029
With AdaBoost (T:03)	0.443	0.760	0.469	1.874	0.023
With AdaBoost (T:04)	0.445	0.760	0.460	2.018	0.017
With AdaBoost (T:05)	0.448	0.760	0.468	2.063	0.016
With AdaBoost (T:06)	0.449	0.760	0.467	1.639	0.036
With AdaBoost (T:07)	0.444	0.760	0.457	1.673	0.034
With AdaBoost (T:08)	0.453	0.760	0.468	1.727	0.031
With AdaBoost (T:09)	0.443	0.760	0.475	2.049	0.016
With AdaBoost (T:10)	**0.459**	**0.760**	**0.484**	2.217	0.012
Model Name	GPT-2 XL	Qwen1.5-1.8B			
Baseline	0.463	0.763	0.504	1.165	0.089
With AdaBoost (T:02)	0.475	0.763	0.508	1.156	0.090
With AdaBoost (T:03)	0.481	0.763	0.512	0.941	0.132
With AdaBoost (T:04)	0.488	0.763	0.500	0.841	0.157
With AdaBoost (T:05)	**0.481**	**0.763**	**0.518**	0.821	0.162
With AdaBoost (T:06)	0.494	0.763	0.514	0.776	0.175
With AdaBoost (T:07)	0.483	0.763	0.499	0.801	0.168
With AdaBoost (T:08)	0.489	0.763	0.513	0.687	0.202
With AdaBoost (T:09)	0.492	0.763	0.516	0.832	0.159
With AdaBoost (T:10)	0.481	0.763	0.519	0.636	0.219

E GENERATIVE TASK DETAILS

E.1 DIFFERENT RATING FOR ALL THE DATASETS

We use GPT-2 for binary classification and pythia-160m for SFT task's easy and hard splitting. We use the same training parameters as used in the training of the actual w2s results.

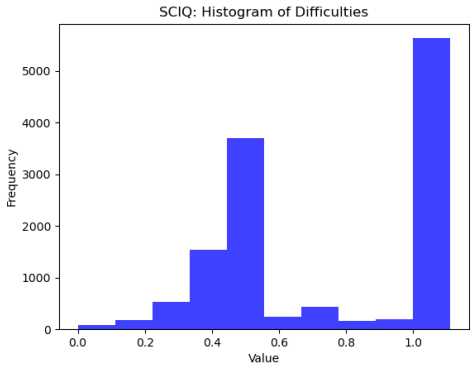

Figure 8: This figure shows the difficulty rating distribution of sciq dataset.

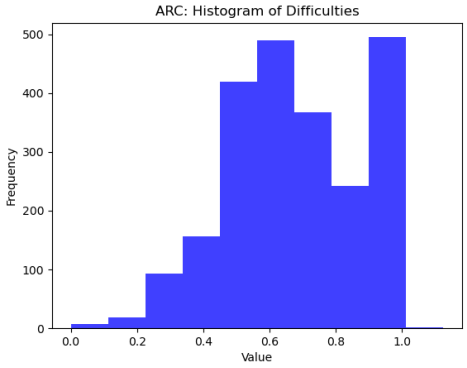

Figure 9: This figure shows difficulty rating distribution of ARC dataset.

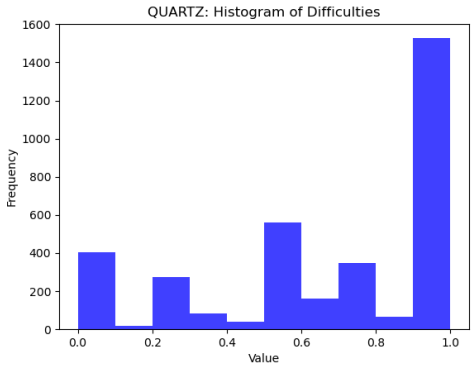

Figure 10: This figure shows difficulty rating distribution of quartz dataset.

E.2 COMPARISON BETWEEN PROBABILITY BASED COMBINATION WITH LOGIT BASED COMBINATION OF THE TOKENS, DURING GENERATION AND EVALUATION OF COMBINED WEAK EXPERTS.

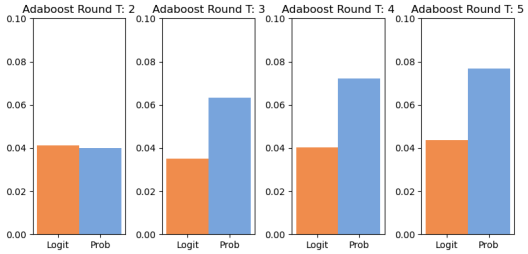

Figure 11: This figure compares probability-based combination with logit-based combination of the tokens across different AdaBoost rounds. Here we show improvement from the baseline where baseline is single model. The orange bars represent logit-based combination, while the blue bars represent probability-based combination, showing that probability-based combination performs better.

E.3 COMPARISON BETWEEN DIFFERENT WINDOW LENGTHS FOR "SAMPLE AND TOKEN WEIGHING".

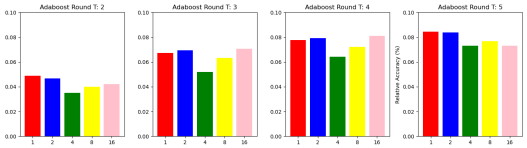

Figure 12: This figure compares different token window lengths for the Pythia 70M model across various AdaBoost rounds. The plots show improvements over the baseline, where the baseline represents a single model. The different bars (red, blue, green, yellow, and pink) correspond to window lengths of 1, 2, 4, 8, and 16, respectively. We observe that, overall, all window lengths perform similarly. Window length in EmsemW2S plays a role only during sampling step.

