A Robust Unsupervised Ensemble of Feature-Based Explanations using Restricted Boltzmann Machines

Abstract

Understanding the results of deep neural networks is an essential step towards wider acceptance of deep learning algorithms. Many approaches address the issue of interpreting artificial neural networks, but often provide divergent explanations. Moreover, different hyperparameters of an explanatory method can lead to conflicting interpretations. In this paper, we propose a technique for aggregating the feature attributions of different explanatory algorithms using a Restricted Boltzmann machine (RBM) to achieve a more accurate and robust interpretation of deep neural networks. Several challenging experiments on real-world datasets show that the proposed RBM method outperforms popular feature attribution methods and basic ensemble techniques.

1 Introduction

As the applications of deep neural networks (DNNs) continue to grow, the black-box nature of DNNs creates potential trust issues [1]. Moreover, numerous life-critical (such as medical, automotive, or financial) applications utilize DNNs for various estimation tasks. In such applications, and especially for the long-term acceptance of Artificial Intelligence (AI) solutions, a deeper understanding and trust in the produced results is crucial.

Explaining how the input influences the output for a given DNN is one form to interpret the black-box nature of the DNN and bring trust to a system. These so-called feature-based explanation methods received a lot of attention in recent years [1, 2, 3, 4]. They can be grouped into three broad categories, (1) approaches based on gradient information [5, 6], (2) perturbation-based approaches [7, 8], and (3) attribution-based approaches [2, 9]. Interestingly, different feature-based explanation approaches regularly produce mixed views on the main attributes (areas of an image or variables), and in the absence of the ground truth, it is still a challenge to verify which explanation method is the most trustworthy. Moreover, in the AI community, there are no accepted quality measures for feature-based explanations. *All these difficulties resulted in a large number of different explanation methods and in a lack of consensus on which techniques are most accurate.*

Within the machine learning (ML) community, there is much work on the combination of methods that do not always agree with each other, i.e. *ensemble learning* [10, 11]. Normally ensemble models outperform the non-ensemble models and turn out to be more robust to outliers. The main idea is that if multiple methods make mistakes in different areas, combining them in an intelligent way improves performance and reduces the effect of outliers as compared to the single method. Moreover, from statistical learning theory and practical applications, it is well understood that ensemble learning is the path of choice towards a more robust machine learning system [12], even in unsupervised learning scenarios where the target is not available [13, 14].

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In this work, utilizing ideas from [14, 10] and [15, 16], we introduce a novel approach for the unsupervised ensemble learning of accurate and robust feature-based explanations for deep neural networks. To this end, we propose using a Restricted Boltzmann Machine (RBM), which achieves this goal by aggregating the results (saliency maps) of different feature-based explanation methods in a principled probabilistic fashion. Also, it has been shown that an RBM can be used in the truth discovery setting [15, 16], which is analogous to our task of finding a reliable feature importance map from different importance maps.

The main contributions of this work are:

- We introduce a novel method for a robust and accurate feature-based explanation using ensemble learning.

- We empirically and visually show the superior performance of the proposed method in comparison to state-of-the-art feature attribution baselines.

- We open-source our code and make it publicly available (https://anonymous.4open.science/r/AggregationOfLocalExplanations-80D7/example.ipynb).

The paper is organized as follows: In Section 2 we discuss the related work and provide essential background information. Section 3 presents the proposed ensemble method for local feature-Based explanations using a restricted Boltzmann machine. In the following Section 4, we present the results of various challenging experiments. Section 5 discuss the limitation of our work and ways how to address in the future. Section 6 concludes our work with a short summary.

2 Background and Related Work

This part of the manuscript provides the background and related work. First, we present the basic notation used in this work and proceed by presenting two ensemble techniques for aggregating feature importance maps.

2.1 Feature Attribution Function

Formally, a feature attribution function can be seen as $\phi(f, \mathbf{x}, c_x)$, where f is a black box model and $\mathbf{x}$ is an input data point from a corresponding class c_x. The output of ϕ is an explanation vector or matrix $\mathbf{e}_{f(\mathbf{x})}$. Where each element of $\mathbf{e}_{f(\mathbf{x})}$ is an importance score for the corresponding feature value in $\mathbf{x}$. A large positive or negative value in $\mathbf{e}_{f(\mathbf{x})}$ indicates that the corresponding feature (pixel) has a large influence on the outcome of the black-box model f.

