Bridge the Gap Between CV and NLP! Optimize Adversarial Texts in Continuous Space

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Abstract

Despite recent success on various tasks, deep learning techniques still perform poorly on adversarial examples with small perturbations. While optimization methods for adversarial attacks are well-explored in the field of computer vision, it is impractical to directly apply them in natural language processing due to the discrete nature of the text. To address the problem, we propose a unified framework to extend the existing optimization-based method in the vision domain to craft textual adversarial samples. In this framework, continuously optimized perturbations are added to the embedding layer and amplified in the forward propagation process. Then the final perturbed latent representations are decoded with a masked language model head to obtain potential adversarial samples. In this paper, we instantiate our framework with an attack algorithm named **T**extual **P**rojected **G**radient **D**escent (**T-PGD**). We find our algorithm effective even using proxy gradient information. Therefore, we perform more challenging transfer black-box attacks and conduct comprehensive experiments to evaluate our attack algorithm with BERT, RoBERTa, and ALBERT on three benchmark datasets. Experimental results demonstrate that our method achieves an overall better performance and produces more fluent and grammatical adversarial samples compared to strong baseline methods. All the code and data will be made public.

1 Introduction

Despite great success in real-world applications, deep neural networks (DNNs) are still vulnerable to adversarial samples, which are crafted by adding small and human-imperceptible perturbations to the inputs and can change the prediction label of the victim model (Szegedy et al., 2014; Goodfellow et al., 2015).

In the field of computer vision (CV), numerous adversarial attack methods have been proposed to evaluate the robustness of DNNs (Papernot et al., 2016a; Madry et al., 2019), and corresponding defense methods are also well-explored (Papernot et al., 2016c; Ross and Doshi-Velez, 2018). Adversarial attacks on images are defined as an optimization problem of maximizing the loss function of the model on specific samples, which can be approximated by gradient ascent algorithms.

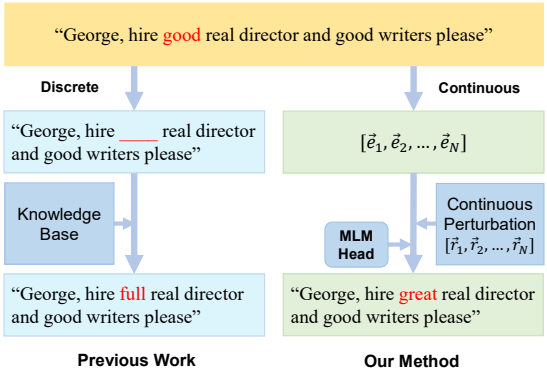

Figure 1: Comparison of our method with previous discrete substitution-based methods.

However, the textual adversarial attack is more challenging due to the discrete and non-differentiable nature of the text space. In Natural Language Processing (NLP), the methods that directly employ the gradients to optimize adversarial samples are not applicable in either the white-box or black-box settings, since they cannot obtain valid discrete texts. For this reason, most works in NLP explore some heuristic methods to produce discrete perturbations, such as manipulating the most important words in the text using corpus knowledge or contextualized information (Ren et al., 2019; Zang et al., 2020; Li et al., 2020). Besides, there are some practices of textual adversarial attacks that employ gradients for first-order approximation to find optimal candidates in vocabulary for word substitution, but the one-off search is less effective and can violate the local linearization assumption (Cheng et al.,

2019; Behjati et al., 2019; Xu and Du, 2020).

To bridge this gap, we propose a general framework to adapt the existing adversarial attack methods optimized in continuous space to NLP (See Figure 1). Essentially, we succeed in obtaining high-quality adversarial samples from the perturbed embedding space. Specifically, we employ a proxy gradient of the loss function to produce perturbations on token embeddings rather than on the original text, thus transforming the problem of searching for adversarial samples in the discrete text space to the continuous and differentiable embedding space. This provides the basis for applying optimization methods investigated in CV to craft textual adversarial samples. In this paper, we adapt the PGD (Madry et al., 2019) algorithm within our framework to perform textual adversarial attacks, denoted as **T-PGD**. Note that T-PGD can be effective with only gradients of a **local proxy model**, leading to a strong transfer attack. To this end, there are two models in the perturbation generation process, one is the local proxy model and the other is the true victim model. Gradient information comes from the local proxy model and only the decision of the victim model can be accessed.

Then the perturbed latent representations should be transferred back to the discrete text. Although there have been some works exploring the feasibility of directly perturbing token embeddings (Sato et al., 2018; Cheng et al., 2019; Behjati et al., 2019), they simply use the first-order approximation of the gradient to select candidate words from vocabulary, which might break the local linearization hypothesis. However, recent work finds that the mask language modeling (MLM) head can reconstruct input sentences from their hidden states with high accuracy, even after models have been fine-tuned on specific tasks (Kao et al., 2021). Inspired by this, we employ an MLM head to decode the perturbed latent representations. With the extensive linguistic knowledge of MLM-head, the coherence and grammaticality of adversarial samples can be guaranteed.