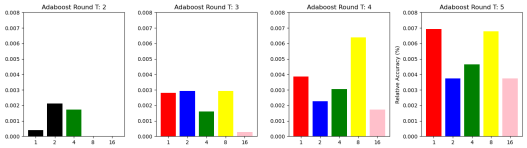

Figure 13: This figure compares different token window lengths for the Pythia 410M model across various AdaBoost rounds. The plots show improvements/decline over the baseline, where the baseline represents a single model. Thus, the black colored bars show decline. The different bars (red, blue, green, yellow, and pink) correspond to window lengths of 1, 2, 4, 8, and 16, respectively. We observe that, overall, all window lengths perform similarly. Window length in EmsemW2S plays a role only during sampling step.

E.4 SUPERVISED-FINE TUNING TASK FOR QUARTZ QUESTION-ANSWER DATASET

Table 3: This table shows weak to strong generalization using random data-splits for quartz dataset. We also study the impact of using ensemble learning methods, which combines weak learners, for weak to strong training. Each model is trained for 5 epochs and uses a learning rate of $5x10^{-5}$. The values in this table are generated by aggregating 3 experiments. We show here mean and Standard Error of the Mean values.

	Weak Model				Strong Model		
	Token-Avg Acc	Option Acc	Option Acc(on w2s)	α	oracle	Token-Avg Acc	Option Acc
	Pythia-70m				Pythia-160m		
Baseline	17.95 ± 0.44	50.21 ± 0.23	49.7 ± 0.28	10.81 ± 0.04	50.77 ± 0.26	34.3 ± 0.44	51.11 ± 0.23
With Adaboost (T:03)	25.94 ± 0.38	50.64 ± 0.39	49.43 ± 0.25	10.67 ± 0.05	50.77 ± 0.26	34.17 ± 0.36	**51.66 ± 0.45**
	Pythia-70m				Pythia-410m		
Baseline	17.95 ± 0.44	50.21 ± 0.23	49.7 ± 0.28	10.81 ± 0.04	59.18 ± 0.78	50.28 ± 0.44	50.68 ± 0.3
With Adaboost (T:04)	25.22 ± 0.15	50.51 ± 0.53	49.8 ± 0.14	10.68 ± 0.05	59.18 ± 0.78	50.88 ± 0.18	**52.42 ± 0.33**
	Pythia-70m				Pythia-1b		
Baseline	17.95 ± 0.44	50.21 ± 0.23	49.7 ± 0.28	10.81 ± 0.04	63.35 ± 0.3	51.87 ± 0.11	50.89 ± 0.16
With Adaboost (T:05)	26.2 ± 0.06	50.55 ± 0.28	49.65 ± 0.11	10.66 ± 0.04	63.35 ± 0.3	51.83 ± 0.38	**51.83 ± 0.31**
	Pythia-70m				Pythia-1.4b		
Baseline	17.89 ± 0.46	49.87 ± 0.06	49.46 ± 0.35	10.82 ± 0.05	68.83 ± 1.28	51.82 ± 0.05	50.17 ± 0.24
With Adaboost (T:04)	25.32 ± 0.82	50.04 ± 0.37	49.23 ± 0.27	10.7 ± 0.06	68.83 ± 1.28	51.76 ± 0.17	**51.45 ± 0.07**
	Pythia-70m				Pythia-2.8b		
Baseline	18.06 ± 0.39	49.4 ± 0.39	49.73 ± 0.33	10.86 ± 0.02	73.38 ± 1.02	52.28 ± 0.29	50.21 ± 0.23
With Adaboost (T:02)	24.37 ± 0.99	50.13 ± 0.4	49.48 ± 0.21	10.74 ± 0.04	73.38 ± 1.02	52.3 ± 0.14	**51.02 ± 0.22**
	Pythia-160m				Pythia-410m		
Baseline	33.51 ± 0.19	50.81 ± 1.0	49.6 ± 0.27	10.03 ± 0.0	59.18 ± 0.78	50.39 ± 0.3	50.68 ± 0.5
With Adaboost (T:04)	40.85 ± 0.49	51.79 ± 0.48	49.08 ± 0.32	9.81 ± 0.05	59.18 ± 0.78	50.39 ± 0.18	**52.13 ± 0.3**
	Pythia-160m				Pythia-1b		
Baseline	33.51 ± 0.19	50.81 ± 1.0	49.6 ± 0.27	10.03 ± 0.0	63.35 ± 0.3	52.36 ± 0.29	50.6 ± 0.33
With Adaboost (T:02)	40.61 ± 0.8	51.36 ± 0.25	49.93 ± 0.52	9.76 ± 0.05	63.35 ± 0.3	52.45 ± 0.42	**51.92 ± 0.31**
	Pythia-160m				Pythia-1.4b		
Baseline	33.42 ± 0.23	51.4 ± 0.59	49.43 ± 0.41	10.03 ± 0.0	68.83 ± 1.28	52.02 ± 0.2	51.02 ± 0.55
With Adaboost (T:03)	40.87 ± 0.49	51.02 ± 0.18	49.28 ± 0.13	9.75 ± 0.02	68.83 ± 1.28	52.11 ± 0.39	**53.02 ± 0.55**
	Pythia-160m				Pythia-2.8b		
Baseline	33.42 ± 0.23	51.4 ± 0.59	49.43 ± 0.41	10.03 ± 0.0	73.17 ± 0.88	52.82 ± 0.02	51.45 ± 0.5
With Adaboost (T:04)	41.13 ± 0.51	51.23 ± 0.4	49.65 ± 0.14	9.78 ± 0.06	73.17 ± 0.88	52.51 ± 0.3	**51.74 ± 0.17**
	Pythia-410m				Pythia-1b		
Baseline	52.71 ± 0.24	59.27 ± 0.46	55.54 ± 0.49	10.0 ± 0.01	63.35 ± 0.3	53.39 ± 0.2	56.21 ± 0.76
With Adaboost (T:02)	53.39 ± 0.17	58.5 ± 0.33	55.91 ± 0.35	9.69 ± 0.08	63.35 ± 0.3	53.87 ± 0.46	**56.42 ± 0.56**
	Pythia-410m				Pythia-1.4b		
Baseline	52.9 ± 0.09	59.65 ± 0.15	55.66 ± 0.51	9.98 ± 0.02	68.83 ± 1.28	53.33 ± 0.74	56.34 ± 0.9
With Adaboost (T:02)	53.26 ± 0.27	58.8 ± 0.42	56.11 ± 0.34	9.66 ± 0.08	68.83 ± 1.28	54.14 ± 0.63	**57.7 ± 0.61**
	Pythia-410m				Pythia-2.8b		
Baseline	52.13 ± 0.64	58.29 ± 1.1	55.94 ± 0.3	9.89 ± 0.06	73.38 ± 1.02	54.38 ± 0.31	55.74 ± 0.73
With Adaboost (T:04)	53.39 ± 0.19	59.18 ± 0.42	55.32 ± 0.51	9.85 ± 0.05	73.38 ± 1.02	55.71 ± 0.53	**59.01 ± 0.94**
	Pythia-1b				Pythia-1.4b		
Baseline	55.65 ± 0.52	61.99 ± 0.51	58.6 ± 1.13	9.85 ± 0.01	68.62 ± 0.12	55.33 ± 0.31	58.93 ± 0.68
With Adaboost (T:03)	56.81 ± 0.47	62.12 ± 0.43	58.14 ± 0.85	9.74 ± 0.11	68.62 ± 0.12	55.99 ± 0.16	**61.69 ± 0.57**
	Pythia-1b				Pythia-2.8b		
Baseline	55.54 ± 0.6	62.12 ± 0.51	58.55 ± 1.14	9.84 ± 0.01	73.3 ± 0.3	57.26 ± 0.3	61.52 ± 1.38
With Adaboost (T:02)	57.09 ± 0.41	62.84 ± 0.12	59.0 ± 0.62	9.63 ± 0.02	73.3 ± 0.3	58.1 ± 0.08	**63.99 ± 0.93**
	Pythia-1.4b				Pythia-2.8b		
Baseline	57.11 ± 0.45	69.64 ± 0.97	66.87 ± 1.1	9.87 ± 0.02	73.76 ± 0.67	59.34 ± 0.24	67.94 ± 0.78
With Adaboost (T:02)	59.17 ± 0.12	70.66 ± 0.06	67.29 ± 0.77	9.65 ± 0.03	73.76 ± 0.67	59.3 ± 0.34	**68.92 ± 1.06**

