COLLABORATIVE CONCEPT DRIFT DETECTION

ABSTRACT

This work draws a comparison with XYZ[1]. Rather than triggering drift detection based on similarities between models-to-features and model-to-model relationships, we propose Collaborative Concept Drift Detection (C2D2) in order to utilize diversity within a heterogeneous ensemble to detect invariant patterns that could relate to drift. C2D2 proposes mapping feature and target spaces into a correlation matrix calculated via FCBF. SVD is used to break down its invariant representations and post-hoc tests are applied to test significance and indicate the occurrence of drift.

1 NEW PERSPECTIVE FOR DRIFT DETECTION

In our earlier work (Doe & Doe)[2], we observed that many authors view **concept drift** (Widmer & Kubat (1996); Lu et al. (2019); Huyen (2022)) as an anomaly acting on a single stream (Gama et al. (2004); Blanco et al. (2015); Sethi & Kantardzic (2017); de Barros et al. (2016)). Such works fail to account for the fact that systems in practice support multiple kinds of models that predict more than one stream. Additionally, in such systems, models learn under a shared data pipeline with the possibility of having overlapping data. Although the models themselves operate independently of each other, and they hold information that describes the relationship between their predictors and respective targets, which may improve the understanding of concepts. Under this premise, our framework, XYZ (Doe & Doe), uses a combination of performance-based (Gama et al. (2004)) and data distribution-based drift detectors (dos Reis et al. (2016)) to act as local drift detectors (*i.e., detection per stream*). A global concept drift detector is proposed by using collaborative filtering (Sarwar et al. (2001)) to form similarity scores between models via shapley values (Sundararajan & Najmi (2020)) based on their model-to-feature and model-to-model relationships. The advantage being that a drift detected via a local drift detector can pre-emptively detect or save the expense of running another local drift detector for a model recommended as being similar.

2 COLLABORATIVE CONCEPT DRIFT DETECTION (C2D2)

This work draws a comparison with XYZ. Similarly, our notion is to learn from multiple models in order to capture evolving concepts, but rather than triggering drift detection based on similarities between models-to-features and model-to-model relationships, we propose Collaborative Concept Drift Detection (C2D2) in order to utilize diversity (Brown et al. (2005); Tang et al. (2006); Nascimento et al. (2014)) within an ensemble to detect invariant patterns (des Combes et al. (2020); Stojanov et al. (2021)) that could relate to drift.

2.1 REASONING BEHIND DETECTING INVARIANTS

To fit a model is to take a function f onto a feature vector, x such that it provides a systematic estimate of the target variable, y (James et al. (2021)). ϵ is independent of x and represents random error, a combination of **irreducible error** and **reducible** error (1).

$$y = f(x) + \epsilon \tag{1}$$

We speculate that ϵ of $f(x)$ can serve as a predictor for another model, $f'(x)$. In other words, ϵ is independent of x, but is related to x' or y. The underlying assumption is that as a concept

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[1]XYZ is the authors' previous work and is redacted to respect the blind reviewing
[2]All references under this is a placeholder to respect the blind reviewing

evolves, predictors that turn into confounding variables (i.e. predictors that affect both the target and other predictor(s)) are related to the source of drift. Additionally, there is the assumption that such confounding variables will be invariant across an ensemble of classifiers with heterogeneous training and prediction subspaces and can be used to indicate the occurrence of drift.

Figure 1: Proposed C2D2 framework. Each row x_i dictates a feature space to predict a respective y_j. Solid or dashed lines within the feature space indicate shared predictors while gaps indicate the absence of features. The feature and target spaces are mapped $m : n$ and their correlations are calculated via FCBF. SVD is used to break down its invariant representations and post-hoc tests are applied to test significance and indicate the occurrence of drift.

3 METHODOLOGY

Our work incorporates the methods of domain adaptation (Nguyen et al. (2021); des Combes et al. (2020)) to engender a context of x on $y \in \mathbb{Y}$ and homogeneous ensembles to provide the context of $x \in \mathbb{X}$ on a specific target y. Incorporating both creates heterogeneous ensembling, where models are trained on a mix of $\mathbb{X}$ and $\mathbb{Y}$ subspaces (2.1)

The correlation of every combination of x within $\mathbb{X}$ mapped to every y in $\mathbb{Y}$ is calculated by Fast Correlation Based Filtering (FCBF) (Nguyen et al. (2012)) to form a correlation matrix, A for every data instance. Singular Value Decomposition (SVD) (2) is then used to reduce the matrix to its invariant representation, representing features that may have drifted. At windows of 30 instances, a post-hoc test on S (Demsar (2006)) is to be followed to indicate *if* drift has occurred with U and V indicating *where* it occurred.

$$A = USV^T \tag{2}$$

4 ANALYSIS AND CONCLUSION

Both frameworks rely on overlapping feature spaces and predictors for systems with many models. A limitation of XYZ is that its similarity scores are calculated via shapley values and the complexity explodes in complexity to $O(2^k)$, where k is the entire feature size across all models. Additionally, it has an inherent trade-off between incurring high false alarms and long delays in detection. With C2D2, however, the complexity is $O(mn)$ and its constraint lies in its ability to identify how diverse an ensemble needs to be in order to isolate the invariants to be related only to drift.

C2D2 is arguably orthogonal in reasoning to XYZ. Instead of basing its detection on similarities between the relationship of models and their shared features, it relies on the diversity of models so that performing decomposition transformations could reveal invariant representations of confounding variables related to concept drift. The idea being that if the source of drift is related to predictors evolving into confounding variables, then it should be capturable within the ensemble feature space.

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