We conduct comprehensive experiments to evaluate the effectiveness of our method by performing transfer black-box adversarial attacks, where only the final decisions of victim models are accessible, against three victim models on three benchmark datasets. Experimental results demonstrate the effectiveness of our framework and T-PGD algorithm, with a higher attack success rate and more fluent and grammatical adversarial examples produced.

To summarize, the main contributions of this paper are as follows: (1) We propose a general textual adversarial attack framework facilitating NLP researchers to produce adversarial texts using optimization-based methods, bridging the gap between CV and NLP in the study of adversarial attacks. (2) Based on the framework, we propose an effective adversarial transfer attack method called T-PGD, handling the challenge of decision-based black-box attack, which is rarely investigated in NLP.

2 Related Work

2.1 Adversarial Attack in CV

In the field of computer vision, adding a small amount of perturbations to input images to mislead the classifier is possible (Szegedy et al., 2014). Based on this observation, various adversarial attack methods have been explored. FGSM (Goodfellow et al., 2015) crafts adversarial samples using the gradient of the model's loss function to the input images. BIM (Kurakin et al., 2017) straightforwardly extends FGSM, iteratively applying adversarial perturbations multiple times with a smaller step size. MIM (Dong et al., 2018) exploits momentum when updating inputs, obtaining adversary samples with superior quality. PGD (Madry et al., 2019) employs uniform random noise as initialization. Both MIM and PGD are variants of BIM.

2.2 Adversarial Attack in NLP

Existing textual attacks can be roughly categorized into white-box and black-box attacks according to the accessibility to the victim models.

White-box attack methods, also known as gradient-based attack methods, assume that the attacker has full knowledge of the victim models, including model structures and all parameters. There are few application scenarios of white-box attacks in real-world situations, so most white-box attack models are explored to reveal the weakness of victim models, including universal adversarial triggers (Wallace et al., 2019), and fast gradient sign inspired methods (Ebrahimi et al., 2018; Papernot et al., 2016b). Although well explored in CV, these methods are not directly transferable to NLP due to the discrete nature of the text. A recent work GBDA (Guo et al., 2021) generates adversarial samples by searching an adversarial distribution, optimizing with a gradient-based algorithm that has

been previously used in image adversarial attacks (Carlini and Wagner, 2017).

Black-box attack models can be further divided into two different attack settings, i.e. score-based and decision-based. The first one assumes the attacker can obtain the decisions and corresponding confidence scores from victim models. Most research works on black-box attacks focus on this setting, exploring different word substitution methods and search algorithms to reduce the victim models' confidence scores. The word substitution methods mainly focus on word embedding similarity (Jin et al., 2020), WordNet synonyms (Ren et al., 2019), HowNet synonyms (Zang et al., 2020), and Masked Language Model (Li et al., 2020). The search algorithms involve greedy search algorithm (Ren et al., 2019; Jin et al., 2020), genetic algorithm (Alzantot et al., 2018), and particle swarm optimization (Zang et al., 2020). The other attack setting assumes the attackers can only obtain decisions from victim models, which is more challenging and less studied. Maheshwary et al. (2021) first substitutes some words in the input sentences to flip the labels and then conducts a search based on a genetic algorithm, expecting to find the most semantic preserved adversarial samples. Chen et al. (2021) propose a learnable attack agent trained by imitation learning to perform a decision-based attack. There also exist some works exploring sentence-level transformation, including syntax (Iyyer et al., 2018) and text style (Qi et al., 2021), to launch attack.

3 Framework

In this section, we first present an overview of our framework, and next, we will give the details of how to add continuous perturbations and reconstruct the text.

3.1 Overview

We have two models in the perturbation generation process: (1) a local proxy model which provides gradient information to optimize the adversarial samples, and (2) the true victim model that the attacker attempts to deceive. Specifically, a proxy BERT model fine-tuned on the attacker's local dataset encodes each discrete text instance into continuous token embeddings and then adds continuous perturbation to it. The perturbation would be iteratively optimized using the gradient of the proxy model, according to the prediction output of the victim model. After perturbation, an MLM head will decode the perturbed latent representation to generate candidate adversarial samples. The overview of the framework is shown in Figure 2.

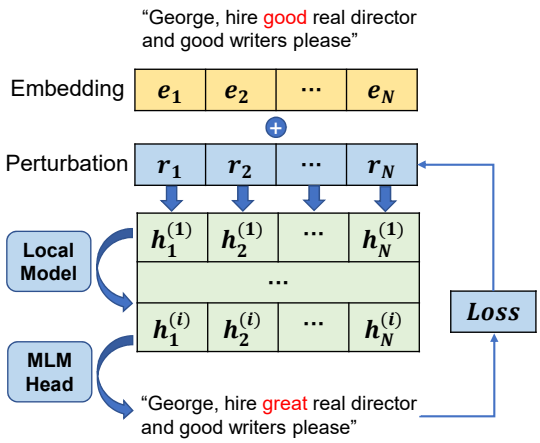

Figure 2: Overview of our framework. Continuous perturbations (r_i) are calculated as gradients of the loss function with respect to token embeddings. The MLM head is employed to decode the perturbed hidden states to obtain potential adversarial samples.