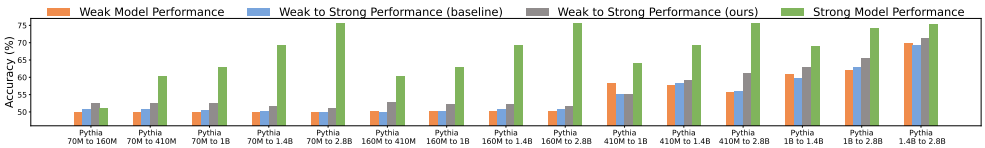

Figure 14: **Quartz Dataset (Random):** This figure shows bar plots comparing accuracy values of weak model performance, w2s model performance (baseline and ours) and strong model performance (oracle) for one specific run of experiments. Values are also mentioned in table 5.

Table 4: This table shows weak to strong generalization using easy-hard data-splits for quartz dataset. We also study the impact of using ensemble learning methods, which combines weak learners, for weak to strong training. Each model is trained for 5 epochs and uses a learning rate of 5×10^{-5}. The values in this table are generated by aggregating 3 experiments. We show here mean and Standard Error of the Mean values.

	Weak Model				Strong Model		
	Token-Avg Acc	Option Acc	Option Acc(on w2s)	α	oracle	Token-Avg Acc	Option Acc
	Pythia-70m				Pythia-160m		
Baseline	16.27 ± 0.14	48.0 ± 0.51	49.21 ± 0.05	10.53 ± 0.0	47.11 ± 0.28	29.24 ± 0.18	49.11 ± 0.39
With Adaboost (T:03)	23.31 ± 0.9	47.11 ± 0.31	49.23 ± 0.41	10.43 ± 0.03	47.11 ± 0.28	29.24 ± 0.25	**49.32 ± 0.23**
	Pythia-70m				Pythia-410m		
Baseline	16.27 ± 0.14	48.0 ± 0.51	49.21 ± 0.05	10.53 ± 0.0	52.3 ± 0.39	43.63 ± 0.29	47.32 ± 0.36
With Adaboost (T:04)	23.81 ± 1.01	47.66 ± 0.5	49.06 ± 0.2	10.42 ± 0.02	52.3 ± 0.39	43.53 ± 0.44	**48.13 ± 0.47**
	Pythia-70m				Pythia-1b		
Baseline	16.27 ± 0.14	48.0 ± 0.51	49.21 ± 0.05	10.53 ± 0.0	55.91 ± 0.37	47.48 ± 0.23	47.92 ± 0.23
With Adaboost (T:05)	24.64 ± 0.22	47.49 ± 0.49	49.41 ± 0.38	10.39 ± 0.0	55.91 ± 0.37	45.5 ± 0.74	**49.74 ± 0.24**
	Pythia-70m				Pythia-1.4b		
Baseline	16.07 ± 0.22	48.17 ± 0.43	49.38 ± 0.14	10.58 ± 0.04	65.35 ± 0.66	46.25 ± 0.61	47.96 ± 0.34
With Adaboost (T:04)	23.79 ± 0.55	46.94 ± 0.18	49.58 ± 0.27	10.44 ± 0.04	65.35 ± 0.66	45.53 ± 0.2	**50.68 ± 0.17**
	Pythia-70m				Pythia-2.8b		
Baseline	16.12 ± 0.21	48.85 ± 0.48	49.75 ± 0.32	10.63 ± 0.04	70.2 ± 0.17	48.08 ± 0.18	48.85 ± 0.31
With Adaboost (T:02)	22.96 ± 0.75	47.02 ± 0.12	49.36 ± 0.11	10.5 ± 0.05	70.2 ± 0.17	48.58 ± 0.16	**49.87 ± 0.06**
	Pythia-160m				Pythia-410m		
Baseline	25.61 ± 0.33	47.75 ± 0.35	49.83 ± 0.29	9.96 ± 0.02	52.3 ± 0.39	42.75 ± 0.91	47.75 ± 0.61
With Adaboost (T:04)	29.63 ± 0.55	47.02 ± 0.09	48.47 ± 0.3	9.7 ± 0.09	52.3 ± 0.39	43.78 ± 0.14	**48.42 ± 0.12**
	Pythia-160m				Pythia-1b		
Baseline	25.61 ± 0.33	47.75 ± 0.35	49.83 ± 0.29	9.96 ± 0.02	55.91 ± 0.37	46.08 ± 0.38	49.36 ± 0.53