Assumption 2.1 In the following, we assume that a true feature attribution $\bar{\mathbf{e}}_f(\mathbf{x})$ for a given model f and input $\mathbf{x}$ exists and can be constructed by adequately aggregating available attributions $\mathbf{e}_{f(\mathbf{x}),i}, i \in \{1, ..., N\}$. For better readability and simplicity, from here we omit the index $f(\mathbf{x})$.

The goal of any explanation method ϕ is to obtain an attribution $\mathbf{e}$ that is as close as possible to $\bar{\mathbf{e}}$. Given this assumption, we can say that there is a joint probability distribution of the pair $(\mathbf{e}, \bar{\mathbf{e}})$ parametrized by θ.

$$p_\theta(\mathbf{e}, \bar{\mathbf{e}}) = p_\theta(\bar{\mathbf{e}})p_\theta(\mathbf{e}|\bar{\mathbf{e}}).$$

The joint distribution $p_\theta(\mathbf{e}, \bar{\mathbf{e}})$ is not known, and neither are the marginals $p_\theta(\mathbf{e})$, $p_\theta(\bar{\mathbf{e}})$.

For the following theoretical results we require that the explanation methods give independent explanations when conditioned on the true explanation. However, for our practical implementation, it does not matter whether this assumption is violated [14].

$$p_\theta(\mathbf{e}|\bar{\mathbf{e}}) = \prod_n^N p_\theta(\mathbf{e}_n|\bar{\mathbf{e}}),$$

where $\mathbf{e}_n$ is a base learner (sometimes a weak learner) in the ensemble involves N different learners.

2.2 Ensemble Learning

As we state in the introduction, ensemble learning is a well studied approach for improving the performance of an ML system. One of the most basic ensemble methods employs the mean of results of base learners [12], where a base learner is a single algorithm from the ensemble.

$$\mathbf{e}_{mean} = \frac{1}{N} \sum_{n=1}^{N} \mathbf{e}_n. \tag{1}$$

A significant drawback of the *mean ensemble approach* is that it still is sensitive to outliers or noisy estimations. Furthermore, data scaling may strongly influence the aggregation. In Section 4, these weaknesses of the *mean ensemble approach* are also seen in the experimental evaluation.

To mitigate these weaknesses, the authors of [17] propose to take the local uncertainty into account. To this end they divide the mean by the local variance plus a constant ϵ for stability reasons, which results in the *variance ensemble approach*:

$$\mathbf{e}_{var} = \frac{1}{N} \sum_{n=1}^{N} \frac{\mathbf{e}_n}{\sigma_*(\mathbf{e}_{i \in \{1,...,N\}}) + \epsilon},$$

where $\sigma_*(\mathbf{e}_{i \in \{1,...,N\}})$ is the point-wise standard deviation over all the available explanations $\mathbf{e}_i, i \in \{1, ..., N\}$. This method assigns less relevance to explanations that have high disagreement with the remaining explanations.

3 Ensemble Learning using Restricted Boltzmann Machines

In this section, we present an unsupervised aggregation of feature attribution maps using a Restricted Boltzmann Machine (RBM). Similar aggregation techniques have been proposed in other contexts, e.g., in [14, 15].

3.1 The Restricted Boltzmann Machine

An RBM is an undirected bipartite graph that can be parametrized by a neural network. It is a variant of the Boltzmann Machine, with the additional property that there are no connections within both the group of visible nodes or the group of hidden nodes. The advantage of this property is that nodes in one group are conditionally independent of each other, given that we know the state of the nodes in the other group. One of the main characteristics of an RBM is that it can learn a probability distribution over its set of inputs. A graphical representation of an example RBM is shown in Figure 1.

The formal definition of an RBM is as follows. There is a set X of n visible binary random variables and a set H of m hidden binary random variables. The RBM has parameters $\lambda = (W, a, b)$. W is the weight matrix of the connections between the nodes, a is the bias of the visible layer and b is the bias of the hidden layer. Each possible state of the RBM, i.e. the particular values of (X, H), is associated with the following energy function (in matrix notation):

Figure 1: An RBM with three visible and two hidden units. In our work, we use an RBM with a single hidden node.

$$E_\lambda(x, h) = -(a^T x + b^T h + x^T W h),$$

which then can also be used to define the joint probability distribution for the visible and hidden vectors is defined in terms of the energy function:

$$P_\lambda(x, h) = \frac{1}{Z} e^{-E(x,h)},$$

Figure 2: An overview on the ensemble of feature attribution maps from four different local explanation algorithms using an RBM for an image from the MNIST dataset [20].