With the help of our proposed framework, it is feasible to perform a textual adversarial attack with various gradient-based methods in CV. In this paper, we examine PGD (Madry et al., 2019) as a case (See Section 4).

3.2 Latent-space Perturbation

Previous work has shown that the latent representations of transformer-based pre-trained language models are effective in providing semantic and syntactic features (Clark et al., 2019; Jawahar et al., 2019), and thus we use a local BERT model fine-tuned on our local dataset as the encoder for our framework.

For each text input, we first calculate the task-specific loss in the forward propagation process, and then perform backward propagation to obtain the gradients of the loss with respect to the token embeddings of the input text. The generated gradients are viewed as the information for updating the perturbations added to the token embeddings, which can be obtained by solving an optimization problem as follows:

$$\delta = \underset{\delta:\|\delta\|_2 \leq \varepsilon}{\arg\max}\, \mathcal{L}\left(E + \delta, y; \theta\right), \qquad (1)$$

where δ is the perturbation, E stands for the embeddings of input tokens, y is the golden label, θ

denotes current parameters of our local model, and $\mathcal{L}(\cdot)$ is the loss function.

The closed-form solution to the optimization problem is hard to directly obtain (Goodfellow et al., 2015), which is thus relaxed to obtain an approximate solution. For example, various methods in CV usually linearize the loss function with gradient information to approximate the perturbations δ (Goodfellow et al., 2015; Kurakin et al., 2017; Madry et al., 2019).

In NLP, most existing gradient-based methods commonly employ first-order approximation to obtain substitution words (Cheng et al., 2019; Behjati et al., 2019; Xu and Du, 2020). However, these one-off approaches may result in large step size perturbations, violating the hypothesis of local linearization (See Figure 3). To ensure the local linearization hypothesis, we consider adjusting the continuous perturbations added to the token embeddings with a minor change at each step, and then iteratively update the token embeddings of the input instance with the perturbations until generating a meaningful adversarial sample for attacking.

3.3 Reconstruction

By means of continuous perturbations, we need to reconstruct the meaningful adversarial text from the optimized token embeddings. The MLM-head is observed to be able to reconstruct input sentences from hidden states in middle layers with high accuracy, even after models have been fine-tuned on specific tasks (Kao et al., 2021). Inspired by this, we adopt the MLM head as the decoder for: 1) MLM-head is capable of interpreting any representation embeddings in the hidden space, which is crucial to search adversarial examples continuously; 2) MLM-head has been fully trained during the pre-trained stage so it acquires linguistic knowledge together with the language model and can reconstruct sentences considering the contextual information.

Without loss of generality, we take an example in Figure 3 to illustrate the discrepancy between the one-off-based attack models and our proposed iterative-attack-based model. One-off attack models are prone to choose the token b to serve as the substitute of token a because $\cos(\overrightarrow{at_1}, \overrightarrow{ab}) < \cos(\overrightarrow{at_1}, \overrightarrow{ac})$. However, in our framework, the one-step perturbation $\overrightarrow{at_1}$ does not cross the decoding boundary, and thus the decoding results remain unchanged if only using one-step perturbation. Based on the iterative search, the perturbations can be

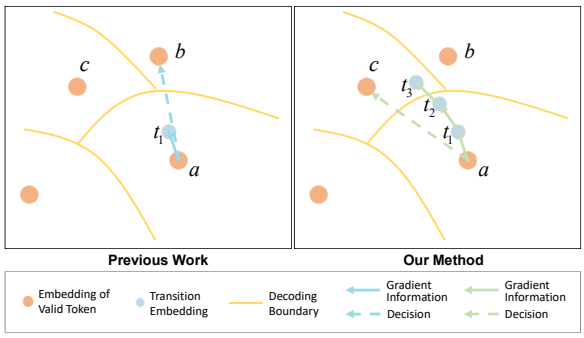

Figure 3: The process of searching for the substitute token of the original instance a in the hidden space. In this case, the one-off attack models are prone to select token b after one-step perturbation (left), while our iterative perturbation-based method is more likely to find the optimal solution token c (right).

accumulated to the extent to cross the decision boundary and reach the transition point t_3, which will be decoded as the optimal solution c. Then a is replaced by c to obtain the adversarial sample to query the victim model for its decision. If this adversarial sample fails to fool the victim model, we start the next searching iteration from the current perturbed token embedding, i.e. t_3 in Figure 3, but not from the embedding of the decoded token c. By exploiting virtual embeddings as transition points, this iterative attack framework can preserve accumulated gradient information and avoid breaking local linearization assumptions.