With Adaboost (T:02)	28.96 ± 0.23	46.43 ± 0.18	48.49 ± 0.11	9.69 ± 0.09	55.91 ± 0.37	44.7 ± 0.58	**49.15 ± 0.73**
	Pythia-160m				Pythia-1.4b		
Baseline	25.76 ± 0.43	47.15 ± 0.15	49.26 ± 0.2	9.96 ± 0.02	65.35 ± 0.66	45.83 ± 0.64	49.7 ± 0.85
With Adaboost (T:03)	28.83 ± 0.84	46.56 ± 0.27	48.17 ± 0.14	9.64 ± 0.06	65.35 ± 0.66	45.4 ± 0.44	**50.0 ± 0.22**
	Pythia-160m				Pythia-2.8b		
Baseline	26.46 ± 0.25	47.49 ± 0.33	48.98 ± 0.14	10.02 ± 0.03	70.2 ± 0.17	48.03 ± 0.13	49.4 ± 0.3
With Adaboost (T:04)	29.61 ± 0.51	46.6 ± 0.25	48.69 ± 0.47	9.54 ± 0.03	70.2 ± 0.17	48.4 ± 0.29	**50.3 ± 0.41**
	Pythia-410m				Pythia-1b		
Baseline	36.73 ± 0.39	51.06 ± 0.39	53.26 ± 0.38	10.07 ± 0.01	55.91 ± 0.37	46.6 ± 0.38	50.72 ± 0.68
With Adaboost (T:02)	38.11 ± 0.44	49.36 ± 0.21	51.66 ± 0.35	9.76 ± 0.14	55.91 ± 0.37	46.4 ± 0.35	**52.09 ± 0.3**
	Pythia-410m				Pythia-1.4b		
Baseline	37.23 ± 0.27	51.11 ± 0.4	53.19 ± 0.42	10.04 ± 0.03	65.35 ± 0.66	47.73 ± 0.78	53.66 ± 0.56
With Adaboost (T:02)	38.31 ± 0.23	50.17 ± 0.44	51.56 ± 0.22	9.53 ± 0.09	65.35 ± 0.66	48.35 ± 0.18	**53.36 ± 0.5**
	Pythia-410m				Pythia-2.8b		
Baseline	37.13 ± 0.23	51.02 ± 0.47	52.87 ± 0.21	10.03 ± 0.03	70.2 ± 0.17	48.48 ± 0.36	54.47 ± 0.16
With Adaboost (T:04)	38.13 ± 0.26	49.87 ± 0.68	51.49 ± 0.28	9.6 ± 0.04	70.2 ± 0.17	49.05 ± 0.14	**55.36 ± 0.47**
	Pythia-1b				Pythia-1.4b		
Baseline	40.3 ± 0.46	54.51 ± 0.73	54.25 ± 0.26	10.33 ± 0.08	66.67 ± 0.72	47.0 ± 0.22	56.76 ± 0.58
With Adaboost (T:03)	40.75 ± 0.67	53.36 ± 0.92	53.61 ± 0.44	11.0 ± 0.72	66.67 ± 0.72	47.25 ± 0.32	**57.23 ± 0.37**
	Pythia-1b				Pythia-2.8b		
Baseline	40.33 ± 0.44	54.08 ± 1.07	54.33 ± 0.19	10.33 ± 0.08	73.09 ± 0.42	49.2 ± 0.2	58.08 ± 0.38
With Adaboost (T:02)	40.53 ± 0.34	52.34 ± 0.09	53.39 ± 0.2	11.68 ± 0.75	73.09 ± 0.42	49.48 ± 0.3	**59.35 ± 0.52**
	Pythia-1.4b				Pythia-2.8b		
Baseline	42.2 ± 1.12	59.69 ± 0.83	62.39 ± 1.06	10.3 ± 0.1	73.17 ± 0.38	51.22 ± 0.5	62.46 ± 0.91
With Adaboost (T:02)	42.98 ± 0.64	59.82 ± 0.51	61.38 ± 0.48	10.52 ± 0.35	73.17 ± 0.38	51.72 ± 0.37	**63.01 ± 0.28**

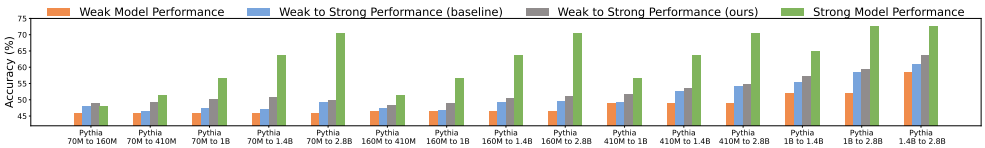

Figure 15: **Quartz Dataset (Easy-Hard):** This figure shows bar plots comparing accuracy values of weak model performance, w2s model performance (baseline and ours) and strong model performance (oracle) for one specific run of experiments. Values are also mentioned in table 5.