112 where Z is the sum over $e^{-E(x,h)}$ for all possible configurations x, h, which can be seen as a
113 normalization constant to ensure that all probabilities sum to 1, also known as the partition function.

114 The optimization objective of the RBM is to maximize the expected log probability of a training
115 sample x:

$$\underset{W}{\mathrm{argmax}} \, \mathbb{E}[\log P_\lambda(X = x)] =$$
$$\underset{W}{\mathrm{argmax}} \, \mathbb{E}[\log \sum_h P_\lambda(X = x, H = h)]. \tag{2}$$

116 To train an RBM, a gradient-based optimization can be applied using the contrastive divergence
117 algorithm [18, 19].

3.2 Aggregation of Local Explanations using an RBM

119 Given an RBM with N visible nodes and one hidden node, with input x from a conditional inde-
120 pendent model, where N is the number of base learners in our ensemble, it can be shown that the
121 true posterior probability of y can be efficiently estimated (Lemma 4.1, Lemma 4.2 from [14]). Fur-
122 thermore, given mild assumptions [14], the maximum likelihood estimate $\bar{\lambda}_{MLE}$ for the parameters
123 of the RBM, the RBM posterior probability $P_{\bar{\lambda}_{MLE}}(H = 1|X = x)$ converges to true posterior
124 $P_\theta(Y = 1|X = x)$.

125 Hence, taking into account the assumption we made in Section 2 and [14], we are able to apply
126 the RBM to the unsupervised aggregation of N available feature-based explanations. We assume a
127 joint distribution $p_\theta(\mathbf{e}, \bar{\mathbf{e}})$, and that the $\mathbf{e}_i$'s are conditionally independent from each other given $\bar{\mathbf{e}}$).
128 By fitting the RBM we learn the parameters θ and thus obtain the relationship between our known
129 explanations $\mathbf{e}_i$ and the true explanation $\bar{\mathbf{e}}$. The ensemble pipeline of the proposed method is depicted
130 in Fig. 2.

131 In order to preserve the spatial information for visual data using the RBM-based ensemble, we do
132 a pixel-wise aggregation. Therefore, for each pixel we train a Bernoulli RBM with a single hidden
133 node.

134 A known limitation of an RBM is the so-called *flipping issue* [14, 15, 16], which arises from the
135 parametrization symmetry. That is, the weights of the RBM can be flipped symmetrically without
136 changing the behavior of the RBM. In order to avoid this unwanted effect, we propose two approaches:
137 flip detection and metric optimization. The *flip detection* algorithm extends the idea from Remark 4.3
138 in [14], by comparing the top 5 % of most important and 5 % of less important pixels to the mean
139 baseline. The algorithm inverts the current important scores if there is a strong disagreement between
140 the proposed approach and the mean baseline. The *metric optimization* method utilizes the chosen
141 metric to overcome the flipping issue. It compares two versions of the RBM ensemble results and
142 selects the one with a better performance according to the selected metric.

4 Experiments

To demonstrate the effectiveness of the proposed ensemble algorithm we conduct various visual and quantitative experiments. First, we present the visual inspection results on the MNIST [20] and ImageNet [21] datasets in two settings, with and without noisy explanation maps in our ensemble.

Despite a growing body of research focusing on explainable ML, the fair quantitative comparison of saliency algorithm benchmarks is still an open question, since the existing methods mostly utilize the pixel perturbation strategy (e.g., removing the most or least important pixels and reporting the change in recognition quality) [22, 23]. However, these benchmarks have a significant drawback, replacing image pixels with black or "mean" or any other pixel values may lead to artifacts affecting the data distribution [23]. Nevertheless, since pixel perturbation benchmarks are employed in many related works, for our quantitative analysis we select the following approaches: the pixel perturbation for insertion (IAUC) and deletion (DAUC) and IROF [24] benchmarks on the CIFAR10 dataset [25]. We explain each benchmark method it details in the corresponding subsections.

In our last experiment, we demonstrate that our ensemble approach can be used within a singe feature attribution framework to achieve more robust and stable explanations. Since, it has been shown that hyperparameters choice can significantly affect the saliency maps [26].