4 Method

We denote each sample as $(x \in \mathcal{X}, y \in \mathcal{Y})$, where x denotes the input text, y denotes its corresponding label. In particular, the hidden state of x is regarded as $\vec{h}$ and the neural network is implied by a mapping function f, which consists of three components, i.e., f_0, f_1 and f_2, holding:

$$f(x) = f_2(f_1(f_0(x))), \tag{2}$$

where f_0 is the embedding layer, f_1 denotes the hidden layers that map embeddings to hidden states of a certain layer, and f_2 denotes the rest of the neural network. Then the forward propagation process can be described as:

$$e = f_0(x), h = f_1(e), y = f_2(h) \tag{3}$$

4.1 T-PGD Algorithm

We instantiate our framework with PGD (Madry et al., 2019) algorithm, and name our attack model

as **T**extual-**PGD** (**T-PGD**). The algorithm flow of T-PGD is shown in Appendix A. To solve the optimization problem in Eq. (1), we iteratively search for the optimal solution by adding the gradient-based perturbations to the token embeddings with the following formula:

$$\begin{aligned} g_{adv} &= \nabla_{\delta} \mathcal{L}\left(E, y; \theta\right) \\ \delta_{i+1} &= Proj\left(\delta_i + \alpha g_{adv} / \|g_{adv}\|_F\right), \end{aligned} \tag{4}$$

where g_{adv} is the gradient of the loss with respect to the continuous perturbation δ, α is the step size of δ, and i denotes the current iteration step. $Proj\left(\cdot\right)$ performs a re-initialization when δ reaches beyond the ϵ-neighborhood of the original embedding. For each sample, we first map it to the token embeddings, where continuous perturbations can be added to. After obtaining the gradient of the loss function with respect to the token embeddings in (i+1)-th iteration, perturbations δ_{i+1} are generated according to Eq. (4) and then added to the token embeddings. Then the perturbations are amplified through the forward propagation process (Goodfellow et al., 2015). Next, the hidden states with perturbations are decoded for reconstructing the crafted adversarial samples:

$$adv_{i+1} = Dec(h_{i+1}), \tag{5}$$

where adv_{i+1} denotes the adversarial sample obtained in the $i+1$ iteration. We query the victim model only when adv_{i+1} satisfying: (1) it varies from adv_0 to adv_i; (2) it is more similar to the original sentences, compared to previous potential adversarial samples. Here we employ the Universal Sentence Encoder (*USE*) score (Cer et al., 2018), a metric for semantic similarity, to measure the similarity between sentences. If attack succeeds and *USE*$(adv_{i+1}, x) > T$, where T is a tunable threshold for *USE* score, then adv_{i+1} is considered as the adversarial sample of the original input. For each sample, the maximum iteration of the searching process is pre-defined to avoid the infinite loop problem.

4.2 Heuristic Strategies

Random Masking for Diversity. To enhance the diversity of adversarial samples, we randomly mask one token in each input sentence to randomly initialize the search for a broader search scope. Specifically, we tokenize x to a list of tokens, $x_{token} = [x_0, ..., x_i, ..., x_n]$. Then we randomly select i-th index token using the uniform distribution and replace it with a special token *[MASK]*. Next, the MLM-head-based decoder will predict the masked word according to its context, which will diversify the generated adversarial samples with semantically consistent consideration. Then, these processed sentences are embedded into continuous token embeddings as mentioned.

Input Reconstruction Task. Intuitively, the quality of generated adversarial samples is largely affected by the reconstruction accuracy of the MLM-head-based decoder. If failing to recover the original sentence even though no perturbations are added, its capacity to generate fluent adversarial samples from perturbed hidden states is limited. To reduce the risk of a catastrophic drop in the quality of adversarial samples generated by continuous perturbation, external constraints on the MLM-head-based decoder should be considered to ensure reconstruction accuracy. Note that the MLM head has been pre-trained to precisely fill the masked word, which is also fitted to our task. We add an additional loss term to force the added perturbations to minimize the loss of input reconstruction task, which will be optimized simultaneously with the adversarial loss so that the adversarial samples can fool the models with minimal perturbations. Specifically, the loss function is defined with two components:

$$\mathcal{L}\left(E, y; \theta\right) = \mathcal{L}_1\left(E, y; \theta\right) + \beta \mathcal{L}_2\left(E, y; \theta\right), \tag{6}$$

where $\mathcal{L}_1\left(E, y; \theta\right)$ is the original loss of the local model on specific tasks (e.g. CE loss in sentiment classification), $\mathcal{L}_2\left(E, y; \theta\right)$ is the cross-entropy loss of the input reconstruction task, and β is a weighting constant. Note that we aim to reduce the reconstruction loss $\mathcal{L}_2$ while increasing $\mathcal{L}\left(E, y; \theta\right)$ along the gradient direction, so β should be negative. Taking two losses into account jointly, we adjust the perturbation searching target to successfully fool the victim models with fewer modifications.

Antonym Filtering. Li et al. (2019) reports that semantically opposite words locate closely in their representation embeddings since antonyms usually appear in similar contexts. Therefore, we filter antonyms of original words using WordNet (Fellbaum, 2010) to prevent invalid adversarial samples.