Table 5: This table shows weak to strong generalization using random as well as easy-hard data-splits for quartz dataset. As compared to previous tables 3 and 4, here we run experiment once and note the improvement of our method with respect to the baseline.

Weak Model Size	Strong Model Size	Data Separation: Random W2S Performance		Improv(%)	Data Separation: Easy-Hard W2S Performance		Improv(%)
		Baseline	Ours		Baseline	Ours	
Pythia-70M	Pythia-160M	0.5077	0.5255	3.5%	0.48	0.4898	2%
Pythia-70M	Pythia-410M	0.5077	0.5255	3.5%	0.4643	0.4923	6%
Pythia-70M	Pythia-1B	0.5051	0.5255	4%	0.4758	0.5026	5.6%
Pythia-70M	Pythia-1.4B	0.5026	0.5153	2.5%	0.4719	0.5089	7.8%
Pythia-70M	Pythia-2.8B	0.5	0.5115	2.3%	0.4923	0.4987	1.3%
Pythia-160M	Pythia-410M	0.5	0.5281	5.6%	0.4758	0.4834	1.6%
Pythia-160M	Pythia-1B	0.5026	0.523	4.1%	0.4681	0.4898	4.6%
Pythia-160M	Pythia-1.4B	0.5077	0.5217	2.8%	0.4936	0.5038	2.1%
Pythia-160M	Pythia-2.8B	0.5077	0.5153	1.5%	0.4949	0.5128	3.6%
Pythia-410M	Pythia-1B	0.551	0.551	0%	0.4921	0.5179	5.2%
Pythia-410M	Pythia-1.4B	0.5816	0.5918	1.8%	0.5268	0.537	1.9%
Pythia-410M	Pythia-2.8B	0.5599	0.611	9.1%	0.5434	0.5485	0.9%
Pythia-1B	Pythia-1.4B	0.5982	0.6288	5.1%	0.5536	0.574	3.7%
Pythia-1B	Pythia-2.8B	0.6288	0.6543	4.1%	0.5855	0.5957	1.7%
Pythia-1.4B	Pythia-2.8B	0.6926	0.713	2.9%	0.6161	0.6288	2.1%
Qwen2.5-3B	Qwen2.5-7B	0.805	0.816	1.4%	0.8087	0.8087	0%

E.4.1 SUPERVISED-FINE TUNING TASK FOR ARC QUESTION-ANSWER DATASET

Table 6: This table shows weak to strong generalization using random data-splits for arc dataset. We also study the impact of using ensemble learning methods, which combines weak learners, for weak to strong training. Each model is trained for 5 epochs and uses a learning rate of $5x10^{-5}$. The values in this table are generated by aggregating 3 experiments. We show here mean and Standard Error of the Mean values.