4.1 Visual Inspection for Image Data

In our first experiment, a visual evaluation on images from ImageNet [21] and MNIST [20] is performed for several baseline and ensemble methods. We provide benchmark outcomes for two settings, with and without fifteen noisy base learners in an ensemble. The results are depicted in Table 1.

Without artificial noise in the ensemble. We select four samples from ImageNet dataset [21] and five base learners for the ensemble models: LIME [7], Guided Backpropagation (GB) [27], Integrated Gradients (IG) [28], Gradient SHAP (GS) [8], and SmoothGrad (SG) [29]. We compare the proposed RBM ensemble strategy to simple mean and variance ensembles [17]. The results in Table 1 show that our approach produces sharp and visually appealing saliency maps in comparison to other ensemble baselines.

With artificial noise in the ensemble. We challenge the discussed approaches by adding fifteen baselines with random noise sampled from the standard normal distribution $\mathbf{e}_{random} \sim \mathcal{N}(0, 1)$ to the ensemble. The results in Table 1 reveal that the proposed RBM-based aggregation method mitigates noise and hence results in more robust saliency maps in comparison to the other ensemble baselines.

4.2 Pixel Perturbation Experiment

In the first quantitative experiments, we compare multiple baseline models and ensemble methods on the CIFAR10 dataset [25] by removing the most important pixels (according to a scoring function) and reporting the area under a curve score (DAUC). In addition, we also follow the approach of inserting the most important pixels into an empty image and again report the area under a curve (IAUC). Thus, an ideal feature scoring function has a large IAUC and low DAUC. These benchmark methods well accepted by the research community [30]. For this experiment, we select the following algorithms as base learners: Gradient SHAP [8], DeepLIFT [2], LIME [7], Saliency maps [31], SmoothGrad [29], Integrated Gradients [28], Guided Backpropagation [27]. As suggested in [10], we add the original image as a base learner to the ensemble. According to our conducted experiments, an original image to the ensemble does improve the overall ensemble performance. We report all scores for base learners and ensemble methods in Table 2.

4.3 IROF Experiment

In [17] the authors propose the IROF measure as an extension to the work [32]. The main idea of the IROF benchmark is as follows: the image is divided into superpixels using the SLIC algorithm [33]. Superpixels are regional blocks of pixels within an image where the contained pixels share a high similarity measure among each other. The relevancy for each superpixel is calculated by averaging

Original	LIME [7]	GB [27]	IG [28]	GS [8]	SG [29]	Mean ensemble	Variance ensemble	**RBM ensemble**

Without noisy feature attribution maps in the ensemble

With noisy feature attribution maps in the ensemble

Table 1: A visual comparison between base learners and ensemble methods on ImageNet [21] and MNIST [20] datasets.

Method	Insertion (IAUC)	Deletion (DAUC)	IROF
Gradient SHAP [8]	0.61 ± 0.42	0.22 ± 0.29	0.73 ± 0.24
DeepLIFT [2]	0.62 ± 0.42	0.23 ± 0.30	0.73 ± 0.23
LIME [7]	$\mathbf{0.80 \pm 0.31}$	0.23 ± 0.23	$\mathbf{0.76 \pm 0.22}$
Saliency map [31]	0.50 ± 0.35	0.37 ± 0.32	0.65 ± 0.25
SmoothGrad [29]	0.60 ± 0.26	0.38 ± 0.29	0.63 ± 0.26
Integrated Gradients [28]	0.66 ± 0.42	$\mathbf{0.19 \pm 0.27}$	0.75 ± 0.23
Guided Backpropagation [27]	0.54 ± 0.38	0.49 ± 0.36	0.65 ± 0.25
Original Image	0.52 ± 0.32	0.53 ± 0.34	0.47 ± 0.30
Mean Ensemble	$\mathbf{0.79 \pm 0.33}$	0.25 ± 0.28	0.70 ± 0.26
Variance Ensemble [17]	0.62 ± 0.36	0.39 ± 0.31	0.71 ± 0.26
RBM ensemble with the flip detection	0.76 ± 0.38	0.19 ± 0.26	0.76 ± 0.22
RBM ensemble with the metric optimization	0.77 ± 0.37	$\mathbf{0.18 \pm 0.24}$	$\mathbf{0.76 \pm 0.22}$

Table 2: A quantitative compression between single and ensemble methods for the pixel perturbation and IROF experiments on 10000 samples from the CIFAR10 validation dataset [25].

over the attribution scores over all contained pixels (inside the superpixel). After, the superpixels are sorted descending by their relevancy. The entire superpixels are gradually replaced by a baseline and sent through the network again to measure the new recognition quality for the modified image wrt. to the target label. For more accurate attribution methods, the recognition quality decreases faster, and thus the area under the curve is lower. The IROF score is defined as the area over the curve (AOC): $AOC = 1 - AUC$. Higher values are therefore indicating a better attribution. We use the same base learners as in the pixel perturbation experiment (Sec. 4.2). The results are listed in Table 2.