Dataset	#Class	Train	Test	Avg Len	BERT Acc	RoBERTa Acc	ALBERT Acc
SST-2	2	7K	1.8K	16.5	89.9	94.2	92.8
MNLI	3	433K	10K	31.7	82.8	83.6	82.3
AG's News	4	30K	1.9K	39.3	91.2	94.7	94.2

Table 1: Detailed information of datasets and original accuracy of victim models.

Dataset	Model	BERT				RoBERTa				ALBERT			
		ASR%	USE	ΔI	ΔPPL	ASR%	USE	ΔI	ΔPPL	ASR%	USE	ΔI	ΔPPL
SST-2	PWWS	75.12	0.83	0.29	533.86	77.03	0.82	0.41	837.7	72.00	0.82	0.40	531.85
	Textfooler	85.36	0.81	0.33	480.14	87.28	0.82	0.32	924.09	72.68	0.79	0.25	706.83
	PSO	85.60	0.75	**0.10**	501.12	85.50	0.74	**0.09**	479.27	91.49	0.77	**0.14**	397.77
	BERT-Attack	90.36	0.81	0.51	378.79	93.53	0.88	0.45	387.95	92.43	0.79	0.81	348.37
	GBDA	57.19	0.64	0.42	**186.21**	58.05	0.64	0.22	**27.45**	54.31	0.64	0.47	**153.94**
	TPGD	**97.00**	**0.92**	0.62	343.65	**94.75**	0.89	0.63	302.70	**93.59**	**0.90**	0.69	291.00
MNLI	PWWS	75.12	0.83	0.34	516.95	71.65	0.84	0.3	715.42	45.88	0.77	4.17	744.49
	Textfooler	72.34	0.83	0.31	780.8	77.27	0.87	0.3	640.21	82.47	0.81	0.31	854.73
	PSO	75.85	0.8	0.11	481.43	76.08	0.80	0.11	411.12	89.41	0.79	0.22	424.48
	BERT-Attack	87.68	0.87	0.55	484.27	91.26	0.89	0.23	604.22	89.65	0.89	0.25	456.31
	GBDA	61.28	0.67	0.08	**265.38**	59.31	0.67	0.12	316.18	62.65	0.67	0.10	288.37
	TPGD	**93.96**	**0.92**	**-0.95**	296.82	**94.55**	**0.91**	**-0.97**	**261.62**	**94.65**	**0.93**	**-0.98**	**259.57**
AG's News	PWWS	65.46	0.84	0.65	394.28	54.70	0.84	0.82	491.48	48.53	0.84	4.71	476.81
	Textfooler	88.71	0.81	0.61	454.13	78.25	0.82	0.59	372.9	73.21	0.84	1.32	367.66
	PSO	66.22	0.79	0.25	539.25	64.63	0.79	0.29	508.76	76.37	0.84	0.15	282.73
	BERT-Attack	81.25	0.84	0.48	431.47	82.58	0.85	0.07	307.74	91.28	0.81	2.52	289.52
	GBDA	77.66	0.69	-0.16	**85.69**	68.97	0.69	-0.59	**96.95**	66.67	0.73	0.20	**54.91**
	TPGD	**94.47**	0.75	**-0.05**	625.08	**99.30**	**0.87**	**-1.42**	285.12	**99.24**	**0.87**	**-1.14**	260.64

Table 2: The results of automatic evaluation metrics on SST-2, MNLI, and AG's News. ASR denotes the attack success rate, *USE* denotes the similarity of original and adversarial samples, ΔI and ΔPPL denotes the increase of grammar errors and perplexity after original texts are transformed into adversaries. We conduct Student t-tests to measure the significant difference. **Bold** numbers indicate significant advantage with p-value 0.05 as the threshold and underline numbers mean no significant difference.

5 Experiments

We conduct comprehensive experiments to evaluate our general framework and T-PGD algorithm on the task of sentiment analysis, natural language inference, and news classification. We consider both automatic and human evaluations to analyze our method in terms of attack performance, semantic consistency, and grammaticality.

5.1 Datasets and Victim Models

For sentiment analysis, we choose SST-2 (Socher et al., 2013), a binary sentiment classification benchmark dataset. For natural language inference, we choose the mismatched MNLI (Williams et al., 2018) dataset. For news classification, we choose AG's News (Zhang et al., 2015) multi-classification datasets with four categories: World, Sports, Business, and Science/Technology. We randomly sample 1,000 samples that models can classify correctly from the test set and perform adversarial attacks on those samples.

For each dataset, we evaluate T-PGD by attacking BERT (Devlin et al., 2019), RoBERTa (Liu et al., 2019), and ALBERT (Lan et al., 2020) with a local fine-tuned BERT model to generate potential adversarial samples. Details of datasets and the original accuracy of victim models are listed in Table 1.