	Weak Model				Strong Model		
	Token-Avg Acc	Option Acc	Option Acc(on w2s)	α	oracle	Token-Avg Acc	Option Acc
	Pythia-70m				Pythia-160m		
Baseline	13.28 ± 0.05	25.31 ± 0.1	25.76 ± 0.94	10.73 ± 0.03	24.12 ± 0.48	26.91 ± 0.1	24.46 ± 0.06
With Adaboost (T:03)	17.93 ± 0.78	24.75 ± 0.76	25.82 ± 0.69	10.68 ± 0.02	24.12 ± 0.48	27.15 ± 0.36	**24.23 ± 0.08**
	Pythia-70m				Pythia-410m		
Baseline	13.28 ± 0.05	25.31 ± 0.1	25.76 ± 0.94	10.73 ± 0.03	28.61 ± 0.08	41.29 ± 0.1	27.25 ± 0.24
With Adaboost (T:04)	17.94 ± 0.88	24.97 ± 0.69	25.82 ± 0.69	10.67 ± 0.04	28.61 ± 0.08	41.61 ± 0.02	**27.27 ± 0.3**
	Pythia-70m				Pythia-1b		
Baseline	13.28 ± 0.05	25.31 ± 0.1	25.76 ± 0.94	10.73 ± 0.03	31.11 ± 0.02	45.13 ± 0.11	28.33 ± 0.18
With Adaboost (T:05)	19.7 ± 1.18	24.92 ± 0.28	26.23 ± 0.49	10.65 ± 0.04	31.11 ± 0.02	45.17 ± 0.11	**28.52 ± 0.09**
	Pythia-70m				Pythia-1.4b		
Baseline	13.35 ± 0.06	25.06 ± 0.14	24.39 ± 0.42	10.77 ± 0.06	32.34 ± 0.3	45.21 ± 0.24	29.86 ± 0.28
With Adaboost (T:04)	19.75 ± 1.16	24.26 ± 0.56	25.7 ± 0.65	10.68 ± 0.05	32.34 ± 0.3	45.33 ± 0.14	**30.35 ± 0.13**
	Pythia-70m				Pythia-2.8b		
Baseline	13.42 ± 0.11	24.63 ± 0.13	23.97 ± 0.55	10.77 ± 0.05	35.18 ± 0.02	48.07 ± 0.12	30.94 ± 0.13
With Adaboost (T:02)	19.88 ± 0.56	24.52 ± 0.49	24.87 ± 0.81	10.68 ± 0.04	35.18 ± 0.02	47.75 ± 0.08	**31.43 ± 0.43**
	Pythia-160m				Pythia-410m		
Baseline	25.5 ± 0.66	24.12 ± 0.45	26.06 ± 0.68	9.89 ± 0.03	29.18 ± 0.04	41.39 ± 0.14	27.5 ± 0.27
With Adaboost (T:04)	31.95 ± 0.47	24.94 ± 0.29	25.88 ± 0.64	9.74 ± 0.03	29.18 ± 0.04	41.28 ± 0.03	**27.7 ± 0.34**
	Pythia-160m				Pythia-1b		
Baseline	25.5 ± 0.66	24.12 ± 0.45	26.06 ± 0.68	9.89 ± 0.03	31.26 ± 0.44	45.12 ± 0.05	28.24 ± 0.18
With Adaboost (T:02)	32.25 ± 0.21	24.52 ± 0.34	26.06 ± 0.57	9.66 ± 0.01	31.26 ± 0.44	45.18 ± 0.14	**28.47 ± 0.24**
	Pythia-160m				Pythia-1.4b		
Baseline	24.74 ± 0.14	23.97 ± 0.36	25.76 ± 0.51	9.86 ± 0.02	32.25 ± 0.35	45.01 ± 0.1	30.55 ± 0.07
With Adaboost (T:03)	32.55 ± 0.21	24.46 ± 0.22	26.12 ± 0.8	9.66 ± 0.01	32.25 ± 0.35	45.23 ± 0.05	**30.86 ± 0.33**
	Pythia-160m				Pythia-2.8b		
Baseline	25.43 ± 0.66	24.34 ± 0.09	26.0 ± 0.32	9.86 ± 0.02	35.44 ± 0.06	47.88 ± 0.02	31.03 ± 0.15
With Adaboost (T:04)	32.6 ± 0.03	24.23 ± 0.18	26.47 ± 0.53	9.66 ± 0.02	35.44 ± 0.06	47.77 ± 0.08	**31.68 ± 0.41**
	Pythia-410m				Pythia-1b		
Baseline	39.76 ± 0.3	27.85 ± 0.52	24.33 ± 0.97	9.39 ± 0.02	30.97 ± 0.08	44.94 ± 0.08	28.9 ± 0.12
With Adaboost (T:02)	40.69 ± 0.14	28.27 ± 0.11	24.33 ± 0.59	9.01 ± 0.04	30.97 ± 0.08	44.76 ± 0.14	**29.41 ± 0.08**
	Pythia-410m				Pythia-1.4b		
Baseline	39.66 ± 0.22	27.82 ± 0.53	24.09 ± 0.8	9.39 ± 0.02	32.82 ± 0.27	45.54 ± 0.03	30.26 ± 0.56
With Adaboost (T:02)	40.82 ± 0.13	28.9 ± 0.21	24.51 ± 0.59	9.01 ± 0.04	32.82 ± 0.27	45.66 ± 0.09	**30.94 ± 0.53**
	Pythia-410m				Pythia-2.8b		
Baseline	39.57 ± 0.24	28.01 ± 0.69	24.69 ± 0.44	9.39 ± 0.01	35.86 ± 0.26	48.06 ± 0.15	31.15 ± 0.3
With Adaboost (T:04)	40.56 ± 0.11	28.7 ± 0.34	25.34 ± 1.12	9.03 ± 0.07	35.86 ± 0.26	48.22 ± 0.12	**31.88 ± 0.27**
	Pythia-1b				Pythia-1.4b		
Baseline	42.31 ± 0.2	30.35 ± 0.24	28.02 ± 0.76	9.53 ± 0.02	32.65 ± 0.43	45.41 ± 0.06	30.26 ± 0.22
With Adaboost (T:03)	43.22 ± 0.13	31.68 ± 0.55	27.79 ± 0.71	9.37 ± 0.01	32.65 ± 0.43	45.44 ± 0.06	**31.28 ± 0.22**
	Pythia-1b				Pythia-2.8b		
Baseline	42.2 ± 0.29	30.46 ± 0.16	27.73 ± 0.89	9.53 ± 0.02	35.12 ± 0.26	48.12 ± 0.06	32.14 ± 0.02
With Adaboost (T:02)	43.61 ± 0.2	31.17 ± 0.93	27.79 ± 0.76	9.26 ± 0.02	35.12 ± 0.26	48.2 ± 0.08	**32.54 ± 0.08**
	Pythia-1.4b				Pythia-2.8b		
Baseline	42.39 ± 0.37	33.42 ± 0.37	30.65 ± 1.82	9.48 ± 0.03	35.12 ± 0.26	48.35 ± 0.11	32.42 ± 0.44
With Adaboost (T:02)	43.58 ± 0.27	33.5 ± 0.22	30.71 ± 1.48	11.07 ± 0.84	35.12 ± 0.26	48.29 ± 0.13	**33.19 ± 0.24**

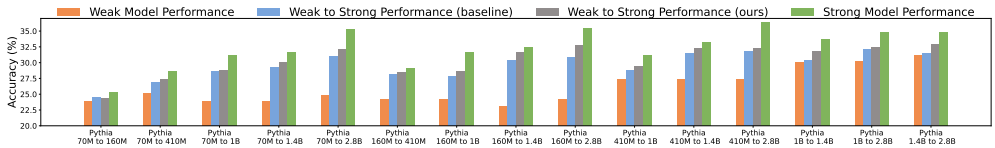

Figure 16: **ARC Dataset (Random):** This figure shows bar plots comparing accuracy values of weak model performance, w2s model performance (baseline and ours) and strong model performance (oracle) for one specific run of experiments. Values are also mentioned in table 8.