4.4 An RBM Ensemble within a Singe Explanation Framework

In this experiment, we demonstrate that even for multiple base learners of the same type, the unsupervised ensemble with an RBM can be an improvement. To this end, we select the LIME [7] method with a different hyperparameter - the number of superpixels in the image. For base learners (LIME-1, LIME-2, and LIME-3), we used 10, 100, and 1000 superpixels per image, respectively. The results can be seen in 3. The main idea is that each lime method has a different granularity level, thus highlighting distinct detail levels, and the proposed method's aggregation improves the accuracy of feature attributions.

4.5 Reproducibility

For reproducibility reasons, we describe the data pre-processing step used for all the experiments and provide information about packages used in this work. Also, the code for every experiment is publicly available online, the link in Section 1.

To achieve a fair comparison, the image data from all datasets was preprocessed in the same way for each baseline. We do per saliency map normalization before aggregation. In every experiment, we use the ResNet18 neural network architecture [34], except for the experiment on the MNIST dataset where we utilize a simple five layers convolutional neural network. We use a pre-trained model for ImageNet dataset[21] from torchvision library [35].

In experiments we utilize the Bernoulli RBM implementation from the scikit-learn library [36] with following hyperparameters for each experiment: for the MNIST dataset we set the batch size to 5, the learning rate to 0.01, and the number of iterations to 100. For CIFAR10 and ImageNet datasets we use the following hyperparameters: a batch size of 35, a learning rate of 0.001, and a number of iterations is 250. The rest of hyperparameters are default to the scikit-learn package. For all baselines (base learners) we use the publicly available open-source implementations from the captum library [37] with their default hyperparameters.

Figure 3: Distributions of differences where the proposed RBM ensemble shows better (green) and inferior (red) results in comparison to a base learner according to insertion, deletion, and IROF metrics (score 1 means them being equal). The ensemble consists of the feature attributions from the same algorithm - LIME, but different hyperparameters. We sample 2000 random images from CIFAR10 dataset [25] for this experiment.

5 Discussion and Future Work

The results of multiple experiments with the proposed RBM ensemble show its competitive performance compared to base learners and other ensemble techniques. We hypothesize moderate performance of the RBM ensemble on the insertion (IAUC) benchmark is connected to our data preparation step since we filter the negatives values for every saliency map in the ensemble.

The computational complexity of an ensemble method primarily depends on the base learner. In our case, the base learners are relatively fast, especially on desiccated hardware (GPU or TPU), where an RBM has low computational complexity. The saliency map generation is a fast process,

The gradient-based methods frequently produce noisy explanations. We empirically demonstrate that our approach reduces the noisiness in the final ensemble (Tab. 1). Therefore, we believe that the RBM aggregation of multiple saliency maps from gradient-based feature attribution methods will reduce the noisiness, and as a consequence, improve the overall correctness.

For future steps, we would want to make certain that ensemble techniques improve this domain. Besides that, we would like to repeat our experiments with a larger sample size. Future research on base learner selection is needed for a more efficient ensemble is needed. In addition, several other unsupervised ensemble methods can be applied to this problem.

6 Conclusion

In this work, we presented a novel approach to unsupervised aggregation of feature-based explanations using Restricted Boltzmann Machines with the aim of accurately interpreting the influence of inputs on the output of deep neural networks. In addition to explanatory reasons, the latter is also essential for debugging and diagnostic purposes and serves the long-term acceptance of deep learning in real-world applications.

Using the proposed approach, we demonstrate with visual and quantitative experiments its ability to obtain more robust and accurate explanations than other existing ensemble methods. In a setting with noisy attribution maps in an ensemble, the proposed approach successfully selects only the valuable information, mitigating the randomness. Moreover, our work illuminates and mitigates the problem of possible contradictory results that may be obtained by different explanation and evaluation methods. Finally, we show that our approach can also be applied within a single interpretability framework to reduce the sensitivity of a feature-based explanatory approach to its hyperparameters.

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