5.2 Experimental Setting

Baseline Methods. We select four strong score-based attacks as baselines: (1) PWWS (Ren et al., 2019); (2) Textfooler (Jin et al., 2020); (3) PSO (Zang et al., 2020); (4) BERT-Attack (Li et al., 2020). Note that all of them require the confidence scores of victim models, while our model only assumes the decisions are available, which is more challenging. We also make a comparison with the decision-based GBDA (Guo et al., 2021).

Evaluation Metrics. We evaluate our method considering the attack success rate and adversarial sample quality. (1) Attack Success Rate (**ASR**) is the proportion of adversarial samples that successfully mislead victim models' predictions. (2) Quality of adversarial samples is evaluated by two automatic metrics and human evaluation, including their semantic consistency, grammaticality, and fluency. Specifically, we use Universal Sentence Encoder (Cer et al., 2018) to compute the semantic similarity between the original text and the corre-

sponding adversarial sample, Language-Tool[1] to calculate the increase of grammar errors in texts after being perturbed, and GPT-2 (Radford et al., 2019) to compute the increase of perplexity to measure fluency. We also conduct a human evaluation to measure the validity and quality of adversarial samples.

5.3 Experimental Results

The results of automatic evaluation metrics are listed in Table 2.

Attack Performance. T-PGD consistently outperforms the strong score-based attack methods considering the attack success rate. We attribute the success of our attack method to the more effective searching process following the guidance of the gradient information, which is verified in the ablation study (Section 6).

Adversarial Sample Quality. We observe that the quality of the adversarial samples generated by T-PGD increases with the text length. Our adversarial samples yield overall higher *USE* scores than baseline models, indicating that our method can manipulate adversarial samples more precisely with explicit gradient information. And although the grammatical performance of T-PGD is not the best on SST-2, which mostly contains shorter text (See Table 1), MNLI and AG's News T-PGD produce the fewest grammatical errors and the lowest perplexity, since the embedding space of longer text is broader and has a better optimal solution. Finally, we attribute the overall high quality of our adversarial samples to the introduction of reconstruction loss, which is demonstrated in Section 6.

5.4 Human Evaluations

To further study the quality and validity of adversarial samples, we randomly selected 100 original SST-2 sentences and 100 adversarial samples from the SOTA baseline BERT-Attack and T-PGD respectively for human evaluation. Following (Li et al., 2020), we shuffle the 300 samples and ask 3 independent human judges to evaluate the quality (300 samples per person). For semantic consistency evaluation, we ask humans to predict the labels of mixed texts. For grammar and fluency, human judges score from 1 to 5 on the above examples. All annotators have no knowledge about the source of the text, and all their evaluation results are averaged (shown in Table 3).

[1] https://github.com/jxmorris12/language_tool_python

Source	Accuracy	Grammar & Fluency
Original	0.92	4.63
BERT-Attack	0.48	3.41
T-PGD	0.68	3.52

Table 3: Human evaluation on SST-2 in terms of prediction accuracy, grammar correctness, and fluency.

Semantic Consistency. Since human judges have high accuracy on the original text, the prediction results on texts can be regarded as ground truth labels. Therefore, human accuracy can be a criterion for semantic consistency between original sentences and adversarial ones. From the results, human judges achieve 0.68 accuracies on adversarial samples crafted by T-PGD, significantly higher than the baseline method. This result verifies that the adversarial samples crafted by T-PGD have a better semantic consistency.

Grammar and Fluency. We can also conclude from Table 3 that adversarial samples crafted by T-PGD have better quality compared to the baseline method considering the grammar and fluency, evaluated by human annotators. However, both BERT-Attack and T-PGD suffer a decline in grammatical correctness and fluency of adversarial text, leaving room for improvement in future research.

6 Further Analysis

Importance of Gradient Information. T-PGD employs the gradient of the proxy local BERT model to approximate the perturbations. To verify the effectiveness of the gradient information, we conduct an ablation experiment on SST-2 by adding only random perturbations in the embedding space without exploiting the gradient information. In detail, we generate a Gaussian noise with the same mean and variance as our gradient-based perturbations. The results in Table 4 shows that without exploiting the direction of the gradient, the search in embedding space may deviate from the vicinity where the optimal and original points are located, reflected by the low ASR and USE score respectively.

Importance of Reconstruction Task. We show the importance of adding a reconstruction loss ($\mathcal{L}_2$ in Eq.(6)) for generating more accurate reconstructions. We conduct an ablation study on SST-2. The results are shown in Table 5. On all three victim

Model	T-PGD		Random	
	ASR	*USE*	ASR	*USE*
BERT	97.00	0.92	47.48	0.79
RoBERTa	94.75	0.89	56.59	0.79
ALBERT	93.59	0.90	51.36	0.79

Table 4: Ablation results of gradient information on SST-2. *Random* corresponds to adding random perturbations to the embeddings.