Table 7: This table shows weak to strong generalization using easy-hard data-splits for ARC dataset. We also study the impact of using ensemble learning methods, which combines weak learners, for weak to strong training. Each model is trained for 5 epochs and uses a learning rate of 5×10^{-5}. The values in this table are generated by aggregating 3 experiments. We show here mean and Standard Error of the Mean values.

	Weak Model				Strong Model		
	Token-Avg Acc	Option Acc	Option Acc(on w2s)	α	oracle	Token-Avg Acc	Option Acc
	Pythia-70m				Pythia-160m		
Baseline	8.17 ± 0.06	22.5 ± 0.33	27.85 ± 0.57	10.45 ± 0.0	22.3 ± 0.16	17.88 ± 0.11	22.27 ± 0.32
With Adaboost (T:03)	13.35 ± 0.54	22.81 ± 0.29	27.78 ± 0.46	10.35 ± 0.02	22.3 ± 0.16	17.87 ± 0.17	**22.56 ± 0.06**
	Pythia-70m				Pythia-410m		
Baseline	8.17 ± 0.06	22.5 ± 0.33	27.85 ± 0.57	10.45 ± 0.0	19.28 ± 0.15	28.92 ± 0.14	17.06 ± 0.31
With Adaboost (T:04)	14.53 ± 0.72	22.93 ± 0.17	27.96 ± 0.46	10.32 ± 0.0	19.28 ± 0.15	28.84 ± 0.05	**18.0 ± 0.07**
	Pythia-70m				Pythia-1b		
Baseline	8.17 ± 0.06	22.5 ± 0.33	27.85 ± 0.57	10.45 ± 0.0	21.5 ± 0.24	32.05 ± 0.13	19.96 ± 0.15
With Adaboost (T:05)	12.95 ± 0.88	22.58 ± 0.38	28.03 ± 0.21	10.35 ± 0.02	21.5 ± 0.24	31.84 ± 0.08	**20.45 ± 0.06**
	Pythia-70m				Pythia-1.4b		
Baseline	8.23 ± 0.1	22.61 ± 0.42	27.37 ± 0.42	10.45 ± 0.0	21.76 ± 0.14	32.98 ± 0.04	20.45 ± 0.42
With Adaboost (T:04)	12.65 ± 0.05	23.24 ± 0.06	28.32 ± 0.76	10.33 ± 0.01	21.76 ± 0.14	32.95 ± 0.17	**21.28 ± 0.02**
	Pythia-70m				Pythia-2.8b		
Baseline	8.33 ± 0.1	23.24 ± 0.23	27.19 ± 0.47	10.45 ± 0.0	26.59 ± 0.13	35.98 ± 0.09	22.78 ± 0.51
With Adaboost (T:02)	14.28 ± 0.15	23.26 ± 0.22	28.27 ± 0.14	10.37 ± 0.01	26.59 ± 0.13	35.86 ± 0.28	**23.15 ± 0.2**
	Pythia-160m				Pythia-410m		
Baseline	17.46 ± 0.16	21.73 ± 0.35	26.95 ± 0.1	9.61 ± 0.0	19.11 ± 0.37	28.8 ± 0.23	18.15 ± 0.15
With Adaboost (T:04)	20.57 ± 0.1	22.16 ± 0.2	27.19 ± 0.5	9.22 ± 0.02	19.11 ± 0.37	28.9 ± 0.11	**18.43 ± 0.04**
	Pythia-160m				Pythia-1b		
Baseline	17.46 ± 0.16	21.73 ± 0.35	26.95 ± 0.1	9.61 ± 0.0	21.59 ± 0.07	32.06 ± 0.06	19.65 ± 0.1
With Adaboost (T:02)	20.47 ± 0.09	22.27 ± 0.29	27.31 ± 0.51	9.24 ± 0.01	21.59 ± 0.07	32.07 ± 0.12	**20.17 ± 0.14**
	Pythia-160m				Pythia-1.4b		
Baseline	17.61 ± 0.07	22.84 ± 0.58	27.79 ± 0.64	9.61 ± 0.0	22.33 ± 0.34	33.11 ± 0.1	21.19 ± 0.15
With Adaboost (T:03)	20.31 ± 0.24	22.5 ± 0.36	27.79 ± 0.42	9.27 ± 0.06	22.33 ± 0.34	33.01 ± 0.05	**21.25 ± 0.28**
	Pythia-160m				Pythia-2.8b		
Baseline	17.64 ± 0.06	23.09 ± 0.54	27.91 ± 0.59	9.6 ± 0.01	26.82 ± 0.1	35.83 ± 0.36	22.44 ± 0.11
With Adaboost (T:04)	20.3 ± 0.19	23.01 ± 0.43	27.73 ± 0.25	9.26 ± 0.06	26.82 ± 0.1	36.06 ± 0.07	**23.35 ± 0.1**
	Pythia-410m				Pythia-1b		
Baseline	27.3 ± 0.16	18.8 ± 0.21	31.01 ± 0.51	9.24 ± 0.0	21.33 ± 0.04	32.06 ± 0.07	20.05 ± 0.08
With Adaboost (T:02)	28.07 ± 0.12	18.35 ± 0.21	32.2 ± 0.31	8.68 ± 0.09	21.33 ± 0.04	32.36 ± 0.05	**20.34 ± 0.06**
	Pythia-410m				Pythia-1.4b		
Baseline	27.5 ± 0.14	18.54 ± 0.32	31.6 ± 0.21	9.24 ± 0.0	22.36 ± 0.3	33.47 ± 0.07	21.13 ± 0.1
With Adaboost (T:02)	28.09 ± 0.08	18.17 ± 0.28	31.78 ± 0.4	8.67 ± 0.09	22.36 ± 0.3	33.18 ± 0.11	**21.47 ± 0.12**
	Pythia-410m				Pythia-2.8b		
Baseline	27.48 ± 0.13	18.12 ± 0.13	31.66 ± 0.17	9.25 ± 0.01	26.03 ± 0.21	36.13 ± 0.09	23.07 ± 0.18
With Adaboost (T:04)	27.96 ± 0.11	18.09 ± 0.2	31.07 ± 0.27	8.69 ± 0.08	26.03 ± 0.21	35.93 ± 0.09	**24.06 ± 0.15**
	Pythia-1b				Pythia-1.4b		
Baseline	30.64 ± 0.17	21.22 ± 0.72	32.5 ± 0.6	9.38 ± 0.01	22.01 ± 0.21	33.13 ± 0.11	21.5 ± 0.07
With Adaboost (T:03)	30.41 ± 0.42	21.11 ± 0.22	32.68 ± 0.56	10.98 ± 0.78	22.01 ± 0.21	33.31 ± 0.03	**21.53 ± 0.08**
	Pythia-1b				Pythia-2.8b		
Baseline	30.64 ± 0.17	21.22 ± 0.72	32.5 ± 0.6	9.38 ± 0.01	25.51 ± 0.2	36.14 ± 0.11	23.75 ± 0.16
With Adaboost (T:02)	31.11 ± 0.12	21.67 ± 0.18	33.21 ± 0.56	9.4 ± 0.24	25.51 ± 0.2	36.13 ± 0.13	**23.75 ± 0.06**
	Pythia-1.4b				Pythia-2.8b		
Baseline	31.09 ± 0.12	22.27 ± 0.55	34.05 ± 0.1	9.31 ± 0.01	25.26 ± 0.11	36.13 ± 0.05	23.49 ± 0.2
With Adaboost (T:02)	31.56 ± 0.1	21.79 ± 0.44	34.35 ± 0.59	10.89 ± 0.65	25.26 ± 0.11	36.36 ± 0.2	**24.37 ± 0.16**

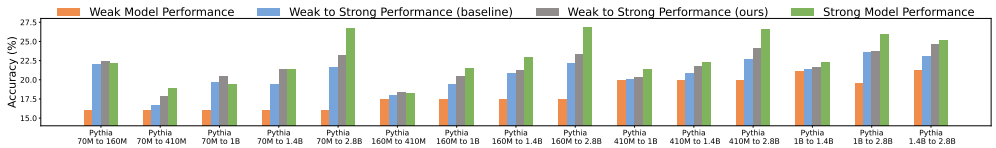

Figure 17: **ARC Dataset (Easy-Hard):** This figure shows bar plots comparing accuracy values of weak model performance, w2s model performance (baseline and ours) and strong model performance (oracle) for one specific run of experiments. Values are also mentioned in table 8.

Table 8: This table shows weak to strong generalization using random as well as easy-hard data-splits for ARC dataset. As compared to previous tables 6 and 7, here we run experiment once and note the improvement of our method with respect to the baseline.

Weak Model Size	Strong Model Size	Data Separation: Random W2S Performance		Improv (%)	Data Separation: Easy-Hard W2S Performance		Improv (%)
		Baseline	Ours		Baseline	Ours	
Pythia-70M	Pythia-160M	0.2457	0.244	-0.7	0.2201	0.2244	2
Pythia-70M	Pythia-410M	0.2688	0.273	1.6	0.1672	0.1783	6.6
Pythia-70M	Pythia-1B	0.2858	0.2875	0.6	0.1962	0.2048	4.4
Pythia-70M	Pythia-1.4B	0.2927	0.3003	2.6	0.1945	0.2133	9.7
Pythia-70M	Pythia-2.8B	0.3106	0.3208	3.3	0.2159	0.2321	7.5
Pythia-160M	Pythia-410M	0.2816	0.285	1.2	0.1792	0.1834	2.3
Pythia-160M	Pythia-1B	0.2782	0.2858	2.7	0.1945	0.2048	5.3
Pythia-160M	Pythia-1.4B	0.3038	0.3166	4.2	0.2082	0.2125	2.1
Pythia-160M	Pythia-2.8B	0.3089	0.3268	5.8	0.2218	0.2338	5.4
Pythia-410M	Pythia-1B	0.2884	0.2935	1.8	0.2005	0.2031	1.3
Pythia-410M	Pythia-1.4B	0.3148	0.3225	2.4	0.209	0.2176	4.1
Pythia-410M	Pythia-2.8B	0.3183	0.3225	1.3	0.227	0.2415	6.4
Pythia-1B	Pythia-1.4B	0.3029	0.3174	4.8	0.2142	0.2167	1.2
Pythia-1B	Pythia-2.8B	0.3217	0.3259	1.3	0.2355	0.2372	0.7
Pythia-1.4B	Pythia-2.8B	0.3148	0.3294	4.6	0.2304	0.2457	6.6
Qwen2.5-3B	Qwen2.5-7B	0.5307	0.54	1.7	0.3882	0.4079	5.1

F BROADER IMPACT

The proposed framework for weak-to-strong (w2s) generalization using ensembles of weak language models (LLMs) has significant implications across various domains. By demonstrating that multiple weak supervisors can effectively train more powerful models, our research addresses the critical challenge of superalignment, potentially transforming how advanced AI systems are developed and supervised. This approach could democratize access to powerful AI technologies by reducing reliance on scarce, high-quality labeled data and enabling more inclusive participation in AI development. Furthermore, our method encourages the creation of robust AI systems capable of tackling complex problems, which can drive advancements in fields such as healthcare, education, and scientific research. However, careful consideration must be given to ethical implications, ensuring that the deployment of these advanced models aligns with societal values and mitigates risks associated with misuse or unintended consequences.