Victim	T-PGD				β=0			
	ASR	USE	ΔI	PPL	ASR	USE	ΔI	PPL
BERT	97.00	0.92	0.62	343.65	100	0.79	1.45	875.64
RoBERTa	94.75	0.89	0.63	302.70	100	0.84	1.36	466.56
ALBERT	93.59	0.90	0.69	291.00	100	0.83	1.50	693.39

Table 5: Ablation results on the reconstruction loss. *β=0* denotes the setting without the reconstruction loss.

models, the attack performances (ASR) improve significantly (up to 100) while the quality of adversarial samples deteriorates, with *USE* score decreasing and grammar errors and perplexity increasing. This validates our claim that without reconstruction loss, the adversarial samples attempt to change the predictions of the model, ignoring whether the semantics is preserved and the linguistic quality is guaranteed. We further tune β to study the trend of ASR and *USE* score. Results on BERT are shown in Figure 4. We observe that as the absolute value of β increases, at the early stage ASR declines while *USE* increases, suggesting that at first the effectiveness is sacrificed for sample quality; at the later stage ASR continues to decline and so does the *USE*, showing that the reconstruction loss should not be over-weighted either.

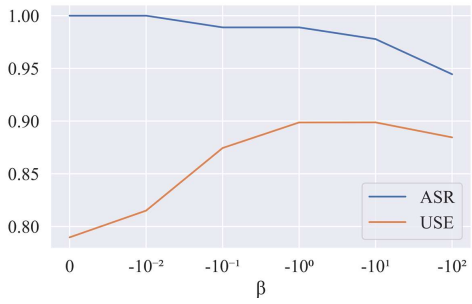

Figure 4: The trend of ASR and *USE* with β changing.

Transferability across models. We investigate the transferability of adversarial examples. We sample 1,000 samples from SST-2 and craft adversarial samples by T-PGD and baseline methods by attacking BERT. Then we test the attack success rate of these adversarial samples on RoBERTa to evaluate the transferability of adversarial samples. As seen in Table 6, adversarial samples crafted by T-PGD achieve the best transferability performance.

Method	PWWS	Textfooler	PSO	BERT-Attack	TPGD
Transfer ASR	28.21	18.00	44.73	11.02	**45.29**

Table 6: The ASR on SST-2 of attacking RoBERTa using adversarial samples crafted on attacking BERT.

Transferability across training datasets. We consider a more practical setting that the attacker does not have the same downstream training dataset as the victim, i.e. the local proxy model is trained on a different dataset from the victim model. To this end, we train a local proxy BERT model on IMDB and attack the victim model on SST-2. We compared the results with attacking with the local proxy model trained on the same dataset as the true victim model in Table 7. We can see that T-PGD can also achieve great attack performance in these practical circumstances, although slightly worse than training on the same dataset.

Victim	BERT-SST-2			
Dataset	ASR	USE	ΔI	ΔPPL
SST-2	97.00	0.92	0.62	343.65
IMDB	93.30	0.90	0.70	204.18

Table 7: Results of attack performance. The local model is fine-tuned on SST-2 and IMDB respectively.

7 Conclusion and Future Work

In this paper, we propose a general framework to facilitate generating discrete adversarial texts using optimization-based methods. In our framework, the problem of searching textual adversarial samples in discrete text space is transformed into the continuous embedding space, where the perturbation can be optimized by gradient information, as explored in CV. The perturbations in embeddings will be amplified in the forward propagation process, then decoded by an MLM head from the latent representations. We instantiate our framework with T-PGD, where the gradient comes from the local proxy model instead of the true victim model, i.e. T-PGD performs a decision-based black-box attack. Experimental results show the superiority of our method in terms of attack performance and adversarial sample quality.

In the future, we will adopt other methods in CV with our framework. Besides, we find that our framework can serve as a general optimization framework for discrete texts, and thus has the potential to provide solutions to other tasks like text generation. We will further explore this direction.

Ethical Consideration

In this section, we discuss the potential broader impact and ethical considerations of our paper.

Intended Use. In this paper, we design a general framework to adapt existing gradient-based methods in CV to NLP, and further, propose a decision-based textual attack method with impressive performance. Our motivations are twofold. First, we attempt to introduce adversarial attack methods of CV to NLP, since image attack methods have been well-explored and proved to be effective, therefore helping these two fields better share research resources hence accelerating the research process on both sides. Second, we hope to find insights into the interpretability and robustness of current black-box DNNs from our study.

Potential Risk. There is a possibility that our attack methods may be used maliciously to launch adversarial attacks against off-the-shelf commercial systems. However, studies on adversarial attacks are still necessary since it is important for the research community to understand these powerful attack models before defending against these attacks.

Energy Saving. We will public the settings of hyper-parameters of our method, to prevent people from conducting unnecessary tuning and help researchers quickly reproduce our results. We will also release the checkpoints including all victim models to avoid repeated energy costs.

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A T-PGD Algorithm

The algorithm flow of T-PGD is shown in Algorithm 1.

A.1 Adversarial Training

We explore to enhance models' robustness against adversarial attacks through adversarial training on SST-2 with BERT. Specifically, we first generate adversarial samples using the original training dataset. Then we fine-tune the BERT model using the training dataset augmented with generated adversarial samples. We evaluate the model's original accuracy on the test set and robustness against different adversarial attack methods. As seen in Table 8, the model shows generally better robustness through adversarial training. Besides, the accuracy on the test set is also improved from 89.90 to 90.48, which is different from previous textual adversarial attacks where accuracy is sacrificed for robustness (Ren et al., 2019; Zang et al., 2020).

Ori Acc	89.90%				
Adv.T Acc	**90.48%**				
Method	PWWS	Textfooler	PSO	BERT-Attack	T-PGD
Ori ASR	69.94	**86.38**	82.03	86.55	92.22
Adv.T ASR	**66.78**	87.41	**73.34**	**84.84**	**83.78**

Table 8: Results of adversarial training. *Adv.T* denotes the adversarial training paradigm.

B Ablation Study of Random Masking

We conduct an ablation study of random masking. Our intuition is that random masking can broaden the searching scope of adversarial examples, and thus lead to diverse adversarial samples and higher attack success rate. To prove this, we attack BERT on SST-2, with and without our random masking strategy. Result are shown in Table 9.

Model	w		w/o	
	ASR	USE	ASR	USE
BERT	97.00	0.92	92.20	0.91

Table 9: Ablation results of random masking on SST-2 against BERT.

C Trade-off between performance and efficiency

Selection of Step Number. Users can make their trade-offs between ASR and efficiency when using our model. The $MaxStep$ in Algorithm 1 determined the perturbation searching scope in embedding space, which contributes to the attack success rate as well as semantic coherence. Intuitively, extending the searching scope boosts performance but costs more time. To determine the proper value range, we conduct experiments to study the statistic of step numbers when obtaining final adversaries.Results on SST-2 with three models are shown in Figure 5. We can observe that most of the attacks finished before step 30. Therefore, $MaxStep = 50$ is virtually enough for an adequate search, and it can also be adjusted to trade-off time costs and attack success rate.

Algorithm 1 T-PGD

Require: Original input x sampled from $\mathcal{X}$

Ensure: Adversary of x

Randomly mask one word in x
$E_0 = f(x)$
$AdvList$=[]
for $j < MaxIter$ **do**
  for $i < MaxStep$ **do**
    $g_{adv} = \nabla_\delta L(E_i, y; \theta_i)$
    $\delta_{i+1} = Proj_{\|\delta\|_F \leq \varepsilon}(\delta_i + \alpha g_{adv} / \|g_{adv}\|_F)$
    $E_{i+1} = E_i + \delta_{i+1}$
    $h_{i+1} = f_1(E_{i+1})$
    $Adv_{i+1} = Dec(h_{i+1})$
    θ_{i+1} = θ_i - $\eta \cdot g_{adv}$
    if Adv_{i+1} **not in** $AdvList$ **then**
      Append Adv_{i+1} to $AdvList$
      Query victim model with Adv_{i+1}
      if attack succeed **and** *USE(Adv, Ori)* > *USE_GATE* **and** no antonyms **then**
        return Adv_{i+1}
      end if
    end if
  end for
  E_0 = $E_0 + \frac{1}{\sqrt{N_{E_0}}} Uniform(-\varepsilon, \varepsilon)$
end for

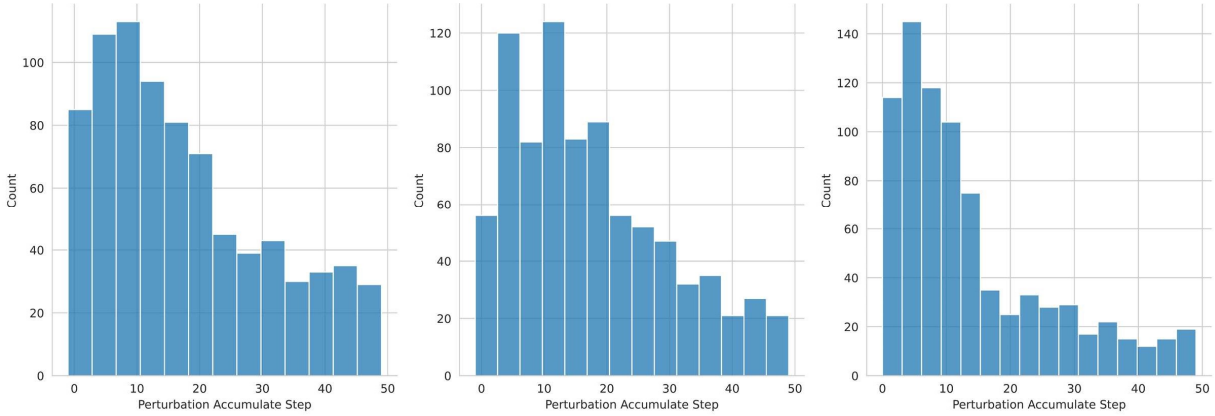

Figure 5: The statistic of perturbation step numbers when successfully obtaining final adversaries. The three pictures represent results on BERT, RoBERTa, and ALBERT in turn.